a) the model is

The model is

Yi ~ Bernoulli(
$$\pi$$
i) independent i=1,..., 714

Bogit(π i) = β_1 + β_2 1 (class:= first) + β_3 1 (gender:= man) + β_4 aga:

dummy = $\begin{cases} 1 & \text{if class} = \text{first} \\ 0 & \text{if class} \neq \text{first} \end{cases}$ dummy = $\begin{cases} 1 & \text{if gender} = \text{man} \\ 0 & \text{if class} \neq \text{first} \end{cases}$

The extimated model is $expir(\hat{R}_i) = exp \frac{\hat{R}_i}{1 + \hat{Q}_i} = 1.50 + 2.01 \text{ } 1 \text{ } (class_i = first) - 2.54 \text{ } 1 \text{ } (gender_i = man) - 0.023 \cdot age_i$ Y: ~ Bernoulli (tic)

likelihood function し(で)= 荒りをが(ルなりしが)

$$L(\frac{\beta}{\beta}) = \frac{n}{12} \left\{ \left(\frac{e^{\frac{2n}{n}}}{1 + e^{\frac{2n}{n}}} \right)^{\frac{n}{n}} \left(\frac{1}{1 + e^{\frac{2n}{n}}} \right)^{\frac{n}{n}} \right\}$$
 where I denote with $\frac{2n}{n}$ the row vector of the observed values of the covortates for individual i

the leglikelihood is

the experienced 25

$$e(\underline{P}) = exp L(\underline{P})$$

$$= \sum_{i=1}^{n} \left\{ \sum_{i=1}^{n} P_{i} - y_{i} exp(1 + e^{\sum_{i=1}^{n} P_{i}}) - (1 - y_{i}) exp(1 + e^{\sum_{i=1}^{n} P_{i}}) \right\}$$

$$= \sum_{i=1}^{n} \left\{ \sum_{i=1}^{n} P_{i} - y_{i} exp(1 + e^{\sum_{i=1}^{n} P_{i}}) - exp(1 + e^{\sum_{i=1}^{n} P_{i}}) + y_{i} exp(1 + e^{\sum_{i=1}^{n} P_{i}}) \right\}$$

$$2 = \frac{\hat{\beta}_3 - o}{\sqrt{[i(\hat{\beta})]_{G,3}^{-1}}}$$
Hence the needed quantity is $2^{ob5} = \frac{-2.5473}{0.2017} = -12.629$

this is the produce of the Test Ho:
$$\beta_u = 0$$
 vs. Hr: $\beta_u \neq 0$
Similar to the provious point, it is based on the quantity
$$\frac{\hat{\beta}_u}{\int [\hat{j}(\hat{\beta})]^{-1}_{C_u(u)}}$$
in NCo.t)

Hence the product is
$$x^{ob5} = P_{Ho}(12|>12^{ob5}!)$$

= 2 $P_{Ho}(2>12^{ob5}!)$
= 2 $(1-\overline{\Phi}(12^{ob5}!)$

d)
$$\hat{\pi}_{A} = (\hat{\pi}_{A} \mid gorden_{A} = 0, class_{A} = 4, age_{A} = 30) = \frac{e^{\frac{c}{k} + \frac{c}{k}}}{1 + e^{\frac{c}{k} + \frac{c}{k}}} = 0.9317$$

since
$$\tilde{X}_{1}^{T}\hat{\beta}=1.5\omega 3+2.0103\cdot 1-2.5673\cdot 0-0.0293\cdot 30=2.6136$$

 $\Rightarrow \frac{e^{\tilde{X}_{1}^{T}\beta}}{1+e^{\tilde{X}_{1}^{T}\beta}}=\frac{e^{2.6136}}{1+e^{2.6136}}=0.9317$

the odds for individual A one
$$\frac{\hat{\pi}_A}{1-\hat{\pi}_A} = 13.648$$

we know that

Copic
$$\hat{H}_A = \hat{\beta}_1 + \hat{\beta}_2 + \hat{\beta}_4 \cdot 30$$

Copic
$$\hat{\pi}_{B} = \hat{\beta}_{1} + \hat{\beta}_{2} + \hat{\beta}_{4} \cdot 31 = \hat{\beta}_{1} + \hat{\beta}_{2} + \hat{\beta}_{4} \cdot 30 + \hat{\beta}_{4}$$

Hence
$$eopt \hat{\pi}_B - eopt \hat{\pi}_A = \hat{\beta}_H$$

$$eop \frac{\hat{\pi}_B}{4 - \hat{\pi}_B} - eop \frac{\hat{\pi}_A}{4 - \hat{\pi}_A} = eop \frac{1 - \hat{\pi}_B}{4 - \hat{\pi}_A} = \hat{\beta}_H$$

$$\Rightarrow \frac{\hat{\pi}_B}{1 - \hat{\pi}_B} = e^{\hat{\beta}_H}$$

1-the odds of individual A change of a multiplicative factor
$$e^{\hat{\beta}_4}$$
 to obtain the odds of individual B.

This is, add $g = \frac{\hat{\pi}_{c} g}{1 - \hat{\pi}_{c} g} = e^{-0.0257}$. 13.648 = 13.246

$$\hat{\beta}_{2} = \log \frac{P(Y_{i}=1 \mid closs_{i}=1)}{P(Y_{i}=0 \mid closs_{i}=0)} \Rightarrow e^{\hat{\beta}_{2}} = \frac{(odd s \mid closs_{i}=1)}{(odd s \mid closs_{i}=0)}$$

$$P(Y_{i}=0 \mid closs_{i}=0)$$

The odds of a person in third class one multiplied by $e^{\frac{2}{3}} = e^{2.0103}$ 7.4657 obtain the odds of a person in first class (keeping the other covariates fixed). Since By is positive, a person with a first-class ticket has a higher probability of surviving, composed to a person with a scond or third-class sicket.

we use the Best stabilities
$$\hat{\beta}_2 = \frac{\hat{\beta}_2 - o}{\hat{se}(\hat{\beta}_2)} \text{ is } N(O_1 1)$$

2008 = 8.11 (in the Table) Hence I do not reject to for all usual or



and E(model) is the maximum of the eq-likelihood under the current model The mull designce is

single parameter to

we want to tast
$$\begin{cases} H_0: \beta_2 = \beta_3 = \beta_4 = 0 \end{cases}$$

we want to task

$$\begin{cases}
H_0: \beta_2 = \beta_3 = \beta_4 = 0 \\
H_1: \text{ at easy one is } \neq 0
\end{cases}$$

under Ho, the model is Yin Ber(
$$\pi$$
) Copit(π) = β_1 "null model" the maximum of the Egetkelihood is e^{α} (null) under H1, I have the complete model

$$W = 2(\hat{c}(model) - \tilde{c}(null)) \approx \chi^2_{P-1} = \chi^2_3$$

$$D(null) - D(model) = 2 i \tilde{c}(soturated) - \tilde{c}(null) - \tilde{c}(soturated) - \hat{c}(model) i$$

$$= 2 i \hat{c}(model) - \tilde{c}(null)$$

Hence the observed value of the Test is

$$w^{obs} = 964.52 - 675.14 = 299.38$$
Reject region: $R = (\chi_{3; 4-\alpha; +\infty}^2)$

1 reject the

