



# **Potential and natural output**

Alejandro Justiniano

Federal Reserve Bank of Chicago

Giorgio Primiceri

Northwestern University

National Bank of Belgium

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# Definitions

- Efficient output

- Level of output that would prevail under perfect competition

- Potential output

- Level of output that would prevail under imperfect competition, but flexible prices and wages and constant markups

- Natural output

- Level of output that would prevail under imperfect competition, but flexible prices and wages

# Why estimate **natural output**?

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- Actual output - natural output
  - Importance of nominal rigidities
  
- Potential output - natural output
  - Exogenous markup variation in prices and wages
  - Monetary policy inflation-output trade-off
  
- If markup shocks are interpreted as tech. or preference
  - Natural = potential

# Model economy

Shocks to preferences  
and technology

Shocks to the degree of  
market competitiveness

**Sticky Prices and Wages**

Habit formation

Etc

**Observed Output**

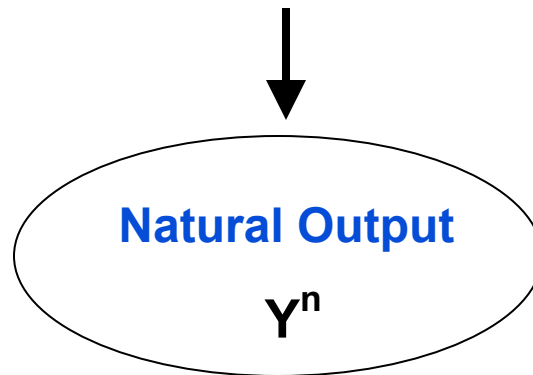
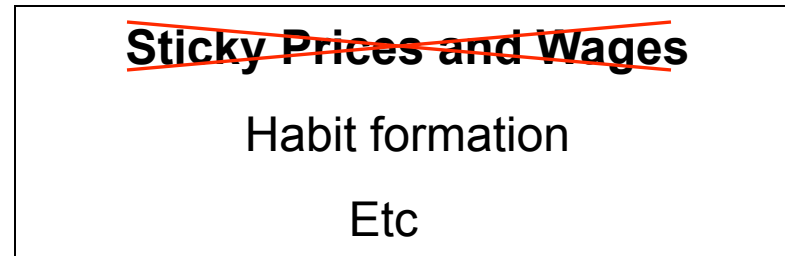
**Y**



# Model economy under **flex prices/wages**

Shocks to preferences  
and technology

Shocks to the degree of  
market competitiveness



**Natural** = level of output that would be observed under imperfectly competitive markets and flexible prices and wages

# Model economy under **flex prices/wages** and **no markup shocks**

Shocks to preferences  
and technology

~~Shocks to the degree of  
market competitiveness~~

~~Sticky Prices and Wages~~

Habit formation

Etc

**Potential Output**

$Y^p$

**Potential** = level of output that would be observed under imperfect competition, but flexible prices and wages and constant markups

# Preview of the results



- Potential output is smooth

- More modest business cycles had markets been competitive
- Large portion of fluctuations are inefficient
- Gap resembles “standard” measures of BC

- Natural output is implausibly volatile

- Casts doubts on structural interpretation of innovations in price and wage Phillips curves

# Outline



- Model
- Estimates of *potential* output
  - What is the share of inefficient fluctuations?
- A brief comparison to the literature
- Estimates of *natural* output
- Alternative interpretation of *markup shocks*



# The model



- NK model with exogenous capital accumulation
- 5 blocks:
  - Intermediate firms
  - Final-good producers
  - Households
  - Employment agencies
  - Policy makers

# The model

- Production technology of final-good producers

$$Y_t = \left[ \int_0^1 Y_t(i)^{\frac{1}{1+\lambda_{p,t}}} di \right]^{1+\lambda_{p,t}}$$

# The model

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price markup shock

# The model

- Production technology of intermediate-goods producers

$$Y_t(i) = A_t L_t(i)^\alpha$$

- Monopolistically competitive markets
- Optimizing firms set prices by maximizing PDV of profits
- Calvo type stickiness: a fraction  $\xi_p$  of firms cannot re-optimize
  - index prices to ss and past inflation

# The model

- Households maximization problem

$$E_0 \sum_{t=0}^{\infty} \beta^t b_t \left[ \log (C_t - hC_{t-1}) - \varphi \frac{L_t^{1+\nu}}{1+\nu} \right]$$

subject to

$$P_t C_t + T_t + B_t \leq R_{t-1} B_{t-1} + Q_t(i) + \Pi_t + W_t(i) L_t(i)$$

- Monopolistically competitive suppliers of specialized labor
- Calvo-type stickiness: a fraction  $\xi_w$  of HH cannot re-optimize
  - index wages to ss and past inflation-productivity

# The model

- **Employment agencies** aggregate differentiated labor into homogeneous labor

$$L_t = \left[ \int_0^1 L_t(i)^{\frac{1}{1+\lambda_{w,t}}} di \right]^{1+\lambda_{w,t}}$$

← wage markup shock

# The model

- **Monetary policy** sets the short-term nominal interest rate following a Taylor-type rule

$$\frac{R_t}{R} = \left( \frac{R_{t-1}}{R} \right)^{\rho_R} \left[ \left( \frac{\bar{\pi}_{t-3,t}}{\pi_t^*} \right)^{\phi_\pi} \left( \frac{Y_t / Y_{t-4}}{e^\gamma} \right)^{\phi_y} \right]^{1-\rho_R} \mathcal{E}_{R,t}$$

# Exogenous disturbances

## ■ Tastes & technology

- Productivity → growth rate is AR(1)
- Inter-temporal preference shock → AR(1)

## ■ Shocks to markets competitiveness

- Mark-up shock in wages → *i.i.d.*
- Mark-up shock in prices → *i.i.d.*

## ■ Monetary policy

- MP shocks → *i.i.d.*
- Inflation target shock → persistent AR(1)



# Data



- Observable variables
  1. GDP
  2. Hours
  3. Wages
  4. Inflation
  5. Federal funds rate
  
- Quarterly data from 1954:III to 2006:II

# Data



- Observable variables

1. GDP
2. Hours → Total hours / population 22-64 age (Francis-Ramey)
3. Wages → Compensation of employees (NIPA) / total hours
4. Inflation
5. Federal funds rate

- Quarterly data from 1954:III to 2006:II

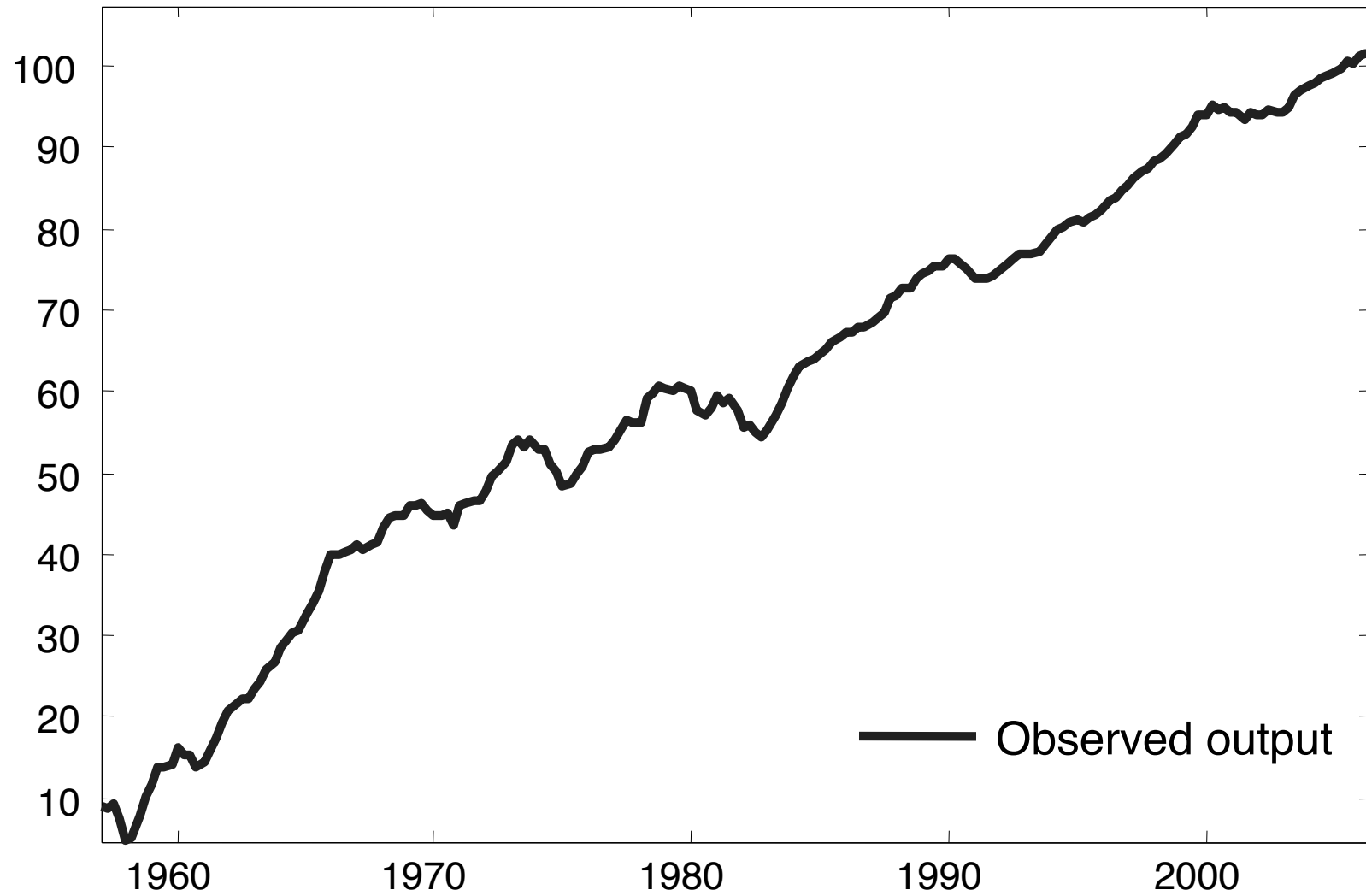
# Why this model



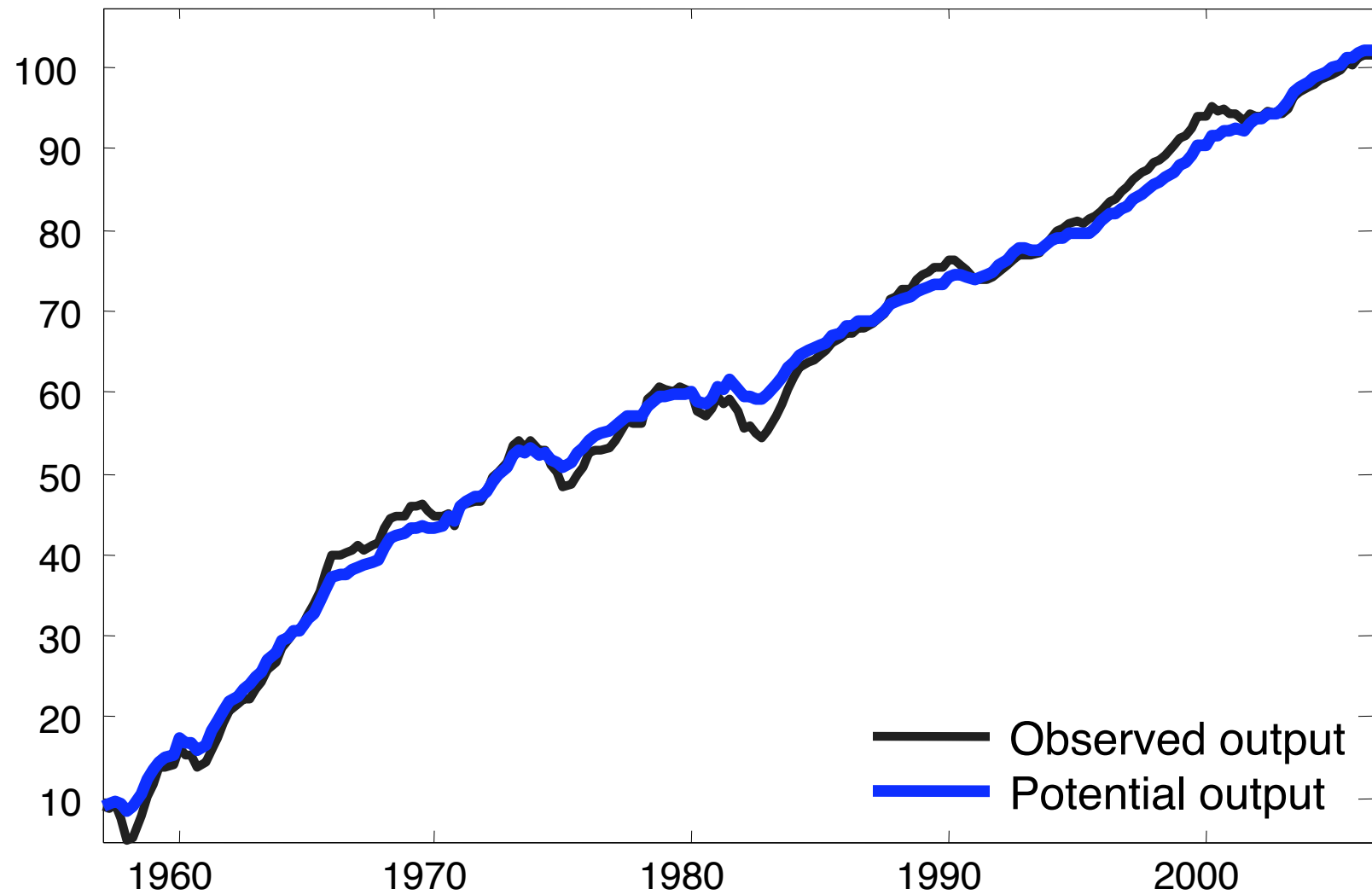
Relative to simplest NK framework

- Additional frictions
  - Habits and indexation
  
- Sticky wages
  - Output gap  $\neq$  real marginal cost
  
- Wages and hours observable
  - Labor share is observable (as in Sbordone, Gali & Gertler)
  - Productivity is observable → make contact with RBC

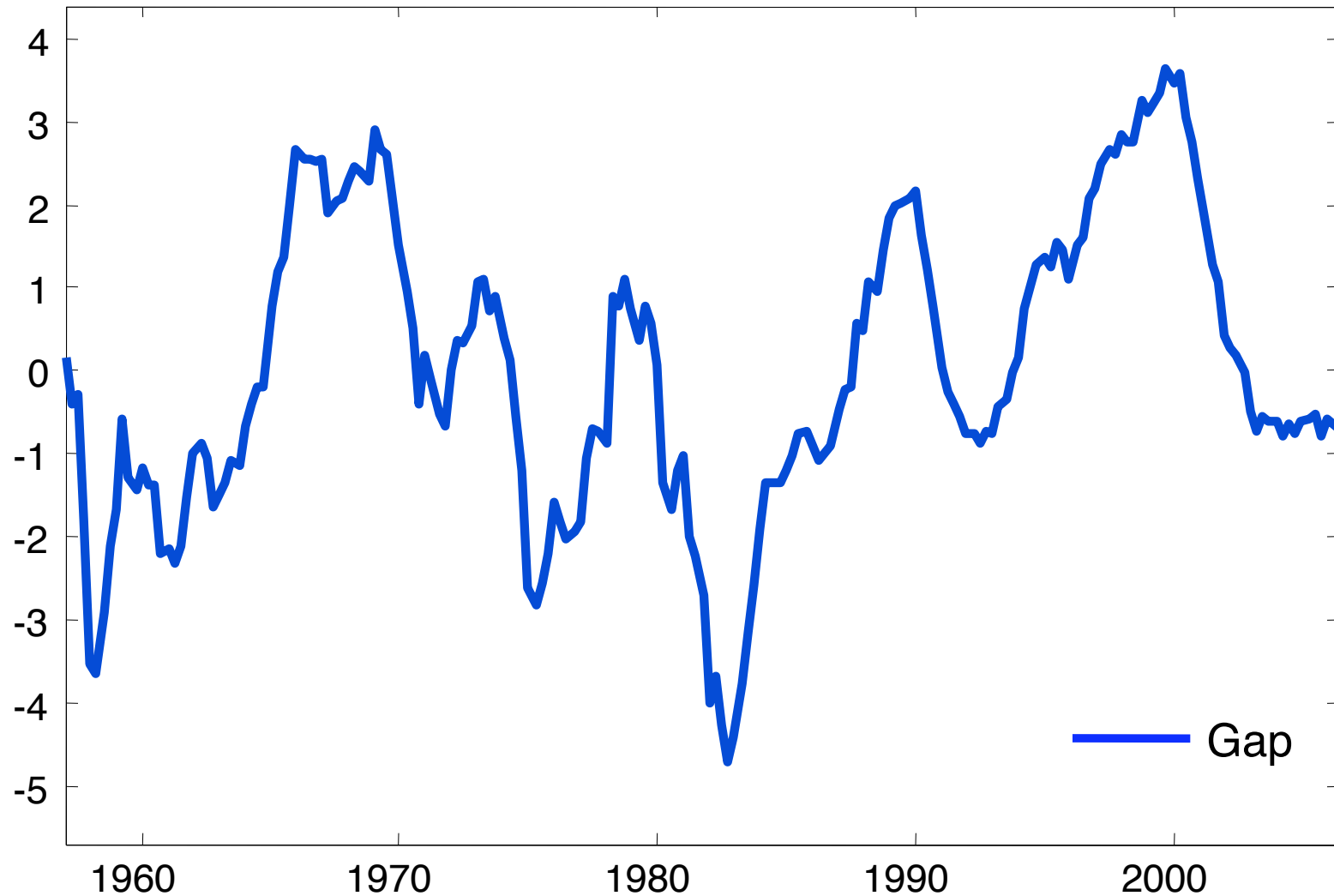
# Output



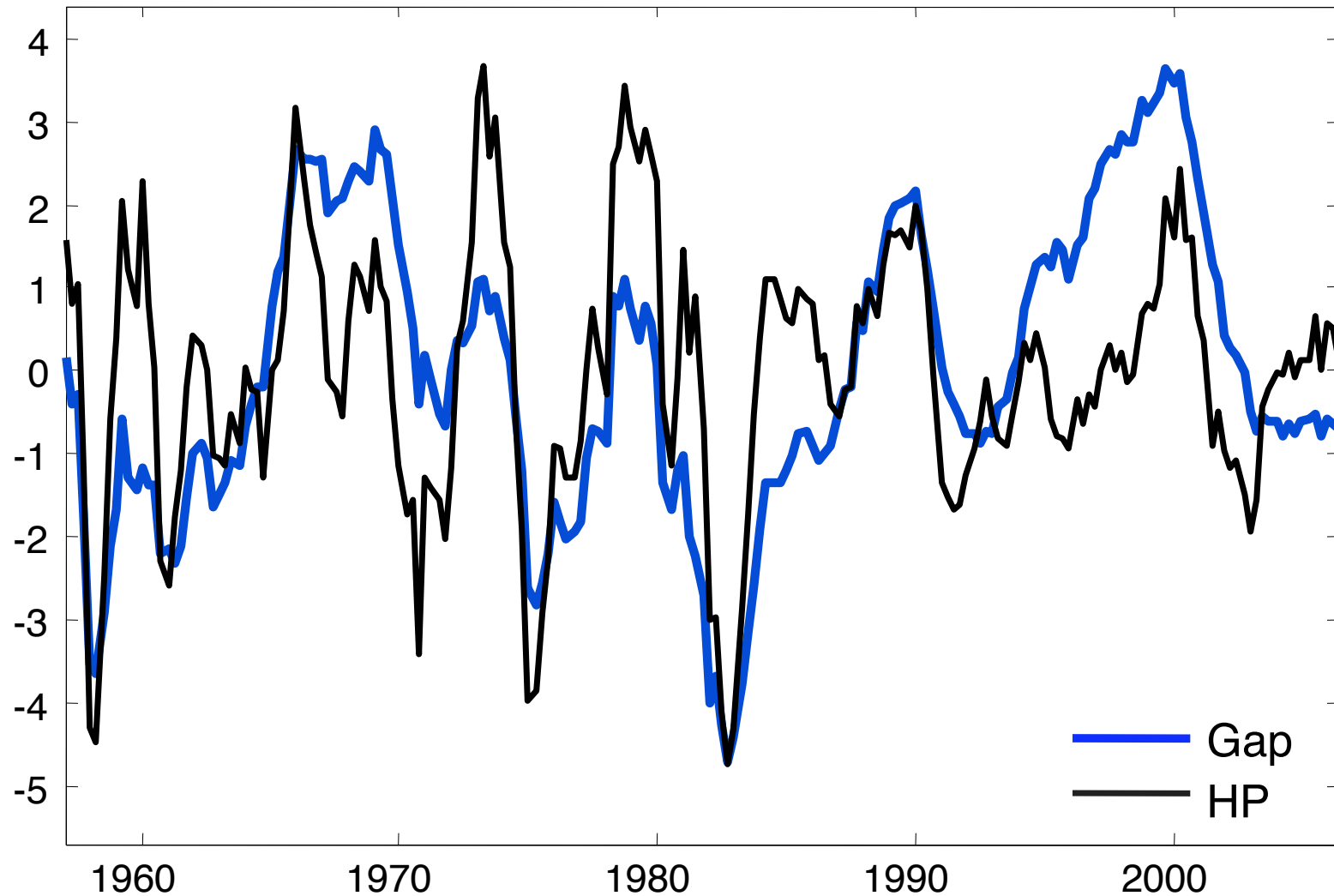
# Potential Output



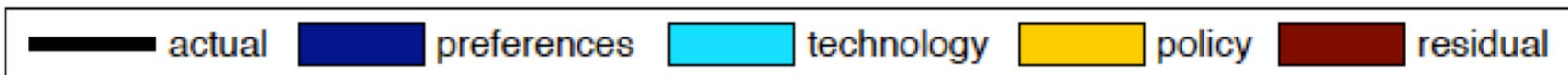
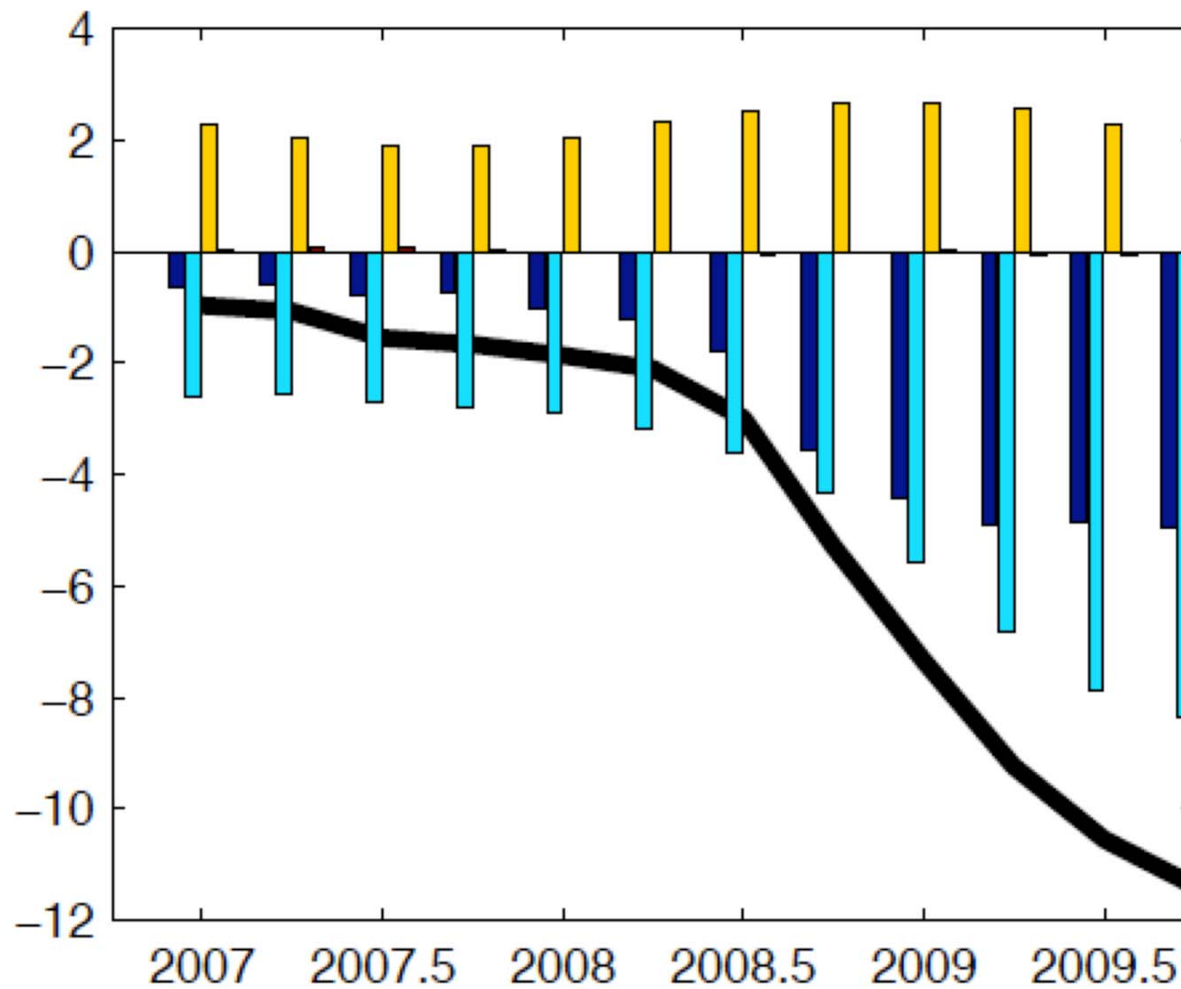
# Output Gap and Business Cycles



# Output Gap and Business Cycles

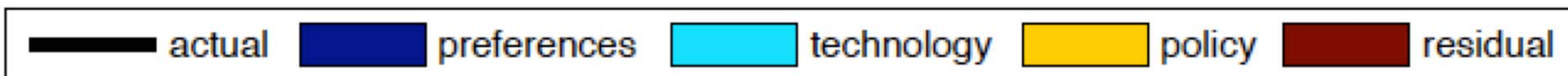
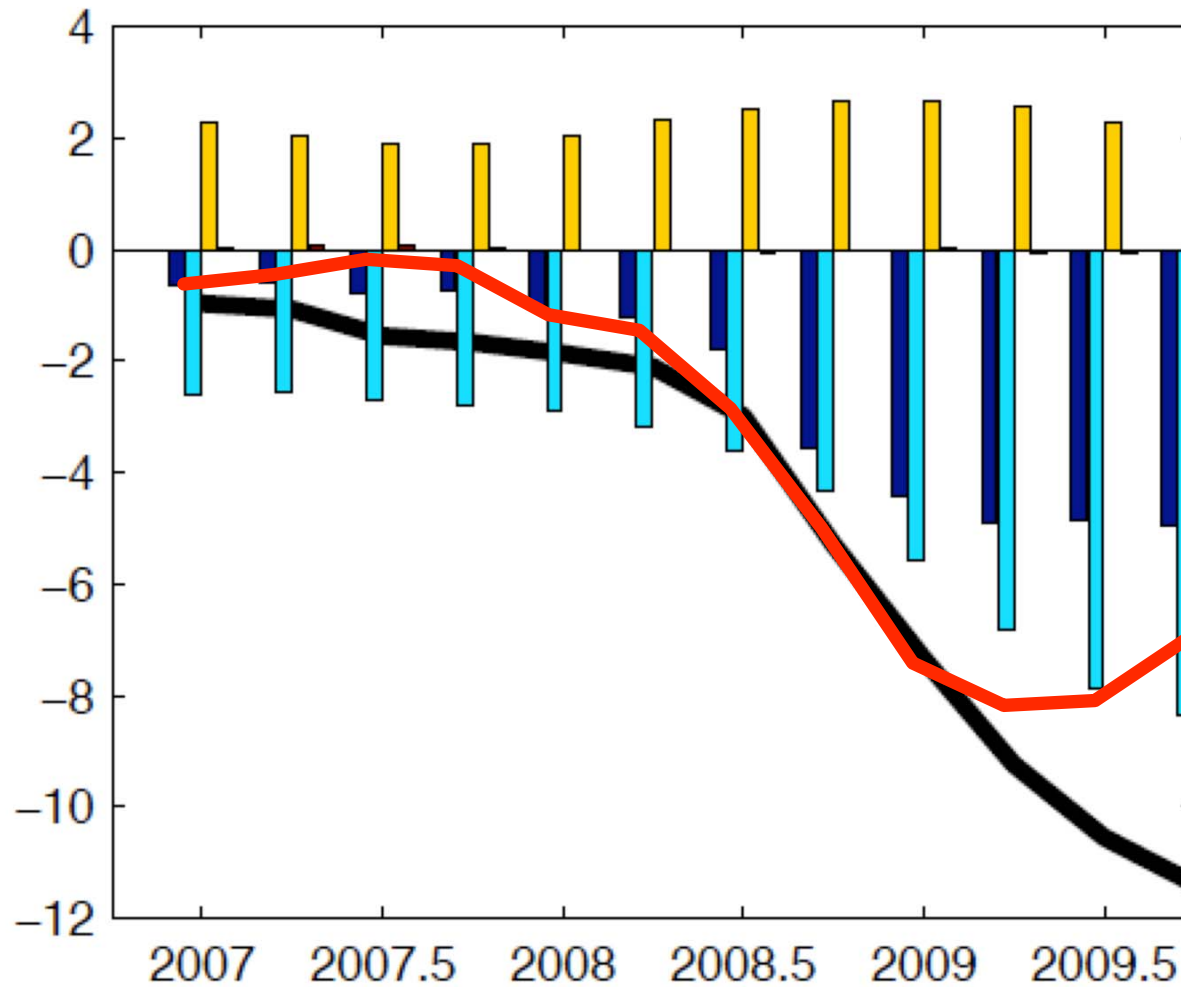


## Most recent estimates of the output gap

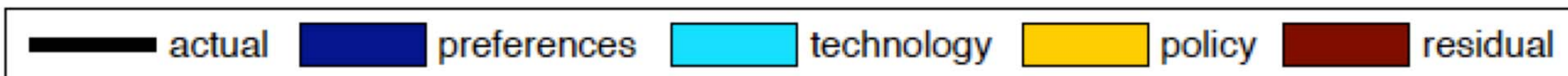
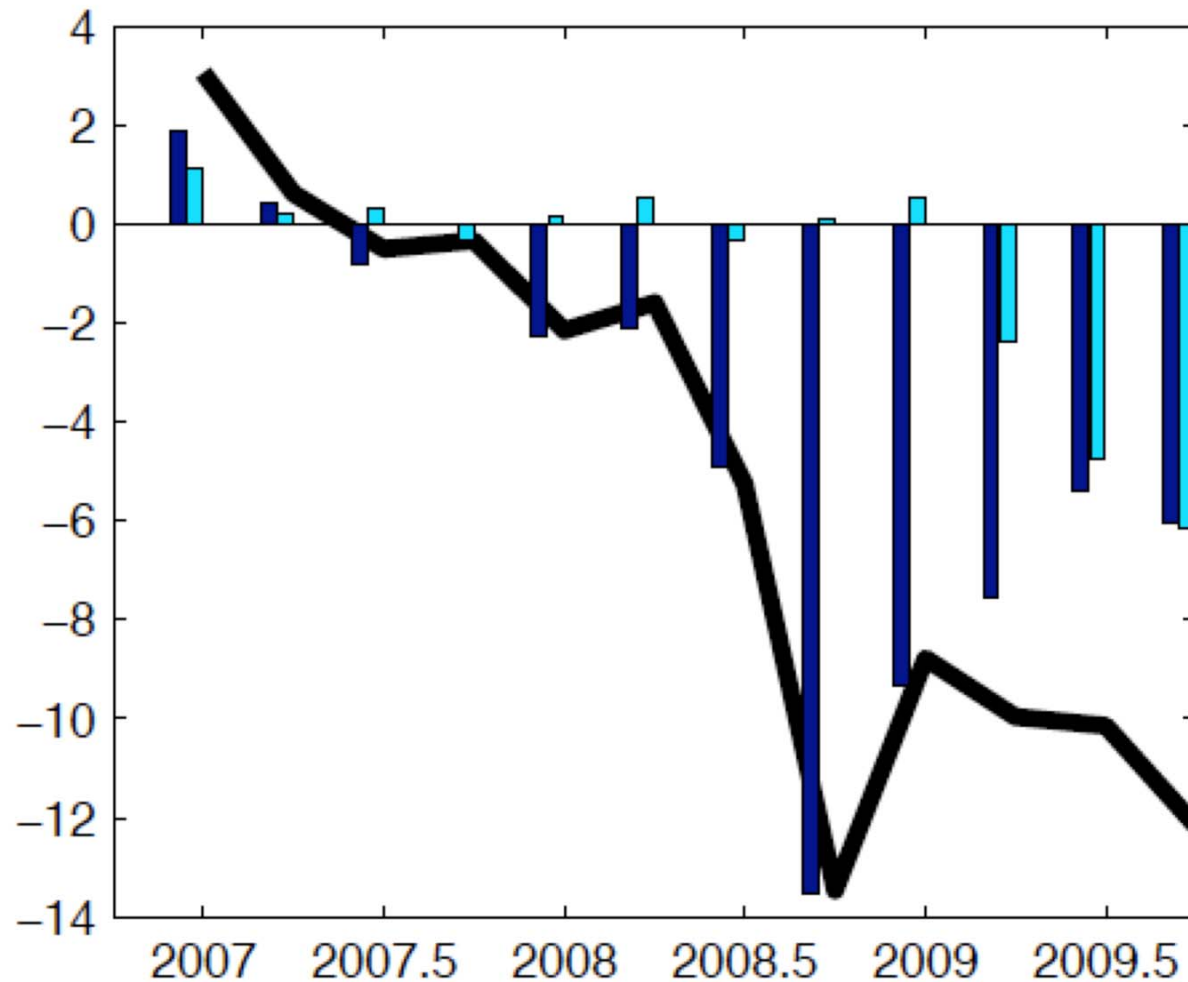




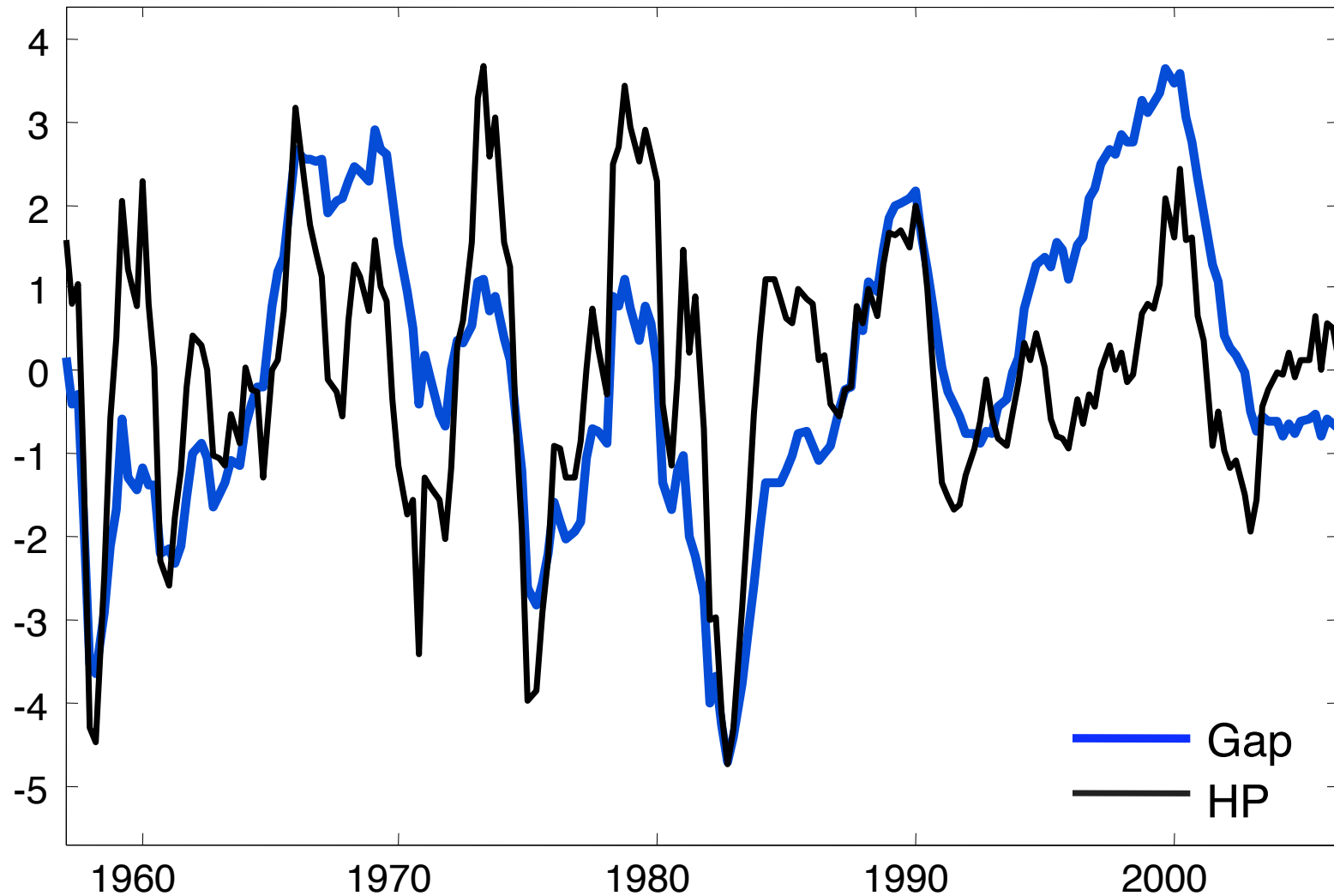
## Most recent estimates of the output gap



## Most recent estimates of the Equilibrium RIR



# Output Gap and Business Cycles



# How inefficient are BC fluctuations?

- A useful decomposition

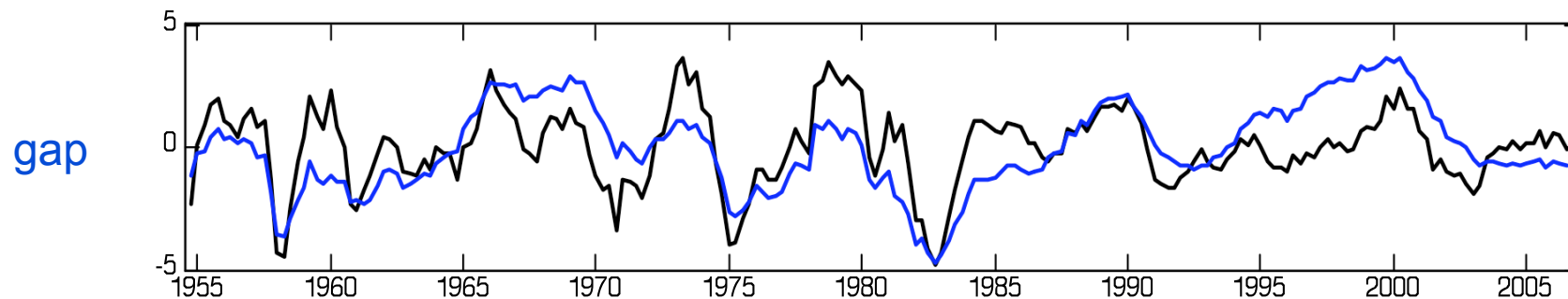
$$\underbrace{y_t - y_t^{hp}}_{\text{BC}} =$$

# How inefficient are BC fluctuations?

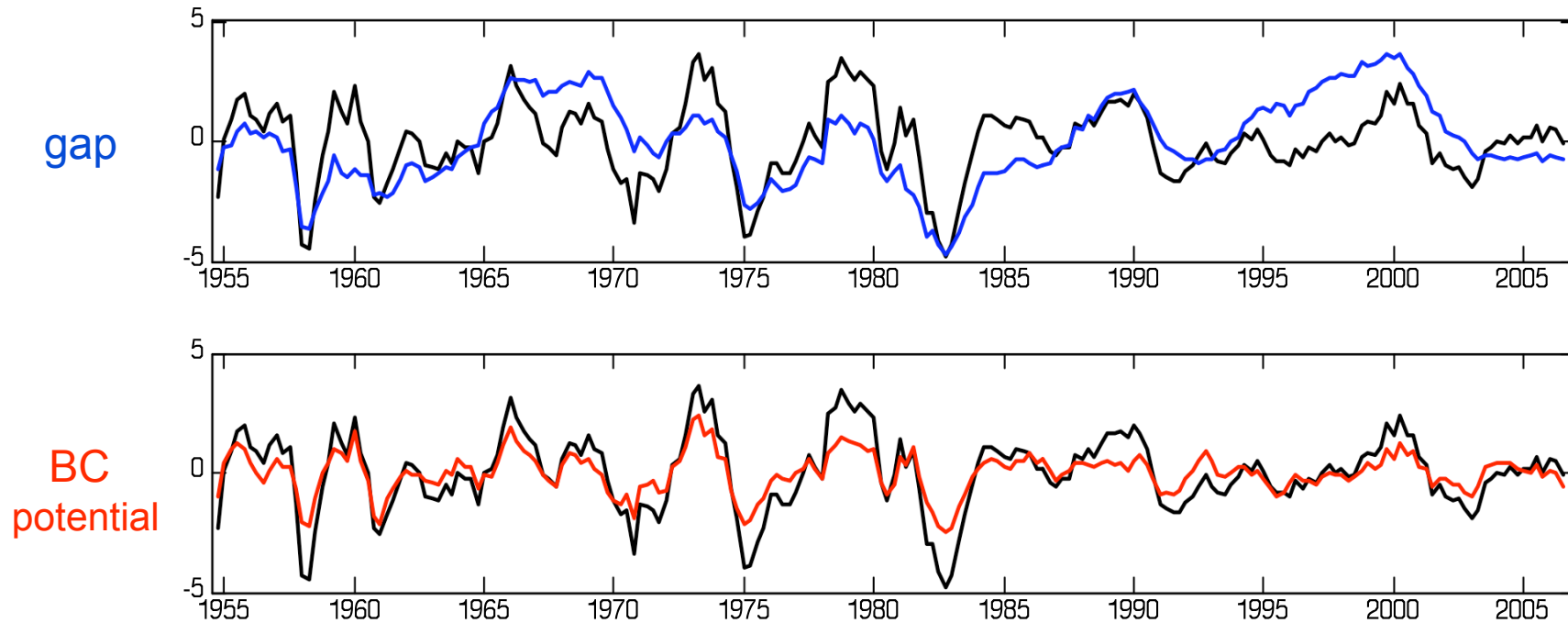
- A useful decomposition

$$\underbrace{y_t - y_t^{hp}}_{\text{BC}} = \underbrace{y_t - y_t^*}_{\text{output gap}} + \underbrace{y_t^* - y_t^{*hp}}_{\text{"BC for potential"}} + \underbrace{y_t^{*hp} - y_t^{hp}}_{\Delta \text{ in HP trends}}$$

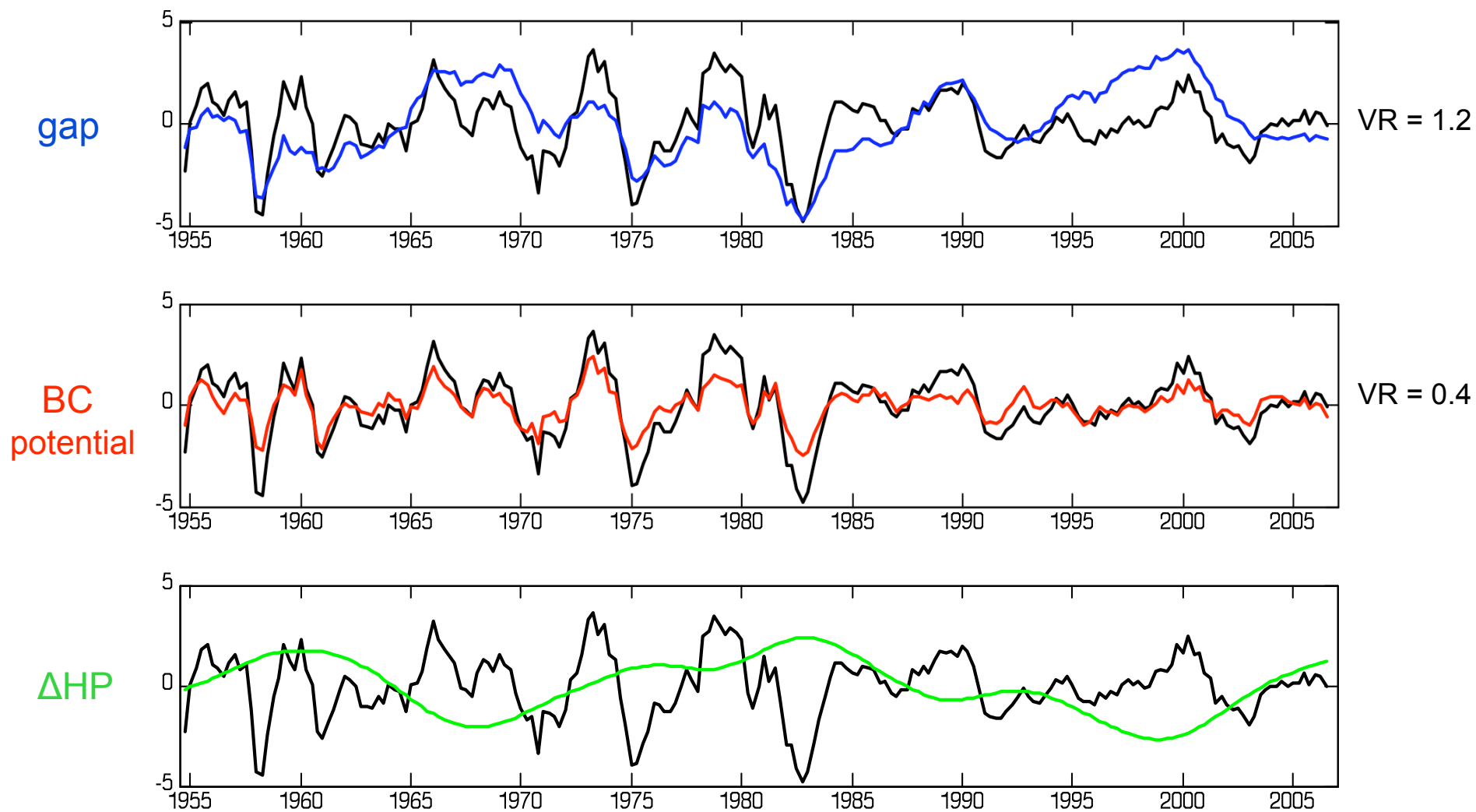
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# How inefficient are BC fluctuations?





# Potential output and business cycles



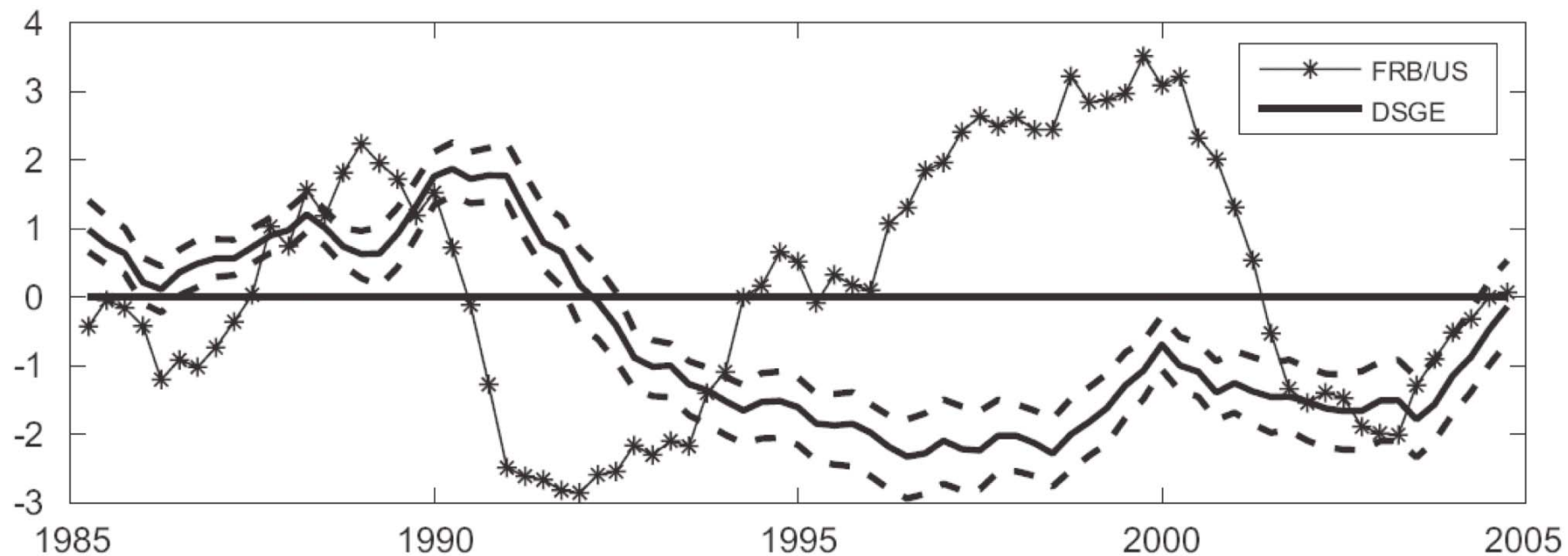
- DSGE-gap resembles “standard” measures of BC
- This result is not typical in the literature

# **“Going after” (a subset of) the literature**

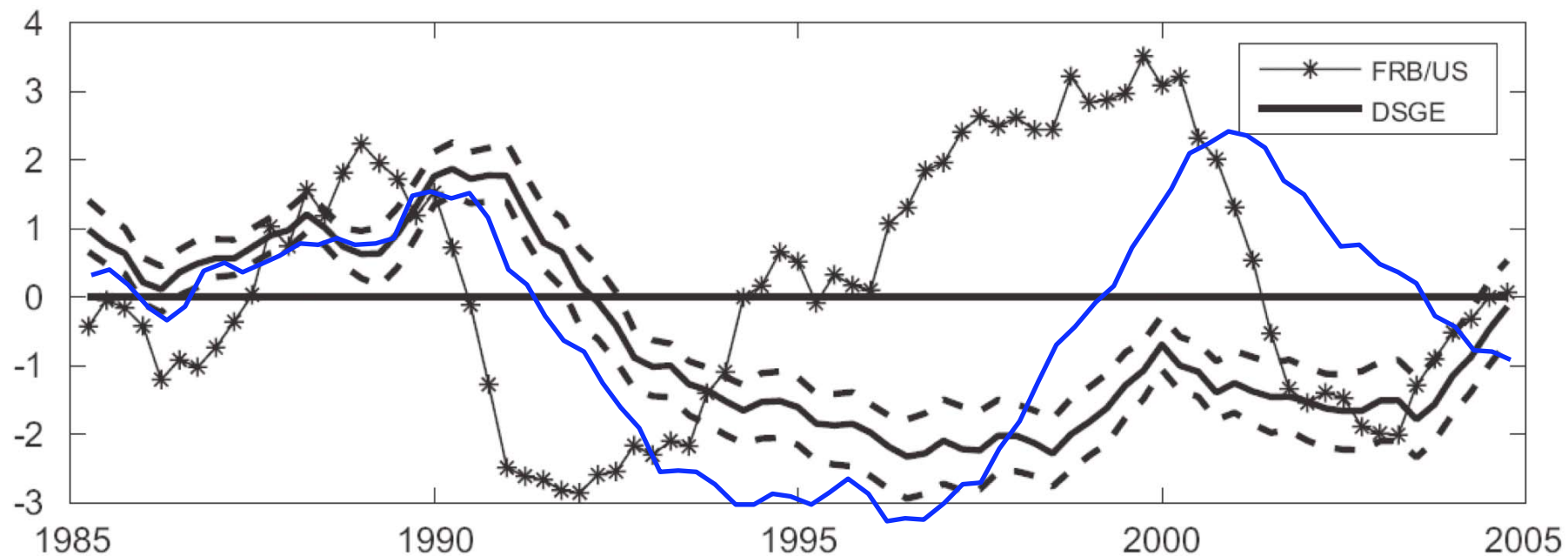
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- Output gap estimates differ from standard measures
  - Edge, Kiley and Laforte (2008)
  - Levin, Onatski, Williams and Williams (2005)
  - Andrés, López-Salido and Nelson (2005)

# Edge, Kiley and Laforge (2008)

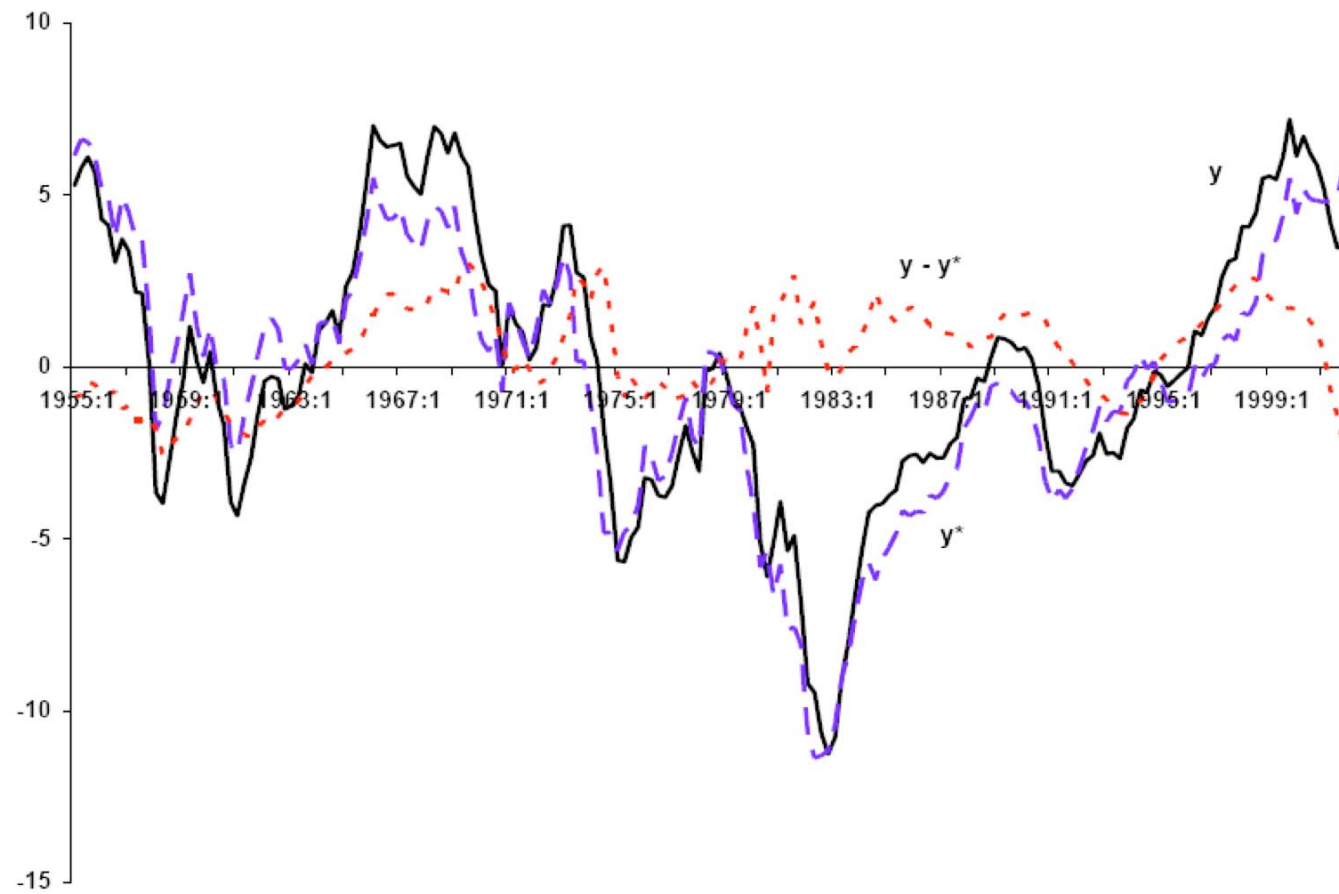


# Edge, Kiley and Laforge (2008)

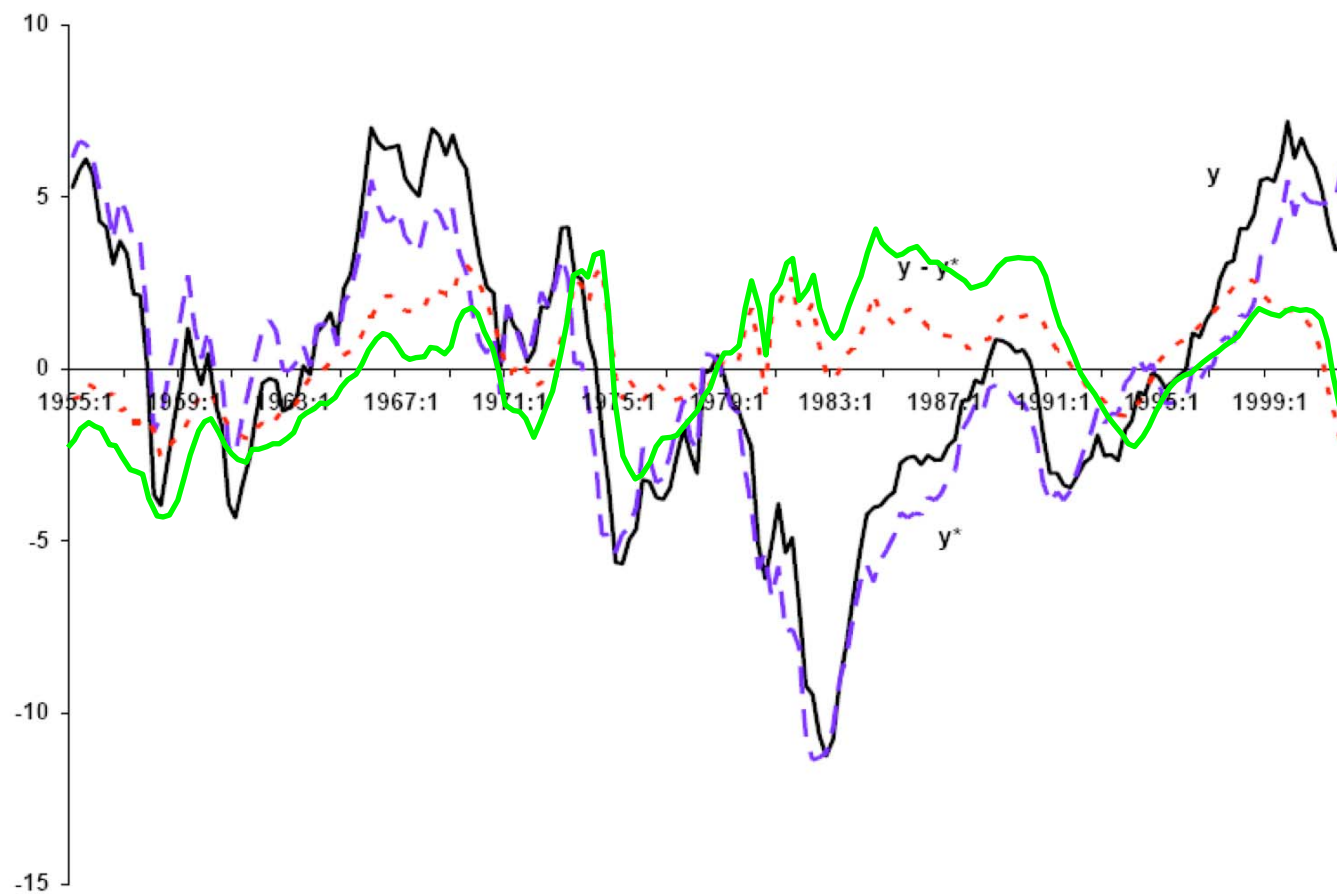


— “Our” gap without  $\pi^*$

# LOWW (2005)

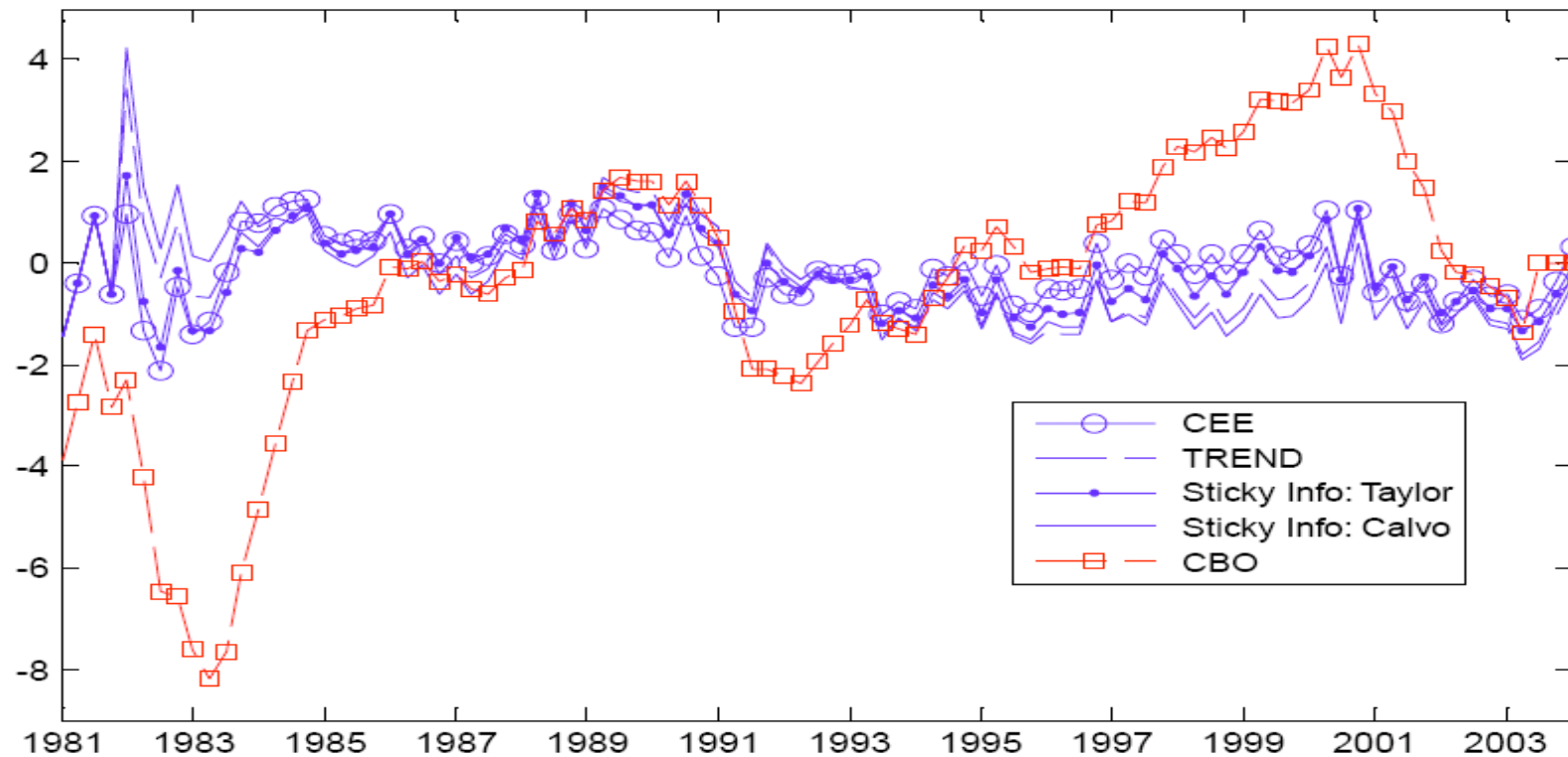


# LOWW (2005)

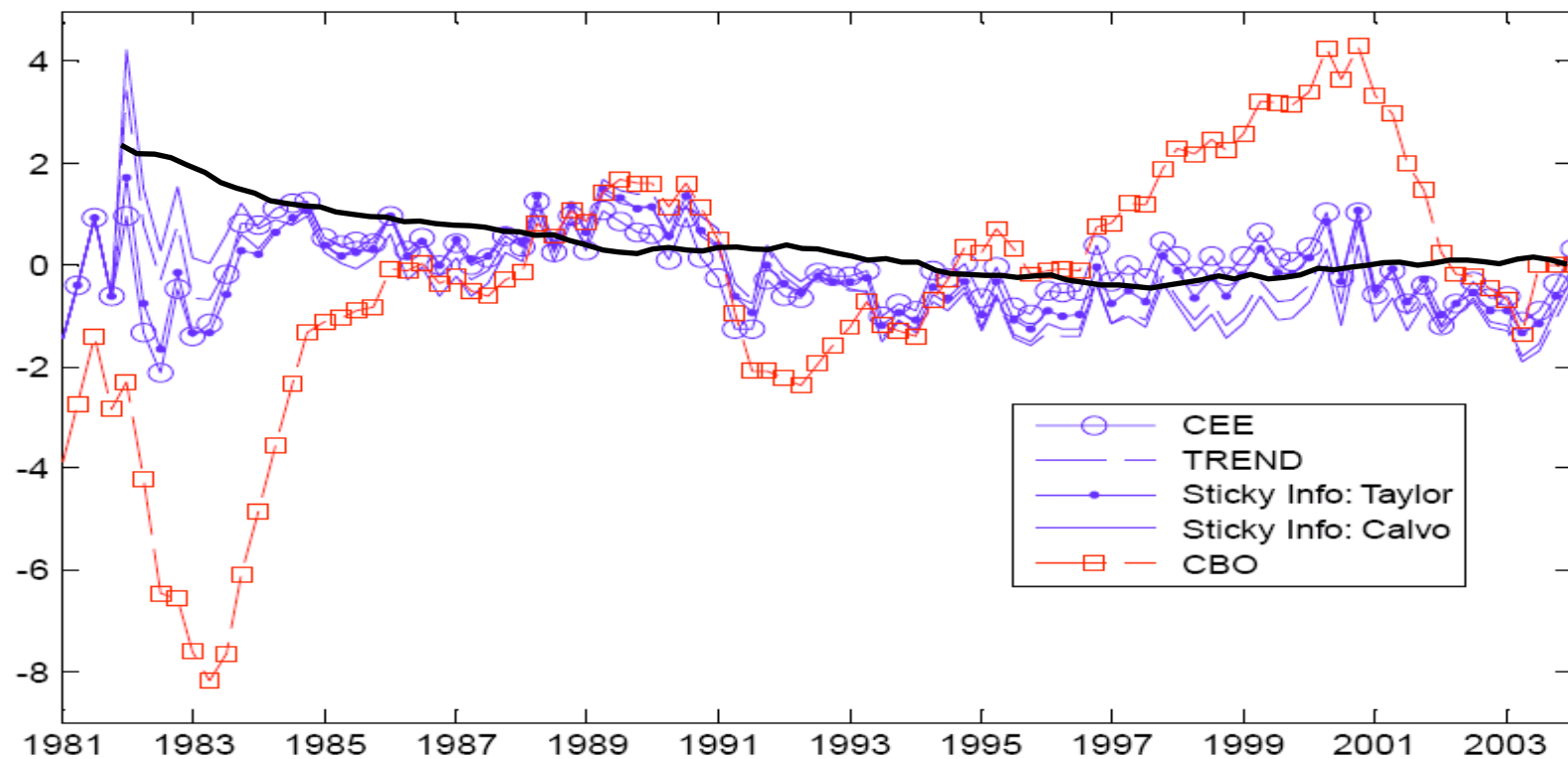


— “Our” gap with LOWW dataset and policy rule

# Andrés, López-Salido and Nelson (2005)



# Andrés, López-Salido and Nelson (2005)



— “Our” gap without *markup shocks*



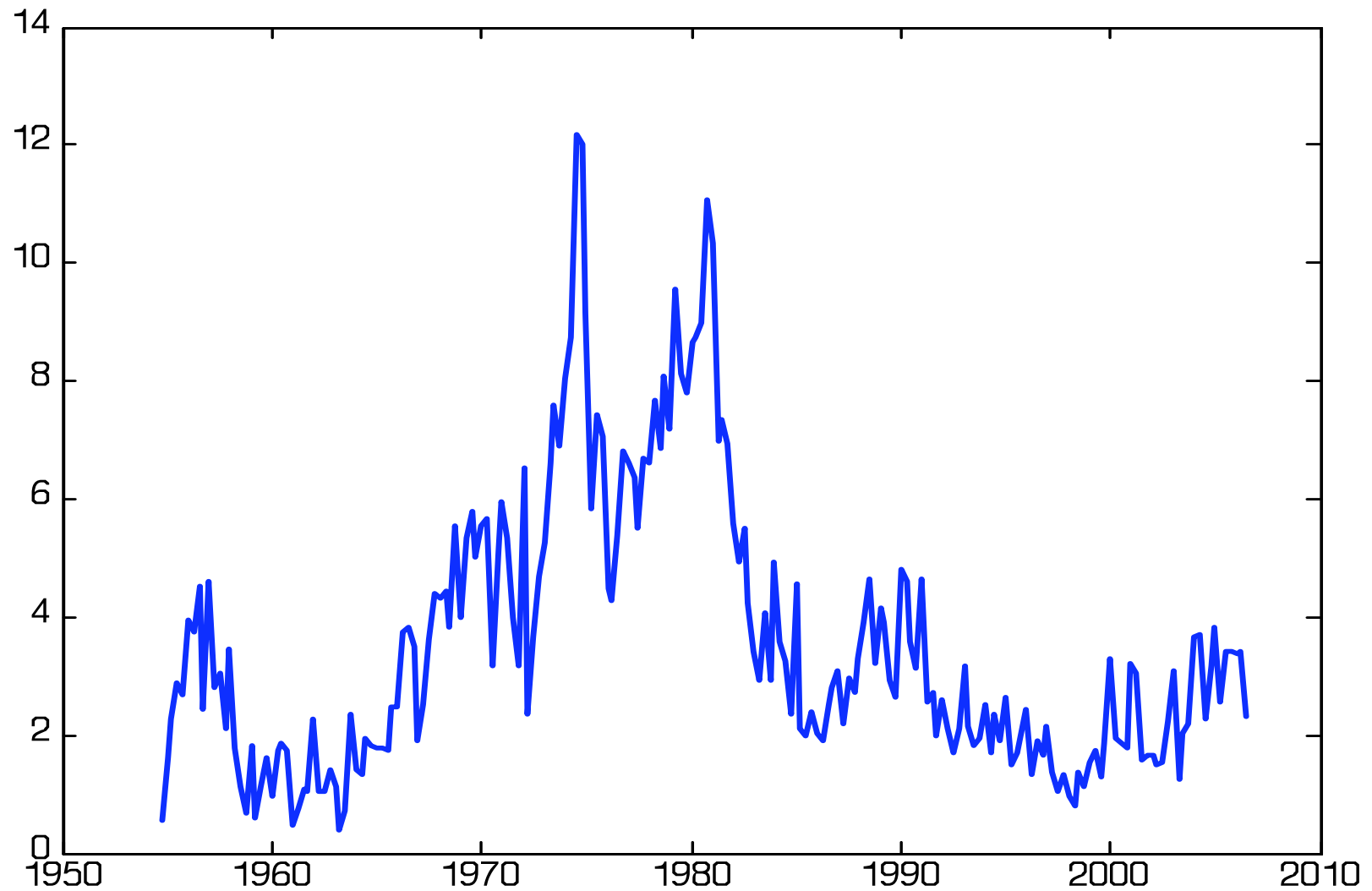
# Importance of shocks to Phillips curve

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- Simplest Phillips curve

$$\pi_t = \beta E_t \pi_{t+1} + \kappa g_t + \lambda_{p,t}$$

# US inflation (GDP deflator)



# Importance of shocks to Phillips curve

- Simplest Phillips curve

$$\pi_t = \beta E_t \pi_{t+1} + \kappa g_t + \lambda_{p,t}$$

- If no shocks to Phillips curve

- ☐ Gap forced to explain high frequency variation in inflation
- ☐ Need low price stickiness
- ☐ Potential output  $\approx$  actual output

# Why the mix of shocks matters

- Gap resembles economic slack if choose shocks to appropriately account for low & high frequency fluctuations in data

Shock	Purpose
Labor supply	Hours, low frequency
Inflation Target	Inflation, low frequency
Price markup	Inflation, high frequency
Wage markup	Wages, high frequency

- **Rationale**: 1) model fits better 2 ) proxies for features outside model's scope, i.e. reduced form shocks

# **“Going after” (a subset of) the literature**

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- Output gap estimates differ from standard measures
  - Edge, Kiley and Laforte (2008)
  - Levin, Onatski, Williams and Williams (2005)
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- One exception: Sala, Soderstrom and Trigari (2008)

# Potential output and business cycles

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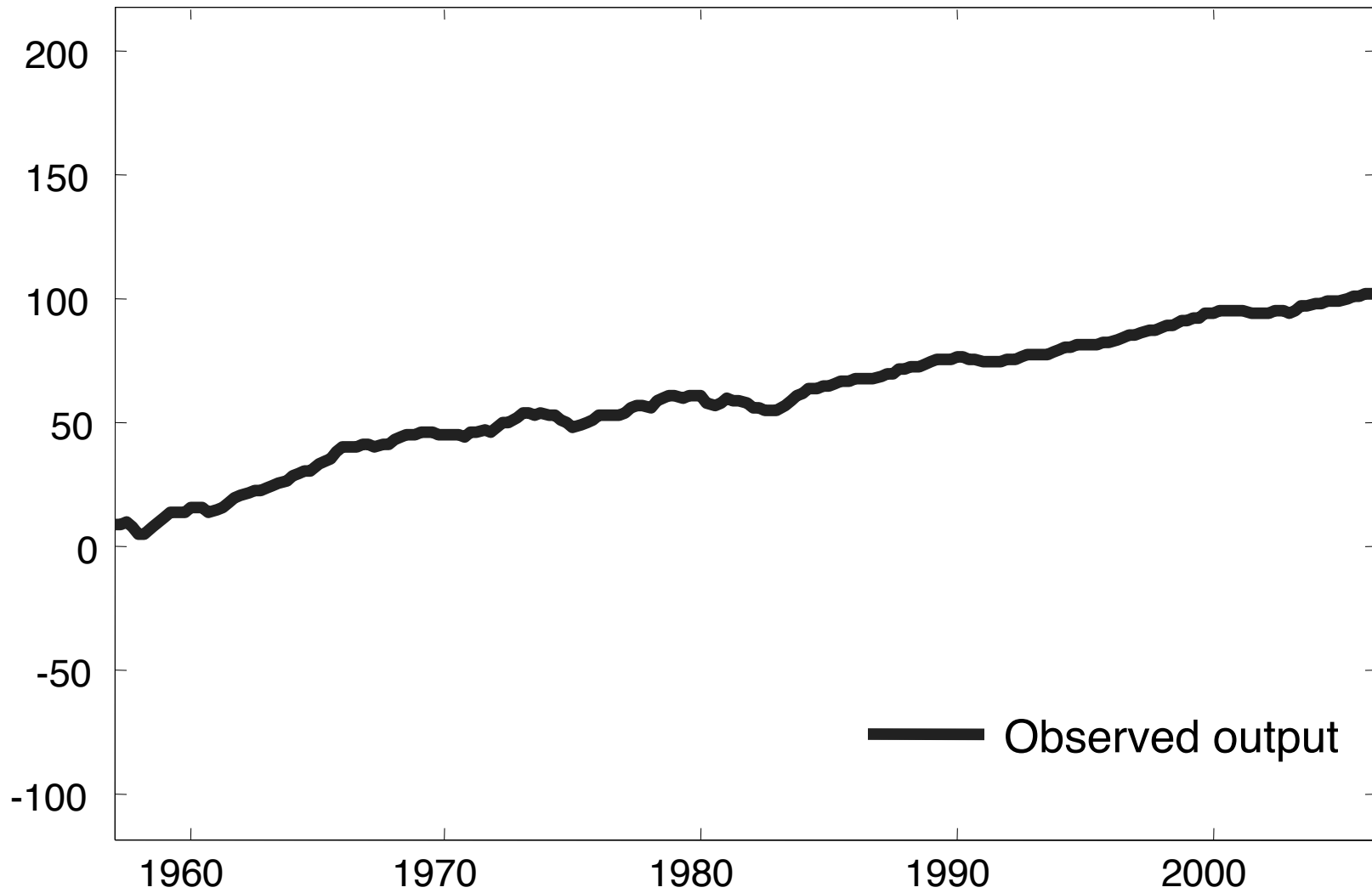
- DSGE-gap resembles “standard” measures of BC
- This result is not typical in the literature
- One important ingredient:
  - Shocks to Phillips curve

# Outline



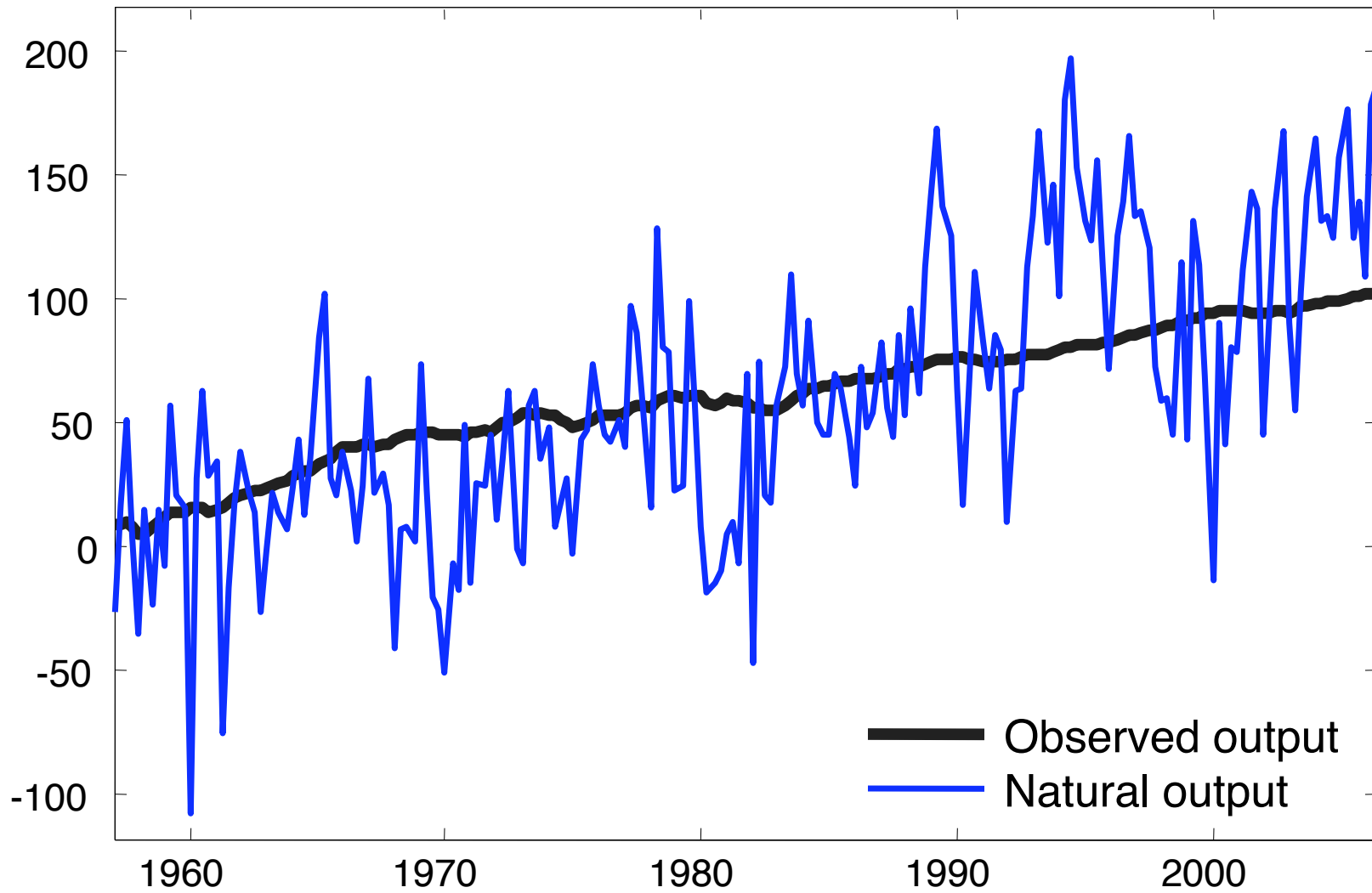
- Model
- Estimates of *potential* output
- A brief comparison to the literature
- Estimates of *natural* output
- Alternative interpretation of markup shocks

# Output





# Natural Output



# Why is natural output so volatile?

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- Wage markup shocks are implausibly volatile
  - Imply variation of desired markups between  $-/+ 400\%$

# Why is natural output so volatile?

- Wage markup shocks are implausibly volatile

➤ Imply variation of desired markups between -/+ 400%

$$w_t = \gamma_1 w_{t-1} + \gamma_2 E_t w_{t+1} + \kappa \mu_t^w + \kappa \lambda_{w,t}$$

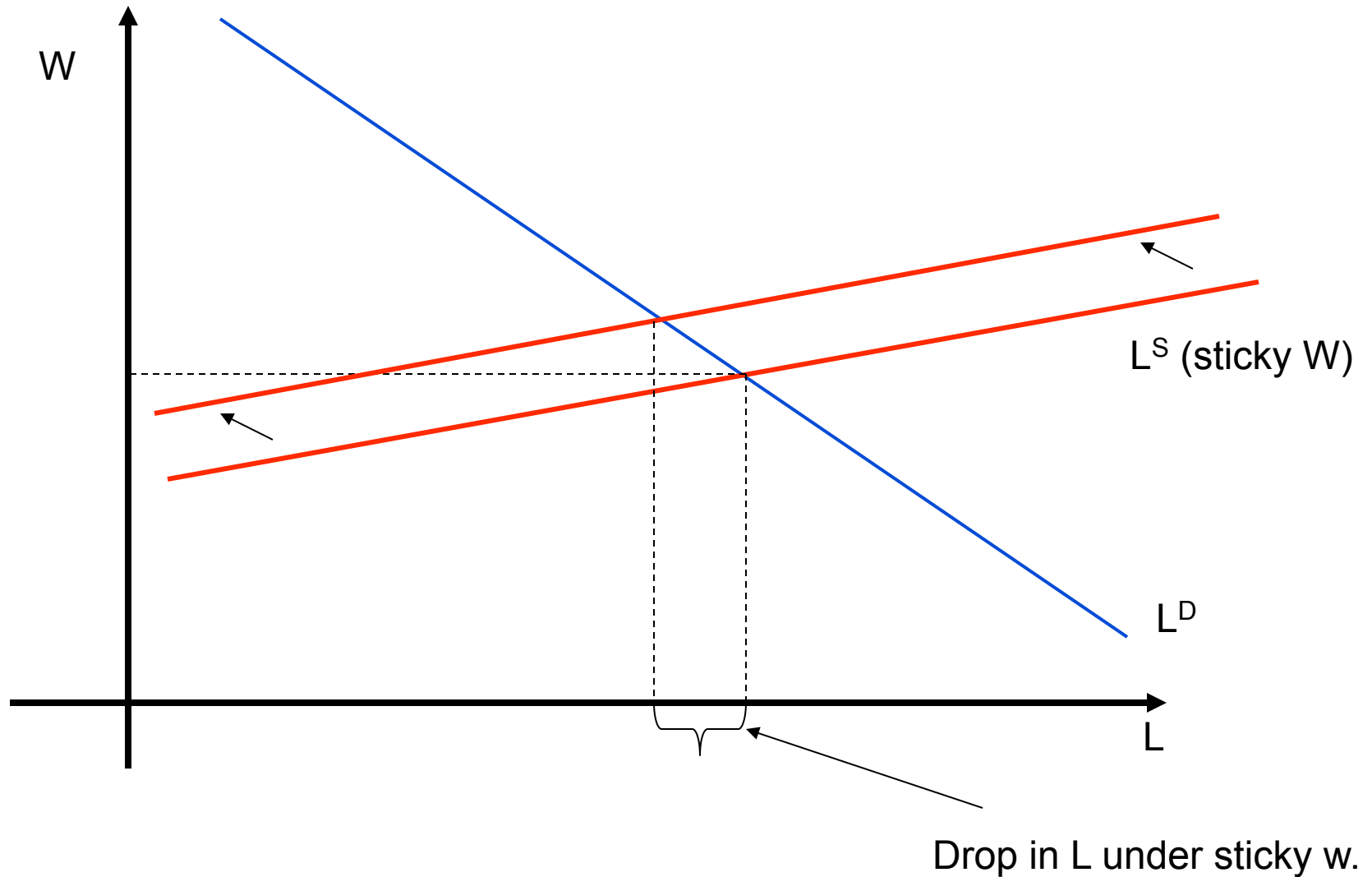
Std  $\approx$  30 basis points

# Why is natural output so volatile?

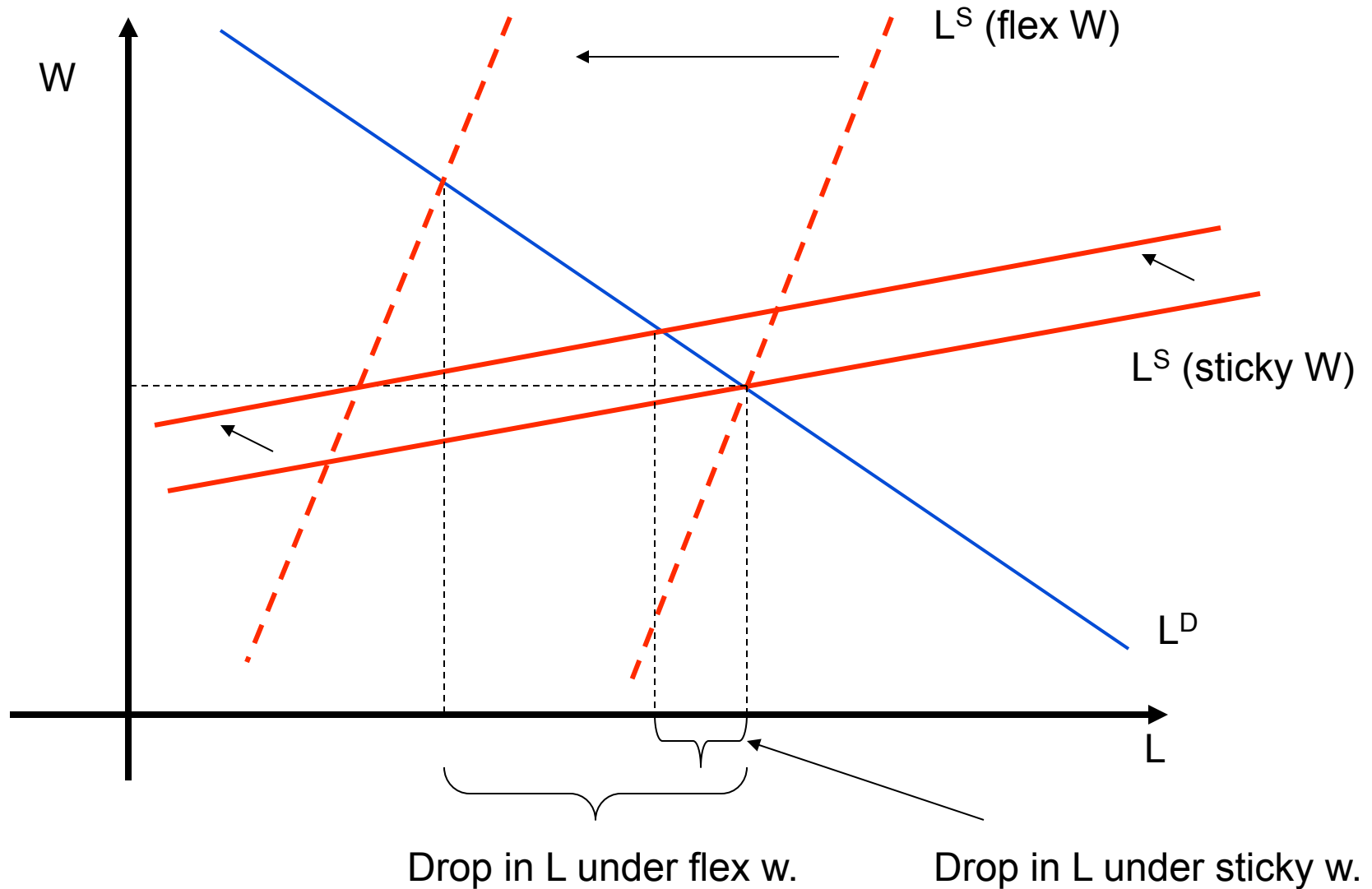
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- Wage markup shocks are implausibly volatile
  - Imply variation of desired markups between  $-/+ 400\%$
  - Why “not a problem” under sticky wages?

# The effect of wage markup shocks



# The effect of wage markup shocks

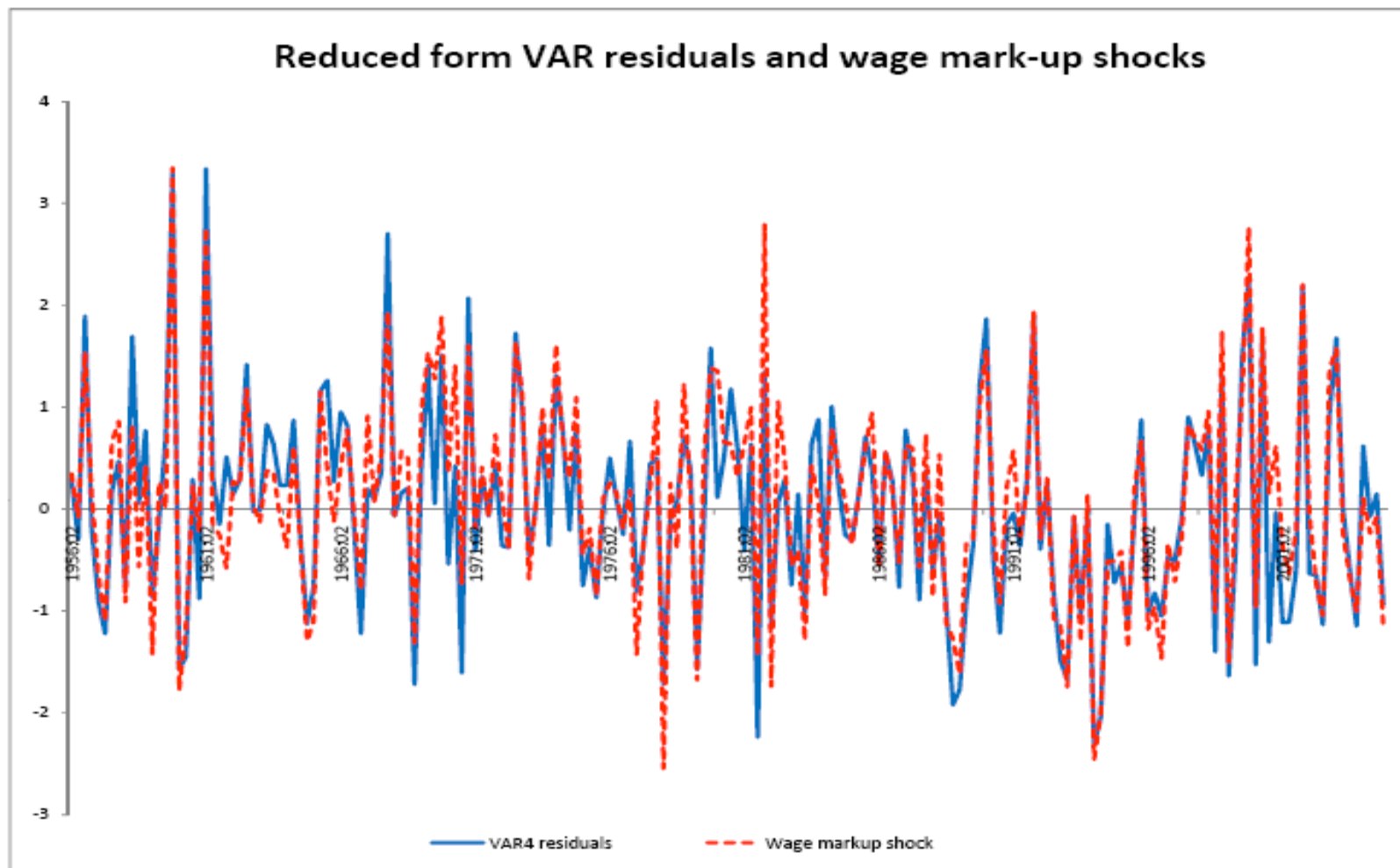


# Wage markup shocks

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- Are these shocks plausible?
  - Model misspecification?
  - Coincide with reduced form residuals from VAR(4)

# Wage markup shocks





# Wage markup shocks

---

- Are these shocks plausible?
  - Model misspecification?
  - Coincide with reduced form residuals from VAR(4)
- Variance decomposition at BC frequencies
  - Explain negligible share of variance in all series but wages
    - 2% output, 5% hours

# Outline



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- A brief comparison to the literature
- Estimates of *natural* output
- Alternative interpretation of markup shocks

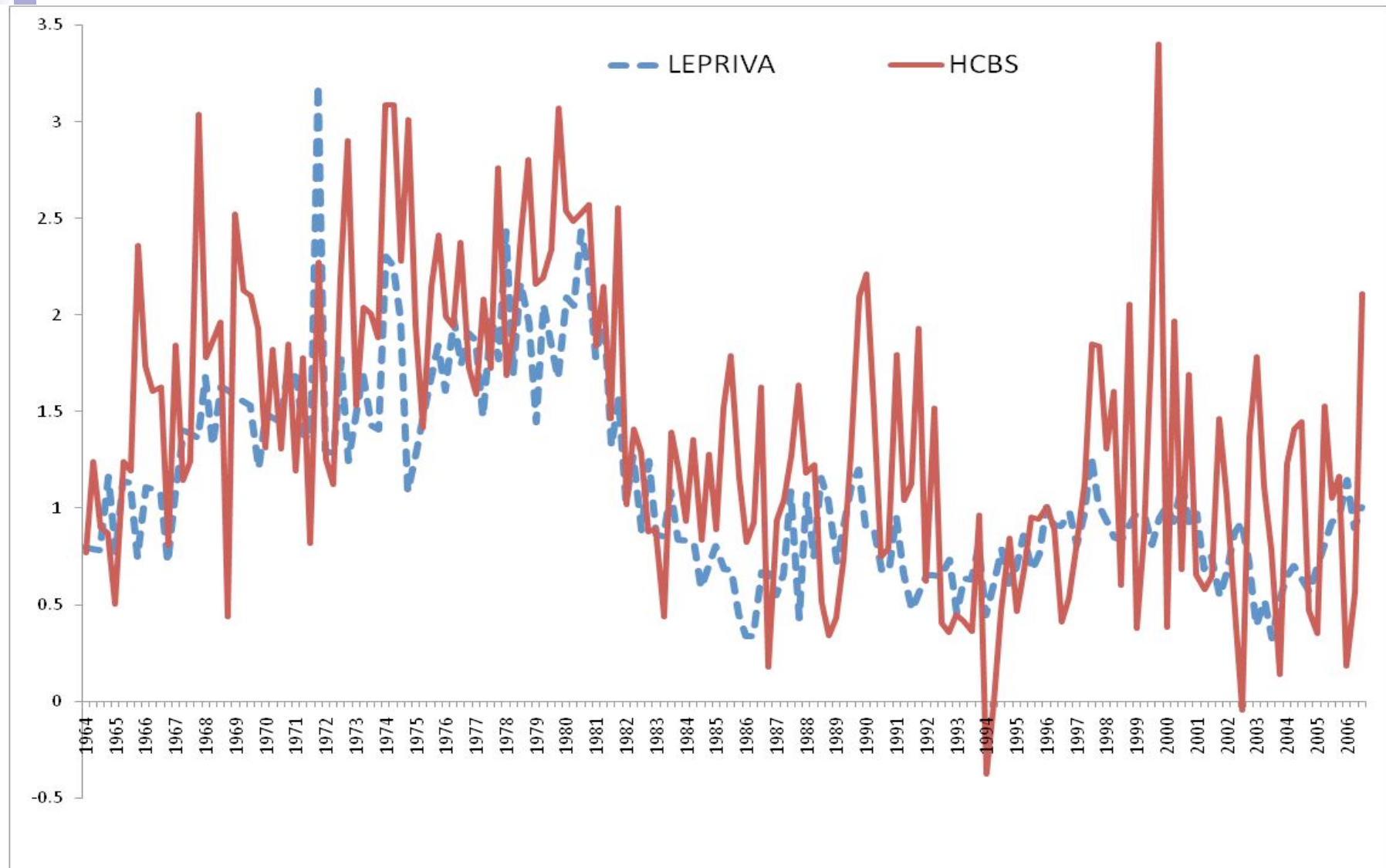
# Alternative interpretation of markup shocks

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## ■ Noise

- sampling error
- idiosyncratic shocks across multiple wage (price) series
  - Very different high frequency behavior
  - Abraham et al. (1999), Bosworth and Perry (1994)
  - Boivin and Giannoni (2006 and 2009)

# Alternative wage series



# Alternative wage series



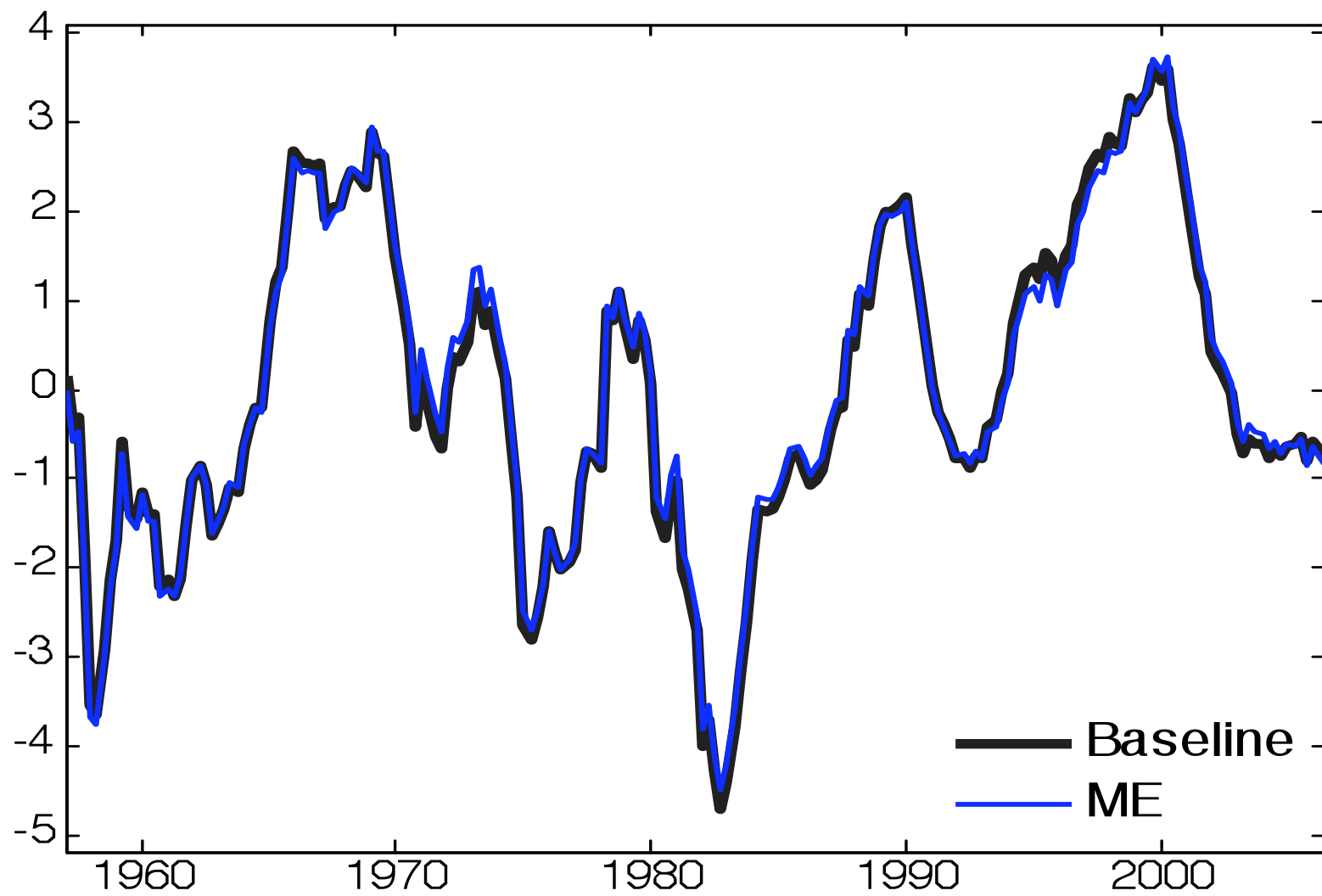
- Growth rate of nominal wages
- LEPRIVA
  - hourly compensation of non-supervisory and production workers (Establishment Survey)
- HCBS
  - hourly compensation in the business sector
  - includes dividend payments and other stuff that has little to do with wages

# Alternative interpretation of markup shocks

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- Noise
- Model with measurement errors fits data as well

# Output Gaps



# Alternative interpretation of markup shocks

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- Noise
- Model with measurement errors fits data as well
- Natural  $\propto$  potential output
  - More plausible implications for flex prices and wages economy



# Alternative interpretation of markup shocks

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- Noise
- Model with measurement errors fits data as well
- Natural  $\propto$  potential output
  - More plausible implications for flex prices and wages economy
- Caveat: all ME, extreme assumption

# Robustness

- MLE

# Robustness



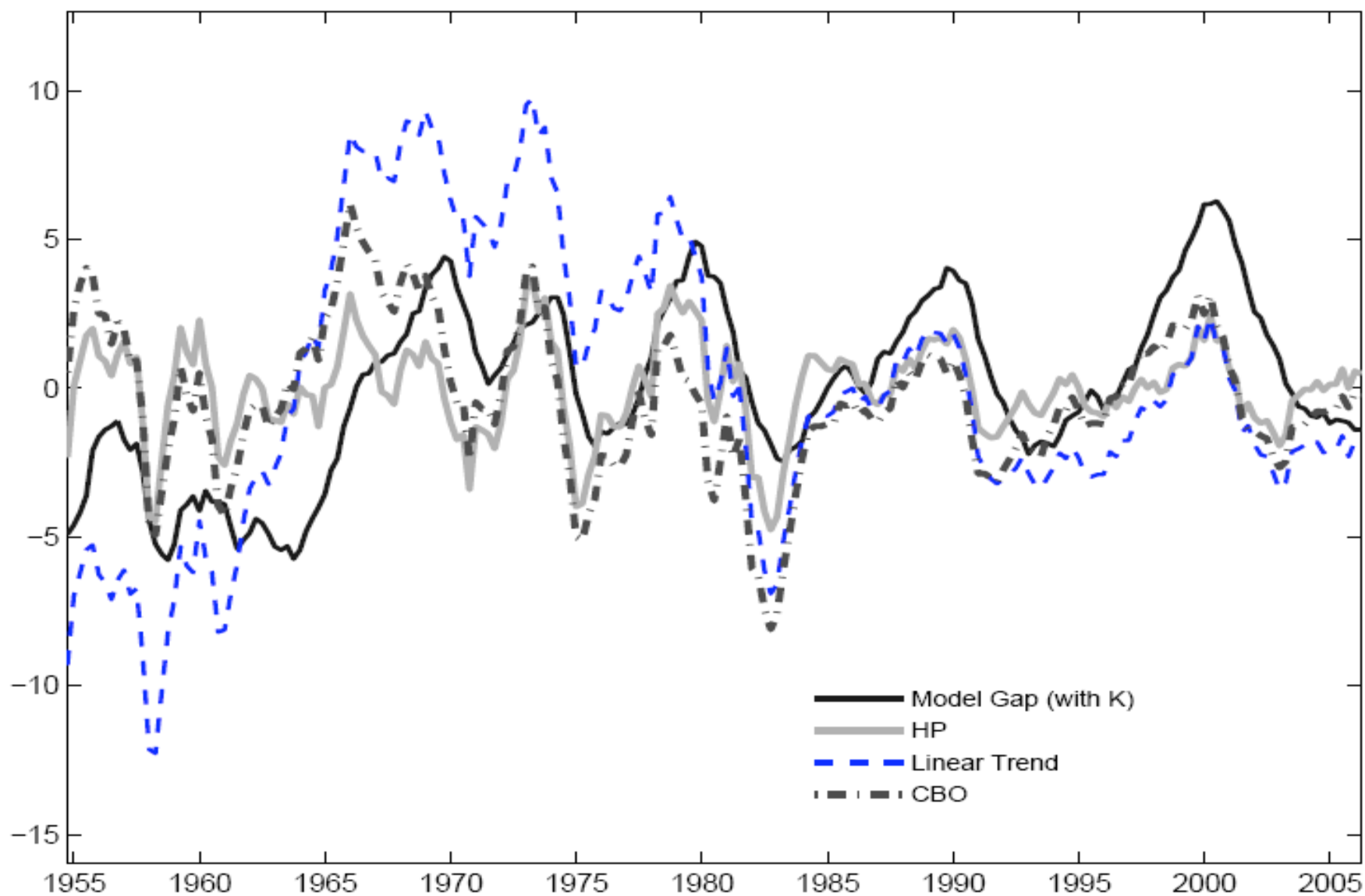
- MLE
- Labor supply shocks (persistent)
  - Gap even closer to HP, CBO

# Robustness



- MLE
  
- Labor supply shocks (persistent)
  - Gap even closer to HP, CBO
  
- Larger model with endogenous capital accumulation and additional propagation mechanisms
  - CEE (2005), Smets and Wouters (2007)

# Gap in Model with Capital



# Conclusions

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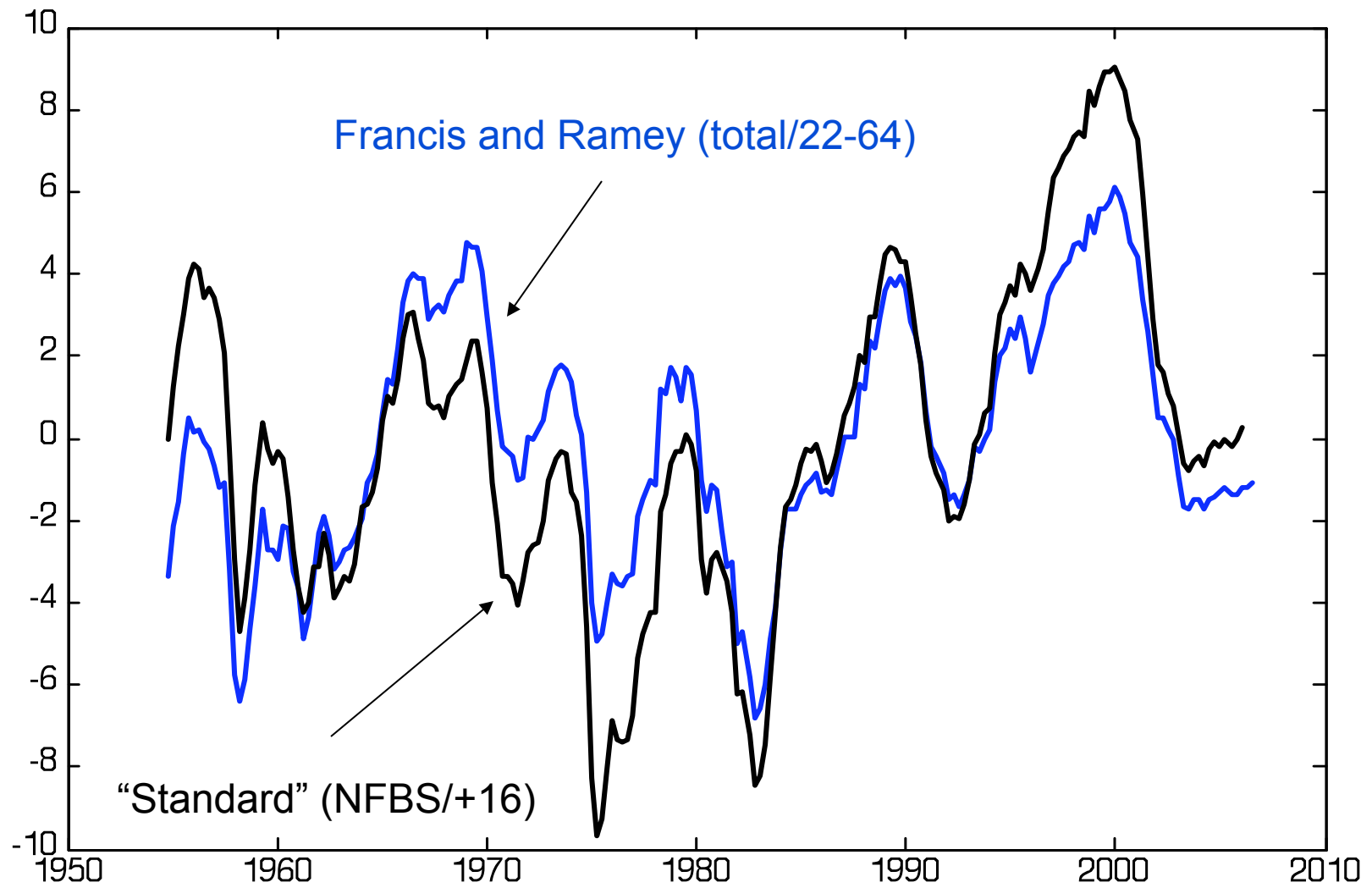
- Potential output is smooth
  - Inefficient business cycles
  
- Natural output is implausibly volatile
  - Casts doubts on structural interpretation of innovations in price and wage Phillips curves
  
- Alternative interpretation that fits data as well
  - Shocks to Phillips curves are not structural
  - ➔ No distinction between natural and potential output

# Additional material



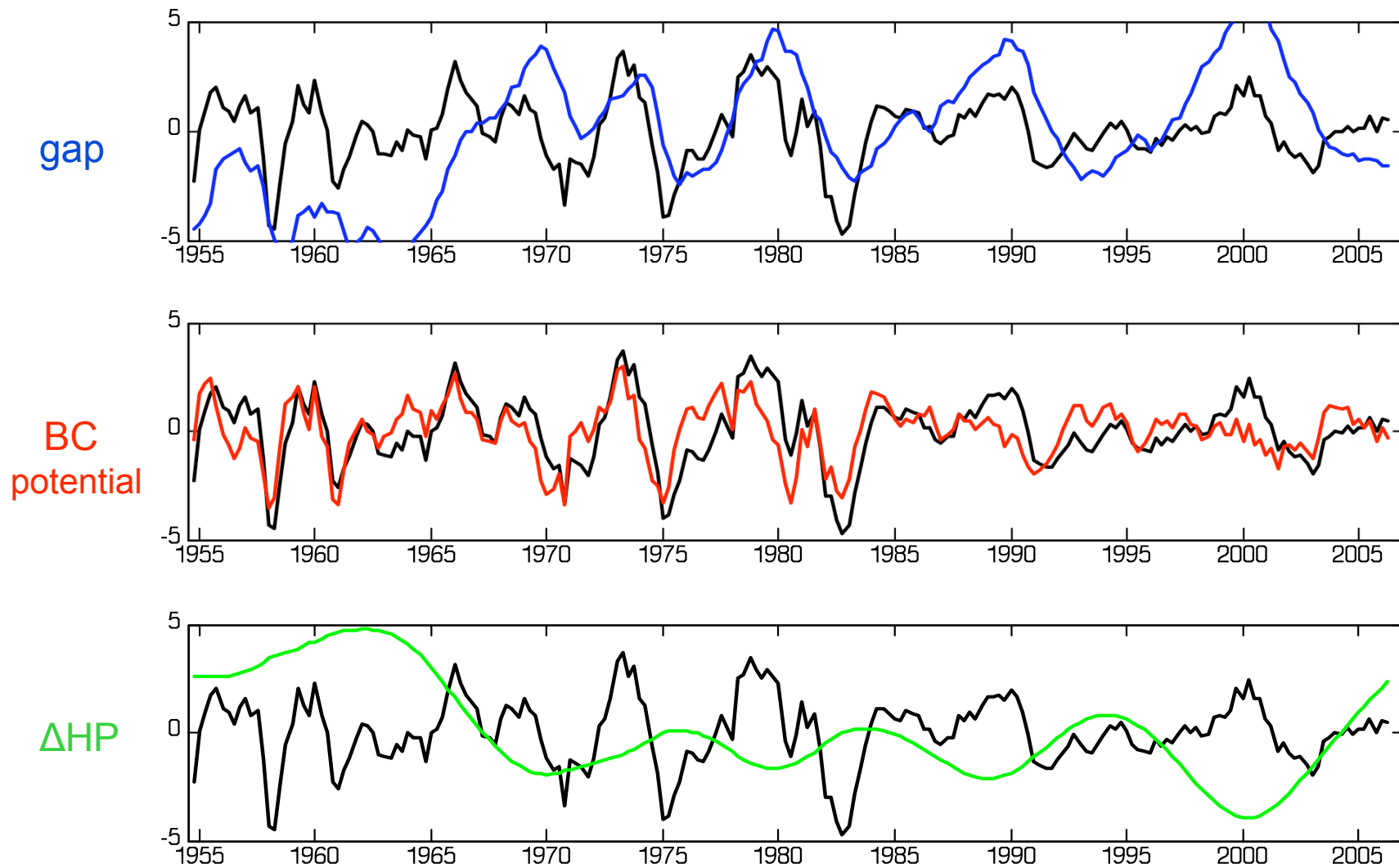
1. Hours measures
2. How inefficient are business cycles in a model with  $K$ ?

# 1. Hours





## 2. BC decomposition in a model with K



## 2. BC decomposition in a model with K (hours)

