Materials 28 - Putting approximating functions and value function iteration together

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The setup of the problem makes the separate issues I'm facing clear:

$$V(x) = \max_{u} p(u, x) + \beta \mathbb{E} V(x')$$
(1)

- 1. Interpolate instead of discretize \leftarrow this is where I'm at
- 2. Interpolation may have to be shape-preserving
- 3. Compute expectation on RHS \rightarrow quadrature
- 4. x is a vector \rightarrow multivariate approximation

ALGORITHM: PARAMETRIC VALUE FUNCTION ITERATION (Judd, Numerical Methods, Algorithm 12.5)

- Objective: Solve Bellman equation \to find coefficients b^* such that the approximation $\hat{V}(x,b)$ is close enough.
- Initialization: Choose a functional form for $\hat{V}(x, b^0)$ and choose a grid of n interpolation nodes $X = \{x_1, \dots, n_n\}$. Choose initial vector of coefficients b^0 and stopping criterion $\varepsilon > 0$.

Step 1 Maximization step

Compute $v_j = T\hat{V}(\cdot, b^i)$ for $x_j \in X$.

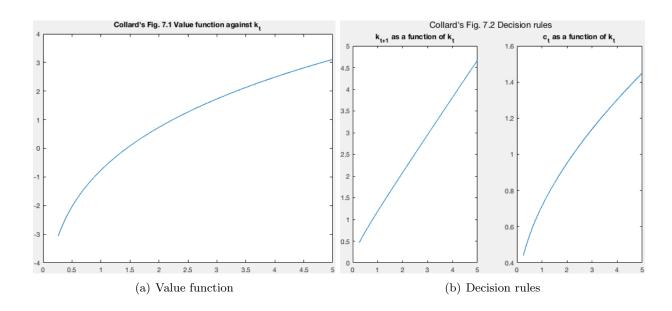
Step 2 Fitting step

Using your choice of approximation method, compute the updated vector of coefficients b^{i+1} such that $\hat{V}(x, b^{i+1})$ approximates the (v_i, x_i) data.

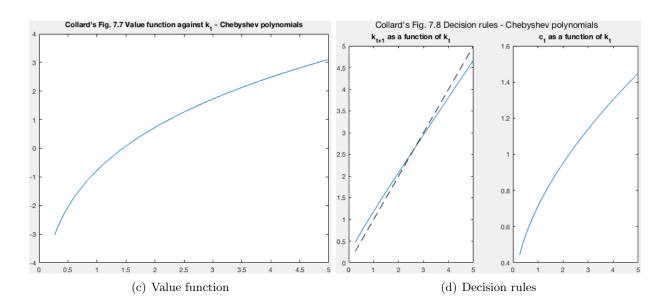
Step 3 If $||\hat{V}(x,b^i) - \hat{V}(x,b^{i+1}) < \varepsilon||$, stop; else go to Step 1.

1 Optimal growth model

1.1 Optimal growth - value function iteration with discretization



1.2 Optimal growth - value function iteration with Chebyshev polynomial interpolation



1.3 Optimal growth - value function iteration with cubic spline interpolation

