Tree Methods

LAEB

12-11-2019

Contents

	Decision Tree Implementation in R1.1 Regression Tree1.2 Classification Tree	
2	Bagging	16
3	Boosting	17

1 Decision Tree Implementation in R

We will implement a regression tree and a classification tree. The same car dataset used to implement PCA will be used. Detailed documentation about the dataset to be used can be found here: http://jse.amstat.org/datasets/04cars.txt

```
## Load packages
library(dplyr)
## Attaching package: 'dplyr'
## The following objects are masked from 'package:stats':
##
##
       filter, lag
## The following objects are masked from 'package:base':
##
##
       intersect, setdiff, setequal, union
library(caret) # splitting into training/test sets
## Loading required package: lattice
## Loading required package: ggplot2
library(rpart) # preforming decision trees
library(rpart.plot) # visualization decision trees
library(rattle) # Visualization decision trees
## Rattle: A free graphical interface for data science with R.
## Version 5.2.0 Copyright (c) 2006-2018 Togaware Pty Ltd.
## Type 'rattle()' to shake, rattle, and roll your data.
library(purrr) # grids
##
## Attaching package: 'purrr'
```

```
## The following object is masked from 'package:caret':
##
##
      lift
library(ipred) # bagging
## Import dataset
cars04 <- readRDS(file =
                     '~/birwe_data/Data/playground/prepared-zone/methods-and-libraries/ml-reading-cours
## Look at dataset
str(cars04)
## 'data.frame':
                   387 obs. of 18 variables:
   $ Sports
               : int
                      0 0 0 1 0 0 0 0 0 0 ...
   $ SUV
                      0 0 1 0 0 0 0 0 0 0 ...
               : int
## $ Wagon
               : int 0000000000...
                      0 0 0 0 0 0 0 0 0 0 ...
  $ Minivan
               : int
## $ Pickup
               : int
                      0 0 0 0 0 0 0 0 0 0 ...
##
                      0 0 1 0 0 0 0 0 0 0 ...
   $ AWD
               : int
## $ RWD
               : int 000100000...
               : int 43755 46100 36945 89765 23820 33195 26990 25940 35940 42490 ...
## $ Retail
                      39014 41100 33337 79978 21761 30299 24647 23508 32506 38325 ...
## $ Dealer
               : int
##
   $ Engine
               : num 3.5 3.5 3.5 3.2 2 3.2 2.4 1.8 1.8 3 ...
## $ Cylinders : int
                      6 6 6 6 4 6 4 4 4 6 ...
   $ Horsepower: int
                      225 225 265 290 200 270 200 170 170 220 ...
                      18 18 17 17 24 20 22 22 23 20 ...
   $ CityMPG
              : int
##
   $ HighwayMPG: int 24 24 23 24 31 28 29 31 30 27 ...
## $ Weight
               : int 3880 3893 4451 3153 2778 3575 3230 3252 3638 3814 ...
## $ Wheelbase : int 115 115 106 100 101 108 105 104 105 105 ...
   $ Length
               : int 197 197 189 174 172 186 183 179 180 180 ...
   $ Width
               : int 72 72 77 71 68 72 69 70 70 70 ...
summary(cars04)
##
       Sports
                         SUV
                                         Wagon
                                                          Minivan
##
   Min.
          :0.0000
                    Min.
                           :0.0000
                                     Min.
                                            :0.00000
                                                       Min.
                                                              :0.00000
   1st Qu.:0.0000
                    1st Qu.:0.0000
                                     1st Qu.:0.00000
                                                       1st Qu.:0.00000
                                     Median :0.00000
  Median :0.0000
                    Median :0.0000
                                                       Median :0.00000
   Mean
          :0.1163
                    Mean
                           :0.1525
                                     Mean
                                            :0.07235
                                                       Mean
                                                              :0.05426
##
   3rd Qu.:0.0000
                    3rd Qu.:0.0000
                                     3rd Qu.:0.00000
                                                       3rd Qu.:0.00000
                         :1.0000
                                            :1.00000
##
   Max.
          :1.0000
                    Max.
                                     Max.
                                                       Max.
                                                              :1.00000
##
       Pickup
                    AWD
                                     RWD
                                                     Retail
                                       :0.0000
                                                        : 10280
##
   Min.
          :0
               Min.
                      :0.0000
                                Min.
                                                 Min.
                                                 1st Qu.: 20997
##
   1st Qu.:0
               1st Qu.:0.0000
                                1st Qu.:0.0000
##
  Median :0
               Median :0.0000
                                Median :0.0000
                                                 Median : 28495
                      :0.2016
                                       :0.2429
   Mean
          :0
               Mean
                                Mean
                                                 Mean
                                                       : 33231
                                                 3rd Qu.: 39552
##
   3rd Qu.:0
               3rd Qu.:0.0000
                                3rd Qu.:0.0000
##
   Max.
          :0
               Max.
                      :1.0000
                                Max.
                                       :1.0000
                                                 Max.
                                                        :192465
##
       Dealer
                        Engine
                                                       Horsepower
                                      Cylinders
          : 9875
                           :1.400
                                          : 3.000
                                                           : 73.0
  Min.
                    Min.
                                    Min.
                                                     Min.
   1st Qu.: 19575
                                    1st Qu.: 4.000
##
                    1st Qu.:2.300
                                                     1st Qu.:165.0
## Median : 26155
                    Median :3.000
                                    Median : 6.000
                                                     Median :210.0
## Mean
         : 30441
                    Mean :3.127
                                    Mean : 5.757
                                                     Mean
                                                           :214.4
## 3rd Qu.: 36124
                    3rd Qu.:3.800
                                    3rd Qu.: 6.000
                                                     3rd Qu.:250.0
## Max.
          :173560
                    Max.
                           :6.000
                                    Max.
                                           :12.000
                                                     Max.
                                                            :493.0
##
      CityMPG
                    HighwayMPG
                                       Weight
                                                    Wheelbase
```

```
Min.
           :10.00
                    Min.
                            :12.00
                                     Min.
                                            :1850
                                                    Min.
                                                            : 89.0
##
    1st Qu.:18.00
                    1st Qu.:24.00
                                     1st Qu.:3107
                                                    1st Qu.:103.0
  Median :19.00
                    Median :27.00
                                     Median:3469
                                                    Median :107.0
##
  Mean
           :20.31
                    Mean
                            :27.26
                                     Mean
                                            :3532
                                                    Mean
                                                            :107.2
##
    3rd Qu.:21.50
                    3rd Qu.:30.00
                                     3rd Qu.:3922
                                                     3rd Qu.:112.0
##
           :60.00
                    Max.
                            :66.00
                                            :6400
                                                            :130.0
   {\tt Max.}
                                     Max.
                                                    Max.
                      Width
##
        Length
##
   Min.
           :143
                  Min.
                          :64.00
##
   1st Qu.:177
                  1st Qu.:69.00
##
  Median :186
                  Median :71.00
## Mean
           :185
                  Mean
                         :71.28
##
   3rd Qu.:193
                  3rd Qu.:73.00
## Max.
           :221
                  Max.
                         :81.00
```

head(cars04)

```
##
                             Sports SUV Wagon Minivan Pickup AWD RWD Retail
## Acura 3.5 RL
                                                                          43755
                                                       0
                                                              0
## Acura 3.5 RL Navigation
                                                                          46100
                                   0
                                       0
                                              0
                                                       0
                                                              0
                                                                   0
                                                                       0
## Acura MDX
                                   0
                                       1
                                              0
                                                       0
                                                              0
                                                                   1
                                                                          36945
## Acura NSX S
                                       0
                                                       0
                                                              0
                                                                   0
                                                                          89765
                                   1
                                              0
                                                                       1
## Acura RSX
                                   0
                                       0
                                                       0
                                                                   0
                                                              0
                                                                          23820
## Acura TL
                                   0
                                       0
                                              0
                                                       0
                                                              0
                                                                   0
                                                                       0
                                                                          33195
##
                             Dealer Engine Cylinders Horsepower CityMPG
## Acura 3.5 RL
                              39014
                                        3.5
                                                     6
                                                                225
                                                                          18
## Acura 3.5 RL Navigation
                              41100
                                        3.5
                                                      6
                                                                225
                                                                          18
## Acura MDX
                                        3.5
                                                      6
                                                                265
                                                                          17
                              33337
## Acura NSX S
                              79978
                                        3.2
                                                      6
                                                                290
                                                                          17
## Acura RSX
                              21761
                                        2.0
                                                      4
                                                                200
                                                                          24
## Acura TL
                              30299
                                        3.2
                                                      6
                                                                270
                                                                          20
##
                             HighwayMPG Weight Wheelbase Length Width
## Acura 3.5 RL
                                      24
                                            3880
                                                        115
                                                                197
                                                                       72
## Acura 3.5 RL Navigation
                                      24
                                            3893
                                                        115
                                                                197
                                                                       72
## Acura MDX
                                                        106
                                                                189
                                                                       77
                                      23
                                            4451
## Acura NSX S
                                      24
                                            3153
                                                        100
                                                                174
                                                                       71
## Acura RSX
                                            2778
                                                        101
                                                                172
                                                                       68
                                      31
## Acura TL
                                      28
                                            3575
                                                        108
                                                                186
                                                                       72
```

Before proceeding to the tree implementation, we split the data into a training and test sets uset the Caret package.

```
## Splitting the data into a train and test set
# Set seed
set.seed(123)
# Do the split
cars04.sub <- cars04 %>%
    select(-c("SUV","Wagon","Minivan","Pickup","AWD","RWD"))
training.sample <- cars04.sub$Sports %>% createDataPartition(p = 0.8, list = FALSE)
cars04.train.data <- cars04.sub[training.sample,]
cars04.test.data <- cars04.sub[-training.sample,]
# Check rows of the train and test datasets
nrow(cars04.train.data)</pre>
```

```
## [1] 310
nrow(cars04.test.data)
```

[1] 77

First rows of the train and test datasets head(cars04.train.data)

##			Sports	Retail	Dealer	Engine	: Cylinders	Horse	epower
##	Acura 3.5 RL	Navigation	0	46100	41100	3.5	6		225
##	Acura NSX S		1	89765	79978	3.2	: 6		290
##	Acura RSX		0	23820	21761	2.0	4		200
##	Acura TSX		0	26990	24647	2.4	. 4		200
##	Audi A4 1.8T		0	25940	23508	1.8	3 4		170
##	Audi A4 1.8T	${\tt convertible}$	0	35940	32506	1.8	3 4		170
##			CityMPC	Highwa	ayMPG W	deight W	heelbase L	ength	Width
##	Acura 3.5 RL	Navigation	18	3	24	3893	115	197	72
##	Acura NSX S		17	•	24	3153	100	174	71
##	Acura RSX		24	Ŀ	31	2778	101	172	68
##	Acura TSX		22	2	29	3230	105	183	69
##	Audi A4 1.8T		22	2	31	3252	104	179	70
##	Audi A4 1.8T	${\tt convertible}$	23	3	30	3638	105	180	70

head(cars04.test.data)

##		Sports	Retail	Dealer	Engine Cy	linders
##	Acura 3.5 RL	0	43755	39014	3.5	6
##	Acura MDX	0	36945	33337	3.5	6
##	Acura TL	0	33195	30299	3.2	6
##	Audi A6 2.7 Turbo Quattro four-door	0	42840	38840	2.7	6
##	Audi A6 3.0 Avant Quattro	0	40840	37060	3.0	6
##	Audi A6 3.0 Quattro	0	39640	35992	3.0	6
##		Horsepo	ower Ci	tyMPG H	ighwayMPG	Weight
##	Acura 3.5 RL		225	18	24	3880
##	Acura MDX		265	17	23	4451
##	Acura TL		270	20	28	3575
##	Audi A6 2.7 Turbo Quattro four-door		250	18	25	3836
##	Audi A6 3.0 Avant Quattro		220	18	25	4035
##	Audi A6 3.0 Quattro		220	18	25	3880
##		Wheelba	ase Leng	gth Wid	th	
##	Acura 3.5 RL	:	115	197	72	
##	Acura MDX	:	106	189 '	77	
##	Acura TL	-	108	186	72	
##	Audi A6 2.7 Turbo Quattro four-door	-	109	192 '	71	
##	Audi A6 3.0 Avant Quattro		109	192 '	71	
##	Audi A6 3.0 Quattro	:	109	192	71	

There are many methodologies for constructing regression trees but one of the oldest is known as the classification and regression tree (CART) approach developed by Breiman et al. (1984).

Basic regression trees partition a data set into smaller subgroups and then fit a simple constant for each observation in the subgroup. The partitioning is achieved by successive binary partitions (aka recursive partitioning) based on the different predictors. The constant to predict is based on the average response values for all observations that fall in that subgroup (if regression tree) or majority vote (if clasification tree).

There exist different packages in R to implement decision trees. In the following we will use the rpart package to implement the tree and the rpart.plot and rattle plackages for visualizations.

1.1 Regression Tree

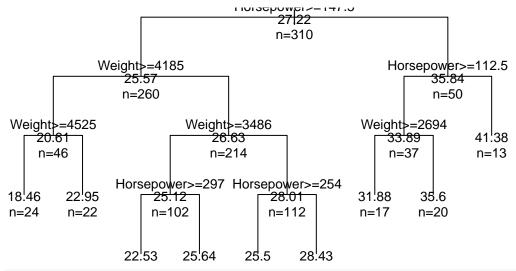
Let's consider that we want to predict the Highway Mileage of a car. We fit a regression tree to the training dataset only and look at the output.

```
## Regression tree
reg.tree.fit <- rpart(</pre>
                  formula = HighwayMPG ~ Retail + Dealer + Engine + Cylinders +
                    Horsepower + Weight + Wheelbase + Length + Width,
                  method ="anova",
                  data = cars04.train.data)
# Look at regression tree
reg.tree.fit
## n= 310
##
## node), split, n, deviance, yval
##
         * denotes terminal node
##
    1) root 310 10023.64000 27.22258
##
##
      2) Horsepower>=147.5 260 3489.88800 25.56538
        4) Weight>=4185 46
##
                              474.95650 20.60870
##
          8) Weight>=4525 24
                                127.95830 18.45833 *
##
          9) Weight< 4525 22
                                114.95450 22.95455 *
##
        5) Weight< 4185 214 1641.83600 26.63084
         10) Weight>=3486 102
##
                                 566.58820 25.11765
           20) Horsepower>=297 17
##
                                      30.23529 22.52941 *
           21) Horsepower< 297 85
##
                                     399.69410 25.63529 *
##
         11) Weight< 3486 112
                                 628.99110 28.00893
           22) Horsepower>=254 16
                                      34.00000 25.50000 *
##
##
           23) Horsepower< 254 96
                                     477.48960 28.42708 *
      3) Horsepower< 147.5 50 2106.72000 35.84000
##
##
        6) Horsepower>=112.5 37
                                   399.56760 33.89189
##
         12) Weight>=2694.5 17
                                   99.76471 31.88235 *
##
         13) Weight< 2694.5 20
                                  172.80000 35.60000 *
##
        7) Horsepower< 112.5 13 1167.07700 41.38462 *
```

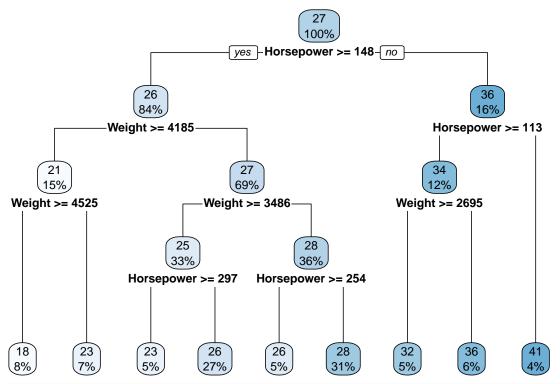
The output tells us that there are 310 observations in the Root branch 310 observations with SSE = 10023 and a HighwayMPG prediction of 27.22. The First split happens on the Horsepower variable. The number of observations i.e. cars with a Horsepower >= 147.5 is 260 and the SSE = 3489 and HighwayMPG prediction = 25.56 for this branch. This means that Horsepower is the variable having the most important reduction in SSE, then it's Engine. The second most important variable is Weight and so on.

The tree can be plotted using base R or the rpart.plot and rattle packages as follow

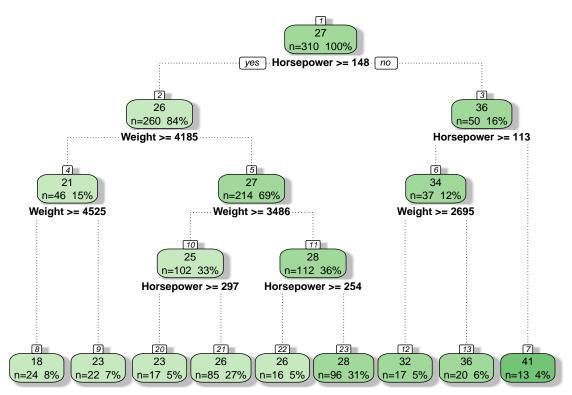
Regression Tree for Highway Mileage



Using rpart package
rpart.plot(reg.tree.fit)



Using the rattle packages
fancyRpartPlot(reg.tree.fit)



Rattle 2019-Nov-12 14:58:31 laeb

We can use this model to predict the HIghwayMPG on the test dataset and compared with the observed value. This is done as follows

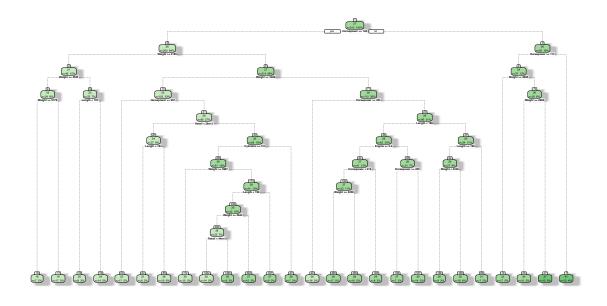
```
# Predict on test dataset
pred <- predict(reg.tree.fit, newdata = cars04.test.data)
RMSE(pred = pred, obs = cars04.test.data$HighwayMPG)</pre>
```

[1] 3.296994

Often a balance needs to be found in the depth and complexity of the tree to optimize predictive performance on unseen data. This is done by pruning the tree. The package rpart is actually behind the scene already aplying a cost complexity alpha values to prune the tree. It is performing a 10 fold CV on the training dataset to decide the optimal value of alpha i.e. the value of alpha for which the CV error is minimal. In our example, the tree was pruned to have 9 leaves i.e. 9 leaves was found to be the size of the tree for which the CV error is minimal. The dashed line indicates the 1 standard deviation of the minimum CV error. In practice it is common to use a tree with the minimum size within 1 standard deviation of the minimum CV error.

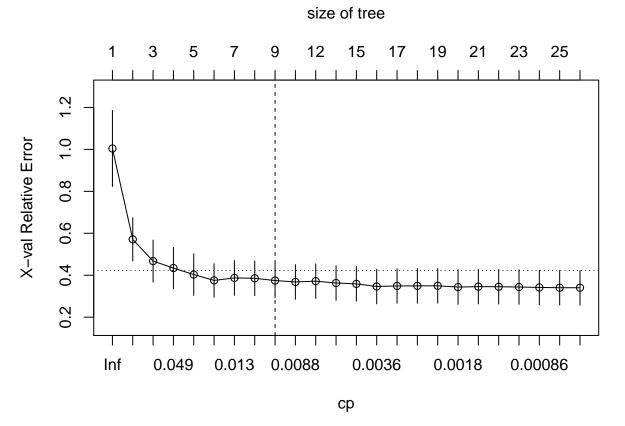
Let's force rpart to generate the full tree (no penalty done i.e. no pruning)

```
# Force rpart to generate a full tree with no penalty
reg.tree.fit2 <- rpart(
  formula = HighwayMPG ~ Retail + Dealer + Engine + Cylinders +
        Horsepower + Weight + Wheelbase + Length + Width,
        data = cars04.train.data,
        method = "anova",
        control = list(cp = 0)
)
fancyRpartPlot(reg.tree.fit2)</pre>
```



Rattle 2019-Nov-12 14:58:32 laeb

```
plotcp(reg.tree.fit2)
abline(v = 9, lty = "dashed")
```



If we were to predict with this tree the HighwayMPG on the testd dataset

```
# Predict on test dataset
pred <- predict(reg.tree.fit2, newdata = cars04.test.data)
RMSE(pred = pred, obs = cars04.test.data$HighwayMPG)</pre>
```

```
## [1] 3.085369
```

In addition to the cost complexity parameter, one can tune other parameters e.g. minsplit and maxdepth using the control arguments of rpart.

- minsplit: Set the minimum number of observations in the node before the algorithm perform a split
- maxdepth: Set the maximum depth of any node of the final tree. The root node is treated a depth 0

One can manually tune these parameters and assess the performance of your model. But this might be cumbersome, instead one can make a grid search.

```
# Make a grid to search
hypergrid <- expand.grid(
  minsplit = seq(5, 20, 1),
  maxdepth = seq(3, 9, 1)
)
head(hypergrid) # head of the grid</pre>
```

```
##
     minsplit maxdepth
## 1
            5
## 2
            6
                      3
## 3
            7
                      3
## 4
            8
                      3
## 5
            9
                      3
## 6
           10
                      3
```

nrow(hypergrid) # total number of combinations

```
## [1] 112
```

```
# One model for each hyperparameter combination
models <- list()
for (i in 1:nrow(hypergrid)) {
  # get minsplit, maxdepth values at row i
  minsplit <- hypergrid$minsplit[i]</pre>
  maxdepth <- hypergrid$maxdepth[i]
  # train a model and store in the list
  models[[i]] <- rpart(</pre>
    formula = HighwayMPG ~ Retail + Dealer + Engine + Cylinders +
      Horsepower + Weight + Wheelbase + Length + Width,
            = cars04.train.data,
    method = "anova",
    control = list(minsplit = minsplit, maxdepth = maxdepth)
  )
}
# function to get optimal cp
getcp <- function(x) {</pre>
         <- which.min(x$cptable[, "xerror"])</pre>
  cp <- x$cptable[min, "CP"]</pre>
}# function to get minimum error
getminerror <- function(x) {</pre>
         <- which.min(x$cptable[, "xerror"])
  xerror <- x$cptable[min, "xerror"]</pre>
```

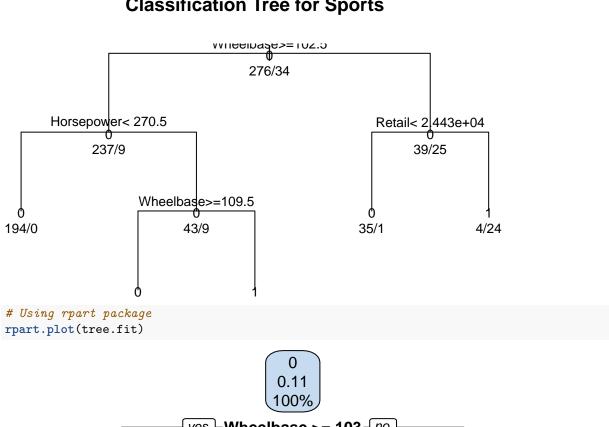
```
hypergrid_min <- hypergrid %>%
  mutate(
          = purrr::map_dbl(models, getcp),
    ср
   error = purrr::map_dbl(models, getminerror)
  ) %>%
 arrange(error) %>%
 top_n(-5, wt = error)
hypergrid_min
     minsplit maxdepth
                                       error
                               ср
                     9 0.01000000 0.3463026
## 1
           10
## 2
           14
                     3 0.01267033 0.3481227
## 3
           7
                     8 0.01000000 0.3493651
## 4
           12
                    7 0.01000000 0.3515852
## 5
           15
                     3 0.01267033 0.3517852
# Optimal Model
reg.tree.fit.opt <- rpart(
  formula = HighwayMPG ~ Retail + Dealer + Engine + Cylinders +
   Horsepower + Weight + Wheelbase + Length + Width,
        = cars04.train.data,
  data
 method = "anova",
  control = list(minsplit = 10, maxdepth = 9, cp = 0.01)
)
# Predict on test dataset
pred <- predict(reg.tree.fit.opt, newdata = cars04.test.data)</pre>
RMSE(pred = pred, obs = cars04.test.data$HighwayMPG)
## [1] 3.296994
```

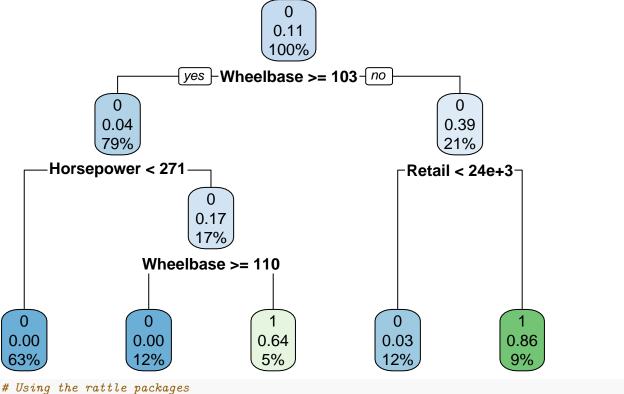
1.2 Classification Tree

```
# Grow tree
tree.fit <- rpart(Sports ~ Retail + Dealer + Engine + Cylinders + Horsepower + CityMPG + HighwayMPG + W
            method="class", data = cars04.train.data)
# Look at output
tree.fit
## n= 310
##
## node), split, n, loss, yval, (yprob)
         * denotes terminal node
##
##
   1) root 310 34 0 (0.89032258 0.10967742)
##
      2) Wheelbase>=102.5 246 9 0 (0.96341463 0.03658537)
##
##
        4) Horsepower< 270.5 194 0 0 (1.00000000 0.00000000) *
##
        5) Horsepower>=270.5 52 9 0 (0.82692308 0.17307692)
##
         10) Wheelbase>=109.5 38 0 0 (1.00000000 0.00000000) *
         11) Wheelbase< 109.5 14 5 1 (0.35714286 0.64285714) *
##
##
      3) Wheelbase< 102.5 64 25 0 (0.60937500 0.39062500)
##
       6) Retail< 24432.5 36 1 0 (0.97222222 0.02777778) *
##
       7) Retail>=24432.5 28 4 1 (0.14285714 0.85714286) *
```

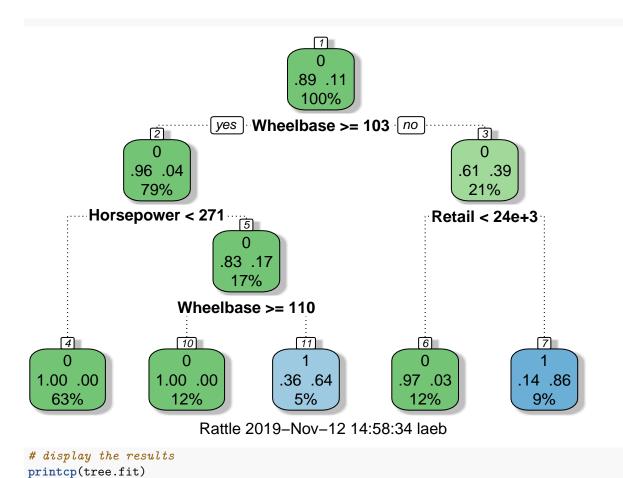
```
# plot tree
\# Directly using base R
plot(tree.fit, uniform=TRUE,
     main="Classification Tree for Sports")
text(tree.fit, use.n=TRUE, all=TRUE, cex=.8)
```

Classification Tree for Sports



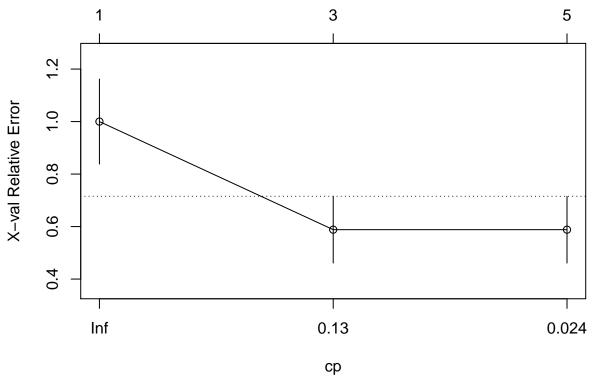


fancyRpartPlot(tree.fit)



```
##
## Classification tree:
## rpart(formula = Sports ~ Retail + Dealer + Engine + Cylinders +
       Horsepower + CityMPG + HighwayMPG + Weight + Wheelbase +
       Length + Width, data = cars04.train.data, method = "class")
##
##
## Variables actually used in tree construction:
## [1] Horsepower Retail
                             Wheelbase
##
## Root node error: 34/310 = 0.10968
##
## n= 310
##
##
           CP nsplit rel error xerror
## 1 0.294118
                   0
                       1.00000 1.00000 0.16182
## 2 0.058824
                   2
                       0.41176 0.58824 0.12722
## 3 0.010000
                   4
                       0.29412 0.58824 0.12722
# visualize cross-validation results
plotcp(tree.fit)
```

size of tree



detailed summary of splits summary(tree.fit)

```
## Call:
## rpart(formula = Sports ~ Retail + Dealer + Engine + Cylinders +
       Horsepower + CityMPG + HighwayMPG + Weight + Wheelbase +
##
       Length + Width, data = cars04.train.data, method = "class")
##
     n = 310
##
##
##
             CP nsplit rel error
                                     xerror
                                                 xstd
                     0 1.0000000 1.0000000 0.1618208
## 1 0.29411765
## 2 0.05882353
                     2 0.4117647 0.5882353 0.1272197
                     4 0.2941176 0.5882353 0.1272197
## 3 0.01000000
##
## Variable importance
##
                                                               CityMPG
       Retail Horsepower
                             Dealer
                                      Wheelbase
                                                     Width
##
           14
                                  13
                                             12
                                                         11
                                                                    10
                      13
## HighwayMPG
                  Length
                              Weight
                                         Engine
                                                 Cylinders
##
##
## Node number 1: 310 observations,
                                        complexity param=0.2941176
     predicted class=0 expected loss=0.1096774 P(node) =1
##
##
       class counts:
                       276
     probabilities: 0.890 0.110
##
     left son=2 (246 obs) right son=3 (64 obs)
##
##
     Primary splits:
##
         Wheelbase < 102.5
                               to the right, improve=12.731720, (0 missing)
                               to the left, improve=11.449810, (0 missing)
##
         Retail
                    < 75880
```

```
##
                    < 69198.5 to the left, improve= 9.848602, (0 missing)
##
                    < 177.5
                              to the right, improve= 7.497176, (0 missing)
         Length
##
         Horsepower < 256.5
                              to the left, improve= 6.378697, (0 missing)
##
     Surrogate splits:
##
         Length
                    < 167.5
                              to the right, agree=0.884, adj=0.438, (0 split)
##
         Weight
                              to the right, agree=0.852, adj=0.281, (0 split)
                    < 3163
##
                              to the right, agree=0.842, adj=0.234, (0 split)
         Horsepower < 126.5
                              to the right, agree=0.839, adj=0.219, (0 split)
##
         Engine
                    < 1.95
                              to the right, agree=0.829, adj=0.172, (0 split)
##
         Retail
                    < 14775
##
## Node number 2: 246 observations,
                                       complexity param=0.05882353
     predicted class=0 expected loss=0.03658537 P(node) =0.7935484
##
##
       class counts:
                       237
##
      probabilities: 0.963 0.037
##
     left son=4 (194 obs) right son=5 (52 obs)
##
     Primary splits:
##
                              to the left, improve=2.4568480, (0 missing)
         Horsepower < 270.5
##
                              to the right, improve=1.0178080, (0 missing)
##
         Retail
                    < 56172.5 to the left, improve=0.8531517, (0 missing)
                    < 50459.5 to the left, improve=0.8531517, (0 missing)
##
         Dealer
##
         HighwayMPG < 26.5</pre>
                              to the right, improve=0.5414634, (0 missing)
##
     Surrogate splits:
##
         Retail
                   < 46182.5 to the left, agree=0.907, adj=0.558, (0 split)
##
         Dealer
                   < 41433.5 to the left, agree=0.898, adj=0.519, (0 split)
##
         Cylinders < 7
                             to the left, agree=0.898, adj=0.519, (0 split)
                             to the left, agree=0.890, adj=0.481, (0 split)
##
         Engine
                   < 4.1
                             to the right, agree=0.833, adj=0.212, (0 split)
##
         CityMPG
                   < 14.5
## Node number 3: 64 observations,
                                      complexity param=0.2941176
     predicted class=0 expected loss=0.390625 P(node) =0.2064516
##
##
       class counts:
                        39
                              25
##
     probabilities: 0.609 0.391
##
     left son=6 (36 obs) right son=7 (28 obs)
##
     Primary splits:
##
         Retail
                    < 24432.5 to the left, improve=21.66716, (0 missing)
##
         Dealer
                    < 22391.5 to the left, improve=21.66716, (0 missing)
##
         Width
                    < 68.5
                              to the left, improve=21.37158, (0 missing)
##
         Horsepower < 205
                              to the left, improve=21.32156, (0 missing)
                              to the right, improve=18.92757, (0 missing)
##
         CityMPG
                    < 21.5
##
     Surrogate splits:
##
                    < 22391.5 to the left, agree=1.000, adj=1.000, (0 split)
         Dealer
                              to the left, agree=0.938, adj=0.857, (0 split)
##
         Horsepower < 167.5
                              to the right, agree=0.906, adj=0.786, (0 split)
##
         CityMPG
                    < 21.5
##
                              to the right, agree=0.906, adj=0.786, (0 split)
         HighwayMPG < 29.5
##
         Width
                    < 68.5
                              to the left, agree=0.906, adj=0.786, (0 split)
##
## Node number 4: 194 observations
     predicted class=0 expected loss=0 P(node) =0.6258065
##
       class counts:
##
                       194
##
      probabilities: 1.000 0.000
##
## Node number 5: 52 observations,
                                      complexity param=0.05882353
##
    predicted class=0 expected loss=0.1730769 P(node) =0.1677419
##
       class counts:
                        43
```

```
##
     probabilities: 0.827 0.173
##
     left son=10 (38 obs) right son=11 (14 obs)
##
     Primary splits:
##
         Wheelbase < 109.5 to the right, improve=8.456044, (0 missing)
##
         Length
                  < 180.5
                           to the right, improve=6.875092, (0 missing)
##
                   < 3555.5 to the right, improve=4.738584, (0 missing)
         Weight
                   < 4.05 to the right, improve=3.869094, (0 missing)
##
         Engine
                             to the right, improve=2.646520, (0 missing)
##
         Cylinders < 7
##
     Surrogate splits:
##
         Length
                   < 181.5 to the right, agree=0.942, adj=0.786, (0 split)
##
         Weight
                   < 3650
                            to the right, agree=0.865, adj=0.500, (0 split)
                             to the right, agree=0.846, adj=0.429, (0 split)
##
                   < 3.7
         Engine
                   < 70.5
##
         Width
                             to the right, agree=0.846, adj=0.429, (0 split)
                             to the right, agree=0.808, adj=0.286, (0 split)
##
         Cylinders < 7
##
## Node number 6: 36 observations
     predicted class=0 expected loss=0.02777778 P(node) =0.116129
##
##
       class counts:
                        35
##
      probabilities: 0.972 0.028
##
## Node number 7: 28 observations
    predicted class=1 expected loss=0.1428571 P(node) =0.09032258
##
##
                         4
       class counts:
                              24
      probabilities: 0.143 0.857
##
##
## Node number 10: 38 observations
     predicted class=0 expected loss=0 P(node) =0.1225806
##
##
       class counts:
                        38
##
     probabilities: 1.000 0.000
##
## Node number 11: 14 observations
##
     predicted class=1 expected loss=0.3571429 P(node) =0.04516129
##
       class counts:
                         5
      probabilities: 0.357 0.643
##
# make predictions from the tree
tree.pred <- predict(tree.fit, cars04.test.data, type = "class")</pre>
cars04.test.data.pred <- cars04.test.data %>% mutate(Sports.pred = tree.pred)
# Performance
tab <- table(cars04.test.data.pred$Sports, cars04.test.data.pred$Sports.pred)
tab
##
##
        0 1
##
     0 64 2
       3 8
     1
# Sensitivity TP/(TP + FN)
tab[2,2]/(tab[2,2] + tab[2,1])
## [1] 0.7272727
# Specificity TN/(TN + FP)
tab[1,1]/(tab[1,1] + tab[1,2])
## [1] 0.969697
```

```
# Precision TP/predicted yes.
tab[2,2]/(tab[2,2] + tab[1,2])
## [1] 0.8
# Accuracy (TP + TN)/(All)
(tab[2,2] + tab[1,1])/(tab[2,2] + tab[1,1] + tab[1,2] + tab[2,1])
## [1] 0.9350649
```

2 Bagging

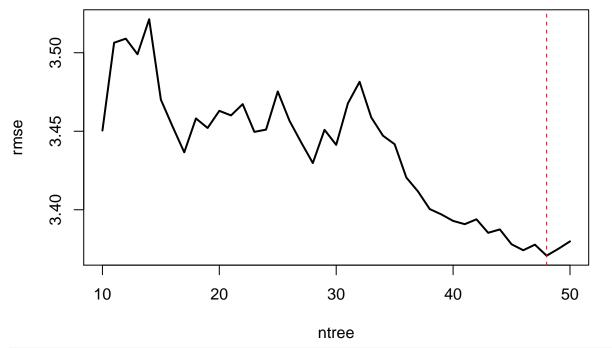
Bagging combines and averages multiple models. Averaging across multiple trees reduces the variability of any one tree and reduces overfitting, which improves predictive performance. Steps:

- Create m bootstrapped samples from the training data
- For each bootstrapped sample train, make an unprunned tree model
- Average the prediction for each tree to create an overall average

Bagging will be implemented with the ipred and caret package.

```
# train bagged model
bagged.reg.tree.fit <- bagging(</pre>
  formula = HighwayMPG ~ Retail + Dealer + Engine + Cylinders +
    Horsepower + Weight + Wheelbase + Length + Width,
          = cars04.train.data,
  data
          = TRUE
  coob
)
bagged.reg.tree.fit
##
## Bagging regression trees with 25 bootstrap replications
## Call: bagging.data.frame(formula = HighwayMPG ~ Retail + Dealer + Engine +
##
       Cylinders + Horsepower + Weight + Wheelbase + Length + Width,
##
       data = cars04.train.data, coob = TRUE)
## Out-of-bag estimate of root mean squared error: 3.4163
# By default the number of trees used is 25 but this might not be enough
# assess 10-50 bagged trees
ntree <- 10:50
# create empty vector to store OOB RMSE values
rmse <- vector(mode = "numeric", length = length(ntree))</pre>
for (i in seq_along(ntree)) {
  # reproducibility
  set.seed(123)
  # perform bagged model
  model <- bagging(</pre>
    formula = HighwayMPG ~ Retail + Dealer + Engine + Cylinders +
      Horsepower + Weight + Wheelbase + Length + Width,
    data
            = cars04.train.data,
    coob
            = TRUE,
```

```
nbagg = ntree[i]
)
# get 00B error
rmse[i] <- model$err
}
plot(ntree, rmse, type = 'l', lwd = 2)
abline(v = 48, col = "red", lty = "dashed")</pre>
```



```
# Use 45 trees instead of 25
opt.bagged.reg.tree.fit <- bagging(
  formula = HighwayMPG ~ Retail + Dealer + Engine + Cylinders +
        Horsepower + Weight + Wheelbase + Length + Width,
        data = cars04.train.data,
        coob = TRUE,
        nbagg = 48
)
opt.bagged.reg.tree.fit</pre>
```

```
##
## Bagging regression trees with 48 bootstrap replications
##
## Call: bagging.data.frame(formula = HighwayMPG ~ Retail + Dealer + Engine +
## Cylinders + Horsepower + Weight + Wheelbase + Length + Width,
## data = cars04.train.data, coob = TRUE, nbagg = 48)
##
## Out-of-bag estimate of root mean squared error: 3.3648
```

3 Boosting

Several supervised machine learning models are founded on a single predictive model (i.e. linear regression, penalized models, naive Bayes, support vector machines). Alternatively, other approaches such as bagging

and random forests are built on the idea of building an ensemble of models where each individual model predicts the outcome and then the ensemble simply averages the predicted values. The family of boosting methods is based on a different, constructive strategy of ensemble formation. The main idea of boosting is to add new models to the ensemble sequentially. At each particular iteration, a new weak, base-learner model is trained with respect to the error of the whole ensemble learnt so far.