

# Materials 22 - GMM of simple anchoring function

Laura Gáti

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## Overview

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## 1 Specifications of anchoring function and estimation

- Anchoring function

$$k_t = k_{t+1} + \frac{1}{(d fe)^2} \quad (1)$$

Agents update their PLM using the inverse gain  $k_t^{-1}$ . Thus the bigger  $\frac{1}{(d fe)^2}$ , the more the gain is *decreasing*. Higher forecast errors  $fe$  or a higher  $d$  means closer to constant gains. I tried the inverse formulation with  $h_t \equiv k_t^{-1}$  and

$$h_t = h_{t-1} + (d fe_{t-1})^2 \quad (2)$$

but it always led to explosive simulations.

- Target: I gather the time series of inflation, output gap and federal funds rate, filter them, and compute empirical autocovariances:

$$ac^{data}(h) \equiv \text{cov}(y_t, y_{t-h}) \quad (3)$$

for  $h = 0, \dots, K$ , selecting  $K = 4$ . I gather these autocovariances for the three variables in the matrix  $AC$ . The target then is  $ac^{data} \equiv \text{vec}(AC)$  (a  $n_y(K+1) \times 1$  vector, i.e.  $15 \times 1$ ). Thus the

objective function can be written as:

$$J \equiv (ac^{data} - ac^{model})' W^{-1} (ac^{data} - ac^{model}) \quad (4)$$

- Initial  $d_0 = 10$ .

## 2 Estimation issues

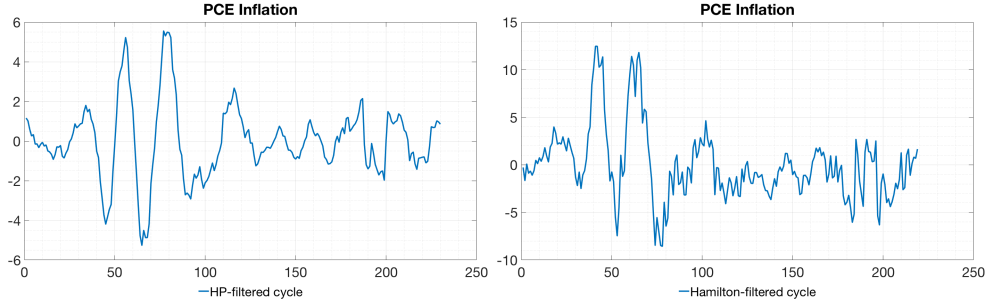
- $W$ : Ideally I'd want to use a weighting matrix with the estimated variances of the target moments on the diagonal:

$$W = \begin{pmatrix} \hat{\sigma}_{ac(\pi,0)}^2 & 0 & \dots & 0 \\ 0 & \hat{\sigma}_{ac(x,0)}^2 & 0 & \dots & 0 \\ \vdots & & \ddots & & \vdots \\ 0 & \dots & 0 & \hat{\sigma}_{ac(i,K)}^2 \end{pmatrix} \quad (5)$$

Since I don't fit the data to a time series process, I create bootstrapped samples from the original (filtered) data. This however results in tiny bootstrapped variances, so  $W^{-1}$  is huge.

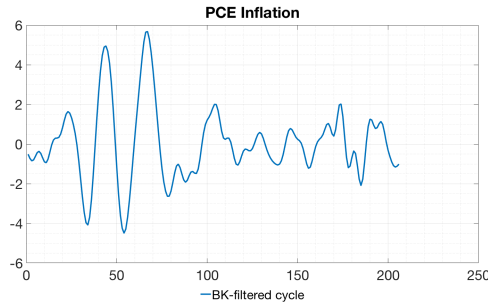
## 3 Robustness to different filters

**Figure 1:** Cyclical component of inflation filtered using different methods



(a) Hodrick-Prescott,  $\lambda = 1600$

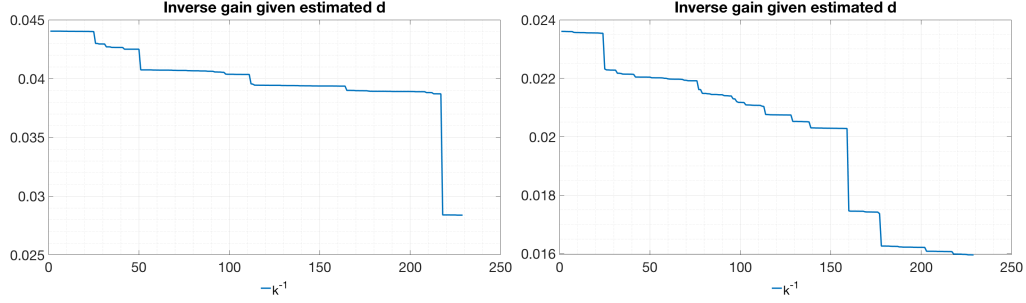
(b) Hamilton, 4 lags,  $h = 8$



(c) Baxter-King, (6, 32) quarters, truncation at 12 lags

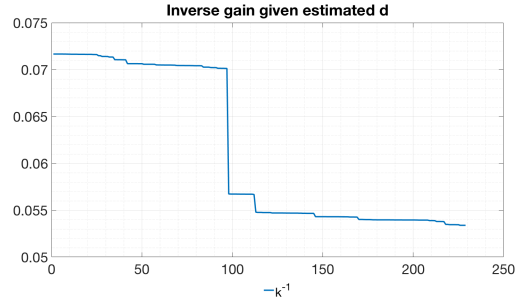
## 4 Estimates

**Figure 2:** Inverse gain for  $\hat{d}$  for the different filters



(a) Hodrick-Prescott,  $\lambda = 1600$

(b) Hamilton, 4 lags,  $h = 8$



(c) Baxter-King, (6, 32) quarters, truncation at 12 lags

**Table 1:**  $\hat{d}$

	$W = I$	$W = \text{diag}(\hat{\sigma}_{ac(0)}, \dots, \hat{\sigma}_{ac(K)})$
HP	77.7899	10
Hamilton	32.1649	10
BK	90.3929	10