# Detecting Photo Manipulation using Reflections on Curved Surfaces

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## Abstract

Abstract goes here

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#### 1. INTRODUCTION

Image forensics, the study of finding hidden information in photographs, is an emerging field with diverse applications. It is comprised of a few general subtopics: determining the source of an image, detecting forgery, and detecting steganography (hiding information in a digital image) [Rocha et al., 2011]. All too often, pictures are used as hard evidence in journalism, scientific research, and criminal cases. For example, there was one incident in the scientific community in which a group of South Korean scientists published groundbreaking stem cell research results, but it was later revealed that the majority of the photographs included with the results were doctored [Rocha et al., 2011]. Image forgery itself predates the digital age, but as computers have become more capable and tools such as Adobe Photoshop have been developed, it has become much easier to manipulate images in a convincing manner. Therefore, there is an increasing need for forensic techniques as the technology develops.

Existing forensic techniques generally involve machine learning, finding statistical anomalies, or finding geometric inconsistencies. The current techniques that take advantage of reflective objects in an image fall into the latter category. Interestingly, the human eye is very insensitive to inconsistencies in reflections [Farid and Bravo, 2010]. Therefore it would be fairly straightforward for a forger to, for example, convincingly show a person in a scene with a reflective surface who was never actually there. It would perhaps be convincing to a human, but may not hold up to analysis with a geometric technique.

Most of the reflective surfaces that might be found in real photos are planar. Some common examples are bodies of still water, mirrors, and glass windows. Non-planar reflective surfaces, which are the focus of this paper, are less common but can be found in the form of store security mirrors, works of art, and even the human eye.

#### 2. PRIOR WORK

#### 2.1 Reflections on Planar Surfaces

Recent research into properties of images that can be exploited to find inconsistencies has shown that an object in an image and its reflection in a mirror must have certain geometric properties in a real, unmanipulated image. O'Brien and Farid's 2012 paper discusses several techniques for determining whether or not an image that contains a planar mirror is consistent. All of these techniques are derived directly from linear perspective projection geometry.

The first step to all of the techniques is obtaining lines in the image that are parallel in three-dimensional scene space (or should be if the image is genuine). The first couple of techniques require hand-picking matching points between the original objects in the scene and their virtual (reflected) counterparts. Then, straight lines are drawn connecting these point pairs out to infinity. These lines, if drawn through the same planar mirror, must all intersect at a single vanishing point. If they don't intersect cleanly, or intersect at multiple vanishing points, the image can be assumed to be forged, as seen in Figure 2.1. Furthermore, the midpoints of the same lines in three-dimensional scene space must also plausibly appear to intersect the reflective surface, as in Figure 2.2. Finally, as in Figure 2.3, if there are orthogonal parallel lines in the image (for example, on the frame of a mirror), we can check if there is a consistent position for the center of projection, or point camera.

If a forger wanted to manipulate an image that contains a reflective surface, they would likely be trying to create a composite of images. For example, if they were trying to place a person in the scene that was never actually there, they would paste in that person and their reflection from another image. It may be relatively simple to align and resize these components so that they look convincing in the new image, but the reflection may still retain some properties of the mirror in the image it came from.

#### 2.2 Other Geometric Techniques

Other forensic techniques exist that take a geometric approach to shadow consistency. Instead of determining if there is a consistent vanishing point, or a plausible consistent camera location, these techniques determine if there is a consistent location for a light source. One simple technique for determining shadow consistency, akin to the techniques for reflection consistency, involve drawing rays

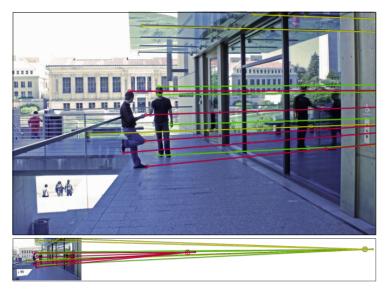


Fig. 2.1: Demonstration of vanishing point inconsistency. The lines corresponding to the man on the left converge to a different vanishing point than those from the rest of the scene, so it is likely that the man and his reflection were edited into the scene. [O'Brien and Farid, 2012, Fig. 1]

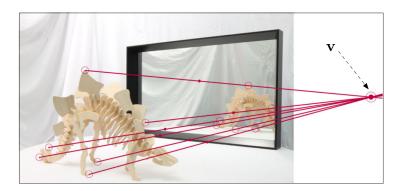


Fig. 2.2: Demonstration of midpoint and vanishing point consistency. The lines converge to a well-defined vanishing point V. Additionally, the midpoints in three-dimensional scene space between the real and reflected features plausibly intersect the mirror plane. [O'Brien and Farid, 2012, Fig. 3]

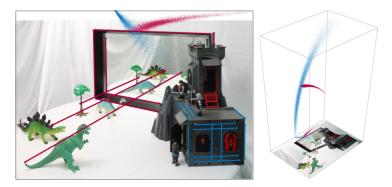
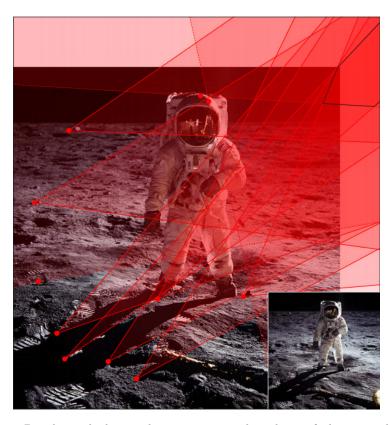


Fig. 2.3: Demonstration of center of projection consistency. The pink and blue point clouds represent sets of possible solutions, generated by randomly perturbing the points selected that form the lines. Since the point clouds intersect, there is a possible consistent center of projection, or camera position. [O'Brien and Farid, 2012, Fig. 6]

between points on an object and corresponding points on the shadow. These rays should intersect in a plausible location for the light source (or they should be nearly parallel if the light source is the sun) [Farid and Bravo, 2010]. This is dependent on the shadows having easily distinguishable features that can be matched up to the object that is casting the shadow.

Another similar technique improves on the previous one by eliminating the need for distinguishable shadow features. Instead of drawing rays, a point is picked on a shadow and a wedge constraint created that contains all of the object that could have plausibly cast that point of the shadow [Kee et al., 2013]. If there exists a region that satisfies all the constraints, the image passes this test, as in Figure 2.4.



**Fig. 2.4:** Based on shadow wedge constraints, this photo of the moon landing has a consistent light source. Original image copyright 1969, NASA. [Kee et al., 2013, Fig. 1]

## 3. MATHEMATICAL TECHNIQUES

#### 3.1 Assumptions

To simplify the geometry of this analysis, we will restrict the form of our nonplanar mirrors to be spherical. Quadric surfaces in general are likely to be good enough for typical use cases because most general curves encountered in the real world can be approximated as either a quadric surface or a set of quadric surfaces.

We also assume the camera used to take any of the images analyzed is a point camera with perspective projection. This is a reasonable assumption considering both the size of most digital camera sensors, and the fact that the camera would have to be far enough away from the subjects of the photograph to capture everything required to perform the analysis. An important idea to note is that showing that an image is consistent according to these techniques is not sufficient to prove that the image is genuine, because the image could have had some counter-forensic techniques applied or been manipulated in a way that is unrelated to reflective geometry.

#### 3.2 Properties of Reflective Geometry

Reflection of light on a surface is directly related to the surface normal at the point of reflection. The incident ray (or ray of light coming towards the surface) must make the same angle with the normal as the reflected ray. Additionally, the incident ray, reflected ray, and normal must all be coplanar, and the reflected and incident rays must be on opposite sides of the normal.

O'Brien and Farid point out that a non-obvious consequence of this law is that if a ray is drawn between the reflected object and its reflection, it should appear to be parallel to the surface normal at the point of reflection. (In the planar case, it would appear perpendicular to the mirror, since the normal is constant over the whole surface.) We will call this the projection of the incident ray. Furthermore, the incident ray and the ray drawn between the reflected object and its reflection's apparent location are co-linear from the perspective of a point camera, as demonstrated in Figure 3.1. This is why drawing rays on a picture between an object and its reflection works: it appears equivalent to drawing rays to the apparent position of the reflected object.

In the case of a planar mirror, all of these rays would be parallel in threedimensional space. An axiom of linear perspective projection is that paral-

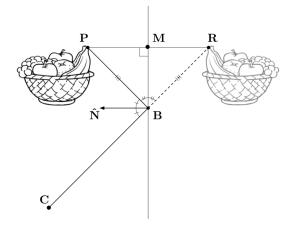


Fig. 3.1: Given a camera location C, a point P on an object and its corresponding reflection R, the ray PR appears equivalent to the ray PB from the point of view of the camera. The ray PR is also perpendicular to the surface normal N. Since all of the points in this diagram must be coplanar, this holds true in 3D space. [O'Brien and Farid, 2012, Fig. 2]

lel lines projected onto a 2D image must converge to some vanishing point V [Hartley and Zisserman, 2004, p. 2], so all such lines through a planar mirror intersect at a single vanishing point if the photograph is unaltered. This is the mathematical basis for the technique described in Section 2.1.

### 3.3 Reflective Sphere Geometry

In the case of a curved surface, the ray to the apparent position of the reflection is still parallel to the normal at the point of reflection. Unlike a planar mirror, since the normal is not constant, all such rays through the same mirror will not be parallel in three-dimensional space.

If the curved surface happens to be spherical we can exploit the fact that the normal at any point on the surface is colinear with some radius of the sphere. This is because any normal on a sphere points directly away from the center of the sphere. Since the incident ray, reflected ray, and normal are all coplanar, and the normal and the radius are coplanar, then the incident ray and any radius in that cross-section of the sphere are coplanar [Figure 3.2].

From the view point of the camera, since the projection of the incident ray is colinear with the normal, it must also be colinear with the radius. Therefore, in theory, in a valid picture of a reflective sphere any incident ray must appear to pass through the center of the sphere [Figure 3.3].

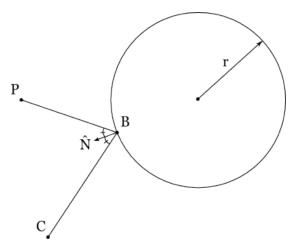


Fig. 3.2: Since the point P, the reflection point B, the camera C, and the normal N are all coplanar, and N is an extension of the radius of a sphere, then PB and any radius on this cross-section of the sphere must be coplanar.

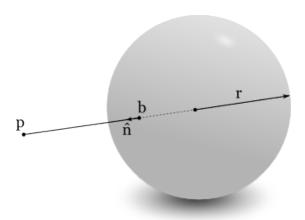


Fig. 3.3: A view of Figure 3.2 from the viewpoint of the camera C.

#### 3.4 Why not estimate the normal?

In general, the types of techniques outlined verify that the incident ray is consistent with the normal at the point of reflection. If the projection of the normal could be estimated on any arbitrary image of a quadric surface, then we could easily have a technique to detect inconsistencies in reflections on most curved surfaces because the projection of the normal and the projection of the incident ray should be colinear. However, when perspective projection is taken into account, it is non-trivial to estimate the normal accurately on an arbitrary visible point on the surface, even for a simple surface like a sphere.

In the unrealistic case where an image was produced using orthographic projection, the projection of the normal could be easily estimated on a sphere because the sphere appears exactly the same no matter the angle from which it is viewed, and the entire hemisphere facing the camera is visible. The x and y components of the projection of the normal vector are simply a function of the projection of the position on the sphere. With perspective projection, the visible region of the sphere is slightly smaller than the projection of the hemisphere so the radius can not be determined from the visible size of the sphere alone.

#### 4. IMPLEMENTATION

In order to expedite the process of obtaining images that meet a variety of very specific conditions, all images used to test these algorithms were computer-generated using Blender 2.68a.

The application consists of a Python script that uses PySide for GUI and drawing, and Numpy and Scipy for mathematical calculations. It has an interface for a user to locate a circle and its center, and to locate projections of incident rays.

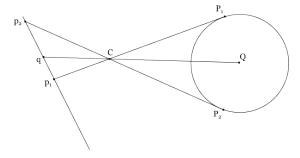
#### 4.1 Circle Finding

To find the center of the sphere, the user picks several points (at least 3, depending on the configuration of the program) along the visible edge of the sphere. The application then finds the best fit for the radius and center of a circle given the points picked.

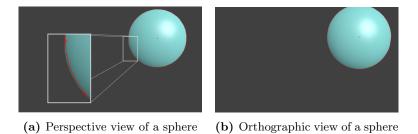
Because accuracy in finding the sphere center is key to this analysis, the application employs some rudimentary edge detection to assist in picking points on the edge of the sphere. Based on an initial point picked, it examines several pixels towards and away from an initial guess for the center and moves the point halfway between the pixels with the greatest difference in color. This edge detection is fairly limited, but is good enough for the purpose of the test images used because of their plain and easily distinguishable colors.

#### 4.1.1 Distortion from Perspective Projection

One issue with this naive approach to finding the center is that perspective projection distorts the shape of the sphere, depending on how centered the sphere is in the camera's view. If the sphere is towards the edge of the camera's view, the extent of the visible part of the sphere towards the edge is closer to the camera than the visible extent of the part of the sphere towards the middle of the image. This causes the sphere to look larger towards the edge of the image and therefore the apparent edge of the circle distorts out towards the edge of the image. This effect is described in Figure 4.1. As a result, the outline projected onto the image is slightly elliptical, as in Figure 4.2.



**Fig. 4.1:** If the image plane is not facing the sphere head-on, the distance from the point  $P_1$  to its projection  $p_1$  through the center of projection C is shorter than the distance from  $P_2$  to  $p_2$ , so one side is distorted. Additionally, the projection q of the sphere center Q is not the midpoint of  $p_1$  and  $p_2$ .



**Fig. 4.2:** Viewing the sphere with perspective projection introduces noticeable error when solving for the circle projected onto the image plane.

#### 5. RESULTS

As detailed in Section 4.1.1, it as not as simple as finding the outline of a perfect circle to find the projection of the center of the sphere in the image. Therefore, for the purpose of testing the method, test images were generated with a small sphere located at the exact center of the reflective sphere made slightly transparent. Figure 5.1 shows how inaccurate the naive center-finding method can be.

Because there is some error associated with having a human input the points to create the projections of the incident rays, it is assumed that in an unaltered image the rays will probably not cross the exact center of the sphere. For this reason, the measure for authenticity will be how close the rays come to the center of the sphere.

One possible alternative to looking at the minimum distance to the center would be to consider the the point of intersection of all the rays, similar to the vanishing point method in the planar case. However, the spherical case is much more sensitive to error than the planar case. In the planar case the incident rays are parallel, so their vanishing point often lies far outside the image, and so the position of the intersection point is not very sensitive to a difference of a few pixels in the points picked. In the spherical case, however, it is not uncommon for the projections of the incident rays to not intersect cleanly even in genuine images.

#### 5.1 Typical Results for Genuine Images

Based on images containing relatively large and relatively small reflective spheres with objects at varying distances, the projections of the incident rays usually come within 5 pixels of the sphere center. This increases with higher resolution images. As seen in Figure 5.2, some objects seem to have a clean intersection point that is offset from the sphere center. The source of this error is unknown.

5.2 Effects of Forgery

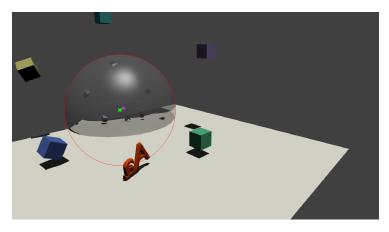


Fig. 5.1: The center found when finding the best fit for a perfect circle (green cross) is significantly offset from the actual projected center of the sphere (pink dot).

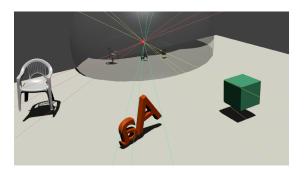
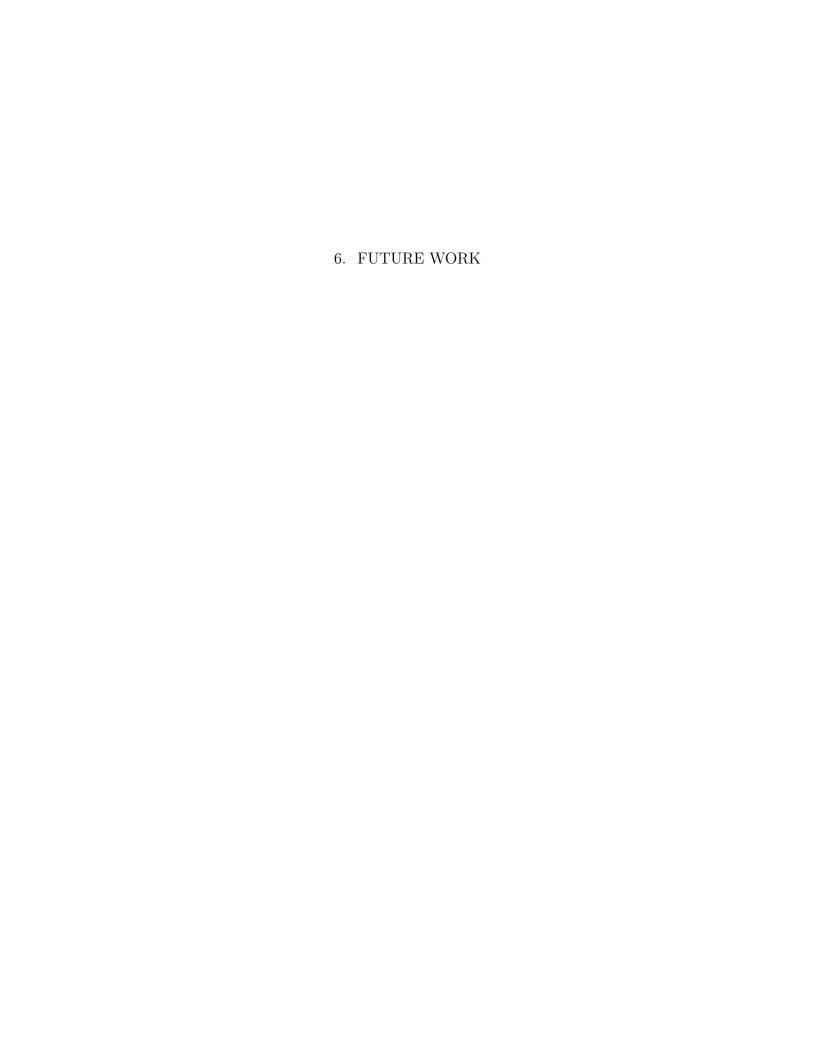


Fig. 5.2: The chair and the cube are reasonably consistent with the center of the sphere, but the incident rays from the letters appear to intersect at a point slightly offset from the center, despite being unmanipulated.





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