



MATRIX FACTORIZATION

INTERPRETATIBILITY OF LATENT FEATURES

Julien – Matthieu – Mathurin - Laurene



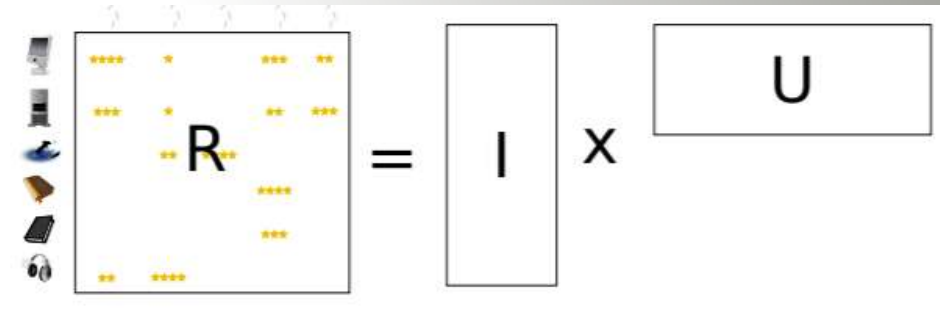
I] Introduction: Matrix Factorization

We chose to work on the **Matrix Factorization** solution for collaborative filtering.

Goal: Find matrices $U(m \times k)$ and $I(k \times n)$ such that we get the mathematical expression for Low rank matrix factorization:

$$\mathbf{R} = \mathbf{I} \times \mathbf{U}^T, \text{ where:}$$

- $\mathbf{R}(m \times n)$ represents the rating matrix / user-item matrix
- $\mathbf{U}(m \times k)$ is the user-feature matrix
- $\mathbf{I}(k \times n)$ is the feature-item matrix



Remind the Cost function formula:

$$C(I, U) = \|R - IU^T\|_{\mathcal{F}}^2 + \lambda \|I\|_{\mathcal{F}}^2 + \mu \|U\|_{\mathcal{F}}^2$$

■ Gradient Descent Method

Take small steps in the cost function analysis and progress in the gradient direction until we get to the minimum.

$$I_{t+1} = I_t - \eta_t \frac{\partial C}{\partial I}(I_t, U_t)$$
$$U_{t+1} = U_t - \xi_t \frac{\partial C}{\partial U}(I_t, U_t)$$

- The matrices U and I are initialized with random values and updated with gradient descent method.

II] Investigation – Interpretability of Latent features

Investigation: What can we learn from interpretability of latent features ?

This section concern is to give meaning to the coefficients of lower dimensional matrices: U (user-feature) and I (item-feature). There exist different techniques, we'll compare some of them:

A) Interpretation based on definition – Baseline method

- └ general definition of MF model to provide coefficients interpretation
- └ small number of latent features explain the user-item interactions – incomplete picture
- └ not always possible to derive meaning

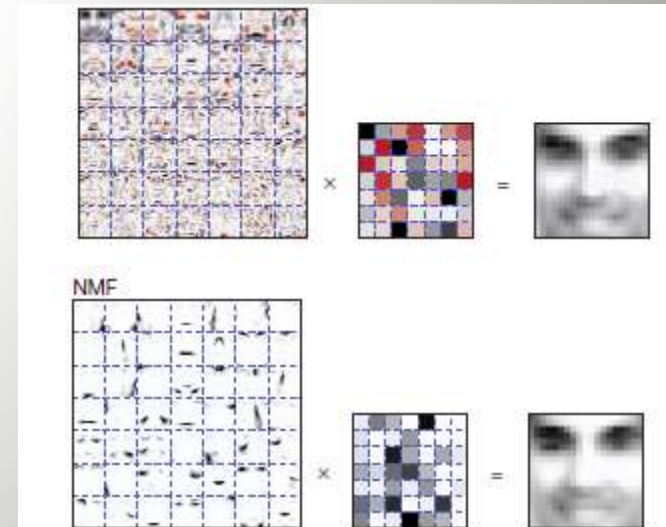
B) Interpretation via non-negative MF - NMF

- └ MF with constraint (all elements must be positive)
- └ represent original data as a weighted addition of vectors
- └ associate features with specific preference pattern
- └ visualization as community of users or imaginary user

$$x_i = \begin{bmatrix} w_{i1} & w_{i2} & \dots & w_{ik} \end{bmatrix} \times \begin{bmatrix} h_1 \\ h_2 \\ \dots \\ h_k \end{bmatrix} = \sum_{j=1}^k w_{ij} \times h_j$$

w_i : weights

components



C) Interpretation via Probabilistic model

- └ Latent features represent different groups of users.
- └ Find relation between users and feature from the rating matrix.
- └ Rows of I reveal the probability of the fact that user from each group like different items.

Rating matrix \rightarrow each user provide information about how much he likes an item.

Entry

N : number of user in the rating matrix.

M : number of items in the rating matrix.

$R_{u,k}$: rating of a user u for an item i .

Parameters

K : number of groups user we want to find.

α : probability that a user belongs to one or more groups.

β : amount of evidence needed to deduce that a group likes an item.

Out

Matrix $N \times K$: $a_{u,k}$ probability that a user belongs to a group $k \rightarrow \sum_{k=1}^K a_{u,k} = 1$

Matrix $K \times M$: $b_{k,i}$ probability that a user from u group k like an item i .

Experiments and evaluation metrics

1. Analysis of the tradeoff of interprobability over performance

- 🔍 Comparison between Baseline and probabilistic methods
 - 🔍 The constraints create a difference in the **RMSE loss**
- 🔍 As loss increases, interprobability increases (probabilistic method)

2. Creation of a dataset

- 🔍 characteristic users and items groups creation
 - 🔍 check if we get coherent results

3. NMF and Probabilistic approach application on MovieLens dataset

- 🔍 What do we learn from the dataset
- 🔍 Comparison between the two methods