

e,g, 7x,20 = 220,0+20; N→N

shesses 2) intensional identity (stress on IdA as data)
want to say; only element in it is cefl; an induction principle p: a=Ab  $(x:A, y:A, z: x=Ay \vdash P(x,y,z)$ 

 $x:A \vdash q: P(x,x,refi)$ 

0)

T[x,y,z.P](x.q;p):P(a,b,p)

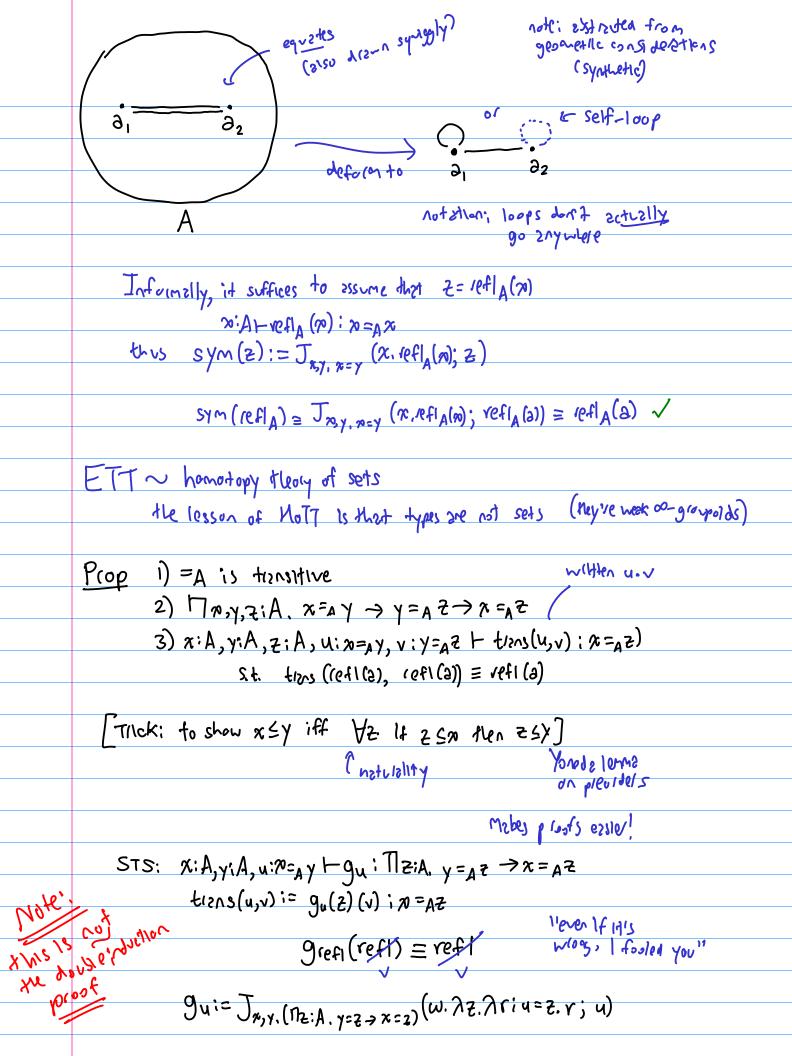
hat sivegenent note: notation is confusing

path induction J(x,q; refla(e)) = [a/x]q; P(a,a, refla(q)) cose-such sis on one cose

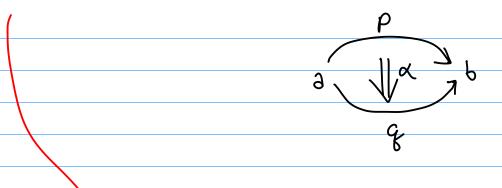
Fact: now con show = A is an equivalence relation

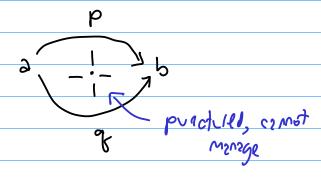
- 1) = A is symmetic
- 2)  $\prod x,y : A \cdot x = A y \longrightarrow y = A^x$
- 3)  $x:A, y:A, z: x = Ay \vdash Sym(z): y = Ax$

s.t.  $Sym(lefl_A(\theta)) \equiv refl_A(\theta)$ 



pre-groupoild refl(a) (unit) not a group, shoe (inverse) the types are not the Some (H is a groupoid) p.q (mult) groupold refl-1 = refl refl. q = q  $p \cdot refl = p$   $p \cdot (q \cdot r) = (p \cdot q) \cdot r$   $p \cdot p^{-1} = refl$   $p^{-1} \cdot p = refl$ equality? here hold 6:A le £1(9) P, 2=AP P-1:P=A3 > refla(8); 8=4 8 this is a type!  $\Omega_{A}(a)$ to we can equality refl(e) (C416) p.p-1 p.p-1  $\Omega_{A}(z)$ 





## Occupaid up to higher homotopy

What are these proofs? I requires inverses, concertenetions, etc in the loop space.

## weak on-groupoid

"Nothing really holds, it only holds up to a bigger lie. Well, as long as you carry these lies to infinity you're fine; it's a Ponzi scheme that runs out. 'Well, what could go wrong?'"

It's not well-founded. There's no spot where something utterly becomes true... unless you truncate. If I demand that these hold definitionally (the groupoid laws), you get a strict groupoid, at any dimension you wish. For example, the fundamental group of a loop space is the zero-truncation of a loop space. That truncation is the starting point of algebraic topology.