

Hierarchical model with school opening variable

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Data

```
regions <- c('Lazio', 'Lombardia', 'Abruzzo', 'Veneto', 'Emilia-Romagna', 'Toscana', 'Campania', 'Friuli Venezia Giulia', 'Sicilia')

regions

## [1] "Lazio"           "Lombardia"        "Abruzzo"
## [4] "Veneto"          "Emilia-Romagna"   "Toscana"
## [7] "Campania"        "Friuli Venezia Giulia" "Sicilia"
## [10] "Calabria"

hier_data <- get_hier_data(data_it, regions, initial_date = as.Date('2020-09-01') )

p_delay <- get_delay_distribution()

## school effect

school_opening <- as.Date('2020-09-14')
school <- rep(0, length(hier_data$dates))
school[which(hier_data$dates > school_opening +10)] <- 1
grow_school <- which(hier_data$dates>=school_opening & hier_data$dates <= school_opening +10)
school[grow_school] <- (grow_school - which(hier_data$dates ==school_opening))^-2 /100

## stan model

stan_data_hier <- list(J = length(regions),
                        N = nrow(hier_data$exposures),
                        N_nonzero = length(hier_data$nonzero_days),
                        nonzero_days = hier_data$nonzero_days,
                        conv_gt = get_gt_convolution_ln2(nrow(hier_data$exposures)),
                        length_delay = length(p_delay),
                        p_delay = p_delay,
                        exposures = hier_data$exposures,
                        nonzero_positives = hier_data$positives[hier_data$nonzero_days ,],
                        school = school
)

)
```

```

compiled_hier <- stan_model('~/stan/hier_model_school.stan')

fit_hier_school <- sampling(compiled_hier, data = stan_data_hier, iter= 2000, cores=getOption("mc.cores"))

##
## SAMPLING FOR MODEL 'hier_model_school' NOW (CHAIN 1).
## Chain 1:
## Chain 1: Gradient evaluation took 0.020438 seconds
## Chain 1: 1000 transitions using 10 leapfrog steps per transition would take 204.38 seconds.
## Chain 1: Adjust your expectations accordingly!
## Chain 1:
## Chain 1:
## Chain 1: Iteration: 1 / 2000 [ 0%] (Warmup)
## Chain 1: Iteration: 200 / 2000 [ 10%] (Warmup)
## Chain 1: Iteration: 400 / 2000 [ 20%] (Warmup)
## Chain 1: Iteration: 600 / 2000 [ 30%] (Warmup)
## Chain 1: Iteration: 800 / 2000 [ 40%] (Warmup)
## Chain 1: Iteration: 1000 / 2000 [ 50%] (Warmup)
## Chain 1: Iteration: 1001 / 2000 [ 50%] (Sampling)
## Chain 1: Iteration: 1200 / 2000 [ 60%] (Sampling)
## Chain 1: Iteration: 1400 / 2000 [ 70%] (Sampling)
## Chain 1: Iteration: 1600 / 2000 [ 80%] (Sampling)
## Chain 1: Iteration: 1800 / 2000 [ 90%] (Sampling)
## Chain 1: Iteration: 2000 / 2000 [100%] (Sampling)
## Chain 1:
## Chain 1: Elapsed Time: 1926.6 seconds (Warm-up)
## Chain 1: 1383.12 seconds (Sampling)
## Chain 1: 3309.72 seconds (Total)
## Chain 1:
## 
## SAMPLING FOR MODEL 'hier_model_school' NOW (CHAIN 2).
## Chain 2:
## Chain 2: Gradient evaluation took 0.011866 seconds
## Chain 2: 1000 transitions using 10 leapfrog steps per transition would take 118.66 seconds.
## Chain 2: Adjust your expectations accordingly!
## Chain 2:
## Chain 2:
## Chain 2: Iteration: 1 / 2000 [ 0%] (Warmup)
## Chain 2: Iteration: 200 / 2000 [ 10%] (Warmup)
## Chain 2: Iteration: 400 / 2000 [ 20%] (Warmup)
## Chain 2: Iteration: 600 / 2000 [ 30%] (Warmup)
## Chain 2: Iteration: 800 / 2000 [ 40%] (Warmup)
## Chain 2: Iteration: 1000 / 2000 [ 50%] (Warmup)
## Chain 2: Iteration: 1001 / 2000 [ 50%] (Sampling)
## Chain 2: Iteration: 1200 / 2000 [ 60%] (Sampling)
## Chain 2: Iteration: 1400 / 2000 [ 70%] (Sampling)
## Chain 2: Iteration: 1600 / 2000 [ 80%] (Sampling)
## Chain 2: Iteration: 1800 / 2000 [ 90%] (Sampling)
## Chain 2: Iteration: 2000 / 2000 [100%] (Sampling)
## Chain 2:
## Chain 2: Elapsed Time: 1990.05 seconds (Warm-up)
## Chain 2: 1518.79 seconds (Sampling)
## Chain 2: 3508.84 seconds (Total)
## Chain 2:

```

```

##  

## SAMPLING FOR MODEL 'hier_model_school' NOW (CHAIN 3).  

## Chain 3:  

## Chain 3: Gradient evaluation took 0.009859 seconds  

## Chain 3: 1000 transitions using 10 leapfrog steps per transition would take 98.59 seconds.  

## Chain 3: Adjust your expectations accordingly!  

## Chain 3:  

## Chain 3:  

## Chain 3: Iteration: 1 / 2000 [ 0%] (Warmup)  

## Chain 3: Iteration: 200 / 2000 [ 10%] (Warmup)  

## Chain 3: Iteration: 400 / 2000 [ 20%] (Warmup)  

## Chain 3: Iteration: 600 / 2000 [ 30%] (Warmup)  

## Chain 3: Iteration: 800 / 2000 [ 40%] (Warmup)  

## Chain 3: Iteration: 1000 / 2000 [ 50%] (Warmup)  

## Chain 3: Iteration: 1001 / 2000 [ 50%] (Sampling)  

## Chain 3: Iteration: 1200 / 2000 [ 60%] (Sampling)  

## Chain 3: Iteration: 1400 / 2000 [ 70%] (Sampling)  

## Chain 3: Iteration: 1600 / 2000 [ 80%] (Sampling)  

## Chain 3: Iteration: 1800 / 2000 [ 90%] (Sampling)  

## Chain 3: Iteration: 2000 / 2000 [100%] (Sampling)  

## Chain 3:  

## Chain 3: Elapsed Time: 1750 seconds (Warm-up)  

## Chain 3: 1984.02 seconds (Sampling)  

## Chain 3: 3734.02 seconds (Total)  

## Chain 3:  

##  

## SAMPLING FOR MODEL 'hier_model_school' NOW (CHAIN 4).  

## Chain 4:  

## Chain 4: Gradient evaluation took 0.011861 seconds  

## Chain 4: 1000 transitions using 10 leapfrog steps per transition would take 118.61 seconds.  

## Chain 4: Adjust your expectations accordingly!  

## Chain 4:  

## Chain 4:  

## Chain 4: Iteration: 1 / 2000 [ 0%] (Warmup)  

## Chain 4: Iteration: 200 / 2000 [ 10%] (Warmup)  

## Chain 4: Iteration: 400 / 2000 [ 20%] (Warmup)  

## Chain 4: Iteration: 600 / 2000 [ 30%] (Warmup)  

## Chain 4: Iteration: 800 / 2000 [ 40%] (Warmup)  

## Chain 4: Iteration: 1000 / 2000 [ 50%] (Warmup)  

## Chain 4: Iteration: 1001 / 2000 [ 50%] (Sampling)  

## Chain 4: Iteration: 1200 / 2000 [ 60%] (Sampling)  

## Chain 4: Iteration: 1400 / 2000 [ 70%] (Sampling)  

## Chain 4: Iteration: 1600 / 2000 [ 80%] (Sampling)  

## Chain 4: Iteration: 1800 / 2000 [ 90%] (Sampling)  

## Chain 4: Iteration: 2000 / 2000 [100%] (Sampling)  

## Chain 4:  

## Chain 4: Elapsed Time: 1651.85 seconds (Warm-up)  

## Chain 4: 1304.21 seconds (Sampling)  

## Chain 4: 2956.06 seconds (Total)  

## Chain 4:  

## Warning: There were 1 transitions after warmup that exceeded the maximum treedepth. Increase max_treedepth or  

## http://mc-stan.org/misc/warnings.html#maximum-treedepth-exceeded  

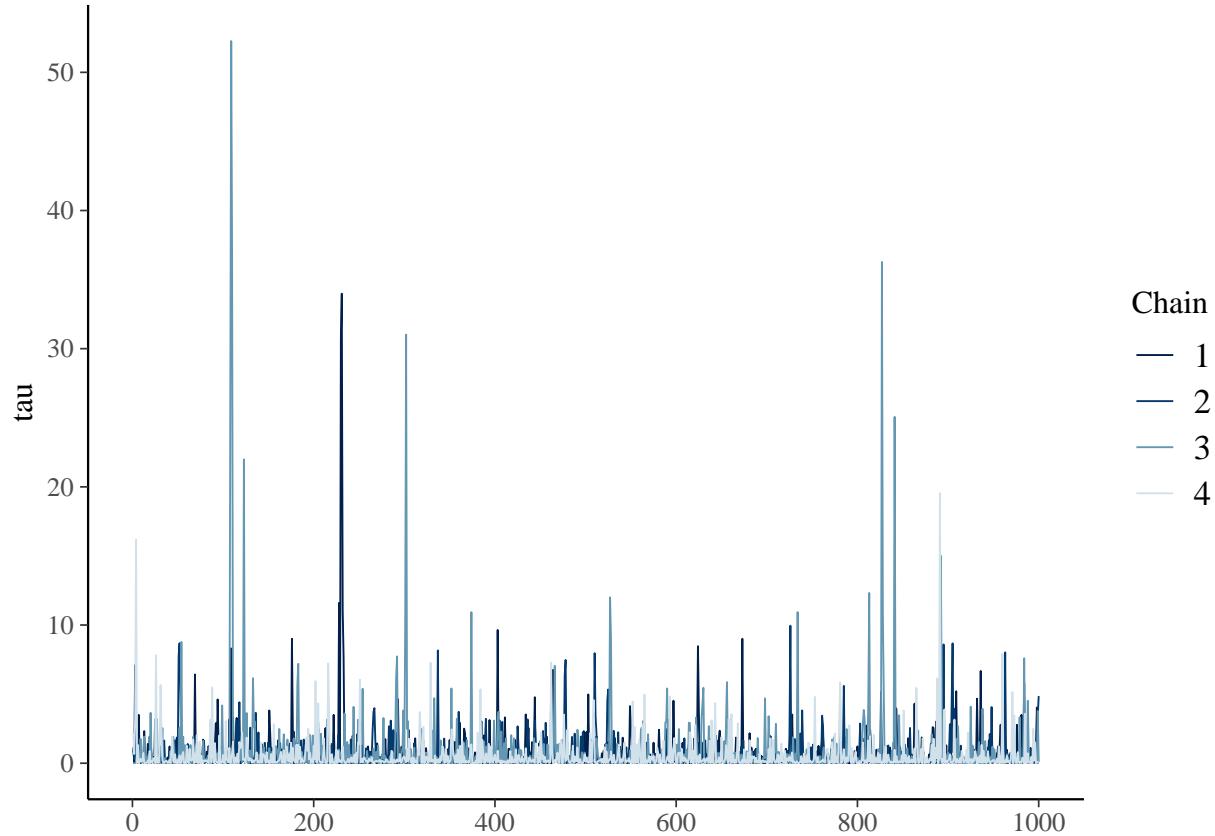
## Warning: Examine the pairs() plot to diagnose sampling problems

```

Trace plots

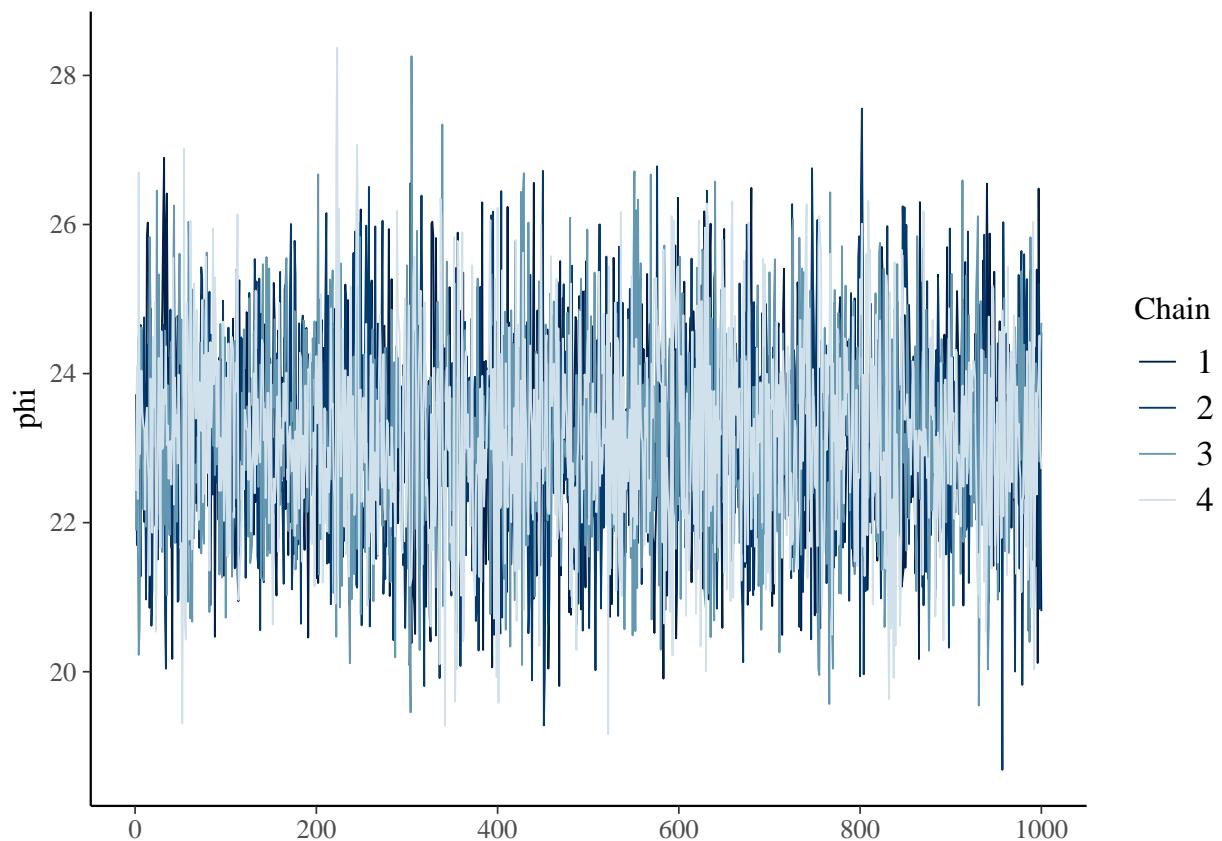
```
mcmc_trace(as.array(fit_hier_school, pars = c('tau')),
            np = nuts_params(fit_hier_school)
)
```

```
## No divergences to plot.
```



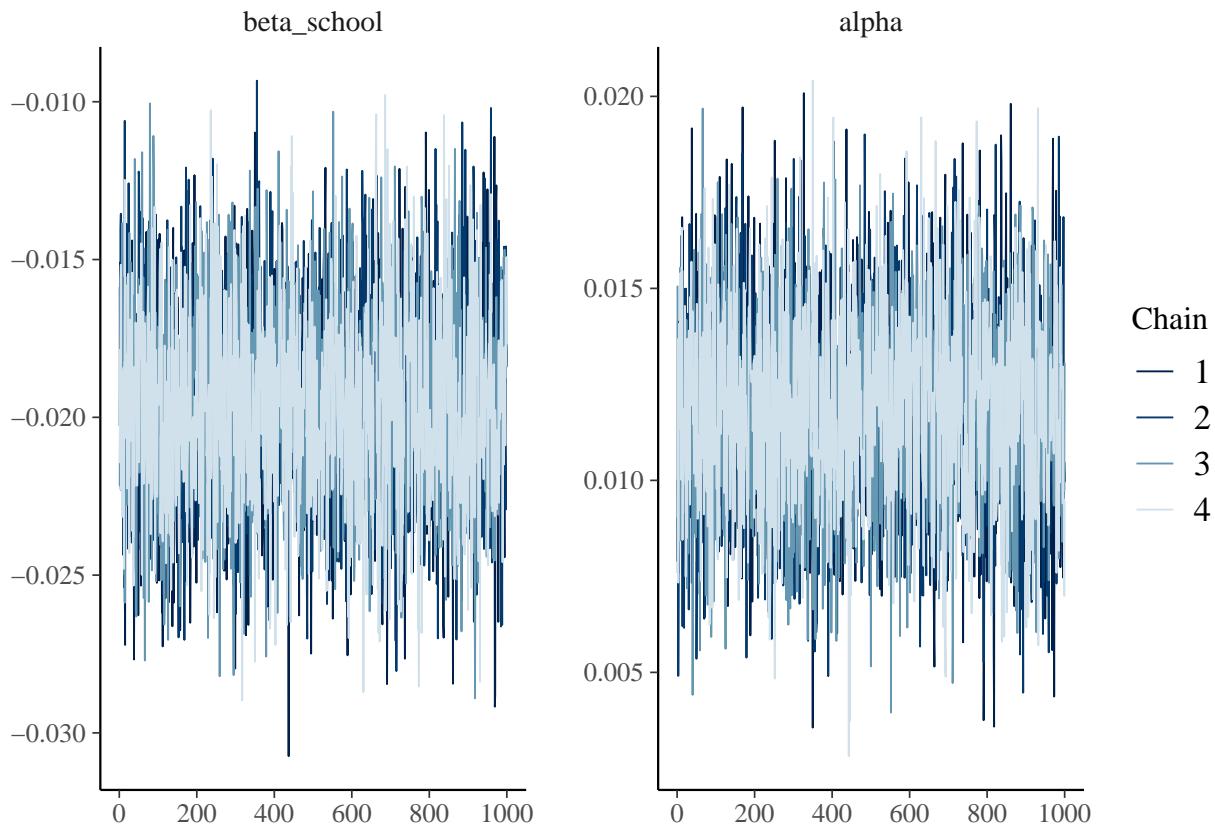
```
mcmc_trace(as.array(fit_hier_school, pars = c('phi')),
            np = nuts_params(fit_hier_school)
)
```

```
## No divergences to plot.
```



```
mcmc_trace(as.array(fit_hier_school, pars = c('beta_school', 'alpha')),
            np = nuts_params(fit_hier_school)
)
```

```
## No divergences to plot.
```



```

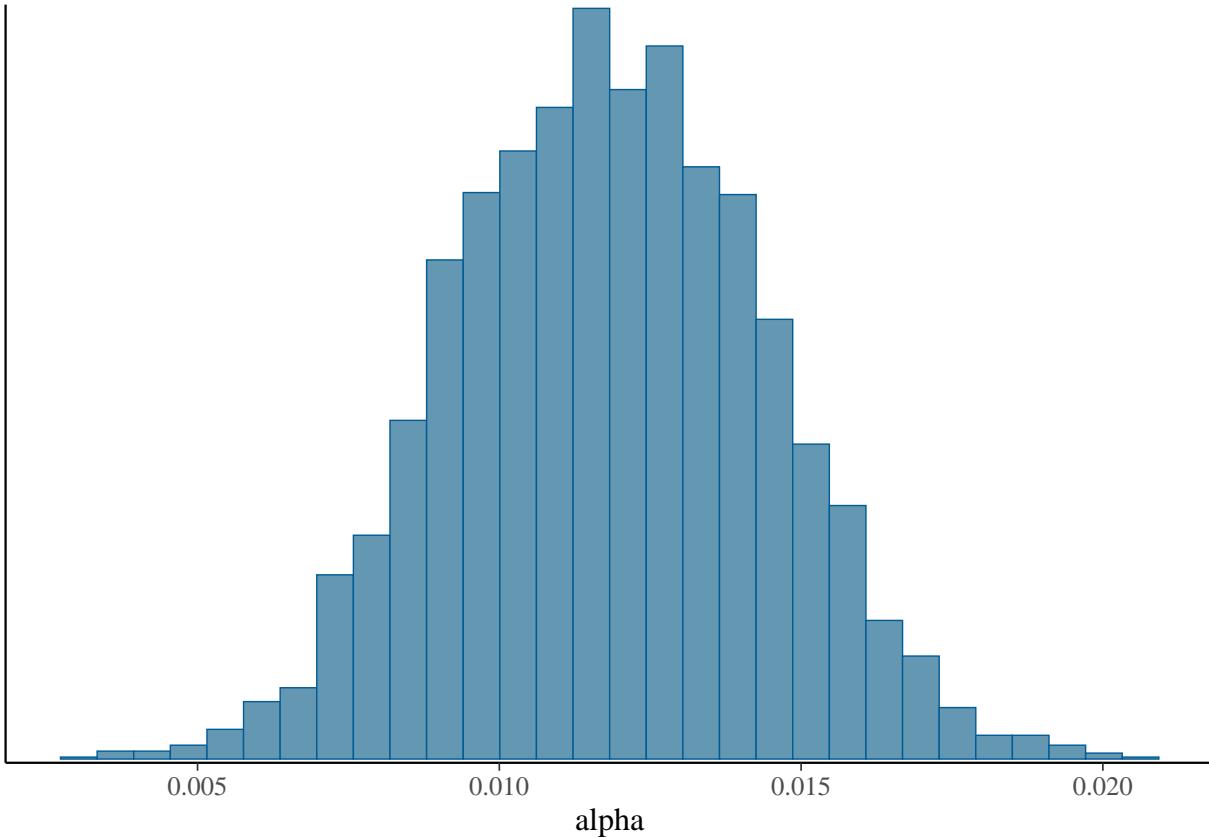
print(fit_hier_school, pars= 'alpha')

## Inference for Stan model: hier_model_school.
## 4 chains, each with iter=2000; warmup=1000; thin=1;
## post-warmup draws per chain=1000, total post-warmup draws=4000.
##
##      mean se_mean sd 2.5%  25%  50% 75% 97.5% n_eff Rhat
## alpha 0.01      0  0 0.01 0.01 0.01 0.01 0.02 3021     1
##
## Samples were drawn using NUTS(diag_e) at Sun Dec  6 16:16:03 2020.
## For each parameter, n_eff is a crude measure of effective sample size,
## and Rhat is the potential scale reduction factor on split chains (at
## convergence, Rhat=1).

mcmc_hist(fit_hier_school, pars = 'alpha')

## `stat_bin()` using `bins = 30` . Pick better value with `binwidth` .

```



```

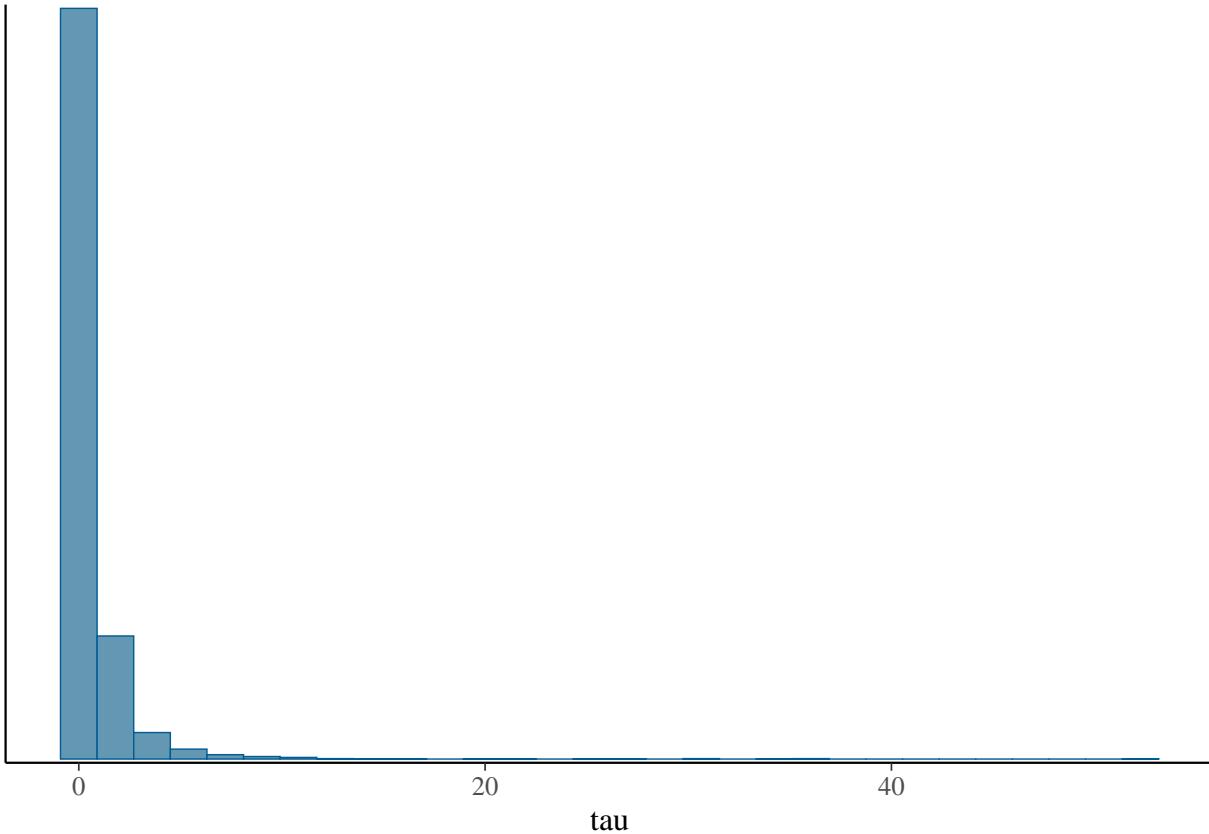
print(fit_hier_school, pars= 'tau')

## Inference for Stan model: hier_model_school.
## 4 chains, each with iter=2000; warmup=1000; thin=1;
## post-warmup draws per chain=1000, total post-warmup draws=4000.
##
##      mean se_mean   sd 2.5%  25%  50%  75% 97.5% n_eff Rhat
## tau 0.69    0.05 2.02 0.01 0.04 0.17 0.63  4.18 1962     1
##
## Samples were drawn using NUTS(diag_e) at Sun Dec  6 16:16:03 2020.
## For each parameter, n_eff is a crude measure of effective sample size,
## and Rhat is the potential scale reduction factor on split chains (at
## convergence, Rhat=1).

mcmc_hist(fit_hier_school, pars = 'tau')

## `stat_bin()` using `bins = 30`. Pick better value with `binwidth`.

```



School opening effect

```

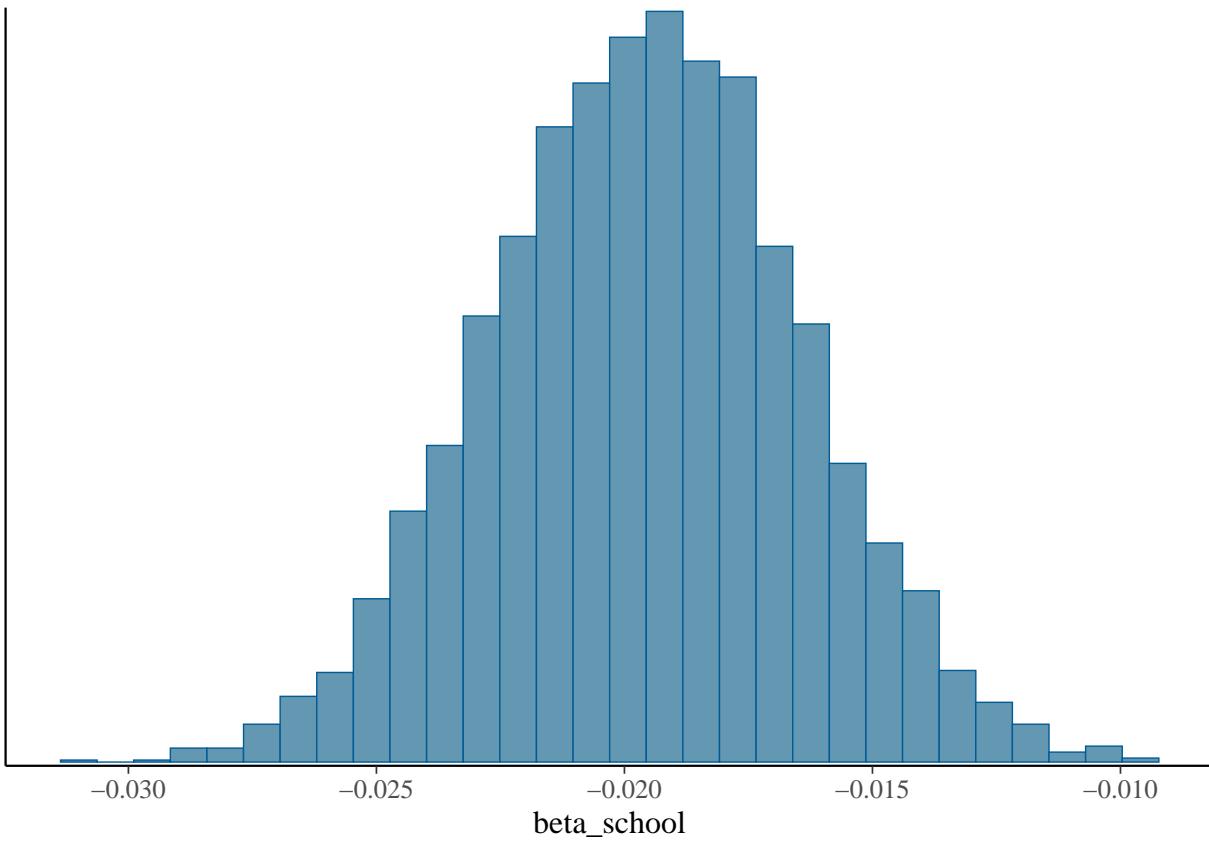
print(fit_hier_school, pars= 'beta_school')

## Inference for Stan model: hier_model_school.
## 4 chains, each with iter=2000; warmup=1000; thin=1;
## post-warmup draws per chain=1000, total post-warmup draws=4000.
##
##           mean se_mean sd  2.5%   25%   50%   75% 97.5% n_eff Rhat
## beta_school -0.02      0  0 -0.03 -0.02 -0.02 -0.02 -0.01  2894     1
##
## Samples were drawn using NUTS(diag_e) at Sun Dec  6 16:16:03 2020.
## For each parameter, n_eff is a crude measure of effective sample size,
## and Rhat is the potential scale reduction factor on split chains (at
## convergence, Rhat=1).

mcmc_hist(fit_hier_school, pars = 'beta_school')

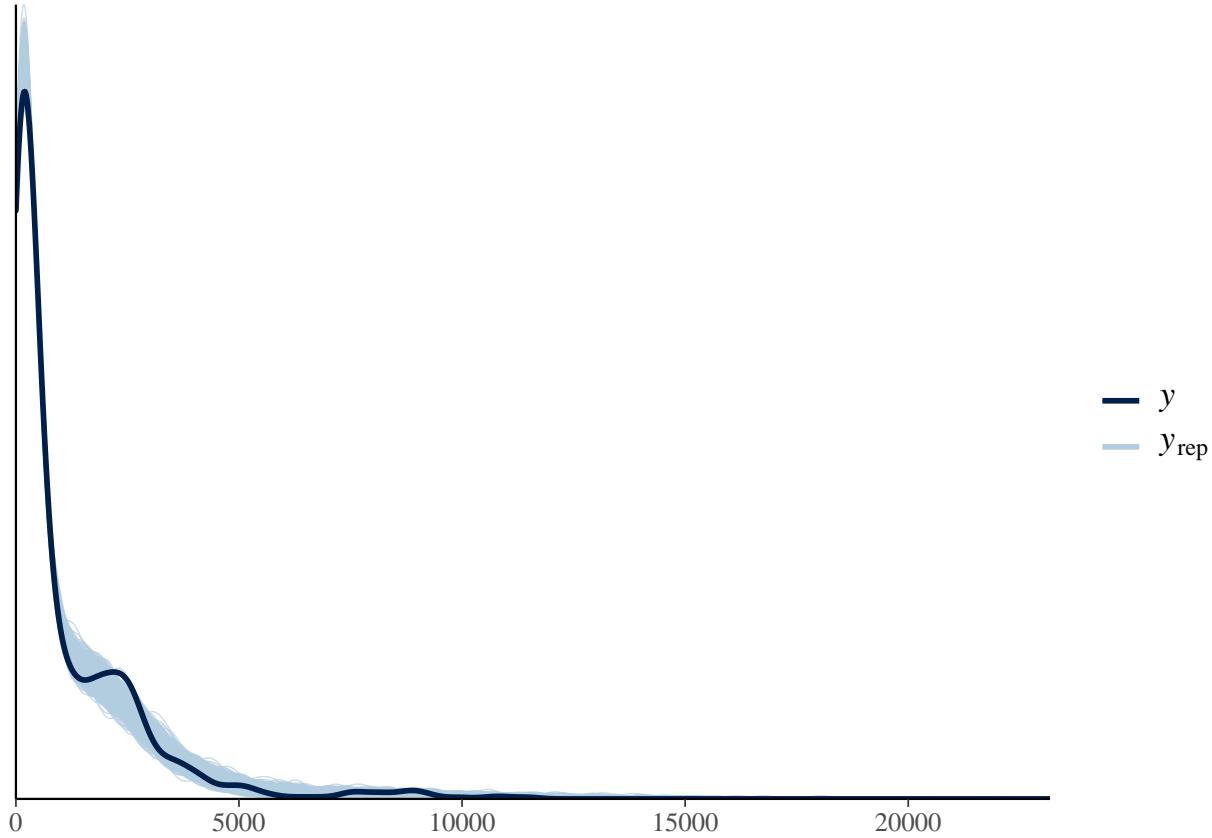
## `stat_bin()` using `bins = 30` . Pick better value with `binwidth` .

```



Posterior predictive check

```
y_rep <- as.matrix(fit_hier_school, pars = "y_rep")
ppc_dens_overlay(y = as.vector(stan_data_hier$nonzero_positives), y_rep[1:1000, ])
```



Posterior predictive check by region

```

regional_yrep_idx <- function(region, regions_vector, nonzero_days){
  region_idx <- which(regions_vector == region)
  yrep_idx <- (region_idx-1)*length(nonzero_days) + 1
  range <- yrep_idx : (yrep_idx + length(nonzero_days)-1)
  return(range)
}

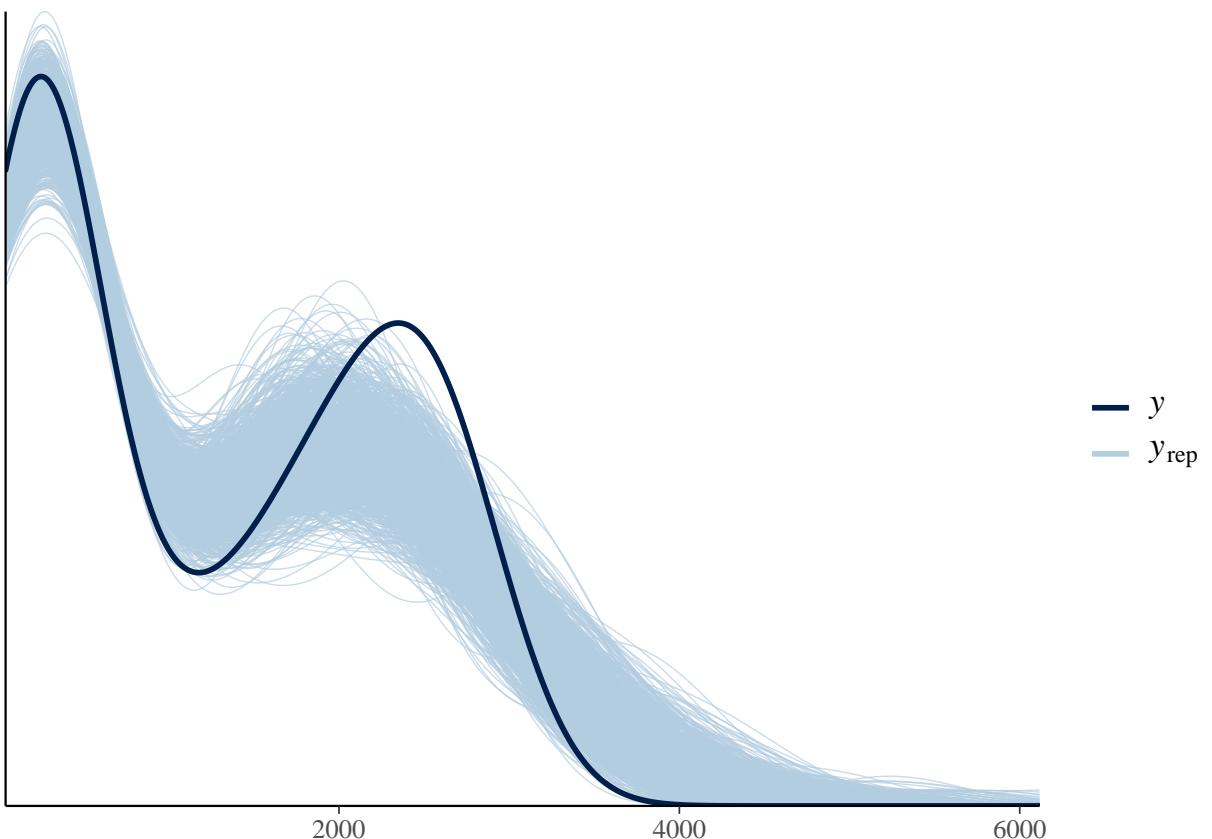
groups <- function(regions, nonzero_days){
  group <- rep(regions[1], length(nonzero_days))
  for(r in 2:length(regions))
    group <- c(group, rep(regions[r], length(nonzero_days)))

  return(group)
}

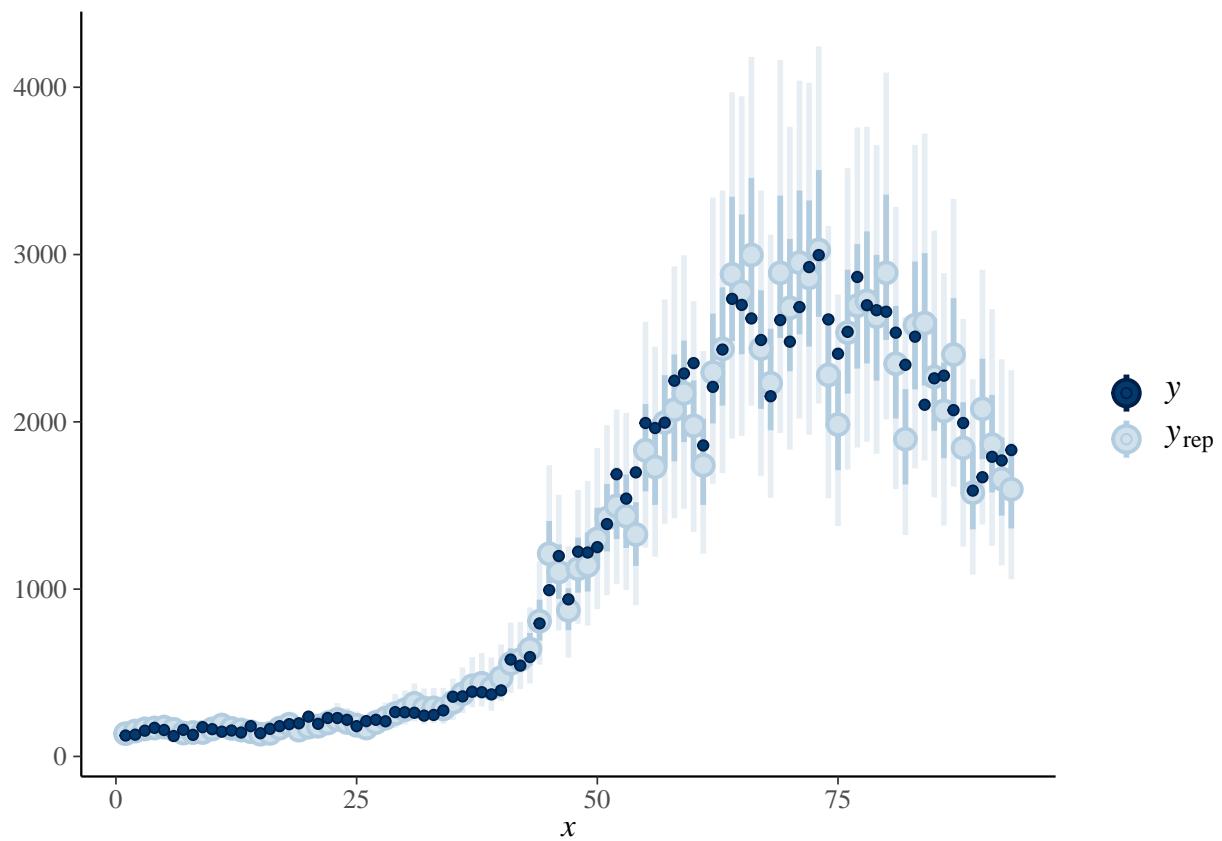
```

Lazio

```
ppc_dens_overlay(y = stan_data_hier$nonzero_positives[, which(regions == 'Lazio')], y_rep[1:1000,regions]
```

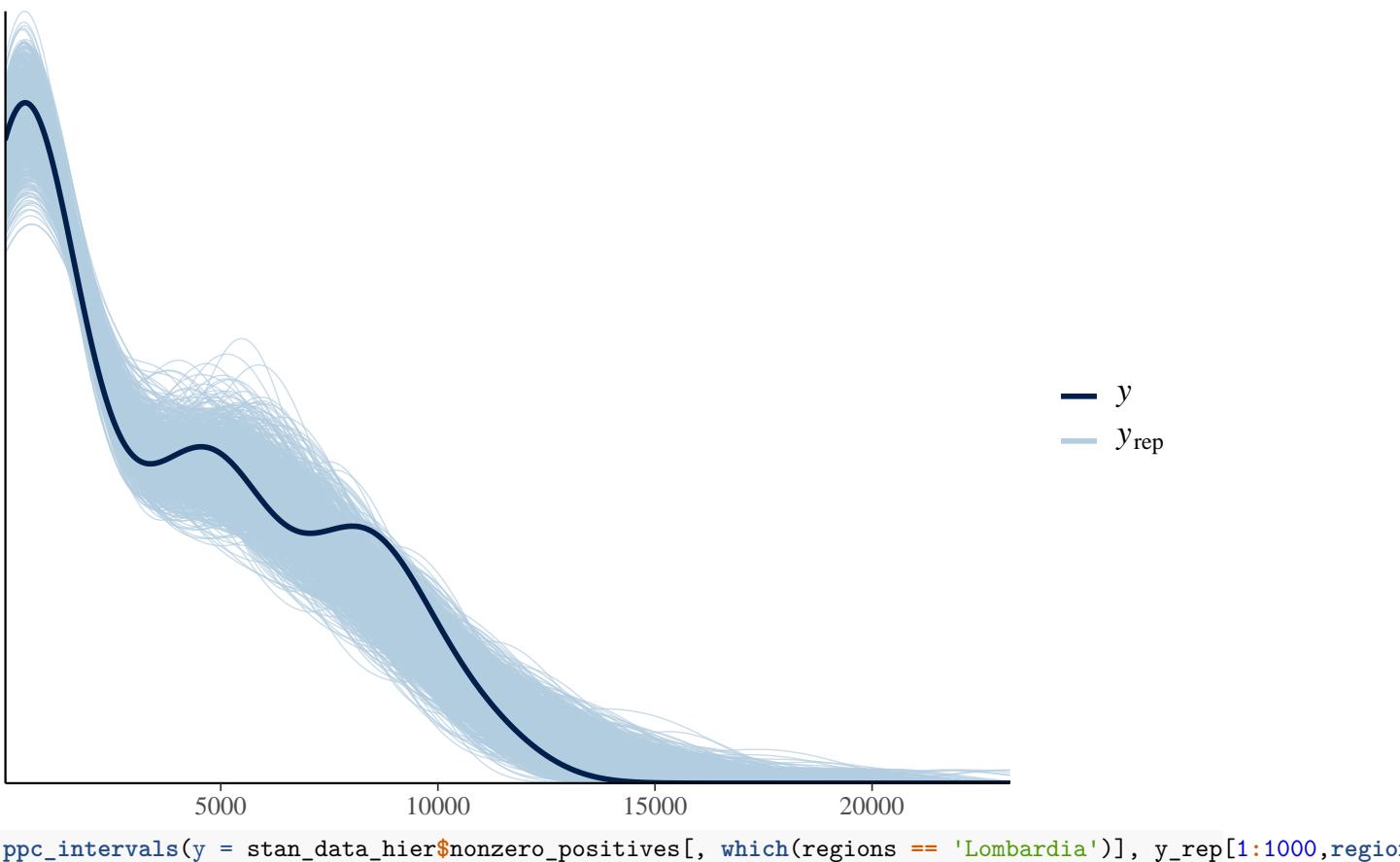


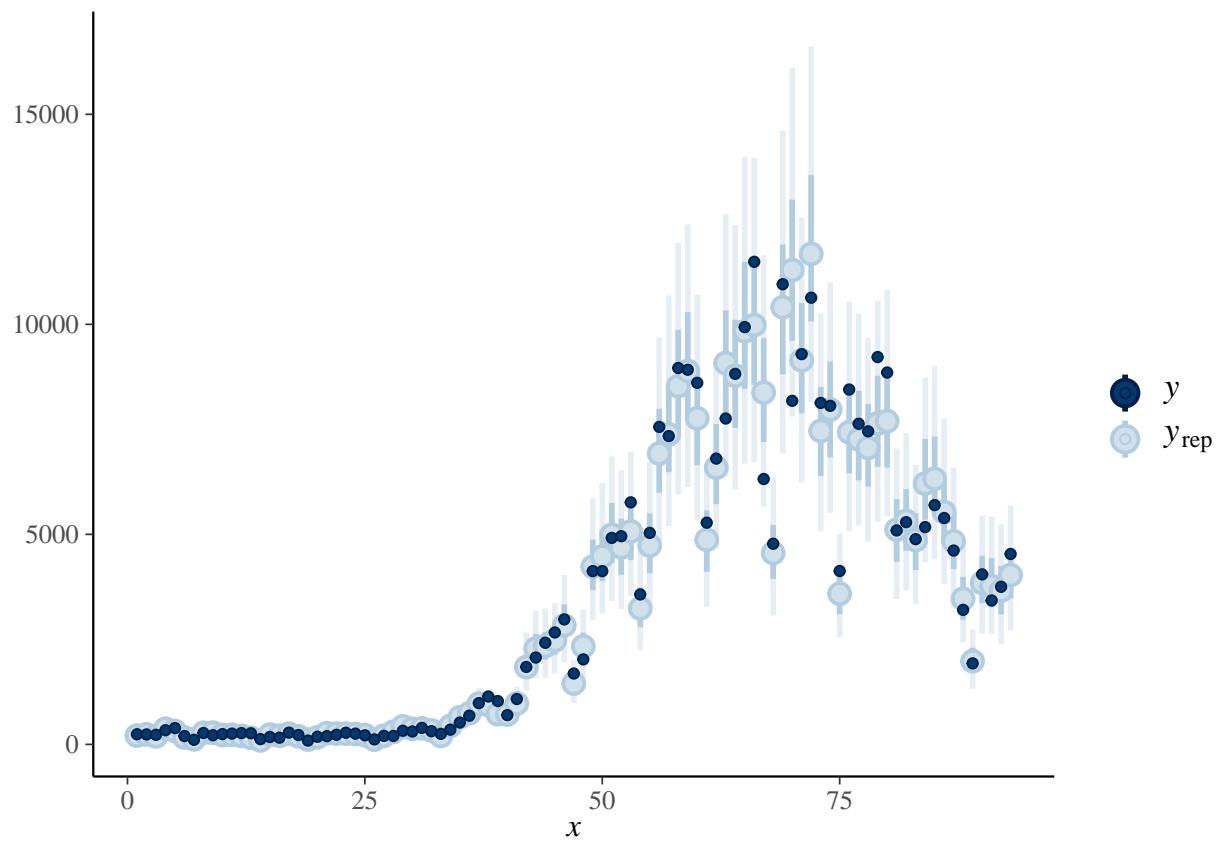
```
ppc_intervals(y = stan_data_hier$nonzero_positives[, which(regions == 'Lazio')], y_rep[1:1000, regional_
```



Lombardia

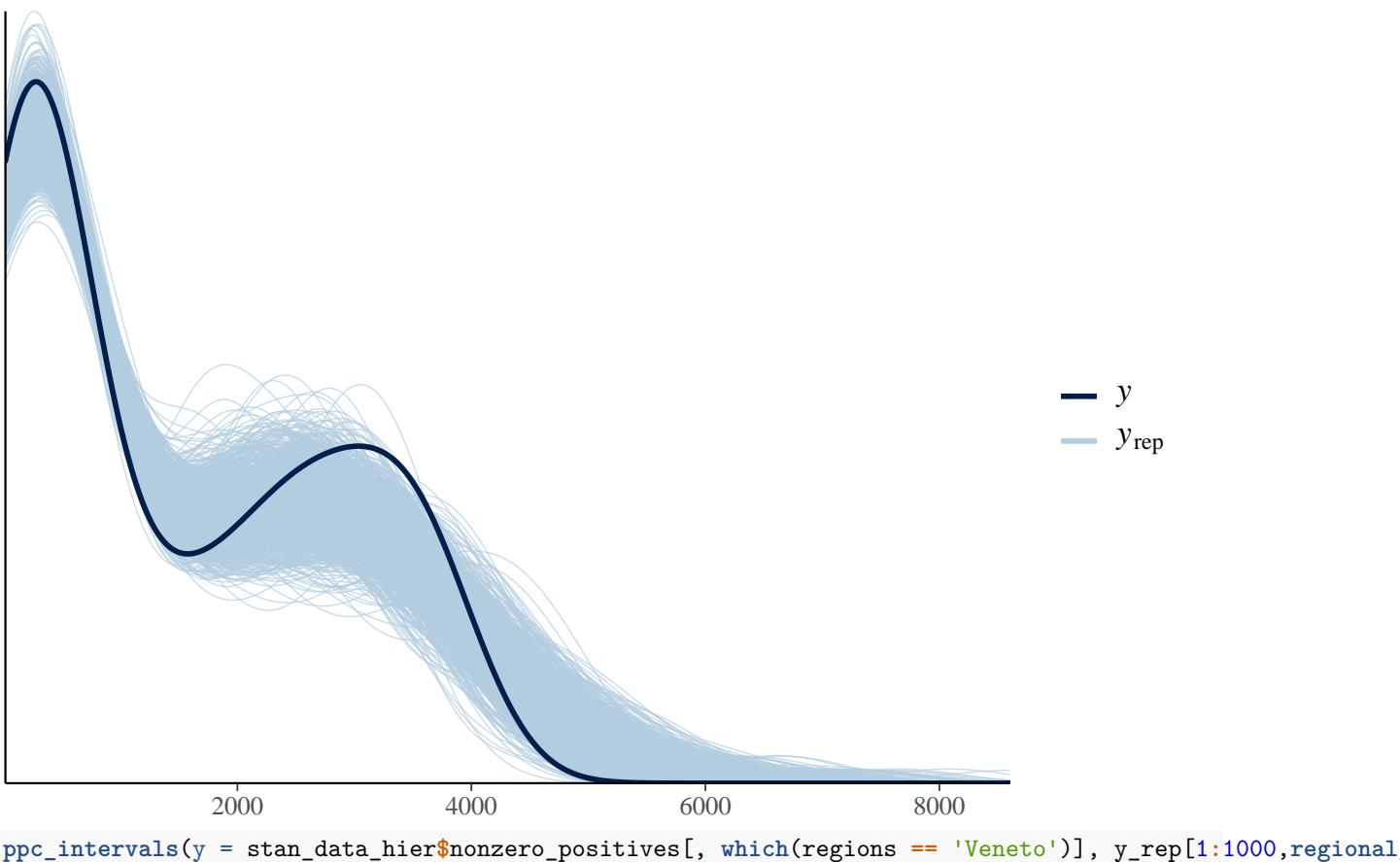
```
ppc_dens_overlay(y = stan_data_hier$nonzero_positives[, which(regions == 'Lombardia')], y_rep[1:1000, rep
```

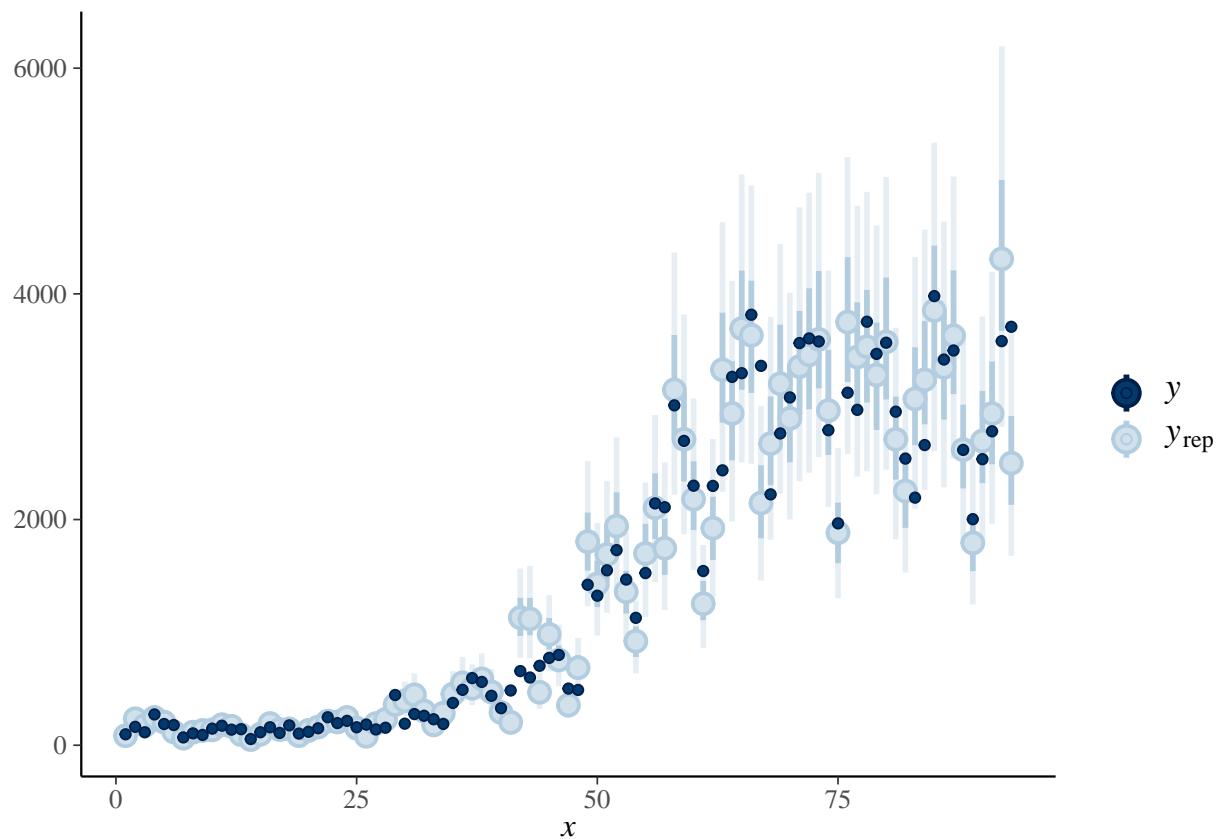




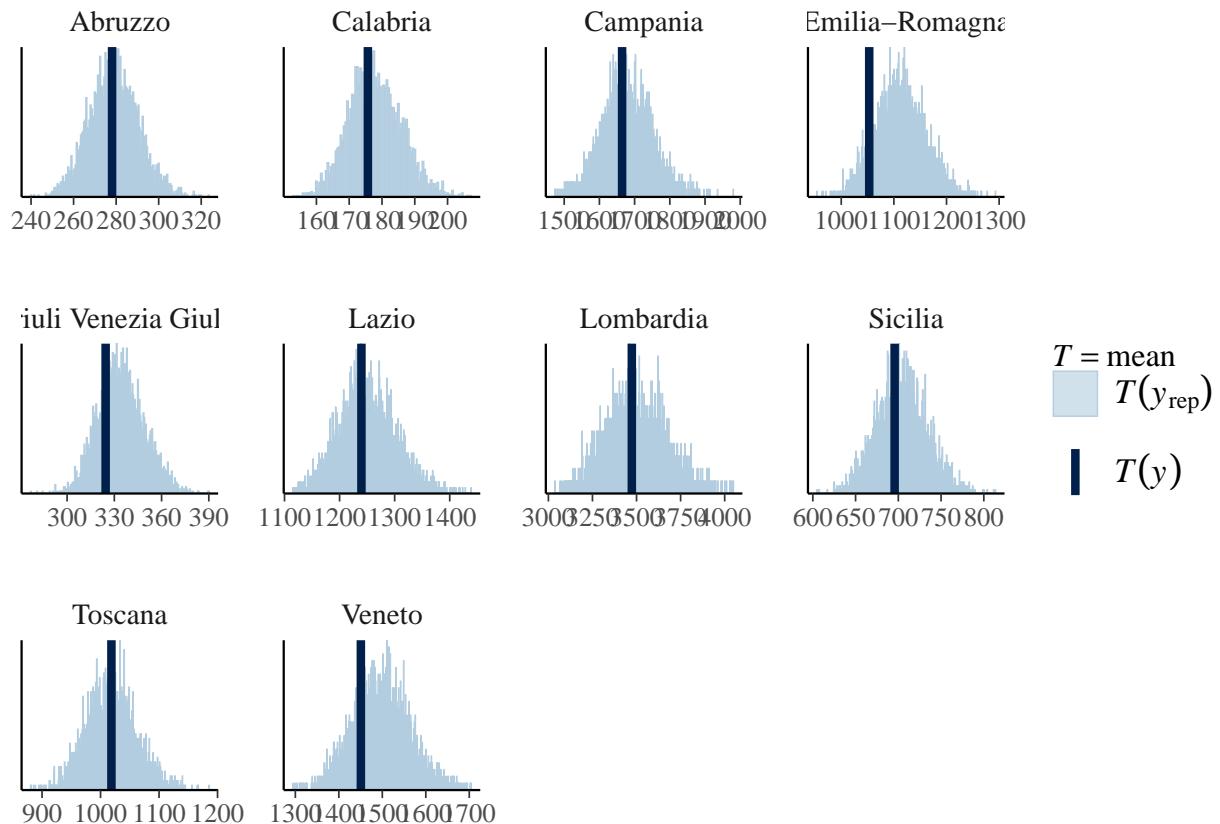
Veneto

```
ppc_dens_overlay(y = stan_data_hier$nonzero_positives[, which(regions == 'Veneto')], y_rep[1:1000,region]
```



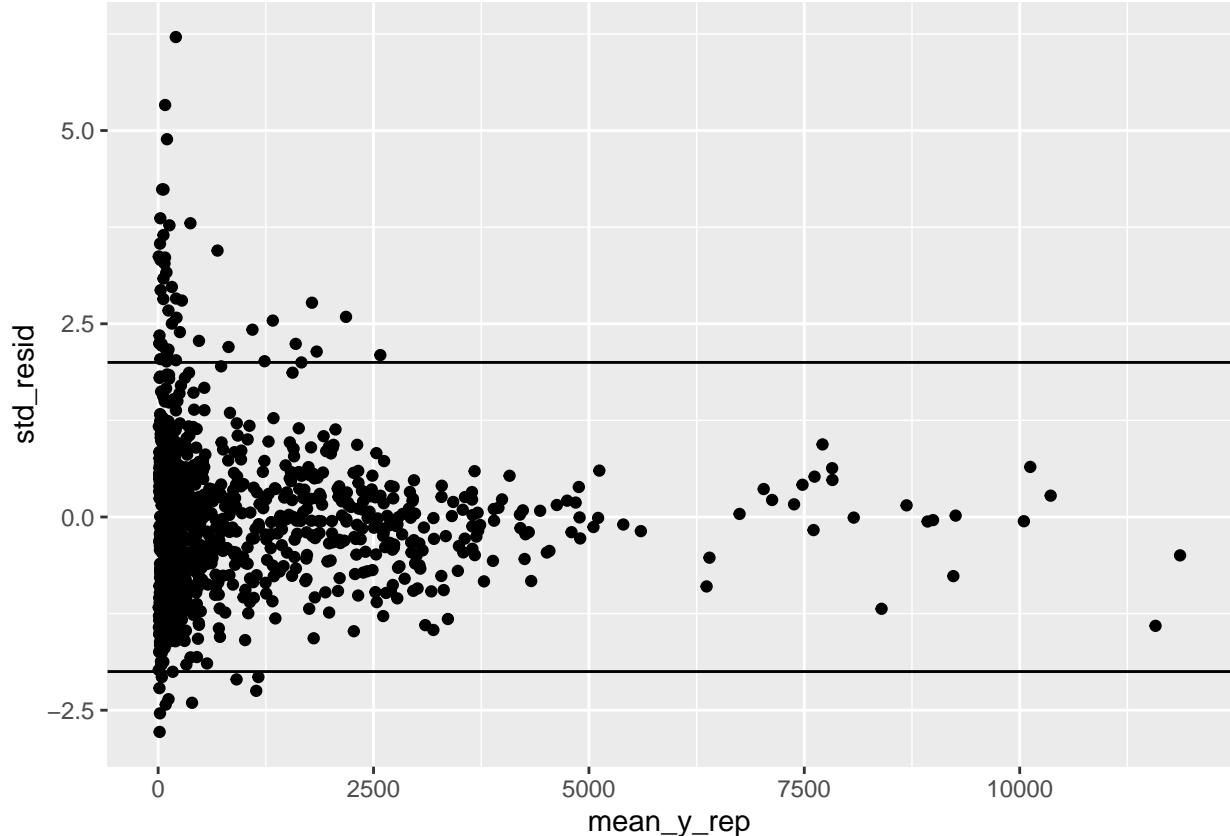


```
ppc_stat_grouped(y=as.vector(stan_data_hier$nonzero_positives), yrep =y_rep, group = groups(regions, st)
```



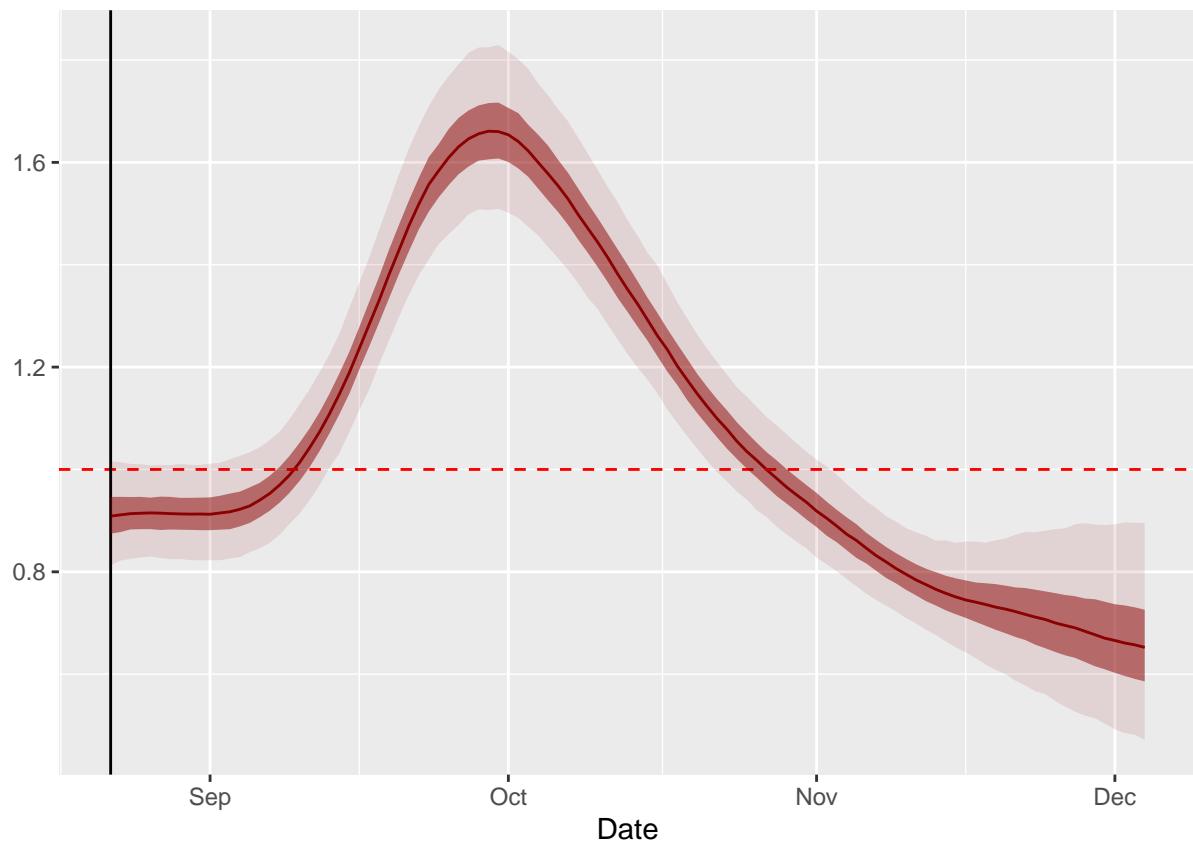
Residuals

```
mean_inv_phi<-mean(rstan::extract(fit_hier_school)$inv_phi)
mean_y_rep<-colMeans(y_rep)
std_resid<-(as.vector(stan_data_hier$nonzero_positives)-mean_y_rep)/sqrt(mean_y_rep+mean_y_rep^2*mean_in
qplot(mean_y_rep, std_resid)+hline_at(2)+hline_at(-2)
```



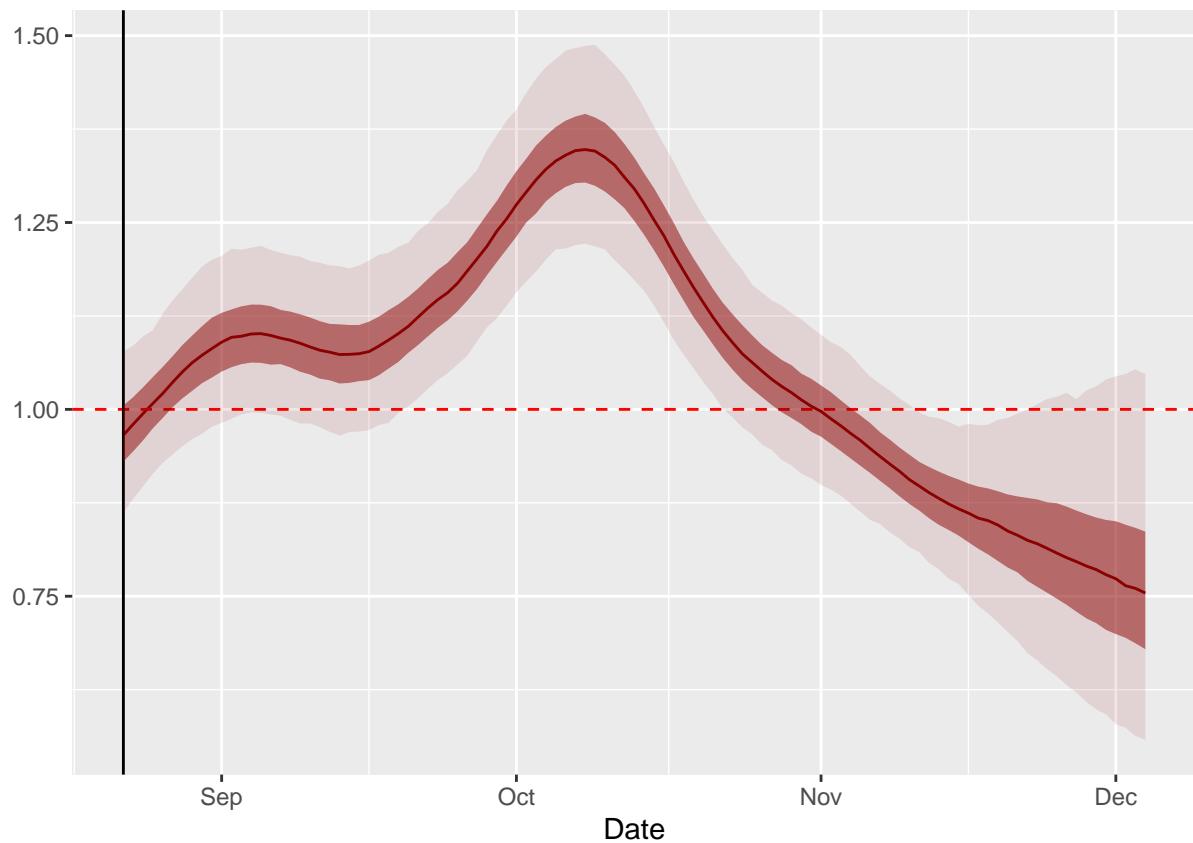
Rt Lombardia

```
plot_rt_hier(hier_data, fit_hier_school, regions, 'Lombardia')
```



Rt Lazio

```
plot_rt_hier(hier_data, fit_hier_school, regions, 'Lazio')
```



Rt Veneto

```
plot_rt_hier(hier_data, fit_hier_school, regions, 'Veneto')
```

