DM_Project_ML

```
In [1]:
        import pandas as pd
        import numpy as np
        import seaborn as sns
        import matplotlib.pyplot as plt
        %matplotlib inline
        import talib
        import statsmodels.api as sm
        # from statsmodels.tsa.stattools import adfuller
        # from statsmodels.tsa.arima model import ARMA
        from sklearn.svm import LinearSVC
        from sklearn import linear model
In [2]: | df = pd.read_csv('fullsetmatrix1.csv', index_col='Time')
        df.index = pd.to datetime(df.index)
        print(df.head())
        n row, n col = df.shape
        print(f'There are {n row} rows and {n col} columns')
                             Unnamed: 0
                                            bch
                                                     btc
                                                             eth
                                                                    ltc
                                                                             xpr
        Time
        2018-08-15 18:45:00
                                                     NaN 297.56
                                            NaN
                                                                    NaN
                                                                             NaN
        2018-08-15 18:46:00
                                      1
                                            NaN 6547.42 297.81
                                                                    NaN
                                                                         0.29083
        2018-08-15 18:47:00
                                      2
                                            NaN 6549.43 297.82
                                                                         0.29084
                                                                    NaN
        2018-08-15 18:48:00
                                      3
                                            NaN 6547.86 298.37
                                                                    NaN 0.29010
        2018-08-15 18:49:00
                                      4 529.41 6534.95 297.94 58.07 0.29084
```

As we've already Identified previously, we have to deal with missing values (NaN) within our dataset. In our correlation analysis, we had backfilled our values. This time, let's follow a linear replacement method using the interpolate method(linear) that identifies all missing values and fills the values (a visualization will help make this clear) based on a linear path. We can also interpolate equivalent to the backfill method using # Interpolate using interpolation_type = 'zero'.

```
In [3]: def interpolate_and_plot(df, interpolation):
    # boolean mask for missing values
    missing_values = df.isna()

# Interpolating missing values
    prices_interp = df.interpolate(interpolation)

# plot while highlighting the interpolated values in black
    fig, ax = plt.subplots(figsize=(10, 5))
    prices_interp.plot(color='k', alpha=.6, ax=ax, legend=False)

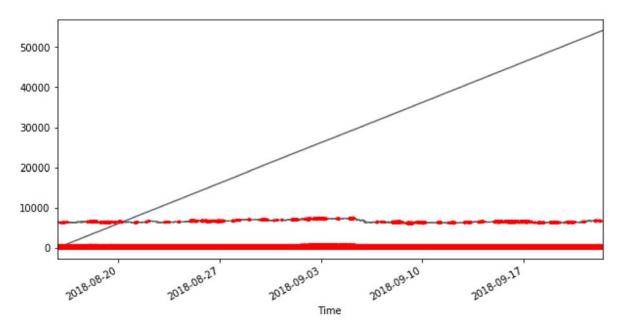
# plot while interpolated values on top in red
    prices_interp[missing_values].plot(ax=ax, color='r', lw=3, legend=False)
    plt.show()
```

12/13/2019

```
In [4]: # linear interpolation type
    interpolation_type = 'linear'
    interpolate_and_plot(df, interpolation_type)

# boolean mask for missing values
    missing_values = df.isna()

# Interpolating with missing values
    df = df.interpolate('linear')
    print(df.head(30))
```



	Unnamed: 0	bch	btc	eth	ltc
\					
Time					
2018-08-15 18:45:00	0	NaN	NaN	297.560000	NaN
2018-08-15 18:46:00	1	NaN	6547.42	297.810000	NaN
2018-08-15 18:47:00	2	NaN	6549.43	297.820000	NaN
2018-08-15 18:48:00	3	NaN	6547.86	298.370000	NaN
2018-08-15 18:49:00	4	529.410000	6534.95	297.940000	58.070000
2018-08-15 18:50:00	5	529.460000	6538.21	297.800000	58.090000
2018-08-15 18:51:00	6	529.156000	6542.46	297.400000	57.850000
2018-08-15 18:52:00	7	528.852000	6536.41	297.680000	57.940000
2018-08-15 18:53:00	8	528.548000	6534.12	297.453333	58.030000
2018-08-15 18:54:00	9	528.244000	6533.92	297.226667	57.925000
2018-08-15 18:55:00	10	527.940000	6519.39	297.000000	57.820000
2018-08-15 18:56:00	11	528.920000	6526.97	297.130000	57.860000
2018-08-15 18:57:00	12	529.132500	6536.53	297.680000	57.890000
2018-08-15 18:58:00	13	529.345000	6535.46	297.960000	57.920000
2018-08-15 18:59:00	14	529.557500	6538.06	297.740000	57.860000
2018-08-15 19:00:00	15	529.770000	6538.23	298.450000	57.930000
2018-08-15 19:01:00	16	529.448571	6534.19	298.180000	57.906667
2018-08-15 19:02:00	17	529.127143	6541.46	298.640000	57.883333
2018-08-15 19:03:00	18	528.805714	6532.36	298.070000	57.860000
2018-08-15 19:04:00	19	528.484286	6528.56	297.500000	57.850000
2018-08-15 19:05:00	20	528.162857	6526.58	298.200000	57.830000
2018-08-15 19:06:00	21	527.841429	6525.77	297.430000	57.720000
2018-08-15 19:07:00	22	527.520000	6520.03	296.700000	57.710000
2018-08-15 19:08:00	23	526.320000	6496.29	296.060000	57.510000
2018-08-15 19:09:00	24	525.040000	6488.99	294.800000	57.440000
2018-08-15 19:10:00	25	525.700000	6508.55	295.780000	57.460000
2018-08-15 19:11:00	26	525.720000	6504.21	296.200000	57.470000
2018-08-15 19:12:00	27	525.740000	6502.66	296.440000	57.310000
2018-08-15 19:13:00	28	525.720000	6498.05	296.130000	57.360000
2018-08-15 19:14:00	29	525.590000	6494.01	295.990000	57.360000
2010 00 13 13:11:00		323.330000	0151101	233,330000	37.300000
	xpr				
Time					
2018-08-15 18:45:00	NaN				
2018-08-15 18:46:00	0.29083				
2018-08-15 18:47:00	0.29084				
2018-08-15 18:48:00	0.29010				
2018-08-15 18:49:00	0.29084				
2018-08-15 18:50:00	0.29084				
2018-08-15 18:51:00	0.29084				
2018-08-15 18:52:00	0.29162				
2018-08-15 18:53:00	0.29158				
2018-08-15 18:54:00	0.29155				
2018-08-15 18:55:00	0.29000				
2018-08-15 18:56:00	0.29044				
2018-08-15 18:57:00	0.28944				
2018-08-15 18:58:00	0.28926				
2018-08-15 18:59:00	0.28927				
2018-08-15 19:00:00	0.28961				
2018-08-15 19:01:00	0.28946				
2018-08-15 19:02:00	0.28972				
2018-08-15 19:03:00	0.29100				
2018-08-15 19:04:00	0.28895				
2018-08-15 19:05:00	0.28981				
	-				

```
2018-08-15 19:06:00 0.28958

2018-08-15 19:07:00 0.28892

2018-08-15 19:08:00 0.28809

2018-08-15 19:09:00 0.28619

2018-08-15 19:10:00 0.28748

2018-08-15 19:11:00 0.28780

2018-08-15 19:12:00 0.28791

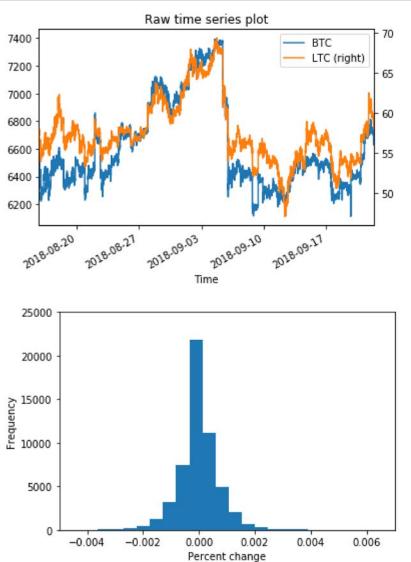
2018-08-15 19:13:00 0.28720

2018-08-15 19:14:00 0.28870
```

In continuation of using Bitcoin and Litecoin from our correlation methods, lets visualize a scatterplot with color relating to time, encoding time as the color of each datapoint. Bitcoin and Litecoin have drastically varying coin values, so we expect to yield interesting results and scale the y-axis. When not comparing coins, the Bitcoin data will be used as it is the most popular and expensive currency.

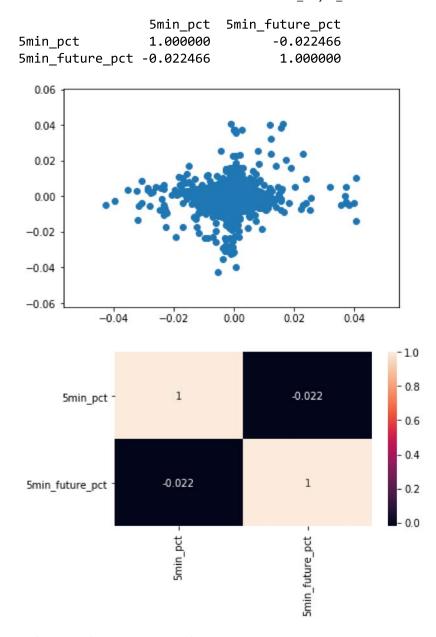
```
In [5]: # Raw time series plot of bitcoin and litecoin
    df['btc'].plot(label='BTC', legend=True)
    df['ltc'].plot(label='LTC', legend=True, secondary_y=True)
    plt.title('Raw time series plot')
    plt.show()
    plt.clf()

# Histogram of the daily price change percent
    df['btc'].pct_change().plot.hist(bins=80)
    plt.axis([-.005,.007,0,25000])
    plt.xlabel('Percent change')
    plt.show()
```



Above we can see a nearly normal distribution. Although we've done correlation analysis already, let's use Pearson's correlation coefficient to detect any linear relationships. We'll check the correlations between current price changes to see if previous price changes can predicture future ones. Below, based on the outputted correlation matrix between 5 day percentage changes (current and future), we can discern a slighly negative correlation (-0.0225) to the change in the last 5 days, an example of mean reversion (stock prices bounce around as opposed to following an upward trend).

```
In [6]: # 5-min % price changes for the current day, and 5 min in the future
        df['5min_future'] = df['btc'].shift(-5)
        df['5min_future_pct'] = df['5min_future'].pct_change(5)
        df['5min pct'] = df['btc'].pct change(5)
        # correlation matrix between 5-min percentage changes (current and future)
        corr = df[['5min_pct', '5min_future_pct']].corr()
        print(corr)
        # Scatter plot for current 5-day percent change vs the future 5-day percent ch
        ange
        plt.scatter(df['5min_pct'], df['5min_future_pct'])
        plt.show()
        # heatmap of correlation matrix
        sns.heatmap(corr, annot=True)
        plt.yticks(rotation=0); plt.xticks(rotation=90)
        plt.tight_layout() # fits plot area to the plot, "tightly"
        plt.show()
        plt.clf()
```



<Figure size 432x288 with 0 Axes>

Matrix and scatter plot show almost no correlation but let's now shift 15, 30, an hour, and even 200 minutes into our dataset to see what interesting correlations exist.

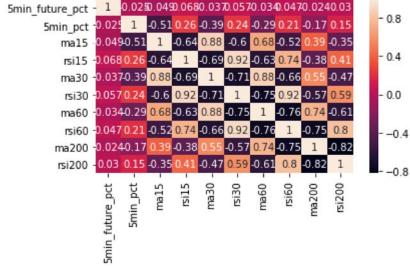
['5min_pct', 'ma15', 'rsi15', 'ma30', 'rsi30', 'ma60', 'rsi60', 'ma200', 'rsi 200']

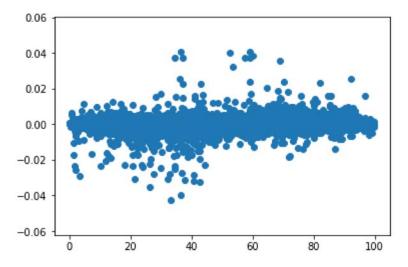
```
In [8]:
       # Drop all nan values
        df = df.dropna()
        # features and targets
        # use feature names for features; '5d close future pct' for targets
        features = df[feature names]
        targets = df['5min future pct']
        # DataFrame from target column and feature columns
        feature_and_target_cols = ['5min_future_pct'] + feature_names
        feat targ df = df[feature and target cols]
        # correlation matrix
        corr = feat targ df.corr()
        print(corr)
                       5min_future_pct
                                       5min_pct
                                                    ma15
                                                             rsi15
                                                                       ma30
        5min_future_pct
                              1.000000 -0.024809 -0.049370
                                                          0.067543 -0.036642
       5min pct
                             -0.024809 1.000000 -0.507850
                                                          0.257641 -0.394141
       ma15
                             -0.049370 -0.507850 1.000000 -0.635906
                                                                   0.880188
       rsi15
                              ma30
                             -0.036642 -0.394141 0.880188 -0.688924
                                                                   1.000000
       rsi30
                              0.057358 0.240323 -0.595650
                                                          0.921034 -0.706848
       ma60
                             -0.034052 -0.294055 0.683584 -0.629773
                                                                   0.883533
       rsi60
                              0.047460 0.214338 -0.521254
                                                          0.737546 -0.656622
       ma200
                             -0.023550 -0.168327 0.393767 -0.380312
                                                                   0.547663
       rsi200
                              0.029912 0.148689 -0.349523
                                                          0.410310 -0.469646
                          rsi30
                                     ma60
                                             rsi60
                                                      ma200
                                                               rsi200
       5min_future_pct  0.057358 -0.034052  0.047460 -0.023550
                                                             0.029912
                       0.240323 -0.294055 0.214338 -0.168327
       5min pct
                                                             0.148689
       ma15
                      -0.595650 0.683584 -0.521254
                                                   0.393767 -0.349523
       rsi15
                       0.921034 -0.629773 0.737546 -0.380312
                                                             0.410310
       ma30
                      rsi30
                       1.000000 -0.745121 0.922238 -0.567929
                                                             0.594106
       ma60
                      -0.745121 1.000000 -0.764499 0.736713 -0.605972
       rsi60
                       0.922238 -0.764499
                                          1.000000 -0.754970
                                                             0.801569
                      -0.567929 0.736713 -0.754970 1.000000 -0.822154
       ma200
                       0.594106 -0.605972 0.801569 -0.822154
       rsi200
                                                             1.000000
```

We can see some high correlations for relative strength index (RSI) rsi60 and rsi30, moving average (ma) ma60 and ma200, rsi15 and rsi30, and strong negative correlation between ma200 and rsi200, ma60 and rsi30. Compared to the target ['5min future pct'], rsi15 has the highest correlation at 0.066734.

```
In [9]: # heatmap of correlation matrix
    sns.heatmap(corr, annot=True)
    plt.yticks(rotation=0); plt.xticks(rotation=90) # fix ticklabel directions
    plt.tight_layout() # fits plot area to the plot, "tightly"
    plt.show() # show the plot
    plt.clf() # clear the plot area

# scatter plot of the most highly correlated variable with the target
    plt.scatter(df['rsi15'], df['5min_future_pct'])
    plt.show()
```





Let's now set up training dataset to be used for preparing some prediction models and compare various performances between models discussed in our class such as decisions trees and k-nearest neighbors. Let's also take a look to see which features have the more importance in strengthening prediction models.

```
In [10]: # Adding a constant to the features
linear_features = sm.add_constant(features)

# size for the training set that is 85% of the number of samples
train_size = int(0.85 * features.shape[0])
train_features = linear_features[:train_size]
train_targets = targets[:train_size]
test_features = linear_features[train_size:]
test_targets = targets[train_size:]
print(linear_features.shape, train_features.shape, test_features.shape)
```

```
((53844, 10), (45767, 10), (8077, 10))
```

C:\ProgramData\Anaconda2\lib\site-packages\numpy\core\fromnumeric.py:2389: Fu tureWarning: Method .ptp is deprecated and will be removed in a future versio n. Use numpy.ptp instead.

return ptp(axis=axis, out=out, **kwargs)

```
In [11]: # Linear model and Least squares fit
    model = sm.OLS(train_targets, train_features)
    results = model.fit()
    print(results.summary())

# examine pvalues
# Features with p <= 0.05 are typically considered significantly different fro
    m 0
    print(results.pvalues)

# Make predictions from our model for train and test sets
    train_predictions = results.predict(train_features)
    test_predictions = results.predict(test_features)</pre>
```

OLS Regression Results

OLS Regression Results										
= Dep. Varia	able: 5min_future_pct		pct R-squ	ared:	0.01					
0 Model:				R-squared:	0.01					
0 Method:		Least Squa	_	F-statistic:						
1					52.5					
Date: 5	Т	hu, 12 Dec 2	019 Prob	(F-statisti	c): 1.38e-9					
Time: 5		18:19:08 Log-Likelihood:			2.2534e+0					
No. Observ	vations:	45767 AIC:		-4.507e+0						
5 Df Residua	als:	45757 BIC:		-4.506e+0						
5 Df Model:			9							
	ovariance Type: nonrobust									
=										
5]	coef	std err	t	P> t	[0.025	0.97				
const	0.0291	0.005	6.367	0.000	0.020	0.03				
8 5min_pct	-0.0730	0.005	-13.424	0.000	-0.084	-0.06				
2 ma15 9	-0.0741	0.007	-9.918	0.000	-0.089	-0.05				
rsi15 5	1.901e-05	2.2e-06	8.658	0.000	1.47e-05	2.33e-0				
ma30	0.0614	0.008	7.978	0.000	0.046	0.07				
6 rsi30 5	-3.595e-05	6.33e-06	-5.681	0.000	-4.84e-05	-2.35e-0				
ma60 1	-0.0197	0.005	-4.305	0.000	-0.029	-0.01				
rsi60 5	3.344e-05	6.97e-06	4.799	0.000	1.98e-05	4.71e-0				
ma200 6	0.0029	0.002	1.703	0.089	-0.000	0.00				
_	-7.131e-06	4.39e-06	-1.624	0.104	-1.57e-05	1.47e-0				
=======================================		========	=======	=======	=======	=======				
Omnibus: 2		22875.	873 Durbi	n-Watson:		0.44				
Prob(Omnib	ous):	0.000		e-Bera (JB)	: 16183011.10					
Skew:		-0.991 Prob(JB):		ЈВ):		0.0				
0 Kurtosis:		95.	100 Cond.	No.		1.32e+0				
5										
=										

Warnings:

[1] Standard Errors assume that the covariance matrix of the errors is correctly specified.

[2] The condition number is large, 1.32e+05. This might indicate that there a

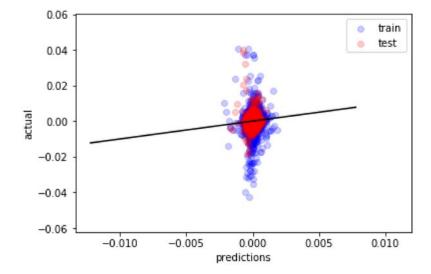
strong multicollinearity or other numerical problems.

```
1.940938e-10
const
5min_pct
            5.229623e-41
            3.654897e-23
ma15
rsi15
            4.950980e-18
ma30
            1.520806e-15
rsi30
            1.344531e-08
            1.674716e-05
ma60
rsi60
            1.596126e-06
ma200
            8.853014e-02
rsi200
            1.043581e-01
dtype: float64
```

```
In [12]: # Scatter the predictions vs the targets with 80% transparency
    plt.scatter(train_predictions, train_targets, alpha=0.2, color='b', label='tra
    in')
    plt.scatter(test_predictions, test_targets, alpha=0.2, color='r', label='test'
)

# Plot the perfect prediction line
    xmin, xmax = plt.xlim()
    plt.plot(np.arange(xmin, xmax, 0.01), np.arange(xmin, xmax, 0.01), c='k')

# Set the axis labels and show the plot
    plt.xlabel('predictions')
    plt.ylabel('actual')
    plt.legend()# show the legend
    plt.show()
```



Let's try a different non-linear machine learning model and begin using decision trees. Decision trees will split our data into groups based on the features (set earlier). We will determine which max_depth can provide the best prediction without overfitting.

```
In [13]: from sklearn.tree import DecisionTreeRegressor

# decision tree regression model with default arguments
decision_tree = DecisionTreeRegressor()

# Fit the model to the training features and targets
decision_tree.fit(train_features, train_targets)

# Checking score on train and test
print(decision_tree.score(train_features, train_targets))
print(decision_tree.score(test_features, test_targets))

0.9869864862576161
-1.1325294323005517
```

A near perfect fit on our training data, but our testing data isn't up to par.

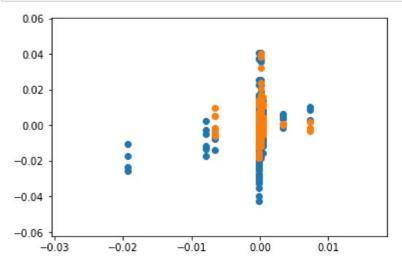
```
In [14]: # Loop through a few different max depths and check the performance
         for d in [3,5,10]:
             # fitting decision tree
             decision tree = DecisionTreeRegressor(max depth = d)
             decision_tree.fit(train_features, train_targets)
             # scores on train and test
             print('max_depth=', str(d))
             print(decision tree.score(train features, train targets))
             print(decision tree.score(test features, test targets), '\n')
         ('max_depth=', '3')
         0.022637132863564946
         (-0.02124880489764669, '\n')
         ('max_depth=', '5')
         0.03760310283870938
         (-0.010740412135679554, '\n')
         ('max depth=', '10')
         0.14322382770387543
         (-0.17721610809276678, '\n')
```

We can see above that the best fit is a max depth of 3 at a score of -0.02125. Below, we would want to see diagonal lines from the lower left to the upper right. However, due to the simplistic nature of decisions trees, our model is not going to do well on the test set. But it will do well on the train set. As seen below, the predictions group into lines due our limited depth.

```
In [15]: # Using best max_depth of 3 to fit a decision tree
    decision_tree = DecisionTreeRegressor(max_depth=3)
    decision_tree.fit(train_features, train_targets)

# Prediction values for train and test
    train_predictions = decision_tree.predict(train_features)
    test_predictions = decision_tree.predict(test_features)

# Scatter the predictions vs actual values
    plt.scatter(train_predictions, train_targets, label='train')
    plt.scatter(test_predictions, test_targets, label='test')
    plt.show()
```



Now that we've examined decision trees, let's briefly look at a random forest model. We will use random sample of training data points to test our results. Let's now examine a random forest model and determine its use for prediction on our dataset. Here, a random forest is made up of multiple decision trees (Reference: https://towardsdatascience.com/an-implementation-and-explanation-of-the-random-forest-in-python-77bf308a9b76)).

```
In [17]: from sklearn.ensemble import RandomForestRegressor

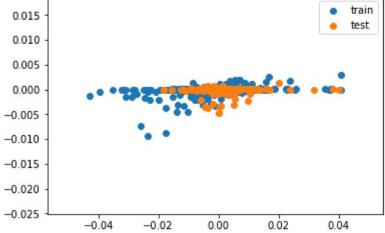
# Create the random forest model and fit to the training data
rfr = RandomForestRegressor(n_estimators=200)
rfr.fit(train_features, train_targets)

# Look at the R^2 scores on train and test
print(rfr.score(train_features, train_targets))
print(rfr.score(test_features, test_targets))
```

0.877225303943836
-0.07967858139001449

We could use sklearn's GridSearchCV() method to search hyperparameters, but with a financial time series, we don't want to do cross-validation due to data mixing. We want to fit our models on the oldest data and evaluate on the newest data. So we'll use sklearn's ParameterGrid to create combinations of hyperparameters to search.

```
from sklearn.model selection import ParameterGrid
In [18]:
         # dictionary of hyperparameters to search
         grid = {'n_estimators': [200], 'max_depth': [3], 'max_features': [4, 8], 'rand
         om_state': [42]}
         test scores = []
         # Loop through parameter grid, set the hyperparameters, and save the scores
         for g in ParameterGrid(grid):
             rfr.set params(**g) # ** is used to unpack the dictionary
             rfr.fit(train_features, train_targets)
             test_scores.append(rfr.score(test_features, test_targets))
         # best hyperparameters from the test score
         best_idx = np.argmax(test_scores)
         print(test scores[best idx], ParameterGrid(grid)[best idx])
         (0.0010660902851407084, {'n_estimators': 200, 'max_features': 4, 'random stat
         e': 42, 'max depth': 3})
         # Using the best hyperparameters from before to fit a random forest model
In [19]:
         rfr = RandomForestRegressor(n_estimators=200, max_depth=3, max_features=4, ran
         dom state=42)
         rfr.fit(train features, train targets)
         # predictions with our model
         train predictions = rfr.predict(train features)
         test_predictions = rfr.predict(test_features)
         # scatter plot with train/test actual vs predictions
         plt.scatter(train targets, train predictions, label='train')
         plt.scatter(test_targets, test_predictions, label='test')
         plt.legend()
         plt.show()
```

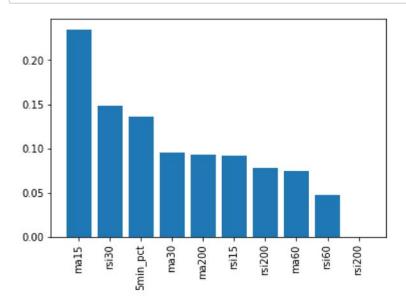


```
In [20]: # Get feature importances from our random forest model
    importances = rfr.feature_importances_

# Get the index of importances from greatest importance to least
    sorted_index = np.argsort(importances)[::-1]
    x = range(len(importances))

# Create tick labels
    labels = np.array(feature_names)[sorted_index-1]
    plt.bar(x, importances[sorted_index], tick_label=labels)

# Rotate tick labels to vertical
    plt.xticks(rotation=90)
    plt.show()
```



We can see moving average 200 and 15 minutes along with relative strength index 200 minutes as the most contributing features to the predictions. Let's focus on these features to possibly enhance/tune them for even strong predictions.

0.045743334887100806-0.0005489804798382014

From random forest, the scores for train/test were 0.8733246218778411 and -0.08374728278454358.

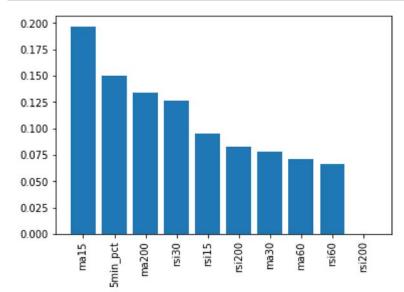
```
In [22]: # Extract feature importances from the fitted gradient boosting model
    feature_importances = gbr.feature_importances_

# Get the indices of the largest to smallest feature importances
    sorted_index = np.argsort(feature_importances)[::-1]
    x = range(len(feature_importances))

# Create tick labels
    labels = np.array(feature_names)[sorted_index-1]

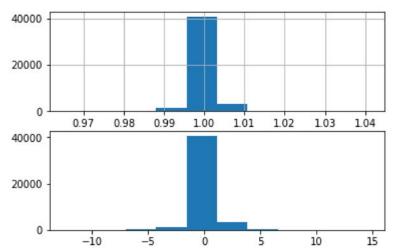
plt.bar(x, feature_importances[sorted_index], tick_label=labels)

# tick lables corresponding to feature names
plt.xticks(rotation=90)
plt.show()
```



Now let's try k nearest neighbors method. As discussed in lecture, KNN takes the k-nearest points to a new point and averages their target values to obtain a prediction. By implementing scale() method, we will try normalizing the data so the features have similar ranges.

In [23]: from sklearn.preprocessing import scale from sklearn.neighbors import KNeighborsRegressor # Standardize the train and test features scaled train features = scale(train features) scaled_test_features = scale(test_features) # histogram before and after scaling (model might work better with dataset spr ead over different timeframe) f, ax = plt.subplots(nrows=2, ncols=1) train_features.iloc[:, 2].hist(ax=ax[0]) ax[1].hist(scaled_train_features[:, 2]) plt.show() for n in range(30, 38): # fitting the KNN model knn = KNeighborsRegressor(n_neighbors=n) # Fitting model to the training data knn.fit(scaled train features, train targets) # number of neighbors score of best value of n print("n neighbors =", n) print('train, test scores') print(knn.score(scaled_train_features, train_targets)) print(knn.score(scaled test features, test targets)) print() # prints a blank line



```
('n_neighbors =', 30)
train, test scores
0.10782220799700026
-0.013995328953734454
()
('n_neighbors =', 31)
train, test scores
0.10514583128183375
-0.016980153515271157
('n_neighbors =', 32)
train, test scores
0.1039407977744532
-0.014317057907725417
('n_neighbors =', 33)
train, test scores
0.10043221657940804
-0.014470602720116466
()
('n_neighbors =', 34)
train, test scores
0.09858075168241198
-0.01264357622191592
()
('n_neighbors =', 35)
train, test scores
0.09630948922517257
-0.01273101911610275
()
('n_neighbors =', 36)
train, test scores
0.09406456360023208
-0.01318752638125309
()
('n_neighbors =', 37)
train, test scores
0.0920245073829623
-0.013343701836921351
()
```

After plugging and testing a various range of values, we can choose n-neighbors 34 for optimal model.

```
In [24]: # model with the best-performing n_neighbors of 34
knn = KNeighborsRegressor(n_neighbors=34)

# Fit the model
knn.fit(scaled_train_features, train_targets)

# predictions for train and test sets
train_predictions = knn.predict(scaled_train_features)
test_predictions = knn.predict(scaled_test_features)

# plotting actual vs predicted values
plt.scatter(train_predictions, train_targets, label='train')
plt.scatter(test_predictions, test_targets, label='test')
plt.legend()
plt.show()
```

