

Point Normal triangles

[Rick]

1. Welcome everybody.
2. Abbreviation PN
3. Vlachos and others (2001)
4. Improve **visual quality** of triangle based **real time entertainment**, e.g. Computer games

Point Normal triangles



[Rick]

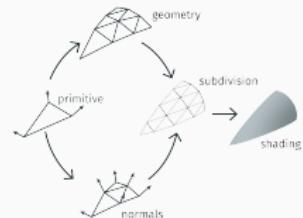
1. Tell what can be seen on the slide.
2. Stand still by the geometry
3. PN triangle -> more **organic shapes** (and **continuous surface**)
4. Relatively easy to extend existing 'pipeline'

Point Normal triangles

└ Single PN Triangle

SINGLE PN TRIANGLE

1. [Rick]
2. Explain (vaguely) process from input to result (prev. slide) -> **input** -> **single** -> **mesh**
3. Start: Construction of single pn triangle ->
Laura



2015-12-13

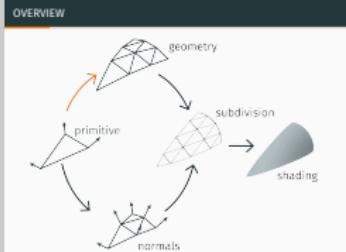
Point Normal triangles

└ Single PN Triangle

[Laura] PN triangle is defined by geometry and normal component.

Point Normal triangles

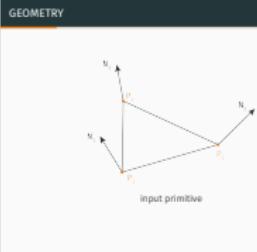
└ Single PN Triangle



Laura From geometric component of input primitive to geometric component of PN triangle

Point Normal triangles

└ Single PN Triangle

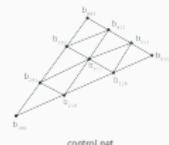


1. **[Laura]** This is a standard triangle primitive, defined by its vertices and normals.
2. **[Laura]** Note that we only have this input primitive, without information about its neighbors.

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Point Normal triangles

└ Single PN Triangle

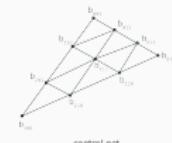


1. [Laura] This is the topology of the final patch
2. [Laura] Mention which vertices are vertex, tangent and center coefficient.

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Point Normal triangles

└ Single PN Triangle



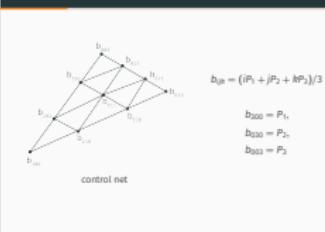
$$b_{ijk} = (iP_1 + jP_2 + kP_3)/3$$

1. [Laura] These are all the initial control point.
Evenly divided on the triangle. -> formula
2. [Laura] Nice formula

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Point Normal triangles

└ Single PN Triangle

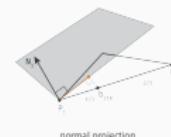


1. [Laura] Stress that the vertex coefficients/control points are the one on the original vertices and that they do not move.

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Point Normal triangles

└ Single PN Triangle



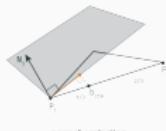
$$\begin{aligned}n_{ij} &= (P_i - P_j) \cdot n_i \in \mathbb{R} \\B_{ij0} &= \frac{n_{ij} + n_{ji}}{2} \\B_{ij1} &= \frac{1}{2} \\B_{ij2} &= \frac{2P_i + P_j - n_{ij}n}{3}\end{aligned}$$

[Laura] Define a plane using the closest vertex and its normal. Find the point on this plane that is closest to the uniformly distributed point.

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Point Normal triangles

└ Single PN Triangle



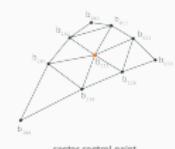
$$w_0 = (P_j - P_i) \cdot N_j \in \mathbb{R}$$
$$b_{210} = \frac{2P_1 + P_2 - w_{12}N_1}{3}$$
$$\vdots$$
$$b_{201} = \frac{2P_1 + P_3 - w_{13}N_1}{3}$$

[Laura] Define a plane using the closest vertex and its normal. Find the point on this plane that is closest to the uniformly distributed point.

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Point Normal triangles

└ Single PN Triangle



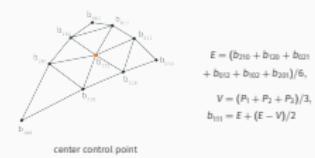
$$\begin{aligned}E &= (\text{Base}_1 + \text{Base}_2 + \text{Base}_3)H, \\&\approx \text{Base}_1 + \text{Base}_2 + \text{Base}_3)H, \\V &= (P_1 + P_2 + P_3)/3, \\S_{PN} &= E + (E - V)/2\end{aligned}$$

1. [Laura] Note that this is the result of the previous step -> now only center coefficient is left.

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Point Normal triangles

└ Single PN Triangle

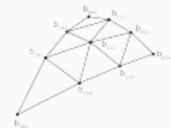


1. [Laura] Average of the tangent coefficients plus half the difference between the tangent and vertex coefficients.

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Point Normal triangles

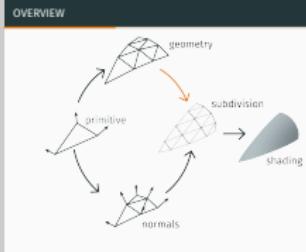
└ Single PN Triangle



[Laura] Results

Point Normal triangles

└ Single PN Triangle

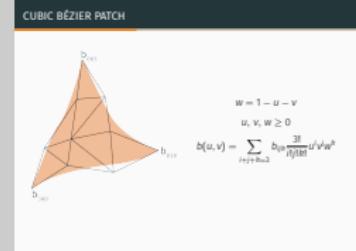


[Rick]

1. From **geometry** to getting a number of **flat triangles**
2. **Number of flat triangles** depends on the **level of detail** -> Later
3. Noticed: Cubic b茅zier patch control net -> next slide.

Point Normal triangles

└ Single PN Triangle

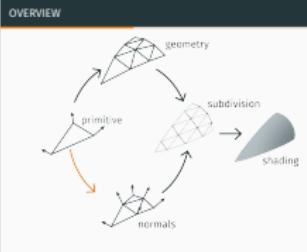


[Rick]

1. Any point is \rightarrow a **unique convex combination** of the control vertices.
(Barycentric coordinates)
2. Computations done with this **cubic bezier triangle** function in **Bernstein form**.

Point Normal triangles

└ Single PN Triangle

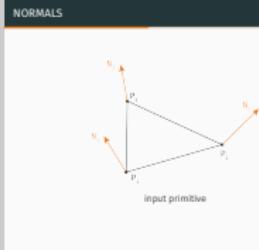


[Rick]

1. **Seen:** Construction of cubic bézier **geometry**
2. Summarize (?)
3. **Now:** Construction of normals -> next slide

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└ Single PN Triangle

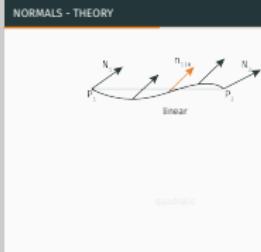


[Rick]

1. This step: Again input primitive \rightarrow only vertices and normals are known
2. Stress (again): no knowledge of adjacent triangles

Point Normal triangles

└ Single PN Triangle



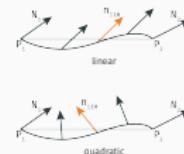
[Rick]

1. Stress: Two (more but ...) methods are possible
2. First: Linear -> GOOD for parabolic curve -> BAD with inflection points (**cubic**)

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Point Normal triangles

└ Single PN Triangle

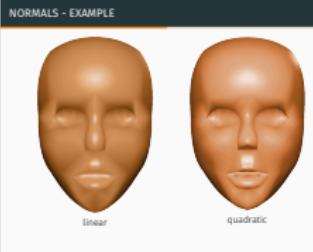


[Rick]

1. **Second** option: quadratic does capture inflection points
2. **Higher order?** not necessary (performance vs quality)

Point Normal triangles

└ Single PN Triangle

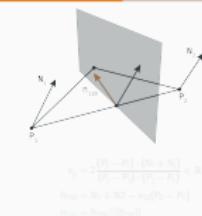


[Rick]

1. Theory is just fine, but what about some results!
2. Which one is more pleasing/better?

Point Normal triangles

└ Single PN Triangle



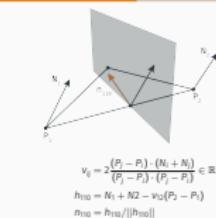
[Rick]

1. Intuitively -> take the average of the two normals.
2. GOOD parabolic (different normals). BAD cubic (same normals)
3. Drawing (?)
4. Solution -> reflect the average.

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Point Normal triangles

- Single PN Triangle



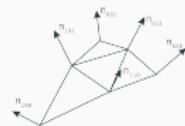
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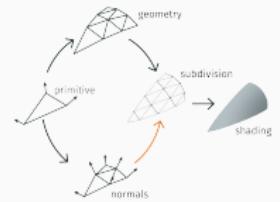
Point Normal triangles

└ Single PN Triangle



[Rick]

1. The 6 control points (normals) for the parametrization used during subdivision. -> Laura



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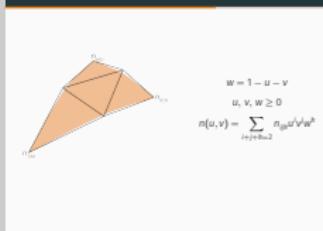
└ Single PN Triangle

laura

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Point Normal triangles

└ Single PN Triangle



$$w = 1 - u - v$$

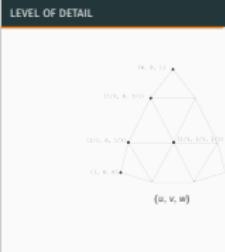
$$u, v, w \geq 0$$

$$n(u, v) = \sum_{i+j+3=2} n_{ij} u^i v^j w^k$$

[Laura] u , v and w are an convex combination

Point Normal triangles

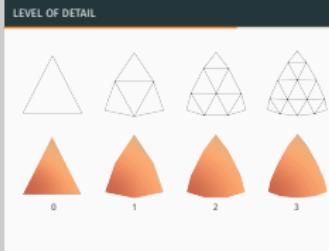
└ Single PN Triangle



[Laura] LOD = 2

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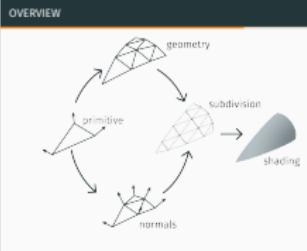
└ Single PN Triangle



[Laura] Level of detail -> subdivision -> how many triangles go through to the next shaders.

Point Normal triangles

└ Single PN Triangle



1. [Laura] Recap of the whole process
2. [Laura] Shading out of the scope of this presentation
3. [Laura] Why quadratic patch for normals, why cubic patch for geometry: We need at least cubic geometry and quadratic normals to capture inflections. There are no additional data to suggest higher degree patches. Simplicity v.s. modeling range

Point Normal triangles

└ A Triangle Mesh

A TRIANGLE MESH

[rick] blaat

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Point Normal triangles

└ A Triangle Mesh

"PN triangles should not deviate too much from the original triangle to preserve the shape and avoid interference with other curved triangles."¹

¹slachin2003isurved

[Rick] Problem when combining multiple triangles, so this is an important property

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Point Normal triangles

└ A Triangle Mesh

PN triangles have:²

- C^1 continuity in the vertex points
- C^0 continuity along the edges
- C^∞ everywhere else

²Jan2003parallel

[Rick] Continuity C^0 is important -> no gaps.
Higher is better because this gives a more smooth result.

Point Normal triangles

└ A Triangle Mesh



[Rick] Curved triangles do not always give the preferred results -> sharp edges. Solution is to insert more triangles at the sharp edges -> model needs to be changed :(

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Point Normal triangles

└ A Triangle Mesh



[Rick] Beyond the scope of the paper extension exist to overcome the problem what you have when combining multiple meshes. Story about shared vertices.

Point Normal triangles

└ Graphics Pipeline

GRAPHICS PIPELINE

[Laura] Blaat

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Point Normal triangles

└ Graphics Pipeline



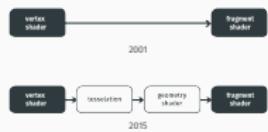
2005

[Laura] Great part of the paper stresses the point that it can easily be implemented as a preprocessing step (CPU.
2001 pipeline (OpenGL 1.3)

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Point Normal triangles

└ Graphics Pipeline



[Laura] 2015 we have OpenGL 4.5 with more programmable shaders and the whole process can be done on the GPU. Since PN triangles only uses the primitive, no neighboring primitives, easy in shaders.

Point Normal triangles

└ Graphics Pipeline



[Laura] Why PN triangles are not suited to rendering for CAD: On real objects, the normal field is determined by the geometry and thus fixed. If you invent fake normals the rendering looks better but the user gets an unpleasant surprise when the product is actually manufactured.

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Point Normal triangles

└ Graphics Pipeline