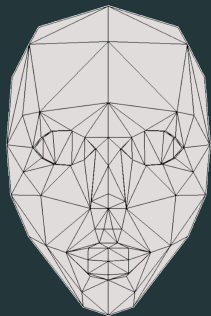


POINT NORMAL TRIANGLES

Rick van Veen Laura Baakman

December 14, 2015

Advanced Computer Graphics



INPUT MESH



GOURAUD



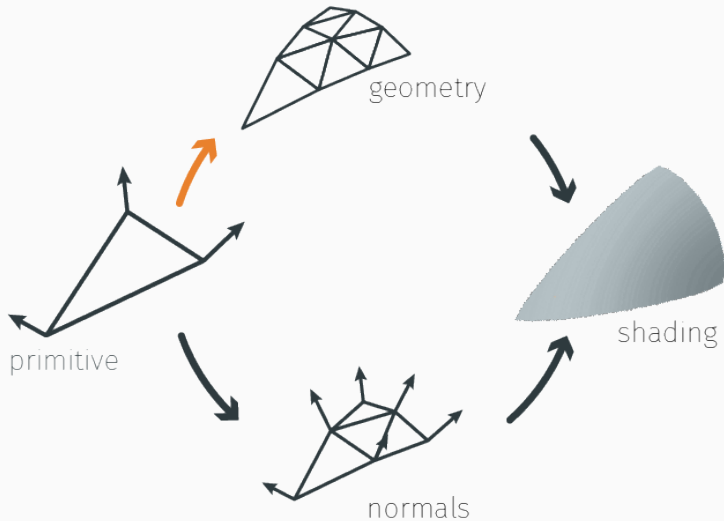
PN GEOMETRY



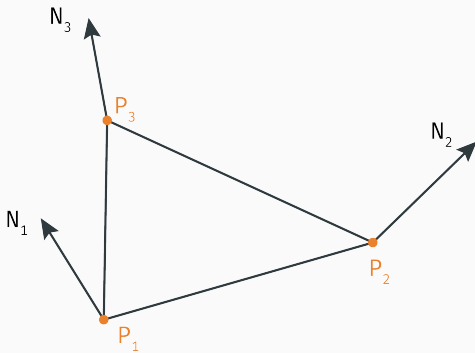
PN TRIANGLES

SINGLE PN TRIANGLE

OVERVIEW

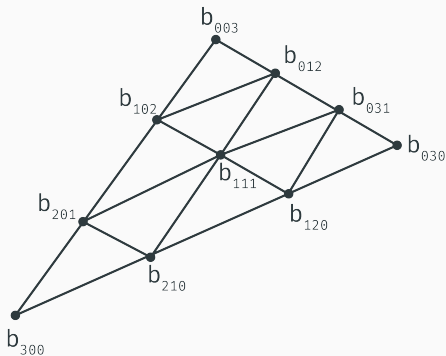


Possible: emphasise vertices better



input primitive

GEOMETRY - VERTEX COEFFICIENTS



control net

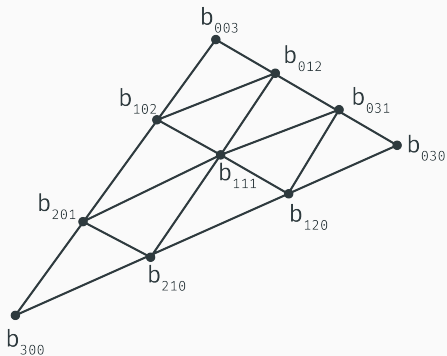
$$b_{ijk} = (iP_1 + jP_2 + kP_3)/3$$

$$b_{300} = P_1,$$

$$b_{030} = P_2,$$

$$b_{003} = P_3$$

GEOMETRY - VERTEX COEFFICIENTS



control net

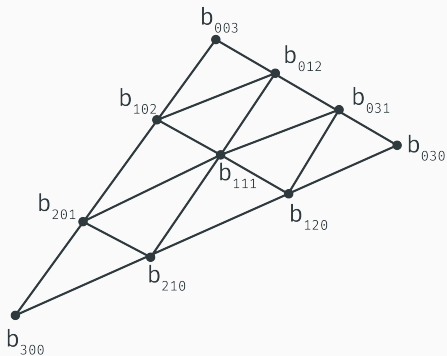
$$b_{ijk} = (iP_1 + jP_2 + kP_3)/3$$

$$b_{300} = P_1,$$

$$b_{030} = P_2,$$

$$b_{003} = P_3$$

GEOMETRY - VERTEX COEFFICIENTS



control net

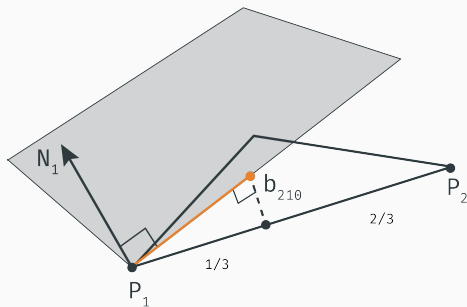
$$b_{ijk} = (iP_1 + jP_2 + kP_3)/3$$

$$b_{300} = P_1,$$

$$b_{030} = P_2,$$

$$b_{003} = P_3$$

GEOMETRY - TANGENT COEFFICIENTS



normal projection

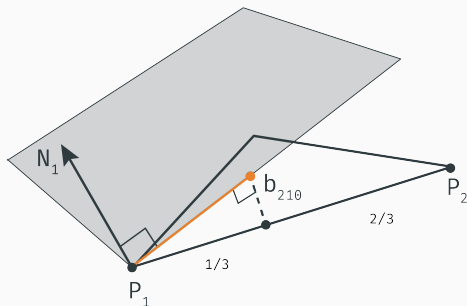
$$w_{ij} = (P_j - P_i) \cdot N_i \in \mathbb{R}$$

$$b_{210} = \frac{2P_1 + P_2 - w_{12}N_1}{3},$$

\vdots

$$b_{201} = \frac{2P_1 + P_3 - w_{13}N_1}{3}$$

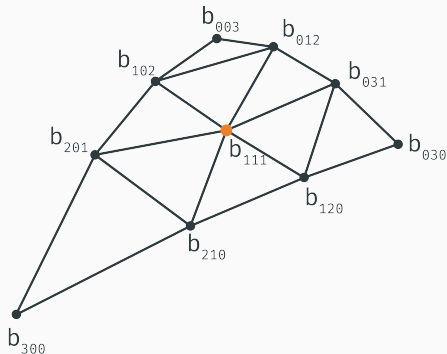
GEOMETRY - TANGENT COEFFICIENTS



normal projection

$$\begin{aligned}w_{ij} &= (P_j - P_i) \cdot N_i \in \mathbb{R} \\b_{210} &= \frac{2P_1 + P_2 - w_{12}N_1}{3}, \\&\vdots \\b_{201} &= \frac{2P_1 + P_3 - w_{13}N_1}{3}\end{aligned}$$

GEOMETRY - CENTER COEFFICIENT



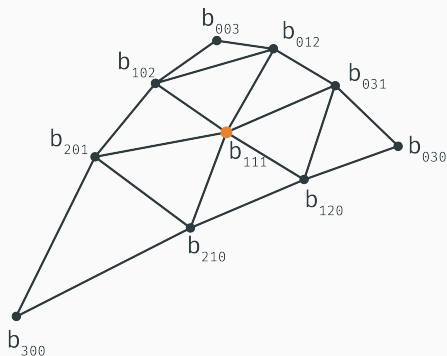
center control point

$$E = (b_{210} + b_{120} + b_{021} + b_{012} + b_{102} + b_{201})/6,$$

$$V = (P_1 + P_2 + P_3)/3,$$

$$b_{111} = E + (E - V)/2$$

GEOMETRY - CENTER COEFFICIENT

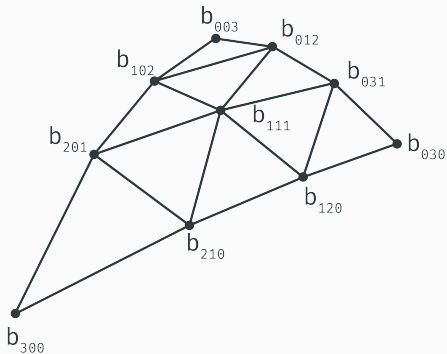


center control point

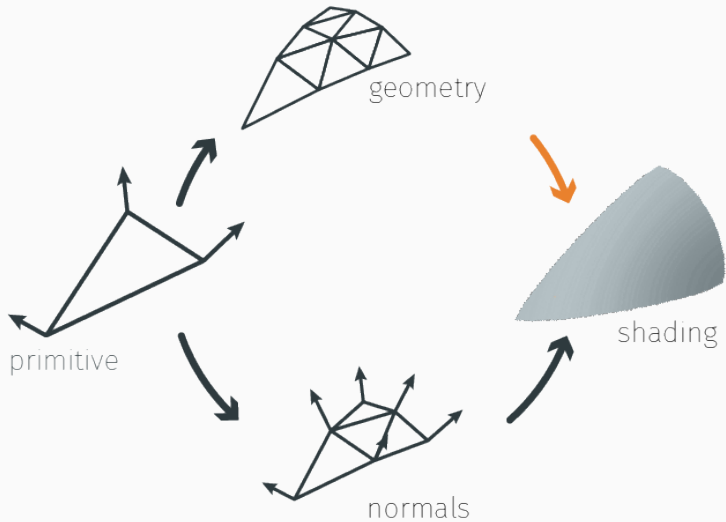
$$E = (b_{210} + b_{120} + b_{021} + b_{012} + b_{102} + b_{201})/6,$$

$$V = (P_1 + P_2 + P_3)/3,$$
$$b_{111} = E + (E - V)/2$$

Set result slide to plain



OVERVIEW



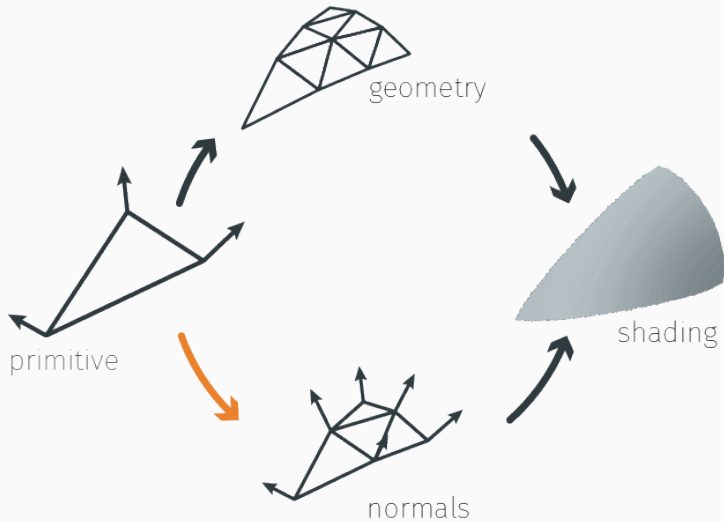
Spacing van de for all

Plaatje?

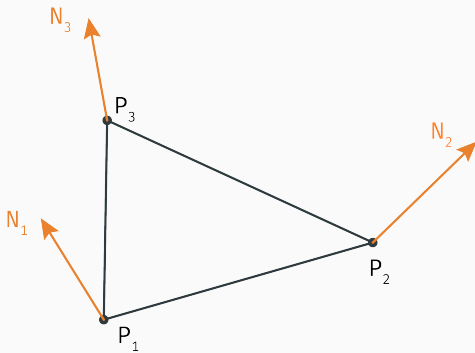
$$b : \mathbb{R}^2 \rightarrow \mathbb{R}^3, \text{ for } w = 1 - u - v, u, v, w \geq 0$$

$$\begin{aligned} b(u, v) &= \sum_{i+j+k=3} b_{ijk} \frac{3!}{i!j!k!} u^i v^j w^k \\ &= b_{300} w^3 + b_{030} u^3 + b_{003} v^3 \\ &\quad + b_{210} 3w^2 u + b_{120} 3wu^2 + b_{201} 3w^2 v \\ &\quad + b_{021} 3u^2 v + b_{102} 3wv^2 + b_{012} 3uv^2 \\ &\quad + b_{111} 6wuv. \end{aligned}$$

OVERVIEW

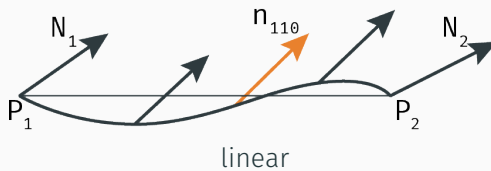


Possible: emphasise normals more



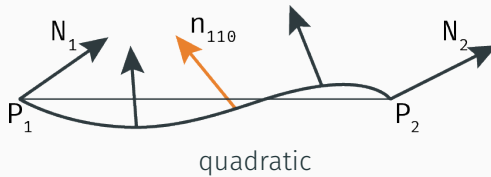
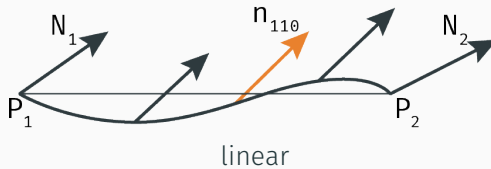
input primitive

NORMALS - THEORY



quadratic

NORMALS - THEORY



NORMALS - EXAMPLE

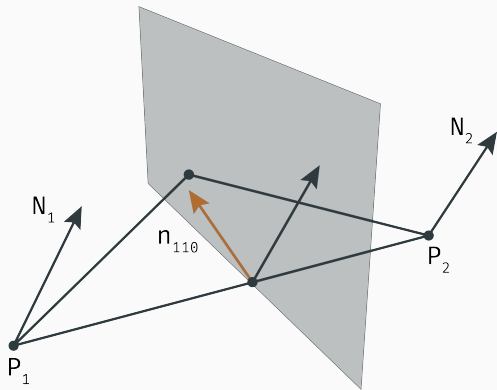


linear



quadratic

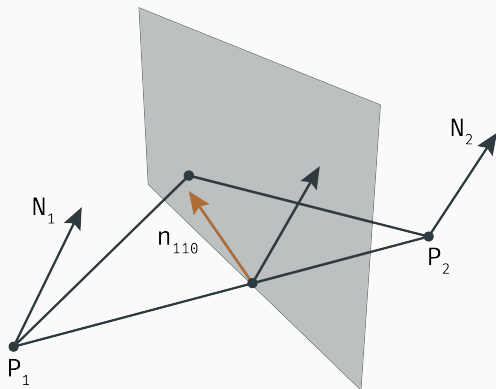
NORMALS - THEORY



$$v_{ij} = 2 \frac{(P_j - P_i) \cdot (N_i + N_j)}{(P_j - P_i) \cdot (P_j - P_i)} \in \mathbb{R}$$

$$h_{110} = N_1 + N_2 - v_{12}(P_2 - P_1)$$

$$n_{110} = h_{110} / ||h_{110}||$$



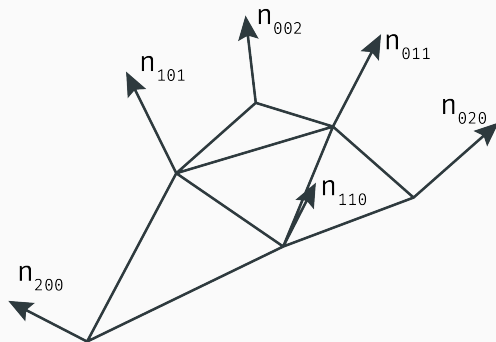
$$v_{ij} = 2 \frac{(P_j - P_i) \cdot (N_i + N_j)}{(P_j - P_i) \cdot (P_j - P_i)} \in \mathbb{R}$$

$$h_{110} = N_1 + N_2 - v_{12}(P_2 - P_1)$$

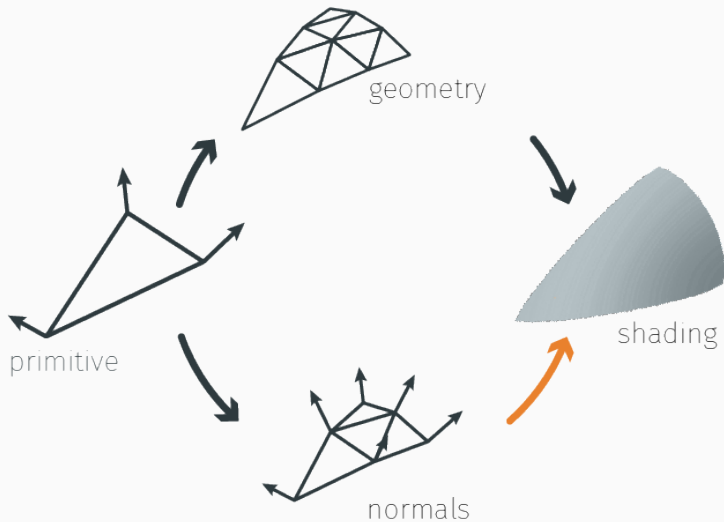
$$n_{110} = h_{110} / \|h_{110}\|$$

NORMALS - RESULT

Set result slide to plain



OVERVIEW

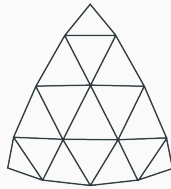
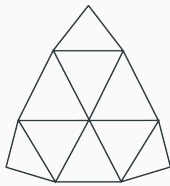
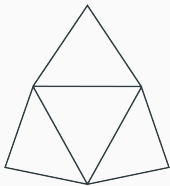
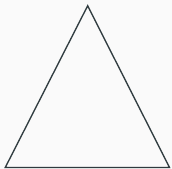


Plaatje

$n : \mathbb{R}^2 \rightarrow \mathbb{R}^3$, for $w = 1 - u - v$, $u, v, w \geq 0$

$$\begin{aligned} n(u, v) &= \sum_{i+j+k=2} n_{ijk} u^i v^j w^k \\ &= n_{200} w^2 + n_{020} u^2 + n_{002} v^2 \\ &\quad + n_{110} wu + n_{011} uv + n_{101} wv \end{aligned}$$

LEVEL OF DETAIL



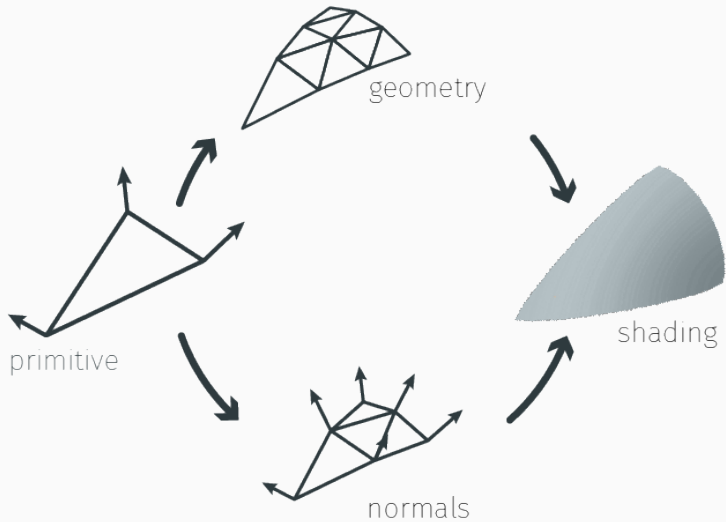
0

1

2

3

OVERVIEW



A TRIANGLE MESH

“PN triangles should not deviate too much from the original triangle to preserve the shape and avoid interference with other curved triangles.”¹

¹Vlachos et al.

PN triangles have:²

- C^1 continuity in the vertex points
- C^0 continuity everywhere else

²Jiao and Alexander

SHARP EDGES



mesh



blunt

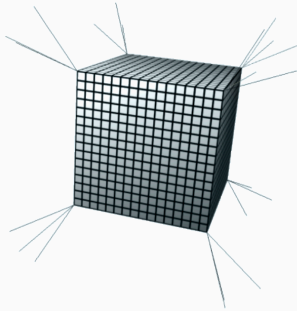


mesh

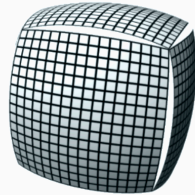


sharp

SEPARATE NORMALS



normals



cracks

GRAPHICS PIPELINE



2001

2015

HARDWARE - PIPELINES



2001



2015

CONCLUSION




CONCLUSION

Some conclusion?



FIGUUR 13 UIT PAPER

QUESTIONS?

-  Xiangmin Jiao and Phillip J Alexander. “Parallel feature-preserving mesh smoothing”. In: *Computational Science and Its Applications–ICCSA 2005*. Springer, 2005, pp. 1180–1189.
-  J McDonald and M Kilgard. *Crack-free point-normal triangles using adjacent edge normals*. 2010.
-  Alex Vlachos et al. “Curved PN triangles”. In: *Proceedings of the 2001 symposium on Interactive 3D graphics*. ACM, 2001, pp. 159–166.