the test about an individual coefficient b; and about the overall significance are particular cases of this test.

· TEST about a single paraketer by

Special case with B = P-1

Assume we one testing the significance of the last parameter Bp.

(or simply sort the columns of X so that the last covariate is the one corresponding to the parameter of interest)

Testing βp is equivalent to testing a model with $\beta = P-1$ covariates In this case we can portition β and X as

$$\beta = \begin{bmatrix}
\beta_1 \\
\vdots \\
\beta_{P-1}
\end{bmatrix}
\beta = P-1$$

$$X = \begin{bmatrix}
x_1 & \dots & x_{P-1} \\
x_P
\end{bmatrix}$$

the text becomes

$$F = \frac{\frac{\tilde{\Sigma}^{2} - \tilde{\Sigma}^{2}}{1}}{\frac{\tilde{\Sigma}^{2}}{N - P}} \quad \text{Ho} \quad F_{1, N - P} \qquad F = (T_{p})^{2} \quad \text{with} \quad T_{p} = \frac{\hat{B}_{p} - 0}{\sqrt{\hat{N}^{2}(\hat{B}_{p})}} \quad \text{ho} \quad \text{tn-p}$$

$$\downarrow \quad (\text{recall}: \text{ if } V_{N} \text{ tm}, \text{ then } V^{2}_{N} F_{1, m})$$

. TEST ABOUT THE OVERALL SIGNIFICANCE

if we consider
$$\beta = 1$$

$$\begin{cases} H_0: \beta_2 = \beta_3 = ... = \beta_p = 0 \\ H_1: \overline{H_0} \end{cases}$$

then
$$\underline{\beta} = \begin{bmatrix} \beta_1 \\ \beta_2 \\ \vdots \\ \beta_P \end{bmatrix} = \begin{bmatrix} \beta_1 \\ \beta_2 \\ \vdots \\ \beta_P \end{bmatrix}$$

$$X = \begin{bmatrix} x_1 \\ x_2 \\ \dots \\ x_P \end{bmatrix}$$

The restricted model corresponds to the NULL HOBEL (model with only the intercept)

the test is
$$F = \frac{\frac{\tilde{\Sigma}^2 - \hat{\Sigma}^2}{P-1}}{\frac{\hat{\Sigma}^2}{n-P}} \stackrel{\text{Ho}}{\sim} F_{P-1, n-P}$$

· Equivalence with the test about the coefficient R2

under the, all coefficients but \$1 (intercept) are zero: none of the coveriates is useful to predict y. The model assumed under the is Yi = P2 + Ei

We know that in the null model the estimate of β_1 is $\beta_1 = \overline{y}$.

The predicted values are gi = 9 for all i = 1,...,n

The residuals one & = yi-y

The estimate $q^2 e^2$ is $\tilde{e}^2 \cdot \frac{1}{n} = \tilde{e}^{-\frac{n}{2}}$

The distribution of the estimator is $\frac{n\Sigma^2}{\sigma^2} \sim \chi^2_{n-1}$

This model corresponds to the case of "no einear relationship between y and the covariates". We have seen that the coefficient R2 in this case is close to zero.

Similarly to what we have seen for the simple linear modely we can Aformulate this hypothesis as a test about the value of the coefficient R^2 associated with the model:

$$\begin{cases} H_0: R^2=0 \\ H_1: R^2\neq 0 \end{cases}$$

We used a transformation of R^2 : $\frac{R^2}{1-R^2}$

$$\frac{1}{1} \cdot \frac{1}{1} \cdot \frac{1}$$

We used a transformation of
$$R^2$$
: $\frac{R^2}{4-R^2}$

Here, $F = \frac{\frac{\Sigma^2 - \Sigma^2}{P-1}}{\frac{\Sigma^2}{N-P}} = \frac{\frac{\Sigma^2 - \Sigma^2}{P-1}}{\frac{\Sigma^2}{N-P}} = \frac{\frac{\Sigma^2 - \Sigma^2}{P-1}}{\frac{E^2 - E^2}{P-1}} = \frac{\frac{E^2 - E^2}{E^2} - \frac{N-P}{P-1}}{\frac{E^2 - E^2}{E^2}} = \frac{\frac{N-P}{P-1}}{\frac{SSE}{N-P}} = \frac{\frac{SSE}{N-P}}{\frac{SSE}{N-P}} = \frac{\frac{N^2}{N-P}}{\frac{N-P}{N-1}} = \frac{\frac{N^2}{N-P}}{\frac{N-P}{N-1}} = \frac{\frac{N^2}{N-P}}{\frac{N-P}{N-1}} = \frac{\frac{N^2}{N-P}}{\frac{N-P}{N-1}} = \frac{\frac{N^2}{N-P}}{\frac{N-P}{N-1}} = \frac{\frac{N^2}{N-P}}{\frac{N-P}{N-1}} = \frac{\frac{N^2}{N-P}}{\frac{N-P}{N-P}} = \frac{\frac{N^2}{N-P}}{\frac{N-P}} = \frac{\frac{N^2}{N-P}}{\frac{N-P}{N-P}} = \frac{\frac{N^2}{N-P}}{\frac{$