Unsupervised Learning

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library(ISLR) library(leaps)	

Principal Components Analysis (PCA)

In this lab, we perform PCA on the USArrests data, which is part of the base R package. The rows of the dataset contain the 50 states, in alphabetical order.

Objective: Perform PCA on the USArrests data, which is contained in the base R package.

```
[1] "Alabama"
                           "Alaska"
                                             "Arizona"
                                                               "Arkansas"
    [5] "California"
                                             "Connecticut"
##
                           "Colorado"
                                                               "Delaware"
##
    [9] "Florida"
                           "Georgia"
                                             "Hawaii"
                                                               "Idaho"
                                             "Iowa"
## [13] "Illinois"
                           "Indiana"
                                                               "Kansas"
## [17]
        "Kentucky"
                           "Louisiana"
                                             "Maine"
                                                               "Maryland"
## [21]
        "Massachusetts"
                                             "Minnesota"
                                                               "Mississippi"
                           "Michigan"
##
  [25]
        "Missouri"
                           "Montana"
                                             "Nebraska"
                                                               "Nevada"
  [29]
        "New Hampshire"
                           "New Jersey"
                                             "New Mexico"
                                                               "New York"
  [33] "North Carolina"
                           "North Dakota"
                                             "Ohio"
                                                               "Oklahoma"
                                             "Rhode Island"
   [37]
        "Oregon"
                           "Pennsylvania"
                                                               "South Carolina"
        "South Dakota"
                           "Tennessee"
                                             "Texas"
                                                               "Utah"
   [41]
## [45]
       "Vermont"
                           "Virginia"
                                             "Washington"
                                                               "West Virginia"
## [49] "Wisconsin"
                           "Wyoming"
```

The columns of the data contain four variables: Murder, Assault, UrbanPop, and Rape.

```
names(USArrests)
```

```
## [1] "Murder" "Assault" "UrbanPop" "Rape"
```

We first briefly examine the data. We notice that the variables have vastly different means.

```
# Briefly examine the mean and variance of the four columns apply(USArrests, 2, mean)
```

```
## Murder Assault UrbanPop Rape
## 7.788 170.760 65.540 21.232
```

Note that the apply() function allows us to apply a function - in this case - mean() - to each row or column of the dataset. The second input here denotes whether we wish to compute the mean of the rows, 1, or the columns 2. We see that there are on average three times as many rapes as murders, and more than eight times as many assaults as rapes. We can also examine the variance of the four variables using the apply() function.

apply(USArrests, 2, var)

```
## Murder Assault UrbanPop Rape
## 18.97047 6945.16571 209.51878 87.72916
```

Not surprisingly, the variables also have vastly different variances: the UrbanPop variable measures the percentage of the population in each state living in an urban area, which is not a comparable number to the number of rapes in each state per 100,000 individuals. If we failed to scale the variables before performing PCA, then most of the principal components that we observed would be driven by the Assault variable, since it has by far the largest mean and variance. Thus, it is important to standardize the variables to have a mean of zero and standard deviation of one before performing PCA.

First, notice how the apply() function is used - we are applying the mean() and variance() functions to the columns (second argument; 2) of the USArrests data. Second, observe the large difference in the means and variances of our variables. If we did not standardize the variables, the PCA ould mainly be driven by Assault.

We now perform principal component analysis using the prcomp() function, which is one of several functions in R that perform PCA.

```
\# Perform principal component analysis usign the prcomp() function pr.out <- prcomp(USArrests, scale = T) \#prcomp() centers the variables to have mean zero by default, where the variables is the precompton of the precompton
```

By default, the procomp() function centers the variables to have a mean of zero. By using the option scale = TRUE, we scale the variables to have a standard deviation of one. The output from prcomp() contains a number of useful quantities.

```
\# Center an scale components correspond to means and std. devs of the variables before implementing PCA names(pr.out)
```

```
## [1] "sdev" "rotation" "center" "scale" "x"
```

The center and scale components correspond to the means and standard deviations of the variables that were used for scaling prior to implementing PCA.

```
pr.out$center
```

```
## Murder Assault UrbanPop Rape
## 7.788 170.760 65.540 21.232
pr.out$scale
```

```
## Murder Assault UrbanPop Rape
## 4.355510 83.337661 14.474763 9.366385
```

The rotation matrix provides the principal component loadings; each column of pr.out\$rotation contains the corresponding principal component loading vector. This function names it the rotation matrix, because

when we matrix-multiply the **X** matrix by pr.out\$rotation, it gives us the coordinates of the data in the rotated coordinate system. These coordinates are the principal component score.

The rotation matrix provides the principal component loading vectors pr.out\$rotation

```
##
                   PC1
                               PC2
                                          PC3
                                                       PC4
## Murder
            -0.5358995
                        0.4181809 -0.3412327
                                               0.64922780
## Assault
            -0.5831836
                        0.1879856 -0.2681484 -0.74340748
## UrbanPop -0.2781909 -0.8728062 -0.3780158
            -0.5434321 -0.1673186
## Rape
                                   0.8177779
                                               0.08902432
```

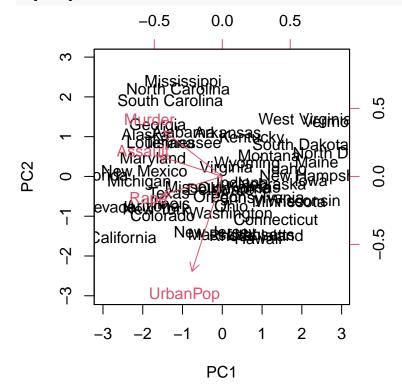
Using the prcomp() function, we do not need to explicitly multiply the data by the principal component loading vectors in order to obtain the principal component score vectors. Rather the 50x4 matrix \mathbf{x} has its columns the principal component score vectors. That is, the kth column is the kth principal component score vector.

```
# x contains the principal component score vectors
dim(pr.out$x)
```

[1] 50 4

We can plot the first two principal components as follows:

biplot(pr.out, scale = 0)



The scale = 0 argument to biplot() ensures that the arrows are scales to represent the loadings; other values for scale give slightly different biplots with different interpretations.

Recall that the principal components are only unique up to a sign change.

The prcomp() function also outputs the standard deviation of each principal component. For instance, on the USArrests dataset, we can access these standard deviations as follows:

```
pr.out$sdev
```

[1] 1.5748783 0.9948694 0.5971291 0.4164494

The variance explained by each principal component is obtained by squaring these:

```
# Find the amount of variance explained by each principal component
pr.var <- pr.out$sdev^2
pr.var</pre>
```

[1] 2.4802416 0.9897652 0.3565632 0.1734301

To compute the proportion of variance explained by each principal component, we simply divide the variance explained by each principal component by the total variance explained by all four principal components:

```
# To compute the proportion of variance explained by each PC, divide the variance explained by each PC pve <- pr.var / sum(pr.var) pve
```

[1] 0.62006039 0.24744129 0.08914080 0.04335752

We see that the first principal component explains 62% of the variance in the data, the next principal component explains 24.7% of the variance, and so forth. We can plot the PVE explained by each component, as well as the cumulative PVE, as follows:

```
# Plot the PVE of each component as well as the cumulative PVE
plot(pve, xlab = "Principal Component",
      ylab = "Proportion of Variance Explained",
      ylim = c(0,1),
      type = "b")
lines(cumsum(pve),
       type = "b",
       col="green")
Proportion of Variance Explained
       \infty
       Ö.
       9
       o.
       0.2
                                                                      \cap
                                                                                                 0
       0.0
               1.0
                            1.5
                                          2.0
                                                       2.5
                                                                                  3.5
                                                                                                4.0
                                                                     3.0
```

Note that the function cumsum() computes the cumulative sum of the elements of a numeric vector. For instance:

Principal Component

```
a = c(1, 2, 8, -3)
cumsum(a)
```

[1] 1 3 11 8

Clustering

K-Means Clustering

The function kmeans() performs K-means clustering in R. We begin with a simple simulated example in which these are truly two clusters in the data: the first 25 observations have a mean shift relative to the next 25 observations.

Objective: Find the clusters of simulated data using the kmeans() function.

```
# Create a matrix containing two well-defined clusters
set.seed(2)
x <- matrix(rnorm(50*2), ncol=2)
x[1:25,1] <- x[1:25, 1] +3
x[1:25,2] <- x[1:25, 2] - 4</pre>
```

We now perform K-means clustering, with K=2.

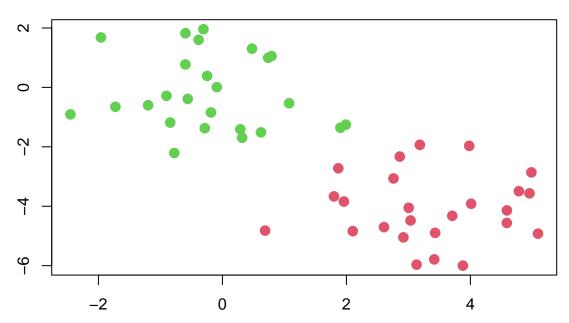
```
# Perform K-means clustering with K=2 and plot the results
km.out <- kmeans(x, 2, nstart=20)</pre>
```

The cluster assignments of the 50 observations are contained in km.out\$cluster.

km.out\$cluster

The K-means clustering perfectly separated the observations into two clusters even though we did not supply any group information to kmeans(). We can plot the data, with each observation coloured according to its cluster assignment.

K-means Clustering with K = 3



Here the observations can be easily plotted because they are two-dimensional. If there were more than two variables then we could instead perform PCA and plot the first two principal components score vectors.

In this example, we knew that there really were two clusters because we generated the data. However, for real data, in general we do not know the true number of clusters. We could instead have performed K-means clustering in this example with K=3.

```
# To run the kmeans() function with multiple initial cluster assignments, use the nstart argument
set.seed(4)
km.out <- kmeans(x, 3, nstart=20)</pre>
km.out
## K-means clustering with 3 clusters of sizes 17, 23, 10
##
## Cluster means:
##
          [,1]
                     [,2]
    3.7789567 -4.56200798
  2 -0.3820397 -0.08740753
    2.3001545 -2.69622023
##
## Clustering vector:
   ## [39] 2 2 2 2 2 3 2 3 2 2 2 2
##
## Within cluster sum of squares by cluster:
  [1] 25.74089 52.67700 19.56137
   (between_SS / total_SS = 79.3 %)
##
##
## Available components:
##
## [1] "cluster"
                    "centers"
                                  "totss"
                                                "withinss"
                                                              "tot.withinss"
## [6] "betweenss"
                    "size"
                                  "iter"
                                                "ifault"
```

When K = 3, K-means clusterings splits up the two clusters.

To run the kmeans() function in R with multiple initial cluster assignments, we use the nstart argument. If a value of nstart greater than one is used, then K-means clustering will be performed using multiple random assignments in Step 1 of the algorithm, and the kmeans() function will report only the best results. Here we compare using nstart = 1 to nstart = 20.

```
set.seed(3)
km.out <- kmeans(x, 3, nstart = 1)
km.out$tot.withinss

## [1] 97.97927

# Observe how this value is smaller than the previous result with only one initial set
set.seed(3)
km.out2 <- kmeans(x, 3, nstart=20)
km.out2$tot.withinss</pre>
```

```
## [1] 97.97927
```

Note that km.out\$tot.withinss is the total within-cluster sum of squares, which we seek to minimize by performing K-means clustering. The individual within-cluster sum-of-squares are contained in the vector of km.out\$withinss.

We strongly recommend always running K-means clustering with a large value of nstart, such as 20 or 50, since otherwise an undesirable local optimum may be obtained.

When performing K-means clustering, in addition to using multiple initial cluster assignments, it is also important to set a random seed using the set.seed() function. This way, the initial cluster assignments in Step 1 can be replicated, and the K-means output will be fairly reproducible.

Hierarchical Clustering

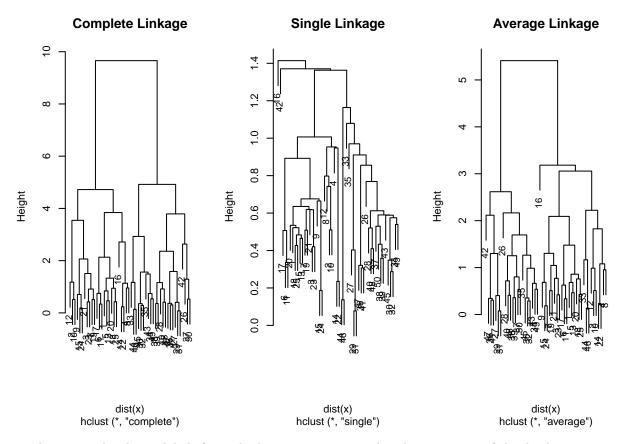
The hclust() function implements hierarchical clustering in R. In the following example, we use data to plot the hierarchical clustering dendrogram using complete, single, and average clustering, with Euclidean distance as the dissimilarity measure. We begin by clustering observations using complete linkage. The dist() function is used to compute the 50x50 inter-observation Euclidean distance matrix.

Objective: Use Euclidean distance as a dissimilarity measure to find clusters in the simulated data from the previous section.

```
hc.complete <- hclust(dist(x), method = "complete")
hc.single <- hclust(dist(x), method = "single")
hc.average <- hclust(dist(x), method = "average")</pre>
```

We can now plot the dendrograms obtained using the usual plot() function. The numbers at the bottom of the plot identify each observation.

```
# Plot the dendrograms for each clustering
par(mfrow=c(1,3))
plot(hc.complete, main = "Complete Linkage", cex = 0.9)
plot(hc.single, main = "Single Linkage", cex = 0.9)
plot(hc.average, main = "Average Linkage", cex = 0.9)
```



To determine the cluster labels for each observation associated with a given cut of the dendrogram, we can use the cutree() function:

If there is a point that belongs to its own cluster, then it is probably necessary to increase the number of clusters.

[39] 2 2 2 2 2 1 2 1 2 2 2 2

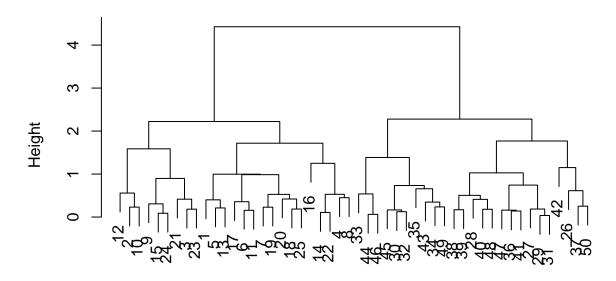
For this data, complete and average linkage generally separates the observations into their correct groups. However, single linkage identifies one point as beloning to its own cluster. A more sensible answer is obtained when four clusters are selected, although there are still two singletons.

To scale the variables before performing hierarchical clustering of the observations, we use the scale()

function:

```
# Rerun hclust() with scaled variables
xsc <- scale(x)
plot(hclust(dist(xsc), method="complete"), main = "Hierarchical Clustering with Scales Features")</pre>
```

Hierarchical Clustering with Scales Features

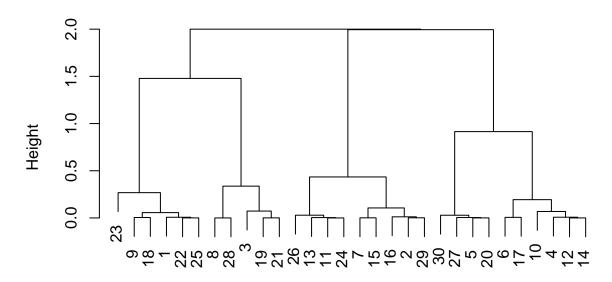


dist(xsc) hclust (*, "complete")

Correlation-based distance can be computed using the as.dist() function, which converts an arbitrary square symmetric matrix into a form that the hclust() function recognizes as a distance matrix. However, this only makes sense for data with at least three features since the absolute correlation between any two observations with measurements on two features is always 1. Hence, we will cluster a three-dimensional dataset.

```
# Practice clustering using a correlation-based distance measure
x <- matrix(rnorm(30*3), ncol=3)
dd <- as.dist(1 - cor(t(x)))
plot(hclust(dd, method="complete"), main = "Complete Linkage with Correlation-Based Distance")</pre>
```

Complete Linkage with Correlation-Based Distance



dd hclust (*, "complete")

NCI60 Data Example

Unsupervised techniques are often used in the analysis of genomic data. In particular, PCA and hierarchical clustering are popular tools. We illustrate these techniques on the NCI60 cancer cell line microarray data, which consists of 6,830 gene expression measurements on 64 cancer cell lines.

```
nci.labs = NCI60$labs
nci.data = NCI60$data
```

Each cell line is labeled with a cancer type. We do not make use of the cancer types in performing PCA and clustering, as these are unsupervised techniques. But after performing PCA and clustering, we will check to see the extent to which these cancer types agree with the results of these unsupervised techniques.

The data has 64 rows and 6,830 columns.

```
dim(nci.data)
## [1] 64 6830
We begin by examining the cancer types for the cell lines.
nci.labs[1:4]
## [1] "CNS" "CNS" "CNS" "RENAL"
table(nci.labs)
```

```
## nci.labs
## BREAST CNS COLON K562A-repro K562B-repro LEUKEMIA
## 7 5 7 1 1 6
## MCF7A-repro MCF7D-repro MELANOMA NSCLC OVARIAN PROSTATE
```

```
## 1 1 8 9 6 2
## RENAL UNKNOWN
## 9 1
```

PCA and the NCI60 Data

We first perform PCA on the data after scaling the variables (genes) to have a standard deviation of one, although one could reasonably argue that is is better not to scale the genes.

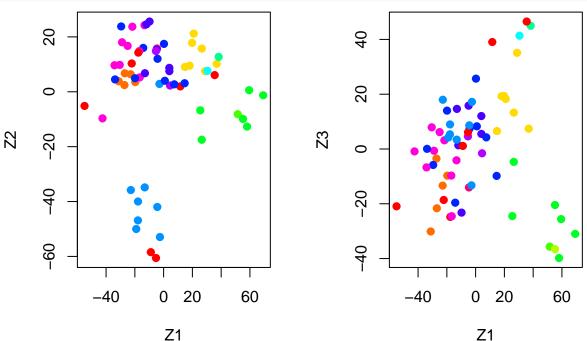
```
pr.out = prcomp(nci.data, scale = TRUE)
```

We now plot the first few principal component score vectors, in order to visualize the data. The observations (cell lines) corresponding to a given cancer type will be plotted in the same colour, so that we can see to what extent the observations within a cancer type are similar to each other. We first create a simple function that assigns a distinct colour to each element of a numeric vector. The function will be used to assign a colour to each of the 64 cell lines, based on the cancer type to which it corresponds.

```
cols = function(vec){
  cols = rainbow(length(unique(vec)))
  return(cols[as.numeric(as.factor(vec))])
}
```

Bote that the rainbow() function takes as its argument a positive integer and returns a vector containing the number of distinct colours. We can now plot the principal component score vectors.

```
par(mfrow=c(1,2))
plot(pr.out$x[,1:2], col=cols(nci.labs), pch=19,
xlab="Z1",ylab="Z2")
plot(pr.out$x[,c(1,3)], col=cols(nci.labs), pch=19,
xlab="Z1",ylab="Z3")
```



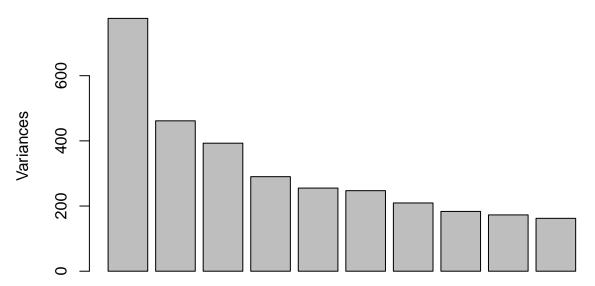
On the whole, cell lines corresponding to a single cancer type do tent to have similar values on the first few principal components score vectors. This indicates that cell lines from the same cancer type tend to have pretty similar gene expression levels. We can also obtain a summary of the proportion of variance explained (PVE) of the first few principal components using the summary() method for a prcomp object:

summary(pr.out)

```
## Importance of components:
##
                              PC1
                                        PC2
                                                 PC3
                                                          PC4
                                                                    PC5
                                                                             PC6
## Standard deviation
                          27.8535 21.48136 19.82046 17.03256 15.97181 15.72108
## Proportion of Variance
                          0.1136
                                    0.06756
                                            0.05752
                                                      0.04248
                                                               0.03735
                                                                         0.03619
## Cumulative Proportion
                           0.1136
                                    0.18115
                                             0.23867
                                                      0.28115
                                                               0.31850
                                                                         0.35468
##
                               PC7
                                         PC8
                                                  PC9
                                                          PC10
                                                                    PC11
                                                                             PC12
                          14.47145 13.54427 13.14400 12.73860 12.68672 12.15769
## Standard deviation
## Proportion of Variance
                           0.03066
                                     0.02686
                                              0.02529
                                                       0.02376
                                                                 0.02357
                           0.38534
## Cumulative Proportion
                                     0.41220
                                              0.43750
                                                       0.46126
                                                                 0.48482
##
                              PC13
                                        PC14
                                                 PC15
                                                          PC16
                                                                    PC17
                                                                             PC18
## Standard deviation
                          11.83019 11.62554 11.43779 11.00051 10.65666 10.48880
## Proportion of Variance
                           0.02049
                                     0.01979
                                              0.01915
                                                       0.01772
                                                                 0.01663
##
  Cumulative Proportion
                           0.52695
                                     0.54674
                                              0.56590
                                                       0.58361
                                                                 0.60024
                                                                          0.61635
                              PC19
                                       PC20
                                                PC21
                                                        PC22
                                                                 PC23
                                                                         PC24
## Standard deviation
                          10.43518 10.3219 10.14608 10.0544 9.90265 9.64766
## Proportion of Variance
                           0.01594
                                     0.0156
                                            0.01507
                                                      0.0148 0.01436 0.01363
## Cumulative Proportion
                           0.63229
                                     0.6479
                                             0.66296
                                                      0.6778 0.69212 0.70575
##
                              PC25
                                      PC26
                                              PC27
                                                     PC28
                                                              PC29
                                                                      PC30
                                                                              PC31
## Standard deviation
                          9.50764 9.33253 9.27320 9.0900 8.98117 8.75003 8.59962
## Proportion of Variance 0.01324 0.01275 0.01259 0.0121 0.01181 0.01121 0.01083
## Cumulative Proportion 0.71899 0.73174 0.74433 0.7564 0.76824 0.77945 0.79027
##
                             PC32
                                      PC33
                                              PC34
                                                      PC35
                                                              PC36
                                                                       PC37
                                                                               PC38
## Standard deviation
                          8.44738 8.37305 8.21579 8.15731 7.97465 7.90446 7.82127
## Proportion of Variance 0.01045 0.01026 0.00988 0.00974 0.00931 0.00915 0.00896
## Cumulative Proportion
                          0.80072 0.81099 0.82087 0.83061 0.83992 0.84907 0.85803
                                                              PC43
##
                                                     PC42
                             PC39
                                      PC40
                                              PC41
                                                                     PC44
                                                                             PC45
## Standard deviation
                          7.72156 7.58603 7.45619 7.3444 7.10449 7.0131 6.95839
## Proportion of Variance 0.00873 0.00843 0.00814 0.0079 0.00739 0.0072 0.00709
##
  Cumulative Proportion
                          0.86676 0.87518 0.88332 0.8912 0.89861 0.9058 0.91290
##
                             PC46
                                     PC47
                                             PC48
                                                     PC49
                                                              PC50
                                                                      PC51
## Standard deviation
                          6.8663 6.80744 6.64763 6.61607 6.40793 6.21984 6.20326
## Proportion of Variance 0.0069 0.00678 0.00647 0.00641 0.00601 0.00566 0.00563
                          0.9198 0.92659 0.93306 0.93947 0.94548 0.95114 0.95678
## Cumulative Proportion
##
                              PC53
                                      PC54
                                              PC55
                                                      PC56
                                                               PC57
                                                                      PC58
## Standard deviation
                          6.06706 5.91805 5.91233 5.73539 5.47261 5.2921 5.02117
## Proportion of Variance 0.00539 0.00513 0.00512 0.00482 0.00438 0.0041 0.00369
## Cumulative Proportion
                          0.96216 0.96729 0.97241 0.97723 0.98161 0.9857 0.98940
                             PC60
                                      PC61
                                              PC62
                                                      PC63
                                                                 PC64
##
## Standard deviation
                          4.68398 4.17567 4.08212 4.04124 2.148e-14
## Proportion of Variance 0.00321 0.00255 0.00244 0.00239 0.000e+00
## Cumulative Proportion 0.99262 0.99517 0.99761 1.00000 1.000e+00
```

Using the plot() function, we can also plot the variance explained by the first few principal components. plot(pr.out)





Note that the height of each bar in the bar plot is given by squaring the corresponding element of pr.out\$sdev. However, it is more informative to plot the PVE of each principal component (i.e., a scree plot) and the cumulative PVE of each principal component. This can be done with just a little work.

```
pve = 100*pr.out$sdev^2/sum(pr.out$sdev^2)
par(mfrow=c(1,2))
plot(pve, type="o", ylab = "PVE", xlab = "Principal Component", col="blue")
plot(cumsum(pve), type="o", ylab = "Cumulative PVE", xlab = "Principal Component", col="brown3")
                                                    100
     10
                                                    80
                                              Cumulative PVE
                                                    9
     9
                                                    9
                                                    20
     0
                                                                              50
           0
              10
                       30
                               50
                                                          0
                                                             10
                                                                      30
              Principal Component
                                                             Principal Component
```

Note that the elements of pve can also be computed directly from the summary, summary(pr.out)\$importance[2,], and the elements of cumsum(pve) are given by summary(pr.out)\$importance[3,].) We see that together, the first seven principal components explain around 40% of the variance in the data. This is not a huge amount of variance. However, looking at the scree plot, we see that while each of the first seven principal

components explain a substantial amount of variance, there is a marked decrease in variance explained by further principal components. That is, there is an *elbow* in the plot after approximately the seventh principal component. This suggests that there may be little benefit to examining more than seven or so principal components (though even examining seven principal components may be difficult).

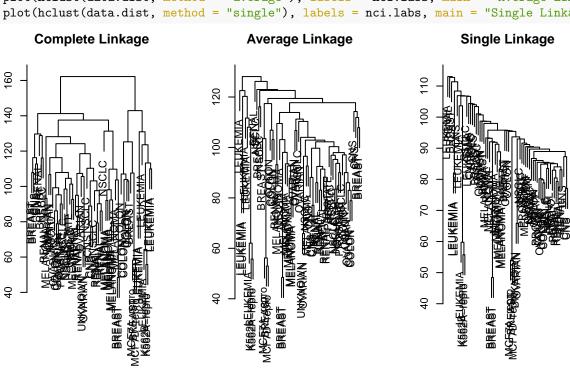
Clustering the Observations of the NCI60 Data

We now proceed to hierarchically cluster the cell lines in the NCI60 data, with the goal of finding out whether or not the observations cluster into distinct types of cancer. To begin, we standardize the variables to have a mean of zero and a standard deviation of one. As mentioned earlier, this step is optional and should be performed only if we want each gene to be on the same *scale*.

```
sd.data = scale(nci.data)
```

We now perform hierarchical clustering of the observations usign complete, average and single linkage. Euclidean distance is used as the dissimilarity measure.

```
par(mfrow = c(1,3))
data.dist = dist(sd.data)
plot(hclust(data.dist), labels = nci.labs, main = "Complete Linkage", xlab = "", sub = "", ylab = "")
plot(hclust(data.dist, method = "average"), labels = nci.labs, main = "Average Linkage", xlab = "", sub
plot(hclust(data.dist, method = "single"), labels = nci.labs, main = "Single Linkage", xlab = "", sub =
```



We see that the choice of linkage certainly does affect the results obtained. Typically, single linkage will tend to yield *trailing* clusters: very large clusters onto which individual observations attach one-by-one. On the other hand, complete and average linkage tend to yield more balanced, attractive clusters. For this reason, complete and average linkage are generally preferred to single linkage. Clearly, cell lines within a single cancer type do tend to cluster together, although the clustering is not perfect. We will use complete linkage hierarchical clustering for the analysis that follows.

We can cut the dendrogram at the height that will yield a particular number of clusters, say four:

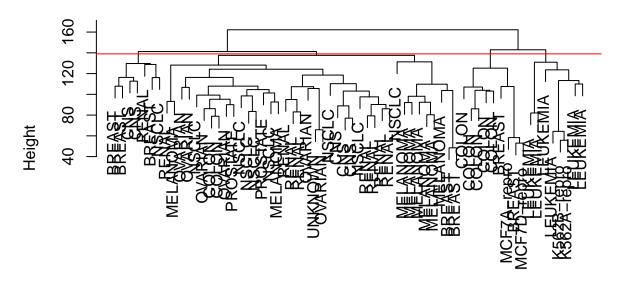
```
hc.out = hclust(dist(sd.data))
hc.clusters = cutree(hc.out, 4)
table(hc.clusters, nci.labs)
```

```
##
               nci.labs
## hc.clusters BREAST CNS COLON K562A-repro K562B-repro LEUKEMIA MCF7A-repro
##
                          3
              2
                      3
                          2
                                 0
                                               0
                                                            0
                                                                      0
                                                                                    0
##
              3
##
                      0
                          0
                                 0
                                               1
                                                            1
                                                                      6
                                                                                    0
                      2
                                 5
                                               0
                                                            0
                                                                      0
                                                                                    1
##
               nci.labs
  hc.clusters MCF7D-repro MELANOMA NSCLC OVARIAN PROSTATE RENAL UNKNOWN
##
##
              1
              2
                            0
                                      0
                                                     0
                                                               0
                                                                               0
##
                                             1
                                                                      1
##
              3
                            0
                                            0
                                                     0
                                                               0
                                                                      0
                                                                               0
                                            0
                                                     0
                                                                               0
##
```

There are some clear patterns. All the leukemia lines fall in cluster 3, while the breast cancer cell lines are spread out over three different clusters. We can plot the cut on the dendrogram that produces these four clusters.

```
par(mfrow=c(1,1))
plot(hc.out, labels = nci.labs)
abline(h=139, col="red")
```

Cluster Dendrogram



dist(sd.data) hclust (*, "complete")

The abline() function draws a stright line on top of any existing plot in R. The argument h=139 plots the horizontal line at height 139 on the dendrogram; this is the height that results in four distinct clusters. It is easy to verify that the resulting clusters are the same ones we obtained using cutree(hc.out, 4).

Printing out the output of hclust gives a useful brief summary of the object:

```
hc.out
##
## Call:
```

```
## hclust(d = dist(sd.data))
##
## Cluster method : complete
## Distance : euclidean
## Number of objects: 64
```

We claimed earlier that K-means clusterign and hierarchical clusterign with the dendrogram cut to obtain the same number of clusters can yield different results. How do these NCI60 hierarchical clustering results compare to what we get if we perform K-means clustering with K = 4?

```
set.seed(2)
km.out = kmeans(sd.data, 4, nstart=20)
km.clusters = km.out$cluster
table(km.clusters, hc.clusters)
```

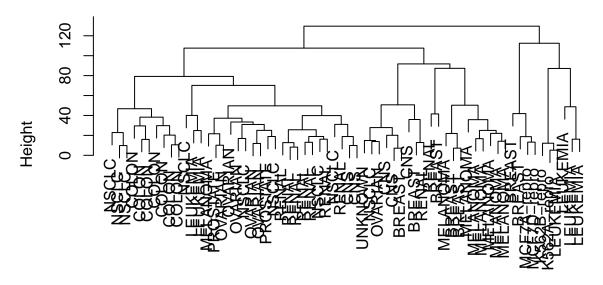
```
##
              hc.clusters
## km.clusters 1 2
                       3
##
             1 11
                       0
                   7
##
             2 20
                       0
                          0
             3
                9
                   0
                       0
                          0
##
                       8
##
               0
                   0
```

We see that the four clusters obtained using hierarchical clustering and K-means clustering are somewhat different. Cluster 4 in K-means clustering is identical to Cluster 3 in hierarchical clustering. However, the other clusters differ: for instance, Cluster 2 in K-means clustering contains a portion of the observations assigned to Cluster 1 by hierarchical clustering, as well as all of the observations to Cluster 2 by hierarchical clustering.

Rather than performing hierarchical clustering on the entire data matrix, we can simply perform hierarchical clustering on the first few principal component score vectors, as follows:

```
hc.out = hclust(dist(pr.out$x[,1:5]))
plot(hc.out, labels = nci.labs, main = "Hierarchical Clustering on \nFirst Five Score Vectors")
```

Hierarchical Clustering on First Five Score Vectors



dist(pr.out\$x[, 1:5]) hclust (*, "complete")

table(cutree(hc.out,4), nci.labs)

```
##
       nci.labs
##
        BREAST CNS COLON K562A-repro K562B-repro LEUKEMIA MCF7A-repro MCF7D-repro
                  2
##
              0
                          7
                                       0
                                                                2
                                                                                            0
      1
                                                     0
##
      2
              5
                  3
                          0
                                       0
                                                     0
                                                                0
                                                                              0
                                                                                            0
              0
                          0
                                                                                            0
      3
                  0
                                       1
                                                      1
                                                                4
                                                                              0
##
##
              2
                          0
                                       0
                                                                                            1
##
       nci.labs
        MELANOMA NSCLC OVARIAN PROSTATE RENAL
##
                                                    UNKNOWN
                       8
                                5
                                           2
                                                  7
##
      1
                7
                                           0
                                                  2
##
      2
                       1
                                1
                                                           1
##
      3
                0
                       0
                                 0
                                           0
                                                  0
                                                           0
                                                  0
##
```

Not surprisingly, these results are different from the ones that we obtained when we performed hierarchical clustering on the full dataset. Sometimes performing clustering on the first few principal components score vectors can give better results than performing clustering on the full data. In this situation, we might view the principal component step as one of denoising the data. We count perform K-means clustering on the first few principal component score vectors rather than the full dataset.