

1. Exercise 2.1

$$\frac{2}{N}, 37, \sqrt{N}, N, N \log \log N, N \log N, N \log^2 N, N \log(N^2), N^{1.5}, N^2, N^2 \log N, N^3, 2^{\frac{N}{2}}, 2^N \log N$$

2. Exercise 2.6

a) 2^{2N}

b) $O(\log(\log D))$

3. a) $O(N)$

b) $O(N^2)$

c) $O(\log_k N)$

4. Exercise 2.11

a) $O(N) \rightarrow k(100) = 0.5$
 $k(500) = 2.5 \text{ ms}$

b) $O(N \log N) \rightarrow k(100 \log 100) = 0.5$
 $k = \frac{0.5}{100 \log 100}$

$$k(500 \log 500) = \frac{0.5(500 \log 500)}{100 \log 100}$$

$$= \frac{0.5(5 \log 500)}{\log 100}$$

$$= 3.374 \text{ ms}$$

c) $O(N^2) \rightarrow k(100^2) = 0.5$
 $k = \frac{0.5}{100^2}$

$$k(500^2) = \frac{0.5(500^2)}{100^2} = 0.5(25) = 12.5 \text{ ms}$$

4) Exercise 2.11 cont'd

$$d) O(N^3) \rightarrow k(100^3) = 0.5$$

$$k = \frac{0.5}{100^3}$$

$$k(500^3) = \frac{0.5(500^3)}{100^3} = 0.5(5^3) = 62.5 \text{ ms}$$

5) Exercise 2.15

```
int start = 0;  
int end = array.length - 1;  
int i;
```

```
while (start <= end) {  
    i = (start + end) / 2;  
    if (array[i] > i) {  
        end = i - 1;  
    } if (array[i] < i) {  
        start = i + 1;  
    } else {  
        return i;  
    }  
}
```

```
}
```

```
return -1;
```

The runtime of this algorithm is $O(\log N)$