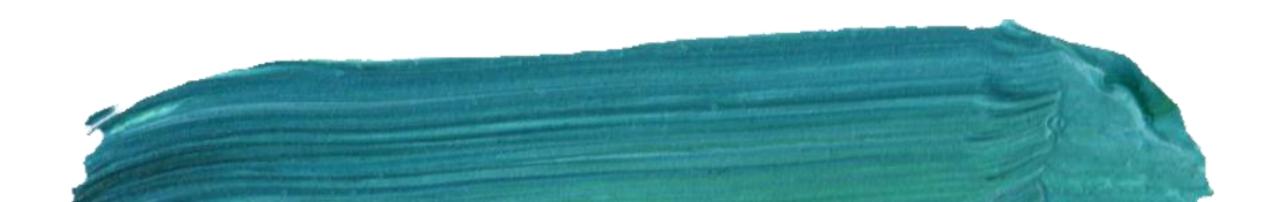
## DATA MINING ASSOCIATION ANALYSIS: BASIC CONCEPTS AND ALGORITHMS







#### WHY KNOW THESE ASSOCIATIONS?

If there is a pair of items, X and Y, that are frequently bought together:

- ✓ Both X and Y can be placed on the same shelf, so that buyers of one item would be prompted to buy the other.
- ✓ Promotional discounts could be applied to just one out of the two items.
- ✓ Advertisements on X could be targeted at buyers who purchase Y.
- ✓ X and Y could be combined into a new product, such as having Y in flavors of X.

#### **ASSOCIATION RULE LOOKS LIKE**



**Antecedent** 

Consequent

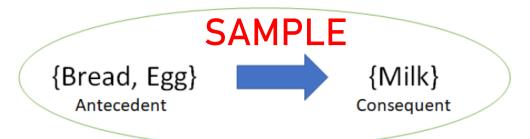
Note that implication here is co-occurrence and not causality

#### **ASSOCIATION RULE LOOKS LIKE**



**Antecedent** 

Consequent



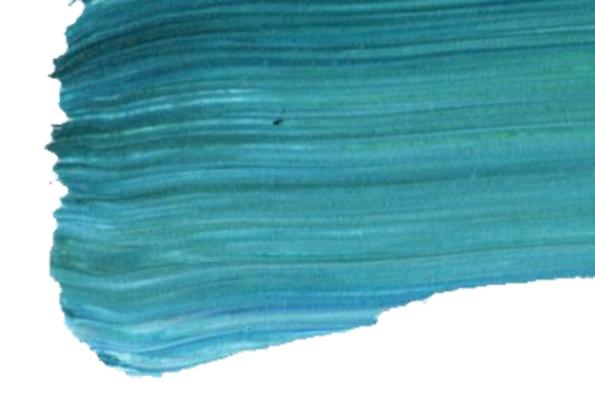
Itemset = {Bread, Egg, Milk}



#### **ITEMSET**

A collection of one or more items Example: {Bread,Egg,Milk}

k-itemset
An itemset that contains k
items



Ex. {X,Y} is a representation of the list of all items which form the association rule



#### **SUPPORT**

Mathematically, support is the fraction of the total number of transactions in which the itemset occurs.

$$Support(\{X\} \rightarrow \{Y\}) = \frac{Transactions\ containing\ both\ X\ and\ Y}{Total\ number\ of\ transactions}$$

#### Example:

For itemsets which occur at least 100 times out of a total of 10,000 transactions What is the support?



#### **SUPPORT**

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If an itemset happens to have a very low support, we do not have enough information on the relationship between its items and hence no conclusions can be drawn from such a rule.



#### SUPPORT

This measure gives an idea of how frequent an itemset is in all the transactions.

```
Which has the higher support?

itemset1 = {bread} itemset2 = {shampoo}

itemset1 = {bread, butter}

itemset2 = {bread, shampoo}
```

Value of support helps us identify the rules worth considering for further analysis.



This measure defines the likeliness of occurrence of consequent on the cart given that the cart already has the antecedents.

#### Example:

That is to answer the question — of all the transactions containing say, {Conditioner}, how many also had {Shampoo} on them?



This measure defines the likeliness of occurrence of consequent on the cart given that the cart already has the antecedents.

$$Confidence(\{X\} \rightarrow \{Y\}) = \frac{Transactions\ containing\ both\ X\ and\ Y}{Transactions\ containing\ X}$$

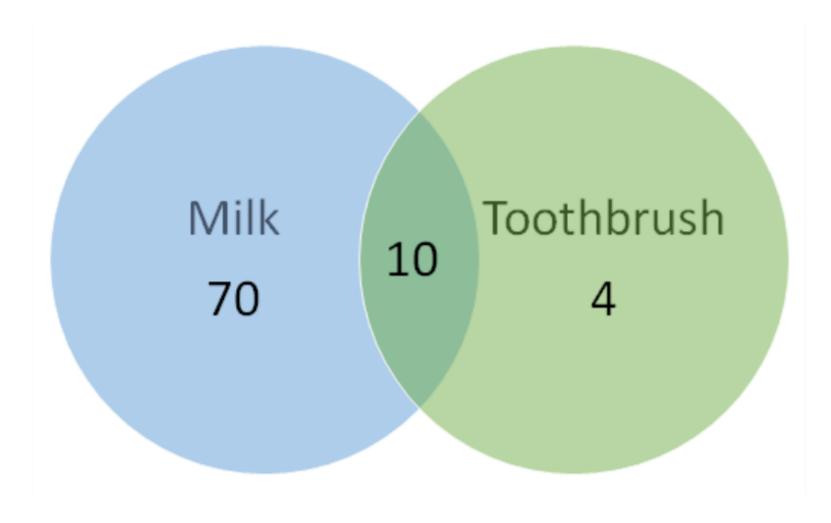
Technically, confidence is the conditional probability of occurrence of consequent given the antecedent.

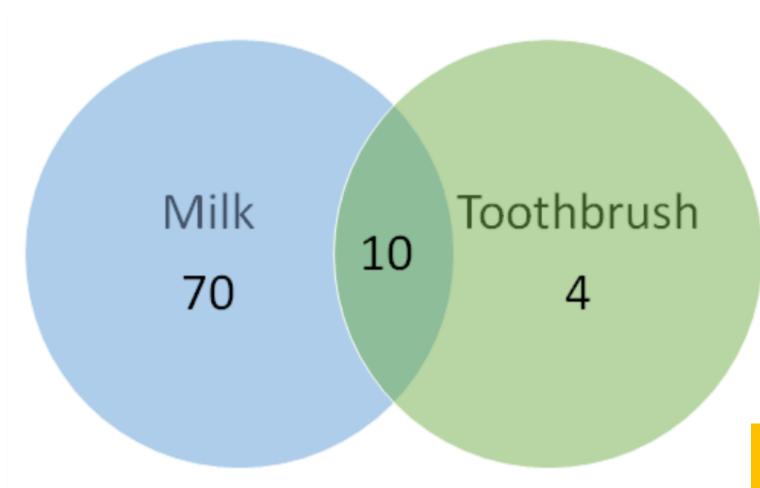


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$$Confidence(\{X\} \rightarrow \{Y\}) = \frac{Transactions\ containing\ both\ X\ and\ Y}{Transactions\ containing\ X}$$

Technically, confidence is the conditional probability of occurrence of consequent given the antecedent.





Confidence for {Toothbrush} → {Milk}?

> 10/(10+4)= 0.7

Oops! Looks like a high confidence value.

But we know intuitively that these two products have a weak association.

#### BUT

Considering just the value of confidence limits our capability to make any business inference.

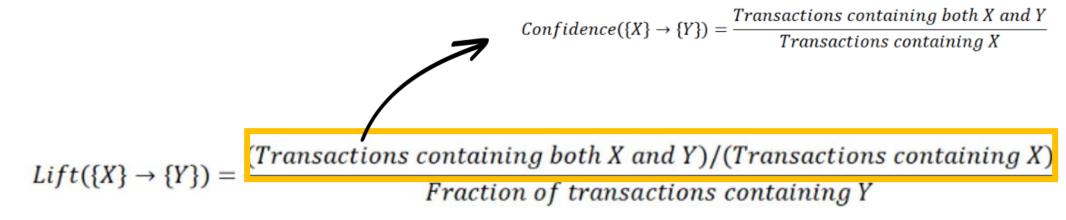


#### **SUPPORT**

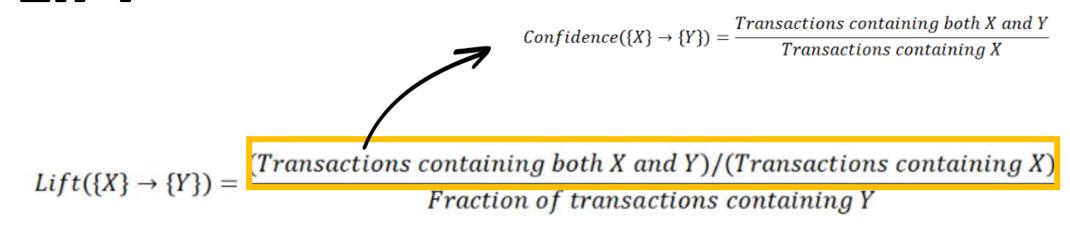
Mathematically, support is the fraction of the total number of transactions in which the itemset occurs.

Lift controls for the support (frequency) of consequent while calculating the conditional probability of occurrence of {Y} given {X}.

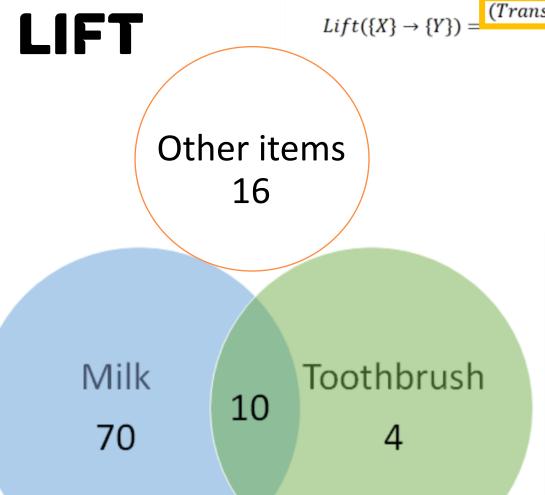
LIFT is the rise in probability of having {Y} on the cart with the knowledge of {X} being present over the probability of having {Y} on the cart without any knowledge about presence of {X}



LIFT is the rise in probability of having {Y} on the cart with the knowledge of {X} being present over the probability of having {Y} on the cart without any knowledge about presence of {X}



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(Transactions containing both X and Y)/(Transactions containing X)

Fraction of transactions containing Y

#### $\{\mathsf{Toothbrush}\} o \{\mathsf{Milk}\}$

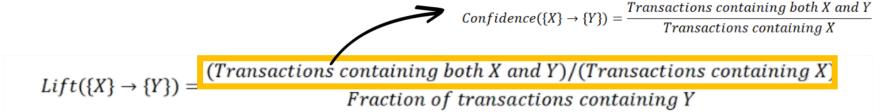
Probability of having milk on the cart with the knowledge that toothbrush is present Confidence: 10/(10+4) = 0.7

Probability of having milk on the cart without any knowledge about toothbrush

80/100 = 0.8

These numbers show that having toothbrush on the cart actually reduces the probability of having milk on the cart from 0.8 to 0.7



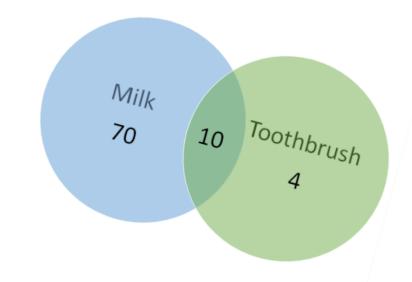


#### $\{\mathsf{Toothbrush}\} o \{\mathsf{Milk}\}$

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#### $\{\mathsf{Toothbrush}\} o \{\mathsf{Milk}\}$

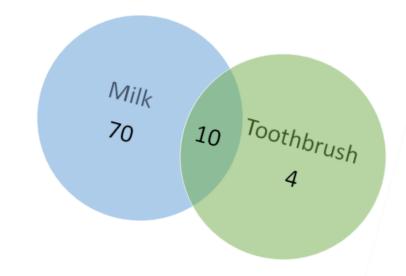
$$\begin{array}{c} 0.7 \\ \hline 0.87 \\ \hline 0.8 \end{array}$$

A value of lift less than 1 shows that having toothbrush on the cart does not increase the chances of occurrence of milk on the cart in spite of the rule showing a high confidence value.

A value of lift greater than 1 vouches for high association between {Y} and {X}. More the value of lift, greater are the chances of preference to buy {Y} if the customer has already bought {X}.







#### $\{Toothbrush\} \rightarrow \{Milk\}$

Lift is the measure that will help store managers to decide product placements on aisle.

A value of lift less than 1 shows that having toothbrush on the cart does not increase the chances of occurrence of milk on the cart in spite of the rule showing a high confidence value.

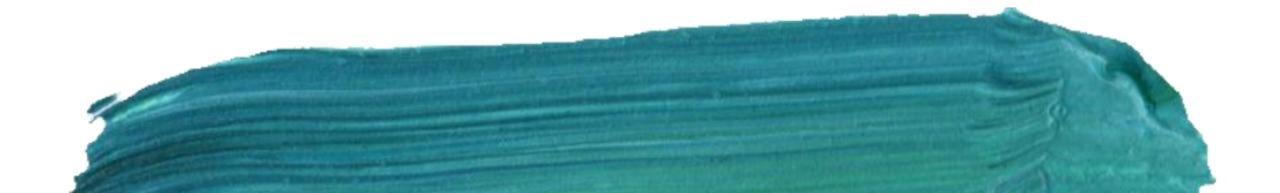
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#### **ASSOCIATION RULE MINING**

We now understand how to quantify the importance of association of products within an itemset

The next step is to

- (1) generate rules from the entire list of items and
  - (2) identify the most important ones



# First step in generation of association rules is to get all the frequent itemsets on which binary partitions can be performed to get the antecedent and the consequent.

#### **ASSOCIATION RULE MINING**

The next step is to

(1) generate rules from the entire list of items

(2) identify the most important ones

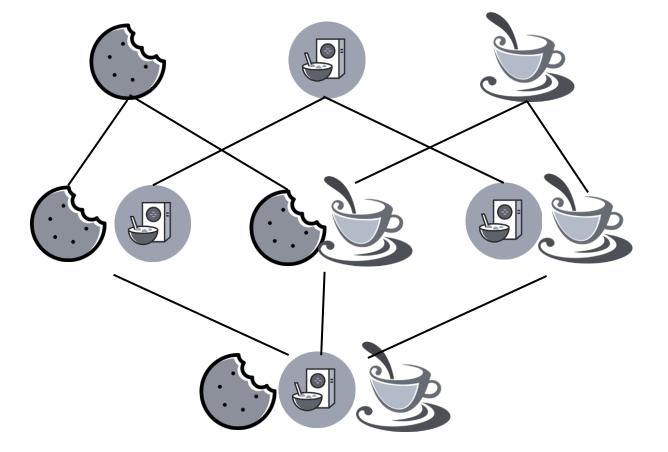
For example, if there are 3 items on all transactions

{Biscuit, Cornflakes, Coffee}

How many itemsets can be generated?

## HOW MANY ITEMSETS CAN BE GENERATED?

**Biscuit Cornflakes Coffee** 



#### **ASSOCIATION RULE MINING**

The next step is to

(1) generate rules from the entire list of items

(2) identify the most important ones

For example, if there are 3 items on all transactions

{Biscuit, Cornflakes, Coffee}

1 {Biscuit}

2 {Cornflakes}

3 {Coffee}

4 {Biscuit, Cornflakes}

5 {Biscuit, Coffee}

6 {Cornflakes, Coffee}

7 {Biscuit, Cornflakes, Coffee}

#### **ASSOCIATION RULE MINING**

The next step is to

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For example, if there are 3 items on all transactions

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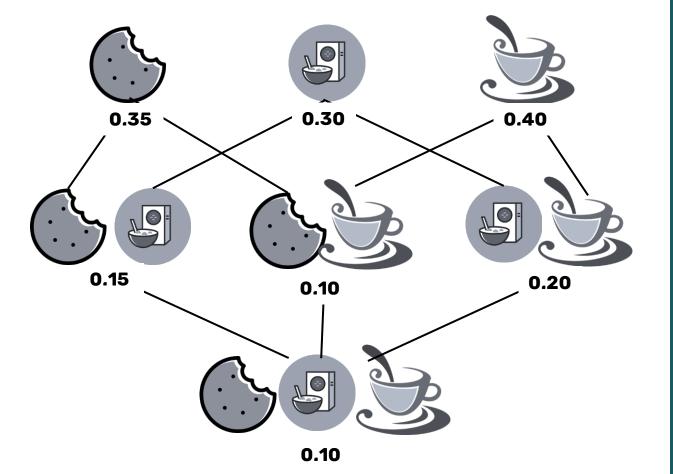
- 1 {Biscuit}
- 2 {Cornflakes}
- 3 {Coffee}
- 4 {Biscuit, Cornflakes}
- 5 {Biscuit, Coffee}
- 6 {Cornflakes, Coffee}
- 7 {Biscuit, Cornflakes, Coffee}





## HOW MANY ITEMSETS CAN BE GENERATED?

**Biscuit Cornflakes Coffee** 



#### **ASSOCIATION RULE MINING**

The next step is to

(1) generate rules from the entire list of items

(2) identify the most important ones

### This what happens if we use **BRUTE FORCE**

Every itemset will be generated

<b>\$</b>	support \$	itemsets <b>≑</b>
0	0.35	(BISCUIT)
1	0.30	(CORNFLAKES)
2	0.40	(COFFEE)
3	0.15	(BISCUIT, CORNFLAKES)
4	0.10	(COFFEE, BISCUIT)
5	0.20	(COFFEE, CORNFLAKES)
6	0.10	(COFFEE, BISCUIT, CORNFLAKES)

#### **APRIORI PRINCIPLES**

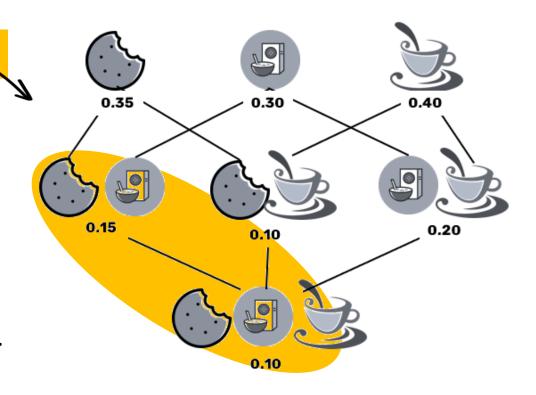
All subsets of a frequent itemset must also be frequent.

#### Remember this?

As you can see as you move up, each subset has greater than or equal support compared to the super set.

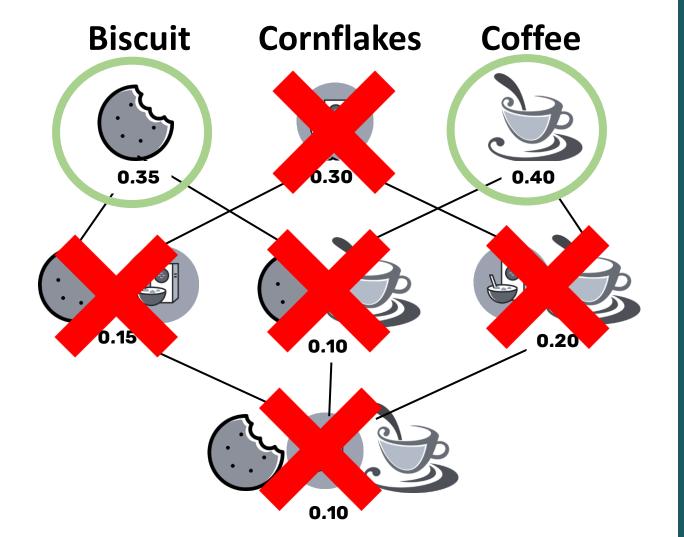
#### **Example:**

Support of {Biscuit, Cornflakes} >
Support of {Biscuit, Cornflakes, Coffee}





## HOW MANY ITEMSETS ARE FREQUENT?



#### **ASSOCIATION RULE MINING**

The next step is to

(1) generate rules from the entire list of items

(2) identify the most important ones

Given minimum support (minsup) of 0.33

#### **USING BRUTE FORCE**

- Brute force algorithm
   will first generate the list
   of all itemsets and
   compute their support
- 2. It will scan the whole database to check which itemsets have greater support than the minsup



## HOW MANY ITEMSETS ARE FREQUENT?

Biscuit Cornflakes Coffee

0.35

0.40

Coffee

GIVEN NO MORE TO TEST FOR MINSUP, THE ALGORITHM STOPS AND REPORTS THE IDENTIFIED FREQUENT ITEMSETS

#### **ASSOCIATION RULE MINING**

The next step is to

(1) generate rules from the entire list of items

(2) identify the most important ones

Given minimum support (minsup) of 0.33

#### **USING APRIORI**

- 1. Take each basic itemset
- 2. Compute support
- 3. Evaluate if greater than minsup, if yes then continue, if not don't consider the itemset as frequent
- 4. Go the identified frequent, go to the next level itemset and go back to step (2)