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The Ostap tutorials

build passing

Ostap is a set of extensions/decorators and utilities over the basic `PyROOT` functionality (python wrapper for `ROOT` framework). These utilities greatly simplify the interactive manipulations with `ROOT` classes through python. The main ingredients of `ostap` are

- preconfigured ipython script `ostap`, that can be invoked from the command line.
- *decoration* of the basic `ROOT` objects, like histograms, graphs etc.
 - operations and operators
 - iteration, element access, etc
 - extended functionality
- *decoration* of many basic `ROOT.RooFit` objects
- set of new useful fit models, components and operations
- other useful analysis utilities

Getting started

The main ingredients of `ostap` are

- preconfigured ipython script `ostap`, that can be invoked from the command line.

```
ostap
```

Challenge

Invoke the script with `-h` option to get the whole list of all command line options and keys

Optionally one can specify the list of python files to be executed before appearance of the interactive command prompt:

```
ostap a.py b.py c.py d.py
```

The list of optional arguments can include also root-files, in this case the files will be opened and their handlers will be available via local list `root_files`

```
ostap a.py b.py c.py d.py file1.root file2.root e.py file3.root
```

Also `ROOT` macros can be specified on the command line

```
ostap a.py b.py c.py d.py file1.root q1.C file2.root q2.C e.py file3.root q4.C
```

The script automatically opens `TCanvas` window (unless `--no-canvas` option is specified) with (a little bit modified) LHCb style. It also loads necessary decorators for `ROOT` classes. At last it executes the python scripts and opens root-files, specified as command line arguments.

Values with uncertainties: `ValueWithError`

One of the central object in `ostap` is C++ class `Gaudi::Math::ValueWithError`, accessible in python via shortcut `VE`. This class stands for a combination of the value with uncertainties:

```
from Ostap.Core import VE
a = VE( 10 , 10 ) ## the value & squared uncertainty - 'variance'
b = VE( 20 , 20 ) ## the value & squared uncertainty - 'variance'
print "a=%s" % a
print "b=%s" % b
print 'Value of a is %s' % a.value()
print 'Error of b is %s' % b.error()
print 'Variance of b is %s' % b.cov2 ()
```

A lot of math operations are predefined for `VE`-objects.

Challenge

Make a try with all binary operations (`+`, `-`, `*`, `/`, `**`) for the pair of `VE` objects and combinations of `VE`-objects with numbers, e.g.

```
a + b
a + 1
1 - b
2 ** a
a += 1
b += a
```

Compare the difference for following expressions:

```
a/a      ## <--- HERE
a/VE(a)  ## <--- HERE
a-a      ## <--- HERE
a-VE(a)  ## <--- HERE
```

Note that for trivial cases the correlations are properly taken into account

Additionally many math-functions are provided, carefully takes care on uncertainties

```
from LHCBMath.math_ve import *
sin(a)+cos(b)/tanh(b)
atan2(a,b)/log(a)
```

Simple operations with histograms

Histogram content

`Ostap.PyRoots` module provides two ways to access the histogram content

- by bin index, using operator `[]` : for 1D histogram index is a simple integer number, for 2D and 3D-histograms the bin index is a 2 or 3-element tuple
- using *functional* interface with operator `()` .

```
histo = ...
print histo[2]    ## print the value/error associated with the 2nd bin
print histo(2.21) ## print the value/error at x=2.21
```

Note that the result in both cases is of type `VE` , *value+/-uncertainty*, and the interpolation is involved in the second case. The interpolation can be controlled using `interpolation` argument

```
print histo ( 2.1 , interpolation = 0 ) ## no interpolation
print histo ( 2.1 , interpolation = 1 ) ## linear interpolation
print histo ( 2.1 , interpolation = 2 ) ## parabolic interpolation
print histo ( 2.1 , interpolation = 3 ) ## cubic interpolation
```

Similarly for 2D and 3D cases, `interpolation` parameter is 2 or 3-element tuple, e.g. `(2,2)` , `(3,2,2)` , `(3,0,0)` , ...

Set bin content

```
histo[1] = VE(10,10)
histo[2] = VE(20,20)
```

Loops over the histogram content:

```
for i in histo :
    print 'Bin# %s, the content%s' % ( i, histo[i] )
for entry in histo.iteritems() :
    print 'item ', entry
```

The *reversed* iterations are also supported

```
for i in reversed(histo) :
    print 'Bin# %s, the content%s' % ( i, histo[i] )
```

Histogram slicing

The slicing of 1D-histogram can be done easily using native `slice` in python

```
h1 = h[3:8]
```

For 2D and 3D-cases the slicing is less trivial, but still simple

```
histo2D = ...
h1 = histo2D.sliceX ( 1 )
h2 = histo2D.sliceY ( [1,3,5] )
h3 = histo2D.sliceY ( 3 )
h4 = histo2D.sliceY ( [3,4,5] )
```

Operators and operations

A lot of operators and operations are defined for histograms.

```
histo += 1
histo /= 10
histo = 1 + histo      ## operations with constants
histo = histo + math.cos  ## operations with functions
histo /= lambda x : 1 + x  ## lambdas are also functions
```

Also binary operations are defined

```
h1 = ...
h2 = ...
h3 = h1 + h2
h4 = h1 / h2
h5 = h1 * h2
h6 = h1 - h2
```

For the binary operations the action is defined according to the rule

- the type of the result is defined by the first operand (type, and binning)
- for each bin i the result is estimated as $a \text{ oper } b$, where:
 - oper stands for corresponding operator ($+$, $-$, $*$, $/$, $**$)
 - $a = h1[i]$ is a value of the first operand at bin i
 - $b = h2(x)$, where x is a bin-center of bin i

More operations

There are many other useful operations:

- `abs` : apply `abs` function bin-by-bin
- `asym` : equivalent to $(h1-h2)/(h1+h2)$ with correct treatment of correlated uncertainties
- `frac` : equivalent to $(h1)/(h1+h2)$ with correct treatment of correlated uncertainties
- `average` : make an average of two histograms
- `chi2` : bin-by-bin chi2-tension between two histograms
- ... and many more

Transformations

```
h1 = histo.transform ( lambda x,y : y ) ## identical transformation (copy)
h2 = histo.transform ( lambda x,y : y**3 ) ## get the third power of the histogram content
h3 = histo.transform ( lambda x,y : y/x ) ## less trivial functional transformation
```

Math functions

The standard math-functions can be applied to the histogram (bin-by-bin):

```
from LHCBMath.math_ve import *
h1 = sin ( histo )
h2 = exp ( histo )
h3 = exp ( abs ( histo ) )
...
```

Sampling

There is an easy way to sample the histograms according to their content, e.g. for toy-experiments:

```
h1 = histo.sample() ## make a random histogram with content sampled according to bin+error in original histo
h2 = histo.sample( accept = lambda s : s > 0 ) ##sample but require that sampled values are positive
```

Smearing/convolution with gaussian

It is very easy to smear 1D histogram according to gaussian resolution

```
h1 = histo.smear ( 0.015 ) ## apply "smearing" with sigma = 0.015
h2 = histo.smear ( sigma = lambda x : 0.1*x ) ## smear using 'running' sigma of 10% resolution
```

Rebin

```
original = ... ## the original histogram to be rebinned
template = ... ## histograms that defined new binning scheme
rebin1 = original.rebinNumbers ( template ) ## compare it!
rebin2 = original.rebinFunction ( template ) ## compare it!
`
```

Note that there are two methods for rebin `rebinNumbers` and `rebinFunction` - they depends on the treatment of the histogram.

Challenge

Choose some initial histogram with non-uniform binning, choose *template* histogram with non-uniform binning and compare two methods: `rebinNumbers` and `rebinFunction` .

Integrals

There are several *integral*-like methods for (1D) histograms

- `accumulate` : useful for *numbers*-like histograms, only bin-content inn used for summation (unless the bin is effectively split in case of low/high summation edge does not coincide with bin edges)

```
s = histo.accumulate ()
s = histo.accumulate ( cut = lambda s : 0.4<=s[1].value()<0.5 )
s = histo.accumulate ( low = 1 , high = 14 ) ## accumulate over 1<= ibin <14
s = histo.accumulate ( xmin = 0.14 , xmax = 14 ) ## accumulate over xmin<= x <xmax
```

- `integrate` : useful for *function*-like histograms, perform integration taking into account bin-width.

```
s = histo.integrate ()
s = histo.integrate ( cut = lambda s : 0.4<=s[1].value()<0.5 )
s = histo.integrate ( lowx = 1 , highx = 14 ) ## integrate over 1<= xbin <14
s = histo.integrate ( xmin = 0.14 , xmax = 21.1 ) ## integrate over xmin<= x <xmax
```

- `integral` it transform the histogram into `ROOT.TF1` object and invokes `ROOT.TF1.Integral`

Running sums

and the efficiencies of cuts_

```
h1 = histo.sumv () ## increasing order: sum(first,x)
h2 = histo.sumv ( False ) ## decreasing order: sum(x,last )
```

Efficiency of the cut

Such functionality immediately allows to calculate efficiency histograms using `effic` method:

```
h1 = histo.effic ()          ## efficiency of var<x cut
h2 = histo.effic ( False )  ## efficiency of var>x cut
```

Conversion to *ROOT.TF(1, 2, 3)*

Scaling

In addition to *trivial* scaling operations `h *= 3` and `h /= 10` there are several dedicated methods for scaling

- `scale` : it scales the histogram content to a given sum of *in-range* bins

```
print histo.accumulate()
histo.scale(10)
print histo.accumulate()
```

- `rescale_bins` : it allows the treatment of non-uniform histograms as density distributions. Essentially each bin `i` is rescaled according to the rule `h[i] *= a / S`, where `a` is specified factor and `S` is *bin-area*. such type of rescaling is important for histograms with non-uniform binning

Density

There is method `density` that converts the histogram into *density* histogram. The density histogram (being interpreted as *function*) has unit integral. It is different from the simple rescaling for histograms with non-uniform bins.

```
d = histo.density()
```

Statistics

There are many *statistic* functions

- `mean`
- `rms`
- `kurtosis`
- `skewness`
- `moment`
- `centralMoment`
- `nEff` : number of equivalent entries
- `stat` : statistical information about bin-to-bin content: mean, rms, minmax, ... in form of `Gaudi::Math::StatEntity` class

Figure-of-Merit evaluation and cut optimisation

If *figure-of-merit* is natural and equals to $\sigma(S)/S$ (note that it is equal to $\sqrt{(S+B)/S}$):

```
signal = ... ## distribution for signal
fom1 = signal.FoM2 () ## FoM for var<x cut
fom2 = signal.FoM2 ( False ) ## FoM for var>x cut
```

Note that no explicit knowledge of background is needed here - it enters indirectly via the uncertainties in signal determination.

If *figure-of-merit* is defined as $S/\sqrt{(S+\alpha*B)}$


```

signal = ...
background = ...
alpha = ...
fom1 = signal.FoM1 ( background , alpha ) ## FoM for var<x cut
fom2 = signal.FoM1 ( background , alpha , False ) ## FoM for var>x cut

```

Solve equations

One can also *solve equations* $h(x) = v$

```

value = 3
solutions = histo.solve ( value )
for x in solutions : print x

```

Conversion to `ROOT.TF(1,2,3)`

The conversion of histogram to `ROOT.TF1` objects is straightforward

```
f = histo.tf1()
```

Optionally one can specify `interpolate` flag to define the interpolation rules.

The obtained `TF1` object is defined with three parameters

1. normalization
2. bias
3. scale

It can be used e.g. for visualize interpolated histogram as function or e.g. in `ROOT.TH1.Fit` method for fitting of other histograms

Efficiencies

There are several special cases to get the efficiency-histograms

```

accepted = ... ## histogram with accepted sample
rejected = ... ## histogram with rejected sample
total    = ... ## histogram with total sample

eff1 = accepted/total          ## value is correct, uncertainties are *NOT* correct
eff2 = 1/(1+rejected/accepted) ## everything is correct (binomial)
eff3 = accepted % total        ## everything is correct (binomial)
eff4 = accepted // total        ## correct binomial, if both histograms are "natural"

```

Binomial efficiencies

In addition to the methods described above, few more sophisticated treatments of *binomial efficiencies* are provided

```

accepted = ...
total    = ...

eff1 = accepted.      zechEff ( total ) ## valid for all histograms, including sPlot-weighted
eff2 = accepted.      binomEff ( total ) ## only for natural histograms
eff3 = accepted.      wilsonEff ( total ) ## only for natural histograms
eff4 = accepted.agrestiCoulEff ( total ) ## only for natural histograms

```

For *natural* histograms only one can use even more [sophisticated methods](#), that evaluates the interval. Each method returns *graph*, and the graphs can be visualised for comparison:

```

accepted = ...
rejected = ...

eff1 = accepted.eff_wald          ( rejected )
eff2 = accepted.eff_wilson_score  ( rejected )
eff3 = accepted.eff_wilson_score_continuity ( rejected )
eff4 = accepted.eff_arcsin       ( rejected )
eff5 = accepted.eff_agresti_coull ( rejected )
eff6 = accepted.eff_jeffreys     ( rejected )
eff7 = accepted.eff_clopper_pearson ( rejected )

```

All of these functions have an optional argument `interval` that defines the confidence interval, the default value is `interval=0.682689492137086` that corresponds to 1 sigma.

Optimal binning?

It is not a rare case when one needs to find the binning of the histogram that ensures almost equal bin populations. This task could be solved using `equal_bins` method

```

very_fine_binned_histo = ... ## get the fine binned histograms
edges1 = fine_binned.equal_edges ( 10 ) ## try to find binning with 10 almost equally populated bins
edges2 = fine_binned.equal_edges ( 10 , wmax = 5 ) ## try to find binning with 10 almost equally populated bins, but avoid bins wider than "wmax"

```

Persistencey

Ostap.ZipShelve

Ostap offers very nice&efficient way to store the objects in persistent dbase. This persistency is build around `shelve` module and differs in two way

1. the conntent of payload is compressed, using `zlib` module making the data base very compact
 - (optionally) the whole database can ve further `gzip` 'ed using `gzip` module, if the extension `.gz` is provided. It makes data banse even more compact.
2. in addition to the native `dict` interface from `shelve` , more extensiveinterface with more methods is supported.

Create database and write objects to it:

```
a = ...
import Ostap.ZipShelve as DBASE
with DBASE.open ( 'my_dbase.db' ) as db : ## create DBASE
    db.ls()
    db['a'] = a
    db['histo'] = ROOT.TH1D('h1','',10,0,1)
```

Reading objects from database

```
with DBASE.open ( 'my_dbase.db' , 'read' ) as db : ## read DBASE
    db.ls()
    b = db['a']
    h2 = db['histo']
```

One can store in database all *pickable* objects, that means all python objects, all (serializeable) `ROOT` objects. All `c++` objects with `LCG/Reflex/Cint` -dictionaries are also could be stored database. In practice, everything is storable, including complex combination of python&C++ objects, like dictionary of historgams and python classed, inherited from `c++` -base classes.

Plain ROOT.TFile

Ostap adds some decorations even for the plain `ROOT.TFile` , making its interface more *pythonic*:

```
rfile = ...
obj = rfile['A/B/C/myobj']      ## READ  object form the file/directory
rfile['A/B/C/myobj2'] = object2 ## WRITE object to the file/directory
obj = rfile.A.B.C.myobj        ## another way to access to the object
obj = rfile.get ( 'A/B/C/q' , None ) ## one more way to get object
for obj in rfile : print obj    ## loop over all objects in file
for key,obj in rfile.iteritems() : print key, obj    ## another loop
for key,obj in rfile.iteritems( ROOT.TH1 ) : print key, obj    ## advanced loop, get only histograms
for k in rfile.keys() : print k    ## get all keys and loop over them
for k in rfile.iterkeys() : print k    ## loop over all keys in the file
del rfile['A/B']                    ## delete the object from the file
rfile.rm ( 'A/B' )                  ## delete the object from the file
if 'A/MyHisto' in rfile : print 'OK!' ## check presence of the key
if rfile.has_key ( 'A/MyHisto' ) : print 'OK!' ## check presence of the key
with ROOT.TFile('aa.root') as rfile : rfile.ls() ## context manager protocol
```

RootOnlyShelve

The module `Ostap.RootShelve` offers the thin wrapper over `ROOT.TFile` that implement `shelve` -interface. As a resutl one gets a lighth database build a top of underlying `ROOT.TFile` , where `ROOT` -objects could be stored:

```
from Ostap.RootShelve import RooOnlyShelf
db = RooOnlyShelf('mydb.root', 'c')
h1 = ...
db ['histogram'] = h1
db.ls()
```

RootShelve

The module `Ostap.RootShelve` offers also more sophisticated wrapper over `ROOT.TFile` that also implements `shelve` -interface and able to store `ROOT` and any other *pickable* objects

```
from Ostap.RootShelve import RooShelf
db = RooShelf('mydb.root', 'c')
h1 = ...
db ['histogram'] = h1
db ['histogramlist'] = h1,h2,h3
db.ls()
```

In details ...

For non- `ROOT` objects, database actually stores them as `ROOT::TString` objects carrying their pickle representation with on-flight removal/substitutions of some magic symbol sequences, since `ROOT::TString` is not a real `BLOB` .

Decorations

Ostap *decorates* many `ROOT.RooFit` classes, adding more convinient methods to them.

RooArgList and RooArgSet

All these classes have got set of additional python-like methods for iteration, extension, addition, elemtn access checking the content etc... Also several methods to provide more coherent interfaces (e.g. `add` vs `Add`) are added.

```
1  # Ostap.PyRoUts          INFO      Zillions of decorations for ROOT/RooFit objects
2  Lengths are 2 2
3  'a' : ( 0 +- 0 )
4  'b' : ( -10 +- 0 )
5  'b' : ( -10 +- 0 )
6  'c' : ( 1 +- 0 )
7  a in l ? True True
8  b in l ? True True
9  c in l ? False False
10 a in l ? False False
11 b in l ? True True
12 c in l ? True True
13 'a' : ( 0 +- 0 ) 'b' : ( -10 +- 0 )
14 'b' : ( -10 +- 0 ) 'c' : ( 1 +- 0 )
15 l1+l1 :      ['a:0.0', 'b:-10.0', 'a:0.0', 'b:-10.0']
16 l1+l2 :      ['a:0.0', 'b:-10.0', 'b:-10.0', 'c:1.0']
17 l2+l2 :      ('b:-10.0', 'c:1.0')
18 l2+l1 :      ('b:-10.0', 'c:1.0', 'a:0.0')
19 l1+c :       ['a:0.0', 'b:-10.0', 'c:1.0']
20 l2+c :       ('b:-10.0', 'c:1.0')
21 l1+d :       ['a:0.0', 'b:-10.0', 'd:-1.0']
22 l2+d :       ('b:-10.0', 'c:1.0', 'd:-1.0')
23 c+l1 :       ['a:0.0', 'b:-10.0', 'c:1.0']
24 c+l2 :       ('b:-10.0', 'c:1.0')
25 d+l1 :       ['a:0.0', 'b:-10.0', 'd:-1.0']
26 d+l2 :       ('b:-10.0', 'c:1.0', 'd:-1.0')
```

output.txt hosted with ❤ by GitHub

[view raw](#)

```
1  import ROOT
2  import Ostap.PyRoUts
3
4  a  = ROOT.RooRealVar ('a','a',-10,10)
5  b  = ROOT.RooRealVar ('b','b',-10)
6  c  = ROOT.RooConstVar('c','c', 1)
7  d  = ROOT.RooConstVar('d','d', -1)
8
```

```

9  l1 = ROOT.RooArgList    ( a , b )
10 l2 = ROOT.RooArgSet     ( b , c )
11
12 print 'Lengths are %s %s ' % ( len ( l1 ) , len( l2 ) )
13
14 for i in l1 : print i
15 for i in l2 : print i
16
17 for l in ( l1 , l2 ) :
18     print ' a in l ? %s %s ' % ( a in l , 'a' in l )
19     print ' b in l ? %s %s ' % ( b in l , 'b' in l )
20     print ' c in l ? %s %s ' % ( c in l , 'c' in l )
21
22
23 print l1[0] , l1[1]
24 print l2['b'] , l2['c']
25
26 print 'l1+l1 :    %s' % ( l1 + l1 )
27 print 'l1+l2 :    %s' % ( l1 + l2 )
28 print 'l2+l2 :    %s' % ( l2 + l2 )
29 print 'l2+l1 :    %s' % ( l2 + l1 )
30
31 print 'l1+c :     %s' % ( l1 + c )
32 print 'l2+c :     %s' % ( l2 + c )
33 print 'l1+d :     %s' % ( l1 + d )
34 print 'l2+d :     %s' % ( l2 + d )
35
36 print 'c+l1 :     %s' % ( c + l1 )
37 print 'c+l2 :     %s' % ( c + l2 )
38 print 'd+l1 :     %s' % ( d + l1 )
39 print 'd+l2 :     %s' % ( d + l2 )

```

roofit_lists.py hosted with ♥ by [GitHub](#)

[view raw](#)

RooAbsData and RooDataSet

These methods also have got the extended interface with many useful methods and operators, like e.g. concatenation of datasets `a+b` and merging them `a*c` .

`RooDataSet` class also has go many methods, that are similar to those of `ROOT.TTree` , in particular `project` and `draw` :

```

dataset = ...
dataset.draw('mass','pt>1')
histo    = ...
dataset.project ( histo , 'mass', 'pt>1' )

```

Many other methodons like `statVar` , `sumVar` , `statCov` , `vminmax` are also the same as for `ROOT.TTree` , see [above](#).

```

s1  = dataset.statVar ( 'eff' )
s2  = dataset.sumVar  ( 'eff' )
r   = dataset.statCov ( 'eff','pt' )
mn,mx = dataset.vminmax ( 'eff' )

```

RooFitResult

The class `RooFitResult` get many decorations that allow to access fit results

```

result = ...
par1 = result.params()  ## get all floating parameters
par2 = result.params( float_only = False ) ## all parameters
a,v  = result.param ( 'a' )      ## par by name
a,v  = result.param ( a )        ## par by RooFit object itself
p    = result.a                 ## par as attribute
for par in result : print par    ## iteration
for name,par in result.iteritems() : print par ## iteration
print result.cov ( 'a' , 'b' )  ## get the covariance submatrix
print result.corr ( 'a' , 'b' ) ## get the correlation coefficient

```

Also the simple math with fitting parameters is supported

```

result = ...
s = result.sum      ( 'S','B' ) ## S+B
d = result.divide   ( 'S','B' ) ## S/B
s = result.subtract ( 'B','B1' ) ## B-B1
m = result.multiply ( 'A','B' ) ## A*B
f = result.fraction ( 'S','B' ) ## S/(S+B)

```

RooRealVar & friends

Few simple operations are added to simplify the calculations with `RooRealVar` objects:

```

x = ROOT.RooRealVar( ... )
x + 10
x - 10
x * 10
x / 10
10 + x
10 - x
10 * x
10 / x
x += 2
x -= 2
x *= 2
x /= 2
x ** 3

```


PDFs and the basic models

Ostap provides set of useful wrapper and helper class that drastically simplify the construction and manipulations with `RooAbsPdf` - objects.

E.g. consider the simplest case - creation of the Gaussian PDF using the standard way the standard way:

```
x      = ROOT.RooRealVar ( 'x'      , 'x'      , 2, 3 )
mean   = ROOT.RooRealVar ( 'mean'   , 'mean'   , 3.100, 3.080, 3.120 )
sigma  = ROOT.RooRealVar ( 'sigma'   , 'sigma'   , 0.015, 0.010, 0.025 )
pdf     = ROOT.RooGaussian( 'Gauss' , 'Gaussian' , x , mean , sigma )
```

In Ostap it can be done in a bit simpler way

```
gauss = Gauss_pdf ( 'Gauss' ,
                    xvar  = ( 2 , 3 ) ,
                    mean  = ( 3.100 , 3.080 , 3.120 ) ,
                    sigma = ( 0.015 , 0.010 , 0.025 ) )
gauss.draw() ## and one can immediately visualize the model
```

How to define parameter?

There are may ways to define parameter

1. One can use the existing `RooAbsReal` object, e.g. `RooRealVar` or `RooConstVar` :

```
mean = ROOT.RooRealVar ( 'mean' , 'mean' , 3.100, 3.080, 3.120 )
gauss = Gauss_pdf ( 'Gauss' ,
                    xvar  = ( 2 , 3 ) ,
                    mean  = mean , ## <--- HERE
                    sigma = ( 0.015 , 0.010 , 0.025 ) )
```

- i. One can use 2 or 3-element tuple `(minval,maxval)` or `(value, minval,maxval)` or plain single number. In this case the variable of the type `RooRealVar` will be automatically created using this specification

```
gauss = Gauss_pdf ( 'Gauss' ,
                    xvar  = ( 2 , 3 ) , ## <-- HERE
                    mean  = ( 3.100 , 3.080 , 3.120 ) , ## <-- HERE
                    sigma = 0.015 ) ## <-- HERE
```

For all models, all known parameter are accessible (and documented) as python *property*

```
gauss = ...
help(gauss.xvar)
print gauss.sigma
help(gauss.mean)
```

There are many predefined models, accesible via `Ostap.FitModels` module:

```
import Ostap.FitModels as Models
help(Models)
```

Base class PDF

All Ostap-based fit models and PDFs (directly or indirectly) inherit from python base class `PDF`, that provides great additional functionality, in particular the methods `fitTo` and `draw` that simplify the fitting procedure itself and visualization of the results:

The method `fitTo`

```
gauss = Gauss_pdf ( ... )
dataset = ....
result , frame = gauss.fitTo ( dataset , silent = True , reFit = 2 )
print 'FitResults: %s' % result
```

All the native `RooFit` *commands* can be specified as optional arguments, as well as many commands specific for Ostap, e.g. `reFit=2` above means *in case of fit failure, try to refit it (up to 2 times)*, and the meaning of `silent=True` is obvious.

The method `draw`

```
gauss = Gauss_pdf ( ... )
dataset = ....
result , frame = gauss.fitTo ( dataset , silent = True , reFit = 2 )
print 'FitResults: %s' % result
frame = gauss.draw ( dataset , nbins = 100 )
```

Fitting and vizualisation can be combined:

```
gauss = Gauss_pdf ( ... )
dataset = ....
result , frame = gauss.fitTo ( dataset , draw = True , nbins = 100 ) ## draw it after the fit
```

Access to the underlying `RooAbsPdf` object

The access to the underlying bare `RooAbsPdf` -object can be done (if needed) via the property `pdf`

```
gauss = Gauss_pdf ( ... )
root_pdf = gauss.pdf
```

Other methods

`PDF` class is equipped with many other useful methods:

- `fitHisto` : The method `fitTo` can be *blindly* applied not only to `RooDataSet` -objects, but also to the histograms:

```
histo = ...
r, f = gauss.fitTo ( histo , draw = True )
```

However the dedicated method `fitHisto` sometimes could be more usefu

```
histo = ...
gauss.fitHisto ( histo , draw = True )
```

- `draw_nll` : vizualize NLL-scans and LL-profiles

```
r, f = gauss.fitTo ( dataset , draw = False )
nll , f1 = gauss.draw_nll ( 'sigma' , dataset ) ## NLL
profile , f2 = gauss.draw_nll ( 'sigma' , dataset , profile = True ) ## PROFILE
```

- `generate` : tiny but useful wrapper for `RooAbsPdf::generate`
- `minmax` : mane the estimates for minimal and maximal values for the PDF. For some models it is done analytically or semianalitycally, for remainnig models it is doen using random shoots.

```
mn,mx = gauss.minmax( 500000 )
```

- `__call__` : it allows to use `PDF` as simple *function*

```
gauss = ...
print gauss( 3.090 ), gauss( 3.100 ), gauss( 3.110 )
```

- Several *statistical* functions. For some models analytical or semi-analytical calculations are used, for remaining models numerical estimations are performed using `scipy`
- `rms` : *rms* for the distribution
- `fwhm` : *full width at half maximum*
- `fwhm` : *full width at half maximum*
- `moment` : the *moment* of the distribution
- `central_moment` : the *central moment* of the distribution
- `skewness` : *skewness* for the distribution
- `kurtosis` : *kurtosis* for the distribution
- `mode` : the *mode* for the distribution
- `median` : *median* value for the distribution
- `get_mean` : *mean* value for the distribution
- `cl_symm` : *symmetric confidence interval*
- `cl_asymm` : *asymmetric confidence interval*
- `quantile` : *quantile* value for the distribution
- `integral` : *integral* for the distribution
- `derivative` : *derivative* of the PDF at the given point

Convolution

...

Generic Wrapper *Generic1D_pdf*

The bare `RooAbsPdf` could be easily converted to Ostap-form using the generic wrapper `Generic1D_pdf` :

```
bare = ROOT.RooGaussian('Gauss','Gaussian', x , mean , sigma )
gauss = Generic1D_pdf ( pdf = bare , xvar = x )
gauss.draw() ## one can immediately use the full power of Ostap-PDF
```

In a similar way there are generic wrappers for `2D` and `3D` -models:

```
bare2D = ...
bare3D = ...
ostap_2d = Generic2D_pdf ( pdf = bare2D , xvar = x , yvar = y )
ostap_3d = Generic3D_pdf ( pdf = bare3D , xvar = x , yvar = y , zvar = z )
```

`2D` and `3D` -cases

For `2D` and `3D` cases there are base classes `PDF2` and `PDF3` that in turn inherit from `PDF` and gets all the nice functionality. Of course several new methods specific for `2D` and `3D` -cases are added and the behavior of some `1D` -specific methods is fixed.

Compound fit models

1D -case

Ostap offers a very easy way to build the compound fit models from the individual components. E.g. the case of the trivial fit model that consists of one signal and one background components:

```
signal      = ...
background  = ...
model       = Fit1D ( signal = signal , background = background ) ## <-- HERE!
dataset     = ...
result , frame = model.fitTo ( dataset , draw = True ) ## fit and visualize
```

The fit model can contain several *signal* and *background* components, and also *other* components :

```
model       = Fit1D ( signal = signal ,
                    background = background ,
                    othersignals = [ ... ] ,
                    otherbackgrounds = [ ... ] ,
                    others      = [ ... ] )
```

In this case several *signal*, *backgrounds* and/or *others* components can be combined into single *signal*, *background* and/or *others* components:

```
model       = Fit1D ( combine_signals = True ,
                    combine_backgrounds = True ,
                    combine_others      = True , ... )
```

In practice it is very convenient; an approach in which several signal/background/other components are specified.

On default *extended* 'RooAddPdf' fit model is created, however, one can force *non-extended* model:

```
model       = Fit1D ( extended = False , ... )
```

In this case one can also instruct the class `Fit1D` to create *recursive* (default) or *non-recursive* fit fractions:

```
model       = Fit1D ( extended = False , recursive = False , ... )
```

All components (*signal/background/others*) can be specified as Ostap-based models. Also one can provide them in a form of bare `RooAbsPdf`, but for this case one needs to provide also `xvar` -variable

```
mass = ROOT.RooRealVar( 'mass', 'mass', 2, 3 )
gauss = ROOT.RooGaussian( 'Gauss', 'Gauss', mass , ... )
model = Fit1D( signal = gauss , xvar = mass , ... )
```

For *background* components there is also an alternative way to specify it:

- `None` : `RooPolynomial` of zero degree (uniform distribution) will be created and used as *background* component
 - Attention: `background=None` does *not* imply the absence of background component
- negative integer `n` : Ostap model `PolyPos_pdf` will be created and used as *background* component. This model corresponds to the *positive* polynomial of degree `-n`. The polynomial is constrained to be non-negative for the whole considered interval of `xvar`. This constraint allows rather robust and stable fits, especially for the low-statistics case.
- non-negative integer `n` : Ostap model `Bkg_pdf`, that is a product of the exponential function and the *positive* polynomial of degree `n` will be created and used as *background* component. Note:
 - The `background=0` case corresponds to simple exponential background

- Since the polynomial is constrained to be *non-negative* this PDF is very stable and robust, especially for the low-statistic case,
- as `RooAbsReal` object, in this case it is interpreted as the exponential slope

Access to the model componens

The individaul components can be accessed using python *properties*

```
gaudd = Gauss_pdf ( ...
model = Fit1D ( signal = gauss , ... )
print model.signal.sigma ## get sigma of Gauss
print model.signal.mean  ## get mean  of Gauss
```

Fit parameters

The parametters of the created `RooAddPdf` can be accessed via python properties, e.g. for *extended* fits:

```
gaudd = Gauss_pdf ( ...
model = Fit1D ( signal = gauss , ... )
print 'signal yield(s):' , model.S
print 'background(s):'   , model.B
print 'others: '         , model.C
model.S = 100 ## set value of signal component to be 100 events
model.B.fix(50) ## fix the yield of the background component at 50 events
model.draw()
```

Depending on the number of corresponing componens and flags `combine_signals` , `combine_backgrounds` , `combine_others` these properties can be *scalar* values or arrays/tuples.

For `combine_signal=True` , `combine_backgrounds=True` , `combine_others=True` cases oen also gets propperities `fs` , `fb` and `fc` that corresponds to the fractions of individual *signal/background/others* components for the compound signal/ *signal/background/others*.

For *non-extended* fits, the main parameters are *fractions*:

```
gaudd = Gauss_pdf ( ...
model = Fit1D ( signal = gauss , ... , extended = False )
...
print 'fractions:' , model.F
```

All the ways to deal with `Fit1D` objects are illustrated here:

```
1  #!/usr/bin/env python
2  # -*- coding: utf-8 -*-
3  # =====
4  ## @file TestComponents.py
5  #
6  # tests for various multicomponents models
7  #
8  # @author Vanya BELYAEV Ivan.Belyaev@itep.ru
9  # @date 2014-05-11
10 # =====
11 """Tests for various multicomponent models
12 """
13 # =====
14 __version__ = "$Revision:"
15 __author__ = "Vanya BELYAEV Ivan.Belyaev@itep.ru"
16 __date__ = "2014-05-10"
```

```

17  __all__      = ()  ## nothing to be imported
18  # =====
19  import ROOT, random
20  from Ostap.PyRoUts import *
21  from Ostap.Utls import rooSilent
22  # =====
23  # logging
24  # =====
25  from AnalysisPython.Logger import getLogger
26  if '__main__' == __name__ or '__builtin__' == __name__ :
27      logger = getLogger ( 'Ostap.TestComponents' )
28  else :
29      logger = getLogger ( __name__ )
30  # =====
31  logger.info ( 'Test for multi-component models from Analysis/Ostap' )
32  # =====
33  ## make simple test mass
34  mass      = ROOT.RooRealVar ( 'test_mass' , 'Some test mass' , 0 , 10 )
35
36  ## book very simple data set
37  varset     = ROOT.RooArgSet ( mass )
38  dataset    = ROOT.RooDataSet ( dsID() , 'Test Data set-0' , varset )
39
40  mmin, mmax = mass.minmax()
41
42  ### fill it
43  m1 = VE(3,0.300**2)
44  m2 = VE(5,0.200**2)
45  m3 = VE(7,0.100**2)
46
47  for i in xrange(0,5000) :
48      for m in (m1,m2,m3) :
49          mass.value = m.gauss ()
50          dataset.add ( varset )
51
52  for i in xrange(0,5000) :
53      mass.value = random.uniform ( *mass.minmax() )
54      dataset.add ( varset )
55
56  logger.info ( 'Dataset: %s' % dataset )
57  import Ostap.FitModels as Models
58
59  signal_1 = Models.Gauss_pdf ( 'G1' , xvar = mass , mean = m1.value() , sigma = m1.error() )
60  signal_2 = Models.Gauss_pdf ( 'G2' , xvar = mass , mean = m2.value() , sigma = m2.error() )
61  signal_3 = Models.Gauss_pdf ( 'G3' , xvar = mass , mean = m3.value() , sigma = m3.error() )
62

```

```

63 wide_1 = Models.Gauss_pdf ( 'GW1' , xvar = mass , mean = 1.0 , sigma = 2 )
64 wide_2 = Models.Gauss_pdf ( 'GW2' , xvar = mass , mean = 9.0 , sigma = 3 )
65
66 narrow_1 = Models.Gauss_pdf ( 'GN1' , xvar = mass , mean = 4.0 , sigma = 1 )
67 narrow_2 = Models.Gauss_pdf ( 'GN2' , xvar = mass , mean = 6.0 , sigma = 1 )
68
69 ## =====
70 logger.info ( 'Test the extended fit with many components' )
71 model_ext1 = Models.Fit1D (
72     name          = 'EXT1'      ,
73     signal        = signal_1 ,
74     othersignals  = [ signal_2 , signal_3 ] ,
75     background    = wide_1     ,
76     otherbackgrounds = [ wide_2 ] ,
77     others        = [ narrow_1 , narrow_2 ] ,
78 )
79 model_ext1.S[0].value = 5000
80 model_ext1.S[1].value = 5000
81 model_ext1.S[2].value = 5000
82
83 model_ext1.B[0].value = 1700
84 model_ext1.B[1].value = 2300
85
86 model_ext1.C[0].value = 500
87 model_ext1.C[1].value = 400
88
89 r, f = model_ext1.fitTo ( dataset , draw = False , silent = True )
90 r, f = model_ext1.fitTo ( dataset , draw = False , silent = True )
91 logger.info ( 'Model %s Fit results:\n#%s ' % ( model_ext1.name , r ) )
92 print 'Signals          [S]:' , model_ext1.S
93 print 'Backgrounds      [B]:' , model_ext1.B
94 print 'Components       [C]:' , model_ext1.C
95 print 'Fractions         [F]:' , model_ext1.F
96 print 'Signal fractions  [fS]:' , model_ext1.fS
97 print 'Background fractions [fB]:' , model_ext1.fB
98 print 'Component fractions [fC]:' , model_ext1.fC
99 print 'Yields           [yields]:' , model_ext1.yields
100 print 'Fractions        [fractions]:' , model_ext1.fractions
101
102
103 ## =====
104 logger.info ( 'Test the extended fit with compound components' )
105 model_ext2 = Models.Fit1D (
106     name          = 'EXT2'      ,
107     signal        = signal_1 ,
108     othersignals  = [ signal_2 , signal_3 ] ,

```

```

109     background          = wide_1 ,
110     otherbackgrounds    = [ wide_2 ] ,
111     others               = [ narrow_1 , narrow_2 ] ,
112     #
113     combine_signals     = True ,
114     combine_backgrounds = True ,
115     combine_others      = True ,
116 )
117 model_ext2.S = 5000
118 model_ext2.B = 4200
119 model_ext2.C = 700
120
121 model_ext2.fS[0].value = 0.33
122 model_ext2.fS[1].value = 0.50
123
124 model_ext2.fB[0].value = 0.40
125 model_ext2.fC[0].value = 0.60
126
127 r, f = model_ext2.fitTo ( dataset , draw = False , silent = True )
128 r, f = model_ext2.fitTo ( dataset , draw = False , silent = True )
129 logger.info ( 'Model %s Fit results:\n#%s ' % ( model_ext2.name , r ) )
130 print 'Signals          [S]:' , model_ext2.S
131 print 'Backgrounds      [B]:' , model_ext2.B
132 print 'Components       [C]:' , model_ext2.C
133 print 'Fractions        [F]:' , model_ext2.F
134 print 'Signal fractions [fS]:' , model_ext2.fS
135 print 'Background fractions [fB]:' , model_ext2.fB
136 print 'Component fractions [fC]:' , model_ext2.fC
137 print 'Yields          [yields]:' , model_ext2.yields
138 print 'Fractions      [fractions]:' , model_ext2.fractions
139
140 ## =====
141 logger.info ( 'Test non-extended fit with all components, non-recursive' )
142 model_ne1 = Models.Fit1D (
143     name          = 'NE1' ,
144     signal        = signal_1 ,
145     othersignals  = [ signal_2 , signal_3 ] ,
146     background    = wide_1 ,
147     otherbackgrounds = [ wide_2 ] ,
148     others        = [ narrow_1 , narrow_2 ] ,
149     ##
150     extended      = False ,
151     recursive     = False
152 )
153
154 model_ne1.F[0].value = 0.25

```



```

155 model_ne1.F[1].value = 0.25
156 model_ne1.F[2].value = 0.25
157 model_ne1.F[3].value = 0.08
158 model_ne1.F[4].value = 0.12
159 model_ne1.F[5].value = 0.05
160
161 r, f = model_ne1.fitTo ( dataset , draw = False , silent = True )
162 r, f = model_ne1.fitTo ( dataset , draw = False , silent = True )
163 logger.info ( 'Model %s Fit results:\n#%s ' % ( model_ne1.name , r ) )
164 print 'Signals                [S]:' , model_ne1.S
165 print 'Backgrounds            [B]:' , model_ne1.B
166 print 'Components             [C]:' , model_ne1.C
167 print 'Fractions              [F]:' , model_ne1.F
168 print 'Signal fractions       [fS]:' , model_ne1.fS
169 print 'Background fractions [fB]:' , model_ne1.fB
170 print 'Component fractions [fC]:' , model_ne1.fC
171 print 'Yields                [yields]:' , model_ne1.yields
172 print 'Fractions            [fractions]:' , model_ne1.fractions
173
174 ## =====
175 logger.info ( 'Test non-extended fit with all components, recursive' )
176 model_ne2 = Models.Fit1D (
177     name          = 'NE2' ,
178     signal         = signal_1 ,
179     othersignals   = [ signal_2 , signal_3 ] ,
180     background     = wide_1 ,
181     otherbackgrounds = [ wide_2 ] ,
182     others         = [ narrow_1 , narrow_2 ] ,
183     ##
184     extended       = False ,
185     recursive      = True ,
186 )
187
188 model_ne2.F[0].value = 0.25
189 model_ne2.F[1].value = 0.33
190 model_ne2.F[2].value = 0.50
191 model_ne2.F[3].value = 0.37
192 model_ne2.F[4].value = 0.74
193 model_ne2.F[5].value = 0.50
194
195 r, f = model_ne2.fitTo ( dataset , draw = False , silent = True )
196 r, f = model_ne2.fitTo ( dataset , draw = False , silent = True )
197 logger.info ( 'Model %s Fit results:\n#%s ' % ( model_ne2.name , r ) )
198 print 'Signals                [S]:' , model_ne2.S
199 print 'Backgrounds            [B]:' , model_ne2.B
200 print 'Components             [C]:' , model_ne2.C

```

```

201 print 'Fractions          [F]:' , model_ne2.F
202 print 'Signal fractions   [fS]:' , model_ne2.fS
203 print 'Background fractions [fB]:' , model_ne2.fB
204 print 'Component fractions [fC]:' , model_ne2.fC
205 print 'Yields            [yields]:' , model_ne2.yields
206 print 'Fractions          [fractions]:' , model_ne2.fractions
207
208
209 ## =====
210 logger.info ( 'Test non-extended fit with compound components, non-recursive' )
211 model_ne3 = Models.Fit1D (
212     name          = 'NE2'          ,
213     signal        = signal_1       ,
214     othersignals  = [ signal_2 , signal_3 ] ,
215     background    = wide_1        ,
216     otherbackgrounds = [ wide_2 ] ,
217     others        = [ narrow_1 , narrow_2 ] ,
218     ##
219     combine_signals = True      ,
220     combine_backgrounds = True  ,
221     combine_others  = True      ,
222     ##
223     extended       = False     ,
224     recursive      = False
225 )
226
227 model_ne3.F[0].value = 0.75
228 model_ne3.F[1].value = 0.30
229
230 model_ne3.fS[0].value = 0.33
231 model_ne3.fS[1].value = 0.50
232
233 model_ne3.fB[0].value = 0.41
234 model_ne3.fC[0].value = 0.58
235
236 r, f = model_ne3.fitTo ( dataset , draw = False , silent = True )
237 r, f = model_ne3.fitTo ( dataset , draw = False , silent = True )
238 logger.info ( 'Model %s Fit results:\n#%s ' % ( model_ne3.name , r ) )
239 print 'Signals          [S]:' , model_ne3.S
240 print 'Backgrounds      [B]:' , model_ne3.B
241 print 'Components       [C]:' , model_ne3.C
242 print 'Fractions        [F]:' , model_ne3.F
243 print 'Signal fractions   [fS]:' , model_ne3.fS
244 print 'Background fractions [fB]:' , model_ne3.fB
245 print 'Component fractions [fC]:' , model_ne3.fC
246 print 'Yields            [yields]:' , model_ne3.yields


```

```

247 print 'Fractions      [fractions]:' , model_ne3.fractions
248
249
250 ## =====
251 logger.info ( 'Test non-extended fit with compound components, recursive' )
252 model_ne4 = Models.Fit1D (
253     name          = 'NE4'          ,
254     signal         = signal_1       ,
255     othersignals   = [ signal_2 , signal_3 ] ,
256     background     = wide_1        ,
257     otherbackgrounds = [ wide_2 ] ,
258     others         = [ narrow_1 , narrow_2 ] ,
259     ##
260     combine_signals = True         ,
261     combine_backgrounds = True     ,
262     combine_others  = True         ,
263     ##
264     extended       = False        ,
265     recursive      = True
266 )
267
268 model_ne4.F[0].value = 0.75
269 model_ne4.F[1].value = 0.80
270
271 model_ne4.fS[0].value = 0.33
272 model_ne4.fS[1].value = 0.50
273
274 model_ne4.fB[0].value = 0.41
275 model_ne4.fC[0].value = 0.50
276
277 r, f = model_ne4.fitTo ( dataset , draw = False , silent = True )
278 r, f = model_ne4.fitTo ( dataset , draw = False , silent = True )
279 logger.info ( 'Model %s Fit results:\n#%s ' % ( model_ne4.name , r ) )
280 print 'Signals          [S]:' , model_ne4.S
281 print 'Backgrounds      [B]:' , model_ne4.B
282 print 'Components       [C]:' , model_ne4.C
283 print 'Fractions        [F]:' , model_ne4.F
284 print 'Signal fractions  [fS]:' , model_ne4.fS
285 print 'Background fractions [fB]:' , model_ne4.fB
286 print 'Component fractions [fC]:' , model_ne4.fC
287 print 'Yields           [yields]:' , model_ne4.yields
288 print 'Fractions      [fractions]:' , model_ne4.fractions
289
290
291 # =====
292 # The END

```

```
293 # =====
```



components.py hosted with ❤ by GitHub [view raw](#)

The corresponding output can be inspected [here](#)

2D -case

Generic **2D** -case

Symmetric **2D** -case

3D -case

Generic **3D** -case

Symmetric **3D** -case

Mixed-symmetry **3D** -case

Contributing

[ostap-tutorials](#) is an open source project, and we welcome contributions of all kinds:

- New lessons;
- Fixes to existing material;
- Bug reports; and
- Reviews of proposed changes.

By contributing, you are agreeing that we may redistribute your work under [these licenses](#). You also agree to abide by our [contributor code of conduct](#).

Getting Started

1. We use the [fork and pull](#) model to manage changes. More information about [forking a repository](#) and [making a Pull Request](#).
2. To build the lessons please install the [dependencies](#).
3. For our lessons, you should branch from and submit pull requests against the `master` branch.
4. When editing lesson pages, you need only commit changes to the Markdown source files.
5. If you're looking for things to work on, please see [the list of issues for this repository](#). Comments on issues and reviews of pull requests are equally welcome.

Dependencies

To build the lessons locally, install the following:

1. [Gitbook](#)

Install the Gitbook plugins:

```
$ gitbook install
```

Then (from the `ostap-tutorials` directory) build the pages and start a web server to host them:

```
$ gitbook serve
```

You can see your local version by using a web-browser to navigate to `http://localhost:4000` or wherever it says it's serving the book.

The title

Learning Objectives

- The starterkit lessons all start with objectives about the lesson
- Objective 2 with some *formatted text like* this

Basic formatting

You can make **bold**, *italic* and ~~striktrough~~ text. Add relative links like [this one](#) and absolute links in a [couple](#) of [different](#) ways.

Have bulleted lists:

- Point 1
- Point 2
 - Sub point
 - Sub point
 - Sub point
- Point 2

Use numbered lists:

1. First
2. Second
 - i. Second first
 - i. Second first first
 - ii. Second second
3. Third

LaTeX

You can use inline LaTeX maths such as talking about the decay $D^{*+} \rightarrow D^0 K^{\pi^+}$.

Code highlighting

And have small lines of code inline like saying `print("Hello world")` or have multiple lines with syntax highlighting for python:

```
import sys

def stderr_print(string):
    sys.stderr.write(string)

stderr_print("Hello world")
```

bash:

```
lb-run Bender/latest $SHELL
dst_dump -f -n 100 my_file.dst 2>&1 | tee log.log
```

and more!

Callouts

Prerequisites

- Prerequisite 1
- Prerequisite 2

Objectives

- Objective 1
- Objective 2

Challenge

Set a challenge here, and the solution will remain hidden until it's clicked

- How to print?

Solution

The answer is:

```
print("Hello world")
```

Extra details that are hidden by default

Some extra details

Keypoints

- Summary point 1

- Summary point 2

Quotes

This was said by someone

Tables

Simple tables are possible

First Header	Second Header
Content from cell 1	Content from cell 2
Content in the first column	Content in the second column

Images



Section types

This is a section

Subsections

And a subsection

Subsubsections

And a subsubsection