Exercises: Simple Gaussian Linear Regression Part III

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(Referring to the theoretical parts: 4, 5, 6, 7, 8)

1 Computer repair data

A corporation sells computer parts and performs maintenance and repair service. The data below have been collected from 18 recent calls to perform maintenance service; for each call, x is the number of repairs and y is the total number of minutes spent by the service person. Assume that a Gaussian linear model $Y_i = \beta_1 + \beta_2 x_i + \varepsilon_i$ is appropriate. Knowing that:

$$\sum_{i=1}^{18} y_i = 1152 \qquad \sum_{i=1}^{18} x_i = 81$$

$$\sum_{i=1}^{18} (y_i - \bar{y})^2 = 16504 \qquad \sum_{i=1}^{18} (x_i - \bar{x})^2 = 74.5 \qquad \sum_{i=1}^{18} (y_i - \bar{y})(x_i - \bar{x}) = 1098$$

where \bar{x} and \bar{y} are the sample means, and

$$\sum_{i=1}^{18} (y_i - \hat{y}_i)^2 = 321.39$$

- a) Obtain the estimated regression function.
- b) Interpret β_2 in your estimated regression function. Does β_1 provide any relevant information here? Explain.
- c) It is reasonable to think that the intervention time increases if the number of repairs increases. Is this idea supported by the data at a significance level 0.05? (Test the hypothesis $H_0: \beta_2 = 0$ vs. $H_0: \beta_2 > 0$.)
- d) Compute a 95% confidence interval for β_2 .
- e) Test the hypothesis $H_0: \beta_2 = 0$ vs. $H_0: \beta_2 \neq 0$ at a significance level 0.05. Was it necessary to perform this test, given what you already knew from the previous points? Explain.

- f) Obtain a point estimate of the mean service time when x=5 parts are repaired. Obtain a confidence interval with level 0.90.
- g) Obtain the partition of the total sum of squares and coefficient \mathbb{R}^2 .