# Data Science Project - Word Embedding

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# Introduction

For many years, Artificial Intelligence have tried to get a mathematical representation of words in order to derive various applications and analyses such as machine translations amongst others. In the context of NLP (Natural Language Processing), we call the vector representation of words: Word Embedding. This revolutionary technique maps words into arrays, thus creating a high-dimensional vector space of words. Monolingual embedding encapsulates semantic relationships between word arguments and this information can later on support bilingual translation through the learning of a transformation matrix that we will call W. This matrix allows the matching of two monolingual cor-

In this paper, we are going to present the Word Embedding technique, the derivation of the translation matrix W and its applications. We will focus on the following languages: english, french, spanish. We will also investigate the influence of different alphabet languages such as russian and hebrew in order to check the effect on our translation model.

pus and thus, the alignment of word pairs, based on closest similarity criteria through their embedding.

Furthermore, we will expand a methodology for unsupervised learning by trying to assess high candidates for translation when we don't have parallel data (i.e, already translated data).

# 1 Word embedding

Statistical machine translation mainly relies on bilingual mappings created out of parallel corpus. In the scope of this project, we will work on already created high-quality labeled data. But without any loss of generality, this computation is costly as the size of bilingual word pairs might be quite consequent. One algorithm that enables this embedding is word2vec that is described in the next paragraph.

#### 1.1 Word2vec

#### Abstract

The Word2vec algorithm was created by Tomas Mikolov in 20213, in order to give a possible solution to Word Embedding. This unsupervised learning algorithm produces a high-dimensional vector space representation of words through the use of neural networks.

The idea relies on the fact that words that occur in the same context tend to have similar meanings and so similar embedding, and this is specifically what the neural network is trained for. In other words, two words semantically close will have similar vector representations. This allows us to analyze links and relations between words and observe their semantic similarities.

Note that simple vector algebra (distance, direction, norm) enable us to perceive both

- syntactic matches such as singular/plural, present/past, adjectives/superlatives relations. Let's observe the following example: where the words dog,dogs and car,cars are visually represented in the following figure: we can observe that the two word pairs have same direction and distance (see Fig.1)
- semantic matches (eg. countries/capitals, family...) eg: 'king' 'man' + 'women' = 'queen'. Let's check this from the 2D representation (Fig.2). We can see that the representation of king-man+women which corresponds to queen, has the same relation (distance-wise, direction-wise) to king as women has to man.

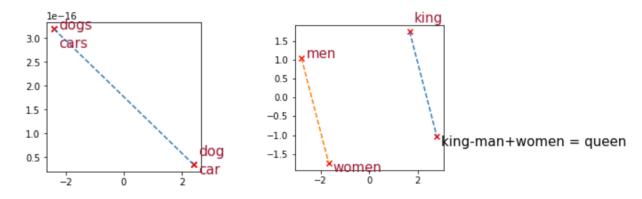


Figure 1: Syntactic visualization relation Figure 2: Semantic visualization relation: singular/plural 'king' - 'man' + 'women' = 'queen'

#### Implementation

The word2vec approach focuses on displaying multiple degrees of similarity both along syntactic and semantic dimensions through a two-layer neural networks which goal is to reduce the loss function by adjusting its weights. However, unlike traditional networks, word2vec is not going to be used on the task it was trained on, but the hidden weights will represent the word embedding and the rest of the model will be tossed.

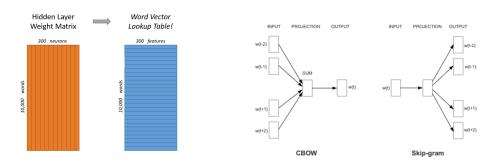


Figure 3: from neural networks to word Figure 4: CBOW vs Skip-Gram model embedding

Let's analyze its implementation: The input of the network corresponds to a monolingual corpus and produces out of it a vector space of the embedded words (high-dimensional). This method can be decomposed in two models (algorithmically equivalent): Continuous Bag-of-Words (CBOW) model and the Skip-Gram model.

The CBOW method predicts target words from the surrounding context word by treating an entire context as one observation, it is easily usable on small data sets. Whereas the Skip-gram predicts surrounding context words from the target words by treating each context-target pair as a new observation (efficient on large data sets).

#### Architecture

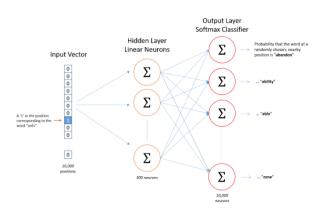
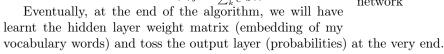


Figure 5: Word2Vec neural network architecture

As you can see on the figure, the network takes as its input a large vector (one-hot vector, filled with zeros except at the index that represents the word to be embedded). It is passed through the hidden layer whose weights are the word embedding and the output layer outputs the probabilities for this word in the whole vocabulary (i.e, the ith output represents the probability that this word is picked if we randomly pick a word near word input j thanks to the softmax activation function  $\sigma(z)_j = \frac{e^{z_j}}{\sum_k e^{z_k}}$ ).



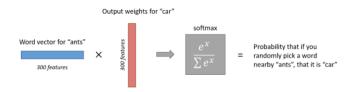


Figure 6: high level view of the neural network

## 1.2 Translation Algorithm

By observing corpus of words, we can observe a surprising fact which is that they have the same shape ! This means that simple linear transformations (rotation, scaling) might enable us to go from one monolingual corpus to another !

By doing so, we should be able to easily obtain translations between languages.

#### 1.2.1 Theory

We based our approach on a simple fact: one can learn a linear transformation matrix from a bilingual dictionary to overlay two monolingual corpus and translate one word in a language to its corresponding translation in another language.

#### Unconstrained translation matrix

Indeed, let  $x_i$  be the word vector of the i-th word in the source language (monolingual dictionary) and  $z_i$  the word vector in the target language, we would like to find a projection matrix W that satisfies the following relation:

$$W = \underset{W \in \mathbb{R}^{p \times p}}{\operatorname{argmin}} \sum_{i} ||Wx_i - z_i||^2 \tag{1}$$

We first choose the  $L_2$  norm and solve this problem with gradient descent. We define the loss function  $f_i: W \to ||Wx_i - z_i||_2^2$  whose gradient is given by  $\nabla f_i: W \to 2(Wx_i - z_i)x_i^T$ .

Thus, we obtain W as presented in the following algorithm

## Algorithm 1 Calculate W without constraints

```
Require: X = (x_1, \dots, x_n)^T, Y = (y_1, \dots, y_n)^T, \alpha \in \mathbb{R}
Initialize W with random values
for i \leq n do
W \leftarrow W - \alpha 2(Wx_i - y_i)x_i^T
end for
return W
```

#### Orthogonal translation matrix (Constrained version)

An alternative method could be to use the cosine similarity (2) as a distance between  $Wx_i$  and  $z_i$ .

$$\cos(Wx_i, z_i) = \frac{\langle Wx_i, z_i \rangle}{||Wx_i|| \cdot ||z_i||} \tag{2}$$

If both  $(Wx_i)$  and  $(z_i)$  are normalized, then the former relation (1) is equivalent to:

$$W = \underset{W \in \mathbb{R}^{p \times p}}{\operatorname{argmax}} \sum_{i} (Wx_i)^T z_i \tag{3}$$

We will note that  $(Wx_i)$  and  $(y_i)$  are normalized as long as  $(x_i)$  and  $(y_i)$  are normalized and W is orthogonal.

To find the matrix W that satisfies (3), we first perform gradient descent with the following update rule

$$W_{k+1} = W_k + \alpha \Delta w_k \quad \text{where } \Delta w_k = x_k z_k^T$$
 (4)

Then, we make sure that W is orthogonal by changing it's singular values to 1, i.e.

if 
$$SVD(W) = U\Sigma V^T$$
, we take  $\tilde{W} = UV^T$ 

Since  $\Delta w$  does not depend on W, if  $\alpha$  is large enough (i.e. the coefficients of  $\alpha \Delta w$  are larger than the ones of  $W_0$ ), the final value of W will not depends on the learning rate.

Indeed, let  $\alpha$  and  $\alpha'$  be large enough. With the update-rule (4), we have

$$W_{\alpha} = W_0 + \alpha \sum_{i} x_i z_i^T \approx \alpha \sum_{i} x_i z_i^T$$
 and  $W_{\alpha'} \approx \alpha \sum_{i} x_i z_i^T$  (5)

If we define  $S = \sum_{i} x_i z_i^T$ , then we have

$$SVD(\alpha S) = \alpha U \Sigma V^T = U \alpha \Sigma V^T = U \Sigma_{\alpha} V^T \qquad \Sigma_{\alpha} = \alpha \Sigma$$
 (6)

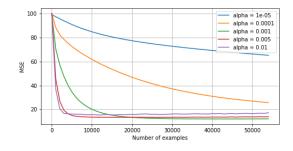
Since we obtain the orthogonal version of  $W_{\alpha}$  and  $W_{\alpha'}$  by replacing  $\Sigma_{\alpha}$  by  $I_d$ , we have  $\tilde{W}_{\alpha} = \tilde{W}_{\alpha'}$ . The procedure to obtain  $\tilde{W}$  is summarize in the following algorithm

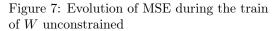
## **Algorithm 2** Calculate $\tilde{W}$ orthogonal

Require:  $X = (x_1, \dots, x_n)^T, Y = (y_1, \dots, y_n)^T, \alpha \in \mathbb{R}$ Initialize W with random values for  $\mathbf{i} \leq \mathbf{n}$  do  $W \leftarrow W + \alpha x_i y_i^T$ end for Perform SVD on W such that  $W = U \Sigma V^T$   $\tilde{W} \leftarrow U V^T$ return  $\tilde{W}$ 

# 1.2.2 Experimental tests: Constrained vs Unconstrained translation matrix implementation

#### Unconstrained vs constrained





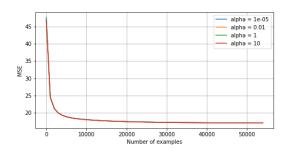


Figure 8: Evolution of MSE during the train of W normalized /constrained

For the unconstrained case, we find that  $\alpha = 10^{-3}$  seems to be a good choice. Whereas for the case in which the translation matrix is normalized, it appears that as long as the learning rate is high enough, we get good accuracy ( $\alpha > 10$ ).

word in french	est	dans	avec	cette	naissance	décès
unconstrained	which	the	with	however	born	buried
constrained	was	in	with	this	birth	death

Figure 9: Examples of translation with both methods

	MSE	Accuracy
unconstrained	10.63	45.0
constrained	13.97	55.6

Figure 10: MSE and Accuracy between both methods

To verify the efficiency of the constrained method, we compare the results obtained with both methods in terms of MSE and accuracy on 500 words.

Even if the MSE seems to be lower with the unconstrained method, forcing W to be orthogonal slightly improves the accuracy of the translation.

Moreover, we can note that the MSE evaluates how close the vectors are, not the words themselves and therefore is not totally representative for performance evaluation as opposite to accuracy.

That is the reason why, for the rest of the project we will use the **constrained implementation** version of the translation matrix W.

# 2 Supervised Learning - French to English

In this part, we are going to evaluate our algorithm on the translation from French to English. For the following results, W will always be constraint.

#### First Results and Visual Representation

To check the efficiency of our algorithm, we have two tools:

- the accuracy of our translation on training and testing set: We split N words with a validation<sub>s</sub> plit to create a training set which will be used to calculate W and to apply translation on this set. The words in the testing set will not be used to calculate W, which give us a proof of the efficiency of our algorithm
- a graphical representation of our translation in the vector space: with a PCA (Principal Component Analysis), we project our 300-dimension space in a 2 dimension space to visualize the translation

On a 3000 Words dataset with a 90% validation split, we obtain a 73% accuracy on the training test and a 89% accuracy on the testing set. To check if we are actually creating the correct W, we use the PCA on a small number of words, before applying W and after applying W. As we can see on Fig. 11, with the application of W, the same words in different languages are closer in the embedding space. We are going to see in the next parts the influence of different parameters on our accuracy.

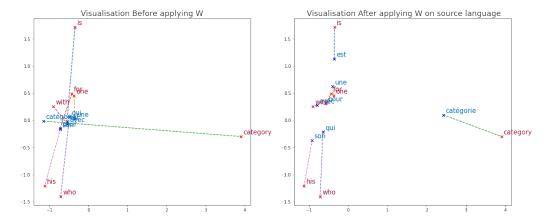


Figure 11: PCA on the target data space and transformation on the key data space before and after applying W

#### Influence of the initialization of W

With the algorithm using W constraint, we changed the value of  $\alpha$ , the learning rate to see the influence of the learning rate and the initialization of W. Those initializations were :

- Matrix of zeros
- Matrix with coefficients following an uniform distribution between -0.2 and 0.2
- Matrix with coefficients following a gaussian distribution centered on 0 with a 0.1 standard deviation

As we can see on Fig. 12 we always obtain the same accuracy for the initialization with 0: which means the learning rate has no influence on the calculation of W, since we obtain a good accuracy. For the two other distributions, we obtain the same behaviour: for small learning rate, the weight of  $\Delta W$  multiplied by  $\alpha$  is too small in regard to the value of the initialized coefficients. When it is big enough, we get a good accuracy.

#### **Accuracy Evaluation**

In this part, we are going to see the influence of different parameters: normalisation of words and distance used for finding the closest word.

All the accuracy are calculated for 1000 words and a 0.9 split between training and testing.

**Normalisation** At the beginning, we wondered if the normalization of the data in the embedding space has an influence on the accuracy. Thus we created a condition in the program which allow the user to normalize or not along the axis of dimension space (each word has a norm of one). We get the following results on accuracy calculated with cosine distance:

As we can observe, there is no difference in the accuracy whether we normalize or not the data. Of course,we checked that the data were not normalized at the beginning. The explanation isn't really clear for us.

**Distance Calculation** When we find the closest word in the target langage, we need to use a distance. Two distances were evaluated for this: the cosine distance defined above and the classical Euclidian

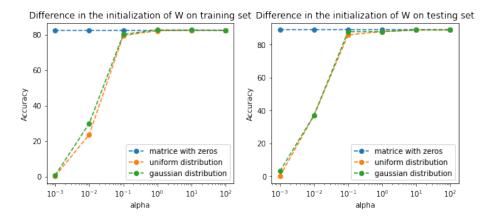


Figure 12: Results on accuracy for different initialization for different value of alpha

	With Normalisation	Without Normalisation
Training Set	82.33	82.44
Testing Set	90,0	90,0

Figure 13: Accuracy for normalized and unnormalized data

Norm. Let's see the influence of the choice of the distance on our algorithm:

	Cosine Distance	Euclidian Norm
Training Set	82.33	76.33
Testing Set	90,0	79,0

Figure 14: Accuracy for different distances

The euclidian results are less interesting than the cosine distance. This was actually expected since the cosine distance measure by definition the similarity between two vectors.

# 3 Different Languages, alphabets Evaluation

In this part of the project, we have selected the constrained version for the translation matrix implementation with the Gaussian initialization (0-1).

We will work on different languages: English, Spanish, Russian and Hebrew. The motivation for these choices reside in the fact that we want to evaluate the influence of the alphabet type and the performances over various different languages translations.

## 3.1 Visual Representation

Hereafter, we can observe the visual representation of the four languages obtained through Principal Component Analysis.

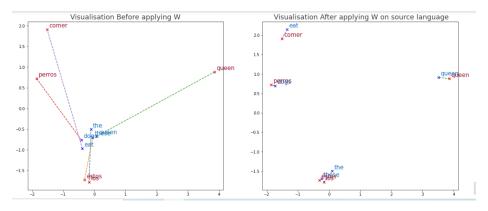


Figure 15: PCA English-Spanish - 5 words

the los these éstos queen queen dogs perros eat comer

Figure 16: Word Pairs English-Spanish

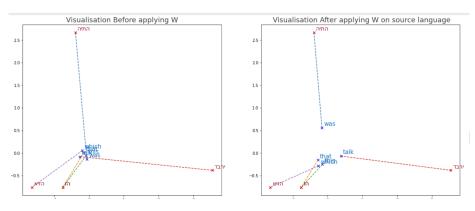


Figure 17: PCA English-Hebrew - 5 words

was היתה that זה this זה talk דברי which איזה

Figure 18: Word Pairs English-Hebrew

# 3.2 Alphabet Influence on accuracy

In this section we will focus our interest on the way the accuracy is affected when dealing with different kind of alphabets.

We will run this experiment on 1000 words, with W (translation matrix) constrained,  $\alpha = 10$  (learning

rate) and cosine distance as evaluation metric.

We expect a higher accuracy for languages with the same alphabet (English-Spanish) rather than on different ones (English-Hebrew, English-Russian, Hebrew-Russian).

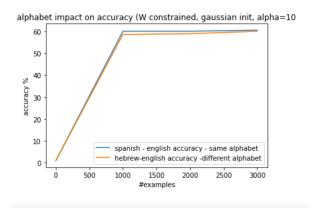


Figure 19: Alphabet impact on accuracy

As we can see, there exists a slight difference in the accuracy between translations Spanish-English and Hebrew-English. This tendency gets negligible as we are dealing with more and more words, but this can be explained by the fact that we are translating languages with different alphabets in the second case.

# References

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