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# Binary Search Trees for Sentiment Analysis

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- If you want to follow along and take notes, you can find today's slides at <http://laura-burdick.github.io/BST.pdf>.

By the end of this lesson, you will be able to:

1. Identify characteristics of a binary search tree (BST).
2. Write pseudo-code for searching a BST.
3. Apply BSTs to the problem of sentiment analysis.

(I will assume prior knowledge of recursion, Big-O notation, and the basics of binary trees.)

[illegible]

# Sentiment Analysis

- Deciding if a piece of text conveys positive or negative emotions

A delectable and intriguing thriller filled with surprises, this movie is an original.

A quietly reflective and melancholy New Zealand film about an eventful summer in a 13-year-old girl 's life.

Her film is unrelentingly claustrophobic and unpleasant.

# Sentiment Analysis

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It's a bittersweet and lyrical mix of elements.

Although occasionally static to the point of resembling a stage play, the film delivers a solid mixture of sweetness and laughs.

## Let's Brainstorm!

**Given:** Movie reviews labeled with sentiment (5-point scale, very positive to very negative) – *training data*

**Goal:** Classify the sentiment of new reviews that we haven't seen before

**What are some ideas to approach this problem?**

**(this is brainstorming – call out any idea that comes to mind!)**



## A Simple Approach

- Look at each word that appears in the training data, and calculate its *average sentiment* (the average sentiment of all the sentences that the word appears in).
- Given a new review, take the sentiment of each word in the review (calculated on the training data), and average the sentiment of the words together.

## A Simple Approach

Suffers from the lack of a compelling or comprehensible narrative.

-2      0      0    -2    0   0   1                      0   0                                      1

What do we need to implement this?

- A fast way to search for words and find out their average sentiment
- Enter... binary search trees (BSTs)!



# A Guessing (\*Searching\*) Game

- Find a partner!
- Person 1: Choose a number between 1 and 15.
- Person 2: Guess the number. Your partner will tell you whether you guessed it correctly, were too high, or too low. Repeat until you guess the number correctly.
- Switch roles, and play again.

# A Guessing (\*Searching\*) Game

- Discuss with your partner:
  - **What technique did you use to decide which number to guess next?**
- I'll ask several people to share with the group.

# Sequential Search v. Binary Search

Sequential search

steps: 0



1	3	5	7	11	13	17	19	23	29	31	37	41	43	47	53	59
0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16

# Sequential Search v. Binary Search

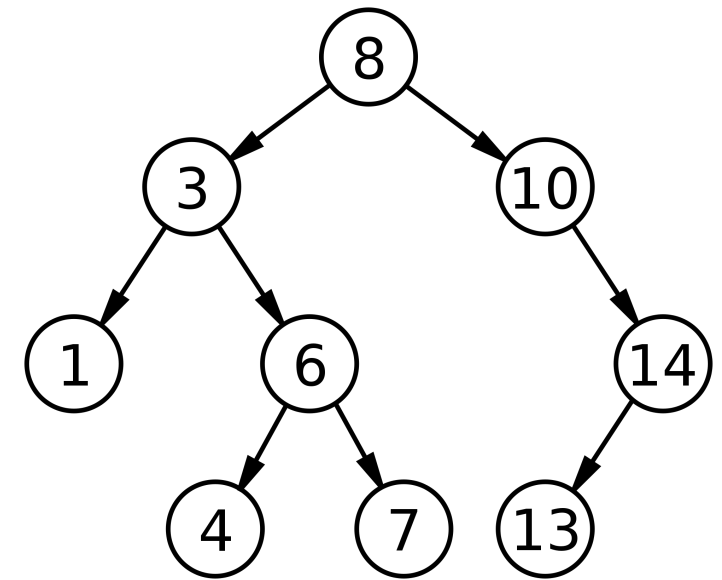
Binary search

steps: 0



# Binary Search Trees (BSTs)

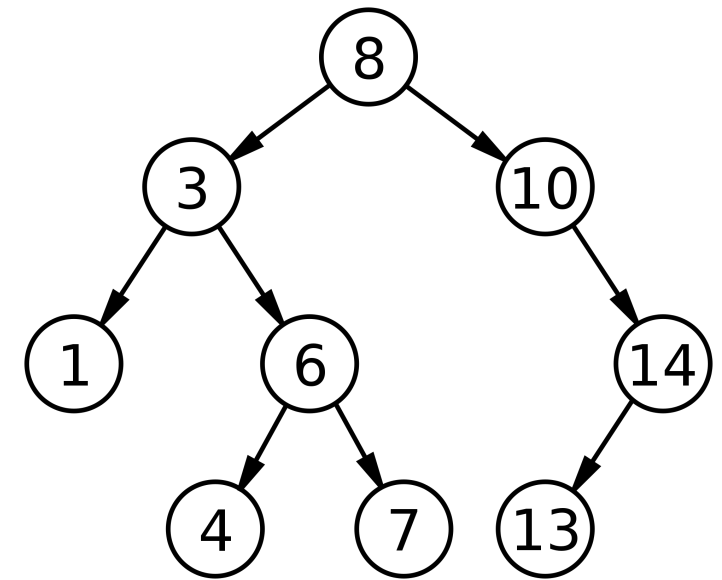
- A **tree** = connected nodes and edges, no cycles, one node designated as the root
- A **binary** tree = each node has at most two children (left child, right child)
- **BST Property** = The left subtree of a node  $x$  only has nodes that are less than or equal to  $x$ . The right subtree of a node  $x$  only has nodes that are greater than or equal to  $x$ .



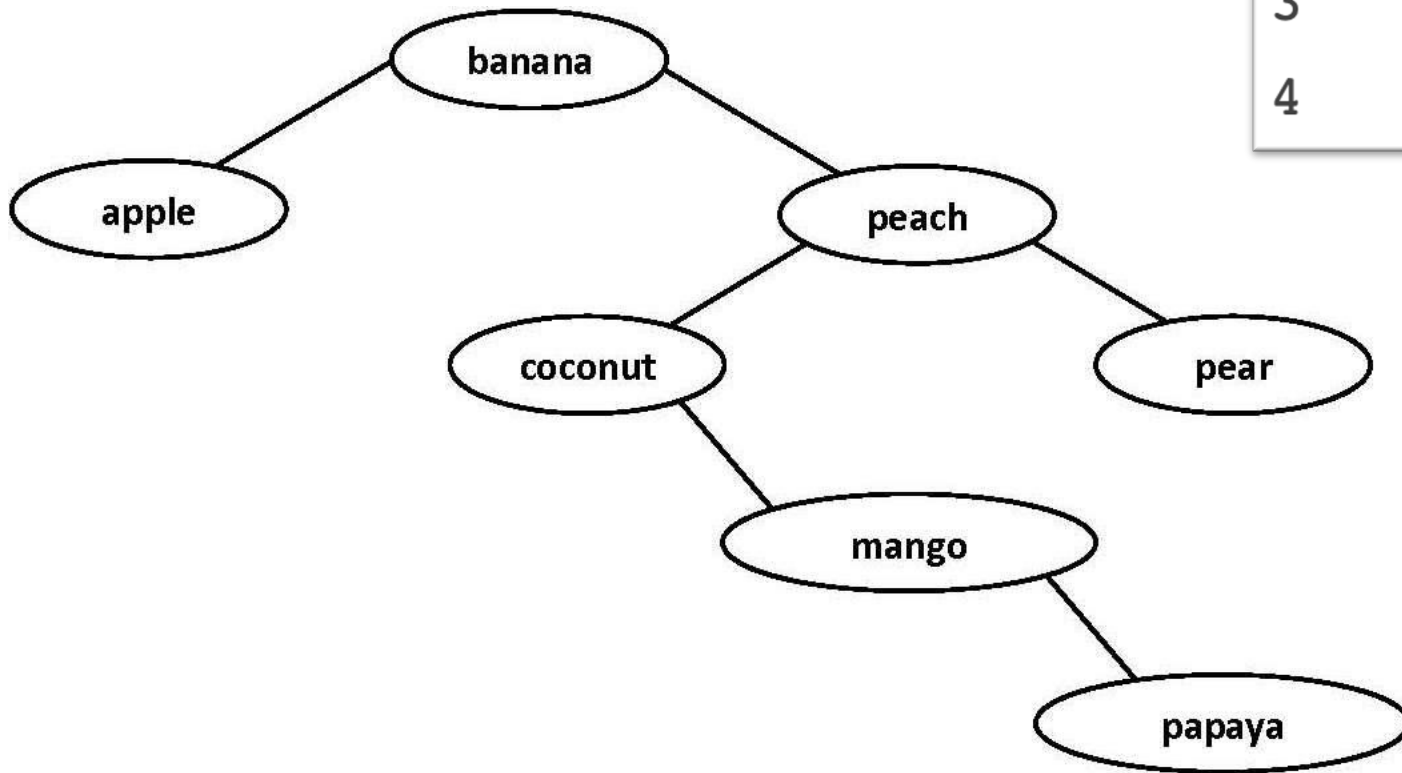
## “Reading” a BST: Inorder Traversal

READ-TREE(*x*)

```
1  if x ≠ NULL
2      then READ-TREE(left[x])
3          print x
4          READ-TREE(right[x])
```



## Let's Practice!



```
READ-TREE(x)
1  if x ≠ NULL
2      then READ-TREE(left[x])
3          print x
4          READ-TREE(right[x])
```

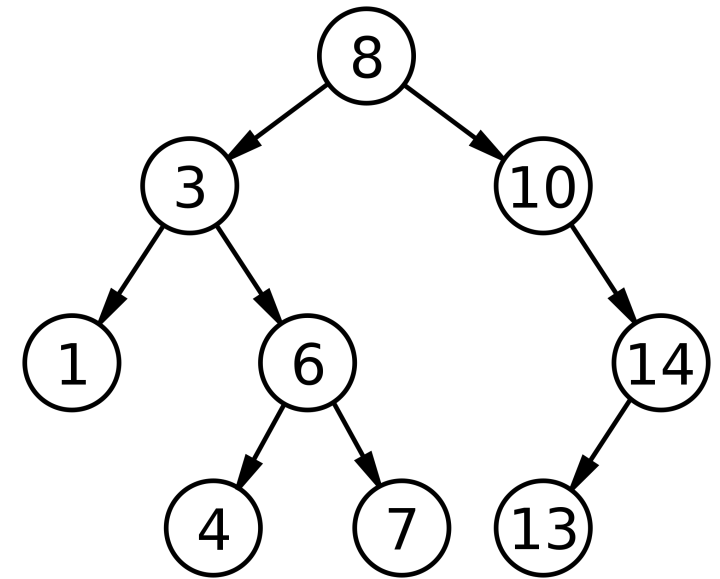


## Searching a BST

- Working individually, write out pseudo-code for the following function:

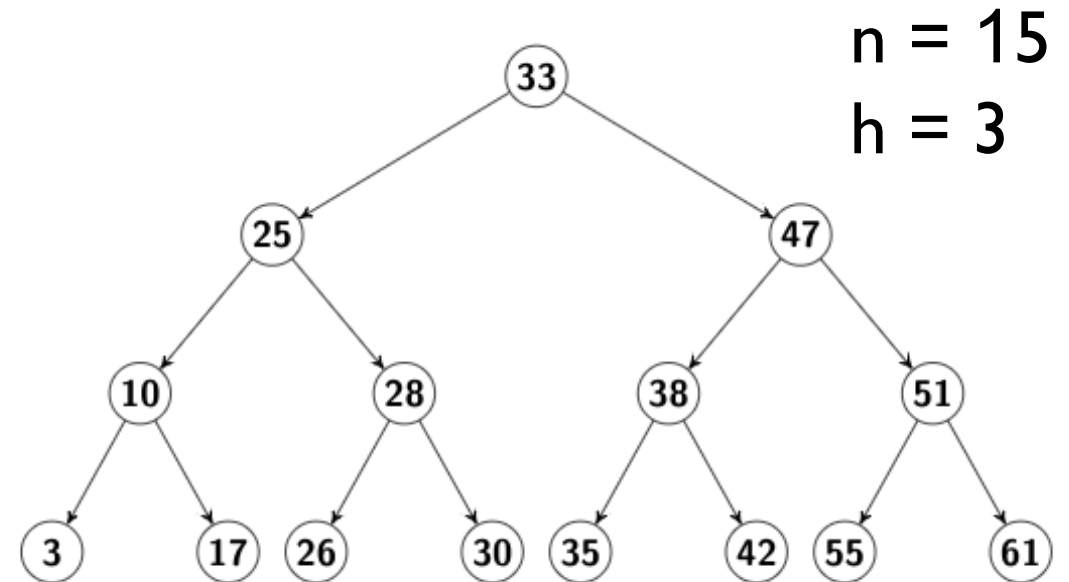
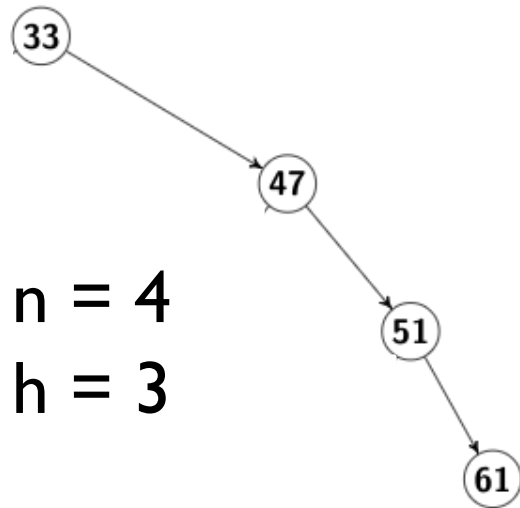
`TREE-SEARCH ( x , v )`

- `x` is the current node you're at (in the beginning, it's the root node)
- `v` is the value you're looking for (e.g., 13)
- *Hint: This will be a recursive function, like the `READ-TREE ( x )` function!*



# How long does it take to find something?

- Searching for an element follows a path downward from the root of the tree. Search is  $O(h)$ , where  $h$  is the height of the tree.
- How tall is a BST?



# How long does it take to find something?

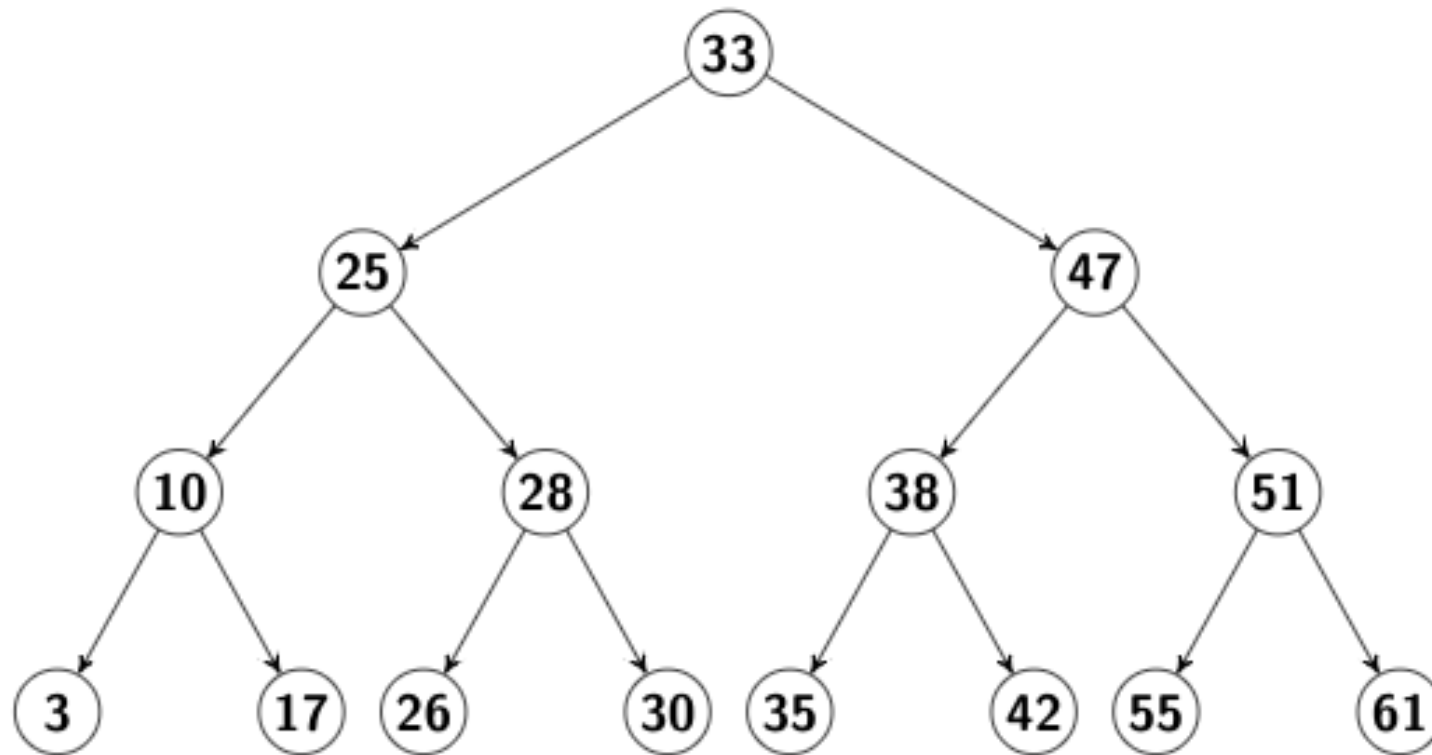
## ■ How tall is a BST?

$$n = 15$$

$$h = \lg(n+1) - 1$$

$$= O(\lg(n))$$

$$= 3$$



1 node

2 nodes

4 nodes

8 nodes

## How long does it take to find something?

- Searching for an element follows a path downward from the root of the tree. Search is  $O(h)$ , where  $h$  is the height of the tree.
- Maximum height of a BST is  $O(n)$ , where  $n$  is the number of data points in the tree.
- Minimum height of a BST is  $O(\lg(n))$ .
- We can show for a randomly built BST, expected height is  $O(\lg(n))$ .

## 1-minute Pause

- Stop and review the material we've covered so far.
- Is there anything that you need clarified?



## Which statement is incorrect?

1. Given a set of numbers, only one valid BST can be constructed containing these numbers.
2. To find the maximum value of a BST, you can follow the right child from the root until a NULL is encountered.
3. To find the minimum value of a BST, you can follow the left child from the root until a NULL is encountered.
4. READ-TREE ( x ) and TREE-SEARCH ( x , v ) can be written in a non-recursive way.

# Sentiment Analysis

- Deciding if a piece of text conveys positive or negative emotions

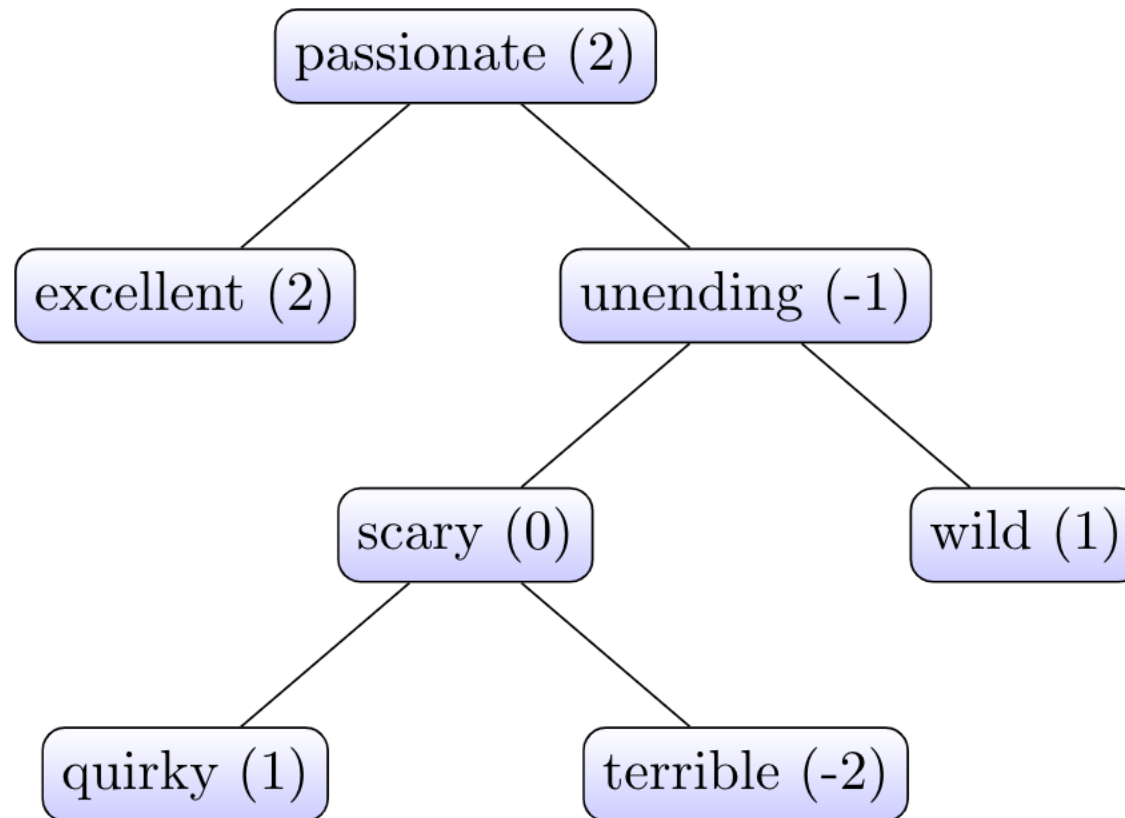
A delectable and intriguing thriller filled with surprises, this movie is an original.

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# Sentiment Analysis



## Main Takeaways

1. Binary search is, on average, more efficient than sequential search.
2. A binary search tree is a data structure that facilitates binary search.
3. Searching through a BST for a value is  $O(\lg(n))$ , where  $n$  is the number of data points in the tree.
4. BSTs can be applied to sentiment analysis, determining whether a piece of text is positive or negative.

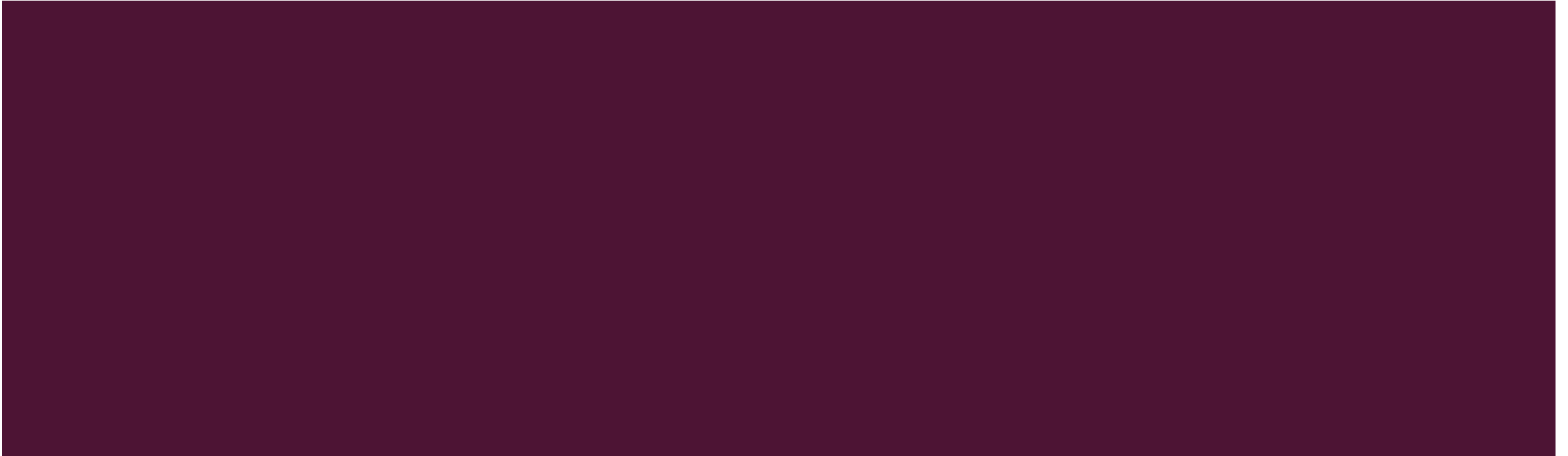
# More Questions?

E-mail me at [wenlaura@umich.edu](mailto:wenlaura@umich.edu).



# Extra Slides!

For your additional enjoyment, or if we have extra time at the end of the lesson.



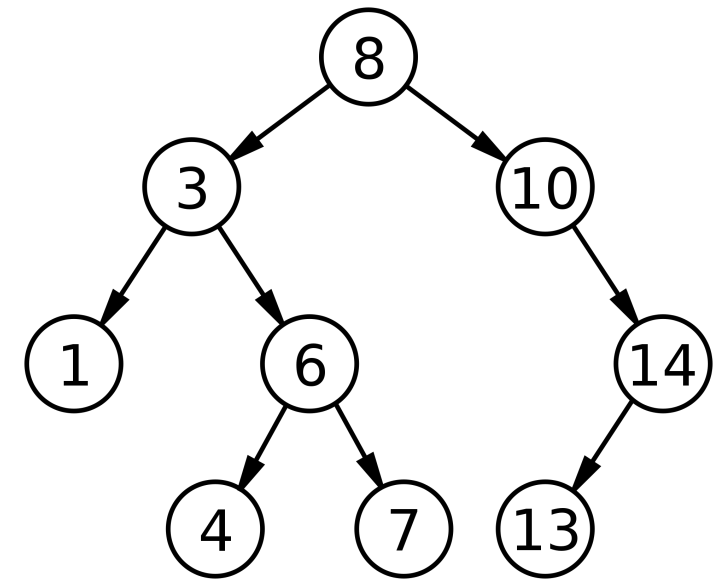
# Inserting into a BST

- $T$  is the tree
- $v$  is the value to insert (e.g., 20)

$\text{TREE-INSERT}(T, v)$

*Search for where the new value should go*

*Insert the new value (rearrange / add tree pointers)*



# Inserting into a BST

- Working individually, write out pseudo-code for the first part of the function (search for where the new value should go).

`TREE-INSERT(T, v)`

*Search for where the new value should go*

*Insert the new value (rearrange / add tree pointers)*

