The Slope of the Phillips Curve: Evidence from US States

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Table of Contents

Theme: Estimate the slope of the Phillips Curve with state-level data to solve the "Phillips Curve Puzzle".

- 1. Introduction to the Phillips Curve Puzzle
 - Why has the Phillips Curve flattened out?
- 2. What is this paper's solution to the puzzle? Why does it work?
 - Regional approach: Estimate a state-level Phillips Curve
 - Long Run approach: Estimate a long-run Phillips Curve
- 3. Theoretical Justification
 - ► A regional model of the Phillips Curve.
 - Shows that the slope of the regional, long-run Phillips Curve is comparable to the overall Phillips Curve.
- 4. Empirical analysis
 - Does our regional, long-run approach solve the "Phillips Curve Puzzle"?

- New Keynesian Phillips Curve measures the relationship between unemployment and inflation.
 - ▶ In the 1980's, we observed a strong negative correlation between unemployment and inflation.
 - Contractionary policy tamped down on inflation while unemployment soared.
 - In the Great Recession, unemployment rose, but we saw small changes in inflation.
- What changed in the last 30 years?
 - Has the Phillips Curve flattened?
- Our Solution: Perhaps, nothing changed.
 - Could we have been estimating the slope of the Phillips Curve wrong all along?
 - Identification problems, which have since subsided, misled our estimate in the late 1900's.
 - ▶ If we deal with the identification problems, estimates of the curve in the 1980's are in line with estimates today.

What happened to the slope of the Phillips Curve?

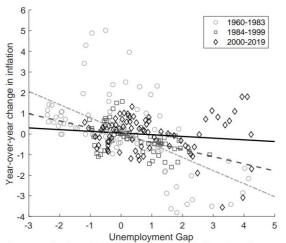
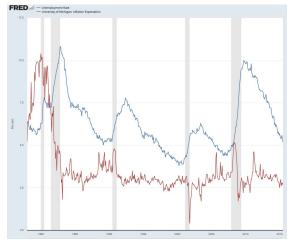


Figure 1: Stock and Watson's Changing Phillips Correlation

- Unemployment has varied across the last 4 decades, but the inflation gap remained small.
- ► What is going wrong here?



Phillips Curve intuition: High demand drives up wages and prices.

$$\pi_t = \beta E_t \pi_{t+1} - \kappa (u_t - u_t^n) + \nu_t \tag{1}$$

- Inflation is related to **inflation expectations** and the unemployment gap.
- κ is the slope of the Phillips Curve.
- Major identification problems:
 - 1. Covariation in inflation expectations and unemployment may bias an estimate of κ .
 - 2. Supply shocks may contaminate an estimate of κ .
 - Supply and demand shocks lead to opposite comovement in inflation and observed unemployment.
- Our solution is a fixed effects approach.
 - 1. Requires estimation of a long-run Phillips Curve.
 - 2. Requires estimation of a regional Phillips Curve.

Problem 1: Inflation Expectations

- In the 80's $Cov(U_t, E_t[\pi_{t+1}]) < 0$ with a large magnitude.
 - ► The estimated slope of the Phillips Curve may have been exaggerated.
- ▶ Theory suggest $E_t \pi_{t+1} \pi_t$ is explained by κu_t .
 - That the difference between these two variables has been relatively constant suggests that κ has not changed by much.



Figure 2: PCE Core Inflation and Long-Term Inflation Expectations

Problem 1: Solve with a long-run approach

- If our estimate of κ is biased from covariance between $E_t \pi_{t+1}$ and u_t , regional fixed effects may provide a solution.
 - Can we difference out inflation expectations?
 - Short run inflation expectations may vary from state to state.
 - ▶ But what about expected long-run expected inflation?
- From (1), derive the long-run Phillips Curve.

$$\pi_t = -\kappa E_t \sum_{j=0}^{\infty} \beta^j \tilde{u}_{t+j} - E_t \pi_{t+\infty} + \omega_t$$
 (2)

- ▶ Inflation expectations show up at the infinite time horizon.
- $ightharpoonup E_t \pi_{t+\infty}$ is regionally invariant,
 - Depend on the public's expectations of the policymaker's long-term behavior.
- Implement regional fixed effects and difference out inflation expectations from estimation.

Problem 2: Contamination from Supply Shocks

- Observed unemployment is a poor proxy for the output gap in the presence of supply shocks.
 - Supply shocks fundamentally alter firm productivity, affecting the natural rate of unemployment.
 - A positive supply shock may accelerate output (and prices) and the natural rate of unemployment.
- We use demand shocks to tradeable goods as an instrument for unemployment.
 - An increase in demand for oil in California reduces unemployment in Texas.
- Why do we need a regional approach?
 - Demand shocks may affect the natural rate of unemployment because consumers need to work more to satisfy demand.
 - ▶ With a regional approach, we isolate shocks in different states.

Identification Problems: Solutions

- 1. **Problem**: κ is biased because u_t and $E_t \pi_{t+1}$ are correlated.
 - Long-run inflation expectations are regionally invariant.
 - Regional fixed effects difference out long-run inflation expectations.
- 2. **Problem**: κ is contaminated because we cannot isolate supply and demand side shocks.
 - ▶ Demand shocks to tradeable goods are correlated with the regional unemployment gap.
 - A regional framework insulates regional markets from tradeable goods markets in other states.
 - So that tradeable demand shocks are a suitable proxy for the unemployment gap.
- Our Strategy:
 - 1. Estimate a long-run version of a regional Phillips Curve...
 - 2. With regional fixed effects...
 - 3. And an instrumental variable for the unemployment gap.



What's Next?

- Why is it OK to estimate the long-run regional curve instead of the overall curve?
- We construct a regional model in which states have tradeable and non-tradeable goods markets.
 - ► Tradeable goods are sold in all regions.
 - ▶ Nontradeable goods are sold in the region they were produced.
- We extract a regional Phillips Curve for the non-tradeable goods market.
 - Slope of regional non-tradeable Phillips Curve is equal to slope of the national Phillips Curve.
- Estimate the long-run version of our regional non-tradeable Phillips Curve with fixed effects and an instrument for unemployment.
 - ► Slope of the long-run regional curve is related to the short-run slope of the overall curve.

Model: Overview

- Consider a two-region, New Keynesian, open economy model with tradeable and non-tradeable sectors.
- ► In the Home Region:
 - 1. Home consumers.
 - 2. Home firms are subject to Calvo-style price rigidities.
 - Firms that produce tradeable goods.
 - Firms that produce non-tradeable goods.
- ▶ The Foreign Region is identical to the Home Region.
- Tradeable and non-tradeable goods are priced and sold in different markets.
- A central monetary policy maker sets nominal interest rates.
 - According to time varying inflation target.
 - Time varying inflation target may cause identification problem

Model: Households

- Households maximize lifetime utility.
 - Utility is separable in leisure and consumption.

$$\mathsf{Max}_{C_{Ht},N_{Ht}} \left\{ E_t \sum_{t=0}^{\infty} \beta^t u(C_{Ht},N_{Ht}) \right\}$$
 (3)

- Households demand both tradeable and non-tradeable goods.
 - The composite consumption good is a CES index over a tradeable and non-tradeable goods index.

$$C_{Ht} = \left[\phi_N^{\frac{1}{\eta}} C_{Ht}^{N\frac{\eta-1}{\eta}} + \phi_T^{\frac{1}{\eta}} C_{Ht}^{T\frac{\eta-1}{\eta}} \right]^{\frac{\eta}{\eta-1}}$$
(4)

- $ightharpoonup C_{Ht}^N$ and C_{Ht}^T are composite tradeable and non-tradeable consumption goods.
 - Subject to demand shocks.

Model: Households

- Households earn wages and firm profits to consume and invest.
- Households supply labor with respect to the real wage.

$$\chi N_{Ht}^{\rho^{-1}} = \frac{W_{Ht}}{P_{Ht}} \tag{5}$$

- P_{Ht} is the overall price level in the home region and differs from the overall price level in the foreign region.
- ► The real wage is measured in "home dollars".
- $\triangleright \chi$ is disutility from labor.
 - Unemployment reflects demand for leisure.

Model: Nominal Rigidities and Price Setting

Firm output is a function of labor input and a productivity shock.

$$Y_{Ht}^N(z) = Z_{Ht}^N N_{Ht}^N(z) \tag{6}$$

- Firms are subject to Calvo-style price rigidities.
 - A fraction 1α of firms may reoptimize each period.
 - Firms set prices to maximize discounted sum of expected profits.

$$\sum_{k=0}^{\infty} \alpha^k E_t \left[M_{Ht,t+k} Y_{H,t+k}^N(z) \left(P_{Ht}^{N*}(z) - \frac{\theta}{\theta - 1} S_{H,t+k}^N(z) \right) \right]$$
(7)

Productivity shocks carry through to nominal marginal cost, affecting the natural rate of unemployment.

Model: Monetary Policy

► The Central Bank operates a common monetary policy rule for both regions.

$$\hat{r}_t^n = \rho_\pi(\pi_t - \bar{\pi}_t) - \rho_u(\hat{u}_t - \bar{u}_t) + \epsilon_{rt}$$
(8)

The interest rate rule balances time-varying inflation and unemployment targets, $\bar{\pi}_t$ and \bar{u}_t .

$$\bar{u}_t = \frac{(1-\beta)\bar{\pi}_t}{\kappa} \tag{9}$$

- Time-varying targets ensure that:
 - 1. Inflation expectations are non-zero at the infinite-time horizon.
 - 2. Inflation and unemployment deviate from their inflation-free steady-state values.
 - Expected unemployment does not equal the natural rate of unemployment.

Model: Inflation and Unemployment

Inflation, π_t , is a population weighted sum of inflation in the home and foreign regions.

$$\pi_{Ht} = p_{Ht} - p_{H,t+1}$$

$$\pi_{Ft} = p_{Ft} - p_{F,t+1}$$
(10)

Economy-wide unemployment is a population weighted average of unemployment in the home and foreign regions.

$$u_{Ht} = 1 - N_{Ht} \tag{12}$$

$$u_{Ft} = 1 - N_{Ft} \tag{13}$$

Model: Regional and Aggregate Phillips Curve

We extract the overall Phillips Curve and regional Phillips Curve for nontradeable goods.

$$\pi_t = \beta E_t \pi_{t+1} - \kappa \hat{u}_t + \nu_t \tag{14}$$

$$\pi_{Ht}^{N} = \beta E_t \pi_{H,t+1} - \kappa \hat{u}_{Ht} - \lambda \hat{p}_{Ht}^{N} + \nu_{Ht}^{N}$$
(15)

- ► They share the same slope.
 - We seamlessly transform from firms' marginal cost to wage to unemployment.
 - Household preferences are additively separable in leisure and consumption.
- ► The regional nontradeable curve includes a term for the relative price of nontradeable goods.
 - Nontradeable marginal costs are deflated by the nontradeable price level.
 - Whereas wage is deflated by the overall regional price level.
- Note: Regional tradeable Phillips Curve has a smaller slope than nontradeable curve.
 - A portion of the tradeable market is unresponsive to regional unemployment.

Empirical Methodology: Putting the model into practice

- ▶ How can we use (15) to solve our identification problems?
 - Can we difference out inflation expectations?
 - Short-run inflation expectations vary region-to-region depending on economic circumstance.
 - ▶ Solution: Use a long-run version of (15).
 - $E_t \pi_{t+\infty}$ depends on expectations of the LR behavior of the monetary regime and is consistent across regions.
- ▶ Up next: Manipulate a long-run version of (15) in order to apply regional and time fixed effects.
 - Afterwards, construct an instrument for unemployment using shocks to demand for tradeable goods.

Empirical Methodology: A long-run approach

▶ Iterate (15) to obtain the long-run nontradeable Phillips Curve for goods produced at home.

$$\pi_{Ht}^{N} = -E_t \sum_{i=0}^{\infty} \beta^j (\kappa \tilde{u}_{H,t+j} + \lambda \hat{p}_{H,t+j}^{N}) + E_t \pi_{t+\infty} + \omega_{Ht}^{N}$$
 (16)

- We can remove $E_t \pi_{t+\infty}$ and include fixed effects.
- ▶ (16) contains expected unemployment and prices at the infinite time horizon.
 - ightharpoonup Truncate infinite expectations at t = T.
 - Replace expected future values with realized values.
 - Include a term for expectational errors.

$$\pi_{it}^{N} = \alpha_i + \gamma_t - \kappa \sum_{j=0}^{T} \beta^j u_{i,t+j} - \lambda \sum_{j=0}^{T} \beta^j \hat{p}_{i,t,j}^{N} + \tilde{\omega}_{it}^{N} + \eta_{it}^{N}$$
 (17)

Empirical Methodology: Contamination from shocks

- ▶ What is the issue with supply shocks?
 - Productivity shocks and future unemployment are correlated.
- We can take two alternate approaches.
 - Instrument for future unemployment with lagged unemployment.
 - Assumes that supply shocks are not systematically related to boom-bust cycles within states.
 - When Texas experiences a boom relative to California, this is not correlated with improvements in technology in Texas relative to California.
 - 2. Instrument for unemployment with tradeable demand shocks.

Empirical Methodology: Tradeable demand shocks

- Why are tradeable demand shocks are a valid proxy for unemployment in our fixed effects regression?
 - ► They differentially affect states' unemployment levels.
 - Increase in demand for oil in California reduces unemployment in Texas by more than it reduces unemployment in Vermont.
 - Beyond the unemployment channel, they shouldn't differentially affect nontradeable sectors.
 - Costs everywhere may rise as a result of higher oil prices, but increases are constant across states.

Tradeable Demand_{it} =
$$\sum_{x} \bar{S}_{x,i} \times \Delta_{3y} \log S_{-i,x,t}$$
 (18)

- $ightharpoonup \bar{S}_{x,i}$: employment share of industry x, excluding state i.
- ▶ $\Delta_{3y} \log S_{-i,x,t}$: three-year growth in employment in industry x, excluding state *i*.

Empirical Results: Has the Phillips Curve Flattened?

Table 2: Has the Phillips Curve Flattened?

Lagged Unempl. IV With Time Fixed Effect		Tradeable Demand IV With Time Fixed Effect	
Pre-1990 (3)	Post-1990 (4)	Pre-1990 (5)	Post-1990 (6)
Estimates of	κ from equati	ion (17)	
0.0107 (0.0080)	0.0050 (0.0040)	0.0109 (0.0062)	0.0055 (0.0028)
Estimates of v	from equati	ion (19)	
0.198	0.090	0.422	0.332 (0.157)
009	0.270	01170	
	With Time Pre-1990 (3) Estimates of (0.0107 (0.0080)) Estimates of (0.198)	With Time Fixed Effect Pre-1990 Post-1990 (3) (4) Estimates of κ from equation (0.0107) 0.0050 (0.0080) (0.0040) Estimates of ψ from equation (0.198) 0.090	With Time Fixed Effect With Time Pre-1990 Post-1990 Pre-1990 (3) (4) (5) Estimates of κ from equation (17) 0.0107 0.0050 0.0109 (0.0080) (0.0040) (0.0062) Estimates of ψ from equation (19) 0.198 0.090 0.422

Empirical Results: Role of inflation expectations

