# Neural Networks Practical Assignment I: Perceptron training

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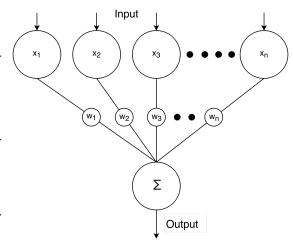
### I. Introduction

Artificial neural networks are non-linear mapping systems inspired by biological nervous systems. The most import parts of a biological neuron include a dendrite that receives signals from other neurons, a soma that integrates the signals and generates a response that is distributed via a branching axon.

An artificial neural network consists of a large numbers of simple processors linked by weighted connections, analogously the neurons. Each processor receives inputs from many other nodes and generates a single scalar output that depends on locally available information. This scalar is distributed as input to other nodes.

The most simple case of a neural network is the perceptron, see Figure 1, This network consists of one layer of input nodes, connected to a processing unit through a single layer of weights, which determine the result of the output node. Mathematically a perceptron is any feed-forward network of noes with responses like  $f(\vec{w}^T\vec{x})$  where  $\vec{w}$  is the vector of weights,  $\vec{x}$  is the pattern and f is a sigmoid-like squashing function[1]. This squashing function ensures the binary output of the perceptron.

The perceptron is a linear binary classifier which means that it can only classify data sets that are homogeneously separable, which means that one can separate the data points of different classes with a vector through the origin. Inhomogeneously separable datasets are linearly separable when the separating vector is moved with some offset with respect to the origin.



**Figure 1:** A perceptron.

It can be shown that the perceptron converges, i.e. it separates positive examples for the negatives, if the input data set is linearly separable.

## II. Метнор

Given a dataset  $\mathcal{D}$  with N patterns  $\xi \in \mathcal{R}^d$  each with a label S:  $\mathcal{D} = \{\xi^i, S^i\}_i^N$ , a perceptron can be trained using the Rosenblatt algorithm which updates the weights each time step  $t = 1, 2, \ldots$ :

$$\vec{w}(t+1) = \begin{cases} \vec{w}(t) + \frac{1}{d}\xi^{\mu(t)}S^{\mu(t)} & \text{if } E^{\mu(t)} \leq 0\\ \vec{w}(t) & \text{otherwise} \end{cases}$$
(1

Where  $\mu(t) = 1, 2, ..., N, 1, 2, ...$  denotes the present pattern.  $E(\cdot)$  the energy function is defined as:

$$E^{\mu(t)} = \vec{w}(t) \cdot \xi^{\mu(t)} S^{\mu(t)}.$$
 (2)

The energy function indicates if the perceptron gives the correct output for the given input pattern  $\xi^{\mu(t)}$ . Since we know that independent of the initial value of the weights the perceptron will converge, if the  $\mathcal{D}$  is linearly separable, we can start with  $\vec{w}=0$ .

The update defined in Equation 1 is executed until  $E^{\xi^i} > 0$  for  $i \in [1, N]$  in this cases the algorithm has converged. If the dataset is not linearly separable the perceptron never converges, thus it is generally a good idea to set a maximum number of time steps,  $d_{max}$ . The total number of steps taken by the algorithm

has thus the upper bound  $d_{max} \cdot N$ .

To classify a inhomogenously separable dataset with a perceptron one needs to add a one extra input to all patterns, namely minus one and one extra weight, associated with the extra input.

# Experimenten uitleggen

### REFERENCES

[1] Russell D Reed and Robert J Marks. Neural smithing: supervised learning in feedforward artificial neural networks. Mit Press, 1998.