Materials 40 - Still trying to understand why not identified

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1 Loss when varying one parameter, more details

Figure 1: Loss for N=100, NOT using 1-step ahead forecasts of inflation, estimate mean moments once, imposing convexity with weight 100K, w/o measurement error, truth with $nfe=5, fe\in(-2,2)$

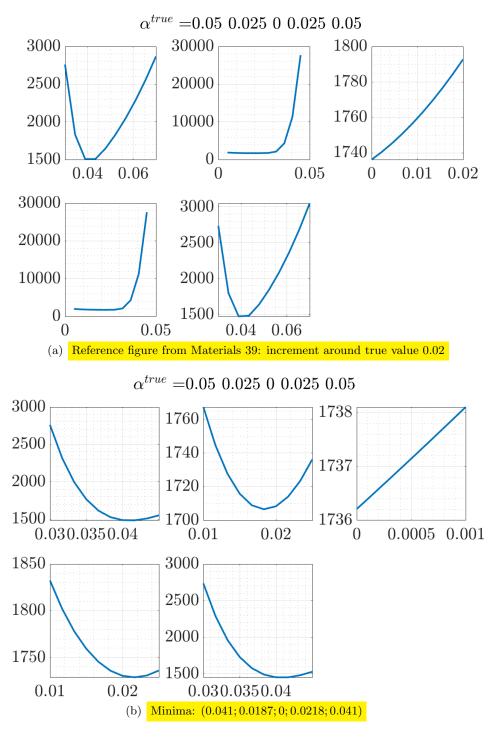


Figure 2: Variations I

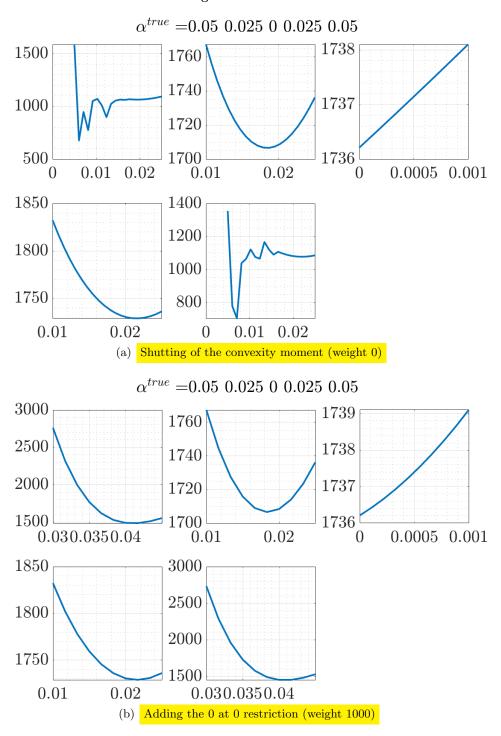


Figure 3: Variations II $\alpha^{true} = 0.05 \ 0.025 \ 0 \ 0.025 \ 0.05$ 0.0626 0.060.07 0.0580.068 0.06250.066 0.0560.064 0.0624 $0.01 \ 0.02$ $0.05 \ 0.055 \ 0.06$ 0 $0 \quad 0.00050.001$ 0.1 0.07 0.080.0650.06 0.04 0.06 0.01 0.02 $0.05 \ 0.055 \ 0.06$ (a) Add measurement error $\alpha^{true} = \!\! 0.05 \ 0.025 \ 0 \ 0.025 \ 0.05$ 0.000020.000017380.00001760.0000190.00001740.000017370.00001720.000018 $0.000017 \\ 0.010.02$ 0.00001736 $0.05 \quad 0.055$ 0.000.50010.00001850.000020.0000190.0000180.000018 0.00001750.000017 0.010.02 $0.05 \quad 0.055$

(b) Rescale W

Figure 4: Variations III

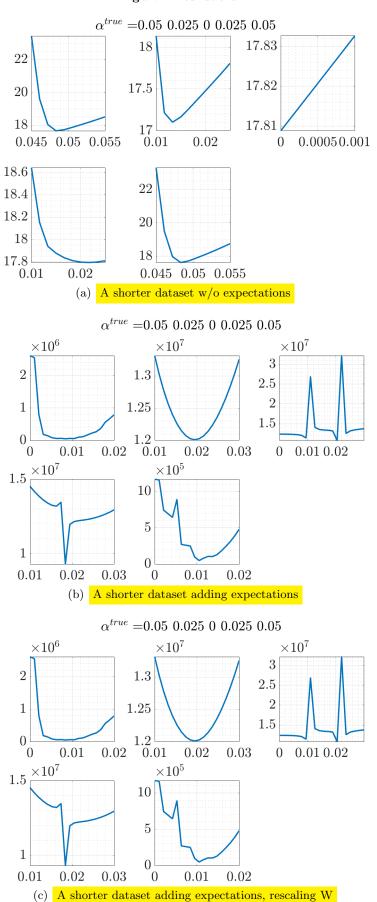
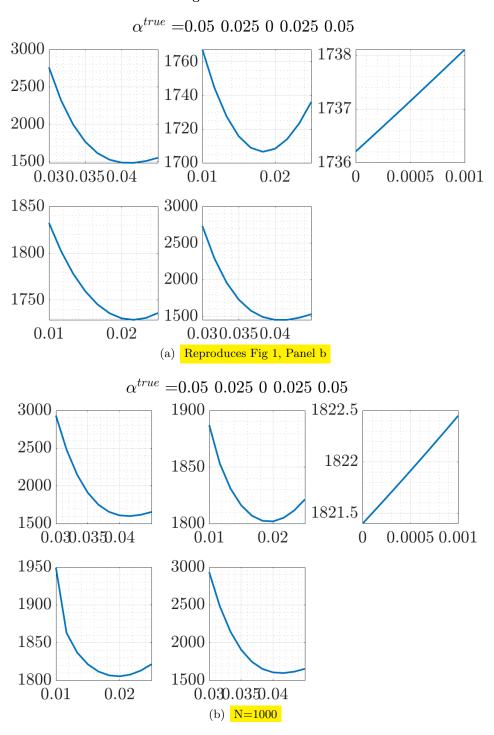
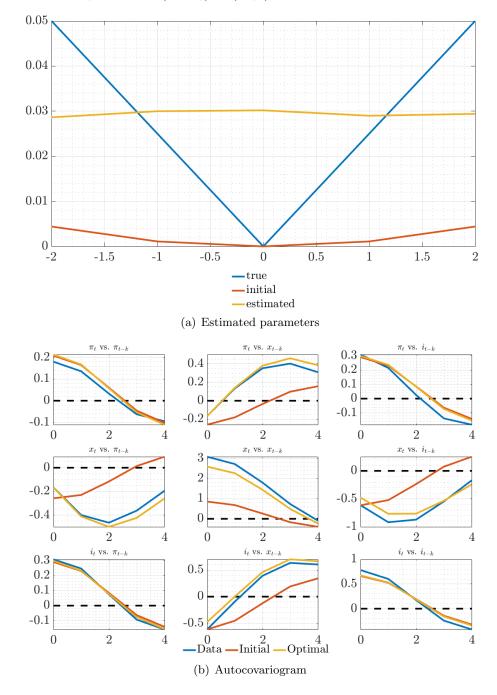


Figure 5: Variations IV



1.1 N = 1000 for N simulations, one estimation

Figure 6: NOT using 1-step ahead forecasts of inflation, estimate mean moments once, imposing convexity with weight 100K, w/o measurement error, truth with $nfe = 5, fe \in (-2, 2)$



A Model summary

$$x_{t} = -\sigma i_{t} + \hat{\mathbb{E}}_{t} \sum_{T=t}^{\infty} \beta^{T-t} \left((1-\beta) x_{T+1} - \sigma(\beta i_{T+1} - \pi_{T+1}) + \sigma r_{T}^{n} \right)$$
(A.1)

$$\pi_t = \kappa x_t + \hat{\mathbb{E}}_t \sum_{T=t}^{\infty} (\alpha \beta)^{T-t} \left(\kappa \alpha \beta x_{T+1} + (1-\alpha)\beta \pi_{T+1} + u_T \right)$$
(A.2)

$$i_t = \psi_\pi \pi_t + \psi_x x_t + \bar{i}_t$$
 (if imposed) (A.3)

PLM:
$$\hat{\mathbb{E}}_t z_{t+h} = a_{t-1} + b h_x^{h-1} s_t \quad \forall h \ge 1 \qquad b = g_x h_x$$
 (A.4)

Updating:
$$a_t = a_{t-1} + k_t^{-1} (z_t - (a_{t-1} + bs_{t-1}))$$
 (A.5)

Anchoring function:
$$k_t^{-1} = \rho_k k_{t-1}^{-1} + \gamma_k f e_{t-1}^2$$
 (A.6)

Forecast error:
$$fe_{t-1} = z_t - (a_{t-1} + bs_{t-1})$$
 (A.7)

LH expectations:
$$f_a(t) = \frac{1}{1 - \alpha \beta} a_{t-1} + b(\mathbb{I}_{nx} - \alpha \beta h)^{-1} s_t$$
 $f_b(t) = \frac{1}{1 - \beta} a_{t-1} + b(\mathbb{I}_{nx} - \beta h)^{-1} s_t$

This notation captures vector learning (z learned) for intercept only. For scalar learning, $a_t = \begin{pmatrix} \bar{a}_t & 0 & 0 \end{pmatrix}'$ and b_1 designates the first row of b. The observables (π, x) are determined as:

$$x_t = -\sigma i_t + \begin{bmatrix} \sigma & 1 - \beta & -\sigma \beta \end{bmatrix} f_b + \sigma \begin{bmatrix} 1 & 0 & 0 \end{bmatrix} (\mathbb{I}_{nx} - \beta h_x)^{-1} s_t$$
 (A.9)

$$\pi_t = \kappa x_t + \begin{bmatrix} (1 - \alpha)\beta & \kappa \alpha \beta & 0 \end{bmatrix} f_a + \begin{bmatrix} 0 & 0 & 1 \end{bmatrix} (\mathbb{I}_{nx} - \alpha \beta h_x)^{-1} s_t$$
 (A.10)

B Target criterion

The target criterion in the simplified model (scalar learning of inflation intercept only, $k_t^{-1} = \mathbf{g}(fe_{t-1})$):

$$\pi_{t} = -\frac{\lambda_{x}}{\kappa} \left\{ x_{t} - \frac{(1-\alpha)\beta}{1-\alpha\beta} \left(k_{t}^{-1} + ((\pi_{t} - \bar{\pi}_{t-1} - b_{1}s_{t-1})) \mathbf{g}_{\pi}(t) \right) \right\}$$

$$\left(\mathbb{E}_{t} \sum_{i=1}^{\infty} x_{t+i} \prod_{j=0}^{i-1} (1 - k_{t+1+j}^{-1} - (\pi_{t+1+j} - \bar{\pi}_{t+j} - b_{1}s_{t+j}) \mathbf{g}_{\bar{\pi}}(t+j)) \right)$$
(B.1)

where I'm using the notation that $\prod_{j=0}^{0} \equiv 1$. For interpretation purposes, let me rewrite this as follows:

$$\pi_{t} = -\frac{\lambda_{x}}{\kappa} x_{t} + \frac{\lambda_{x}}{\kappa} \frac{(1-\alpha)\beta}{1-\alpha\beta} \left(k_{t}^{-1} + f e_{t|t-1}^{eve} \mathbf{g}_{\pi}(t) \right) \mathbb{E}_{t} \sum_{i=1}^{\infty} x_{t+i}$$

$$-\frac{\lambda_{x}}{\kappa} \frac{(1-\alpha)\beta}{1-\alpha\beta} \left(k_{t}^{-1} + f e_{t|t-1}^{eve} \mathbf{g}_{\pi}(t) \right) \left(\mathbb{E}_{t} \sum_{i=1}^{\infty} x_{t+i} \prod_{j=0}^{i-1} (k_{t+1+j}^{-1} + f e_{t+1+j|t+j}^{eve}) \mathbf{g}_{\pi}(t+j) \right)$$
(B.2)

Interpretation: tradeoffs from discretion in RE + effect of current level and change of the gain on future tradeoffs + effect of future expected levels and changes of the gain on future tradeoffs

(A.8)

C Impulse responses to iid monpol shocks across a wide range of learning models

 $T = 400, N = 100, n_{drop} = 5$, shock imposed at t = 25, calibration as above, Taylor rule assumed to be known, PLM = learn constant only, of inflation only.

Figure 7: IRFs and gain history (sample means)

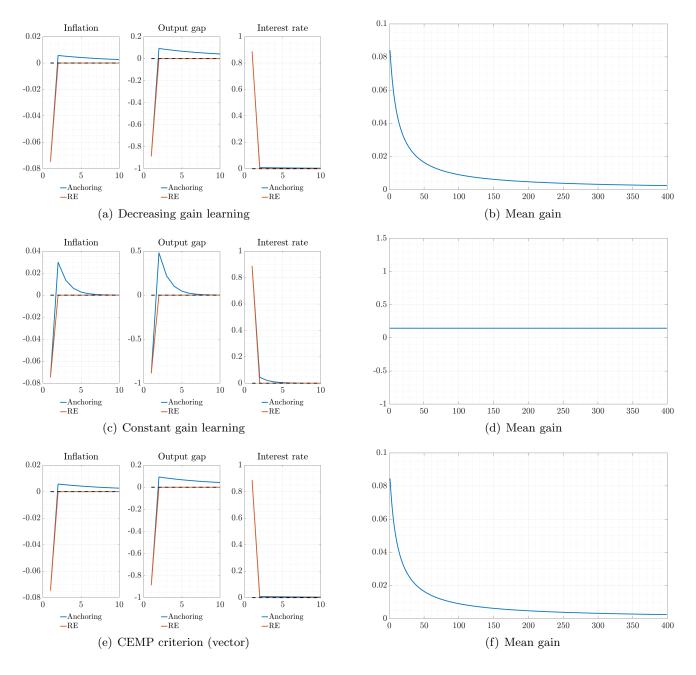


Figure 8: IRFs and gain history (sample means), continued

