

Lauren Fromm
404751250
CS 161

HW 6

1.

- a) $\{x/A, y/B, z/C\}$
- b) No unifier exists: $\{y/G(x,x)\} \rightarrow x/A$ and x/B ?
- c) $\{x/A, y/A\}$
- d) $\{x/John, y/John\}$
- e) No unifier exists: $\{x/y\} \rightarrow x \neq \text{father}(x)$

2.

a)

Basic functions: $\text{food}(a)$, $\text{likes}(\text{liker}, \text{likee})$, $\text{eats}(\text{eater}, \text{food})$, $\text{killed}(\text{killed}, \text{killer})$, $\text{alive}(b)$

John likes all kinds of food

$(\forall x) (\text{food}(x) \Rightarrow \text{likes}(\text{john}, x))$

Apples are food

$\text{food}(\text{apples})$

Chicken is food

$\text{food}(\text{chicken})$

Anything someone eats and isn't killed by is food

$(\forall x) ((\exists y) ((\text{eats}(y, x) \ \& \ \sim \text{killed}(y, x)) \Rightarrow \text{food}(x)))$

If you are killed by something, you are not alive

$(\forall y, x) ((\text{killed}(y, x) \Rightarrow \sim \text{alive}(y)))$

Bill eats peanuts and is still alive

$(\text{eats}(\text{bill}, \text{peanuts}) \ \& \ \text{alive}(\text{bill}))$

Sue eats everything Bill eats

$(\forall x) (\text{eats}(\text{bill}, x) \Rightarrow \text{eats}(\text{Sue}, x))$

b)

$(\forall x) (\text{food}(x) \Rightarrow \text{likes}(\text{john}, x))$

$(\sim \text{food}(x) \mid \text{likes}(\text{john}, x))$

$\text{food}(\text{apples})$

$\text{food}(\text{chicken})$

$(\forall x, y) (eats(y, x) \wedge \neg killed(y) \Rightarrow food(x))$
 $\neg(eats(y, x) \wedge \neg killed(y)) \vee food(x)$
 $(\neg eats(y, x) \vee killed(y, x) \vee food(x))$

$(\forall y) (killed(y) \Rightarrow \neg alive(y))$
 $(\neg killed(y, x) \vee \neg alive(y))$

$(eats(bill, peanuts) \wedge alive(bill))$
 $eats(bill, peanuts)$
 $alive(bill)$

$(\forall x) (eats(bill, x) \Rightarrow eats(Sue, x))$
 $(\neg eats(bill, x) \vee eats(Sue, x))$

1. $(\neg food(x) \vee likes(john, x))$
2. $food(apples)$
3. $food(chicken)$
4. $(\neg eats(y, x) \vee killed(y, x) \vee food(x))$
5. $(\neg killed(y, x) \vee \neg alive(y))$
6. $eats(bill, peanuts)$
7. $alive(bill)$
8. $(\neg eats(bill, x) \vee eats(Sue, x))$

C) John likes peanuts ($likes(john, peanuts)$)

0. $\neg likes(john, peanuts)$
9. $\neg food(peanuts) \quad 0, 1 \{x/peanuts\}$
10. $\neg eats(y, peanuts) \vee killed(y, peanuts) \quad 4, 9 \{x/peanuts\}$
11. $killed(bill, peanuts) \quad 6, 11 \{y/bill\}$
12. $\neg alive(bill) \quad 5, 11 \{y/Bill, x/peanuts\}$
13. $alive(bill) \quad 7$
14. Contradiction $12, 13$

Therefore we have proven John likes Peanuts through resolution.

D) What food does Sue eat?

Assume Sue does not eat any food

0. $\neg eats(Sue, x)$
9. $\neg eats(bill, x) \quad 0, 8$
10. $\neg eats(bill, peanuts) \quad 9 \{x/peanuts\}$
11. Contradiction $10, 6$

Therefore we have proven Sue eats all food.

E)

If you don't eat, you die.

If you die, you are not alive.

Bill is alive.

$(\forall x, y) (\neg \text{eat}(y, x) \Rightarrow \text{dead}(y))$

$(\forall y) (\text{dead}(y) \Rightarrow \neg \text{alive}(y))$

$\text{alive}(\text{Bill})$

CNF:

$(\text{eat}(y, x) \mid \text{dead}(y))$

$(\neg \text{dead}(y) \mid \neg \text{alive}(y))$

$\text{alive}(\text{Bill})$

Given:

1. $(\neg \text{food}(x) \mid \text{likes}(\text{john}, x))$

2. $\text{food}(\text{apples})$

3. $\text{food}(\text{chicken})$

4. $(\neg \text{eats}(y, x) \mid \text{killed}(y, x) \mid \text{food}(x))$

5. $(\neg \text{killed}(y, x) \mid \neg \text{alive}(y))$

6. $(\text{eat}(y, x) \mid \text{dead}(y))$

7. $(\neg \text{dead}(y) \mid \neg \text{alive}(y))$

8. $\text{alive}(\text{Bill})$

9. $(\neg \text{eats}(\text{bill}, x) \mid \text{eats}(\text{Sue}, x))$

What food does Sue eat?

0. $\neg \text{eats}(\text{sue}, x)$

10. $\neg \text{eats}(\text{bill}, x)$ 0, 9

11. $\text{dead}(\text{bill})$ 6, 10 {y/bill}

12. $\neg \text{alive}(\text{bill})$ 7, 11

13. Contradiction 8, 12

Therefore we can still prove that Sue eats everything.