The system should allow users to register with email and password. Use OAuth2 for authentication.

Create a REST API for product listing and cart management. Implement unit testing for all API endpoints. Deploy the application on AWS Lambda.