

# Coronal Waves and Oscillations

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## Abstract

Wave and oscillatory activity of the solar corona is confidently observed with modern imaging and spectral instruments in the visible light, EUV, X-ray and radio bands, and interpreted in terms of magnetohydrodynamic (MHD) wave theory. The review reflects the current trends in the observational study of coronal waves and oscillations (standing kink, sausage and longitudinal modes, propagating slow waves and fast wave trains, the search for torsional waves), theoretical modelling of interaction of MHD waves with plasma structures, and implementation of the theoretical results for the mode identification. Also the use of MHD waves for remote diagnostics of coronal plasma - MHD coronal seismology - is discussed and the applicability of this method for the estimation of coronal magnetic field, transport coefficients, fine structuring and heating function is demonstrated.

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## 1 Introduction

The magnetically dominated plasma of the solar corona is an elastic and compressible medium which can support propagation of various types of waves. For a large class of waves with wavelengths and periods large compared with the ion Larmor radius ( $< 1$  m for almost all combinations of coronal parameters) and the gyroperiod ( $< 10^{-4}$  s), respectively, the waves can be described using magnetohydrodynamics (MHD). These waves perturb macro-parameters of the coronal plasma, such as density, temperature, bulk velocity and the frozen-in magnetic field. For wavelengths comparable with the characteristic sizes of coronal plasma structures (e.g., loop major and minor radii, widths of plumes and helmet structures, size of active regions, and so on), the typical periods are in the range from a few seconds to several minutes. This range is well covered by temporal resolution of presently available ground-based and spaceborne observational tools, allowing for the observational detection of the waves. However, it is very important to understand that in normal circumstances both spatial and temporal resolution are necessary ingredients of successful detection of the waves: e.g., the pixel size must be much smaller than the wavelength (taking into account the projection effect!) and the cadence time must be shorter than the period. Only in certain exceptional cases, e.g., when the wave passes through a bright object with the geometrical size smaller than the wavelength, the wave can be detected with poorer spatial resolution.

The launch of SOHO and TRACE spacecrafts led a revolutionary breakthrough in the observational study of coronal wave activity, including the discoveries of EIT (or coronal Moreton) waves (Thompson *et al.*, 1998), compressible waves in polar plumes (Ofman *et al.*, 1997; DeForest and Gurman, 1998; Ofman *et al.*, 1999) and in coronal loops (Berghmans and Clette, 1999; De Moortel *et al.*, 2000; Robbrecht *et al.*, 2001), flare-generated global kink oscillations of loops (Aschwanden *et al.*, 1999, 2002; Nakariakov *et al.*, 1999; Schrijver *et al.*, 2002), and longitudinal standing oscillations within loops (Kliem *et al.*, 2002; Wang *et al.*, 2002). Also, ground-based radio observations have long revealed the presence of periodic and quasi-periodic phenomena in the corona (Aschwanden, 1987). Moreover, very recently ground-based optical observations of eclipses have revealed the presence of rapid oscillations in coronal loops (Williams *et al.*, 2001, 2002). Extensive observational reviews of this diversity of coronal oscillations are given in Aschwanden (2003); Nakariakov (2003); Aschwanden (2004). The current state of the theoretical studies of MHD wave propagation in the solar atmosphere is discussed in Roberts (2000, 2002); Goossens *et al.* (2002b); Roberts and Nakariakov (2003); Roberts (2004).

MHD waves in the corona have been intensively investigated for more than two decades, primarily in the context of the enigmatic problems of coronal heating and acceleration of the fast solar wind. Discussion of those issues is out of scopes of this review and may be found in Walsh and Ireland (2003); Cranmer (2004); Ofman (2004). It is also believed that the coronal MHD waves play an important role in solar-terrestrial connections. The investigation of the coronal waves is now an essential part of solar physics, space physics, geophysics and astrophysics.

The aim of this review is to reflect the current trends in the observational study of coronal wave and oscillatory phenomena, their phenomenology, their interpretation in terms of MHD wave theory, latest achievements in the theoretical modelling of interaction of MHD waves with inhomogeneous plasmas and its relevance to the coronal waves, and recent progress in MHD coronal seismology.

### 1.1 The method of MHD coronal seismology

Despite significant progress in coronal physics over several decades, a number of fundamental questions, for instance, what are the physical mechanisms responsible for the coronal heating, the solar wind acceleration, and solar flares, remain to be answered. All these questions, however, require detailed knowledge of physical conditions and parameters in the corona, which cannot

yet be measured accurately enough. In particular, the exact value of the coronal magnetic field remains unknown, because of a number of intrinsic difficulties with applications of direct methods (e.g., based upon the Zeeman splitting and gyroresonant emission), as well as indirect (e.g., based upon extrapolation of chromospheric magnetic sources). Also, the coronal transport coefficients, such as volume and shear viscosity, resistivity, and thermal conduction, which play a crucial role in coronal physics, are not measured even within an order of magnitude and are usually obtained from theoretical estimations. Other obscured parameters are the heating function and filling factors.

The detection of coronal waves provides us with a new tool for the determination of the unknown parameters of the corona – *MHD seismology of the corona*. Measurement of the properties of MHD waves and oscillations (periods, wavelengths, amplitudes, temporal and spatial signatures, characteristic scenarios of the wave evolution), combined with a theoretical modelling of the wave phenomena (dispersion relations, evolutionary equations, etc.), leads to a determination of the mean parameters of the corona, such as the magnetic field strength and transport coefficients. This approach is illustrated in Figure 1. Philosophically, the method is similar to the acoustic diagnostics of the solar interior, helioseismology. But, MHD coronal seismology is much richer by its very nature as it is based upon three different wave modes, namely, Alfvén, slow, and fast magnetohydrodynamic modes. These MHD modes have quite different dispersive, polarisation, and propagation properties, which makes this approach even more powerful. A similar method for the determination of physical parameters of laboratory plasmas, MHD spectroscopy, has been successfully used for a decade (see, e.g., the recent review of Fasoli *et al.*, 2002). In particular, the measurements of Alfvén eigenmode frequencies and mode numbers and the comparison between the antenna driven spectrum and that calculated theoretically give information on the bulk plasma, allowing for the improved equilibrium reconstruction in terms of radial profiles of density and safety factor. In contrast with the MHD spectroscopy, MHD coronal seismology utilises propagating waves too.

Originally, the method of MHD coronal seismology was suggested by Uchida (1970) for global and Roberts *et al.* (1984) for local seismology, and has recently been applied to obtain estimates of the magnetic field (Roberts *et al.*, 1984; Nakariakov and Ofman, 2001), the coronal dissipative coefficients (Nakariakov *et al.*, 1999), and to probe coronal sub-resolution structuring (Robbrecht *et al.*, 2001; King *et al.*, 2003). These implementations are discussed in Sections 3.3, 3.4 and 6.3, respectively.

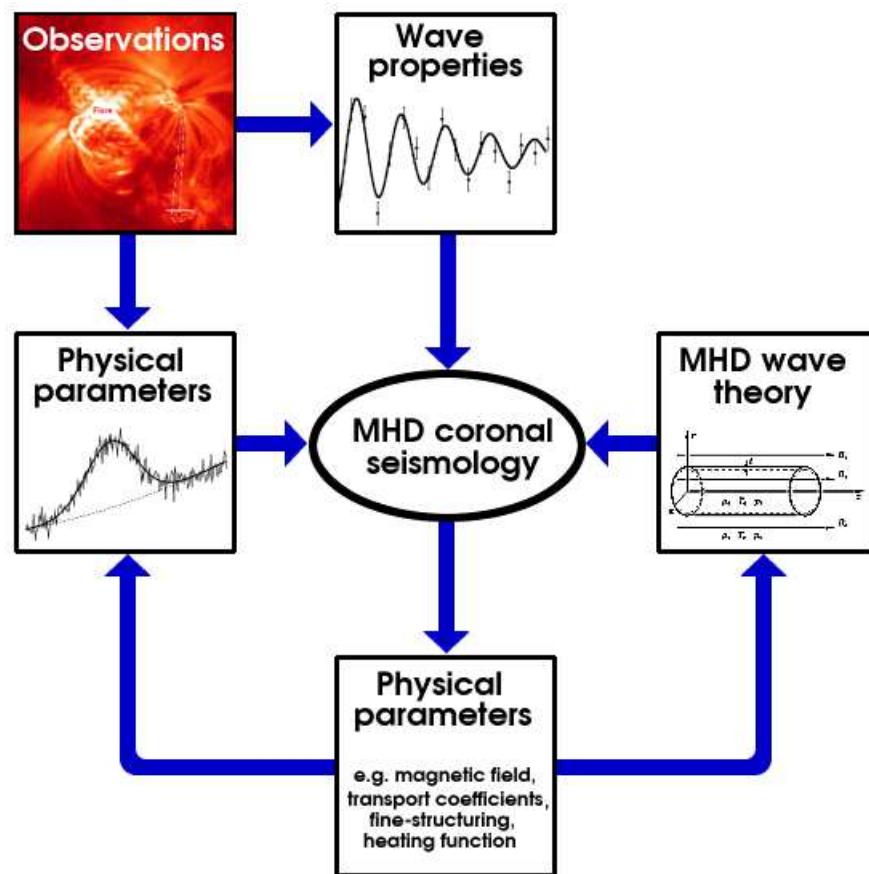


Figure 1: A scheme of the method of MHD coronal seismology.

## 2 Properties of MHD Modes of Plasma Structures

In MHD, wave and oscillatory phenomena have spatial and temporal scales much longer than the ion gyroradii and gyroperiods, respectively, the conditions which are satisfied well by the coronal observational constraints. The characteristic speeds of the MHD phenomena are associated with plasma compressibility and elasticity connected with the frozen-in magnetic field of strength  $B_0$  and with gas pressure  $p_0$ , and with the ion inertia described by the mass density  $\rho_0$ . They are the usual sound speed,  $C_s = (\gamma p_0 / \rho_0)^{1/2}$  with  $\gamma$  the adiabatic index, normally taken to be about 5/3 in the corona, and the Alfvén speed,  $C_A = B_0 / (\mu_0 \rho_0)^{1/2}$ , where  $\mu_0$  is the permeability of vacuum. It is convenient to introduce also the cusp or tube speed,  $C_T = C_s C_A / (C_A^2 + C_s^2)^{1/2}$  which is a combination of the sound and Alfvén speeds. Typical values of those speeds in coronal active regions vary from a hundred to a few thousand km s<sup>-1</sup>.

There are three basic MHD waves: an incompressible Alfvén wave and a fast and slow magnetoacoustic waves, which are both essentially compressible. Properties of MHD waves strongly depend upon the angle between the wave vector and the magnetic field, consequently, MHD waves are highly affected by plasma structuring and filamentation. Structuring of the solar coronal plasma modifies those waves and may lead to their coupling, bringing such interesting features of MHD wave dynamics as phase mixing, resonant absorption, and guided wave propagation, dramatically influencing manifestation of the waves in observations. This makes the theory of MHD wave modes of plasma structures to be the key ingredient of the coronal wave study. Also, the theory provides the necessary classification of wave and oscillatory phenomena in coronal plasmas.

### 2.1 MHD modes of a straight cylinder

An important elementary building block of this theory is dispersion relations for modes of a magnetic cylinder (see Figure 2). Magnetic cylinders are believed to model well such common coronal structures as coronal loops, various filaments, polar plumes, etc. Consider a straight cylindrical magnetic flux tube of radius  $a$  filled with a uniform plasma of density  $\rho_0$  and pressure  $p_0$  within which is a magnetic field  $B_0 \mathbf{e}_z$ ; the tube is confined to  $r < a$  by an external magnetic field  $B_e \mathbf{e}_z$  embedded in a uniform plasma of density  $\rho_e$  and pressure  $p_e$  (here we neglect the effects of twist and steady flows). The very existence of such a plasma configuration requires the balance of the total pressure  $P_{\text{tot}}$ , which is the sum of the plasma and magnetic pressures, between the two media at the boundary. For the equilibrium state, this condition is

$$p_0 + \frac{B_0^2}{2\mu_0} = p_e + \frac{B_e^2}{2\mu_0}. \quad (1)$$

Similarly, a magnetic slab may be introduced in much the same way, having a width  $2a$ .

In the internal and external media, the sound speeds are  $C_{s0}$  and  $C_{se}$ , the Alfvén speeds are  $C_{A0}$  and  $C_{Ae}$ , and the tube speeds are  $C_{T0}$  and  $C_{Te}$ , respectively. Relations between those characteristic speeds determine properties of MHD modes guided by the tube.

The presence of the internal spatial scale, the radius of the tube  $a$ , brings wave dispersion. The standard derivation of linear dispersion relations is based upon linearisation of MHD equations around the equilibrium. The following system of first order differential equations and algebraic equation governs the behaviour of linear perturbations of the form  $\delta P_{\text{tot}}(r) \exp[i(k_z z + m\phi - \omega t)]$  (Sakurai *et al.*, 1991a):

$$\begin{aligned} D \frac{d}{dr} (r \xi_r) &= (C_A^2 + C_s^2) (\omega^2 - C_T^2 k_z^2) \left( \kappa^2 + \frac{m^2}{r^2} \right) r \delta P_{\text{tot}}, \\ \frac{d}{dr} (\delta P_{\text{tot}}) &= \rho_0 (\omega^2 - C_A^2 k_z^2) \xi_r, \end{aligned} \quad (2)$$

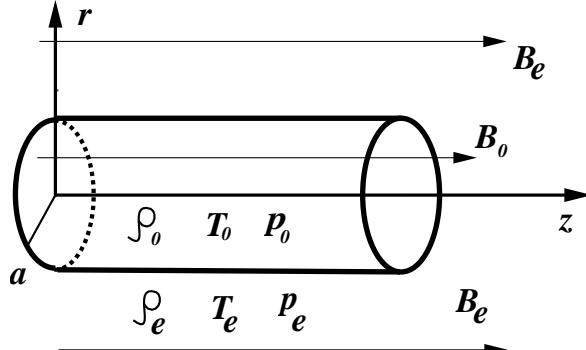


Figure 2: A magnetic flux tube of radius  $a$  embedded in a magnetised plasma.

and

$$\rho_0 (\omega^2 - C_A^2 k_z^2) \xi_\varphi = -\frac{im}{r} \delta P_{\text{tot}}, \quad (3)$$

where  $\xi_r$  and  $\xi_\varphi$  are the perturbation displacements in the radial and azimuthal direction, respectively. The quantity  $D$  is defined as

$$D = \rho_0 (C_A^2 + C_s^2) (\omega^2 - C_A^2 k_z^2) (\omega^2 - C_T^2 k_z^2), \quad (4)$$

and  $\kappa$  plays the role of the transverse wave number and is defined as

$$\kappa^2(\omega) = -\frac{(\omega^2 - C_s^2 k_z^2)(\omega^2 - C_A^2 k_z^2)}{(C_s^2 + C_A^2)(\omega^2 - C_T^2 k_z^2)}. \quad (5)$$

In each medium separately, the system of Equations (2, 3) can be reduced to the equation

$$(\omega^2 - C_{A\alpha}^2 k_z^2) \left[ \frac{d^2}{dr^2} + \frac{1}{r} \frac{d}{dr} - \left( \kappa_\alpha^2 + \frac{m^2}{r^2} \right) \right] \delta P_{\text{tot}} = 0, \quad (6)$$

where  $\alpha = 0, e$ . The first term of Equation (6) represents torsional Alfvén wave solutions with  $\omega = \pm C_{A\alpha} k_z$ . The second term is a Bessel-like equation that describes magnetoacoustic wave modes. External and internal solutions of this equation have to be matched by the use of jump conditions: the continuity of total pressure and the normal velocity (see, e.g., Roberts, 1981a,b). Furthermore, a condition of mode localisation is applied, requiring that the wave energy should decline with a lateral distance from the structure (tube or slab). In the presence of a steady flow, the condition of continuity of normal velocity is replaced by continuity of the transverse displacement (see, e.g., Nakariakov and Roberts, 1995a). Applying the boundary conditions to the solutions of the Bessel equation leads to the dispersion relation for magnetoacoustic waves in a magnetic flux tube (Edwin and Roberts, 1983; see also Roberts and Nakariakov, 2003 and references therein)

$$\rho_e (\omega^2 - k_z^2 C_{Ae}^2) \kappa_0 \frac{I'_m(\kappa_0 a)}{I_m(\kappa_0 a)} + \rho_0 (k_z^2 C_{A0}^2 - \omega^2) \kappa_e \frac{K'_m(\kappa_e a)}{K_m(\kappa_e a)} = 0. \quad (7)$$

$I_m(x)$  and  $K_m(x)$  are modified Bessel functions of order  $m$ , and the prime denotes the derivative of a function  $I_m(x)$  or  $K_m(x)$  with respect to argument  $x$ . The functions  $\kappa_e$  and  $\kappa_0$  are the transverse wave numbers in the external and internal media, respectively, which are obtained from Equation (5) by the substitution of the appropriate characteristic speeds. For modes that are confined to the tube (evanescent outside, for  $r > a$ ), the condition  $\kappa_e^2 > 0$  has to be fulfilled. In the

equation, it is assumed that  $\kappa_{e,0} > 0$ . The integer  $m$  determines the azimuthal modal structure: waves with  $m = 0$  are called *sausage* modes, waves with  $m = 1$  are *kink* modes, waves with higher  $m$  are sometimes referred to as *flute* or *ballooning* modes. The existence and properties of the modes are determined by the equilibrium physical quantities. In particular, a coronal loop or a filament can trap MHD waves if the external Alfvén speed is greater than internal.

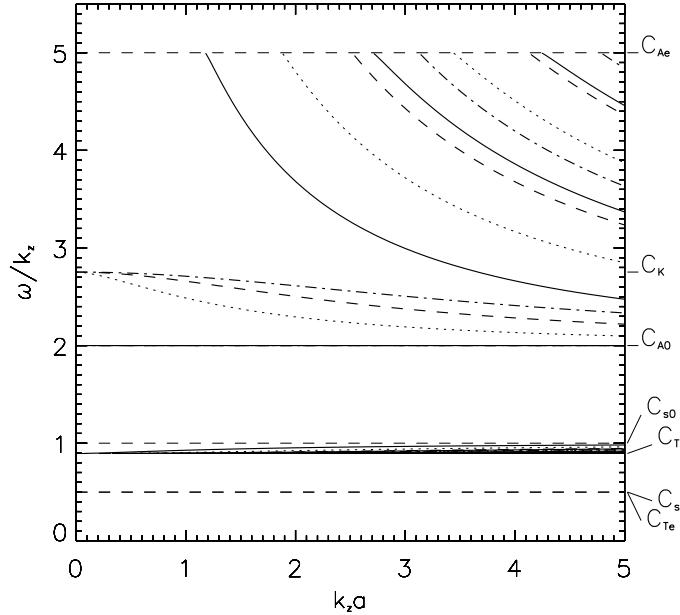


Figure 3: Dispersion diagram showing the real phase speed solutions of dispersion relation (7) for MHD waves in a magnetic cylinder as a function of the dimensionless parameter  $k_z a$ . The typical speeds in the internal and external media are shown relative to the internal sound speed:  $C_{A0} = 2C_{s0}$ ,  $C_{Ae} = 5C_{s0}$ , and  $C_{se} = 0.5C_{s0}$ . The solid, dotted, dashed and dash-dotted curves correspond to solutions with the azimuthal wave number  $m$  equal to 0, 1, 2 and 3, respectively. The torsional Alfvén wave mode solution is shown as a solid line at  $\omega/k_z = C_{A0}$ .

Figure 3 shows a typical dispersion diagram of a coronal loop. This figure generalises the dispersion plot given by [Edwin and Roberts \(1983\)](#) to the inclusion of higher- $m$  modes. In the Figure 3, all the possible modes correspond to *body* modes, which have oscillatory behaviour inside and evanescent behaviour outside. This is in contrast with *surface* modes, which have evanescent behaviour in both media. Phase speeds of MHD modes guided by the tube can have values in two bands: either between  $C_{A0}$  and  $C_{Ae}$  (provided  $C_{A0} < C_{Ae}$ ) and between  $C_{T0}$  and  $C_{s0}$ . The wave modes in these two bands have been named, respectively, *fast* and *slow*, in analogy with the types of magnetoacoustic wave modes present in a homogeneous medium. The fast modes are highly dispersive. In the long wavelength limit, the phase speed of all but sausage fast modes tends to the so-called *kink* speed

$$C_K = \left( \frac{B_0^2/\mu_0 + B_e^2/\mu_0}{\rho_0 + \rho_e} \right)^{1/2} = \left( \frac{\rho_0 C_{A0}^2 + \rho_e C_{Ae}^2}{\rho_0 + \rho_e} \right)^{1/2}, \quad (8)$$

which corresponds to the density weighed average Alfvén speed. The sausage mode approaches a cut-off at the external Alfvén speed. Trapped sausage modes do not exist at longer wavelengths.

But mode solutions can be found if the condition of mode localisation is relaxed, i.e., if waves are allowed to radiate into the external medium. Such wave modes are called leaky modes and have complex eigenfrequencies. To include leaky modes, dispersion relation (7) is modified such that the modified Bessel functions  $K_m(x)$  are replaced by Hankel functions. Details of the leaky solutions may be found in Zaitsev and Stepanov (1975); Cally (1986); Stenuit *et al.* (1998). In Figure 3, leaky waves would be situated outside the regions of existence of the trapped waves. In particular, the sausage mode continues in the region over the horizontal asymptote  $C_{\text{Ae}}$  but its frequency is complex there.

In closed fields of coronal active regions, the longitudinal wave number  $k_z$  of standing modes is usually prescribed by the line-tying boundary conditions at the photosphere. Modes with the lowest wave numbers are called *global* or *fundamental*.

The magnetoacoustic modes (with an important exception) are collectively supported by the plasma environment, i.e., the wave mode acts across neighbouring magnetic field lines and across transverse plasma inhomogeneities. Alfvén waves, though, are locally supported. They have phase and group velocities, with magnitudes equal to the local Alfvén speed, which are directed along the magnetic field. This means that an Alfvén wave propagates along its local magnetic field line without interaction with neighbouring field lines. This particular property allows for the existence of continua of eigenfrequencies and which will be discussed in Section 2.2.

In a cylinder model, Alfvén waves are torsional waves that twist tube. In the case of a straight cylinder these modes are incompressible, however in a slightly twisted cylinder they are accompanied by perturbations of plasma density (Zhugzhda and Nakariakov, 1999). In the slab geometry, torsional waves perturb the magnetic field and generate perturbations of plasma velocity in the direction perpendicular to magnetic field and to the direction of the inhomogeneity. Alfvén waves are very weakly dissipative. This means they can propagate very long distances and deposit energy and momentum far from their source. Concerning the generation of Alfvén waves, they can easily be excited by various dynamical perturbations of magnetic field lines. This makes Alfvén waves a promising tool for heating and diagnostics of coronal magnetic structures.

Movies visualising the structure of the MHD modes in a magnetic cylinder are available in Resource 1. Figure 4 shows the transverse and longitudinal density and velocity structure of a magnetic cylinder perturbed by a fundamental fast kink oscillation.

## 2.2 MHD continua

When the group speed of wave modes is directed along the magnetic field, then such modes on neighbouring field lines do not interact with each other. They may oscillate locally with their own eigenfrequency without disturbing the rest of the medium. If the equilibrium parameters of the plasma vary continuously across the magnetic field, then the eigenfrequency of such modes may also vary continuously. This gives rise to continuous intervals of eigenfrequencies, i.e., continua, in frequency space. This situation, though, may change by including resistivity or non-MHD effects (see, e.g., Appert *et al.*, 1986).

In ideal MHD, there exist two continua: the Alfvén continuum and the slow (or cusp) continuum (see Goedbloed, 1983; Goedbloed and Poedts, 2004). Equations (2, 3) are also valid for linear waves in a coronal loop modelled as a plasma cylinder if the equilibrium quantities vary continuously in the radial direction (see, e.g., Sakurai *et al.*, 1991a). The continua are in this case characterised by the frequencies  $C_A(r)|k_z|$  and  $C_T(r)|k_z|$ . There are two effects associated with wave modes from these continua: resonant absorption and phase-mixing.

### 2.2.1 Resonant absorption

If the loop supports a collective (a mode) wave, either driven externally or set up initially, which has a frequency  $\omega$  that falls within one of the two continua, a resonance is set up at the location(s)

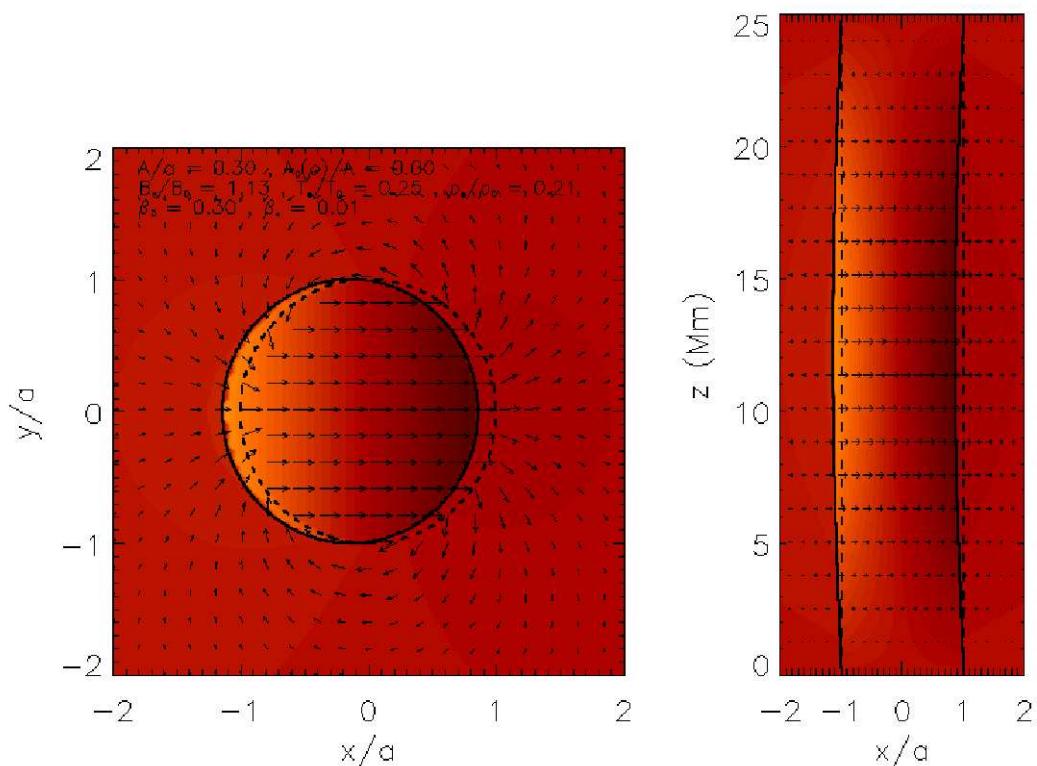


Figure 4: Transverse and longitudinal density perturbation (shown as intensity) and velocity structure (shown as a vector field) of a homogeneous magnetic cylinder model of a coronal loop, perturbed by a fundamental fast kink oscillation (from Resource 1).

where  $\omega^2 = C_A^2(r)k_z^2$  or  $\omega^2 = C_T^2(r)k_z^2$  (where Equation (4) becomes zero). The physical location where the resonance occurs is called the resonance layer and in the plasma cylinder model it corresponds to a radial shell (see Figure 5). From now on we shall consider the case of a resonance in the Alfvén continuum only. The locally excited resonant wave mode is a torsional Alfvén wave and its amplitude peaks in the resonance layer where the perturbation develops large gradients. Dissipation has to be taken into account to prevent the perturbation to diverge. The amplitude of the resonant mode scales as  $Re^{1/3}$  at the resonant layer, where  $Re$  is the shear viscous and/or the magnetic Reynolds number (Kappraff and Tataronis, 1977). In the solar corona this number is much larger than unity ( $Re \sim 10^{14}$ ). Since non-resonant modes dissipate with an amplitude proportional to  $Re$ , it is clear that the resonantly excited modes experience enhanced dissipation. This also implies that the resonant absorption process is inherently nonlinear, since the amplitude of the resonant mode can not grow to the values implied by the  $Re^{1/3}$  scaling (Ofman *et al.*, 1994; Ofman and Davila, 1995). Thus, wave energy is extracted secularly through the resonance from the collective wave to the benefit of a local wave mode (mode conversion), which then is dissipated in an enhanced manner. This mechanism of wave heating is called *resonant absorption* (Goedbloed, 1983, and references therein) and has been put forward in the context of the coronal heating problem (Ionson, 1978) and in sunspot seismology for explaining the loss of acoustic power in sunspots (see, e.g., Sakurai *et al.*, 1991b; Bogdan, 2000, and references therein).

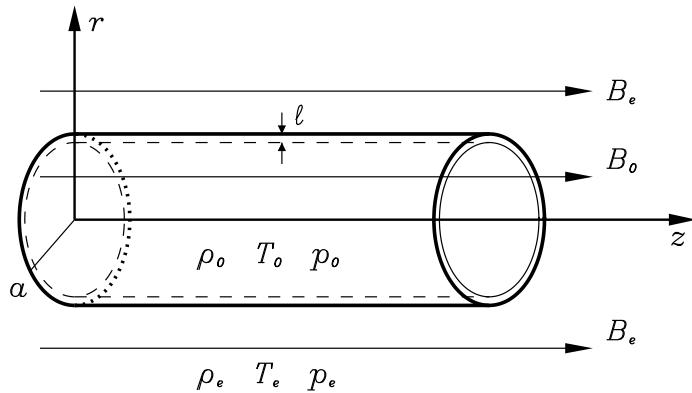


Figure 5: A magnetic flux tube of radius  $a$  embedded in a magnetised plasma with a thin edge layer of width  $\ell$  where the density varies monotonically.

There are inherently two time scales involved. Firstly, there is the damping time scale of the mode conversion from the collective to the local mode, which generally is independent of dissipation. From the point of view of linear theory and classical, theoretical values of dissipation coefficients, it is generally much shorter than the second time scale, which is linked to the dissipative damping of the small-scale perturbations of the local mode in the resonance layer.

Note that for sausage wave modes, where  $m=0$ , the equations describing the magnetoacoustic and torsional waves (i.e., Equations (2, 3)) are decoupled so that mode conversion and absorption through the Alfvén resonance cannot take place (the slow resonance can still operate; see, e.g., Erdélyi, 1997). For the slab geometry, this corresponds to propagation parallel to the magnetic field, i.e.,  $k_y = 0$ .

To study resonant absorption the following procedure is often undertaken. Whilst outside of the resonant layer the ideal MHD equations can be applied, inside the resonant layer dissipative

effects have, in principle, to be taken into account to ensure that the solution remains regular. But unless one is interested in the details of the solution in the resonant layer, this can be avoided. The thickness of the resonant layer,  $\delta$ , is proportional to  $(\ell L^2 \text{Re})^{-1/3}$ , where  $\ell$  is the length scale over which the Alfvén speed varies around the resonance. In the solar atmospheric context  $\delta$  can be assumed to be small. The solution in the resonant layer is replaced by a jump relation, which is based upon a Taylor series expansion of the ideal MHD equations around the resonance (Kapraff and Tataronis, 1977; Ionson, 1978; Hollweg, 1987; Hollweg and Yang, 1988; Sakurai *et al.*, 1991a). It is assumed that the quantities that are conserved across the layer in ideal MHD will remain so in weakly dissipative MHD.

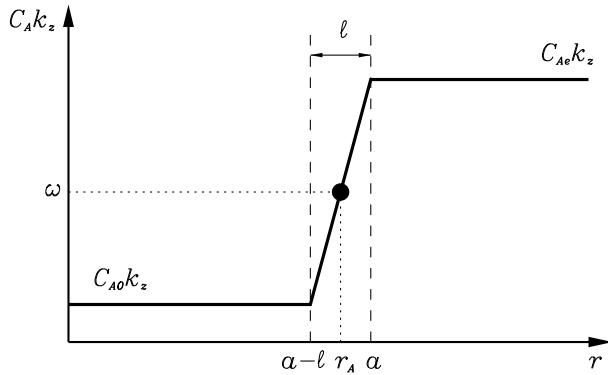


Figure 6: Radial profile of the Alfvén frequency in a loop with a thin edge layer of width  $\ell$  where the density varies monotonically. A resonance occurs where the global wave mode frequency  $\omega$  matches locally the Alfvén frequency  $C_A(r_A)k_z$  inside the edge layer.

Consider a loop model where the internal and external media are homogeneous, except for a loop edge layer of width  $\ell$  where the density varies monotonically from  $\rho_0$  to  $\rho_e$  (see Figure 5). A global wave mode is present, which has a frequency  $\omega$  which matches the Alfvén frequency at  $C_A(r = r_A)|k_z|$  within the Alfvén continuum of the edge layer (see Figure 6). In the internal and external media the solutions are calculated using, e.g., Equation (6). Those solutions contain arbitrary integration constants, which are related to each other with use of certain jump relations at the edge layer. The width of the edge layer,  $\ell$ , is considered to be thin, i.e.,  $\ell \ll a$ , but wider than the resonant layer, i.e.,  $\delta > \ell$ . The jump relations are constructed as follows. Inside the edge layer, the system of Equations (2) is Taylor expanded around the resonance using the small parameter  $s \equiv r - r_A$  ( $|s| \ll 1$ ). Thus, a second order differential equation for  $\delta P_{\text{tot}}/s$  is derived, which is of the form

$$\left[ \frac{d^2}{ds^2} + \frac{1}{s} \frac{d}{ds} - \left( \frac{1}{s^2} + \frac{m^2}{r_A^2} \right) \right] \left( \frac{\delta P_{\text{tot}}}{s} \right) = 0. \quad (9)$$

It has solutions in the form of modified Bessel functions. The total pressure perturbation is described as

$$\delta P_{\text{tot}} = a s I_1 \left( \frac{|m|s}{r_A} \right) + b s K_1 \left( \frac{|m|s}{r_A} \right) \approx b \frac{r_A}{|m|}, \quad (10)$$

which is approximately constant across the layer (Hollweg, 1987; Sakurai *et al.*, 1991a). Since for  $m=0$  no resonant coupling can occur, the Equation (10) does not apply for that case. Therefore, the jump relation for the total pressure perturbation is simply  $[\delta P_{\text{tot}}] = 0$ , where the square brackets denote the difference between the solutions in the right and left limits of  $s$  tending to

zero, respectively. Note that, when the loop is twisted, the total pressure is no longer a conserved quantity (Sakurai *et al.*, 1991a). Similarly, the solution for the radial displacement perturbation can be found to be approximately

$$\xi_r \approx b \frac{|m|}{r_A} \frac{1}{\rho_0(r_A)\Delta} \ln\left(\frac{|m|s}{2r_A}\right) + \text{constant}, \quad (11)$$

where  $\Delta = d(\omega^2 - C_A^2 k_z^2)/dr|_{r=r_A}$ .  $\xi_r$  depends on  $s$  through a logarithmic term, which diverges for  $s$  tending to zero. The jump relation for  $\xi_r$  is

$$[\xi_r] = -i\pi \frac{m^2}{r_A^2} \frac{\text{sign}\omega}{\rho_0(r_A)|\Delta|} \delta P_{\text{tot}}(r_A), \quad (12)$$

for which the relation  $[\ln(s)] = -i\pi \text{sign}(\omega) \text{sign}(\Delta)$  has been used. To match the internal and external solutions, the usual jump conditions of continuity of total pressure and radial displacement are now replaced by the above derived jump relations. Depending on the condition that is imposed at  $r \rightarrow \infty$ , the trapped and/or leaky eigenmodes of the system may be studied (involving a dispersion relation) or the reflection/absorption problem of an externally driven wave that interacts with the loop.

By scanning through the frequency of the collective wave, the wave absorption as a function of  $\omega$  is studied (see, e.g., the numerical simulations by Poedts *et al.*, 1989). The fractional absorption spectrum often shows well-defined maxima where the absorption reaches 100%. The spatial structure of the excited wave mode at those maxima shows a combination of localised and global behaviour. It is a global wave (e.g., discrete fast eigenmode) with a frequency that lies in the Alfvén continuum and is, therefore, locally coupled to an Alfvén wave. These types of wave modes are known as *quasi-modes* and they are natural wave modes of the dissipative and inhomogeneous system (Balet *et al.*, 1982; Steinolfson and Davila, 1993; Ofman *et al.*, 1994; Ofman and Davila, 1995; Tirry and Goossens, 1996). Therefore, it is easily understood why maximum absorption occurs when driving at the frequency of a quasi-mode. Also, the presence of steady flows can significantly change the efficiency of resonant absorption (Erdélyi, 1998).

Furthermore, in the absence of flow, these modes are damped (Poedts *et al.*, 1990; Ofman *et al.*, 1994; Wright and Rickard, 1995). From the point of view of the global nature of the mode, the damping is primarily a conversion of energy from the collective to the local. This damping rate has been calculated for various geometries (see, e.g., Lee and Roberts, 1986; Hollweg, 1987; Goossens *et al.*, 1992). Ruderman and Roberts (2002) calculated the damping time,  $\tau$ , of a global kink wave in a long, thin loop ( $a \ll L$ ) in the limits of weak dissipation ( $\text{Re} \gg 1$ ) and zero plasma- $\beta$ :

$$\tau = \frac{2a|\Delta|(\rho_0 + \rho_e)^3}{\pi\rho(r_A)|C_K k_z|^3(\rho_0 - \rho_e)^2}. \quad (13)$$

This time scale is generally much shorter than the time scale of the dissipative damping of the small-scale perturbations of the local mode in the resonance layer. In Section 3.4 this aspect of rapid mode conversion will be explored further within the context of the observed rapid damping of transverse loop oscillations (Roberts, 2000; Ruderman and Roberts, 2002; Goossens *et al.*, 2002a; Van Doorsselaere *et al.*, 2004).

Ofman *et al.* (1994) and Ofman and Davila (1995) studied numerically nonlinear resonant absorption and found that the large shear velocities produced at the resonance layer are subject to Kelvin–Helmholtz instabilities. The velocity amplitudes derived from linear theory are much larger than the observed velocities from nonthermal broadening of coronal emission lines. This discrepancy may be explained by a turbulent enhancement of dissipation parameters due to the instabilities. Additional complexity is brought by the effects of boundary conditions in the longitudinal direction, e.g., Beliën *et al.* (1999) examined numerically the effect of the transition region and

chromosphere on the resonant absorption in coronal loops. They found that the nonlinear energy transfer from the Alfvén waves to slow magnetoacoustic waves in the lower atmosphere can much diminish the absorption efficiency compared with models of line-tied loops without a lower atmosphere. The driver they considered was, though, monoperiodic and this study should be extended to include more realistic drivers. Furthermore, the heating of the resonance layer would spread due to thermal conduction and heat the lower atmosphere. The resulting chromospheric evaporation enhances the loop density at the resonance layer and, hence, shifts the Alfvén frequency away from resonance, as well as change the quasi-mode frequencies (see, e.g., the discussion in Ofman and Davila, 1995). Ofman *et al.* (1998a) considered a broad band Alfvén wave driver (see also DeGroof and Goossens, 2002), and coupling to the chromosphere of the loop density with the use of a quasi-static equilibrium scaling law. They found that the heating is concentrated in multiple resonance layers, rather than in the single layer of previous models, and that these layers drift throughout the loop to heat the entire volume. These properties are in much better agreement with coronal observations that imply multithreaded loop structure.

### 2.2.2 Alfvén wave phase mixing

Consider again a structure with a continuous inhomogeneity profile across the magnetic field. Instead of an initial collective mode, this time on each field line an Alfvén wave is excited. This wave oscillates independently from its neighbours, with a frequency that lies in the Alfvén continuum. For simplicity a Cartesian geometry is chosen where the magnetic field is in the  $z$ -direction and the inhomogeneity is in the  $x$ -direction. The Alfvén waves, which are polarised in the  $y$ -direction, are described by the wave equation (Heyvaerts and Priest, 1983)

$$\left( \frac{\partial^2}{\partial t^2} - C_A^2(x) \frac{\partial^2}{\partial z^2} \right) V_y = 0, \quad (14)$$

with the solution

$$V_y = \Psi(x) f(z \mp C_A(x)t), \quad (15)$$

where  $f(z)$  and  $\Psi(x)$  are functions prescribed by the initial profile of the wave. The sign in the argument of this function corresponds to a wave propagating in the positive or negative direction of the  $z$ -axis, respectively. When  $\Psi(x) = \text{const}$ , the wave is plane.

Equation (15) shows that the Alfvén waves propagate on different magnetic surfaces, corresponding to different values of  $x$ , with different phase speeds equal to the local Alfvén speed  $C_A(x)$ . If the wave is initially plane in the  $x$  direction, it gets gradually inclined. This leads to generation of very small transverse (in the direction of the inhomogeneity) spatial scales. These high transverse gradients, in the presence of finite viscosity or resistivity, which leads to the appearance of a  $\nu \partial/\partial t \nabla^2 V_y$  term on the right hand side of Equation (14), are subject to efficient dissipation. Here,  $\nu$  is the coefficient of viscosity and/or resistivity, small enough so that dissipation may be considered weak. This is the effect of Alfvén wave phase mixing, suggested by Heyvaerts and Priest (1983) as a possible mechanism for heating of open coronal structures.

In the developed stage of phase mixing (when  $\partial/\partial x \gg \partial/\partial z$ ) the Alfvénic perturbations of different magnetic surfaces become uncorrelated with each other, the perturbations decay according to the law (Heyvaerts and Priest, 1983)

$$V_y(z) \propto V_y(0) \exp \left\{ -\frac{\nu k_z^2}{6C_A^3(x)} \left[ \frac{dC_A(x)}{dx} \right]^2 z^3 \right\}, \quad (16)$$

for propagating harmonic Alfvén waves, and

$$V_y(t) \propto V_y(0) \exp \left\{ -\frac{\nu k_z^2}{6} \left[ \frac{dC_A(x)}{dx} \right]^2 t^3 \right\}, \quad (17)$$

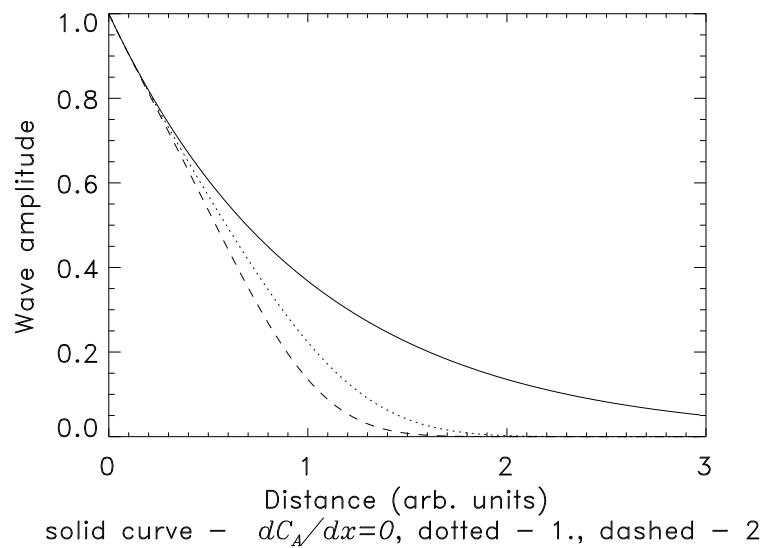


Figure 7: Comparison of the dissipative decay of Alfvén waves in 1D plasma inhomogeneities with Alfvén speed profiles of different steepness. The solid curve shows the dissipative decay of Alfvén waves in an homogeneous plasma. Phase-mixing is therefore absent and the damping time is proportional to  $\text{Re}$ . The other curves show the dissipative decay in a 1D plasma inhomogeneity with a nonzero gradient in the Alfvén speed. Phase-mixing, therefore, occurs and the damping times are proportional to  $\text{Re}^{1/3}$ .

for standing harmonic Alfvén waves. The decay time due to phase-mixing is proportional to  $\text{Re}^{1/3}$ , similar to the dissipative decay of Alfvén waves due to resonant absorption. Figure 7 shows the dissipative decay of propagating Alfvén waves in a 1D plasma inhomogeneity with Alfvén speed profiles of different steepness, compared with the dissipative decay of Alfvén waves in a homogeneous medium (solid curve).

If instead of a monochromatic wave in the longitudinal direction a *localised* Alfvén pulse is considered, Heyvaerts and Priest's expression for the exponential decay (17) should be replaced by the power law

$$V_y \propto \left[ \nu \left( \frac{dC_A(x)}{dx} \right)^2 t^3 \right]^{-1/2}; \quad (18)$$

see Hood *et al.* (2002) and Tsiklauri *et al.* (2003) for two methods of derivation and comparison with results of numerical modelling.

In the nonlinear regime, growing transverse gradients induce oblique fast magnetoacoustic waves (Nakariakov *et al.*, 1997). Consequently, phase mixing regions may be characterised by the presence of compressible perturbations.

### 2.3 Zero plasma- $\beta$ density profiles

The limiting case of zero plasma- $\beta$  (where  $\beta$  is the ratio of the gas pressure to the magnetic pressure), when the plasma pressure force is neglected in comparison with the Lorentz force, and there is a one-dimensional profile of the plasma density, embedded in the constant and parallel magnetic field, the eigenvalue problem is similar to the quantum mechanical problem of the interaction of a particle with a nonuniform potential. In this section we restrict our attention to the Cartesian geometry only. The governing equations, in this case, allow for exact analytical solutions. We consider wave propagation along the magnetic field (i.e.,  $k_y = 0$ ) to avoid the Alfvén resonance. Nakariakov and Roberts (1995b) established that the qualitative dispersive properties depend weakly upon the specific profile of the density. Consider a coronal loop as a magnetic slab with a *smooth* density profile, given by the profile function

$$\rho_0 = \rho_{\max} \operatorname{sech}^2 \left( \frac{x}{a} \right) + \rho_{\infty}, \quad (19)$$

where  $\rho_{\max}$ ,  $\rho_{\infty}$  and  $a$  are constant. Here, the parameter  $\rho_{\max}$  is the density at the centre of the inhomogeneity,  $\rho_{\infty}$  is the density at  $x = \infty$  and  $a$  is a parameter governing the inhomogeneity width. This inhomogeneity, plotted in Figure 8, is called the *symmetric Epstein profile* (see, e.g., Nakariakov and Roberts, 1995b). With an inhomogeneity of this form exact analytical solutions can be obtained. The plasma is inhomogeneous across the straight and uniform magnetic field  $\mathbf{B}_0 = B_0 \hat{\mathbf{z}}$ . In the zero plasma- $\beta$  limit considered, the equilibrium total pressure balance is identically fulfilled.

According to Nakariakov and Roberts (1995b), linear perturbations of the transverse plasma velocity  $V_x = U(x) \exp(i\omega t - ik_z z)$  are described by the equation

$$\frac{d^2U}{dx^2} + \left[ \frac{\omega^2}{C_{A\infty}^2} - k_z^2 + \frac{\omega^2}{C_{Ad}^2} \operatorname{sech}^2 \left( \frac{x}{a} \right) \right] U = 0, \quad (20)$$

where  $C_{A\infty}$  is the Alfvén speed as  $x \rightarrow \infty$  and  $C_{Ad}$  is the Alfvén speed based upon the excess density at  $x = 0$ , i.e.,  $C_{Ad} = B_0 / (\mu_0 \rho_{\max})^{1/2}$ . As the corresponding profile of the Alfvén speed has a minimum at the centre of the slab, the slab is a *refractive waveguide* for fast magnetoacoustic waves (see Edwin and Roberts, 1988, for discussion).

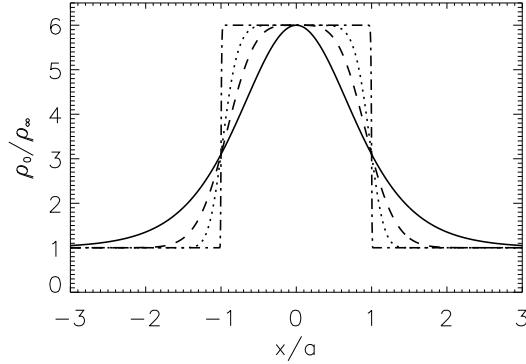


Figure 8: Symmetric Epstein density profiles of the form  $\rho_0 = \rho_{\max} \operatorname{sech}^2 [(x/a)^p] + \rho_\infty$  with the solid, dashed, dotted and dash-dotted curves corresponding to values of  $p = 1$ ,  $p = 2$ ,  $p = 4$ , and  $p = 100$  (effectively  $p \rightarrow \infty$ ). The case of  $p = 0$  corresponds to Equation (19).

The eigenvalue problem stated by Equation (20) supplemented by the boundary conditions  $U(x \rightarrow \pm\infty) \rightarrow 0$  can be solved analytically (Nakariakov and Roberts, 1995b; Cooper *et al.*, 2003). The eigenfunctions describing kink and sausage modes are respectively given by

$$U = \begin{cases} A \operatorname{sech}^\alpha \left( \frac{x}{a} \right) & \text{kink mode} \\ A \tanh \left( \frac{x}{a} \right) \operatorname{sech}^\alpha \left( \frac{x}{a} \right) & \text{sausage mode} \end{cases}, \quad (21)$$

where  $A$  is the amplitude. Here  $\alpha$  is given by

$$\alpha = \frac{|k_z|a}{C_{A\infty}} \sqrt{C_{A\infty}^2 - V_{ph}^2}, \quad (22)$$

with  $V_{ph} = \omega/k_z$  being the phase speed, which is determined by the dispersion relations

$$\sqrt{C_{A\infty}^2 - V_{ph}^2} = |k_z|a \frac{C_{A\infty}}{C_{A0}} (V_{ph}^2 - C_{A0}^2) \quad (23)$$

and

$$\frac{|k_z|a}{C_{A0}^2} (V_{ph}^2 - C_{A0}^2) - \frac{2}{|k_z|a} = \frac{3}{C_{A\infty}} \sqrt{C_{A\infty}^2 - V_{ph}^2}, \quad (24)$$

where  $C_{A0} = C_{A\infty} C_{Ad} / (C_{A\infty}^2 + C_{Ad}^2)^{1/2}$  is the Alfvén velocity at the centre of the profile,  $x = 0$ .

Dispersion relations (23) and (24) and solutions (21) are a convenient tool for the study of the effect of the transverse profile on wave properties. In particular, Figure 9 demonstrates that the sausage mode group speed is affected by the steepness of the profile quite significantly. One of the observational manifestations of this effect is the shape of the fast wave trains formed by the dispersive evolution of initially broad band perturbations. Applications of this theory are discussed in Section 7.

## 2.4 Effects of twisting

It is clear that twisting of the magnetic field in the cylinder will lead to linear coupling of various MHD modes. However, modification of dispersion relation (7) by the twisting is not well understood.

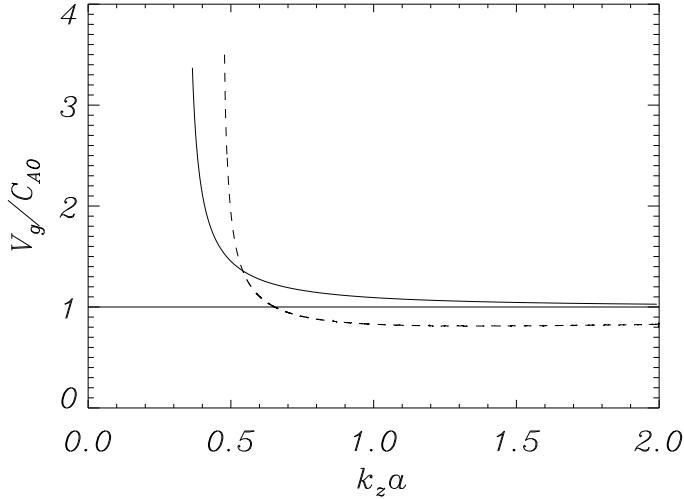


Figure 9: Comparison of group speeds of a propagating sausage mode guided by a 1D plasma inhomogeneity with the Alfvén speed contrast ratio of 4, with the step function profile (the dashed line), and with the symmetric Epstein profile (the solid line). The group speed is normalised to the minimum value of the Alfvén speed, which is equal to the Alfvén speed inside the slab with the step function profile, represented by the horizontal solid line.

Considering the thin flux tube limit, Zhugzhda and Nakariakov (1999) showed that long-wavelength ( $k_z a \ll 1$ ) torsional perturbations of a weakly twisted cylinder are described by the dispersion relation

$$\omega^2 \approx C_A^2 \left( 1 + \frac{K\beta}{2} \right) k_z^2 \left( 1 + \frac{a^2 K^2 \beta^2 (1 - \beta)}{16} k_z^2 \right), \quad (25)$$

where  $K = \alpha^2 a^2 / 8$  is the twist parameter (here  $K \ll 1$ ), with  $\alpha = 2J_0/B_0$  ( $J_0$  is the current density) being the parameter of force-free magnetic fields and  $a$  being the radius of the cylinder. The parameter  $\alpha = 2J_0/B_0$ , where  $J_0$  is the current density. The twist results into the appearance of dispersion and modifies the phase speed of the mode. Actually, the considered mode cannot be referred to as a pure torsional mode as it perturbs the plasma density and its phase speed depends upon the plasma- $\beta$ . The compressibility of the torsional wave in a twisted cylinder may be demonstrated as follows. According to Zhugzhda (1996), the torsional components of the velocity,  $V_\phi$ , and the magnetic field,  $B_\phi$ , are connected with the longitudinal components of the magnetic field  $B_z$  and the velocity  $V_z$  by the equation

$$\frac{\partial}{\partial t} \left( \frac{B_\phi}{B_z} \right) + \frac{\partial}{\partial z} \left( V_z \frac{B_\phi}{B_z} \right) = \frac{\partial V_\phi}{\partial z}. \quad (26)$$

If the equilibrium value of the twist  $B_{\phi 0} r$  is non-zero, the torsional motions generate longitudinal flows and, consequently the density perturbations.

Bennett *et al.* (1999) considered the collective MHD modes of a straight uniformly twisted magnetic cylinder in the *incompressible* limit, and concluded that the twist leads to the appearance of body modes with phase speeds about the “longitudinal” Alfvén speed (calculated with the use of the longitudinal component of the field only). As well as in the untwisted case, there is a surface mode with the phase speed about the kink speed.

An alternative approach to the modelling of twisted and curved coronal loops was suggested by Cargill *et al.* (1994), which allowed the authors to take into account the hoop force – the feature missing from the straight cylinder model. The force is connected with both the loop twist *and* the curvature. The presence of the new restoring force was shown to give rise to a new oscillation mode manifested as the periodic change of the loop major radius and the loop density, whose frequency could be independent of the loop length. Oscillations of the loop minor radius were also found. The oscillation frequencies obtained were significantly different from the frequencies of straight cylinder eigenmodes. This approach certainly requires attention and further development.

Also, oscillations of current carrying loops can be described in terms of the LCR-model, see Section 3.5.

### 3 Kink Oscillations of Coronal Loops

#### 3.1 TRACE observations

On 14 July 1998, the imaging telescope on board the Transition Region and Coronal Explorer (TRACE) registered, in both 171 Å and 195 Å lines, spatially resolved decaying oscillating displacements of coronal loops in the active region AR 8270 (Aschwanden *et al.*, 1999; Nakariakov *et al.*, 1999; Schrijver *et al.*, 1999). These oscillations happened shortly after a solar flare and, most probably, were generated by the flare. The mechanism of the excitation remains hidden, but it can be connected with a blast wave generated in the flare epicentre. Some of the loops seem to be more responsive to the oscillation than others and it could probably be connected with the magnetic topology of the active regions (Schrijver and Brown, 2000). Oscillations of different loops were not synchronised in phase. The highest amplitude was seen near the loop apices.

Since this discovery, the loop oscillations were subject to an extensive observational study and the results are summarised in Schrijver *et al.* (2002) and Aschwanden *et al.* (2002). In particular, it was found that the kink oscillations do not always have a simple form of a global (or principle) mode and there can be higher spatial harmonics observed.

Anyway, the oscillation examined by Nakariakov *et al.* (1999) may be considered as a typical example of kink oscillations of coronal loops. The analysis of the loop displacement shows that the oscillation is almost harmonic with the period of about  $P = 256$  s (the frequency about 4 mHz). Figure 10 shows the temporal evolution of the displacement at the loop apex. About three periods of oscillation were observed. Displacement amplitudes are several Mm for the distance between the loop footpoints estimated to be about  $2L/\pi = 83$  Mm. The displacement amplitude is several times larger than the loop cross-section radius, which was observed to be about  $2a = 1$  Mm. The oscillation shows evidence of strong damping. Simultaneously, similar quasi-periodic oscillations were observed in several other loops at the distance of several Mm to 60–70 Mm from the flare epicentre (Aschwanden *et al.*, 1999). All these observational findings suggested the oscillations, at least observed in this event, to be interpreted as a *kink global standing mode* of the loop.

Taking the observed period  $P$  and loop length  $L$ , and applying that the wavelength of a global standing mode is double the length of the loop, one can estimate the phase speed required as

$$\frac{\omega}{k} = \frac{2L}{P} \approx 1020 \pm 132 \text{ km s}^{-1}. \quad (27)$$

According to the theory of MHD modes of a magnetic cylinder, discussed in Section 2, the fast kink magnetoacoustic modes of a magnetic cylinder do not have dispersive cut-offs and exist for all wavenumbers. In all cases, the wavelength of the observed kink oscillations is much longer than the loop cross-section diameter (e.g., the width of the oscillating loop observed on 14 July 1998 is about 1 Mm, while the loop length may be estimated as 261 Mm for the distance between the footpoints of about 83 Mm; Nakariakov and Ofman, 2001). In this limit, the phase speed of fast kink modes waves approaches the *kink speed*  $C_K$  given by Equation (8).

Terradas and Ofman (2004) pointed out intensity variations localised at the tops of some large-amplitude oscillating loops observed with TRACE in the flaring event on 14 July 1998. As no noticeable changes of the plasma temperature were found at those regions, the intensity variations were interpreted as density variations, approximately in the range 14%–52%. The amplitude could possibly be even higher if the filling factor was less than 1. In the analysed loop, the projected maximum amplitude of the oscillations was about 90 km s<sup>-1</sup>. In the loops oscillating with smaller amplitudes this effect is not detected, indicating its nonlinear nature.

The majority of kink oscillation events corresponds to the horizontal perturbations of coronal loops, which do not change the length of the loop. Recently, Wang and Solanki (2004) found an example of vertically polarised kink oscillations in TRACE 195 Å data. The oscillation period was 3.9 min, the displacement amplitude was about 8 Mm and the decay time was 11.9 min. The

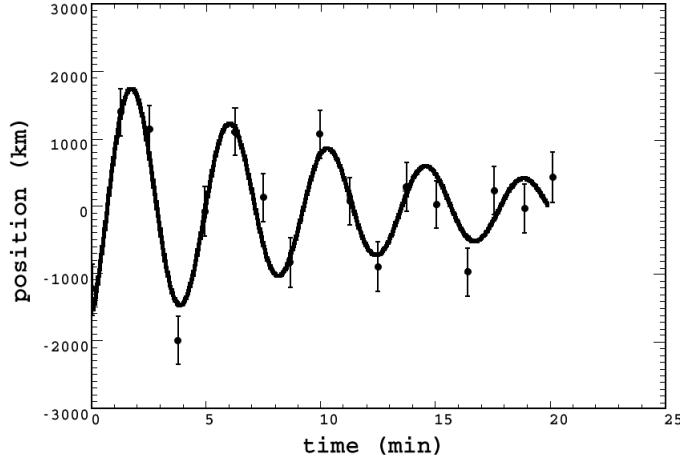


Figure 10: The temporal evolution of the loop displacement as an average coordinate of the loop position for four neighbouring, perpendicular cuts through the loop apex (diamonds), with error bars ( $\pm 0.5$  pixels), starting at 13:13:51 UT on 14 July 1998. The solid curve is a best fit of the function  $A \sin(\omega t + \phi) \exp(-\lambda t)$  with  $A = 2030 \pm 580$  km,  $\omega = 1.47 \pm 0.05$  rad min $^{-1}$ , and  $\lambda = 0.069 \pm 0.013$  min $^{-1}$ , corresponding to a period and e-folding decay time of  $P = 4.3 \pm 0.9$  min and  $\tau = 14.5 \pm 2.7$  min, respectively (from Nakariakov *et al.*, 1999).

main difference of this polarisation from the horizontal one is that in the curved loop the vertically polarised kink mode changes the length of the loop. Consequently, as the mass in the loop should be conserved, this mode can have a significant compressible component. The fractional intensity perturbations associated with this mode were estimated as

$$\frac{\Delta I}{I} \propto \frac{2\Delta\rho}{\rho} \propto \frac{2\Delta L}{L}, \quad (28)$$

where  $\Delta\rho$  is the density perturbation and  $\Delta L$  is the perturbation of the loop length. Here it is assumed that the oscillation does not deform the loop cross-section, i.e.,  $\Delta a/a \ll \Delta L/L$ . An alternative is associated with bulk field-aligned flows through the loop footpoints, which do not have observational confirmation.

Another possible polarisation of kink oscillations is when the loop moves in the same plane and its apex displaces horizontally. This mode has not been identified yet.

### 3.2 Non-TRACE observations

Kink modes of coronal loops – often erroneously called Alfvén waves (erroneously, because the true Alfvén waves guided by coronal loops are the torsional modes, see Section 8) – can also be observed through modulation of the broadband gyrosynchrotron emission by the periodic variation of the local magnetic field in flaring loops and through periodic variations of the Doppler shift.

The optically thin gyrosynchrotron emission intensity  $I_f$  at a frequency  $f$  can be estimated with the use of (Dulk and Marsh, 1982)'s approximated formula

$$I_f \approx 3.3 \times 10^{-24} \frac{BN}{2\pi} \times 10^{-0.52\delta} (\sin \theta)^{-0.43+0.65\delta} \left( \frac{f}{f_B} \right)^{1.22-0.90\delta}, \quad (29)$$

where  $N$  is the concentration of the nonthermal electrons with energies higher than 10 keV,  $\theta$  is the angle between the magnetic field and the line-of-sight,  $f_B$  is the gyrofrequency and  $\delta$  (usually  $> 3 - 5$ ) is the power law spectral index of the electrons. Transverse oscillations are accompanied by the changes of the angle  $\theta$  and, consequently, modulate the gyrosynchrotron emission coming from the loop. This mechanism can be responsible for quasi-periodic pulsations with periods from several s to several min, abundantly present in the microwave emission coming from flaring loops.

However, confident identification of the kink mode requires observations with high spatial resolution. The pixel size should be smaller than the wave length of the mode. The first spatially resolved detection of microwave quasi-periodic pulsations, which could be associated with the fast kink mode, was performed by Asai *et al.* (2001) with the Nobeyama Radioheliograph (see Figure 11). The oscillation period was 6.6 s. They determined the number density in the loop to be  $4.5 \times 10^{16} \text{ m}^{-3}$  from filter ratios of soft X-ray images taken by SXT. The loop length was 16 Mm. The microwave pulsations had a less weaker modulated counterpart in hard X-ray emission observed by the HXT on Yohkoh. The modulation of the hard X-ray emission by the kink wave can be connected with modulation of the electron acceleration by the kink oscillation of the flaring loop, or with interaction of the flaring loop with another loop which performs kink oscillations. In both cases the reconnecting magnetic field is periodically fed to the reconnection site by the kink oscillation. As the thickness of the reconnection site is believed to be very small, even weak kink oscillations can produce the required modulation.

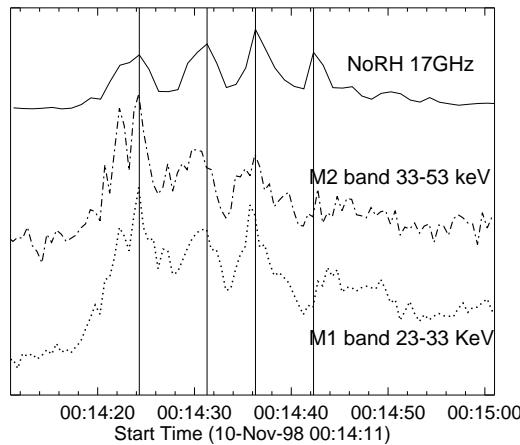


Figure 11: Light curves of the second burst (scaled arbitrarily). From top to bottom: Radio brightness temperature observed at 17 GHz by NoRH (solid line) and hard X-ray count rate measured in the M2 band (3353 keV; dash-dotted line) and M1 band (2333 keV; dotted line) of Yohkoh/HXT. The vertical lines show the peak times of the microwave emission (from Asai *et al.*, 2001).

When the line of sight has a significant component parallel to the plane of the oscillations, the kink mode can be detected with spectral instruments through the periodically modulated Doppler shift. For example, 300 s, 80 s, and 43 s periodicities were found by Koutchmy *et al.* (1983) in the Doppler shift of the green coronal line. In this event, no prominent intensity variations were observed. These oscillations were interpreted as standing kink waves by Roberts *et al.* (1984).

### 3.3 Determination of coronal magnetic fields

In the low plasma- $\beta$  limit, the expression for the kink speed (8) reduces to

$$C_K \approx \left( \frac{2}{1 + \rho_e/\rho_0} \right)^{1/2} C_{A0}, \quad (30)$$

and contains two unknown parameters, the Alfvén speed  $C_{A0}$  and the density ratio  $\rho_e/\rho_0$ . By observationally measuring  $C_K$  and considering the density ratio as a parameter, the Alfvén speed in the loop can be determined. Assuming a density ratio  $\rho_e/\rho_0 = 0.1$ , we obtain  $C_A = 756 \pm 100 \text{ km s}^{-1}$  for the kink speed of  $1020 \pm 132 \text{ km s}^{-1}$ , for the event on the 14 July 1998 (see Nakariakov and Ofman, 2001, for more details).

The Alfvén speed is defined by the magnetic field strength and the density of the medium. Consequently, by using Equation (30), we can estimate the value of the magnetic field in the loop:

$$B_0 = \sqrt{\mu_0 \rho_0} C_{A0} \approx \frac{\sqrt{2\mu_0 L}}{P} \sqrt{\rho_0(1 + \rho_e/\rho_0)}, \quad (31)$$

(there is a typo in Equation (6) of Nakariakov and Ofman (2001), corrected, e.g., in Roberts and Nakariakov (2003)).

A practical formula for the magnetic field determination by the observables is

$$B_0 \approx 1.02 \times 10^{-12} \frac{d \sqrt{\mu n_0} \sqrt{1 + n_e/n_0}}{P}, \quad (32)$$

where the magnetic field  $B_0$  is in G, the distance between the footpoints  $d$  is in m, the number density in the loop  $n_0$  is in  $\text{m}^{-3}$ , and the oscillation period  $P$  is in s;  $\mu$  is the effective particle mass with respect to the proton mass. In the solar corona, because of the presence of heavier elements,  $\mu = 1.27$ . Applying this formula, Nakariakov and Ofman (2001) estimated the magnetic field in an oscillating loop observed on the 14 July 1998, as  $13 \pm 9$  G (see Figure 12, where the number density is measured in  $\text{cm}^{-3}$ ). This error bar can be significantly reduced by improving the determination of the density in the loop and by better statistics.

A similar estimation for the field strength (about 15 G) was obtained by Roberts *et al.* (1984) from the observations of Koutchmy *et al.* (1983) discussed in Section 3.2. However, in contrast with the TRACE observations, the lack of the direct observability of the oscillating loop did not make the interpretation of the oscillations in terms of the kink modes absolutely secure.

Asai *et al.* (2001) observed microwave quasi-periodic pulsations with a periodicity of 6.6 s, which are associated with a global kink oscillation. Using Equation (32) and assuming  $n_e/n_0 = 0.1$ , we find the loop to have a magnetic field strength of 400 G. This value is consistent with a magnetic field extrapolation (see Asai *et al.*, 2001, which found a magnetic field strength of 300 G). For an alternative interpretation of this observation in terms of the global fast sausage mode, see Section 4.

### 3.4 Decay of the oscillations

The physical mechanism responsible for the quick decay of the oscillations is under intensive discussion. The direct dissipation caused by viscosity or resistivity, considering classical values of the coronal viscosity and resistivity, cannot explain the observed decay times (see the discussion in Roberts, 2000). Ofman *et al.* (1994) numerically established the scaling law

$$\frac{\tau}{P} = 16.3 \text{ Re}^{0.22}, \quad (33)$$

which connects the decay time  $\tau$  of the oscillation, the Reynolds number  $\text{Re} (= LC_{A0}/\nu)$  associated with the shear viscosity  $\nu$ , and the oscillation period  $P$  of a fundamental mode with wavelength

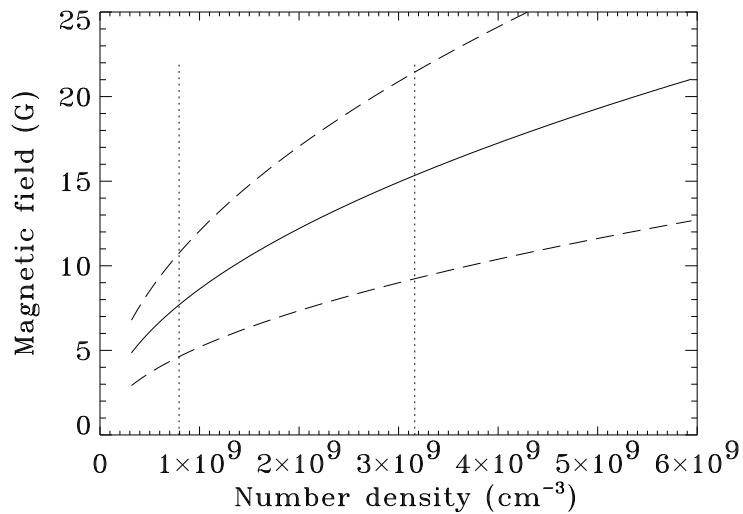


Figure 12: The magnetic field inside a coronal loop as function of plasma density inside the loop, determined by Equation (32). The external to internal density ratio is 0.1. The solid curve corresponds to the central value of the kink speed  $C_K = 1030 \pm 410 \text{ km s}^{-1}$  (for the event of the 4 July 1999), and the dashed curves correspond to the upper and the lower possible values of the speed. The vertical dotted lines give the limits of the loop density estimation using TRACE 171 Å and 195 Å images. The distance between the loop footpoints is estimated as 83 Mm (from Nakariakov and Ofman, 2001).

$2L$ . In this study, the decay mechanism was resonant absorption (see Section 2.2.1) of a collective kink mode and the authors restricted their attention to linear perturbations only. Applying this law, Nakariakov *et al.* (1999) suggested that the decay of kink oscillations might be explained by resonant absorption with enhanced shear viscosity. It should be pointed out that this result is not in contradiction to common sense, as enhanced dissipation actually means that the coefficient of shear viscosity in the Braginskii viscosity tensor is comparable to the bulk viscosity coefficient. If so, this must be connected with coronal micro-turbulence. Such a situation is not unusual in astrophysics (e.g., the invoking of turbulent viscosity in the understanding of the physical properties of accretion disks) and is often seen in laboratory plasmas.

The basic idea behind resonant absorption is that the wave energy of the damped global fast kink mode is converted to a localised Alfvén mode through resonant coupling. This coupling occurs in a shell in the loop boundary where the kink mode frequency, which is always between the internal and external Alfvén frequencies, matches the local Alfvén frequency. The combination of these two modes, through resonant coupling, is also called a quasi-mode. In the absence of an equilibrium flow this mode damps independently of dissipation. For a thin, weakly dissipative loop with a thin boundary layer between  $a - \ell$  and  $a$  of the form  $\rho(r) = [(\rho_0 + \rho_e) - (\rho_0 - \rho_e) \cos((r - a)\pi/\ell)]/2$ , the global kink wave has a decay time (which may be derived from Equation (13)) (Ruderman and Roberts, 2002)

$$\frac{\tau}{P} = \frac{2}{\pi} \left( \frac{\ell}{a} \right)^{-1} \left( \frac{\rho_0 + \rho_e}{\rho_0 - \rho_e} \right), \quad (34)$$

where  $\ell$  is the width of the loop boundary, which is assumed to be thin compared with the loop width  $2a$ , and  $P$  is the mode period  $2L/C_K$ . This expression does not contain the viscosity coefficient, and the authors concluded that the observed decay time was not connected with dissipation. However, the observed decay times could be explained if  $\ell = 0.23a$ . Sharper profiles give longer damping times; shallower profiles lead to global motions that are rapidly damped. Goossens *et al.* (2002a) examined the observations further, using the selection of eleven loops presented by Ofman and Aschwanden (2002), and concluded that the resonant absorption decay Equation (34) was able to reproduce the observed decay times provided the inhomogeneity scale  $\ell$  as a fraction of tube radius  $a$  ranged in value from  $\ell/a = 0.16$  to  $\ell/a = 0.49$ . This result would violate, though, the assumption  $\ell \ll a$ . But Van Doorsselaere *et al.* (2004) showed numerically that, even for this range of values of  $\ell/a$ , the analytical Equation (34) remains valid. Aschwanden *et al.* (2003) compared the theoretically predicted values of the density ratio  $\rho_e/\rho_0$  with observations and concluded that they are in poor agreement, which was attributed to the narrowness of the TRACE 171 Å temperature bandpass.

In addition, Equation (34) may give unrealistically short decay times comparable with the oscillation period. It is not clear how the phenomenon of resonant absorption can happen in those cases when the decay time is comparable with the oscillation period and, consequently, the oscillation is not harmonic, making the resonance impossible. In any case, resonant absorption remains a plausible interpretation of the decay.

Another alternative interpretation is connected with the effect of phase-mixing (Roberts, 2000; Ofman and Aschwanden, 2002) (see Section 2.2.2). The decay of a standing Alfvén waves by phase-mixing, given by Equation (17), becomes after assuming that  $dC_A/dx \approx C_A/\ell$ :

$$\frac{\tau}{P} = \left( \frac{3}{4\pi^2} \right)^{1/3} \left( \frac{\ell}{L} \right)^{2/3} \text{Re}^{1/3}. \quad (35)$$

In principle  $\text{Re}$  is the shear Reynolds number,  $\text{Re} = LC_A/\nu$ , with  $\nu$  the kinematic shear viscosity coefficient. If we take the theoretical values for  $\nu$ , then the decay time due to phase-mixing is orders of magnitude longer than the observed decay. Ofman and Aschwanden (2002) claimed that, due to micro-turbulence or kinetic processes modifying the velocity distribution of ions,  $\nu$

could be of the same order as the bulk viscosity coefficient, practically returning back to the idea suggested by Nakariakov *et al.* (1999). Hence, decay due to phase-mixing can be of the same order as the observed decay. We would like to emphasise that in the case discussed here, the phase mixing mechanism does not involve the torsional modes, but is connected with kink perturbations of neighbouring loops.

A different approach to the problem is based on the leakage of wave energy from the loop. Cally (1986, 2003) showed that the fast kink mode is almost identical to a fast leaky kink mode. In the long wavelength limit both modes propagate at the kink speed. In the limit of the plasma- $\beta$  tending to zero, the amplitude of the leaky kink mode decreases as it radiates into the coronal environment with a decay time (Cally, 2003, note a factor 2 error in his expression)

$$\frac{\tau}{P} = \frac{2}{\pi^4} \left( \frac{a}{L} \right)^{-2} \left( \frac{\rho_0 + \rho_e}{\rho_0 - \rho_e} \right)^2, \quad (36)$$

which, unless the loop width  $2a$  is considerably larger than the observed loop emission width, is too long to explain the observed decay, especially for large loops (see Figure 13). For example for a loop of length 200 Mm,  $a$  needs to be in the range of 10–20 Mm.

The wave energy may also leak through its footpoints. Roberts (2000) concluded from the theoretical study by Berghmans and de Bruyne (1995) that this type of leakage is insufficient to explain the observed decay. De Pontieu *et al.* (2001), though, argued that this study did not take the chromosphere into account. The amplitude decay of an Alfvén wave leaking into a chromosphere with density scale-height  $h$ , typically 150–200 km, is (Hollweg, 1984)

$$\frac{\tau}{P} = \frac{1}{4\pi^2} \left( \frac{h}{L} \right)^{-1}, \quad (37)$$

which is about five times longer than the observed decay (see Figure 13). This was confirmed by the numerical study by Ofman (2002), who also pointed out some inconsistencies in the work by De Pontieu *et al.* (2001). A similar study of footprint leakage of fast kink modes themselves has not yet been undertaken but it should take into account the stratification of the external medium and the magnetic field divergence with height. Both effects are expected to increase the efficiency of the reflection of kink modes at the footpoints and, consequently, reduce the leakage.

Ofman and Aschwanden (2002) suggested that observationally determined scaling laws, connecting the decay times with oscillation periods and lengths of oscillating loops, may provide some information allowing us to distinguish between the interpretations discussed above. Indeed different decay mechanisms give different scaling laws: coronal leakage ( $\tau \propto L^2 P$ ), footprint leakage ( $\tau \propto LP$ ), resonant absorption ( $\tau \propto P$ ), and phase-mixing ( $\tau \propto P^{2/3}$ ). By using the fact that the period is proportional to the loop length, one can be eliminated in favour of the other.

Ofman and Aschwanden (2002) determined scaling laws from observational decay times measured by Nakariakov *et al.* (1999) and Aschwanden *et al.* (2002). In particular they found that  $\tau \propto P^{1.17 \pm 0.34}$ . They concluded that the mechanism of phase-mixing agrees best with the scaling laws. They, though, assumed that the length  $\ell$  in Equation (35) is proportional to the length of the loop to obtain a modified scaling law for phase-mixing:

$$\tau \propto (LP)^{2/3} \propto P^{4/3}. \quad (38)$$

There is indeed a good correspondence between the theoretical and observational power law index. However, it is not clear why  $\ell$  should be proportional to  $L$ . If the original scaling law for phase-mixing is considered, then the difference is larger than one standard deviation. Also, the mechanism of resonant absorption, which has a power law index of 1 falls within one standard deviation of the observationally determined power law index and can, therefore, not be excluded. The mechanisms

of coronal and footpoint leakage have power law indices of 3 and 2, respectively, which is clearly not consistent with observations.

Figure 13 shows the observationally determined decay times as a function of wavelength and period and uses measurements from Nakariakov *et al.* (1999), Aschwanden *et al.* (2002), Wang and Solanki (2004), and Verwichte *et al.* (2004), which adds two more measurements compared with the study of Ofman and Aschwanden (2002). We have to bear in mind, though, that the measurement from Wang and Solanki (2004) refers to a vertically polarised oscillation and that the measurement from Verwichte *et al.* (2004) is an averaged value from seven damped kink oscillations in a prominence driven loop arcade. The data points are fitted by power laws which have the dependencies  $\tau \propto \lambda^{0.70 \pm 0.32}$  and  $\tau \propto P^{1.12 \pm 0.36}$ . The dependence on the wavelength seems to favour phase-mixing, without excluding resonant absorption, and the dependence on period seems to favour resonant absorption but is also consistent with the modified scaling law for phase-mixing. In any case, more examples are needed as the data are too scattered.

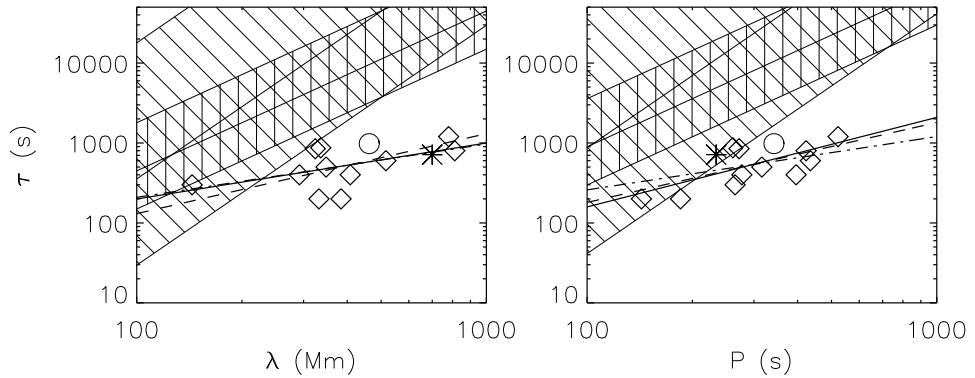


Figure 13: Observationally determined loop oscillation decay times as a function of wavelength (left) and period (right) from: Nakariakov *et al.* (1999) and Aschwanden *et al.* (2002) ( $\diamond$ ), Wang and Solanki (2004) (\*), and Verwichte *et al.* (2004) ( $\circ$ ). The solid lines are a best fit to the observations, corresponding to  $\tau \propto \lambda^{0.70 \pm 0.32}$  and  $\tau \propto P^{1.12 \pm 0.36}$ . The dashed and dash-dotted lines are the best fits using the models of resonant absorption and phase-mixing, respectively. The vertically and diagonally shaded region correspond to theoretical decay times due footpoint leakage of Alfvén waves (Hollweg, 1984) and coronal leakage of a fast leaky kink mode (Cally, 2003), respectively, for a range of realistic coronal values for  $C_A = 500 - 2000 \text{ km s}^{-1}$ ,  $a = 1 - 8 \text{ Mm}$ , and  $\rho_e/\rho_0 = 5 - 100$ .

Verwichte *et al.* (2004) studied TRACE observations of 15 April 2001 of kink oscillations in a post-flare loop arcade. The loops of this arcade were made to oscillate by the actions of a nearby prominence eruption. The oscillation signatures of nine loops were determined as a function of distance along each loop. They found that the displacement amplitude decreases with distance from the loop top as expected for a fundamental mode. However, two of the loops showed two, simultaneous oscillation modes with the longest period, roughly twice the shortest period. Also, the displacement amplitude of the shortest period oscillation increases with distance from the loop top, which indicates that it is an harmonic mode. The measured decay times of the loop oscillations shows the same dependence on the oscillation period as for previous observations, but with a clear bias towards longer decay times. There are several possible explanations for this bias. Firstly, this study considered an oscillating arcade of post-flare loops, while previous observations are concerned with more isolated active region loops. The decay times may be influenced by the different structuring of post-flare loops or by interactions between neighbouring loops in the arcade.

Secondly, the arcade oscillation is driven by a nearby prominence eruption that may have given multiple impulses to the arcade. If a time of 5–10 min is subtracted from all the decay times, then they fall in the range of decay times of the earlier studies. The relationship between the decay time and the period, though, would then be much steeper.

Further development of this discussion on the decay of kink oscillations is connected with the improvement of the observational statistics and high-resolution 3D numerical modelling of oscillating loops. In particular, an important issue is whether the loop cross-section remains unperturbed during kink oscillations. Also, the question of the excitation of these modes, connected with the observational fact that the kink oscillations are a rather rare phenomenon, is still open.

### 3.5 Alternative mechanisms

The idea that a coronal loop is twisted and then carries an electric current gave rise to several alternative mechanisms for the loop oscillations.

An LCR-circuit model developed by [Zaitsev et al. \(1998\)](#) explains the loop oscillations in terms of eigen oscillations of an equivalent electric circuit, where the current is associated with the loop twist. Approximating the magnetic loop by a thin torus and estimating the effective circuit capacitance  $\mathcal{C}$  and inductance  $\mathcal{L}$  as

$$\mathcal{C} = \frac{c^4 \rho_0 S^2}{2\pi L I^2}, \quad (39)$$

$$\mathcal{L} = 4L \left( \log \frac{8L}{(\pi S)^{1/2}} - \frac{7}{4} \right), \quad (40)$$

where  $c$  is the speed of light,  $\rho_0$  is the density inside the loop,  $L$  and  $S$  are the length and cross-sectional area of the coronal part of the loop, respectively, and  $I$  is the electric current along the loop axis. The period of the oscillations is then given by the expression

$$P = \frac{2\pi}{c} (\mathcal{LC})^{1/2}. \quad (41)$$

As one of the physical quantities perturbed by this effect is the current (or the twist), its periodic pulsations would be observed through the direct modulation of the gyrosynchrotron emission by the period change of the angle between the LOS and the magnetic field in the emitting region. Also, as the periodic twist is accompanied by perturbations of density – see Equation (26) –, the oscillations would modulate thermal emission as well. Also, twist perturbations could modulate the loop minor radius, resembling the sausage mode. The decay of the oscillations is normally estimated by this model to be very small.

[Khodachenko et al. \(2003\)](#) applied the idea of inductive interaction of electric currents in a group of neighbouring loops to an alternative interpretation of kink oscillations, suggesting that they are caused by the ponderomotoric interaction of currents in groups of inductively coupled current-carrying loops. More specifically, the ponderomotoric interaction of current-carrying magnetic loops can lead to the oscillatory change of the loops inclination. The efficiency of coupling, the period of oscillations and the decay time are connected with mutual inductance of different loops in the active region analysed. Also, it was pointed out that the interaction of the oscillating loop with neighbouring loops can lead to strong damping of the oscillations.

We would like to stress that the periods of loop oscillations described by LCR-contour models should be longer than the Alfvén travel time *along* the loop, which determines the response time of the current system, so  $P > L/C_{A0}$ .

Dynamic models of magnetic reconnection predict that the processes of tearing instability and coalescence of magnetic islands occur iteratively, leading to an intermittent or impulsive bursty energy release and particle acceleration. [Tajima et al. \(1987\)](#) demonstrated the possibility of

oscillatory regimes in coalescence of current carrying loops, combining a simplified 1D analytical approach and numerical modelling. The minimal period of oscillations was found to be

$$P = 2\pi \frac{C_{s0}^3 \varepsilon}{C_{A0}^4}, \quad (42)$$

where  $\varepsilon$  is the characteristic length of the interaction process, connected in this case with the width of a current sheet formed at the boundary between two interacting twisted loops. These oscillations are essentially nonlinear, and it is likely that their period is somehow connected with amplitude.

## 4 Sausage Oscillations of Coronal Loops

The fast magnetoacoustic *sausage* mode ( $m = 0$ ) is another type of localised, modified fast magnetoacoustic wave. It is associated with perturbations of the loop cross-section and plasma concentration. This mode is mainly transverse and the perturbations of plasma velocity in the radial direction are stronger than perturbations along the field. According to Figure 3, the phase speed of this mode is in the range between the Alfvén speed inside and outside the loop. This mode has a long wavelength cutoff (Roberts *et al.*, 1984),

$$k_{zc} a = j_0 \left[ \frac{(C_{s0}^2 + C_{A0}^2)(C_{Ae}^2 - C_{T0}^2)}{(C_{Ae}^2 - C_{A0}^2)(C_{Ae}^2 - C_{s0}^2)} \right]^{1/2}, \quad (43)$$

where  $j_0 \approx 2.40$  is the first zero of the Bessel function  $J_0(x)$ . For a magnetic slab with the step function and Epstein density profiles, this value is

$$k_{zc} a = \sqrt{\frac{C_{A0}^2}{C_{Ae}^2 - C_{A0}^2}} \begin{cases} \pi/2 & (\text{step function}) \\ \sqrt{2} & (\text{Epstein function}) \end{cases}, \quad (44)$$

For  $k \rightarrow k_{zc}$  the mode approaches the cut-off, the phase speed,  $C_{ph}$ , which is equal to  $\omega/k_z$ , tends to  $C_{Ae}$  from below, and in the short wave length limit, for  $k \rightarrow \infty$ ,  $C_{ph}$  tends to  $C_{A0}$  from above.

The period  $P_{GSM}$  of the global sausage mode of a coronal loop is determined by the loop length  $L$ ,

$$P_{GSM} = \frac{2L}{C_{ph}}, \quad (45)$$

where  $C_{ph}$  is the specific phase speed of the sausage mode corresponding to the wave number  $k_z = \pi/L$ ,  $C_{A0} < C_{ph} < C_{Ae}$ . The length of the loop  $L$  should be smaller than  $\pi/k_{zc}$  to satisfy the condition  $k > k_c$ . For a strong density contrast inside and outside the loop, the period of the sausage mode satisfies the condition

$$P_{GSM} < \frac{2\pi a}{j_0 C_{A0}} \approx \frac{2.62a}{C_{A0}}, \quad (46)$$

as the longest possible period of the global sausage mode is achieved when  $k = k_{zc}$ . We would like to emphasise that Equation (46) is an *inequality*, and that the actual resonant frequency is determined by Equation (45), provided Equation (46) is satisfied. Combining Equations (46) and (45), we conclude that the necessary condition for the existence of the global sausage mode is

$$\frac{L}{2a} < \frac{\pi}{2j_0} \frac{C_{Ae}}{C_{A0}} \approx 0.65 \sqrt{\frac{\rho_0}{\rho_e}}, \quad (47)$$

so the loop should be sufficiently thick and dense (e.g., in the case of a flaring loop).

Nakariakov *et al.* (2003) demonstrated the applicability of the correct estimation for the global sausage mode period (Equation (45)) by interpreting high spatial and temporal resolution observations of 14–17 s oscillations of coronal loops, performed with the Nobeyama radioheliograph. For the analysed flare, it was found that the time profiles of the microwave emission at 17 and 34 GHz exhibit synchronous quasi-periodical variations of the intensity in different parts of the corresponding flaring loop. The length of the flaring loop is estimated as  $L = 25$  Mm and its width at half intensity at 34 GHz as about 6 Mm. These estimations are confirmed by Yohkoh/SXT images taken on the late phase of the flare. The distribution of the spectral density in the interval 14–17 s along the loop showed the peak of oscillation amplitude near the loop apex and depression

at the loop legs, consistent with the structure theoretically predicted for a global (fundamental) mode. Estimation of the period of this mode, according to Equation (47), gives the resonant period in the observed range. Also, for the loop considered, the sausage mode cut-off value  $k_{zca}$  is about  $0.25 - 0.28$ . Thus, the longest theoretically possible wavelength  $\lambda$  of the trapped sausage mode of the considered loop is  $\lambda \approx (22 - 25)a$ . Consequently, as the observed loop radius is about 1/8 of its length, this loop could indeed support the global sausage mode.

Observations in the radioband and in X-rays often show also shorter periodicities, in particular in the range  $0.5 - 10$  s (see, e.g., Aschwanden, 1987, 2003). These oscillations are also traditionally associated with sausage (or radial) modes (see, e.g., Zaitsev and Stepanov, 2002, 1989). It was suggested that the energetic particles produced by a flare are somehow modulated by the sausage oscillations of the flaring loop, localised near the top of the loop. The period of this oscillations is supposed to be given by the fast magnetoacoustic wave travel time across the loop, in other words as the ratio of the loop diameter and the fast magnetoacoustic speed  $(C_{A0}^2 + C_{s0}^2)^{1/2}$ . However, it is not clear what determines the longitudinal length of the oscillation and why it does not propagate along the loop. If the longitudinal wave length is prescribed by the length of the loop, the sausage mode wave number is lower than the cut-off value and the mode is leaking, which is in contradiction with observed high quality of the short period oscillations (see also Aschwanden *et al.*, 2004). The last difficulty can be overcome if there is some mechanism continuously feeding the oscillations or if the leakage is negligible. Also, quasi-periodic pulsations of shorter periods ( $0.5 - 10$  s) may be associated with sausage modes of higher spatial harmonics (Roberts *et al.*, 1984), if the longitudinal wave length is shorter than the loop length. However, usually the short period oscillations are observed as a single high quality peak in the periodogram, and it is not clear why only this particular harmonics is excited. The role of ballooning modes has not been established yet.

Earlier, we discussed the microwave quasi-periodic pulsations observed by Asai *et al.* (2001) in the context of a global kink mode. The spatial resolution of the radio data is not sufficient to actually observe the spatial loop displacements. Therefore, can this pulsation also be attributed to a global sausage mode? A sausage mode can more naturally explain the modulation of X-ray emission as it is compressive. Asai *et al.* (2001) estimated the loop width to be 6 Mm. Condition (47) for the existence of a sausage normal mode restricts the density ratio to be  $\rho_0/\rho_e > 17$ , which is reasonable. If we take  $\rho_0/\rho_e = 20$ , then the external Alfvén speed is approximately  $C_{Ae} \approx 2L/P = 4850$  km s $^{-1}$ . The internal Alfvén speed is then found to be  $C_{A0} \approx (\rho_e/\rho_0)^{1/2}C_{Ae} = 1080$  km s $^{-1}$ . Using the value of the loop density determined by Asai *et al.* (2001), a value for the magnetic field strength of 120 G follows. This value is three times smaller than Asai *et al.* (2001) obtained from a magnetic field extrapolation. From this point of view the global kink mode seems to be the most likely explanation for the microwave pulsations, but the global sausage mode cannot be dismissed outright.

## 5 Acoustic Oscillations of Coronal Loops

Acoustic or, more precisely, slow magnetoacoustic waves are an abundant feature of the coronal wave activity, confidently observed by several instruments, e.g., SOHO (EIT, UVCS, and SUMER), and TRACE. These MHD wave modes are practically longitudinal, perturbing the density of the plasma and the parallel component of the velocity. Consequently, they are observed as disturbances of EUV (and, possibly, X-ray) emission and, if the line of sight has a component parallel to the local magnetic field, as the periodic Doppler shift. Both propagating and standing waves are observed.

### 5.1 Global acoustic mode

The SOHO/SUMER spectral instrument has recently discovered quasi-periodic oscillations of intensity and a Doppler shift in the coronal emission lines Fe XIX and Fe XXI (Kliem *et al.*, 2002; Wang *et al.*, 2002, 2003b,a, and references therein). Figure 14 gives an illustration of such oscillations. These spectral lines are associated with a temperature of about 6 MK, corresponding to the sound speed of about  $370 \text{ km s}^{-1}$ . The observed periods are in the range 7–31 min, with decay times 5.7–36.8 min, and show an initial large Doppler shift pulse with peak velocities up to  $200 \text{ km s}^{-1}$ . The intensity fluctuation lags the Doppler shifts by 1/4 period. In a statistical study of 54 oscillation cases, Wang *et al.* (2003a) found that except for a few cases, the presence of definite periodicity in intensity fluctuations is not certain. Moreover, oscillations are not seen in other emission lines observed simultaneously with the oscillating lines. In the initial stage of all 54 cases analysed by Wang *et al.* (2003a), there is a rapid increase in the line intensity and a large Doppler shift, indicating that the oscillations are excited impulsively.

Ofman and Wang (2002) suggested that these oscillations are produced by the global standing acoustic mode,

$$V_z(s, t) \propto \cos\left(\frac{\pi C_s}{L} t\right) \cos\left(\frac{\pi}{L} s\right), \quad (48)$$

$$\rho(s, t) \propto \sin\left(\frac{\pi C_s}{L} t\right) \sin\left(\frac{\pi}{L} s\right), \quad (49)$$

where  $V_z$  is the longitudinal velocity,  $C_s$  is the speed of sound,  $L$  is the loop length, and  $s$  is a distance along the loop with the zero at the loop top. More strictly, the phase speed of the longitudinal mode of a coronal loop should, in the long wave length limit, be equal to the tube speed  $C_{T0}$  inside the tube, however in the low plasma- $\beta$  plasma of the solar corona this value is very close to the sound speed  $C_s$ . From Equation (48), the oscillation period is given by the expression  $2L/C_s$ . According to the thermally conductive, viscous, nonlinear one-dimensional MHD simulations, the short decay time is connected with the dissipation because of high thermal conductivity of the hot plasma filling the loop. Mendoza-Briceño *et al.* (2004) has recently developed this study, taking into account effects of stratification. It was found that stratification would lead to insignificant changes in the decay times (maximum 15–20%).

There are still several open questions in both the theory and the observations: how are the oscillations triggered and excited; why are intensity oscillations not always seen, whether the occurrence rate of oscillations is temperature dependent (in major cases in Fe XIX, i.e., in hot plasma), what is the role of non-adiabatic effects (e.g., thermal instability)?

Also, it is not clear how the SUMER oscillations are related with other coronal oscillations, observed in the radio (e.g., Aschwanden, 2003) and X-ray bands.

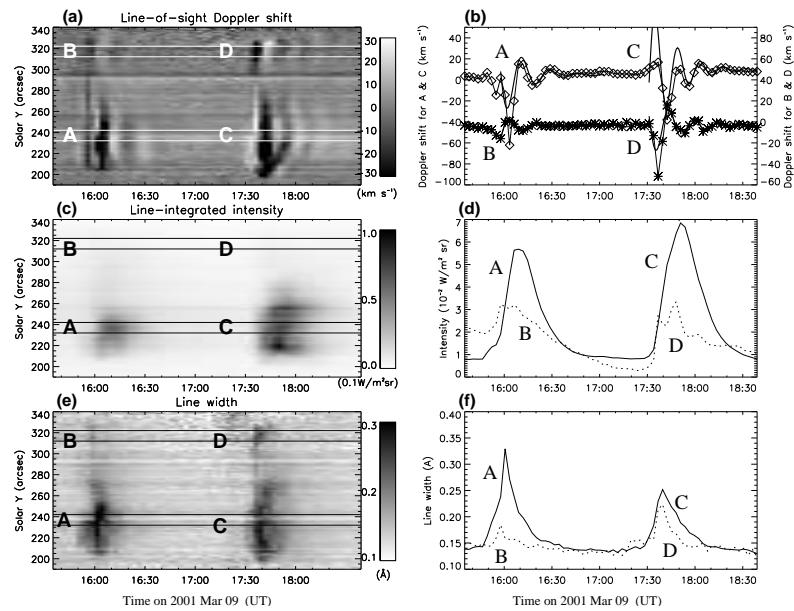


Figure 14: Doppler oscillation events in the Fe xix line observed with the SUMER instrument on 9 March 2001. **a)** Doppler shift time series. The redshift is represented with the bright colour, and the blueshift with the dark colour. **b)** Average time profiles of Doppler shifts along cuts AC and BD. The thick solid curves are the best fit functions of the form  $V(t) = V_0 + V_D \sin(\omega t + \phi) \exp(-\gamma t)$ . **c)** Line-integrated intensity time series. **d)** Average time profiles of line-integrated intensities along cuts AC and BD. For a clear comparison, the intensity profile for BD has been stretched by a factor of 10. **e)** Line width (measured Gaussian width) time series. **f)** Average time profiles of line width along cuts AC and BD (from Wang *et al.*, 2003a).

## 5.2 Second standing harmonics

Recently, Nakariakov *et al.* (2004b) modelled the evolution of a coronal loop in response to an impulsive energy release and demonstrated that the second standing acoustic harmonics appears as a *natural response* of the loop to an impulsive energy deposition. Modelling the loop as a 1D hydrodynamic system with nonlinearity, radiative damping, thermal conduction and accounting for possible chromospheric up and down flows, it was demonstrated that the second harmonics is a common feature of the loop evolution. Figure 15 shows typical time curves of the density and temperature at the loop apex. The quasi-periodic behaviour is clearly seen in the apex density curve, which is consistent with the mode structure

$$V_x(s, t) = A \cos\left(\frac{2\pi C_s}{L} t\right) \sin\left(\frac{2\pi}{L} s\right), \quad (50)$$

$$\rho(s, t) = -\frac{A\rho_0}{C_s} \sin\left(\frac{2\pi C_s}{L} t\right) \cos\left(\frac{2\pi}{L} s\right), \quad (51)$$

where  $A$  is the wave amplitude. (The paper of Nakariakov *et al.*, 2004b, contains a misprint, the factor of two is missing from Equations (3) and (4)). The density perturbations have a maximum near the loop apex, while longitudinal velocity perturbations have there a node.

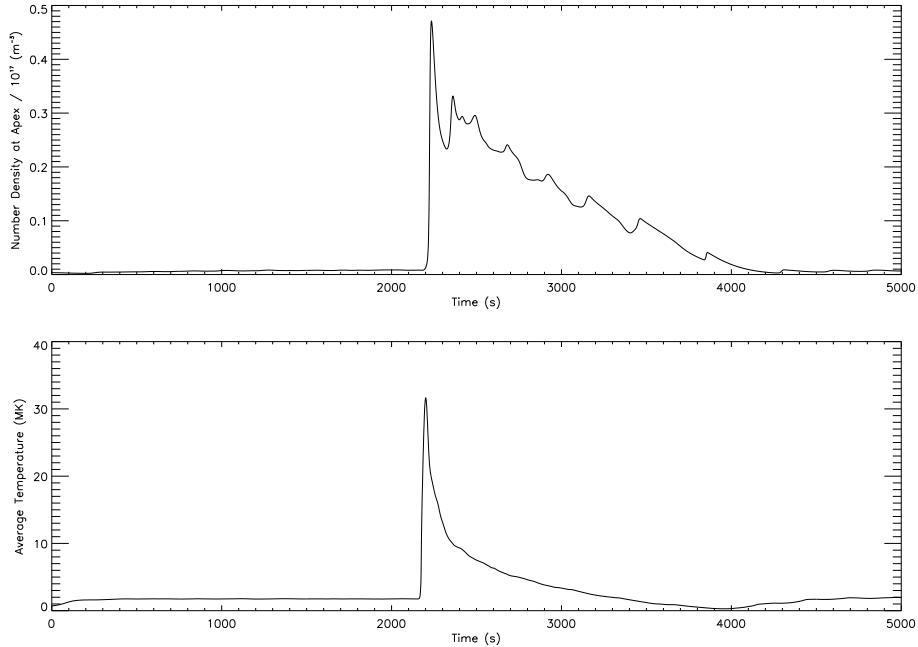


Figure 15: A typical response of a 1D loop to the flaring heat deposition near the apex. The density curve demonstrates pronounced quasi-periodic pulsations associated with the second standing acoustic harmonics.

The second standing acoustic mode may be responsible for quasi-periodic pulsation with periods in the range 10–300 s which are often observed in flare light curves in radio and X-ray bands. The SUMER oscillations mentioned above are likely to be associated with some other excitation mechanism, as only a small fraction of SUMER oscillations are observed in association with solar flares (Wang *et al.*, 2003a). Traditionally, the acoustic wave interpretation has been excluded as the waves of these periodicities were supposed to be highly dissipative in the hot plasma of flaring

loops. However, the numerical simulations performed by Nakariakov *et al.* (2004b), as well as the recently gained abundant observational evidence of the presence of acoustic waves in the solar corona, suggest that the observed periodicities can be associated with this mode. The decayless character of these oscillations may be explained in terms of auto-oscillations: By the competition of the oscillation energy losing by dissipation and the energy deposition to the oscillation, e.g., through thermal over-stability.

## 6 Propagating Acoustic Waves

### 6.1 Observational results

One of the most wide-spread examples of the coronal wave activity is the slow propagating intensity disturbances observed with imaging telescopes in both open and closed coronal magnetic structures. The standard detection technique is the use of the stroboscopic method: the emission intensities along a chosen path, taken in different instants of time are laid side-by-side to form a time-distance map. Diagonal stripes on these maps exhibit disturbances which change their position in time and, consequently, propagate along the path. This method allows the determination of periods (or wavelengths), relative amplitudes and projected propagation speeds. Usually these waves are observed propagating along the assumed coronal magnetic structures and, thus, along the magnetic field. Their speeds are usually much slower than the expected coronal Alfvén speed which leads to their interpretation as longitudinally propagating slow magnetoacoustic (aka acoustic or longitudinal) waves.

The first observational detection of longitudinal waves came from analysing the polarised brightness (density) fluctuations. The fluctuations with periods of about 9 min, were detected in coronal holes at a height of about  $1.9 R_{\odot}$  by Ofman *et al.* (1997, 1998b) using the white light channel of SOHO/UVCS. Developing this study and analysing several other UVSC data sequences with a 75–125 s cadence time, Ofman *et al.* (2000b) determined the fluctuation periods in the range of 7–10 min. The propagation speeds of the fluctuations indicated values in the range of  $160$ – $260 \text{ km s}^{-1}$  at  $2 R_{\odot}$ . This value of the speed is slightly below the estimated value of the sound speed. Possibly, a similar phenomenon was observed by Marsh *et al.* (2002), who detected quasi-periodic variability of coronal EUV emission lines covering a temperature range of  $\log T_e = 5.3$ – $6.1 \text{ K}$  with SOHO/CDS. Statistically significant periods were found within the range 100–900 s and 1500 s, also short wavepackets with periods of the order 50–100 s with durations of 2–5 cycles were reported.

DeForest and Gurman (1998), using EIT 171 Å data confirmed this discovery: Outwardly propagating perturbations of the intensity were observed at distances of  $1.01$ – $1.2 R_{\odot}$ , gathered in quasi-periodic groups of 3–10 periods, with periods of about 10–15 min, The projected speeds are about  $75$ – $150 \text{ km s}^{-1}$  and the relative amplitude (in density) was about 2–4 %.

A similar phenomenon was observed near the footpoints of coronal loops, with EIT (Berghmans and Clette, 1999) and TRACE (Nightingale *et al.*, 1999; De Moortel *et al.*, 2000, 2002a,b) imagers as near-isothermal EUV intensity disturbances, which start near the loop footpoints and propagate along the loops at the apparent speed lower than the sound speed. Multi-wavelength observations have been performed by Robbrecht *et al.* (2001) combining TRACE 171 Å and EIT 195 Å and by King *et al.* (2003) with TRACE 171 Å and 195 Å. Robbrecht *et al.* (2001) found the projected propagation speeds to vary roughly between 65 and 150  $\text{km s}^{-1}$  for both instruments, which is close to and below the expected sound speed in the coronal loops, respectively. King *et al.* (2003) pointed out the high correlation of the disturbances observed in the different bandpasses. Also, recently, a coordinated observation of this phenomenon with SOHO/CDS and TRACE instruments has been carried out Marsh *et al.* (2003). A propagating oscillation with a period of about 300 s, observed by TRACE in the 171 Å bandpass, was also observed in He I, O V and Mg IX emission lines with CDS, corresponding to the chromospheric, transition region, and coronal temperatures, respectively. This is consistent with about 5 min oscillations observed by O'Shea *et al.* (2001) with CDS in both velocity and intensity time series associated with the coronal lines Mg IX and Fe XVI, as well as in O V.

A comprehensive overview of observational properties of the longitudinal oscillations, based upon the analysis of 38 examples, is given in De Moortel *et al.* (2002a), and a more recent one in Nakariakov (2003). The properties of propagating EUV disturbances may be summarised as

follows: the projected propagation speed is  $35 - 165 \text{ km s}^{-1}$ ; the amplitudes are always less than 10 % in intensity (less than 5 % in density); the disturbances are quasi-periodic with the periods about 140–420 s. In most cases, only upwards propagating disturbances have been detected (from the footpoints to the apex of the loop). Sometimes, the waves can be present for several consecutive hours with, more or less, constant period. It is possible that the disturbances with shorter, about 3 min, periods are situated above sunspot regions, whereas disturbances propagating along the loops which are not associated with sunspots have longer periodicity, of about 5 min (De Moortel *et al.*, 2002c). However, King *et al.* (2003) showed that both 3 min and 5 min perturbations can coexist in the same coronal structure, at least in the analysed example, so the question still remains open.

The propagation direction and speed, together with the fact that the observed waves are compressible suggest their interpretation as slow magnetohydrodynamic waves. Slow waves of the observed periodicities (shorter than 20 min) can propagate without reflection in the 1.0–2.0 MK corona, as the acoustic cut-off period is about 70 min. According to this interpretation, the waves propagate at about the sound speed in the loop. The observed speed of the waves is reduced by line-of-sight projection.

Waves were also recently detected in the Doppler velocity data in the 1–3 mHz and 5–7 mHz ranges by Sakurai *et al.* (2002). The line intensity and line width did not show clear oscillations, but their phase relationship with the Doppler velocity indicates propagating waves rather than standing waves. These waves were interpreted as superposition of propagating slow and Alfvén waves.

## 6.2 Theoretical modelling

Theoretical models of the propagation of longitudinal waves in stratified coronal structures, such as polar plumes (Ofman *et al.*, 1999, 2000a) and coronal loops (Nakariakov *et al.*, 2000), describe the evolution of the wave shape and amplitude with the distance along the structure  $s$  in terms of the extended Burgers equation

$$\frac{\partial A}{\partial s} - a_1 A - a_2 \frac{\partial^2 A}{\partial \xi^2} + a_3 A \frac{\partial A}{\partial \xi} = 0, \quad (52)$$

where the coefficients  $a_1$ ,  $a_2$ , and  $a_3$  are, in general, functions of  $s$  and describe:  $a_1$  – the effects of stratification, radiative losses, and heating;  $a_2$  – dissipation by thermal conductivity and viscosity;  $a_3$  – nonlinearity. The  $\xi = s - C_s t$  is the running coordinate. When  $a_1 = 0$ , Equation (52) reduces to the Burgers equation. Specific expressions for the coefficients depend upon the geometry of the problem and are different in the plume and loop cases.

Let us illustrate the derivation of Equation (52) in a specific situation. Following Tsiklauri and Nakariakov (2001), we consider a semi-circular loop of the curvature radius  $R_L$ , with the inclination angle  $\alpha$  (measured from the normal to the solar surface) and a non-zero offset of circular loop centre from the coronal base line,  $Z_0$  (i.e., distance from the circle's centre to the solar surface). The loop cross-section is taken to be constant. The loop is filled with a gravitationally stratified magnetised plasma of constant temperature. The sketch of the model is shown in Figure 16.

The gravitational acceleration along the loop is

$$g(s) = \frac{GM_\odot}{R_\odot^2} \frac{\left[ \frac{X_0}{R_L} x - \frac{Z_0}{R_L} h \right] \cos \alpha}{\left[ 1 + \frac{R_L}{R_\odot} \left( \frac{X_0}{R_L} h - \frac{Z_0}{R_L} (1-x) \right) \cos \alpha \right]^2}, \quad (53)$$

where  $h = \sin(s/R_L)$ ,  $x = \cos(s/R_L)$ , and  $X_0/R_L = (1 - Z_0^2/R_L^2)^{1/2}$ . The use of the hydrostatic equilibrium equations and the isothermal equation of state, allows us to write the stationary density

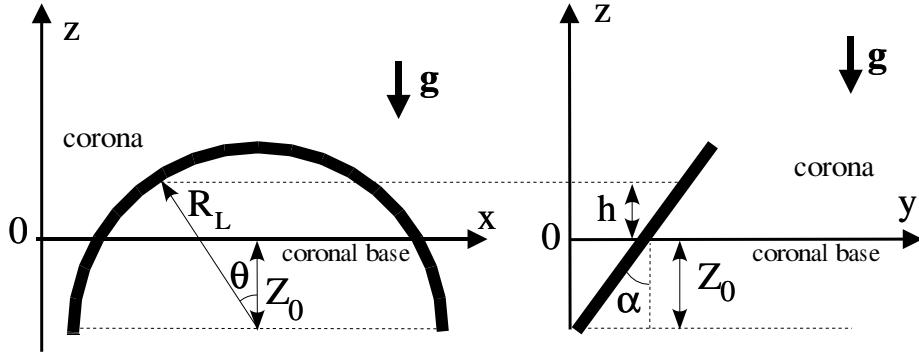


Figure 16: The sketch of the coronal loop model suggested by Tsiklauri and Nakariakov (2001). A coronal loop is considered as a magnetic field line with density and gravitational acceleration varying along the axis of the cylinder.

profile along the loop as

$$\rho_0(s) = \rho_0(0) \exp \left[ -\frac{\frac{\gamma g(0)}{C_s^2} [X_0 h - Z_0(1-x)] \cos \alpha}{1 + \frac{R_L}{R_\odot} \left[ \frac{X_0}{R_L} h - \frac{Z_0}{R_L}(1-x) \right] \cos \alpha} \right]. \quad (54)$$

Assuming that the wavelength is much less than the scale height, the dissipation and the nonlinearity lengths, and applying the multi-scale expansion method, we obtain the evolutionary equation for weakly nonlinear, weakly dissipative slow magnetoacoustic waves in stratified coronal loops,

$$\frac{\partial V}{\partial s} - \frac{1}{2H(s)}V + \frac{\gamma+1}{2C_s}V \frac{\partial V}{\partial \xi} - \frac{1}{2\rho_0(s)C_s} \left[ \frac{4\eta_0}{3} + \frac{\kappa_{||}(\gamma-1)^2}{\mathcal{R}\gamma} \right] \frac{\partial^2 V}{\partial \xi^2} = 0, \quad (55)$$

where an effective scale height is introduced as  $H(s) = C_s^2/\gamma g(s)$ ,  $\kappa_{||}$  is the coefficient of thermal conduction, and  $\eta_0$  denotes the volume viscosity or thermal conductivity.

Similarly, in the radially stratified vertical polar plume, the evolutionary equation is

$$\frac{\partial \rho}{\partial R} + \left( \frac{1}{R} + \frac{g(R)}{2C_s^2} \right) \rho + \frac{1}{\rho_0} \rho \frac{\partial \rho}{\partial \xi} - \frac{2\eta}{3C_s \rho_0(R)} \frac{\partial^2 \rho}{\partial \xi^2} = 0, \quad (56)$$

where  $R$  is the radial (or vertical) coordinate (see Ofman *et al.*, 2000a, for details; both the viscosity and thermal conduction are included in the dissipative coefficient  $\eta$ ).

Solutions of Equation (52) are in a satisfactory agreement with the observed evolution of the wave amplitude: For example, Figure 17 demonstrates the comparison of the observed and theoretically predicted growth of the longitudinal wave amplitude with height. Also, full MHD 2D numerical modelling of these waves gives similar results (see Ofman *et al.*, 1999, 2000a). The comparison of the observed and modelled evolution scenarios give the possibility of estimating, in particular, the efficiency of non-adiabatic processes, such as the competition of heating and radiative losses.

The energy carried and deposited by the observed waves is certainly insufficient for heating of the loop. However, Tsiklauri and Nakariakov (2001) have shown that sufficiently broadband

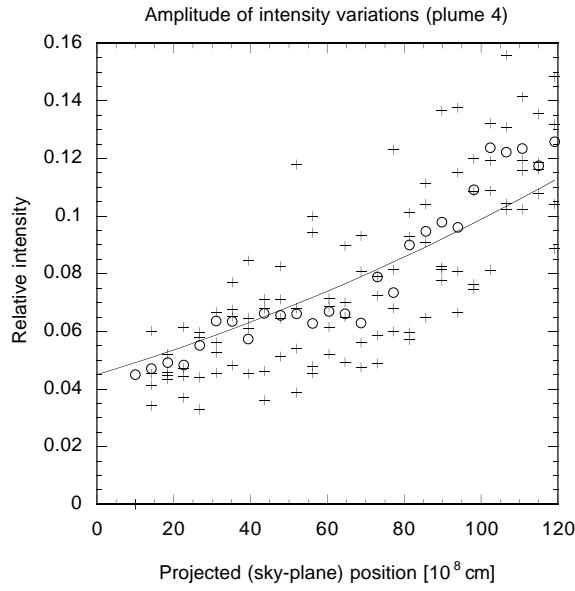


Figure 17: The comparison of the theoretically predicted (the continuous curve) and observed amplitudes of the upwardly propagating EUV disturbances observed in polar plumes (from Ofman *et al.*, 1999).

slow magnetoacoustic waves, consistent with currently available observations in the low frequency part of the spectrum, can provide the rate of heat deposition sufficient to heat the loop. In this scenario, the heat would be deposited near the loop footpoints which agrees with observationally determined positioning of the heat source.

### 6.3 Propagating slow waves as a tool for coronal seismology

According to the previous sections, slow magnetoacoustic waves follow magnetic field lines and propagate at the local sound speed. Because of the high coronal thermal conduction along the field, the equilibrium temperature does not experience significant changes in this direction, at least at the distances comparable with the detection distance of the slow waves. As the sound speed is proportional to the temperature squared, the propagation speed should be constant along the structure, and the speed measured observationally would contain information about the temperature and about the value of the adiabatic index  $\gamma$ . However, such a measurement is impossible at the moment, because the observations with the single line of sight provide us with the apparent speed only, which is affected by the projection effect. Possibly, future 3D observations of the propagating slow waves with STEREO will make such an estimation possible.

Another interesting possibility arises when the waves are observed simultaneously in different bandpasses which correspond to different temperatures of the emitting plasma. First such observation was done by Robbrecht *et al.* (2001) with SOHO/EIT 195 Å filter and TRACE 171 Å filter. It was found that wave propagating along the same coronal structure was detected in both bandpasses. The big difference in spatial resolution of EIT and TRACE imagers (2.5" vs 0.5") did not allow to study the correlation in detail. Later on, King *et al.* (2003) analysed slow waves observed in 171 Å and 195 Å with TRACE, confirming the correlation (see Figure 18). Figure 19 shows the evolution of the correlation coefficient of the perturbations observed in the different bandpasses with distance along the loop. There is a systematic decrease of the correlation coef-

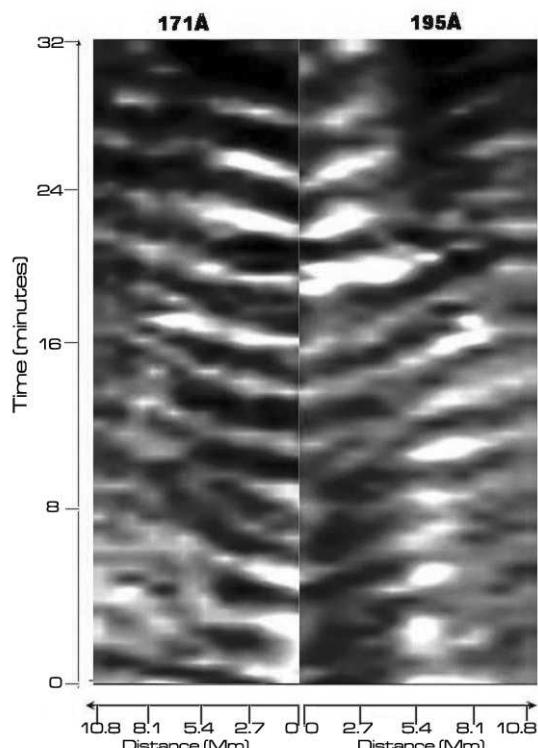


Figure 18: Simultaneous time-distance plots of propagating EUV disturbances observed by TRACE in the 171 Å and 195 Å bandpasses along a slit. The distance along the slit is shown in opposite directions to demonstrate that the disturbances observed in different bandpasses form a “fishbone” structure (from King *et al.*, 2003).

ficient which may be caused by the different propagating speed of the disturbances observed in different bandpasses. This may be interpreted as an indication to the sub-resolution structuring of the analysed active region: The observed loop can be either a bundle of magnetic threads of varying temperature, or have a transverse temperature profile. The further development of this study seems to be promising.

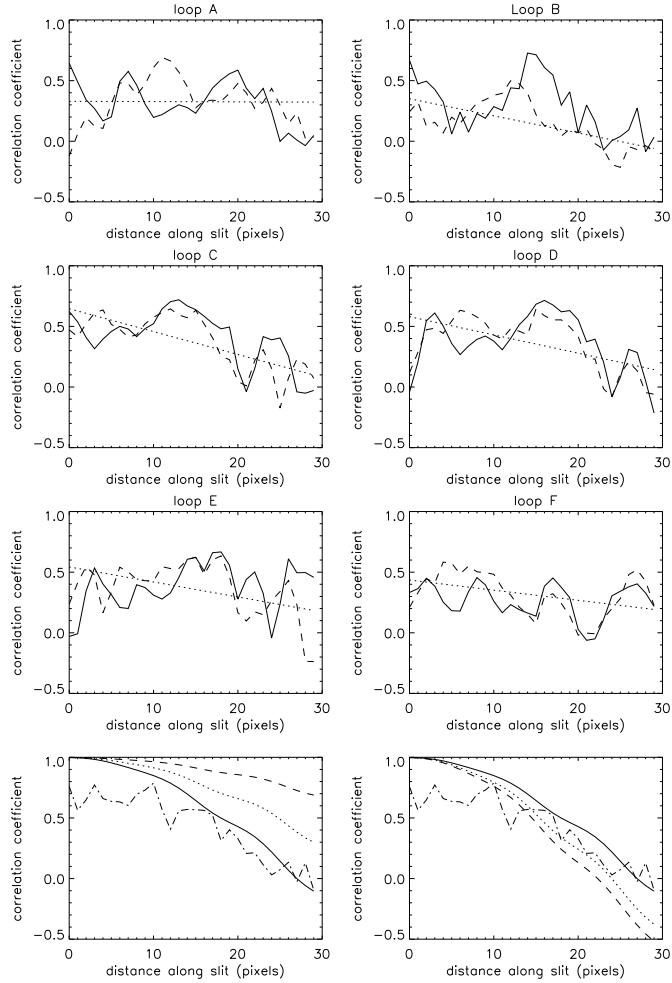


Figure 19: *Six upper panels* (loops A – F): Evolution of correlation coefficients of propagating disturbances observed simultaneously in 171 Å and 195 Å bandpasses with the distance along six different slits. The solid lines show the correlation of unfiltered data while the dashed lines show the correlation of the signals after subtraction of slower variation. The dotted lines are the best-fitted straight lines. *Two lower panels*: Evolution of correlation coefficients of simulated signals. The left panel shows the correlation for the same angle with the line of sight, but for different temperatures  $T_{171} = 1.05, 1.15$ , and  $1.2$  MK and  $T_{195} = 1.55, 1.55$ , and  $1.45$  MK for the solid, dotted and the dashed line, respectively. The right panel shows varying angle  $\theta_{171} = 15^\circ$  and  $\theta_{195} = 15^\circ, 14.5^\circ$ , and  $14^\circ$  for the solid, dotted and dashed lines, respectively, while keeping the temperature the same. The dash-dotted lines in both panels are the correlation of the simulated signals with amplitude noise added (from King *et al.*, 2003).

## 7 Propagating Fast Waves

### 7.1 Propagating fast waves in coronal loops

Wave lengths of propagating waves should be much shorter than the size of the structure guiding the wave. The shorter wave lengths correspond to shorter periods of the waves, requiring high cadence observational tools. In particular, the typical cadence time of TRACE and EIT EUV imagers is 20–30 s, which gives the minimal period of detected waves to be about 2–3 min. For a typical coronal Alfvén speed of about  $1000 \text{ km s}^{-1}$ , at least, this corresponds to wavelengths longer than 120–180 Mm, which is comparable with the typical size of a coronal loop. Thus, the EUV imagers cannot normally be used for the detection of propagating fast waves guided by coronal loops. On the other hand, time resolution of a second or better can be achieved with ground based coronographs or radioheliographs.

Recently, Williams *et al.* (2001, 2002) and Katsiyannis *et al.* (2003) reported the observational discovery of rapidly propagating compressible wave trains in coronal loops with the SECIS instrument during a full solar eclipse. As the observed speed was estimated at about  $2100 \text{ km s}^{-1}$ , these waves were interpreted as fast magnetoacoustic modes. The waves were observed to have a quasi-periodic pattern with a mean period of about 6 s. Cooper *et al.* (2003) found an encouraging agreement between the observed evolution of the wave amplitude along the loop with the theoretical prediction made for kink and sausage modes (see Figure 20). Unfortunately, the high uncertainty in the measurement of the amplitude does not allow the authors to distinguish between the kink and sausage modes in this observation.

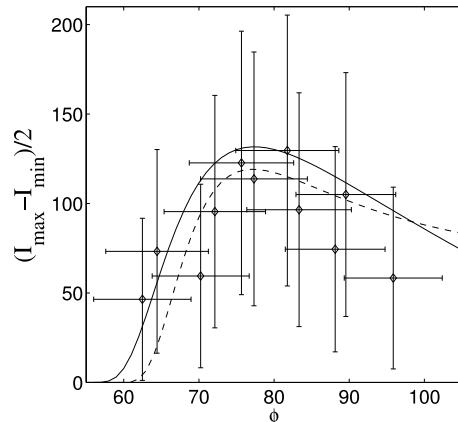


Figure 20: A plot of the maximum amplitude at the most frequent scale of the points, analysed by Williams *et al.* (2001), against their loop position. The  $x$  axis error bars are the uncertainty in position and the  $y$  axis error bars have been calculated statistically by taking the square root of the number of photons and normalising with respect to time. The figure also includes theoretically calculated dependences for kink (solid) and sausage (dashed) modes with the parameters (from Cooper *et al.*, 2003).

The main difference of these works from a number of previous papers analysing eclipse observations is the application of the methods of the time-distance (stroboscopic) plot (Williams *et al.*, 2001, 2002) and of the wavelet transform (Katsiyannis *et al.*, 2003). Those techniques are certainly more preferable in the situation when the waves have modulation or form wave trains. According to dispersion relation (7), fast waves are highly dispersive when their wave length is comparable or longer than the radius of the loop. It is well known that, in a dispersive medium, impulsively

generated (or broadband because of another reason) waves evolve into a quasi-periodic wave train with a pronounced period modulation. In the coronal context, it was pointed out by [Edwin and Roberts \(1983\)](#) and [Roberts \*et al.\* \(1983, 1984\)](#) that periodicity of fast magnetoacoustic modes in coronal loops is not necessarily connected with the wave source, but can be created by the dispersive evolution of an impulsively generated signal. Studying the dispersive evolution, [Roberts \*et al.\* \(1984\)](#) analytically predicted that the development of the propagating sausage pulse forms a characteristic quasi-periodic wave train with three distinct phases. Such evolution scenario is determined by the presence of minimum in the group speed dependence upon the wave number. That analysis was restricted to the case of the slab with sharp boundaries and to sausage modes only. The initial stage of the pulse evolution was numerically modelled by [Murawski and Roberts \(1993, 1994\)](#), [Murawski \*et al.\* \(1998\)](#), and was found to be consistent with the analytical prediction.

[Nakariakov and Roberts \(1995b\)](#) studied the case of a smooth density profile of a zero plasma- $\beta$  plasma,

$$\rho_0 = \rho_{\max} \operatorname{sech}^2 \left[ \left( \frac{x}{a} \right)^p \right] + \rho_{\infty}, \quad (57)$$

(cf. Equation (19) and Figure 8). The power index  $p$  determines the steepness of the profile. The cases when the power index  $p$  equals to either unity or infinity correspond to the symmetric Epstein profile or to the step function profile, respectively, both with known analytical solutions in the eigenvalue problem. The group speed has a minimum for all profiles with the power index greater than unity, which are steeper than the symmetric Epstein profile. Thus, the steepness of the profile affects the shape of the wave train and, consequently, the analysis of wave trains can give us information about this profile.

[Nakariakov \*et al.\* \(2004a\)](#) numerically simulated the developed stage of the dispersive evolution of a fast wave train in a smooth straight slab of a low plasma- $\beta$  plasma. It was found that development of an impulsively generated pulse leads to formation of a quasi-periodic wave train with the mean wavelength comparable with the slab width. In agreement with the analytical theory ([Roberts \*et al.\*, 1984](#)), the wave train has a pronounced period modulation which was demonstrated with the wavelet transform technique (see Figure 21). In particular, it is found that the dispersive evolution of fast wave trains leads to the appearance of characteristic “tadpole” wavelet signatures. Similar signatures were found in the wavelet analysis of SECIS data ([Katsiyannis \*et al.\*, 2003](#)), strengthening the interpretation of the SECIS waves as the fast magnetoacoustic wave trains.

This mechanism may also be responsible for the formation of quasi-periodic pulsations with the periods of about a second, observed in association with flares. However, the main property of this effect, which must be taken into account in interpretation, is the period modulation.

## 7.2 Propagating fast kink waves in open structures

Recently, [Verwichte \*et al.\* \(2005\)](#) presented for the first time a direct observational study of propagating fast waves in an open magnetic structure, i.e., observations of a long duration flaring event using TRACE 195 Å (a movie of this event can be seen in Resource 2). Because of the presence of an Fe XXIV emission line in the instrumental bandpass, which is sensitive to temperatures of around 20 MK, the hot supra-arcade above the post-flare loop arcade was also visible. The supra-arcade is an open magnetic structure containing plume-like rays. In the particular event analysed, dark, tadpole-like structures appeared in the lanes between the rays. They were density depletions that moved sunwards, decelerating from speeds above 500 km s<sup>-1</sup> to less than 100 km s<sup>-1</sup>. We shall adopt the name *tadpole* to describe such structures.

Tadpoles were first reported by [McKenzie and Hudson \(1999\)](#) using the Yohkoh Soft X-ray Telescope. Their physical nature is not fully understood and various models have been put forward. Here we shall focus on one particular behavioural feature of tadpoles, namely, after the passage of the tadpole head, the boundaries of the tail regions with the neighbouring rays oscillate transversely.

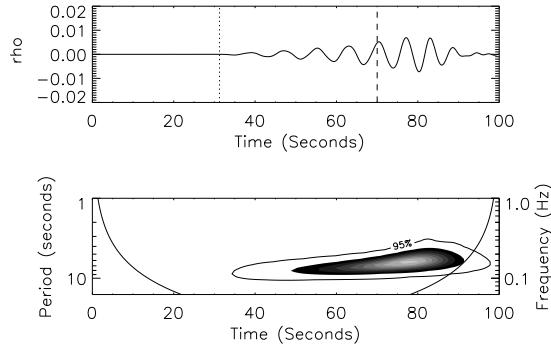


Figure 21: Numerical simulation of an impulsively generated fast magnetoacoustic wave train propagating along a coronal loop with a density contrast ratio of 5 and profile steepness power index equal to 8. *Upper panel:* The characteristic time signature of the wave train at  $z = 70a$ , where  $a$  is the loop semi-width, from the source point. The vertical lines show the pulse arrival time if the density was uniform, the dotted line using the external density, and the dashed line using the density at the centre of the structure. *Lower panel:* Wavelet transform analysis of the signal, demonstrating the characteristic ‘‘tadpole’’ wavelet signature (from Nakariakov *et al.*, 2004a).

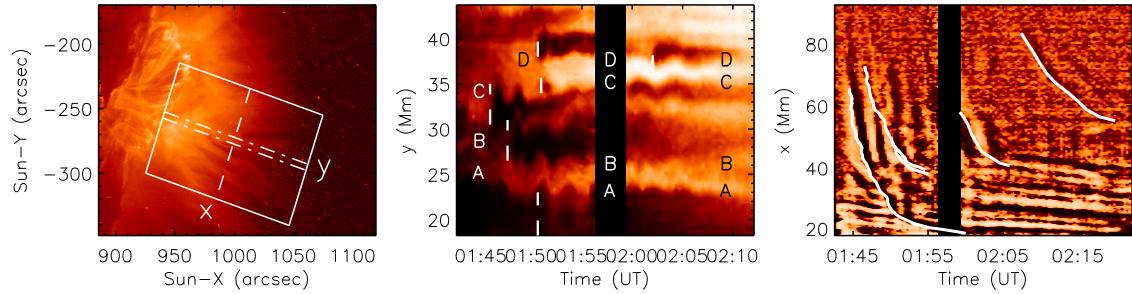


Figure 22: Left: TRACE 195 Å field of view on 21 April 2002 at 01:49:57 UT. The square gives the location of the subfield used in the data analysis. The subfield data cube has spatial coordinates  $x$  and  $y$ , which represent height and horizontal coordinates, respectively. Middle: Slice of the subfield data cube for fixed vertical coordinate  $x = 45.6$  Mm, as a function of  $t$  and  $y$  (dashed line in left panel). The oscillatory motions of the tadpoles are clearly visible. The tadpole heads are indicated with dashed lines. The tadpole edges analysed in Verwichte *et al.* (2005) are marked with letters. Right: Slice of the subfield data cube averaged over  $y = 32.8$ – $36.4$  Mm, as a function of  $t$  and  $x$  (between the dash-dotted lines in left panel). This range of  $y$  corresponds to the location of edge C (see middle panel). The solid lines indicate the location of tadpole heads (from Verwichte *et al.*, 2005).

In other words, one can say that the tadpole *wiggles* its tail. Figure 22 shows slices of the data set analysed by Verwichte *et al.* (2005). The transverse motions of the tadpole-ray boundaries are clearly visible as wave packets of 3–4 oscillation periods, following the tadpole heads. From this data cube the transverse displacement of four edges, which each may contain multiple tadpole events, have been extracted. Figure 23 illustrates the typical characteristics of these wave packets. A wave packet propagates sunwards, decelerating with phase speeds in the ranges  $200\text{--}700\text{ km s}^{-1}$  and  $90\text{--}200\text{ km s}^{-1}$  at heights above the post-flare loop footpoints of 90 and 60 Mm, respectively. Simultaneously, the displacement amplitude, which is of the order of several Mm, decreases. The nature of this decrease is not obvious. Besides dissipation, vertical structuring of the supra-arcade may be responsible. The wave periods lie in the range of 90–220 s. The equivalent wavelengths are of the order of 20–40 Mm, which is much shorter than for the standing, fast kink oscillations in coronal loops.

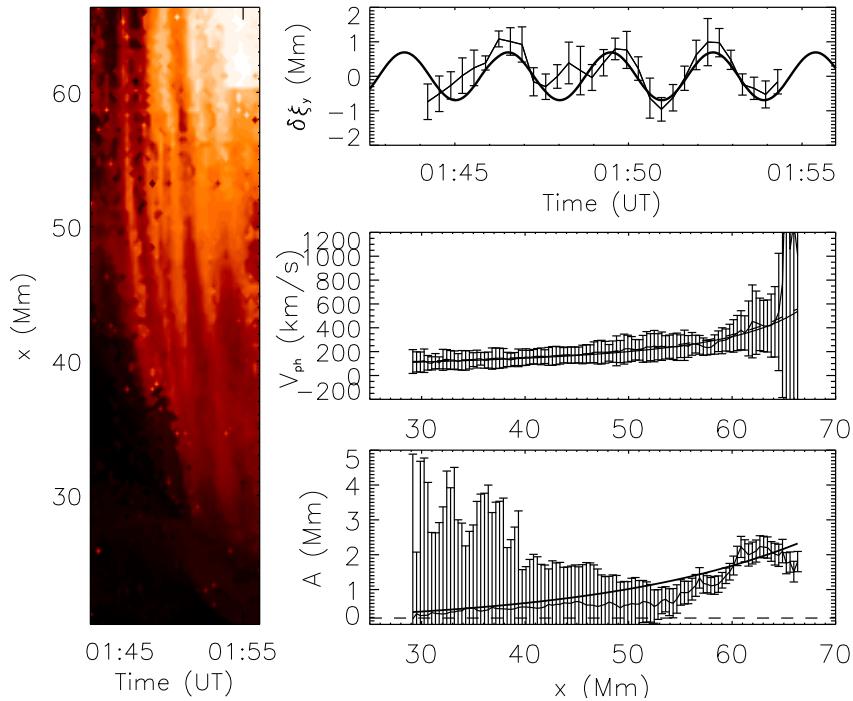


Figure 23: Characterisation of the transverse displacement of a wave packet in edge B (see middle panel in Figure 22). Left: Transverse displacement as a function of  $t$  and height  $x$ . The wave packet is visible as quasi-periodic sets of ridges. Right-top: Relative displacement  $\delta\xi_y$  as a function of time for  $x = 45.3\text{ Mm}$ . The thick line is a fitted cosine function. Right-middle: Phase speed  $V_{\text{ph}}$  as a function of height  $x$ . The thick, solid line is an inverse linear fit. Right-bottom: Displacement amplitude  $A$  as a function of height  $x$ . The thick, solid line is a fitted exponential curve and the dashed line represents the minimum amplitude that can be resolved (from Verwichte *et al.*, 2005).

Because of their clear transverse signatures, the tadpole waves are interpreted as fast magnetoacoustic kink waves. They are guided by the vertical, ray-tadpole structure. An MHD model with slab geometry may be used to characterise the structure (Roberts, 1981b). A slab is preferred over a cylindrical model because little is known about the extent of the structure along the line of sight. Because the density is lower in the tadpole than in the ray, the observed waves may be

surface modes. Fast surface modes have a phase speed below the minimal Alfvén speed, i.e., the ray Alfvén speed. If we assume that this speed lies plausibly in the range of  $500\text{--}1000\text{ km s}^{-1}$ , then there is quite a difference with the observed phase speeds, especially at lower heights. This discrepancy may be explained by considering the geometric configuration of the angles between wave propagation, tadpole and ray magnetic field directions and/or by the presence of upflows, possibly connected with the strong Doppler blue shifts reported by SUMER (Innes *et al.*, 2003). In the last case, these waves may be generated by negative energy mechanisms (see, e.g., Ruderman *et al.*, 1996; Joarder *et al.*, 1997), which lead to amplification of waves by nonuniform steady flows.

The period (phase speed) of consecutive tadpole wave packets passing the same neighbouring ray show a linear increase (decrease) with time. This trend can be explained by a density increase in the ray. Using the simple assumptions  $I - I_0 \sim n_e^2 \sim V_{A,\text{ray}}^{-4}$  and  $V_{\text{ph}} \sim V_{A,\text{ray}}$ , where  $V_{A,\text{ray}}$  is the Alfvén speed in the ray, we find the relations  $I - I_0 \sim P^4$  and  $I - I_0 \sim V_{\text{ph}}^{-4}$ .  $I_0$  is an arbitrarily chosen constant background intensity. A fit to the observed intensity profile yields the dependencies  $I - I_0 \sim P^{2.8 \pm 2.0}$  and  $I - I_0 \sim V_{\text{ph}}^{-3.0 \pm 1.5}$ . The difference with the theoretical power law indices lies within the error. Theoretical modelling of excitation and propagation of kink waves in supra-arcades has not been fulfilled.

## 8 Torsional Modes

Alfvén waves, e.g., as torsional modes of coronal loops (described by the first factor in Equation (6)) are incompressible and, therefore, do not perturb the density and, hence, do not modify the loop emission. In this section we restrict our attention to torsional modes of untwisted magnetic structures. If the loop is twisted, torsional modes are compressible (see Section 2.4 for details). The velocity perturbations of Alfvén waves, though, can be observed through variations of the Doppler shift. Whilst long period waves may show resolved Doppler shifts, short period waves, with periods less than a few minutes, can be observed only indirectly by measuring the additional broadening of coronal emission lines, i.e., non-thermal broadening. An effective temperature  $T_{\text{eff}}$ , associated with a coronal optically thin emission line, can be defined that combined the effects of thermal and non-thermal broadening (McClements *et al.*, 1991):

$$T_{\text{eff}} = T_i + \mathcal{C} \frac{m_i}{2k_B} \langle V_{\text{LOS}}^2 \rangle, \quad (58)$$

where  $T_i$  and  $m_i$  are the temperature and mass of the line forming ion, respectively,  $k_B$  is the Boltzmann constant, and  $V_{\text{LOS}}$  is the velocity in the line of sight. The constant  $\mathcal{C}$  is defined by polarisation and other effects, and its value lies in the interval  $2/3 < \mathcal{C} < 1$ .

There have been several attempts to study the evolution of the amplitude of non-thermal broadening along possible wave paths. Banerjee *et al.* (1998) and Doyle *et al.* (1999), using SOHO/SUMER, measured the evolution of non-thermal broadening of the emission lines Si VIII and O VI in inter-plume regions of polar coronal holes and found that the amplitude of unresolved thermal broadening (possibly, the Alfvén wave amplitude) is growing up to  $1.2 R_\odot$ , then has a plateau to  $1.5 R_\odot$ , and then grows sharply again. The authors suggested that this phenomenon could be associated with nonlinear overturning of the waves, but a rigorous theoretical modelling is still required. Harrison *et al.* (2002) examined the width of Mg X emission line and found out the emission line narrowing as a function of altitude. This result was interpreted as further evidence for coronal wave activity in closed field regions, and most likely the first evidence of the dissipation of Alfvén waves in the corona. A similar conclusion was reached by O’Shea *et al.* (2003) by the analysis of the same emission line in polar plumes and inter-plume lanes. However, the analysis of the widths and its height variation of the Mg X doublet lines, in both the quiet equatorial corona and in a polar hole performed by Wilhelm *et al.* (2004), gave the opposite result: The Doppler width broadened with height in both the equatorial plane and in a polar coronal hole.

An indirect evidence for the presence of unresolved Alfvén waves in the corona was obtained by Erdélyi *et al.* (1998), who found out that quiet sun line widths increase from the disk centre outwards in SUMER data. This anisotropy of the non-thermal broadening could be caused by transverse waves; however, some other physical processes such as anisotropic turbulence could produce this effect too.

Alfvén waves with sufficiently long wave lengths can be observed directly through the spatial variation of the Doppler shift. Zaqrashvili (2003) suggested that the global torsional oscillations may be observed as a periodical variation of the spectral line width along the loop, as the loop footpoints are likely to provide the waves with rigid wall boundary conditions. The amplitude of the variation must be maximal at the velocity antinodes and minimal at the nodes of the torsional oscillation. The resonant period of a standing torsional mode of  $n$ -th order is given by the expression

$$P = 2L/nC_{A0}. \quad (59)$$

For example, for  $L = 200$  Mm and  $C_{A0} = 1$  Mm s<sup>-1</sup>, there can be several standing torsional modes with periods and wave lengths resolvable with modern coronal spectrometers. Such observational detection can be obtained in the raster mode, as usual 1D slit spectral observations do not give the required spatial information.

Another possibility to observe torsional modes is connected with the gyrosynchrotron emission, which can be detected in the radio band. As the observed emission depends strongly upon the angle  $\zeta$  between the magnetic field and the LOS, torsional waves changing the local direction of the field can modulate the observed emission. According to the simple estimations made by Tapping (1983) with the use of Equation (29), in the presence of torsional perturbations a substantial fraction of the emission can be observed from the axial direction, e.g., when the perturbed segment of loop is viewed end-on.

## 9 Conclusions

Recently achieved spatial and temporal resolution performance of coronal telescopes and spectral instruments, space-borne as well as ground-based, makes possible *systematic* observational investigations of various waves and oscillations in the corona. The theory of interaction of MHD modes with plasma structures, in particular, of the MHD modes of a magnetic cylinder, developed in early eighties, provides the theoretical basis for interpretation of the phenomena. Observationally determined properties of MHD modes of solar coronal structures, such as active region loops, polar plumes, and other open structures, showed an excellent agreement with the theory. The combination of the observationally gained knowledge with MHD wave theory and direct numerical simulations of the phenomena, gives rise to a new method of investigation of coronal plasmas, the MHD seismology of the corona. This makes the investigation of coronal MHD waves and oscillations to be an interesting, rapidly developing, and promising branch of solar physics.

Some important topics, such as the coronal Moreton or EIT wave, oscillations in coronal bright points, sub-second radio pulsations, nonlinear effects, and other, remained out of the scope of the present version of this review, and will be covered in the next edition.

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## Resources

**Resource 1:** Movies visualising the structure of the MHD modes in a magnetic cylinder.

<http://solarphysics.livingreviews.org/Articles/lrsp-2005-3/resources/cylindermodes/index.html>

**Resource 2:** Movie of observations of a long duration flaring event using TRACE 195 Å.

<http://solarphysics.livingreviews.org/Articles/lrsp-2005-3/resources/tadpolemovie/index.html>

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