

for ordinals σ_j is 1
for normals

$$y_{ij} = \beta_{j0} + \beta^T x_i + \sigma_j \varepsilon_{ij}, \quad \varepsilon_j \sim N(0, \sigma^2)$$

should we do β_j ?

$y_1, \dots, y_n \rightarrow y_1, \dots, y_{g_0} \rightarrow$ ordinal (g_0 - ordinal vars)

$y_{g_0+1}, \dots, y_{g_0+g_n} \rightarrow$ normal (g_n - normal vars)

Pairwise likelihood:

3 cases: 2 ordinals

(A)

2 normals

(B)

1 ordinal + 1 normal (C)

(A) (as in mood)

$$\Pr(y_{j1} = r_1, y_{j2} = r_2) = \Pr(\tilde{y}_j L_j \leq \tilde{y}_{j1} \leq u_1, L_2 \leq \tilde{y}_{j2} \leq u_2)$$

→ rectangular probability.

(B). $l(y_1, y_2) = \phi_2(y_1, y_2, r)$ (ϕ_2 is the 2-variate normal pdf)

(C) $l(y_1, y_2) = \Pr(y_1 = r_1 | y_2) \cdot \phi(y_2)$ → $d\text{norm}(y_2, \mu_2, \sigma_2^2)$

$$\Pr(y_1 = r_1 | y_2) = \Pr(\tilde{y}_j L_1 \leq \tilde{y}_{j1} \leq u_1 | y_2)$$

$$(\tilde{y}_1, y_2) \sim \text{Bivariate normal} \left(\begin{pmatrix} \mu_1 & \mu_2 \\ \beta_{10} + \beta_1 y_2 & \mu_2 \\ \beta_{20} + \beta_2 y_2 & \mu_2 \\ \end{pmatrix}, \begin{pmatrix} 1 & r \sigma_2 \\ r \sigma_2 & \sigma_2^2 \\ \end{pmatrix} \right)$$

$$\tilde{y}_1 | y_2 \sim N\left(\mu_1 + r \cdot \frac{1}{\sigma_2} \cdot (y_2 - \mu_2), (1 - r^2) \cdot \sigma_2^2\right)$$