LoanLogisticRegModel

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EDA

Looking into the data

Statistics

- ID can be dropped since it is not a useful predictor and just a unique identifier and will affect the results of the model
- Age mean is 45 years old, 23 has is the lowest and 67 is the highest. There seems to be a normal distribution.
- ***There are negative values in Experience which is odd because there can't be negative years of experience. This will be looked at next.***
- The mean income is 73 while the median is 64 showing skewness which seems normal representation of society. The minimum income is 8,000 and the max is 224,000. These are common Salaries
- ZIP.Code should not be numberic they should be changed to categorical. There are 467 distinct ZIP codes
- There seems to be an equal distribution for families size 1,2,3,4. Each are compose of about 25%
- The CCAVG, Average Spending per 1000 goes from 0 to 10,000, however the median is 1,5000. Here we can see that there are outliers.
- For Education, 41% have have up to highschool, 28% up to under grad studies and interestingly 30% have up to grad school. That seems like a reasonable distribution.
- For mortgage we can see how skewed it is, the mean is 56.5 and the median is 0. Showing the extreme outliers. **This needs to be looked at**
- For the target variable, personal loan, we can see quite a difference, 90% without a loan and only 10% with loan. This makes sense because not many people take loan from banks
- Securities account also has a big difference where 90% does not have a security account while 10% does
- For CD.Account (Ceritificate deposit) once again we see the 94% does not have it while 6% has it.
- As for online (online banking capability), 40% doe not have it while 60% has it. That distribution is a little more balanced and makes sense.
- As for Credit card 70% does not have it while 30% has it.

```
       ID              Age            Experience       Income          ZIP.Code
 Min.   :   1   Min.   :23.00   Min.   :-3.0   Min.   :  8.00   Min.   : 9307
 1st Qu.:1251   1st Qu.:35.00   1st Qu.:10.0   1st Qu.: 39.00   1st Qu.:91911
 Median :2500   Median :45.00   Median :20.0   Median : 64.00   Median :93437
 Mean   :2500   Mean   :45.34   Mean   :20.1   Mean   : 73.77   Mean   :93152
 3rd Qu.:3750   3rd Qu.:55.00   3rd Qu.:30.0   3rd Qu.: 98.00   3rd Qu.:94608
 Max.   :5000   Max.   :67.00   Max.   :43.0   Max.   :224.00   Max.   :96651
     Family          CCAvg          Education        Mortgage
 Min.   :1.000   Min.   : 0.000   Min.   :1.000   Min.   :  0.0
 1st Qu.:1.000   1st Qu.: 0.700   1st Qu.:1.000   1st Qu.:  0.0
 Median :2.000   Median : 1.500   Median :2.000   Median :  0.0
```

```
 Mean   :2.396   Mean   : 1.938   Mean   :1.881   Mean   : 56.5
 3rd Qu.:3.000   3rd Qu.: 2.500   3rd Qu.:3.000   3rd Qu.:101.0
 Max.   :4.000   Max.   :10.000   Max.   :3.000   Max.   :635.0
 Personal.Loan   Securities.Account   CD.Account         Online
 Min.   :0.000   Min.   :0.0000     Min.   :0.0000   Min.   :0.0000
 1st Qu.:0.000   1st Qu.:0.0000     1st Qu.:0.0000   1st Qu.:0.0000
 Median :0.000   Median :0.0000     Median :0.0000   Median :1.0000
 Mean   :0.096   Mean   :0.1044     Mean   :0.0604   Mean   :0.5968
 3rd Qu.:0.000   3rd Qu.:0.0000     3rd Qu.:0.0000   3rd Qu.:1.0000
 Max.   :1.000   Max.   :1.0000     Max.   :1.0000   Max.   :1.0000
   CreditCard
 Min.   :0.000
 1st Qu.:0.000
 Median :0.000
 Mean   :0.294
 3rd Qu.:1.000
 Max.   :1.000
```

Looking into questions obtained in the statistical analysis

- ***Looking at the entries with negative experience***
- The 52 people with negative total experience are between 23 to 29 years old and salary median of 65,000. Sound like these could just young people that just started working. We can change their negative values to 1 since they have an income, thus are are working.

```
     Age            Income       Personal.Loan
 Min.   :23.00   Min.   : 12.00   Min.   :0
 1st Qu.:24.00   1st Qu.: 40.75   1st Qu.:0
 Median :24.00   Median : 65.50   Median :0
 Mean   :24.52   Mean   : 69.94   Mean   :0
 3rd Qu.:25.00   3rd Qu.: 86.75   3rd Qu.:0
 Max.   :29.00   Max.   :150.00   Max.   :0
```

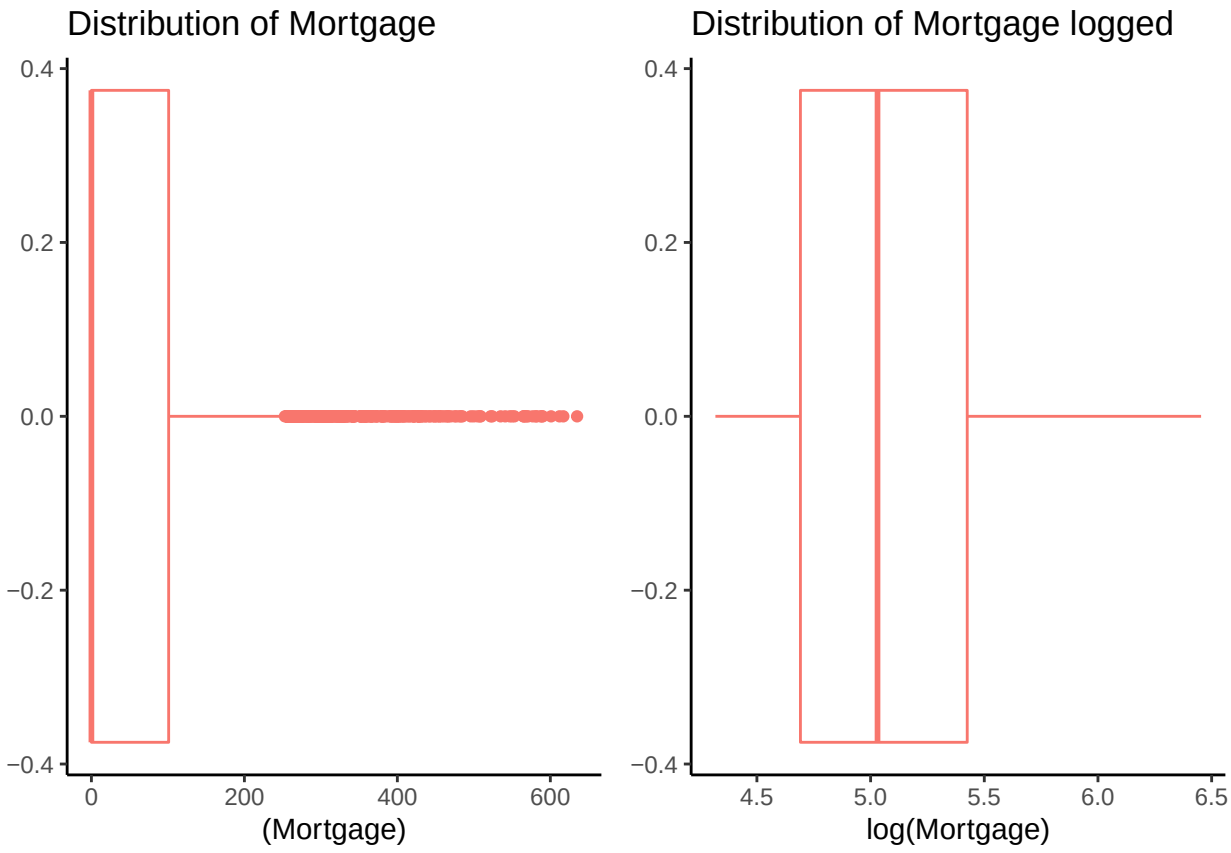
- Setting categories as factors
- Creating a new variable called Exprience 2 due to Age and experience having a correlation of 97%. That way we can get rid of Age and Experience

```
PersonalLoan

 11  Variables      5000  Observations
--------------------------------------------------------------------------------
Income
       n  missing distinct     Info     Mean      Gmd      .05      .10
    5000        0      162        1    73.77    50.91       18       22
     .25      .50      .75      .90      .95
      39       64       98      145      170

lowest :   8   9  10  11  12, highest: 203 204 205 218 224
--------------------------------------------------------------------------------
Family
       n  missing distinct
    5000        0        4
```

```
Value          1     2     3     4
Frequency   1472  1296  1010  1222
Proportion 0.294 0.259 0.202 0.244
---------------------------------------------------------------------------
CCAvg
       n  missing distinct     Info     Mean      Gmd      .05      .10
    5000        0      108    0.999    1.938    1.794      0.1      0.3
     .25      .50      .75      .90      .95
     0.7      1.5      2.5      4.3      6.0

lowest :  0.0  0.1  0.2  0.3  0.4, highest:  8.8  8.9  9.0  9.3 10.0
---------------------------------------------------------------------------
Education
       n  missing distinct
    5000        0        3

Value          1     2     3
Frequency   2096  1403  1501
Proportion 0.419 0.281 0.300
---------------------------------------------------------------------------
Mortgage
       n  missing distinct     Info     Mean      Gmd      .05      .10
    5000        0      347    0.668     56.5    88.16        0        0
     .25      .50      .75      .90      .95
       0        0      101      200      272

lowest :   0  75  76  77  78, highest: 590 601 612 617 635
---------------------------------------------------------------------------
Personal.Loan
       n  missing distinct
    5000        0        2

Value         No   Yes
Frequency   4520   480
Proportion 0.904 0.096
---------------------------------------------------------------------------
Securities.Account
       n  missing distinct
    5000        0        2

Value          0     1
Frequency   4478   522
Proportion 0.896 0.104
---------------------------------------------------------------------------
CD.Account
       n  missing distinct
    5000        0        2

Value         0    1
Frequency  4698  302
Proportion 0.94 0.06
---------------------------------------------------------------------------
Online
       n  missing distinct
```

```
    5000        0        2

Value          0     1
Frequency   2016  2984
Proportion 0.403 0.597
--------------------------------------------------------------------------------
CreditCard
       n  missing distinct
    5000        0        2

Value          0     1
Frequency   3530  1470
Proportion 0.706 0.294
--------------------------------------------------------------------------------
Experience2
       n  missing distinct     Info     Mean      Gmd      .05      .10
    5000        0      178        1    0.404   0.1848  0.07678  0.14286
     .25      .50      .75      .90      .95
 0.28571  0.44444  0.53846  0.58730  0.60317

lowest : 0.00000000 0.03225806 0.03448276 0.03571429 0.03703704
highest: 0.62500000 0.62686567 0.63076923 0.63636364 0.64179104
--------------------------------------------------------------------------------
```

- ***Checking mortgage distribution***
- Mortgage may need to be logged as it is very skewed.

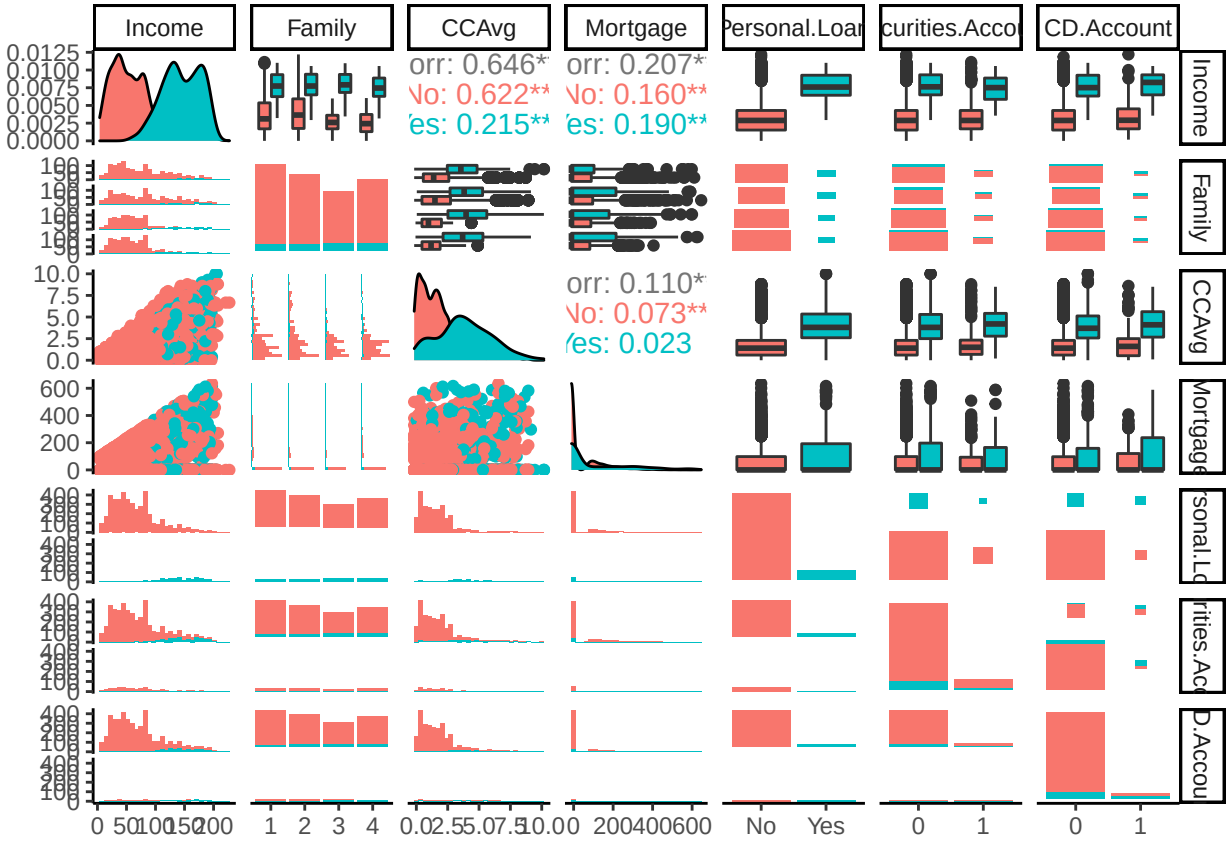


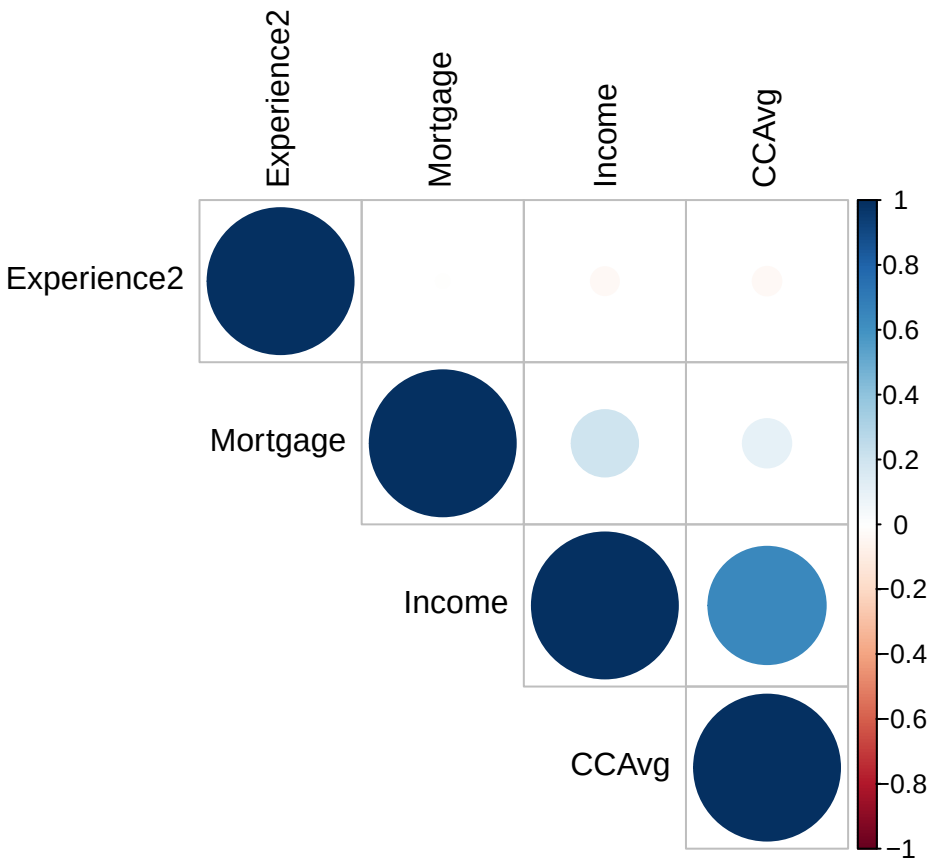
- Creating another data set with Mortgage logged since logging did improve the distribution. The zero's were replaced to with 1 in order to not get infitiy when logging. Also, removing age since it has a 99% correlation with Experience, therefore only one is needed

```
#Creating a new data set with the modified attributes
PersonalLoan2=mutate(PersonalLoan)
#Updating values
PersonalLoan2$Mortgage[PersonalLoan2$Mortgage==0]=1
PersonalLoan2$MortgageLogged=log(PersonalLoan2$Mortgage)
#PersonalLoan2=PersonalLoan2 %>% select(-Mortgage)
```

Relationships and correlations

- Experience and Age has a Correlation of 99%.Too high. However, they seem to have no relationship with Loan as both; yes loan and no loan, have the same correlation with experience and age of 0.99
- CCAvg and Income has a 64% correlations and it does seems to have a relationship with Loan since there is 0.62 with no loan and .02 with yes loan.
- The rest of the explanatory variables do not seem to have relationship between each other





Checking realtionship between Loan (response variable) and the rest of the predictors

Very high Relationship present

- ***Income***, the more income the more changes to get a loan
- ***Mortgage***, people high mortgages seem to ask for loans more so than those with lower mortgages

Relationship present

- ***CD.Account*** (certificate of deposit) seem to have a relationship with Personal Loan. Those with personal loan tend to have CD.Account more so than those with no CD.Account
- ***Personal education***, people with up to highschool tend do not get loans as much as does with an education of higher than highschool
- `!!**there seems to be relationship with loan and education but that of education 2 and 3 seem to be`

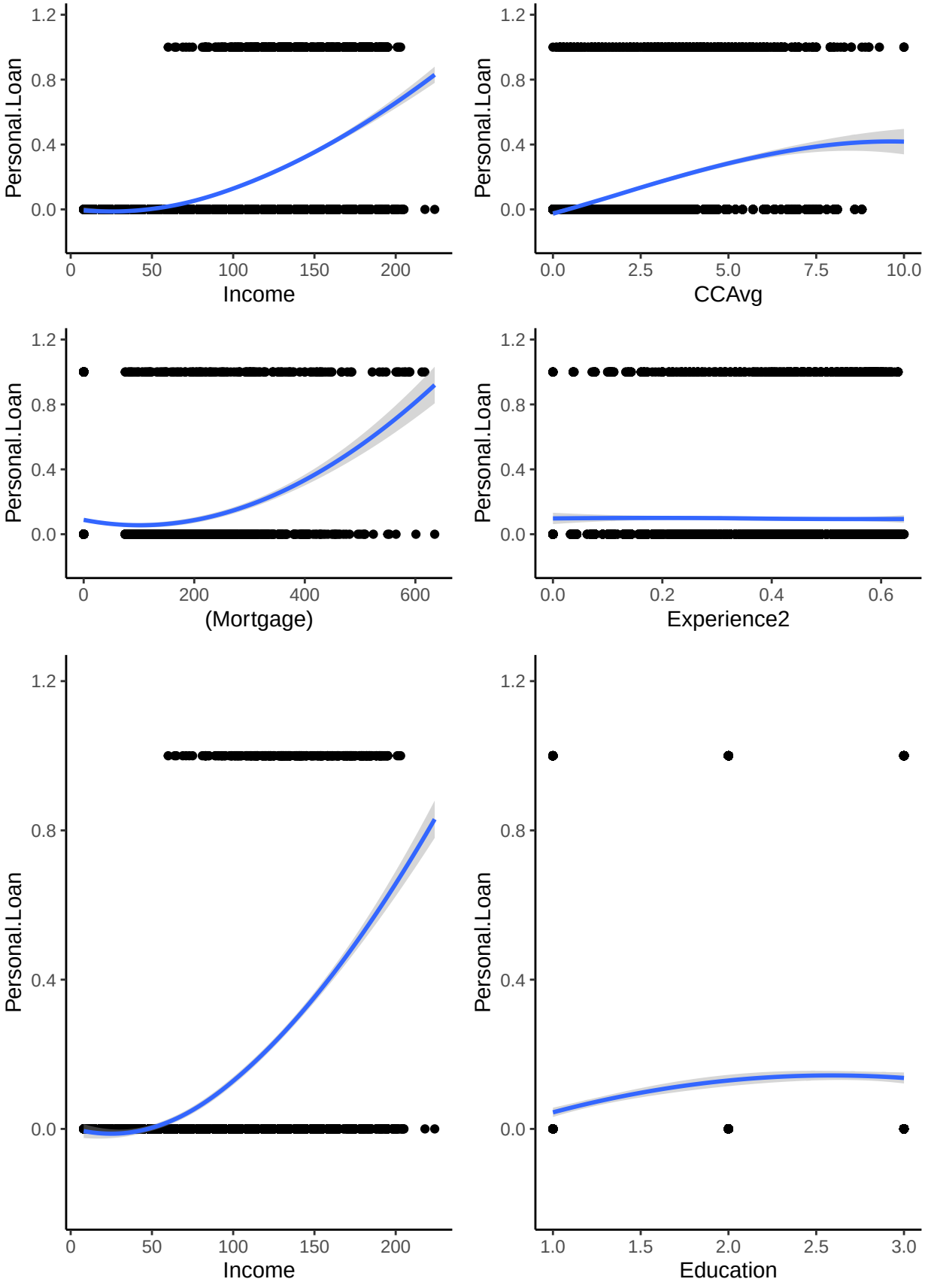
Very small relationship

- ***Security account*** and Personal Loan seem to have slight relationship

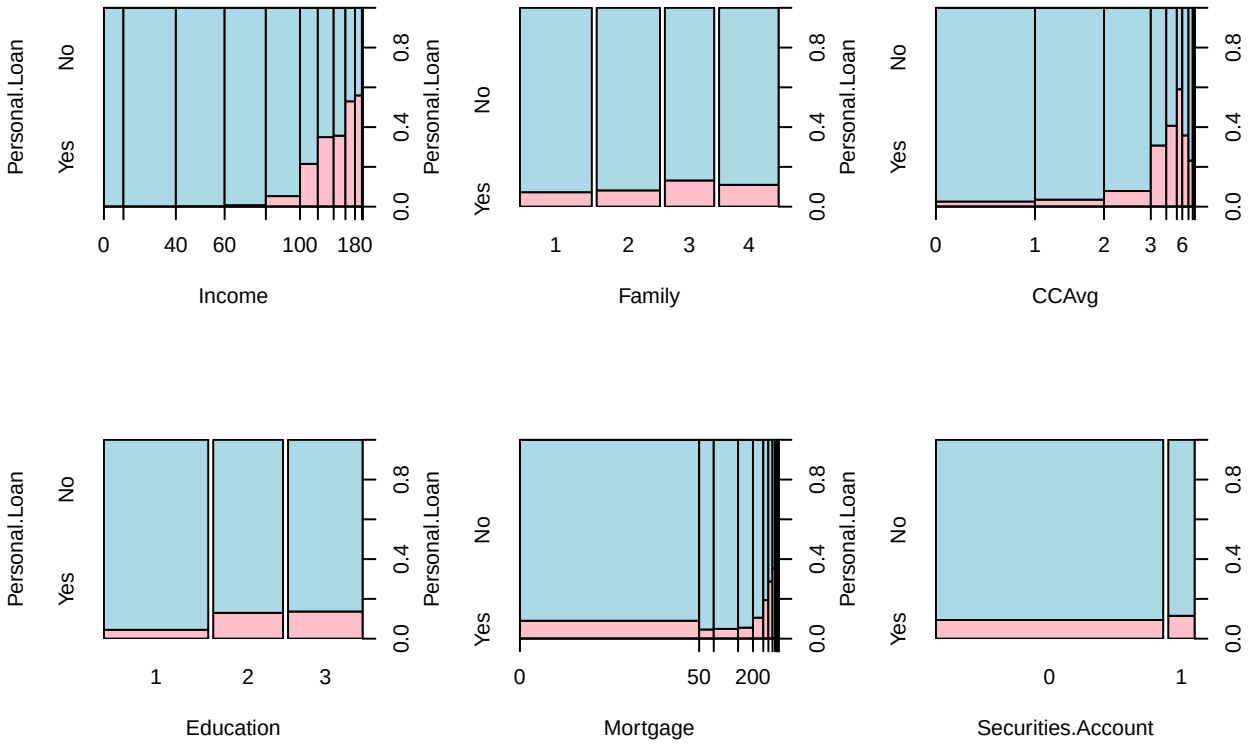
No relationship with response

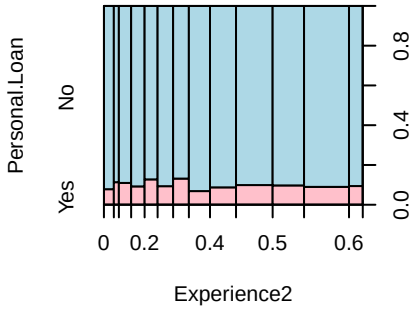
- ***Online and Credit card*** don't seem to have a relationship

Looking closer at each realationship to see if anything was missed



- More detailed graph on each variable with response





Model: Objective 1

```
# Train Test Split
set.seed(123)
index<-sample(1:dim(PersonalLoan)[1],round(.70 * dim(PersonalLoan)[1]))
train<-PersonalLoan[index,]
test<-PersonalLoan[-index,]


# Split Predict for lasso
dat.test.x = model.matrix(Personal.Loan ~ Income + Family + CCAvg-1 + Education + Securities.Account-1 +

dat.train.x = model.matrix(Personal.Loan ~ Income + Family + CCAvg-1 + Education + Securities.Account-1
dat.train.y = train$Personal.Loan
```

Performing model with all variables, some feature selection methods (forward, stepwise, LASSO) and another based on EDA + With the full model with all attributes it showed that the only important were Income, Family,CCavg, Education,Securites.Account, CD.Account, Online, CreditCard

- Once Stepwise was added to the full model it selected all of those that appeared as significant in the full model:Income, Family, CCAvg, Education, Securities.Account, CD.Account, Online, CreditCard. It also selected Experience2 but that one was not significant as we had seen in the EDA.

- When the forward model was added to the full model it selected the same thing as stepwise but included CCAVG which was significant and Mortgage which was not significant .
- As for LASSO it selected all of the attributes by Stepwise and included CCAvg.

```
Call:
glm(formula = Personal.Loan ~ ., family = "binomial", data = train)

Deviance Residuals:
    Min       1Q   Median       3Q      Max
-2.8582  -0.1818  -0.0647  -0.0193   4.1124

Coefficients:
                      Estimate  Std. Error z value             Pr(>|z|)
(Intercept)         -12.5251518   0.7051046 -17.764 < 0.0000000000000002 ***
Income                0.0632191   0.0037351  16.926 < 0.0000000000000002 ***
Family2              -0.2376211   0.2832713  -0.839             0.401556
Family3               1.9082393   0.2950650   6.467      0.0000000000998 ***
Family4               1.3733143   0.2907382   4.724      0.0000023177032 ***
CCAvg                 0.1330478   0.0558477   2.382             0.017203 *
Education2            4.0306143   0.3351091  12.028 < 0.0000000000000002 ***
Education3            4.1978282   0.3350516  12.529 < 0.0000000000000002 ***
Mortgage              0.0009203   0.0007186   1.281             0.200303
Securities.Account1  -0.7246928   0.3493892  -2.074             0.038063 *
CD.Account1           3.5261823   0.4039920   8.728 < 0.0000000000000002 ***
Online1              -0.8210820   0.2024400  -4.056      0.0000499357901 ***
CreditCard1          -0.8793800   0.2592112  -3.393             0.000693 ***
Experience2          -0.0876285   0.5689759  -0.154             0.877601
---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

(Dispersion parameter for binomial family taken to be 1)

    Null deviance: 2163.7  on 3499  degrees of freedom
Residual deviance:  792.4  on 3486  degrees of freedom
AIC: 820.4

Number of Fisher Scoring iterations: 8


[1] 0.0009615423
```

- Using different threholds

Changing the threshold

```
[1] "All_Attributes"


[1] "Threashhold | Accuracy| Sensitivity| Specificy"


$`0.3`
[1] 0.3000000 0.9566667 0.9747212 0.8000000
```

```
$`0.5`
[1] 0.5000000 0.9620000 0.9947955 0.6774194

$`0.7`
[1] 0.7000000 0.9553333 0.9992565 0.5741935

[1] "--------------------------------"

[1] "StepWiseAIC"

[1] "Threashhold | Accuracy| Sensitivity| Specificy"

$`0.3`
[1] 0.3000000 0.9573333 0.9747212 0.8064516

$`0.5`
[1] 0.5000000 0.9620000 0.9947955 0.6774194

$`0.7`
[1] 0.7000000 0.9553333 0.9992565 0.5741935

[1] "--------------------------------"

[1] "Threashhold | Accuracy| Sensitivity| Specificy"

[1] "ForwardModel"

$`0.3`
[1] 0.3000000 0.9566667 0.9747212 0.8000000

$`0.5`
[1] 0.5000000 0.9620000 0.9947955 0.6774194

$`0.7`
[1] 0.7000000 0.9553333 0.9992565 0.5741935

[1] "--------------------------------"

[1] "Threashhold | Accuracy| Sensitivity| Specificy"

[1] "LASSO"

$`0.3`
[1] 0.3000000 0.9560000 0.9747212 0.7935484

$`0.5`
[1] 0.5000000 0.9613333 0.9955390 0.6645161

$`0.7`
[1] 0.7000000 0.9553333 1.0000000 0.5677419
```

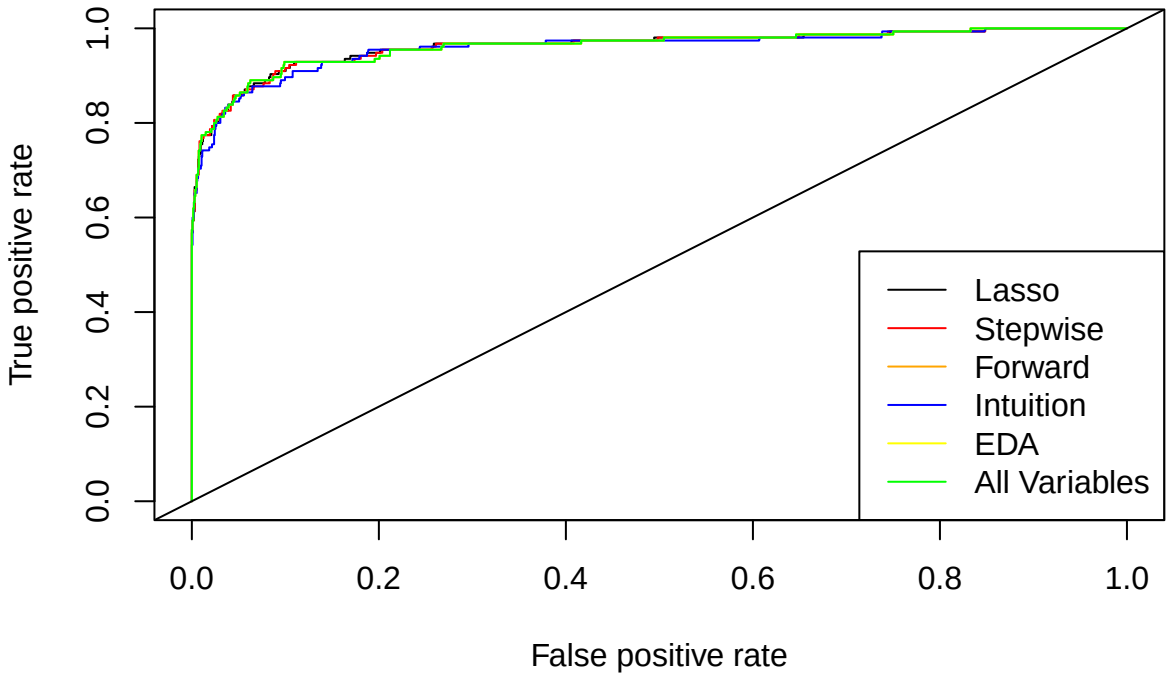
```
[1] "--------------------------------"

[1] "Intuition"

[1] "Threashhold | Accuracy| Sensitivity| Specificy"

$`0.3`
[1] 0.3000000 0.9553333 0.9762082 0.7741935

$`0.5`
[1] 0.5000000 0.9593333 0.9947955 0.6516129

$`0.7`
[1] 0.7000000 0.9540000 0.9992565 0.5612903

[1] "--------------------------------"

[1] "EDA"

[1] "Threashhold | Accuracy| Sensitivity| Specificy"

$`0.3`
[1] 0.3000000 0.9533333 0.9739777 0.7741935

$`0.5`
[1] 0.5000000 0.9600000 0.9955390 0.6516129

$`0.7`
[1] 0.7000000 0.9553333 0.9992565 0.5741935
```

Choosing 0.3 threshold based of the threashold results. Criterion Comparison of all models

```
all_results
```

```
    Criterion Full_Model Step_Wise Forward_Model LASSO_model Intuition     EDA
1         AIC    820.398   818.074       820.398       0.000   836.879 844.481
2         BIC    906.645   892.000       906.645       0.000   892.324 899.926
3    Accuracy      0.957     0.957         0.957       0.956     0.955   0.953
4 Sensitivity      0.975     0.975         0.975       0.975     0.976   0.974
5 Specificity      0.800     0.806         0.800       0.794     0.774   0.774
```

The ROC of models



Verify Proportions in test and train manually + Distribution in train and test do represent that of the whole data

```
[1] "All data"
```

```
   No   Yes
0.904 0.096
```

```
[1] "Train"
```

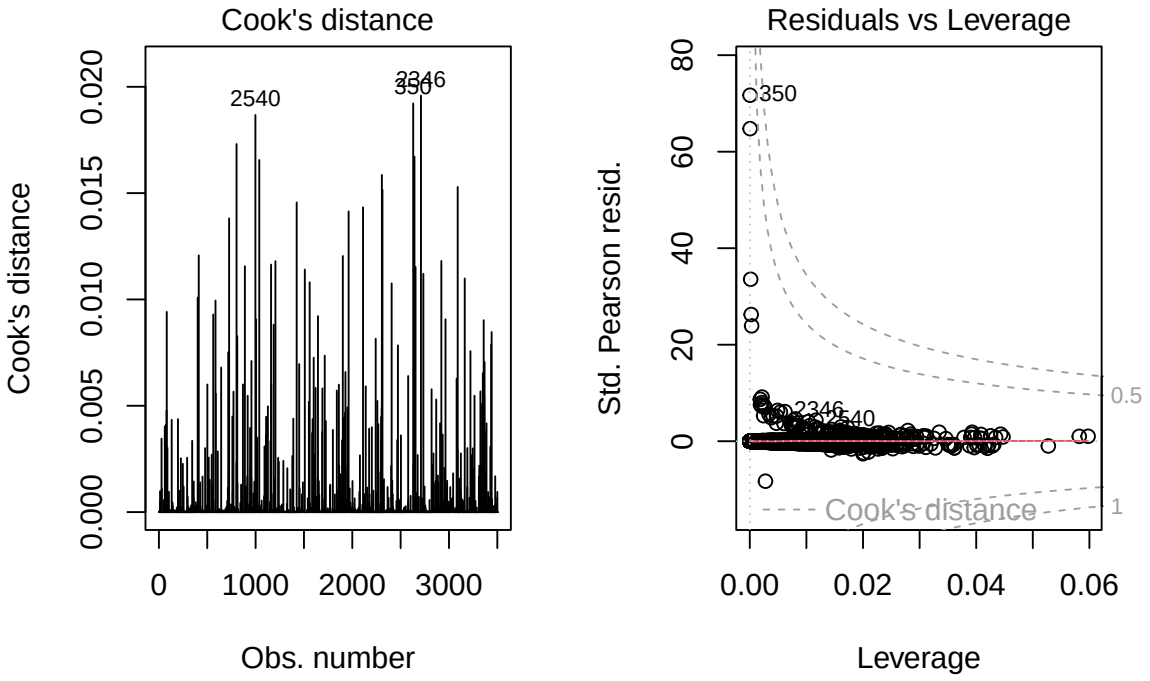
```
        No        Yes
0.90714286 0.09285714
```

```
[1] "Test"
```

```
       No       Yes
0.8966667 0.1033333
```

- Assumptions via PLOTS of selected model, Stepwise and checking VIF

- Plots look normal and there seems to be multicolinarity among variables based on VIF



	GVIF	Df	GVIF^(1/(2*Df))
Income	2.940809	1	1.714879
Family	1.529409	3	1.073381
CCAvg	1.516750	1	1.231564
Education	2.323075	2	1.234570
Securities.Account	1.291648	1	1.136507
CD.Account	1.936714	1	1.391659
Online	1.143566	1	1.069376
CreditCard	1.383602	1	1.176266

Conclusion from Part 1

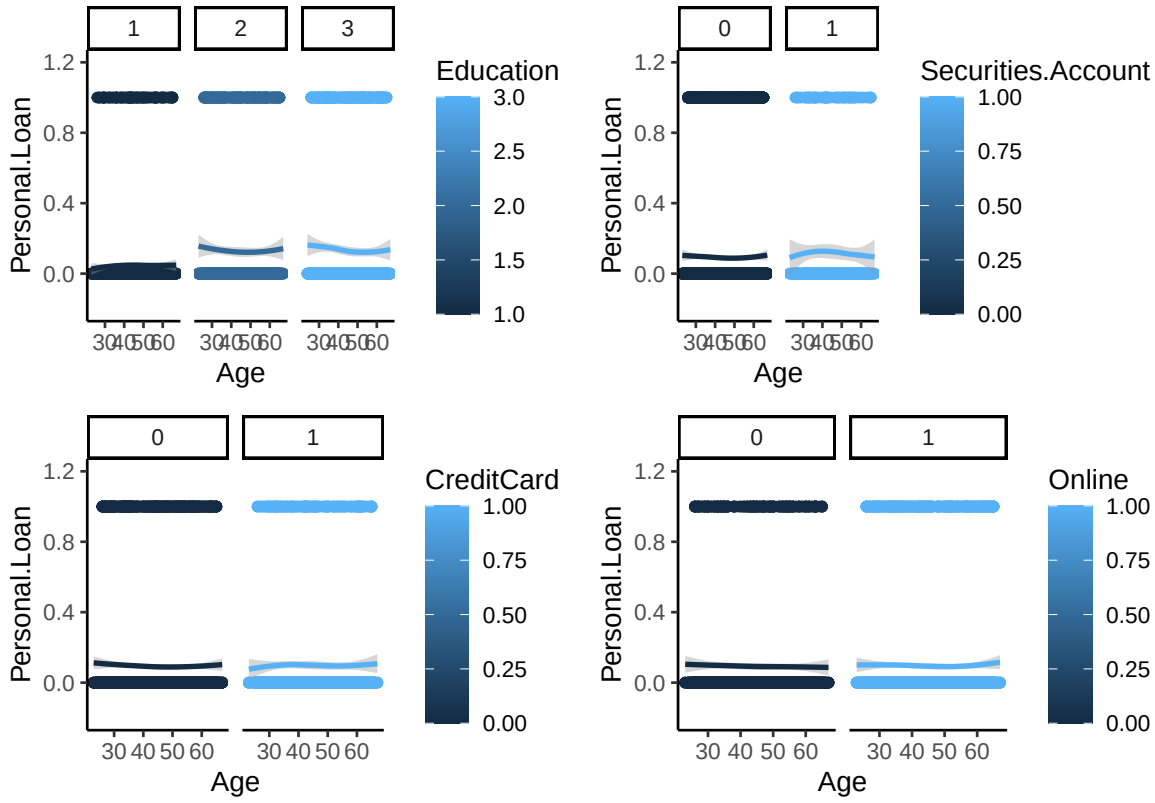
- The best model was step setting the threshold to 0.3 it gave an sensitivity of 94 and specificity of 72
- Due to the imbalance of amount of people with loan and without loan we do see we do see that the model favors no loan due to it but 72 compared to the 55 specificity was a great increase. This model is about trying to predict those who will say yes to Loan therefore Specificity is important.
- The attributes found useful were : Income, Family,CCavg, Education,Securites.Account, CD.Account, Online, CreditCard
- The threshold was set to 0.3 and it lead to a Sensitivity of 0.96 and specificy of 0.71
- These were variables seen in the EDA as related to the loan.
- Coefficients results: For every unit increase in income the odd of getting a loan are e^1.06 times higher For every unit increase in Family the odd of getting a loan are e^0.698209 times higher For every unit increase in CCAvg the odd of getting a loan are e^0.120635 times higher For every unit increase in Education the odd of getting a loan are e^1.713690 times higher For every unit increase in

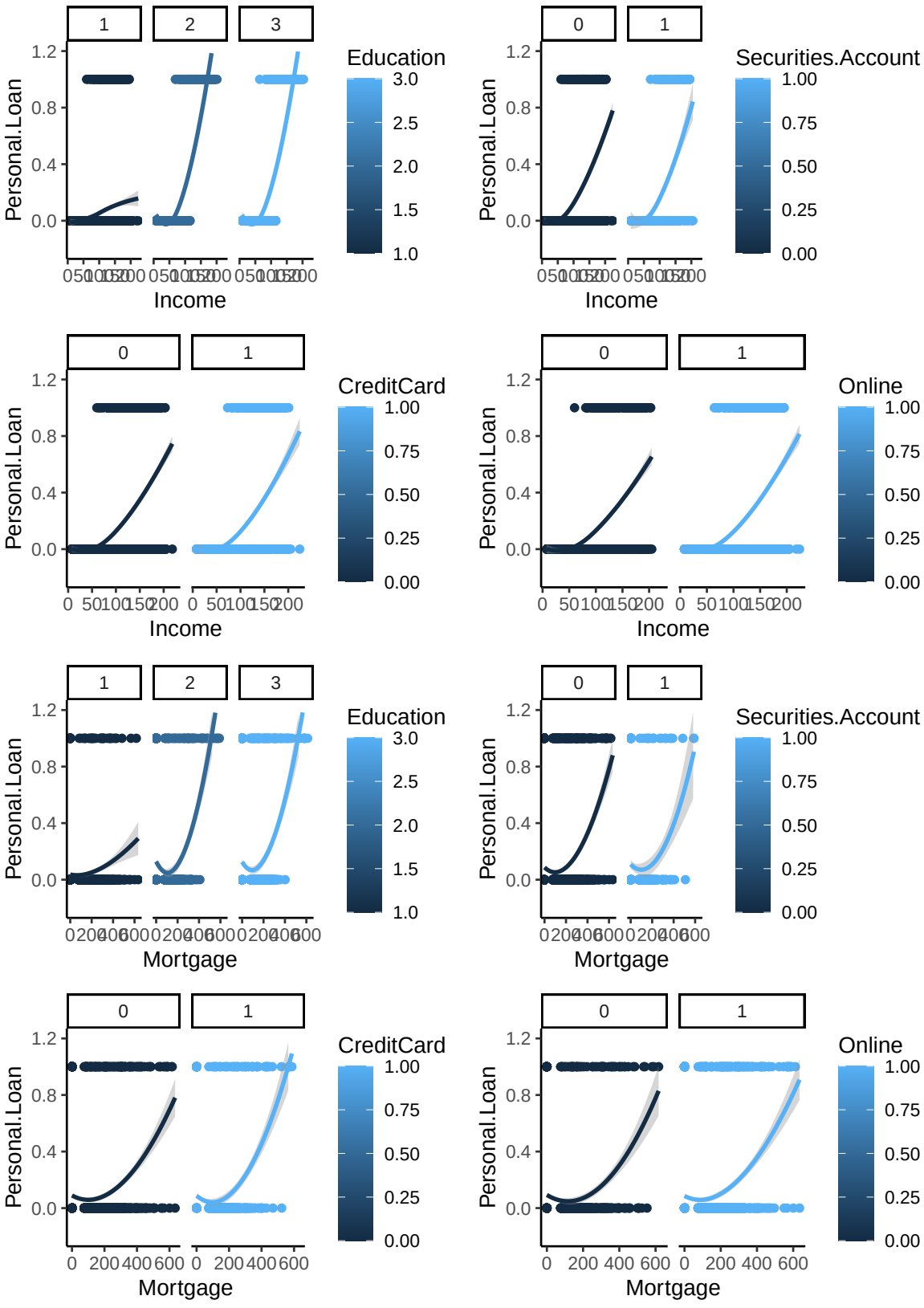
Securities.Account 1 the odd of getting a loan are e^-0.937183 times less likely For every unit increase in CD.Account1 the odd of getting a loan are e^3.840892 times higher For every unit increase in Online1 the odd of getting a loan are e^-0.673230 times less likely For every unit increase in CreditCard1 the odd of getting a loan are e^ -1.122701 times higher

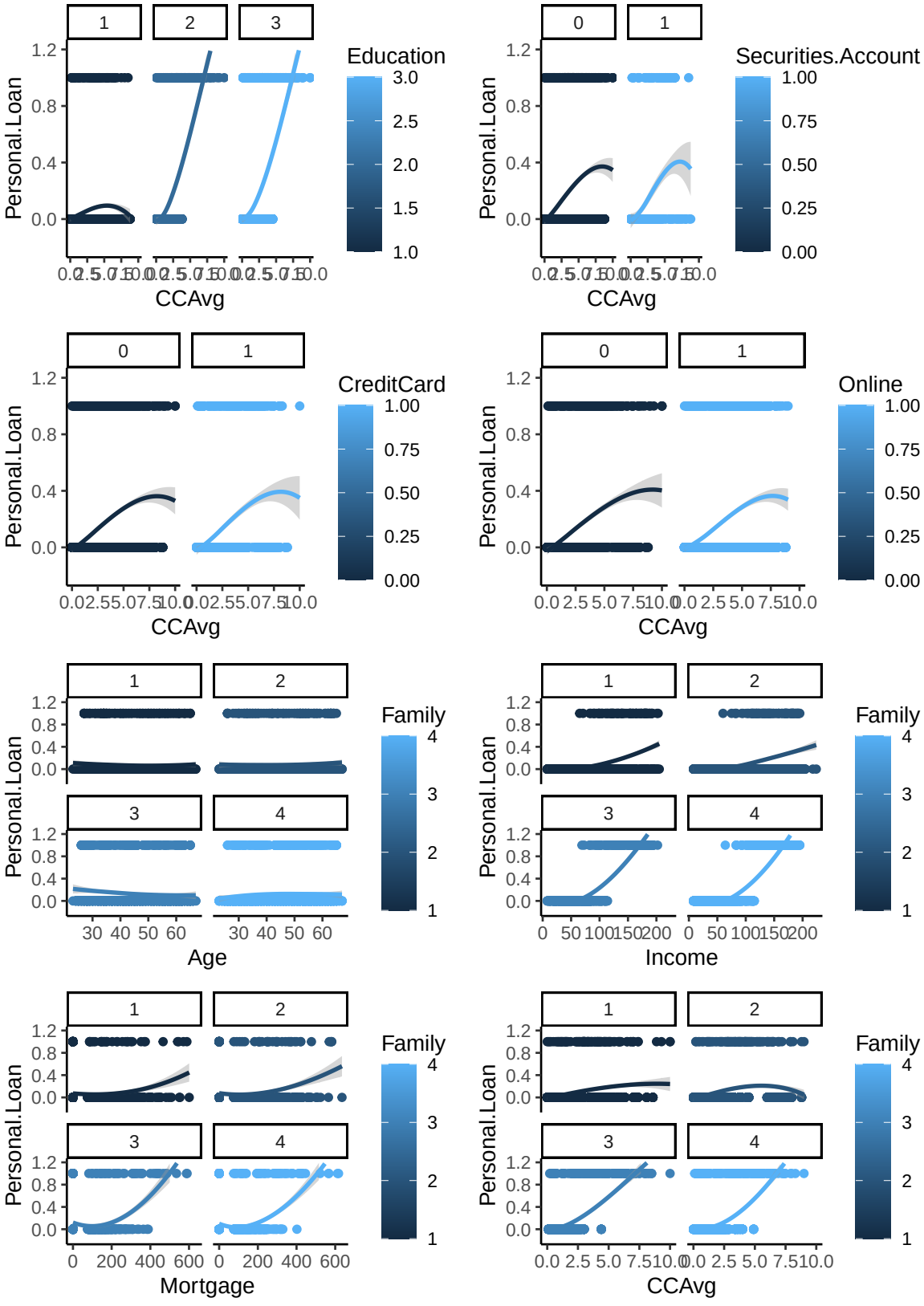
##

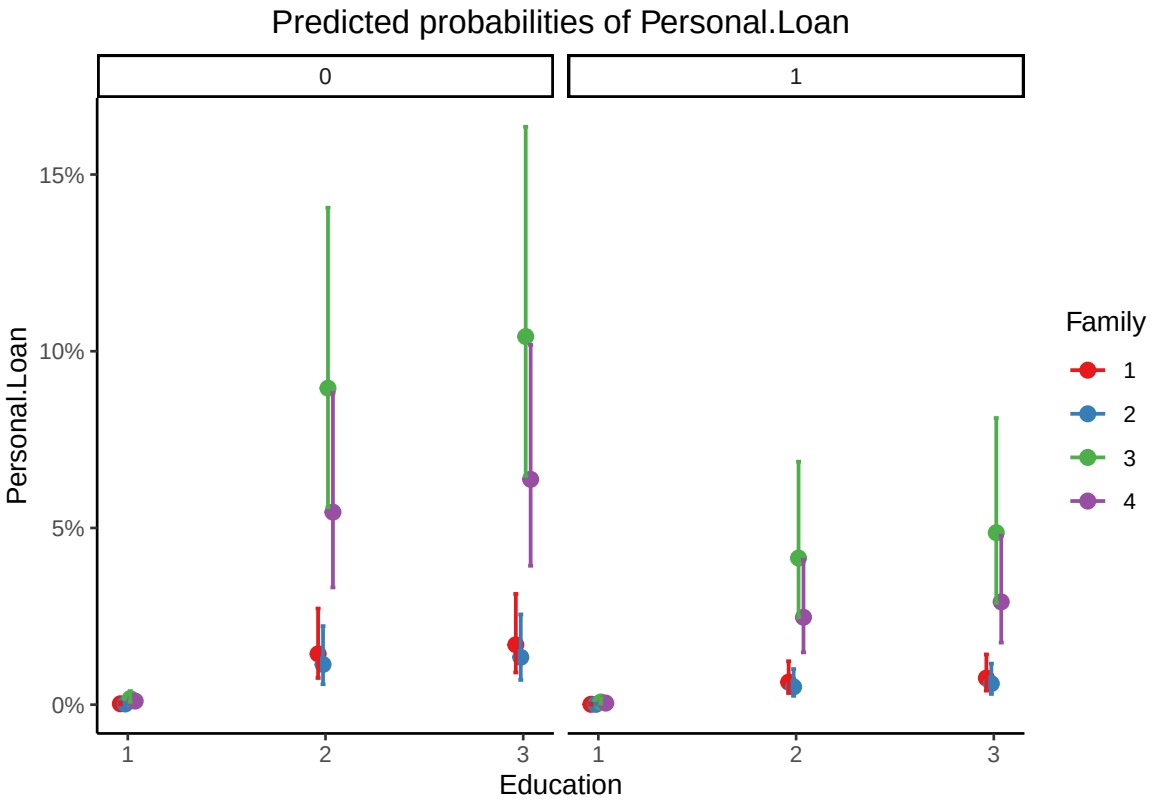
MODEL: Part 2

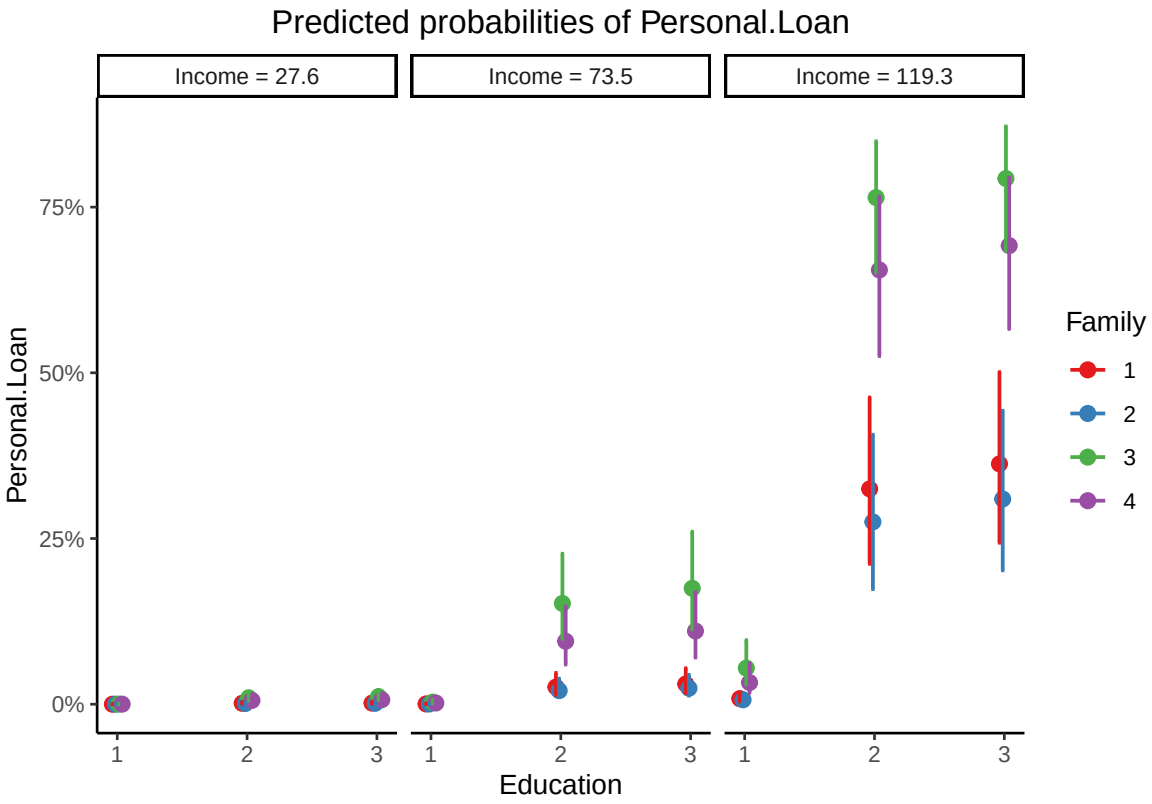
- Checking graphs for interactions
- Across all of the plots only one age with mortgage showed to maybe have an interaction
-

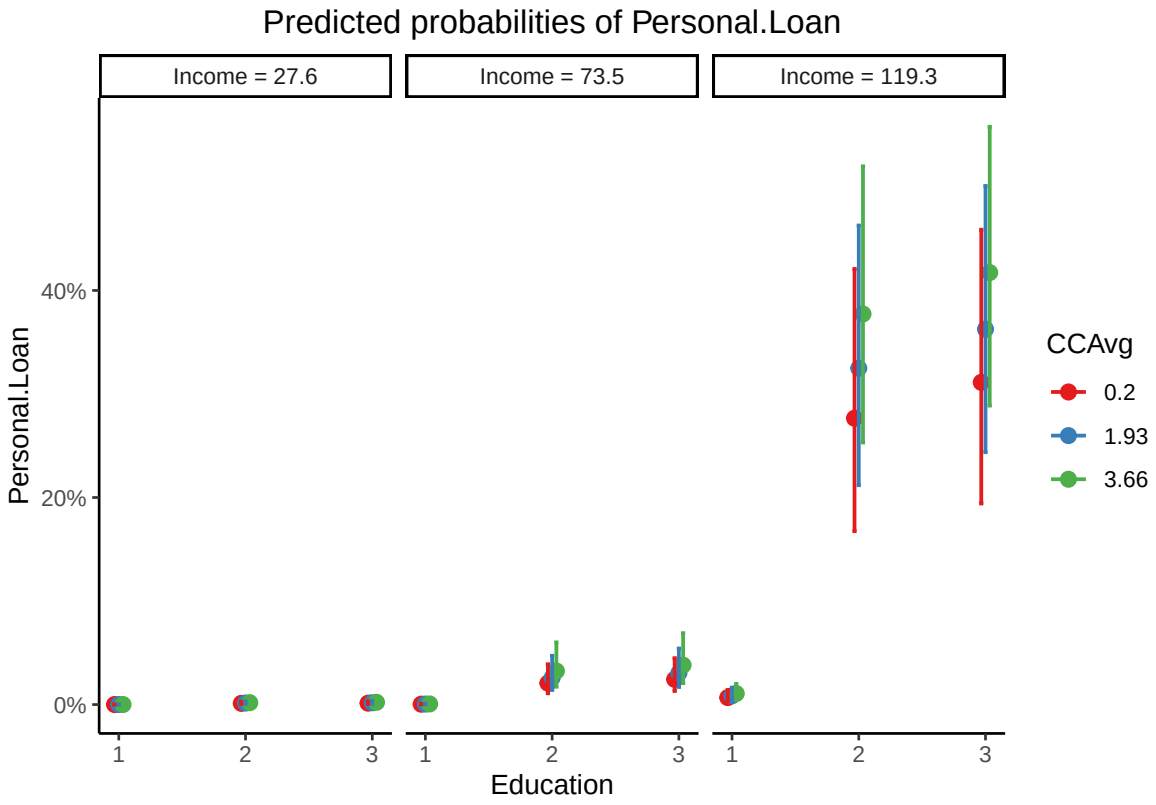



1
2
3
Education
3.0
2.5
2.0
1.5
1.0
0
1
Securities.Account
1.00
0.75
0.50
0.25
0.00
CreditCard
Online
Personal.Loan
1.2
0.8
0.4
0.0
0
50
100
150
200
Income
0
200
400
600
Mortgage


1
2
3
Education
3.0
2.5
2.0
1.5
1.0
0
1
Securities.Account
1.00
0.75
0.50
0.25
0.00
CreditCard
Online
Family
4
3
2
1
Personal.Loan
1.2
0.8
0.4
0.0
CCAvg
Age
Income
Mortgage
0.0 2.5 5.0 7.5 10.0
30 40 50 60
0 50 100 150 200
0 200 400 600


Predicted probabilities of Personal.Loan
0
1
15%
10%
5%
0%
Personal.Loan
1
2
3
Education
Family
1
2
3
4


Predicted probabilities of Personal.Loan
Income = 27.6
Income = 73.5
Income = 119.3
75%
50%
25%
0%
Personal.Loan
1
2
3
Education
Family
1
2
3
4



- **Running the models**
- In part 1 we saw that, Income, Family, CCAvg, CD.Account, Education and Credit Card were significant, therefore we leverage those varibles and kept mortgage (just like in part 1) based on the EDA analysis, for Part 2

Interaction

- All variables:Income, Family, CCAvg, CD.Account, Education, and Credit Card and the in the interaction of family and mortgage were significant.
- When passing the model model through stepwise and forward it kept the all variables including the interaction and thus kept the same significant variables showing signs that the interaction is indeed useful.
- When Anova was applied, it did show the interaction as significant
- The Hoslem test however showed that the model was a poor fit, yes again this is not reliable due to the size of the data (This I asked in class and Dr.Turner said we couldn't relly on this metric with big data)

Logged + We logged morgage + All variables were significant: Income, Family, CCAvg, CD.Account, Education, and Credit Card including the log mortgage and log income + Once the models were mixed, having logged income and the interaction of logged mortgage with family lead to the interaction no longer being significant however all other variable remained significant.

Polynomials + When income was set to poly 2 all variables were significant + The income was set to 3 polys, the first poly income was significant but the rest were no longer significant. However, the rest of the variables are still significant + CCAvg set to poly2 showed all variables as significant just like poly 3 + when setting both CCavg and income to poly 2 all variables showed importance however when setting both CCAvg and income to poly 3, income ^2 and income^3 did not show significance in the model while all

the rest of the attributes did show significance. + Interesting when MortagaLogged or mortgage was added it reduced the specificity and sensitivity + Therefore the attributes used where income, Family, CCAvg, CD.Account, Education, Credit Card . we brought up Securites.Account agian as well as online since we had seem that they had importance in some models and EDA. Of course the difference within the models was having Incompo Poly or CCAvg or both to ^2 and ^3 polynomial.

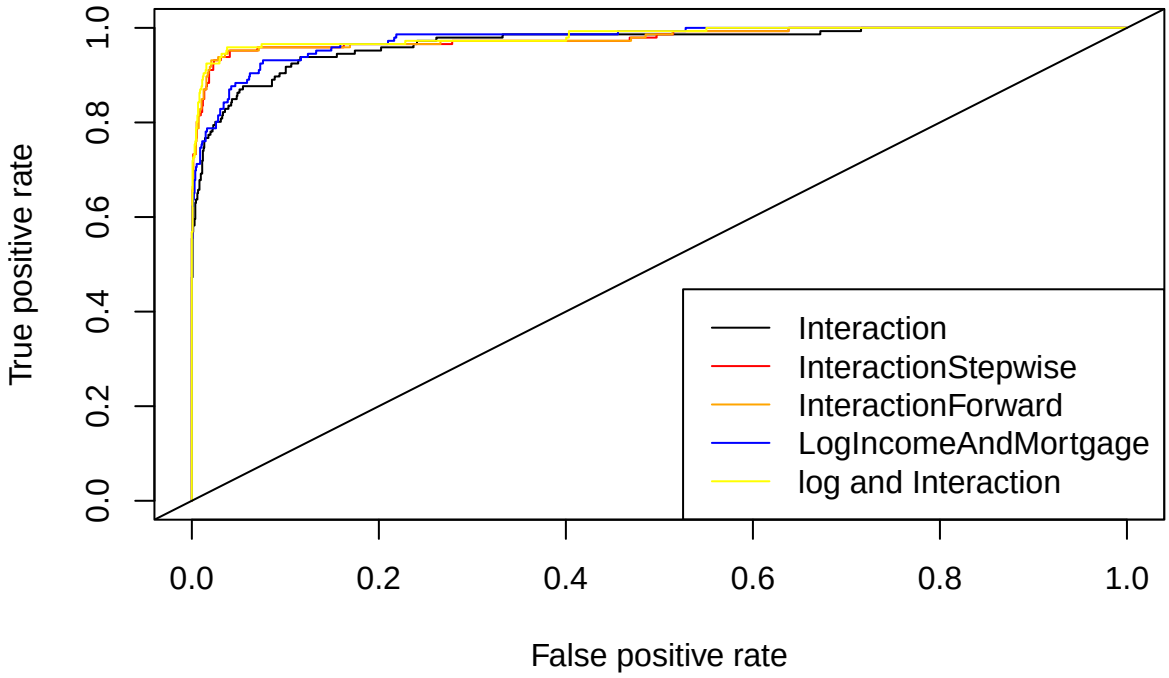
LDA and QDA + LDA mode and QDA model did poorly however between the two, LDA model out performed QDA. This makes sense since the groups have a clear division of who gets loans and who doesn't which would be LDA. + Also this is a non parametric test therefore we can also explain why it did not do as good as the logisti regression models

```
Personal.Loan ~ Securities.Account + CD.Account + CreditCard +
    Education + Income + CCAvg + Family * Mortgage
```

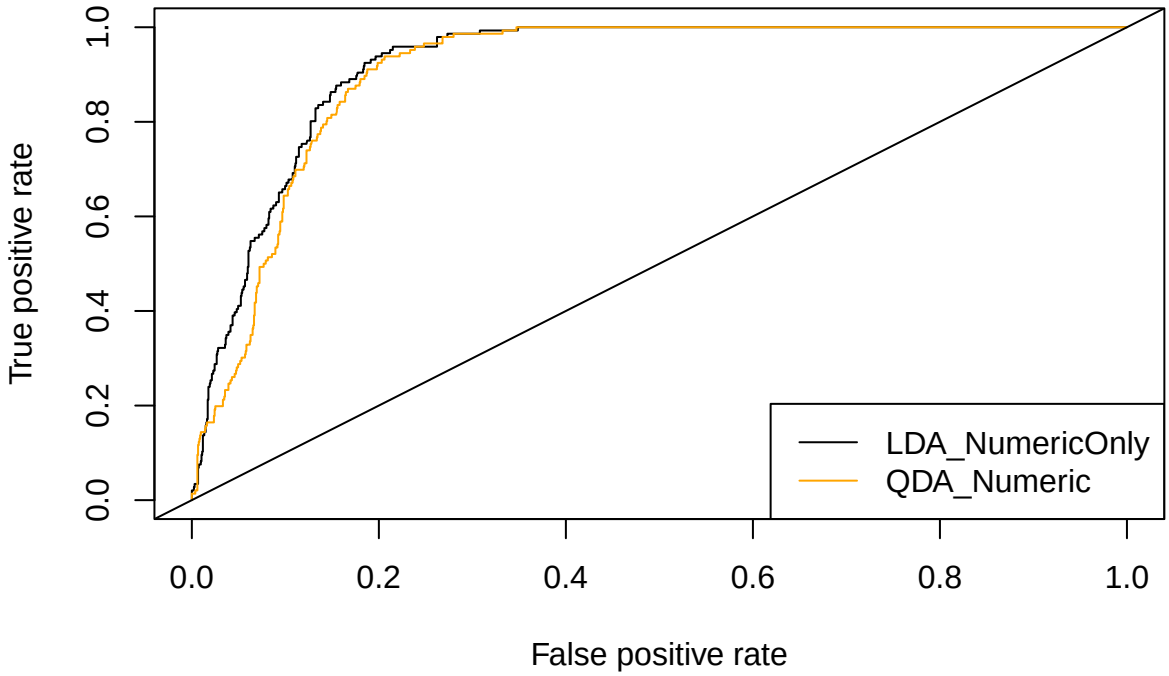
	Criterion	AllInteractions	LogIncomeMortgage	LogAndInteraction
1	AIC	628.246	771.857	620.167
2	BIC	751.456	845.784	786.501
3	Accuracy	0.974	0.955	0.977
4	Sensitivity	0.984	0.972	0.985
5	Specificity	0.877	0.801	0.904

The ROC of models

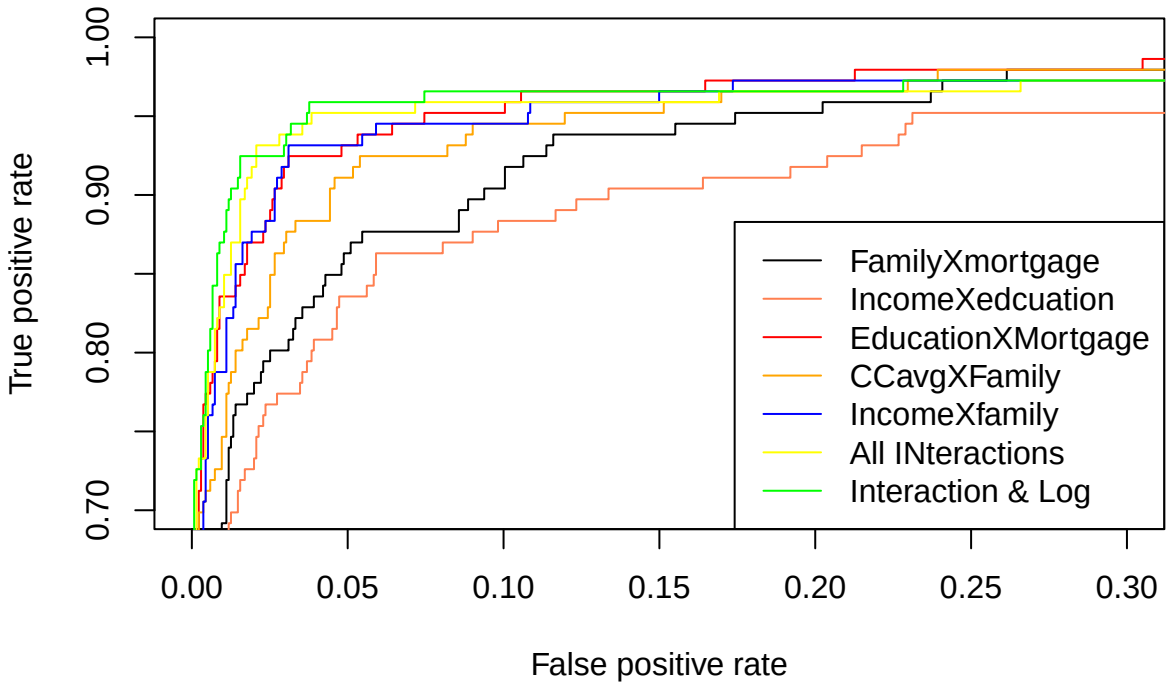
- ***Interaction models***



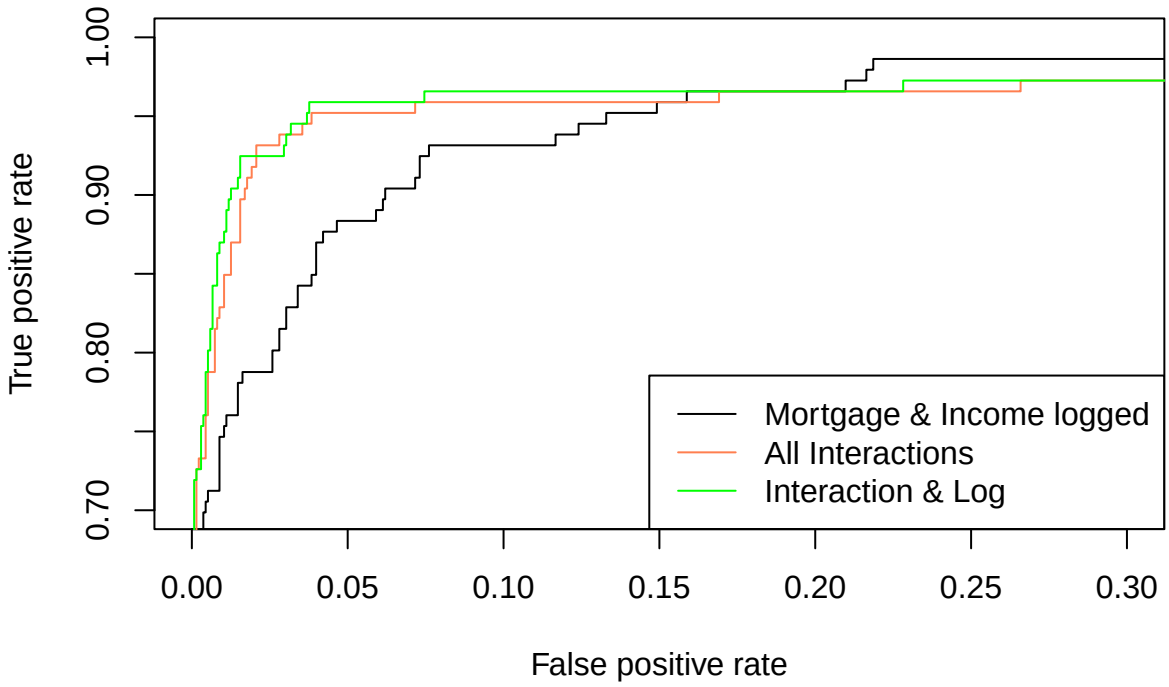
- ***LDA & QDA***

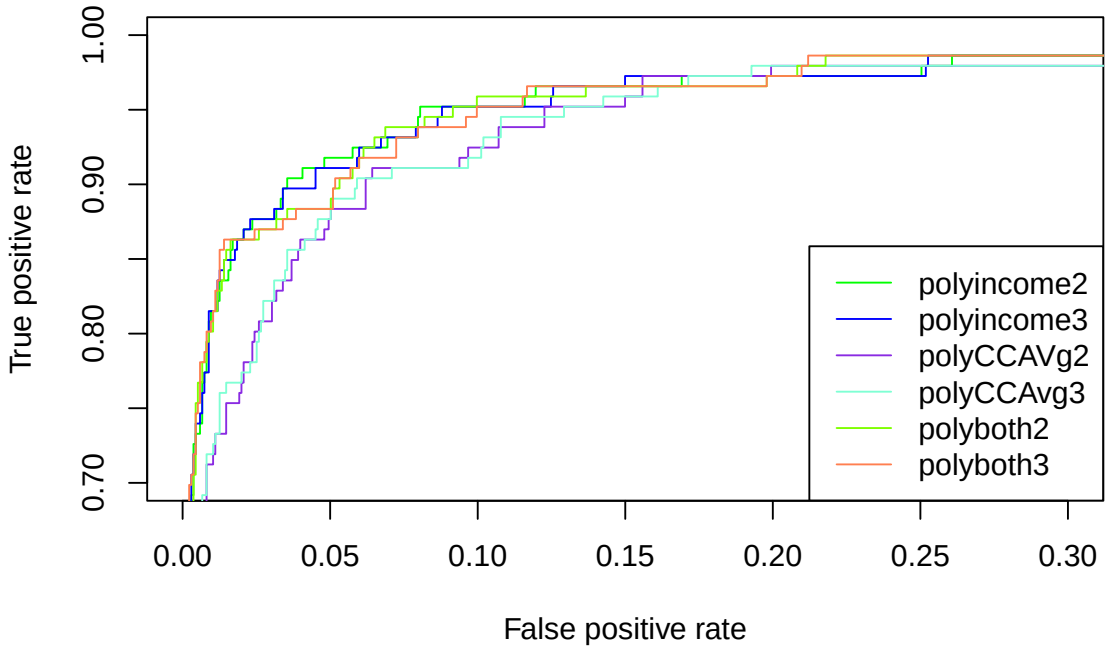


- ***Best of logs and interactions***



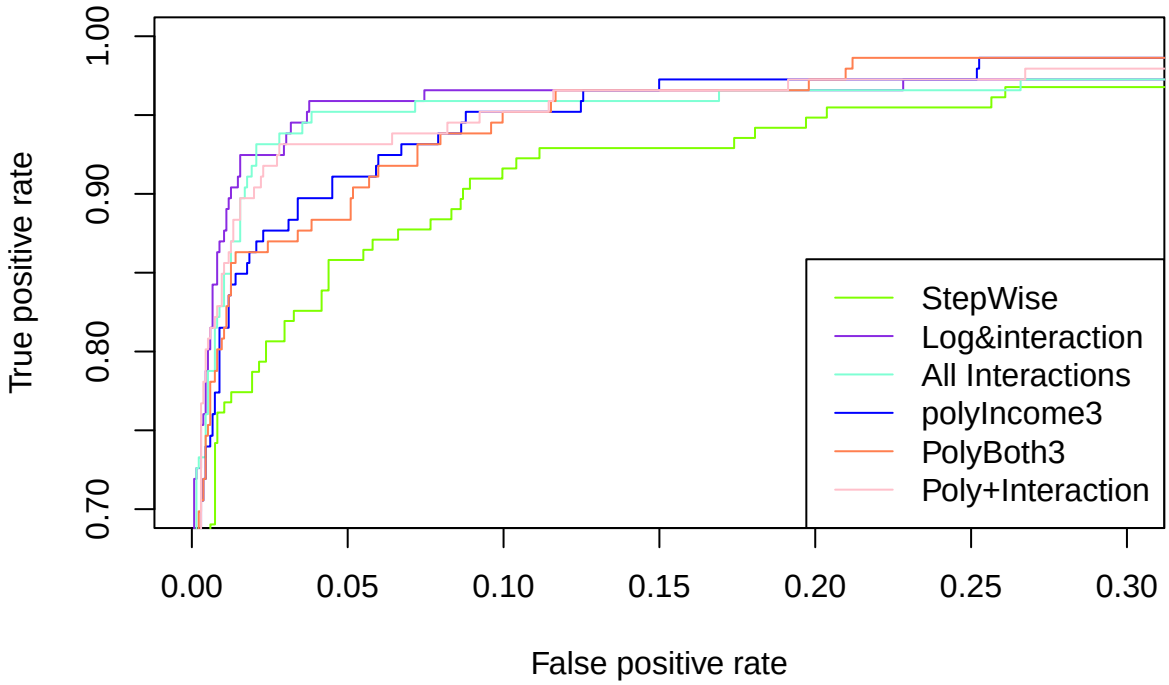
+ ***Lets get closer look at all the log and interaction , interaction with log and logging alone***


True positive rate
1.00
0.90
0.80
0.70
0.00
0.05
0.10
0.15
0.20
0.25
0.30
False positive rate
Mortgage & Income logged
All Interactions
Interaction & Log

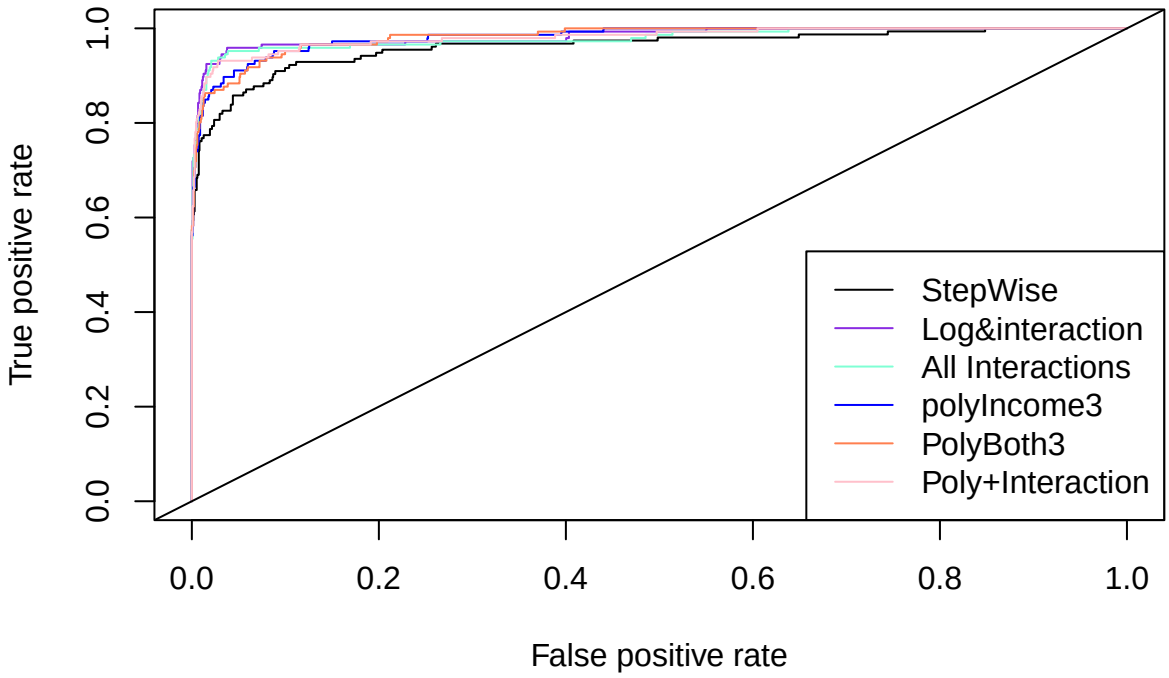

True positive rate
1.00
0.90
0.80
0.70
0.00
0.05
0.10
0.15
0.20
0.25
0.30
False positive rate
polyincome2
polyincome3
polyCCAVg2
polyCCAvg3
polyboth2
polyboth3

- ***Poly models***

- ***The best model from the first part vs the best models of the second set***




```
[1] "Closer view"
```



Criterion of best models

	Criterion	Step_Wise	LogAndInteraction	QDAnum	polyIncome3
1	AIC	818.074	620.167	0.000	695.393
2	BIC	892.000	786.501	0.000	781.640
3	Accuracy	0.957	0.977	0.875	0.969
4	Sensitivity	0.975	0.985	0.914	0.979
5	Specificity	0.806	0.904	0.514	0.870

	LogAndInteraction.1	AllInteractions	InteractinPolyLog
1	620.167	628.246	603.767
2	786.501	751.456	714.656
3	0.977	0.974	0.974
4	0.985	0.984	0.982
5	0.904	0.877	0.897

These could be for the extra info of criterion of all models

[1] "First basic models"

	Criterion	Full_Model	Step_Wise	Forward_Model	LASSO_model	Intuition	EDA
1	AIC	820.398	818.074	820.398	0.000	836.879	844.481
2	BIC	906.645	892.000	906.645	0.000	892.324	899.926
3	Accuracy	0.957	0.957	0.957	0.956	0.955	0.953
4	Sensitivity	0.975	0.975	0.975	0.975	0.976	0.974
5	Specificity	0.800	0.806	0.800	0.794	0.774	0.774

```
[1] "Interaction, Logginb and LDA/QDA results"
```

	Criterion	Famxmortgage	EduXMortgage	CCAvgxFam	IncomeXedu	FamxIncome	AllInteractions
1	AIC	844.759	916.902	768.813	619.763	655.916	628.246
2	BIC	937.167	984.668	855.061	699.850	748.324	751.456
3	Accuracy	0.961	0.953	0.962	0.971	0.973	0.974
4	Sensitivity	0.980	0.973	0.977	0.984	0.984	0.984
5	Specificity	0.781	0.774	0.822	0.849	0.870	0.877

```
[1] "LDA/QDA results"
```

	Criterion	AllInteractions	LogIncomeMortgage	LogAndInteraction	LDA	QDAnum
1	AIC	628.246	771.857	620.167	0.000	0.000
2	BIC	751.456	845.784	786.501	0.000	0.000
3	Accuracy	0.974	0.955	0.977	0.896	0.875
4	Sensitivity	0.984	0.972	0.985	0.945	0.914
5	Specificity	0.877	0.801	0.904	0.445	0.514

```
[1] "Polynomials resuls"
```

	Criterion	polyIncome2	polyIncome3	polyCCAvg2	polyCCAvg3	PolyBoth2	PolyBoth3	ExtremexModel	InteractinPolyLog
1	AIC	694.203	695.393	784.087	780.157	661.317	663.552	672.042	603.767
2	BIC	774.290	781.640	870.334	872.564	747.564	762.120	795.252	714.656
3	Accuracy	0.968	0.969	0.955	0.957	0.965	0.966	0.966	0.974
4	Sensitivity	0.979	0.979	0.971	0.975	0.976	0.977	0.978	0.982
5	Specificity	0.870	0.870	0.808	0.795	0.863	0.863	0.856	0.897