

1) Coaxial Cable Design



TOP VIEW



$$2a = 1 \text{ mm}$$

$$a = 0.5 \text{ mm}$$

$$\lambda = \frac{c}{f} = 42.857 \text{ mm}$$

$$l = 85.711 \text{ mm} = 2\lambda$$

SCREEN 0

$$120\pi = \sqrt{\mu_0/\epsilon_0}$$

$$\epsilon = \epsilon_0 \epsilon_r = 2.1 \text{ (Teflon)}$$

$$Z = 50 \Omega = \sqrt{\frac{\mu_0}{\epsilon}} \frac{\ln(b/a)}{2\pi}$$

$$b = a e^{\frac{(\epsilon_r - 1)\sqrt{2\pi}}{2}} = 1.673 \text{ mm}$$

We choose a and b to get matching with the characteristic impedance

In theory we shouldn't get any losses - But in practice, the transmission gets power absorbed by the coaxial cable

- mismatch losses

- ohmic losses

→ dielectric losses

We normalize the S-Parameters to 50Ω
(set up solver)

[Screen 1,2] → S_{21}, S_{12} around $0 \text{ dB} \rightarrow$ no significant losses

[Screen 3,4] → S_{11}, S_{22} optimized below -25 dB

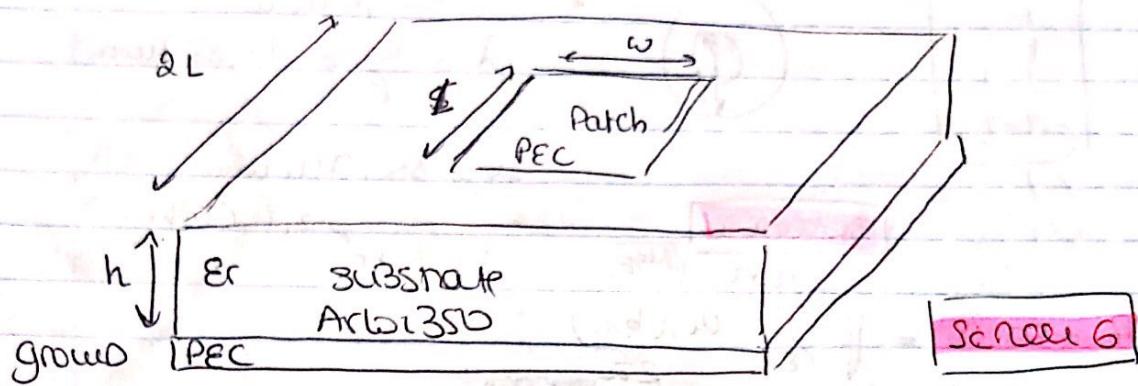
insertion loss @ freq $f = 7 \text{ GHz} \rightarrow$ [Screens]

$$S_{21}(f=7 \text{ GHz}) \approx 0 \text{ dB}$$

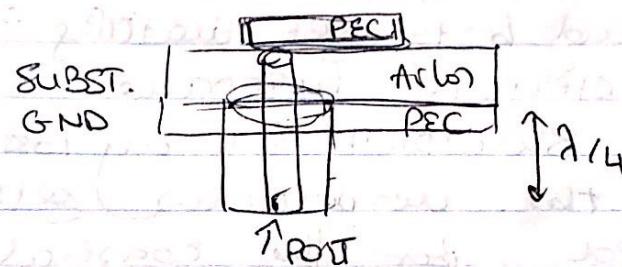
/1

S Parameters optimized cable \rightarrow min insertion loss \rightarrow matching [Screen 1 \rightarrow 5]

2)



SIDE VIEW



According to theory:

$$Er = 3,5 \leftarrow \text{Arlon 350}$$

$$w = \frac{c}{2f_r} \sqrt{\frac{2}{Er + 1}} \quad \text{Permittivity const}$$

$$L = \frac{c}{2f_r \sqrt{Er_{eff}}} - 2 \Delta L \quad Er_{eff} = \frac{Er + 1}{2} + \frac{Er - 1}{2} \left[1 + 12 \frac{h}{w} \right]^{-1/2}$$

$$\Delta L = 0,412h \quad \frac{(Er_{eff} + 0,3) \left(\frac{w}{h} + 0,764 \right)}{(Er_{eff} - 0,758) \left(\frac{w}{h} + 0,8 \right)} =$$

$$x_f = \frac{L}{2\sqrt{Er_{eff}}} = \text{location of pin.}$$

1/2

$\epsilon_{eff} \rightarrow$ Because of fringing effect of the electric field $\rightarrow \epsilon_r$ of substrate and ϵ_0 of the air combine to ϵ_{eff}
 \hookrightarrow lower than ϵ_r , dielectric substrate
 We can also change a and b nodes of the coaxial cable to get matching as long as their ratio doesn't change

We chose the following parameters

$$\begin{array}{lll}
 \omega = 13,33 \text{ mm} & \epsilon_{eff} = 3,05 & x_f = 2,86 \text{ mm} \\
 L = 9,994 \text{ mm} & \Delta L = 0,779 \text{ mm} & r_{out} = b = 0,873 \\
 h = 1,6 \text{ mm} & & r_{in} = a = 0,25 \\
 \text{grom height} = \frac{\text{patch height}}{3} = 0,02 \text{ mm} & & \text{coax length: } \approx 1/4 \\
 \text{patch height} = 0,5 \text{ mm} \approx h/3 & & \lambda = 40 \text{ mm}
 \end{array}$$

Input matching over $0,7f: 1,3f \rightarrow 4,9 \rightarrow 9,1 \text{ GHz}$
 Screen 7) $\rightarrow 6,86 \rightarrow 7,14 \text{ GHz}$ freq. range has return loss better than -10 dB !

We got the size patch according to the theoretical results. Small deviations can be explained by fine tuning parameters due to practical losses!

3D far field RP of the Patch Antenna @ $f = 7 \text{ GHz}$

Screen 8)

Theory
match w/
 $\epsilon_r(SG^{1/2})$

RP γ -plane: Elevation RP | Screen 9a,b

RP \times -plane: Azimuth RP | Screen 10a,b

We can see that our Patch antenna has a maximum of 7.21 dBi which is very comparable to an ideal patch 7.5 dBi. The difference can be explained by practical losses.

- Direction of Peak Gain: γ -direction

Peak gain: 7.05

| Screen 11

Directivity: 7.22

| Screen 12

$$\gamma = G/D = 97.65\%$$

- Surface Currents on Patch antenna

| Screen 13

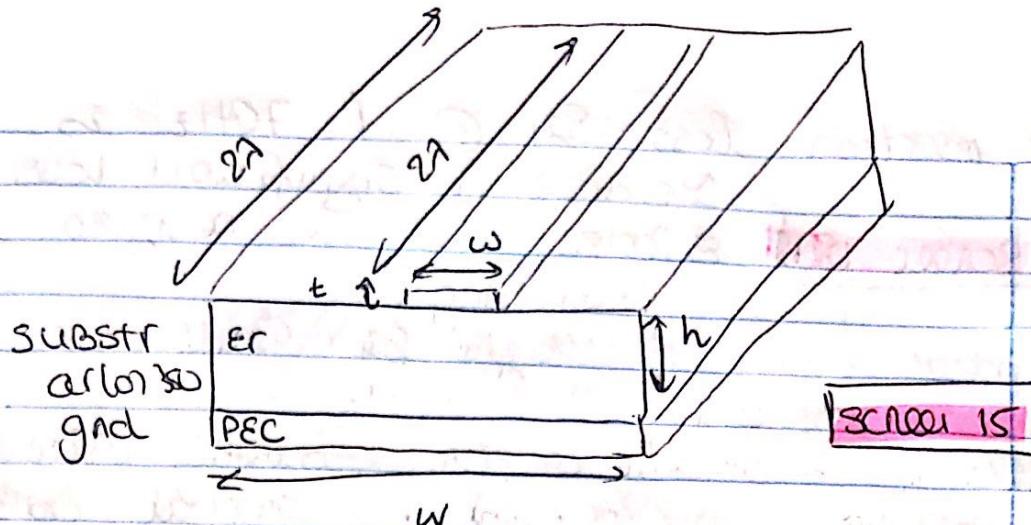
- Surface Currents on the ground plane

| Screen 14

As expected from theory, we can see from the last 2 screens that the highest current comes from the port (at the edge of the coaxial cable) and then spreads up to the ground plane and to the patch antenna through the inner pin of the coaxial cable (PEC). Since we extended the inner pin up to the point between substrate and patch antenna.

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3)



$$l = 27 = 80 \text{ mm}$$

$$W = 13,33 \text{ mm}$$

$$w = 0,312 \text{ mm}$$

$$h = 1,6 \text{ mm}$$

$$t = 0,5 \text{ mm}$$

t is chosen as the same height as the Patch antenna

while w is calculated for 100Ω impedance matching

⚠️ Simulate \rightarrow Setup Solver \rightarrow Normalize to fix impedance: 100Ω

We place ports @ edges of microstrip line.

$$w = \frac{7,48h}{e^{\left(\frac{(Z_0 \sqrt{h+t})}{8f}\right)}} - 1,25t$$

when using w from the patch antenna we were matching $f = 7,25 \text{ GHz}$ instead of 7 GHz . So we tuned our model in order to get matching @ f By modifying $w = 14 \text{ mm}$.

- S_{11} Screen 16 $\rightarrow -35 \text{ dB} @ f = 7 \text{ GHz}$
- S_{22} Screen 17 $\rightarrow " " "$

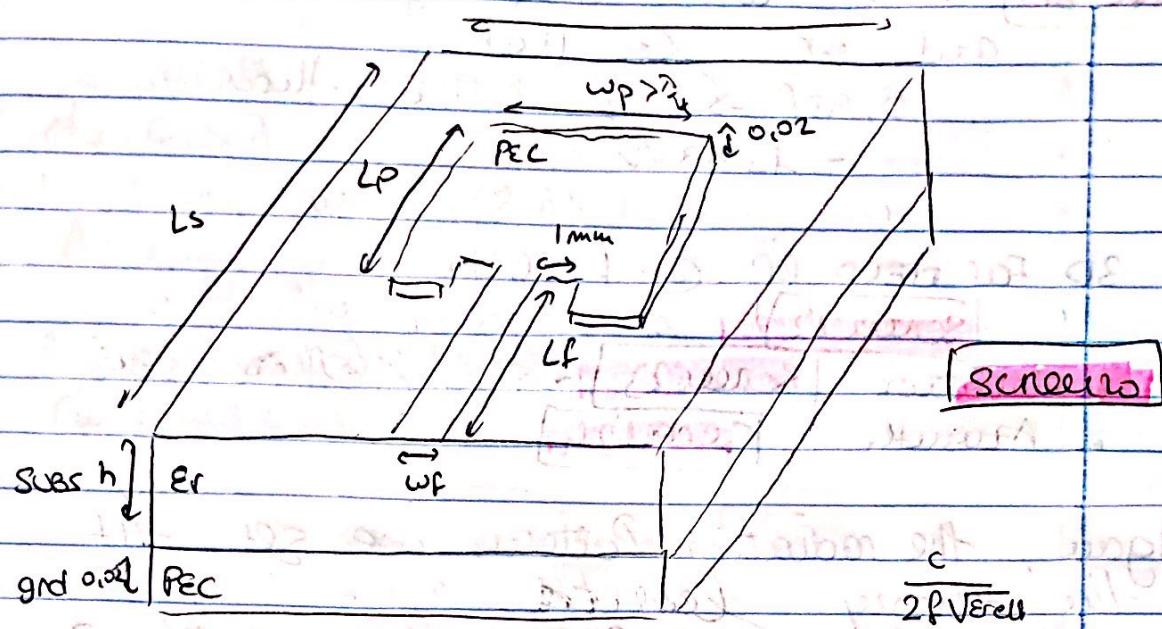
↳ Below $-25 \text{ dB} \checkmark$

- The insertion loss S_{21} @ $f = 7\text{GHz}$ is
 $\sim 0\text{dB} \rightarrow$ no significant loss
Expected since we design for matching!

A coaxial cable of length 2λ would have "better" insertion loss -

Stripline depending on its geometry usually is slightly higher than coaxial cable i.e. loss ($\sim 1 \times 10$)

4)



$$\lambda = \frac{c}{f} = 11.38 \quad w_p = \frac{c}{2f} \sqrt{\frac{2}{\epsilon_r + 1}} \quad L_p = \text{left} - 2\Delta L$$

$$h = \frac{0.06062}{\sqrt{\epsilon_r}} \quad L_s = L_p + 6h \quad w_s = w_p + 6h$$

$$\lambda_g = \frac{\lambda}{\sqrt{\epsilon_{\text{refl}}}} \quad L_p = \frac{\lambda_g}{4} \quad w_f = \frac{\lambda_g h}{(2 \sqrt{\epsilon_r + 1.41})} - 1.25t$$

Because our dielectric substrate is not that high we used other matching options of the Patch antenna to the line. By tuning the above parameters: and we used the following values

$$w_p = 13.79 \mu m \quad \epsilon_{\text{refl}} = 3.598$$

$$h = 1.34 \mu m \quad L_p = 10.492 \mu m$$

$$w_s = 21.83 \mu m \quad L_s = 18.532 \mu m$$

$$L_P = 5.88 \mu m \quad w_f = 0.76 \mu m$$

(f=7.25 GHz)

NOTE: the impedance of the line remains low!

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Screen 21 → S₁₁ watched @ f = 70 Hz
and we see flat

$0.98f \rightarrow 1.02f$ Better than
- 10 dBW

- 3D far field RP @ $f = 3GHz$

Screen 22

- Elevation [Screen 23]
 - Azimuth [Screen 24]

Again, the radiation patterns we get fit the theory correctly.

We get similar shape as in section 3 with directivity direction: z-axis

5) Normalized Array Factor

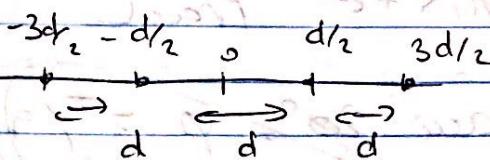
4 elements along x-axis

$$d = 0.5\lambda \quad N = 4$$

$$AF = \frac{1}{N} \sum_{m=1}^{N-1} e^{j(\hat{r} \cdot \hat{r}_m) k}$$

$$\hat{r} = \sin\theta \cos\varphi \hat{x} + \sin\theta \sin\varphi \hat{y} + \cos\theta \hat{z}$$

$$\hat{r}_m = m d \hat{x}$$



$$AF = \frac{1}{4} \left[e^{j \sin\theta \cos\varphi \frac{kd}{2}} - e^{j \sin\theta \cos\varphi \frac{kd}{2}} + e^{j \sin\theta \cos\varphi \frac{3\pi}{2}} + e^{-j \sin\theta \cos\varphi \frac{3\pi}{2}} \right]$$

$$AF = \frac{1}{2} \left[\cos(\sin\theta \cos\varphi \frac{\pi}{2}) + \cos(\sin\theta \cos\varphi \frac{3\pi}{2}) \right] =$$

$\xrightarrow{k\lambda = \pi} \xrightarrow{\Delta\phi = 0} \boxed{\text{Screen 25+26}}$

we get a sinc shaped as expected
from the Theory.

$$\varphi = \sin\theta \cos\varphi \frac{\pi}{2} = \Delta\phi$$

- Array Directivity

$$D = \frac{2\pi}{P_{rad}} \quad P_{rad} = \int_{\theta=0}^{\pi/2} \int_{\phi=0}^{2\pi} M(\theta, \phi) \sin \theta d\phi d\theta$$

$$M(\theta, \phi) = AF^2 \quad \text{using Matlab Numerical Solver}$$

$$D = 4 = \frac{2\pi}{1.57 \times P_{rad}}$$

- Steer Beam $\theta = 20^\circ, \bar{\alpha}_g \approx 0.35 \text{ rad}$

$$\psi = \frac{kd}{\pi} \cos(\theta) \sin(\theta) - \Delta\phi = 0$$

$$\Rightarrow \Delta\phi = \bar{\alpha} \sin\left(\frac{\lambda}{d}\right) = 1.074$$

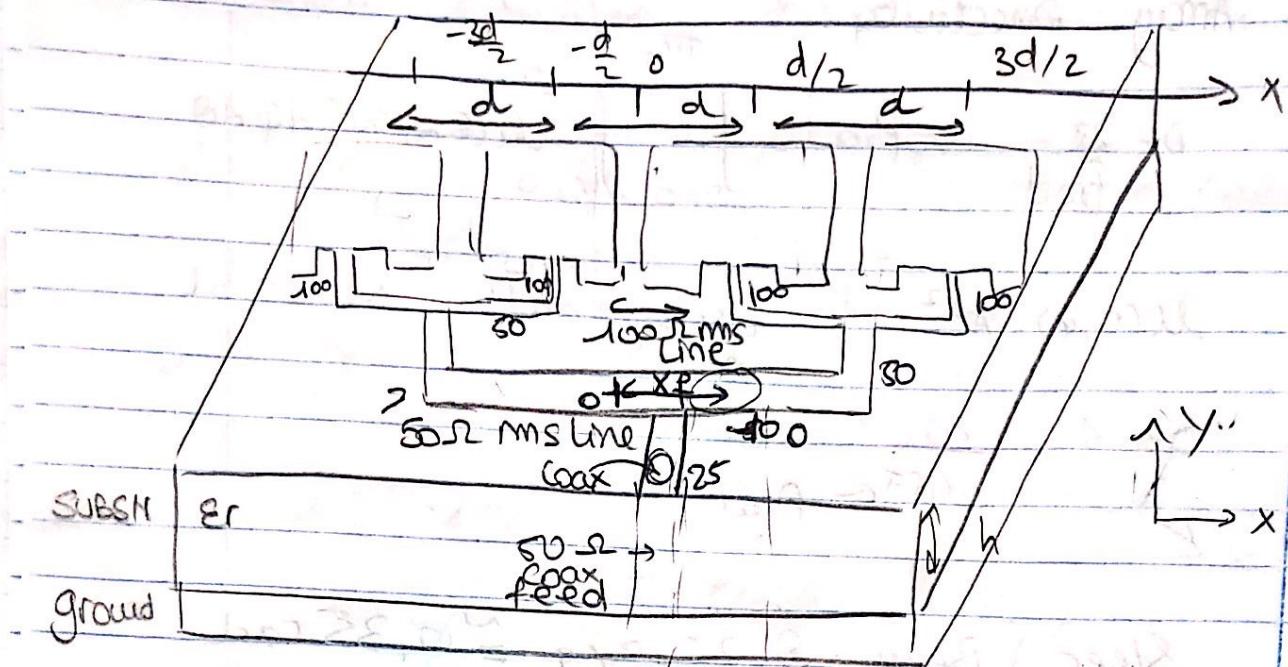
$$\psi = k d \sin \theta - \Delta\phi$$

$$AF = \frac{1}{2} [\cos(\psi_2) + \cos(3\psi_2)]$$

Screen 27 As we can see

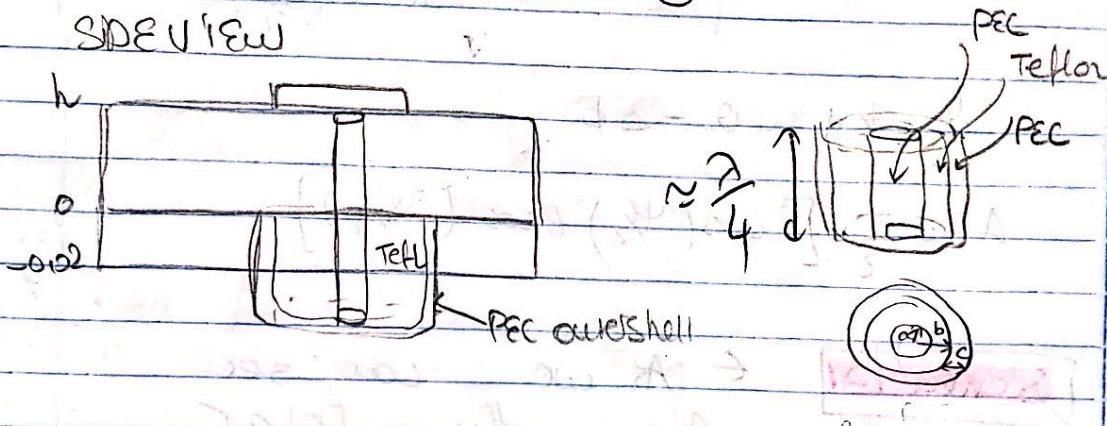
from the polar representation, get a pattern directed towards $\theta = 20^\circ$. Moreover the cartesian representation shows maxima at $\theta = 0.35 \text{ rad} = 20^\circ$ as expected.

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SCREEN 28,29

4 elements array
along the x axis



4 elements x axis $d=0,57$

vertical Polarization $\theta=0$ $E=E_0 \hat{y}$

The array configuration leaves the Radiation Pattern in the y plane

The physics of the array does not depend on the arbitrary chosen axis system

due to width
so thus V transformers were calculated
thanks to the following formula

$$\omega = \frac{7.68 h}{\sqrt{\frac{80}{20} \frac{\mu_r + \mu_i}{87}}} - 1.25 t = 1.63$$

$$w_{100} = 0.76 \text{ mm} = w_f$$

$$d = \lambda/2 \quad \lambda = 61.38 \text{ mm}$$

$$lf = 5.88 \text{ mm}$$

$$ws = 21.83 \text{ mm}$$

$$h = 1.34 \text{ mm}$$

$$ls = 18.532 \text{ mm}$$

$$l_{out} = 0.35 \text{ mm}$$

$$wp = 13.79 \text{ mm}$$

$$r_i = 0$$

$$lp = 10.492 \text{ mm}$$

x_f = dist of the coaxial cable on the \hat{x} -axis from the origin.

middle of a 100Ω line $\rightarrow 50\Omega$

We can take the formulas developed in class for away along the \hat{z} axis and replace θ by ϕ

1) this is only valid when looking at the yz -plane (for x -array)
or one should consider to add correction terms.

We can see that for the centered ($11(\hat{x}$ -axis) coaxial $\alpha B/c$) we get matching $\Leftrightarrow f = 7.61 \text{ Hz}$

[Screen 30]

S_{11} is matched and our frequency and gets 1 better than -10dB

- Different from section 4 since now 4 patch antennas interact with each other
 \hookrightarrow coupling effect

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Polar, 2D
3D, 2D Rad Pattern Screen 31, 32, 33

u u u Azimuth RP Screen 34, 35, 36

u u u Elevation Screen 37, 38, 39

- We get expected Radiation Pattern
- Since for an array we have

$$RP_{\text{array}} = RP_{\text{single element (patch)}} * AF$$

and as expected, most of the radiation happens around the origin (coax cable)

Peak Directivity: 11.89 Screen 33, 34

gain: 11.82 Screen 33, 34

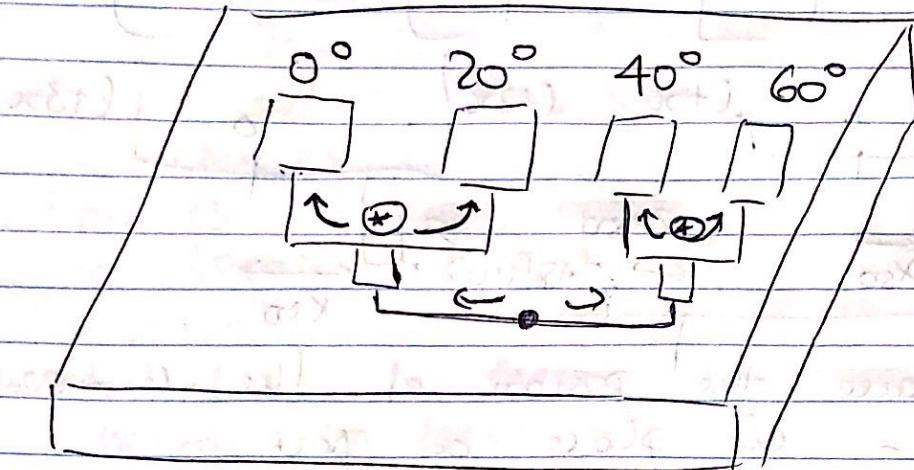
$\eta = 99.9\%$ Efficiency @ $f = 7 \text{ GHz}$.

We can see that we get very high efficiency -

- Difference from Matlab comes from the fact that we used the following approximation

$$M \approx (HF)^2$$

Beam Steering



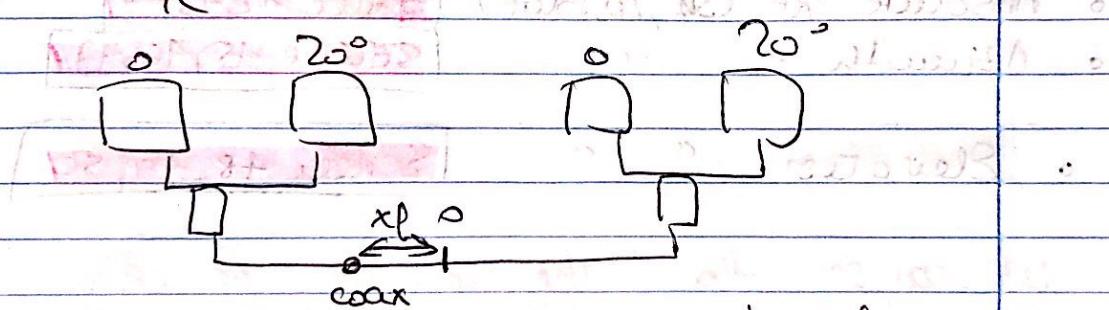
$\lambda_{\text{prop const}}$

$$\beta l = \Delta\phi \quad \beta(l_1 - l_2) = \Delta\phi$$

$\ell_{\text{total length}}$

we should create an offset

Bw + 2 patch antennas (transformer $\frac{1}{4}$)
should not be centered (to the left)
But the 2 groups of 2 patch antennas
won't be delayed between them



to create the phase delay of the first
picture we'll also need to move the
feeding point = coaxial cable

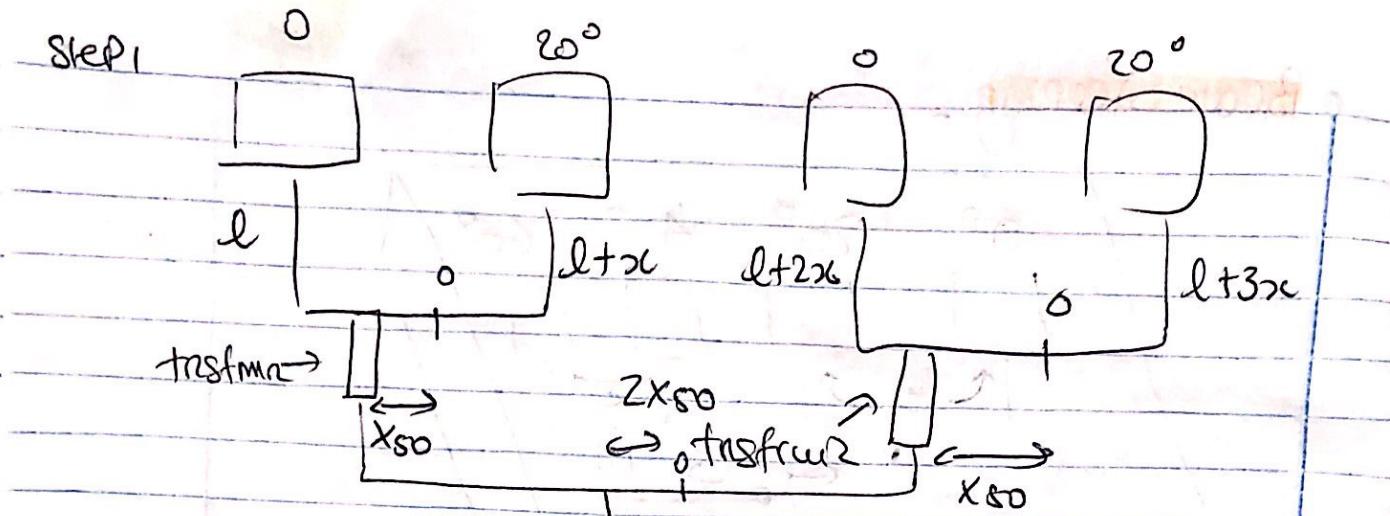
$$\beta x_f = \beta \Delta l = \frac{40/2}{180} \pi = \frac{\pi}{q} = \frac{\pi}{20^\circ} = \beta \Delta l$$

$$\Delta l = x_f = \frac{\pi}{q\beta} = \frac{\pi}{9} \cdot \frac{1}{2\pi} = \frac{1}{18} = 2 \times 50$$

$$x_{50} = \frac{\Delta l}{2} = \frac{1}{36}$$

$$\beta d = \frac{2\pi}{\lambda} \frac{x}{z} = \pi = 180^\circ$$

✓ 1h



We imbalance the position of the lower transformer - We place a port on each antenna and check the phase of the S_{ij} parameters where $j=1$ is the coaxial port.

So $S_{21}, S_{31}, S_{41}, S_{51}$

- Absolute RP. (3D, 2D, Polar) [Screen 42, 43, 44]
- Azimuth " " [Screen 45, 46, 47]
- Elevation " " [Screen 48, 49, 50]

We can see that the radiation pattern got affected / different shape when applied with beam steering and this is expected since the location of the feeding point changes the main lobe direction \rightarrow for directivity purposes

- input matching S₁₁ Screen 51

To apply linear phase, we unbalanced our picture and so the input matching also changes.

This is because, when moving the source location (coaxial cable) matched to 50 Ω from the middle of the 100 Ω horizontal line, exact

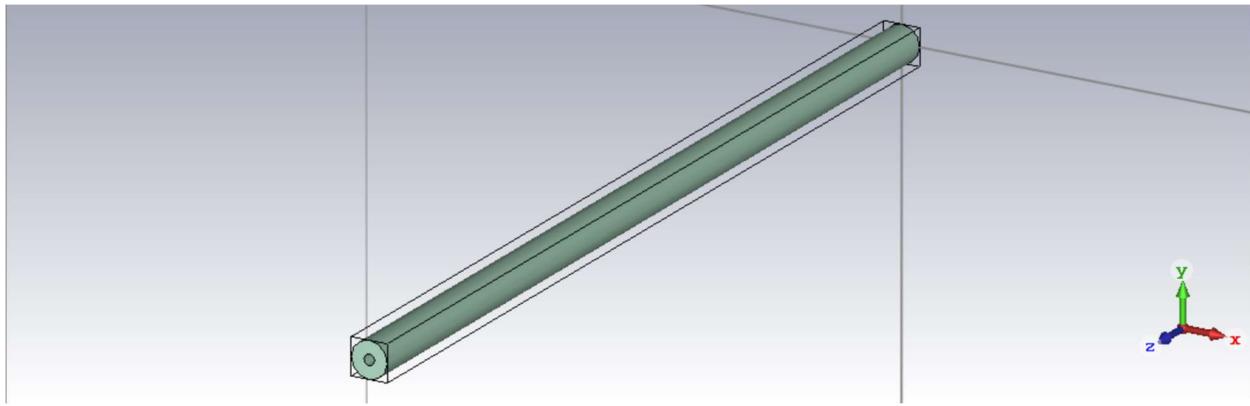
you're no longer at 50 Ω.

This of course affect the S-parameter behaviour.

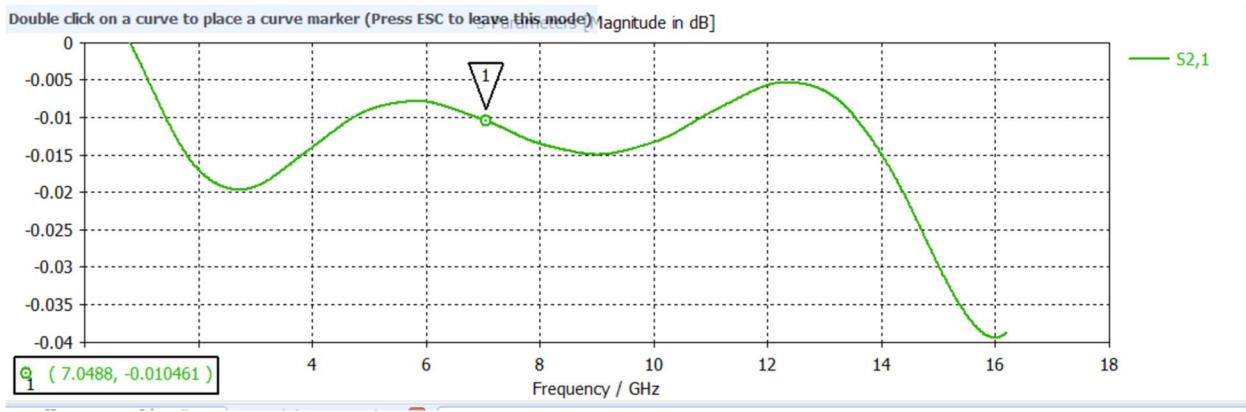
However, our undirected R.P was already close to 20° so we didn't have to use a big distance so that's the reason why our input matching pattern is still valid.

PART 1: COAXIAL CABLE

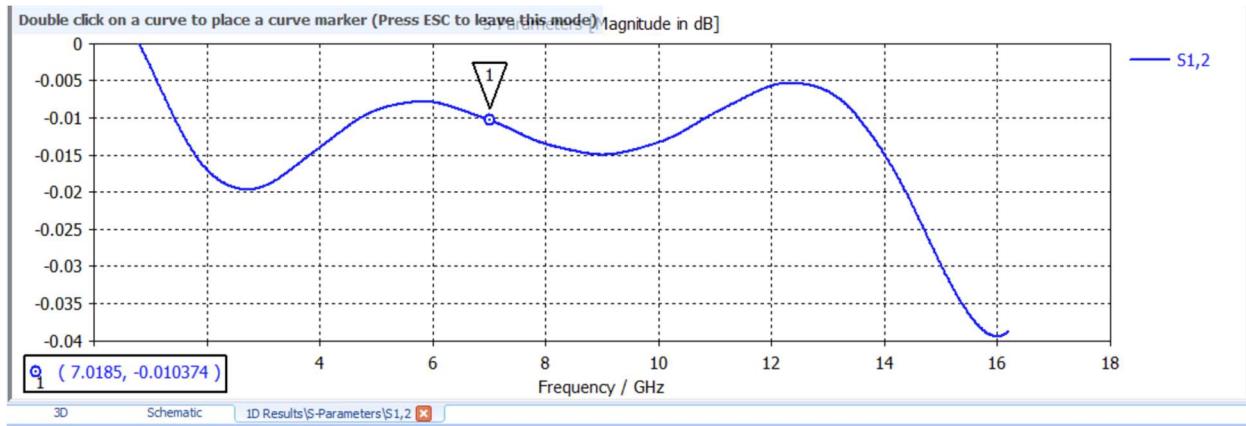
Screen 0: coaxial cable



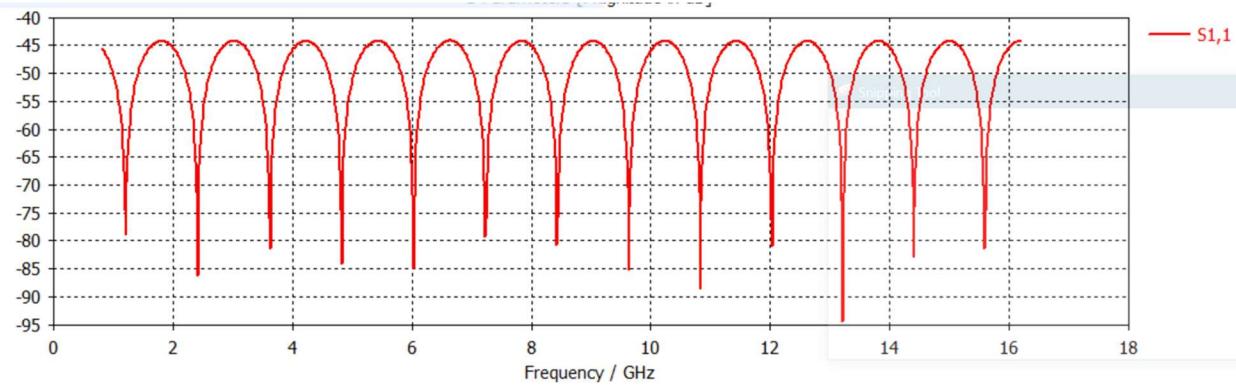
Screen 1: S21 magnitude



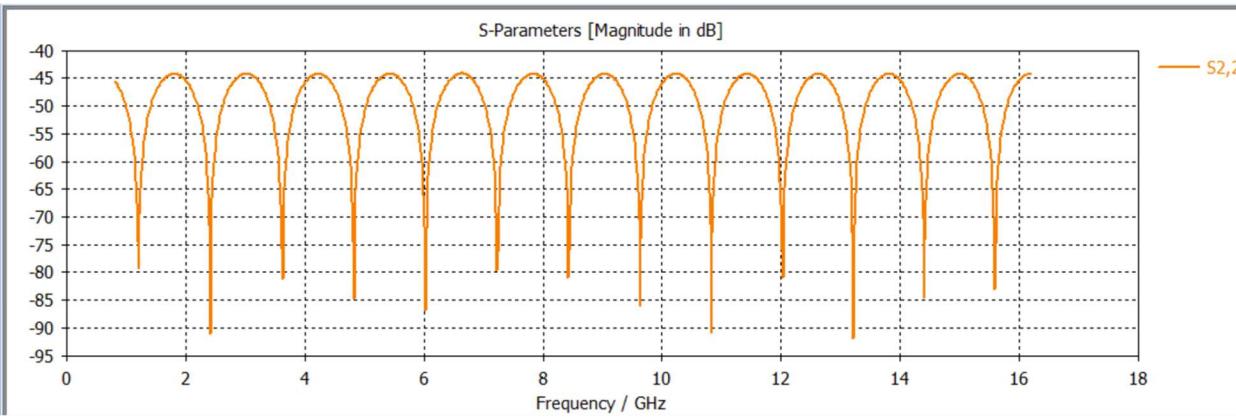
Screen 2: S12 magnitude



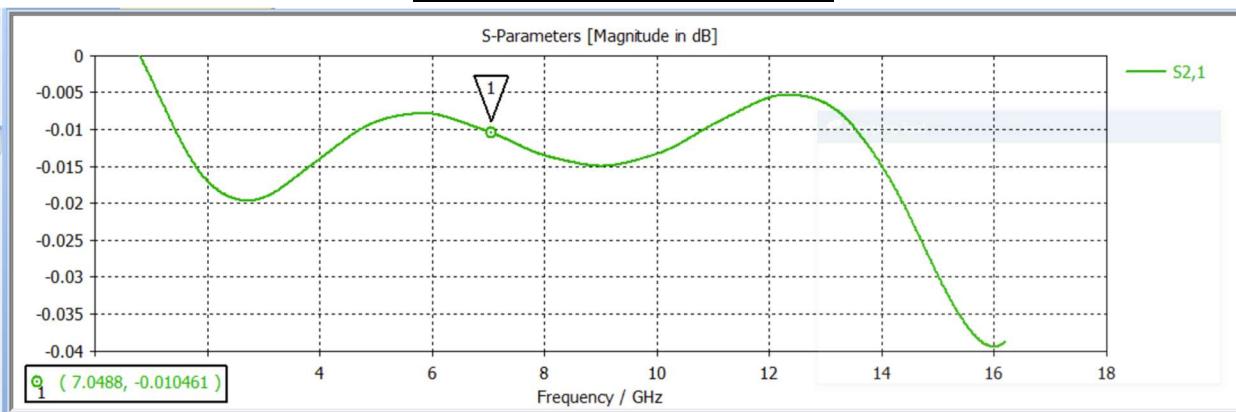
Screen 3: S11 magnitude



Screen 4: S22 magnitude

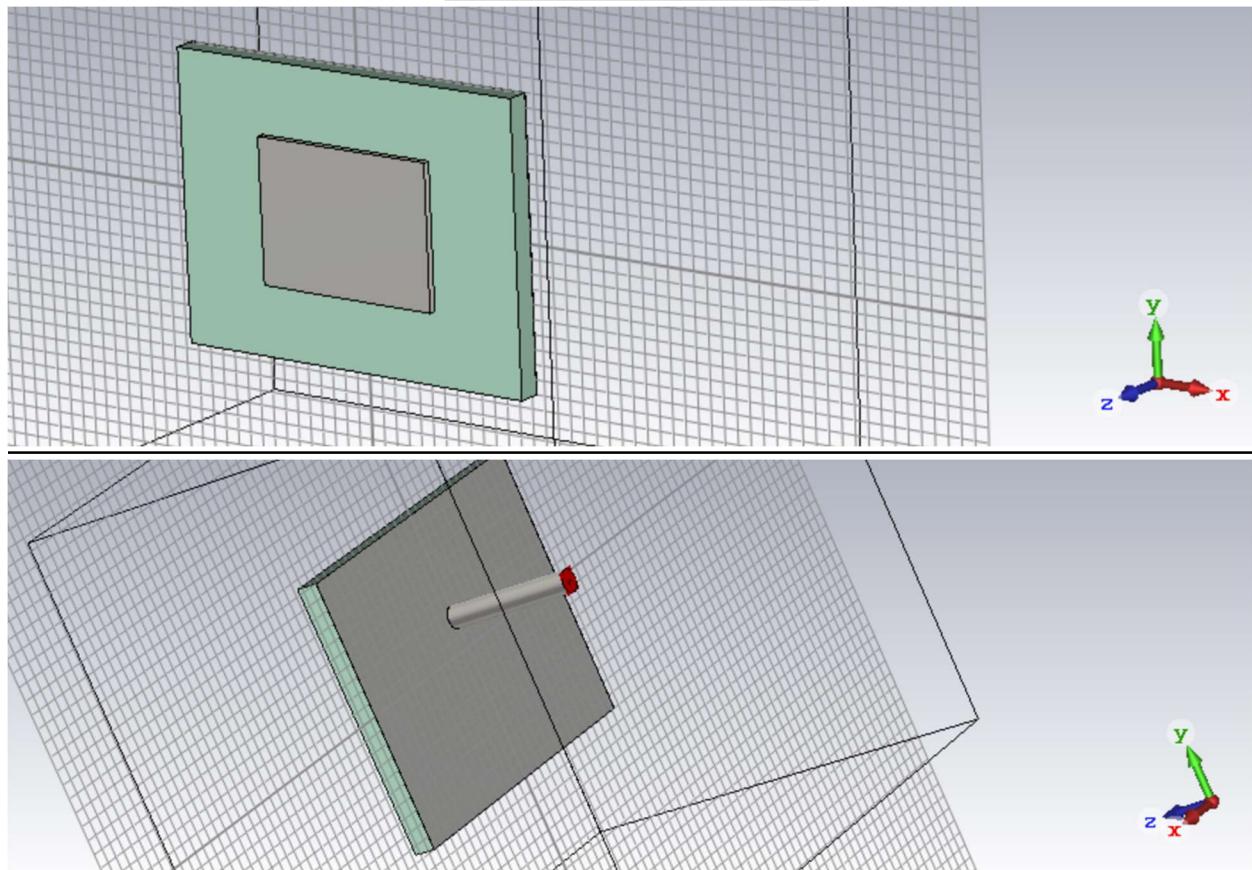


Screen 5: insertion loss S21

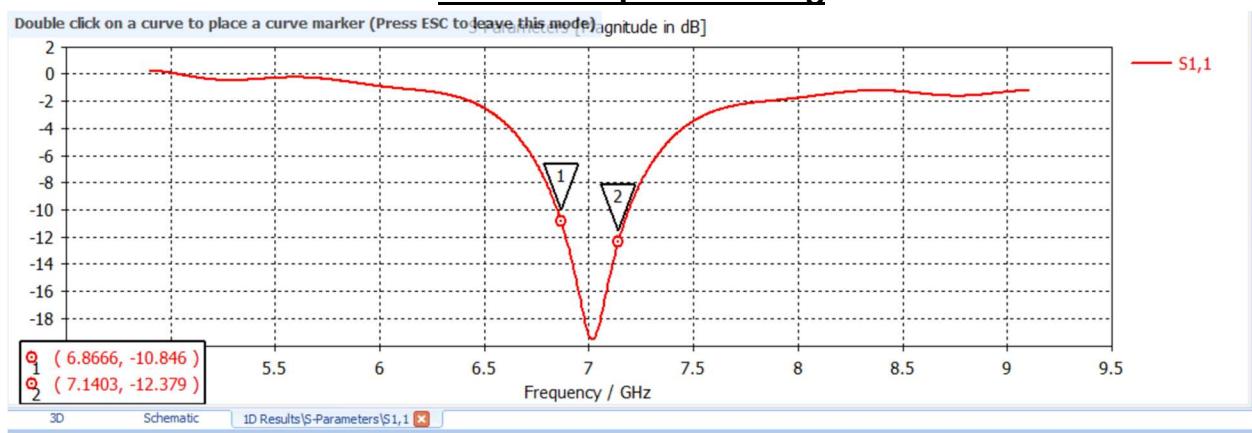


PART 2: PATCH ANTENNA COAX FEED

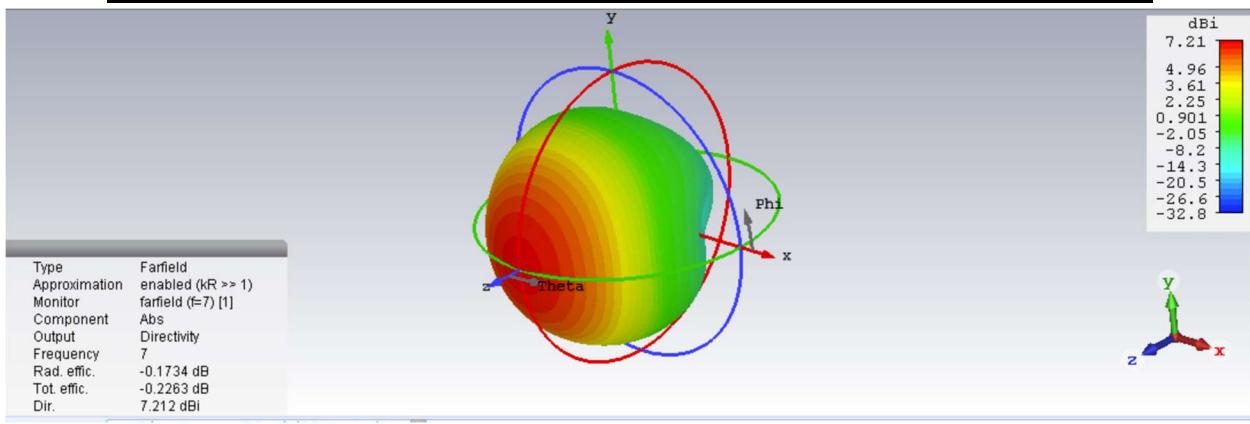
Screen 6: Patch antenna



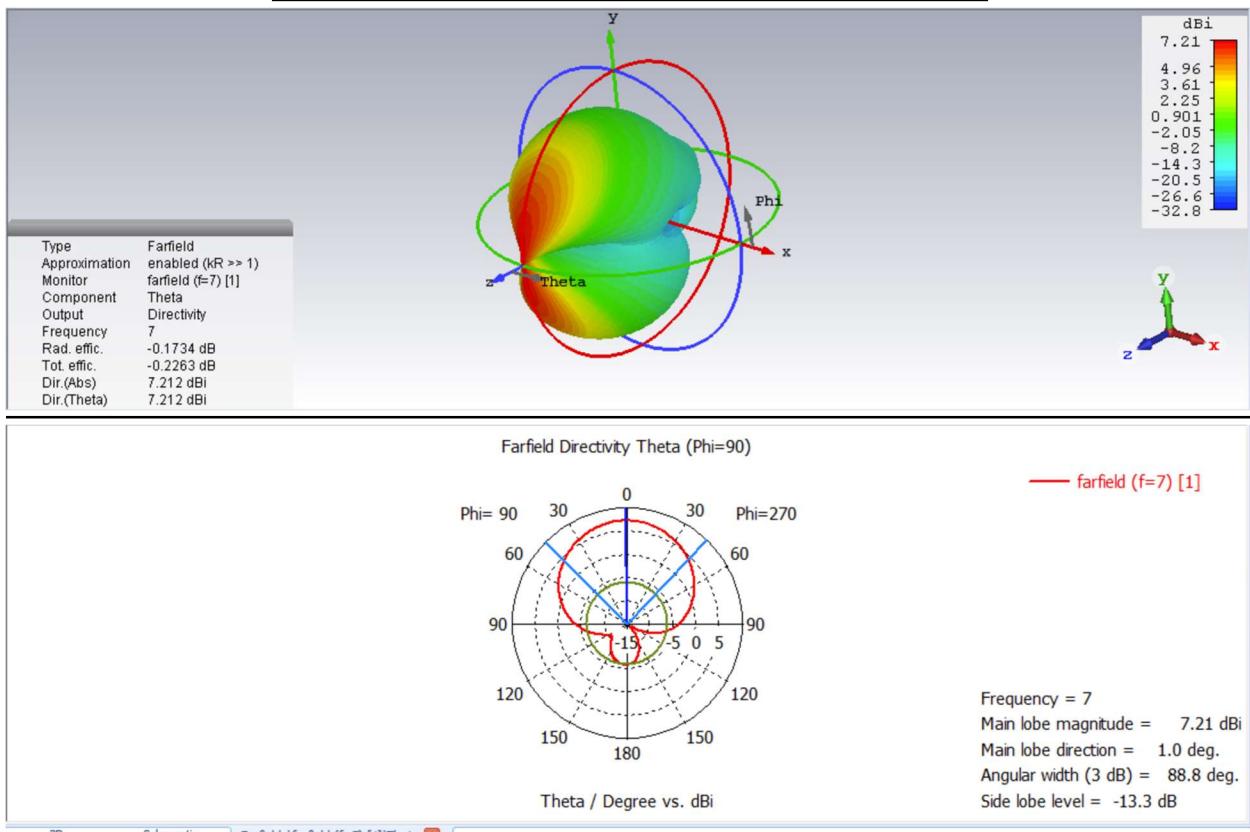
Screen 7: Input matching



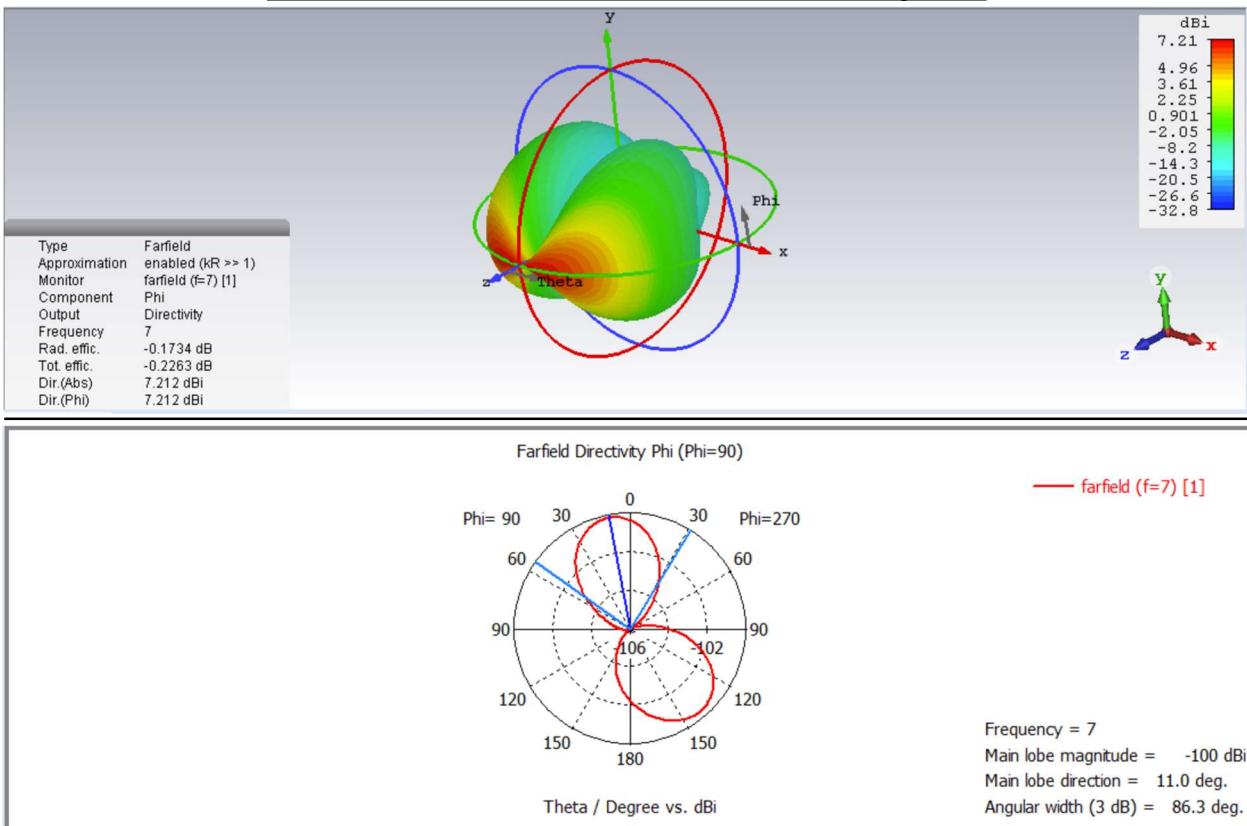
Screen 8: 3D field Radiation Pattern of the Patch antenna at f=7GHz



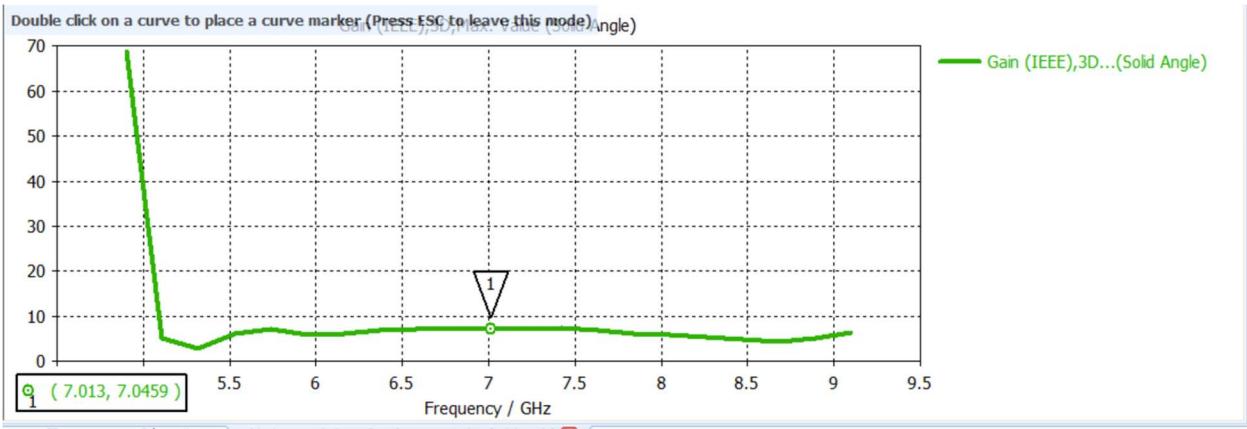
Screen 9: Elevation Radiation Pattern yz-plane



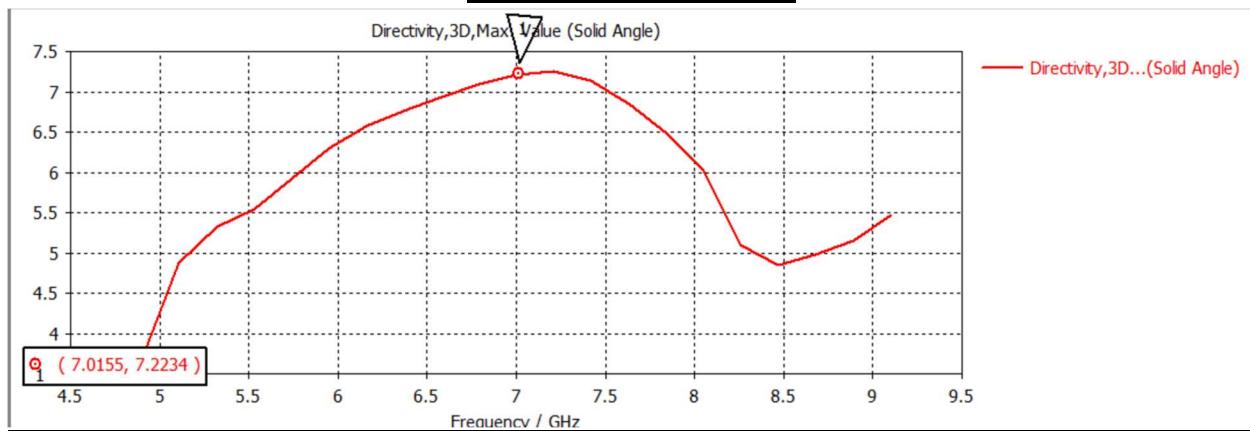
Screen 10: Azimuth Radiation Pattern xz-plane



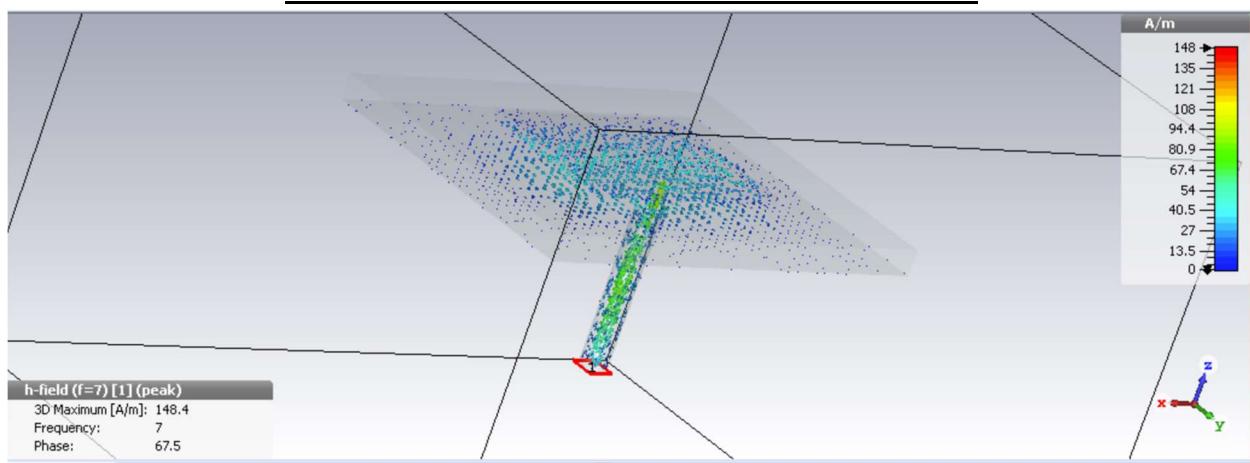
Screen 11: Peak gain



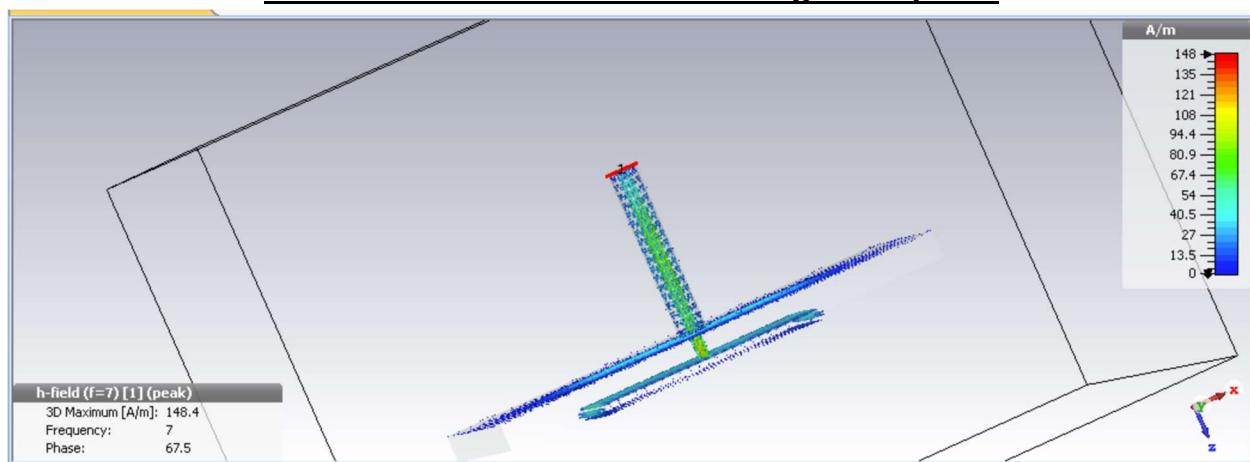
Screen 12: Directivity



Screen 13: Surface Current on Patch antenna

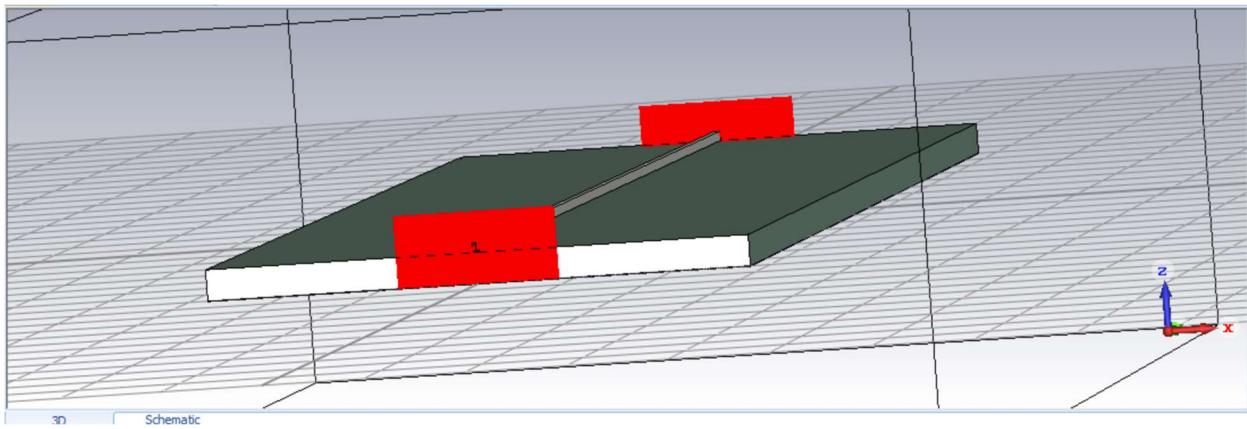


Screen 14: Surface Current on the ground plane

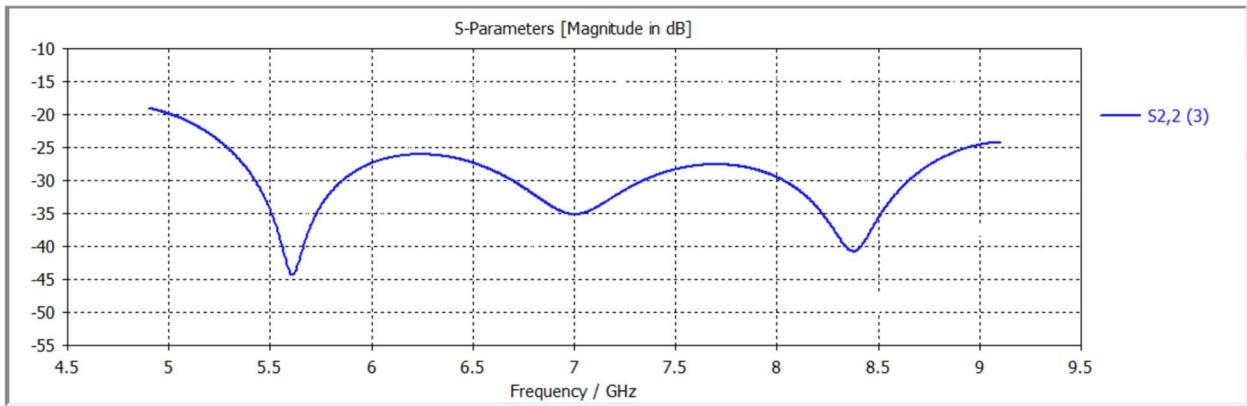


PART 3: MICROSTRIP ANTENNA

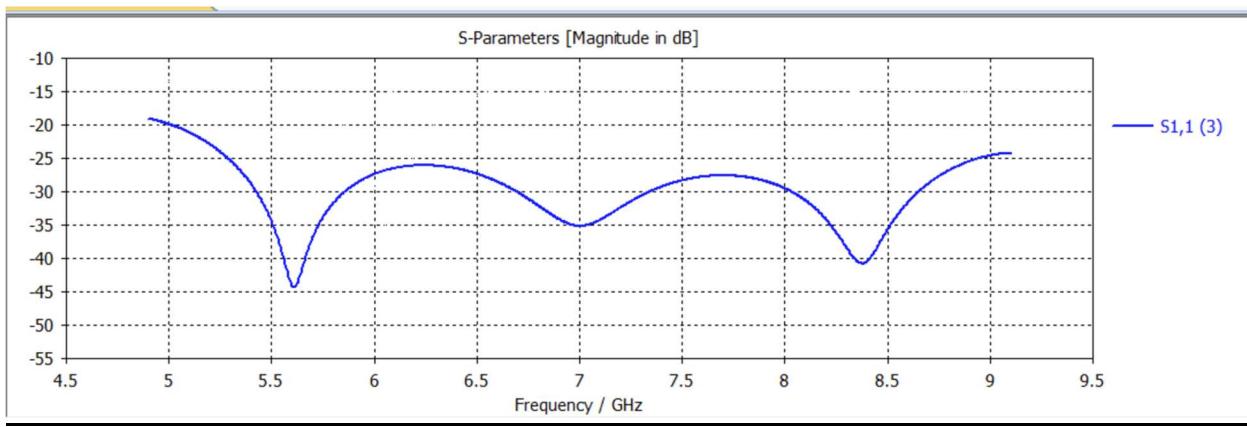
Screen 15: Microstrip antenna



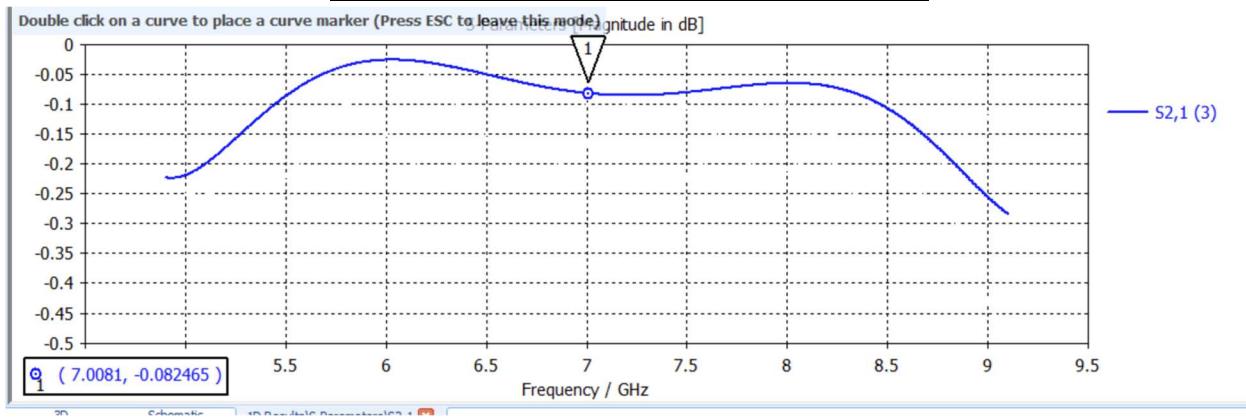
Screen 16: S22 magnitude



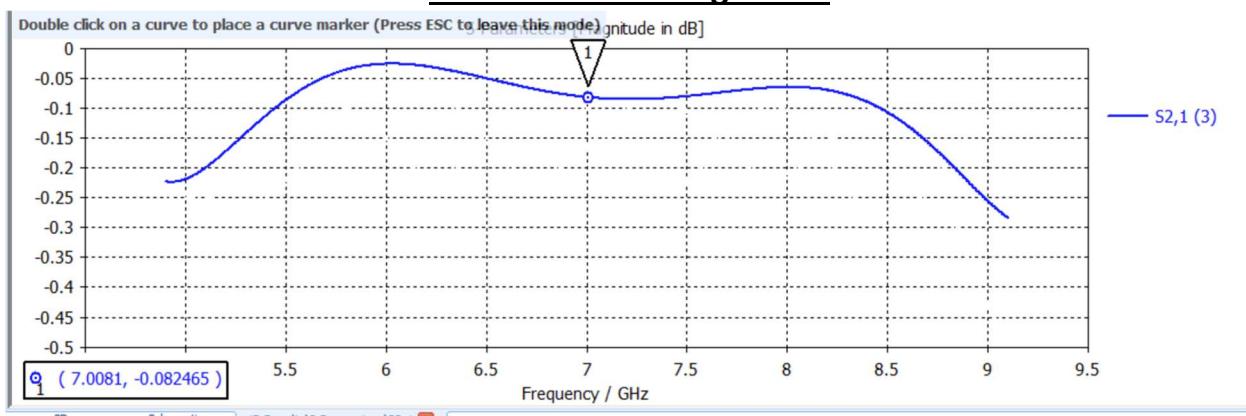
Screen 17: S11 magnitude



Screen 18: insertion loss S21 at f=7GHz

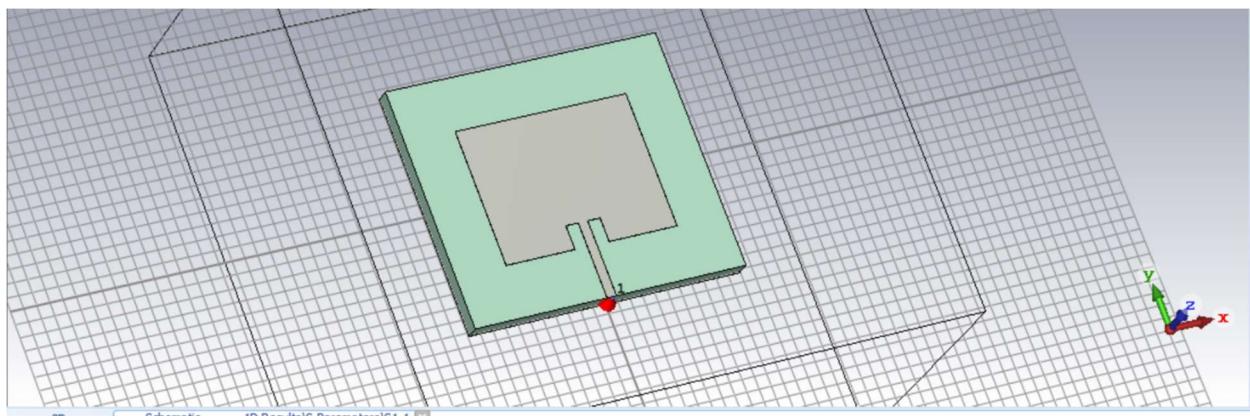


Screen 19: S12 magnitude

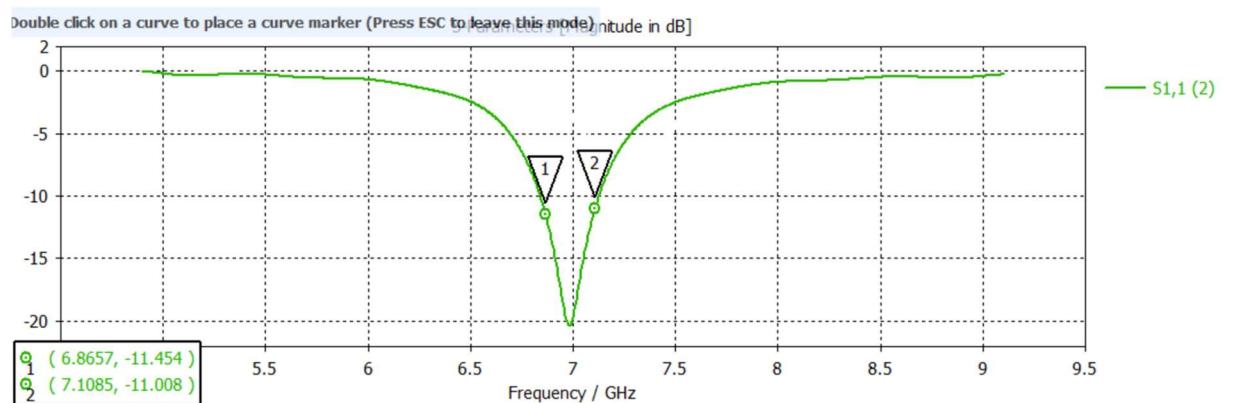


PART 4 : PATCH ANTENNA MICROSTRIP FEED

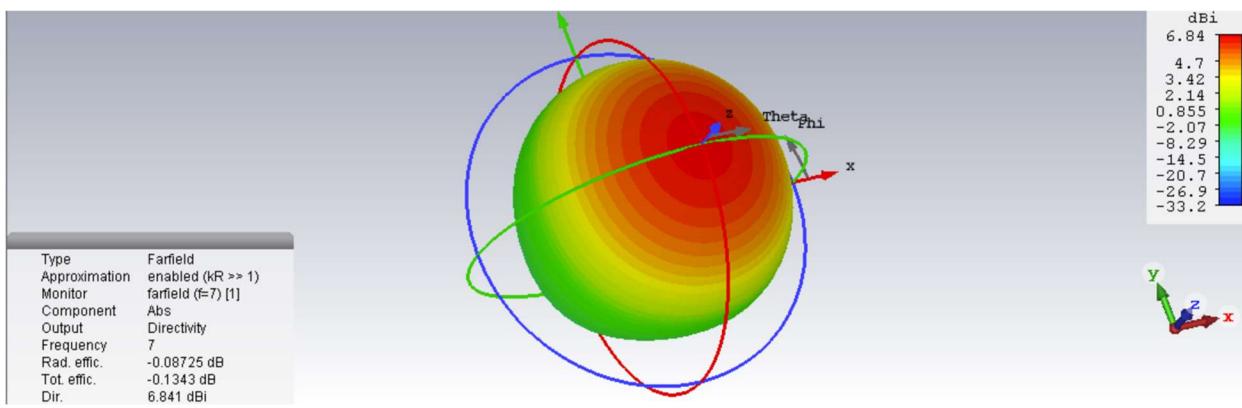
Screen 20: Patch Antenna



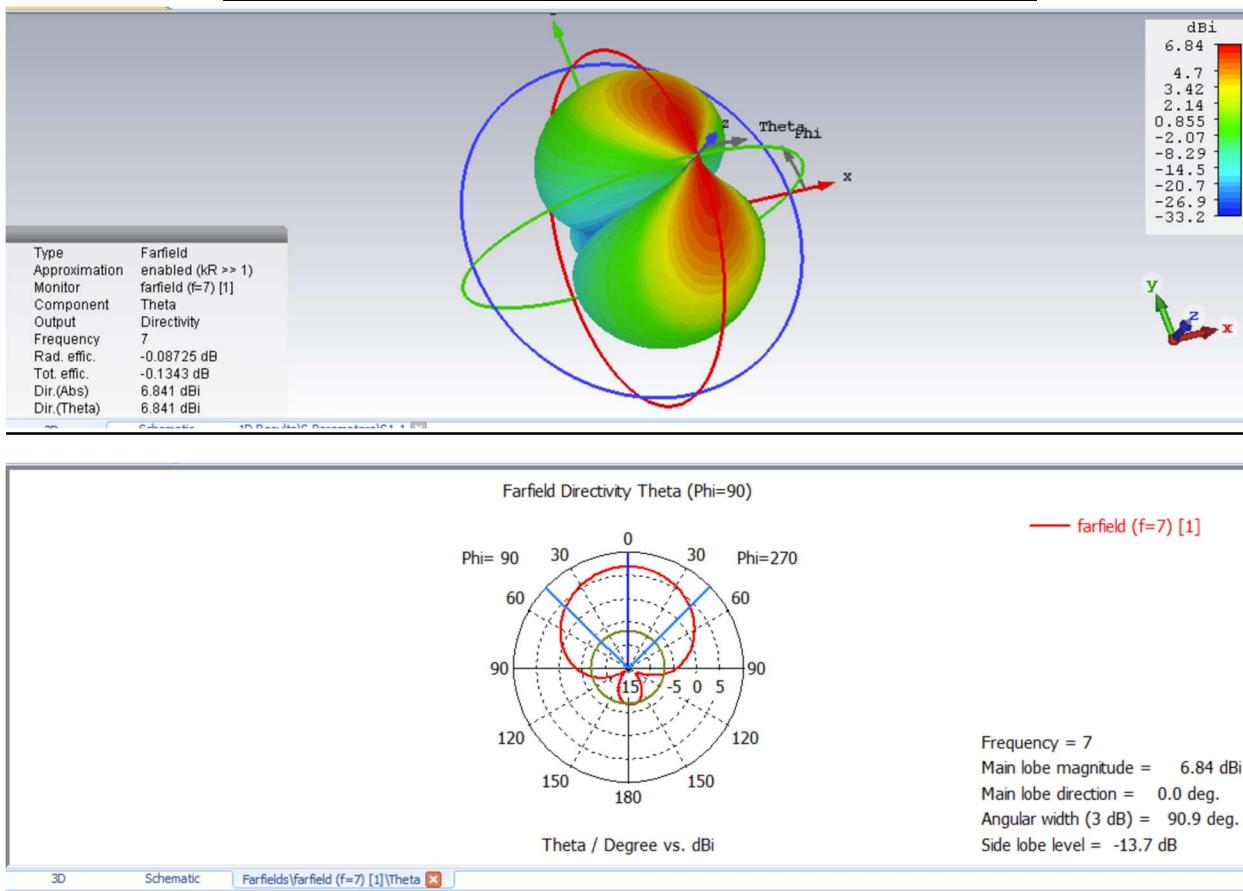
Screen 21: S11 magnitude



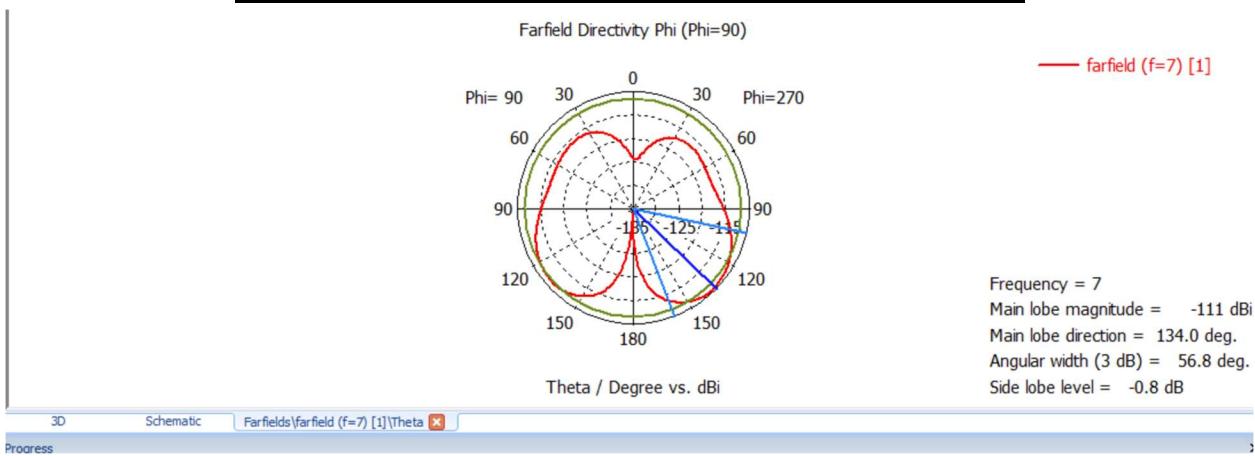
Screen 22: 3D far field radiation pattern

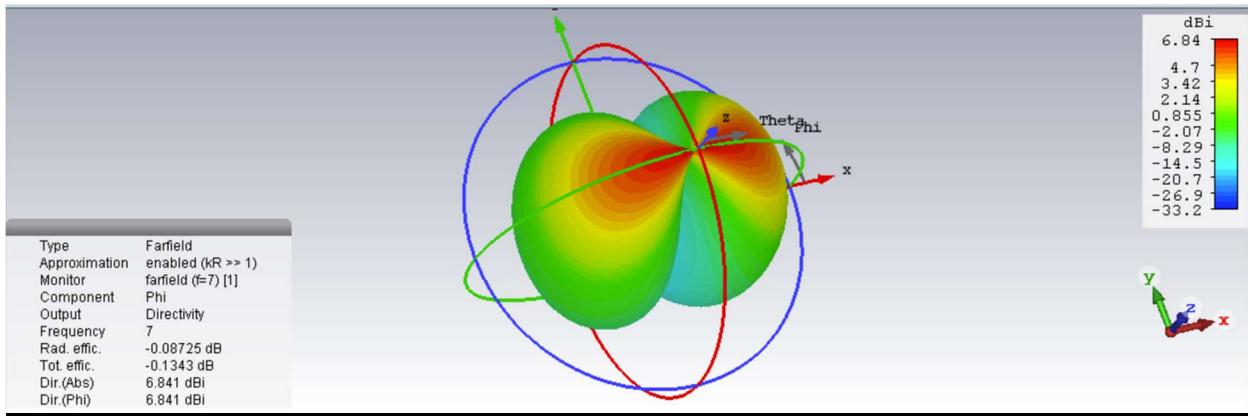


Screen 23: Elevation Radiation pattern, 3D and polar



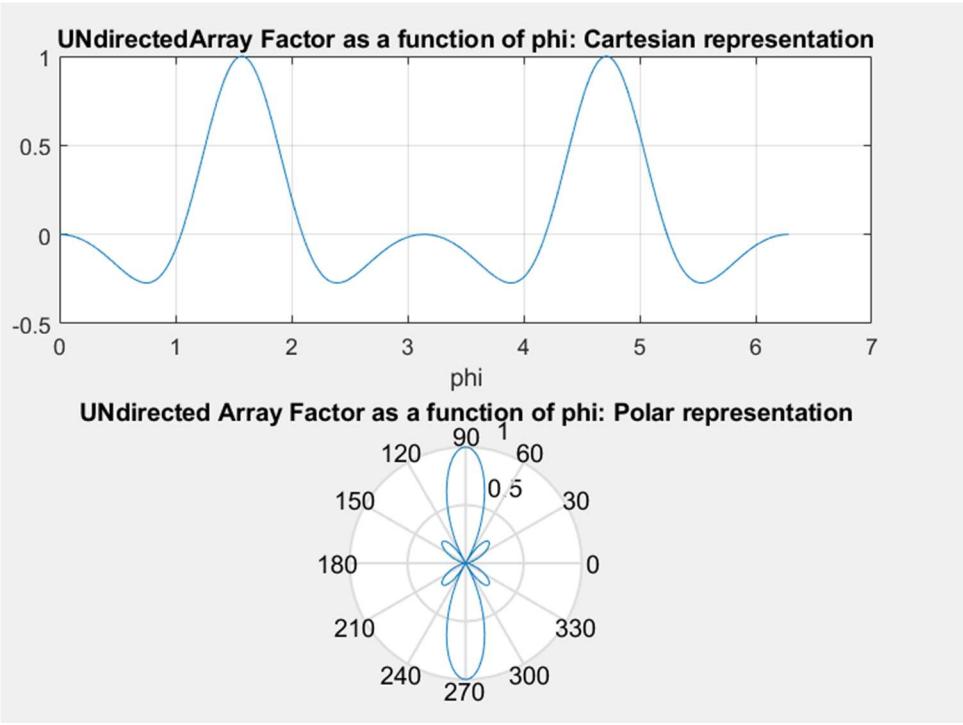
Screen 24: Azimuth Radiation pattern 3D and polar



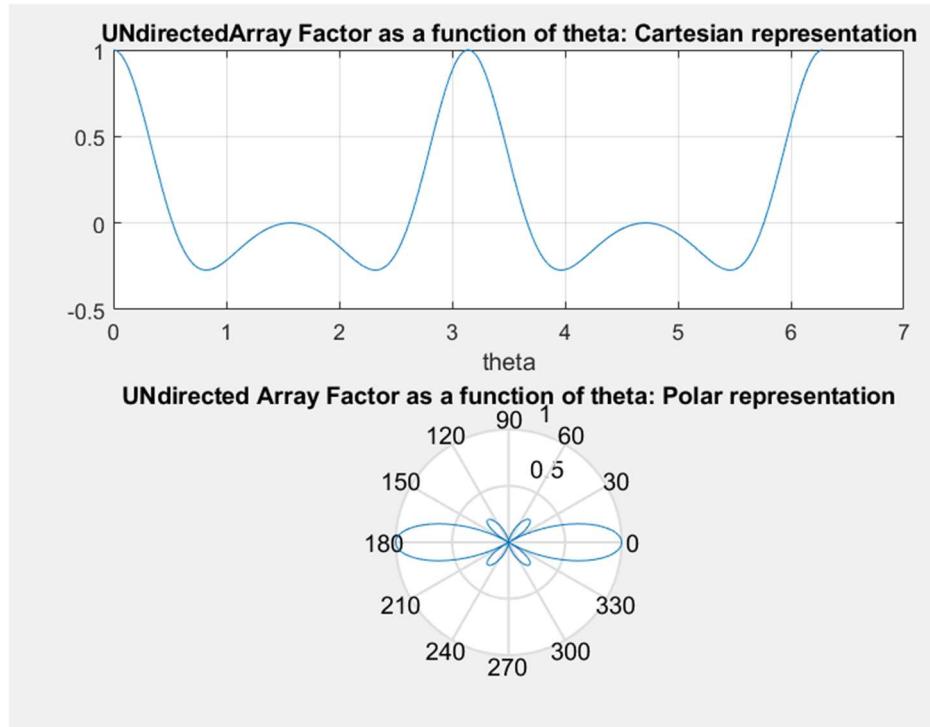


PART 5: ARRAY OF PATCH ANTENNA 4x1

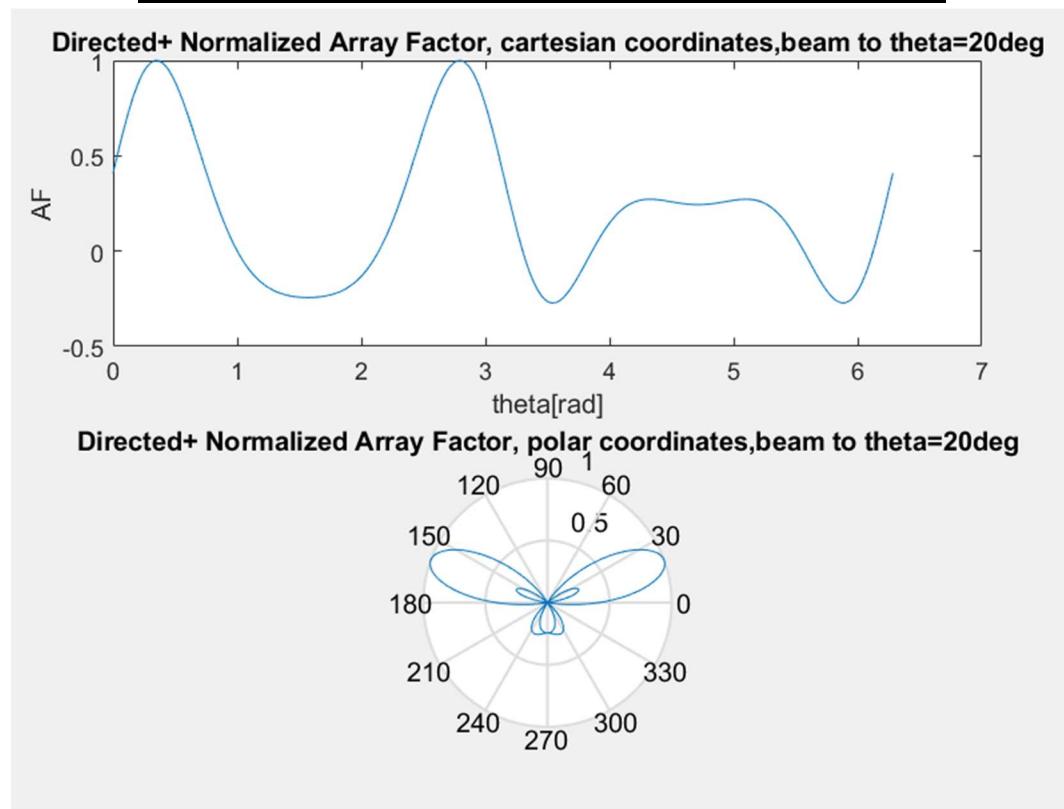
Screen 25: Undirected AF // phi



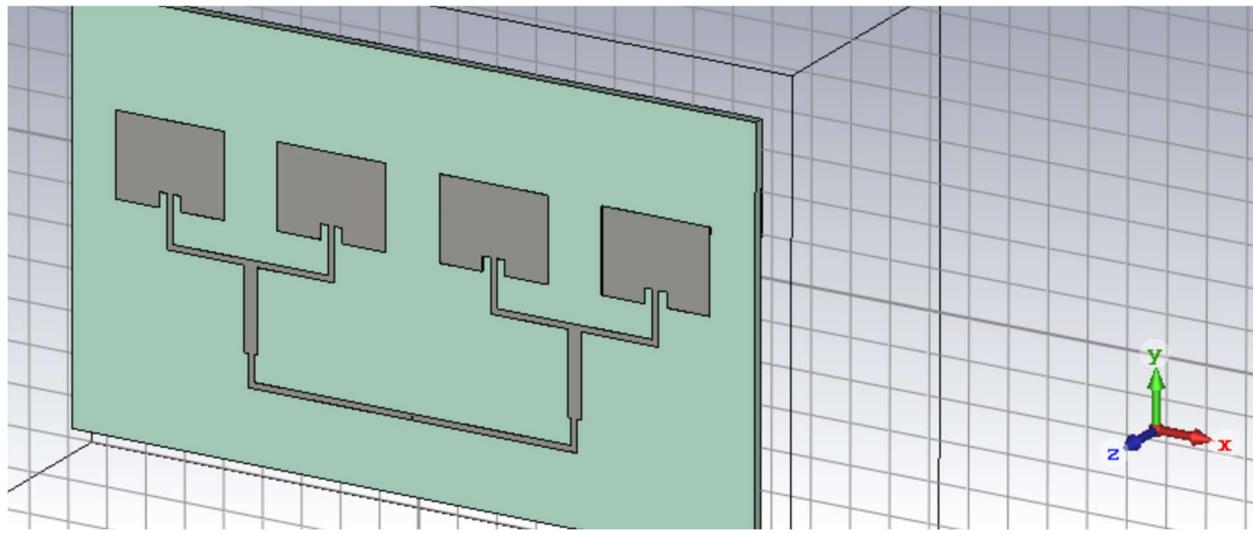
Screen 26: Undirected AF as a function of theta



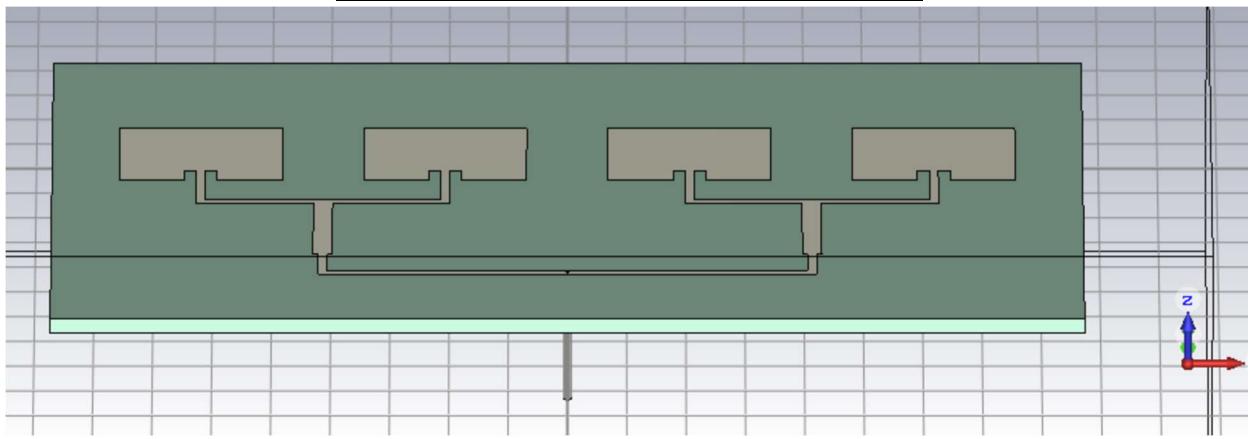
Screen 27: Directd and normalized AF (theta=20deg)



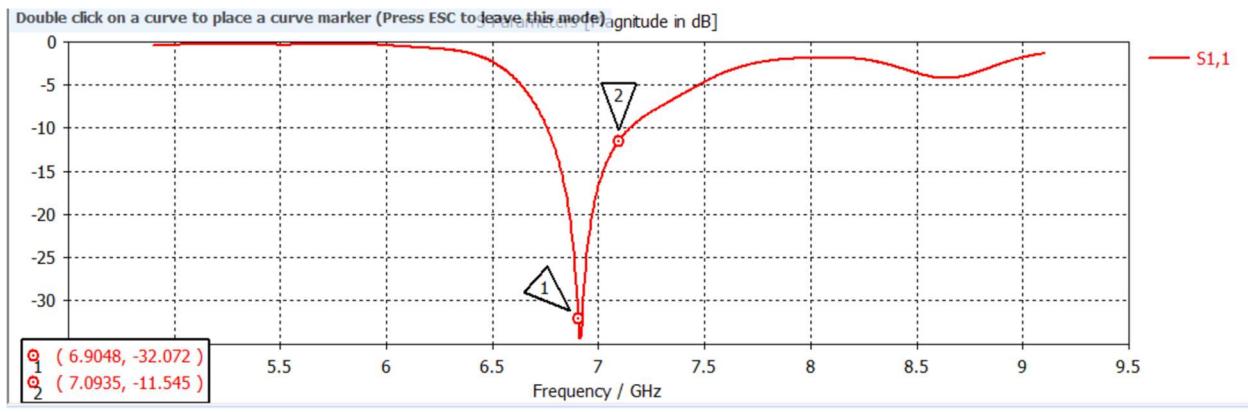
Screen 28: Patch Antenna perspective



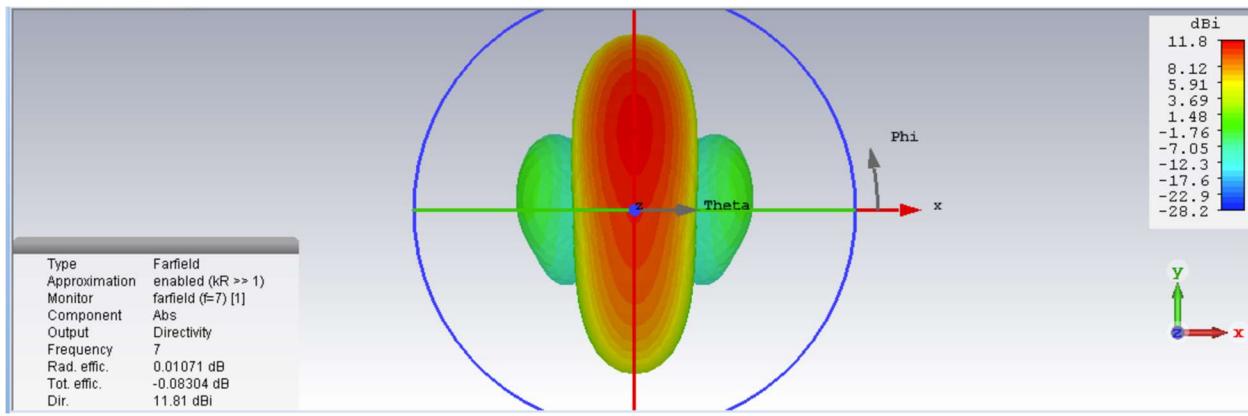
Screen 29: Patch Antenna perspective



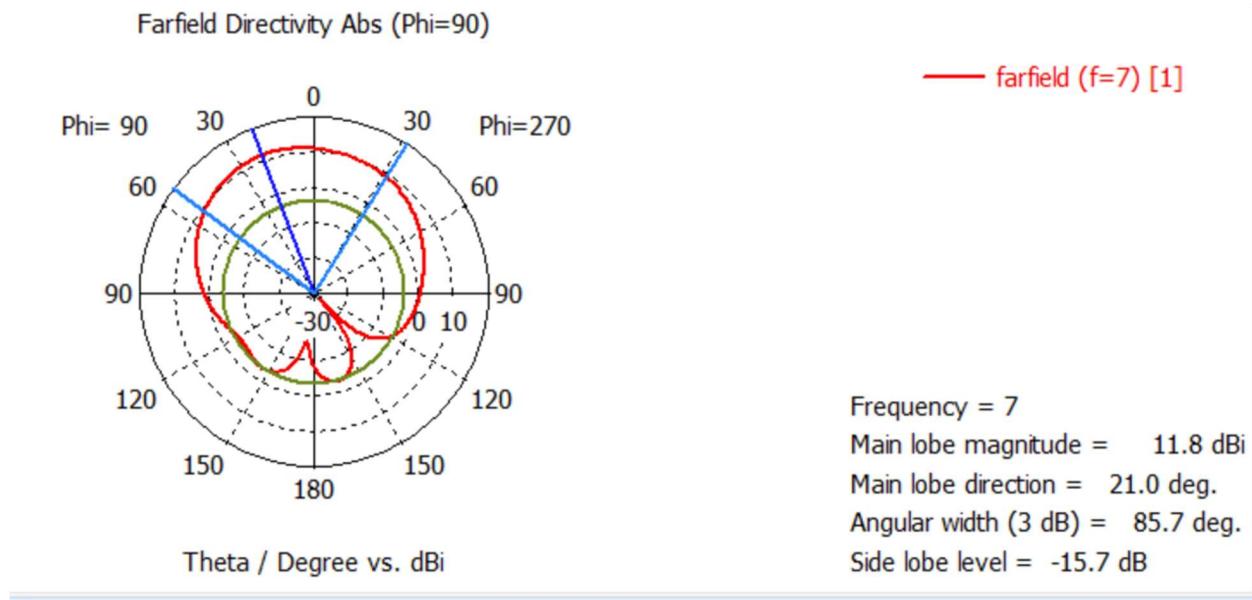
Screen 30: S11 magnitude matched at f=7GHz



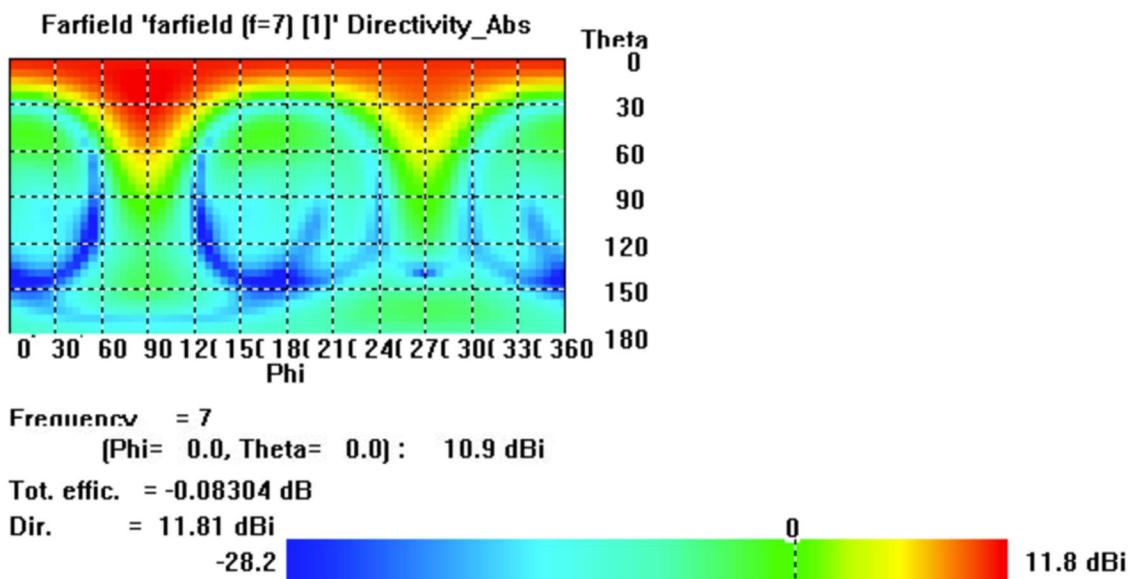
Screen 31: Radiation Pattern 3D



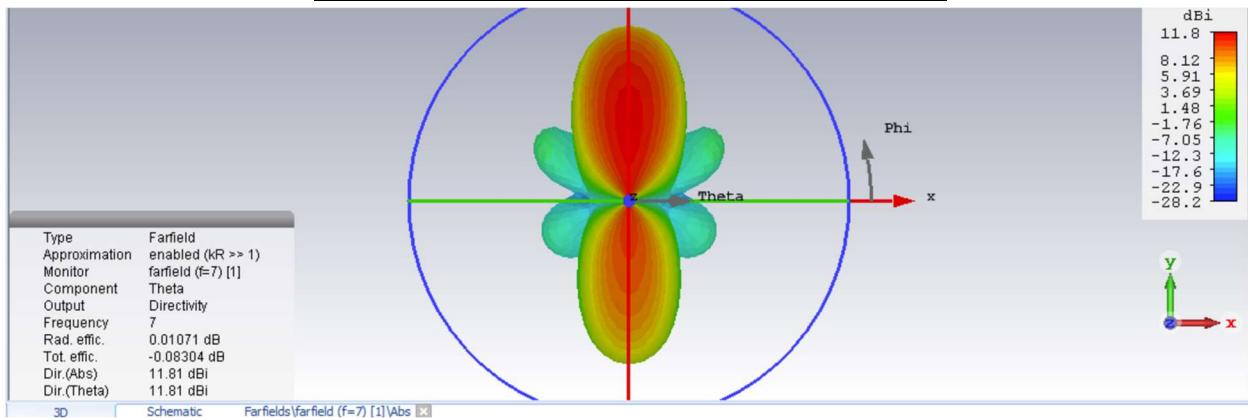
Screen 32: Radiation Pattern polar



Screen 33: Radiation Pattern 2D

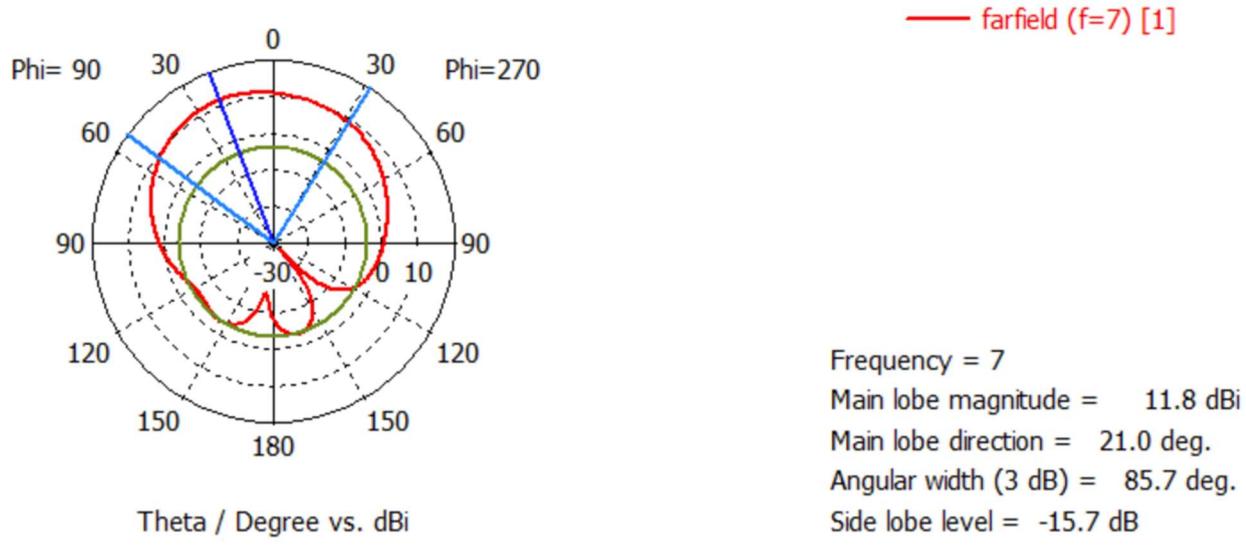


Screen 34: Azimuth Radiation Pattern 3D

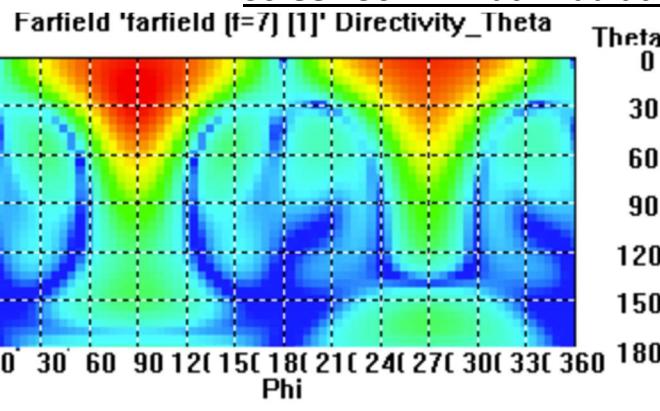


Screen 35: Azimuth Radiation Pattern polar

Farfield Directivity Theta (Phi=90)



Screen 36: Azimuth Radiation Pattern 2D



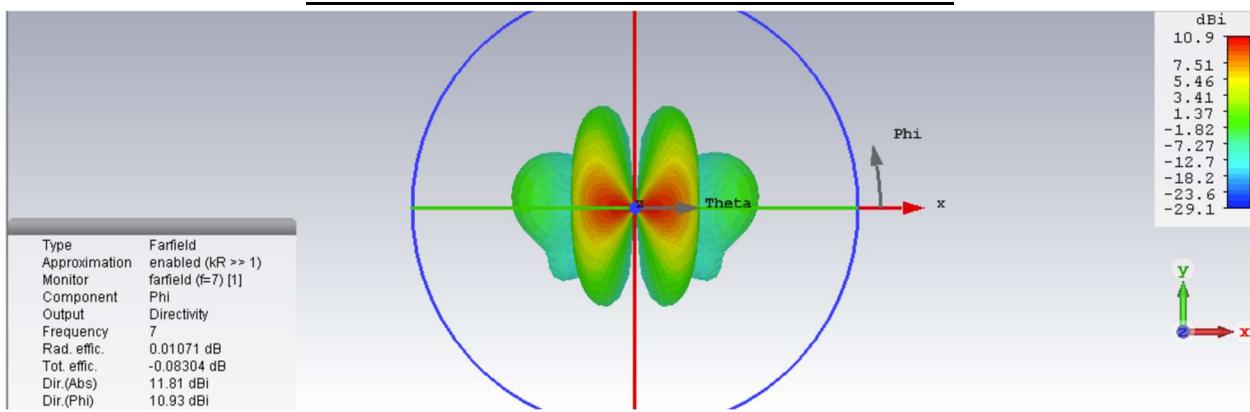
Frequency = 7
(Phi= 0.0, Theta= 5.0) : -19.9 dBi

Tot. effic. = -0.08304 dB

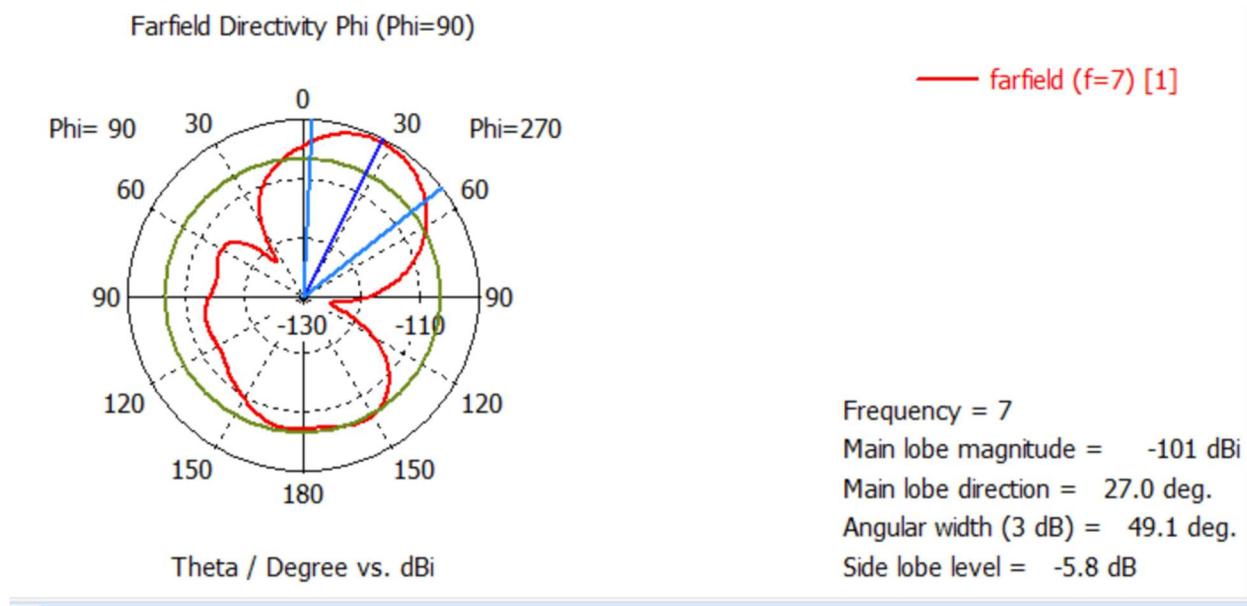
Dir.(Abs) = 11.81 dBi



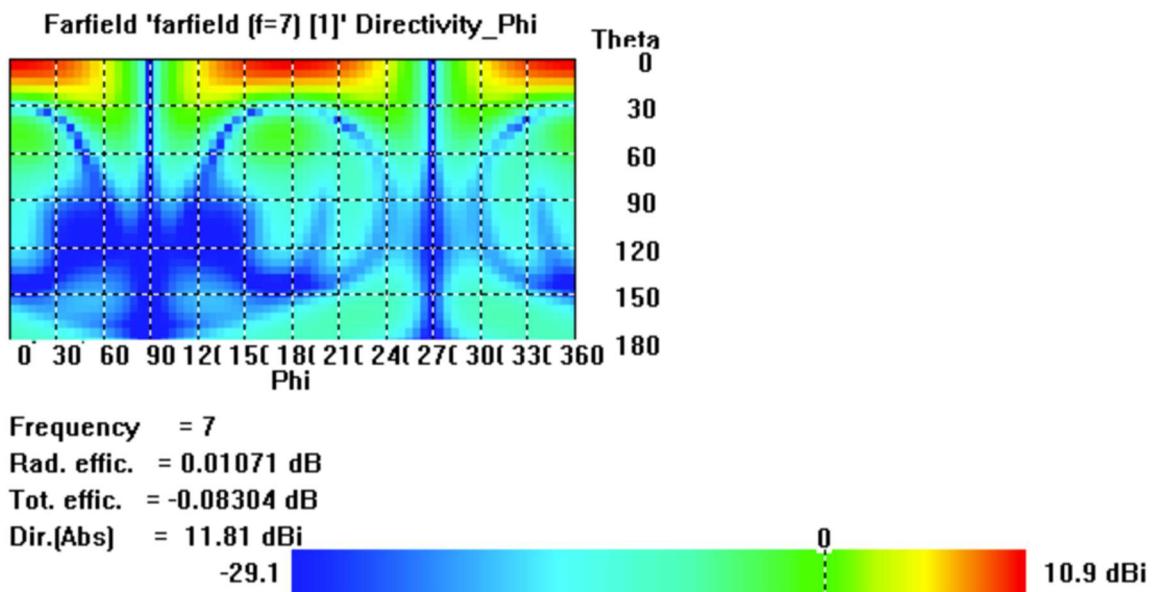
Screen 37: Elevation Radiation Pattern 3D



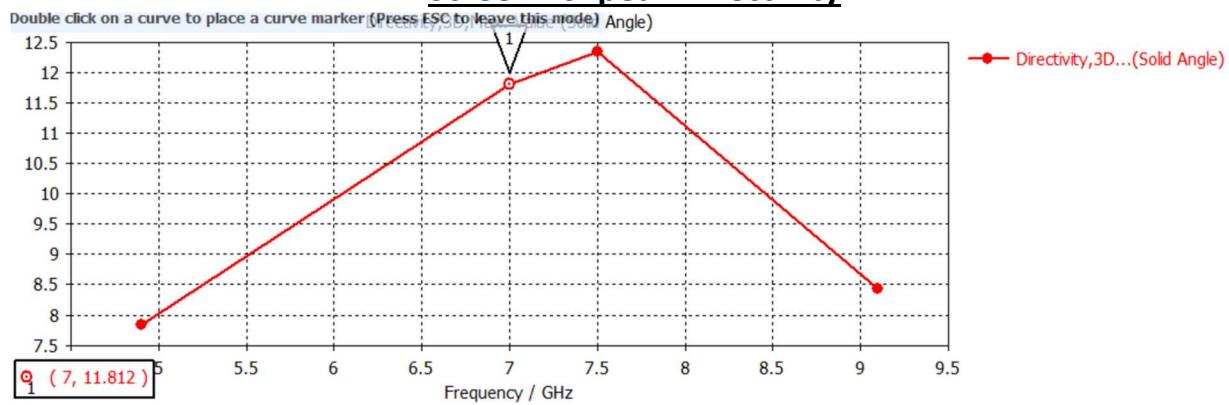
Screen 38: Elevation Radiation Pattern polar



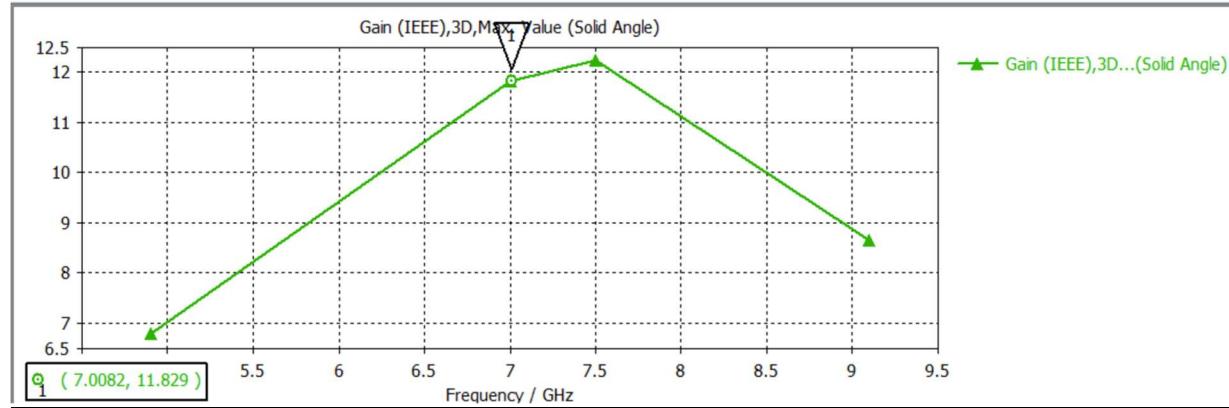
Screen 39: Elevation Radiation Pattern 2D



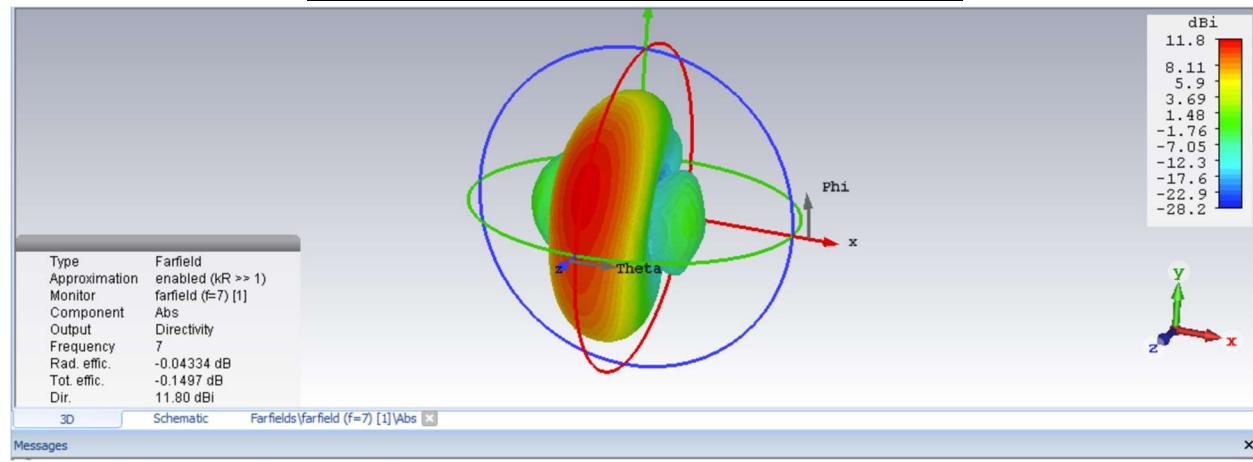
Screen 40: peak Directivity



Screen 41: Gain



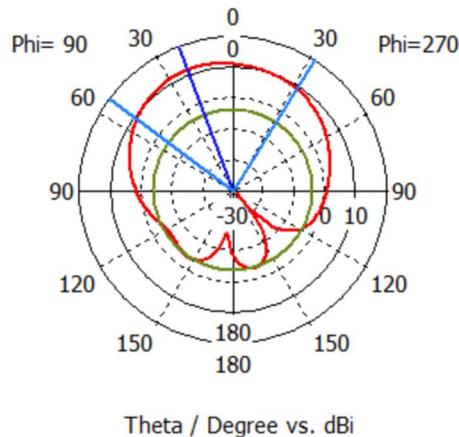
Screen 42: absolute Radiation pattern : 3D



Screen 43: absolute Radiation pattern : polar

Farfield Directivity Abs (Phi=90)

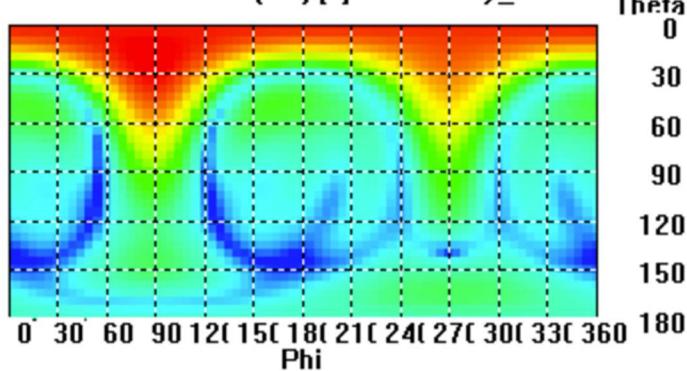
— farfield (f=7) [1]



Frequency = 7
Main lobe magnitude = 11.8 dBi
Main lobe direction = 21.0 deg.
Angular width (3 dB) = 85.8 deg.
Side lobe level = -15.6 dB

Screen 44: absolute Radiation pattern : 2D

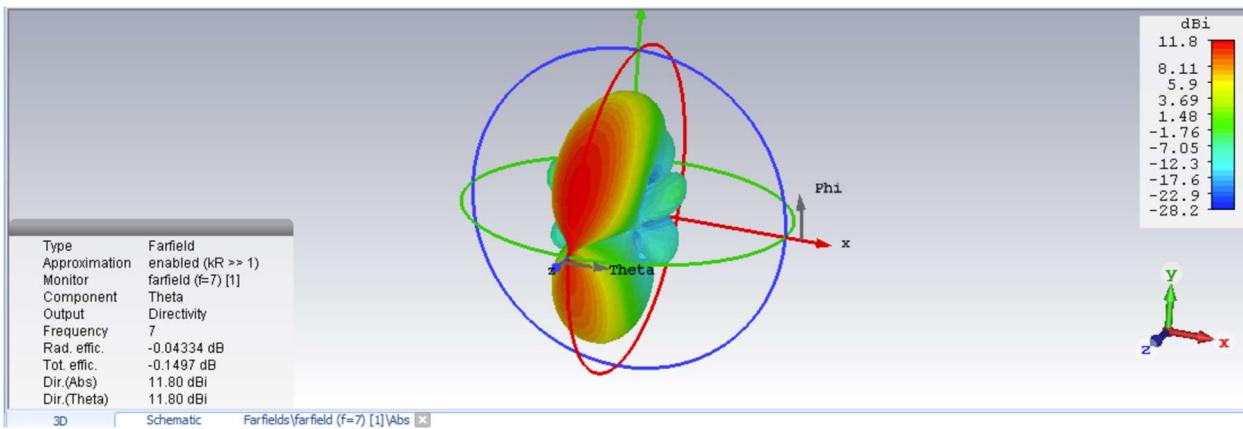
Farfield 'farfield (f=7) [1]' Directivity_Abs



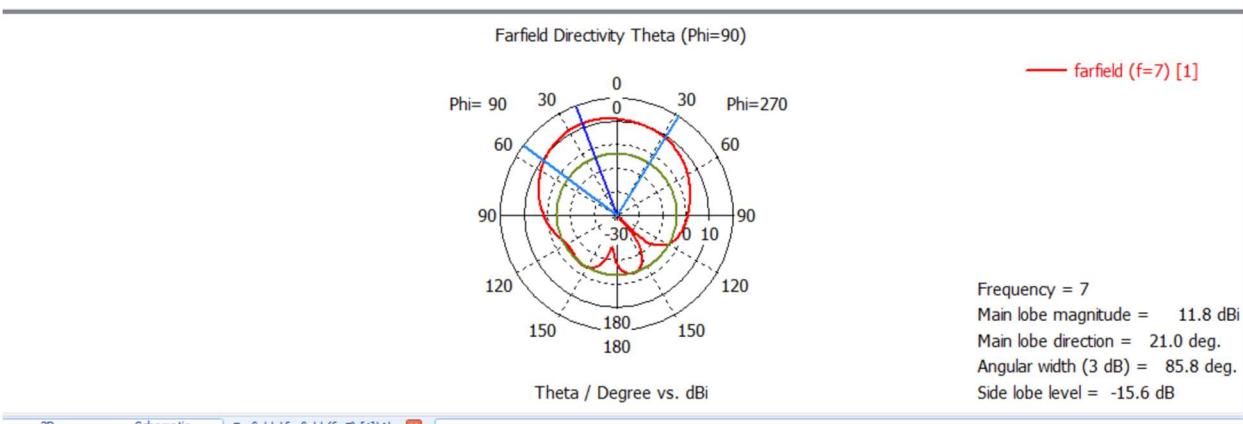
Frequency = 7
Rad. effic. = -0.04334 dB
Tot. effic. = -0.1497 dB
Dir. = 11.80 dBi

-28.2 0 11.8 dBi

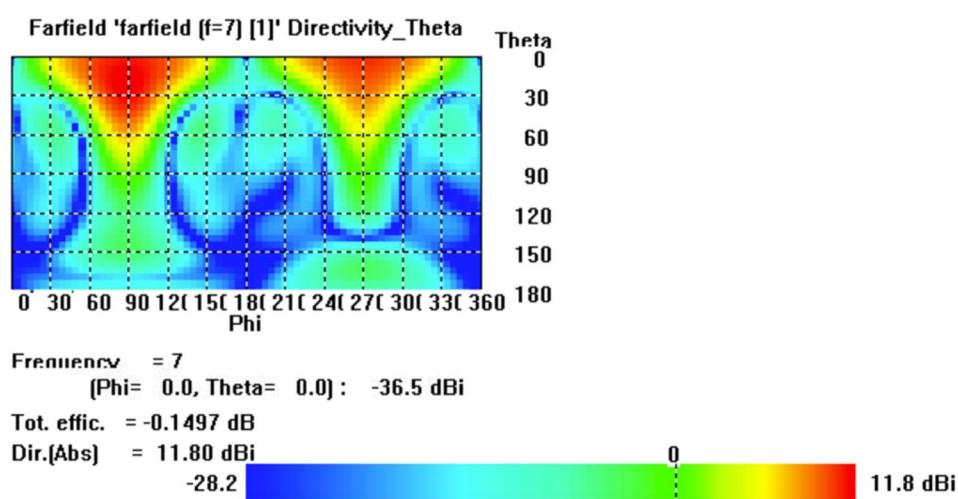
Screen 45: Azimuth Radiation pattern : 3D



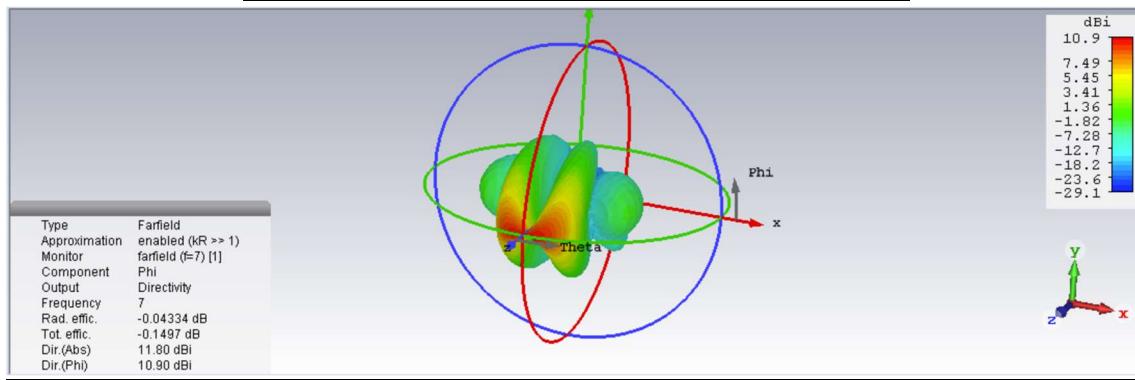
Screen 46: Azimuth Radiation pattern : polar



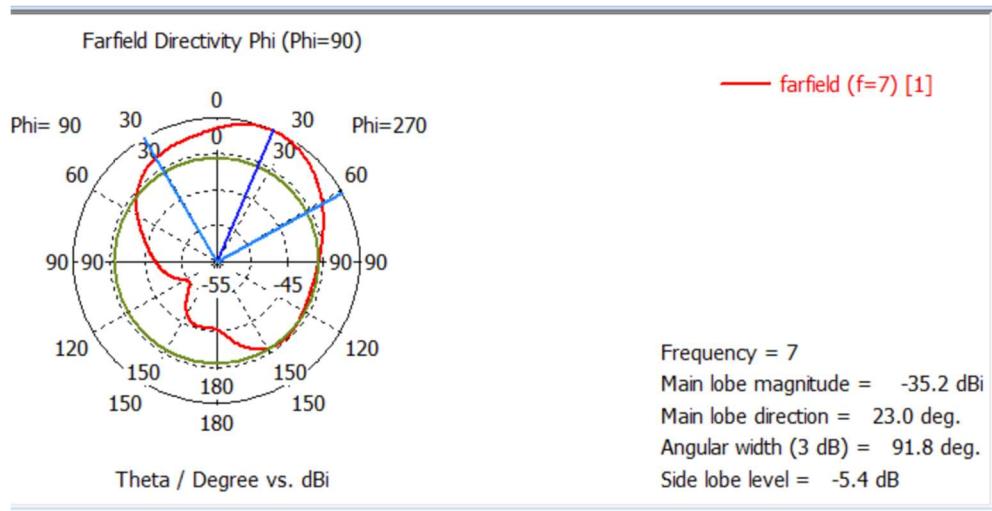
Screen 47: Azimuth Radiation pattern : 2D



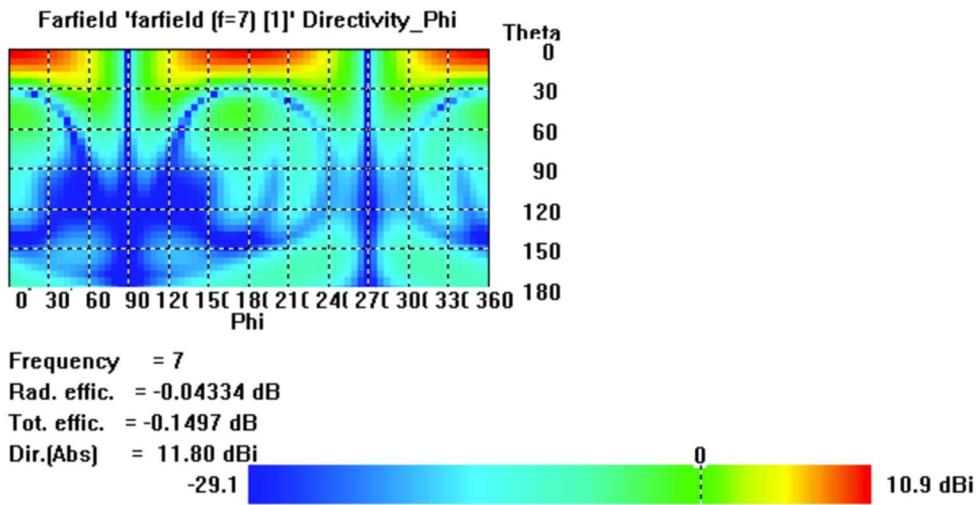
Screen 48: Elevation Radiation pattern : 3D



Screen 49: Elevation Radiation pattern : polar



Screen 50: Elevation Radiation pattern : 2D



Screen 51: Input matching S11

