

For any constants C , a , ω , and $k \in \mathbb{N}$ we have the Laplace Transforms of the following functions $y(t)$:

$$y(t) = C \quad \mathcal{L}\{C\} = \frac{C}{s} \quad \text{Constant}$$

$$y(t) = e^{at} \quad \mathcal{L}\{e^{at}\} = \frac{1}{s-a} \quad \text{Exponential Function}$$

$$y(t) = \cos(\omega t) \quad \mathcal{L}\{\cos \omega t\} = \frac{s}{s^2 + \omega^2} \quad \text{Cosine}$$

$$y(t) = \sin(\omega t) \quad \mathcal{L}\{\sin \omega t\} = \frac{\omega}{s^2 + \omega^2} \quad \text{Sine}$$

$$y(t) = t^k \quad \mathcal{L}\{t^k\} = \frac{k!}{s^{k+1}} \quad \text{Power Function}$$

$$y(t) = e^{at}f(t) \quad \mathcal{L}\{e^{at}f(t)\} = F(s-a) \quad \text{First Shift Theorem}$$

$$y(t) = t^k f(t) \quad \mathcal{L}\{t^k f(t)\} = (-1)^k \frac{d^k}{ds^k} F(s) \quad \text{Resonance}$$

$$\mathcal{L}\{y'\} = sY(s) - y(0)$$

$$\mathcal{L}\{y''\} = s^2Y(s) - sy(0) - y'(0)$$