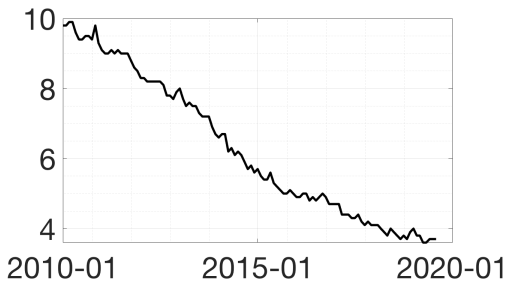


# MONETARY POLICY & ANCHORED EXPECTATIONS

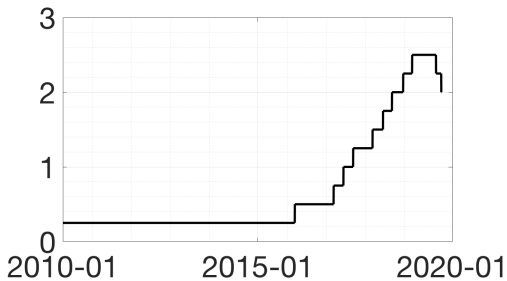
Laura Gáti

Boston College

October 1, 2019



(a) Unemployment rate



(b) Fed funds rate target range, upper limit

# THIS PROJECT

- ① Combines a formal definition of an anchoring mechanism (AM) from econometric learning
  - ② with a standard macro model of monetary policy
- ⇒ Explains current monetary policy as a concern to keep expectations anchored
- Reinterprets Great Inflation as a period of unanchored expectations
  - Reevaluates optimal monetary policy

# STRUCTURE OF TALK

① RELATED LITERATURE

② INTUITION: WHAT IS ANCHORING AND WHY SHOULD IT MATTER?

③ A FORMAL NOTION OF ANCHORING

④ MODEL WITH ANCHORING MECHANISM

⑤ SIMULATIONS

# RELATED LITERATURE

- **Optimal monetary policy in New Keynesian models**

Clarida, Gali & Gertler (1999), Woodford (2003)

- **Econometric learning**

Evans & Honkapohja (2001), Preston (2005), Graham (2011)

- **Anchoring**

Carvalho et al (2019), Svensson (2015), Hooper et al (2019)

# STRUCTURE OF TALK

- 1 RELATED LITERATURE
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- 4 MODEL WITH ANCHORING MECHANISM
- 5 SIMULATIONS

# NEW KEYNESIAN PHILLIPS CURVE

$$\pi_t = \beta \hat{\mathbb{E}}_t \pi_{t+1} + \kappa x_t$$

- $\pi_t$  = inflation
- $x_t$  = output gap
- $\hat{\mathbb{E}}_t$  = expectation-operator (not necessarily rational)

Suppose a negative demand shock:

$$\pi_t = \beta \hat{\mathbb{E}}_t \pi_{t+1} + \kappa \underset{\downarrow}{x_t}$$



If expectations do not move:

$$\underset{\downarrow}{\pi_t} = \beta \hat{\mathbb{E}}_t \pi_{t+1} + \underset{\downarrow}{\kappa x_t}$$

If seeing  $\pi_t$ , expectations adjust:



$$\pi_t = \beta \hat{\mathbb{E}}_t \pi_{t+1} + \kappa X_t$$

↓ ↓      ↓      ↓

Keeping expectations stable may be desirable

→ “Anchored”: notion of stable expectations

# STRUCTURE OF TALK

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# A LEARNING MODEL OF EXPECTATION FORMATION

Suppose firms and households

- observe everything up to time  $t$
- do not observe future variables
- KEY: are unsure about the long-run mean of inflation,  $\bar{\pi}$

Agents construct one-period-ahead inflation forecasts as

$$\hat{\mathbb{E}}_t \pi_{t+1} = \bar{\pi}_{t-1} + bs_t \quad (1)$$

$\bar{\pi}$  = estimate of inflation drift (= long-run mean, “target”)

$\hat{\mathbb{E}}$  = subjective expectation operator (not rational expectations,  $\mathbb{E}$ )

$b$  = matrix of constants

$s$  = shocks

# DEFINITION: ANCHORING MECHANISM

$$\bar{\pi}_t = \bar{\pi}_{t-1} + k_t \overbrace{(\pi_t - (\bar{\pi}_{t-1} + bs_{t-1}))}^{\text{short-run forecast error}} \quad (2)$$

$$k_t = \begin{cases} \frac{1}{k_{t-1}+1} & \text{if } \overbrace{|\hat{\mathbb{E}}_{t-1}\pi_t - \mathbb{E}_{t-1}\pi_t|/\sigma_s}^{\equiv \theta_t} \leq \bar{\theta} \\ \bar{g} & \text{otherwise} \end{cases} \quad (3)$$

Equation (3): endogenous gain

- Carvalho et al (2019)
- Difference to standard econometric learning

- Expectations anchored = when agents choose **decreasing** gains
- Expectations unanchored = when agents choose **constant** gains

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# THE MODEL

### 3-EQUATION NEW KEYNESIAN MODEL

$$x_t = -\sigma i_t + \hat{\mathbb{E}}_t \sum_{T=t}^{\infty} \beta^{T-t} ((1-\beta)x_{T+1} - \sigma(\beta i_{T+1} - \pi_{T+1}) + \sigma r_T^n) \quad (4)$$

$$\pi_t = \kappa x_t + \hat{\mathbb{E}}_t \sum_{T=t}^{\infty} (\alpha\beta)^{T-t} (\kappa\alpha\beta x_{T+1} + (1-\alpha)\beta\pi_{T+1} + u_T) \quad (5)$$

$$i_t = \psi_\pi \pi_t + \psi_x x_t + \bar{i}_t \quad (6)$$

“Long-horizon forecasts”  $\rightarrow$  agents do not know the model  
Preston (2005)

# STRUCTURE OF TALK

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# CALIBRATION

$\beta$	0.98
$\sigma$	0.5
$\alpha$	0.5
$\psi_\pi$	1.5
$\psi_\chi$	1.5
$\bar{g}$	$1/0.145^*$
$\bar{\theta}$	$5^*$
$\rho_r$	0
$\rho_i$	$0.877^*$
$\rho_u$	0
$\sigma_i$	$0.359^*$
$\sigma_r$	0.1
$\sigma_u$	$0.277^*$

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\* Carvalho et al (2019)'s estimates. Exception:  $\bar{\theta} = 0.029$ .

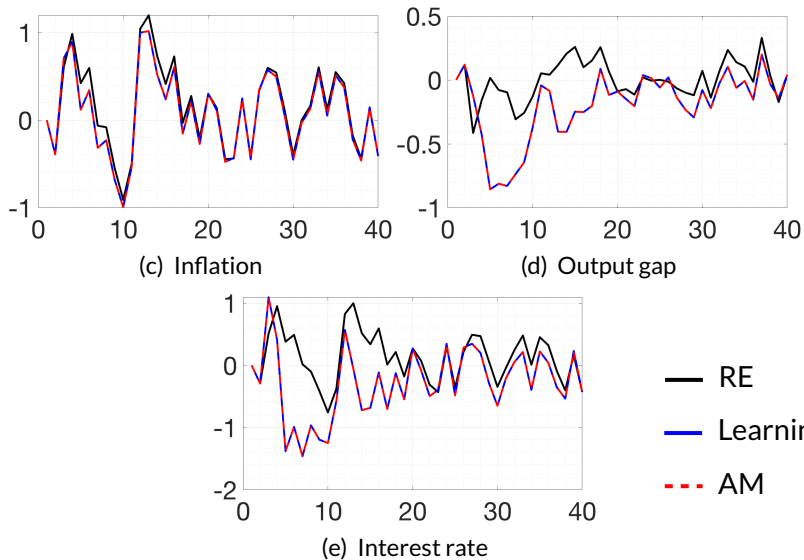


FIGURE: Rational expectations (RE), learning and anchoring mechanism (AM)

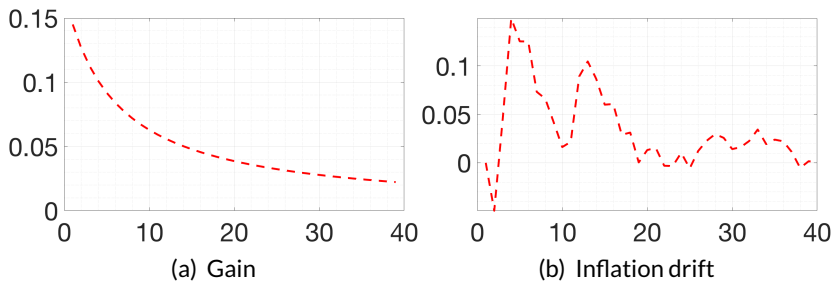


FIGURE: Well anchored expectations: decreasing gain

# DECREASING $\bar{\theta}$ : AN UNANCHORED CASE

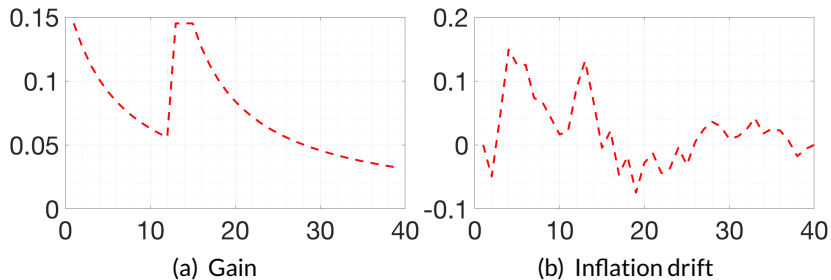
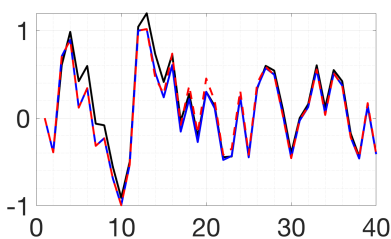
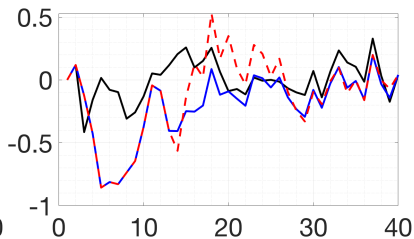


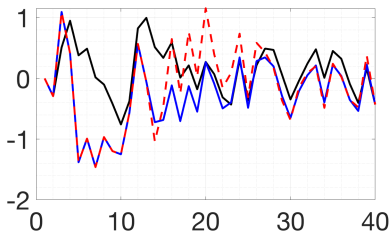
FIGURE:  $\bar{\theta} = 1$ . Unanchored expectations: constant gain



(a) Inflation



(b) Output gap



(c) Interest rate

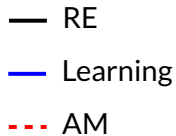


FIGURE:  $\bar{\theta} = 1$



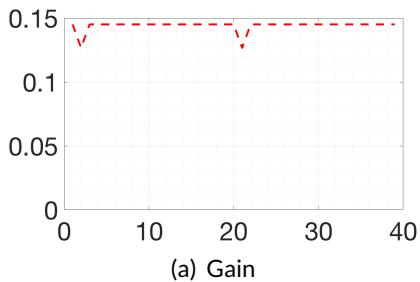


FIGURE:  $\bar{\theta} = 0.029$ . Carvalho et al's estimate extremely unanchored!

# GAIN WHEN VARYING TAYLOR-RULE COEFFICIENTS

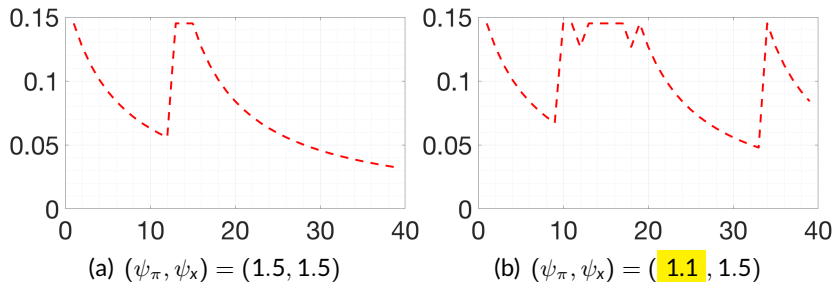
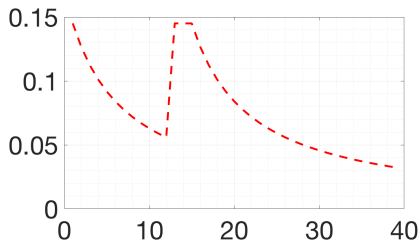
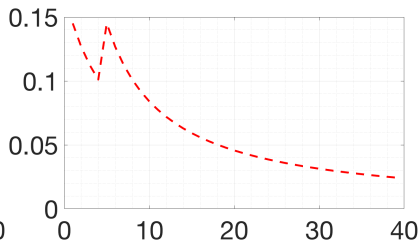


FIGURE: Less aggressive on inflation

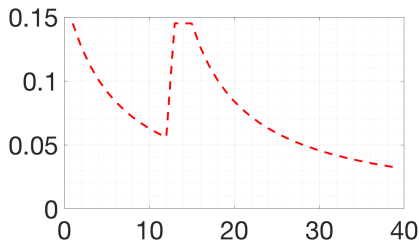


(a)  $(\psi_\pi, \psi_x) = (1.5, 1.5)$

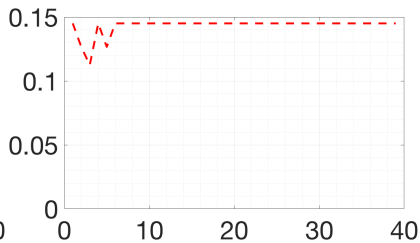


(b)  $(\psi_\pi, \psi_x) = (3, 1.5)$

FIGURE: More aggressive on inflation



(a)  $(\psi_\pi, \psi_x) = (1.5, 1.5)$



(b)  $(\psi_\pi, \psi_x) = (5, 1.5)$

FIGURE: Too aggressive on inflation?

# TODAY'S CONCLUSION AND WORK AHEAD

- Formal definition of anchoring + New Keynesian model

→ investigation of new constraint on monetary policy

- Next steps
  - Write and solve monetary policy problem
  - Estimate model

Thank you!

# COMPACT NOTATION

$$z_t = A_1 f_{a,t} + A_2 f_{b,t} + A_3 s_t \quad (7)$$

$$s_t = P s_{t-1} + \epsilon_t \quad (8)$$

where

$$z_t \equiv \begin{pmatrix} \pi_t \\ x_t \\ i_t \end{pmatrix} \quad s_t \equiv \begin{pmatrix} r_t^n \\ \bar{i}_t \\ u_t \end{pmatrix} \quad (9)$$

and

$$f_{a,t} \equiv \hat{\mathbb{E}}_t \sum_{T=t}^{\infty} (\alpha \beta)^{T-t} z_{T+1} \quad f_{b,t} \equiv \hat{\mathbb{E}}_t \sum_{T=t}^{\infty} (\beta)^{T-t} z_{T+1} \quad (10)$$