

# 1 Black-box Testing

## 1.A linalg.dot

### 1.A.1 documentation

For 2-D arrays it is equivalent to matrix multiplication, and for 1-D arrays to inner product of vectors (without complex conjugation). For N dimensions it is a sum product over the last axis of a and the second-to-last of b:

$$\text{dot}(a, b)[i,j,k,m] = \text{sum}(a[i,j,:] * b[k,:,m])$$

**Parameters** : two arrays a: array\_like First argument.

b : array\_like Second argument.

out : ndarray, optional output argument. This must have the exact kind that would be returned if it was not used. In particular, it must have the right type, must be C-contiguous, and its dtype must be the dtype that would be returned for dot(a,b). This is a performance feature. Therefore, if these conditions are not met, an exception is raised, instead of attempting to be flexible.

**Returns** : output : ndarray

Returns the dot product of a and b. If a and b are both scalars or both 1-D arrays then a scalar is returned; otherwise an array is returned. If out is given, then it is returned. Raises: ValueError If the last dimension of a is not the same size as the second-to-last dimension of b.

### 1.A.2 tests

## 1.B linalg.multidot

Compute the dot product of two or more arrays in a single function call, while automatically selecting the fastest evaluation order.

multi\_dot chains numpy.dot and uses optimal parenthesization of the matrices [R44] [R45]. Depending on the shapes of the matrices, this can speed up the multiplication a lot.

If the first argument is 1-D it is treated as a row vector. If the last argument is 1-D it is treated as a column vector. The other arguments must be 2-D.

### 1.B.1 tests

## 1.C linalg.vdot

### 1.C.1 documentation

Return the dot product of two vectors.

The vdot(a, b) function handles complex numbers differently than dot(a, b). If the first argument is complex the complex conjugate of the first argument is used for the calculation of the dot product.

Note that vdot handles multidimensional arrays differently than dot: it does not perform a matrix product, but flattens input arguments to 1-D vectors first. Consequently, it should only be used for vectors.

### 1.C.2 tests

## 1.D linalg.inner

### 1.D.1 documentation

Inner product of two arrays.

Ordinary inner product of vectors for 1-D arrays (without complex conjugation), in higher dimensions a sum product over the last axes.

### 1.D.2 tests

## 1.E linalg.outer

### 1.E.1 documentation

Compute the outer product of two vectors.

**Parameters** : a : (M,) array\_like First input vector. Input is flattened if not already 1-dimensional. b : (N,) array\_like Second input vector. Input is flattened if not already 1-dimensional.

out : (M, N) ndarray, optional A location where the result is stored

**Returns** : out : (M, N) ndarray  $out[i, j] = a[i] * b[j]$

### 1.E.2 tests

## 1.F linalg.matmul

### 1.F.1 documentation

Matrix product of two arrays.

The behavior depends on the arguments in the following way.

If both arguments are 2-D they are multiplied like conventional matrices.

If either argument is N-D,  $N \geq 2$ , it is treated as a stack of matrices residing in the last two indexes and broadcast accordingly.

If the first argument is 1-D, it is promoted to a matrix by prepending a 1 to its dimensions. After matrix multiplication the prepended 1 is removed.

If the second argument is 1-D, it is promoted to a matrix by appending a 1 to its dimensions. After matrix multiplication the appended 1 is removed.

Multiplication by a scalar is not allowed, use \* instead. Note that multiplying a stack of matrices with a vector will result in a stack of vectors, but matmul will not recognize it as such.

### 1.F.2 tests

## 1.G linalg.tensordot

### 1.G.1 documentation

Compute tensor dot product along specified axes for arrays  $\geq$  1-D.

Given two tensors (arrays of dimension greater than or equal to one), a and b, and an array\_like object containing two array\_like objects, (a\_axes, b\_axes), sum the products of a's and b's elements (components) over the axes specified by a\_axes and b\_axes. The third argument can be a single non-negative integer-like scalar, N; if it is such, then the last N dimensions of a and the first N dimensions of b are summed over.

## 1.G.2 tests

## 1.H linalg.matrix\_power

### 1.H.1 documentation

Raise a square matrix to the (integer) power n.

For positive integers n, the power is computed by repeated matrix squarings and matrix multiplications. If n == 0, the identity matrix of the same shape as M is returned. If n < 0, the inverse is computed and then raised to the abs(n).

### 1.H.2 tests

## 1.I linalg.eig

Compute the eigenvalues and right eigenvectors of a square array.

**Parameters** : a : (... , M, M) array

**Returns** : w : (... , M) array

Raises: LinAlgError If the eigenvalue computation does not converge.

### 1.I.1 documentation

### 1.I.2 tests

## 1.J linalg.eigh

### 1.J.1 documentation

Return the eigenvalues and eigenvectors of a Hermitian or symmetric matrix.

Returns two objects, a 1-D array containing the eigenvalues of a, and a 2-D square array or matrix (depending on the input type) of the corresponding eigenvectors (in columns).

**Parameters** : a : (... , M, M) array

**Returns** : w : (... , M) ndarray The eigenvalues in ascending order, each repeated according to its multiplicity.

Raises: LinAlgError If the eigenvalue computation does not converge.

### 1.J.2 tests

## 1.K linalg.eigvalsh

### 1.K.1 documentation

Compute the eigenvalues of a Hermitian or real symmetric matrix.

Main difference from `eigh`: the eigenvectors are not computed.

**Parameters** : `a` : (... , M, M) array\_like

**Returns** : `w` : (... , M,) ndarray The eigenvalues in ascending order, each repeated according to its multiplicity.

Raises: `LinAlgError` if the eigenvalue computation does not converge.

### 1.K.2 tests

## 1.L linalg.eigvals

### 1.L.1 documentation

Compute the eigenvalues of a general matrix.

Main difference between `eigvals` and `eig`: the eigenvectors are not returned.

**Parameters** : `a` : (... , M, M) array\_like A complex- or real-valued matrix whose eigenvalues will be computed.

**Returns** : `w` : (... , M,) ndarray The eigenvalues, each repeated according to its multiplicity. They are not necessarily ordered, nor are they necessarily real for real matrices.

Raises: `LinAlgError` If the eigenvalue computation does not converge.

### 1.L.2 tests

## 1.M linalg.norm

### 1.M.1 documentation

Matrix or vector norm.

This function is able to return one of eight different matrix norms, or one of an infinite number of vector norms (described below), depending on the value of the `ord` parameter.

**Parameters** : `x` : array\_like Input array. If `axis` is `None`, `x` must be 1-D or 2-D. `ord` : non-zero int, inf, -inf, fro, nuc, optional Order of the norm (see table under Notes). `inf` means `numpy.inf` object. `axis` : int, 2-tuple of ints, `None`, optional If `axis` is an integer, it specifies the axis of `x` along which to compute the vector norms. If `axis` is a 2-tuple, it specifies the axes that hold 2-D matrices, and the matrix norms of these matrices are computed. If `axis` is `None` then either a vector norm (when `x` is 1-D) or a matrix norm (when `x` is 2-D) is returned. `keepdims` : bool, optional If this is set to `True`, the axes which are normed over are left in the result as dimensions

with size one. With this option the result will broadcast correctly against the original x. New in version 1.10.0.

**Returns** : n : float or ndarray Norm of the matrix or vector(s).

## 1.M.2 tests

### 1.N linalg.matrix\_rank

#### 1.N.1 documentation

Return matrix rank of array using SVD method Rank of the array is the number of singular values of the array that are greater than 'tol'.

**Parameters** : M : (M,), (... , M, N) array\_like input vector or stack of matrices tol : (...) array\_like, float, optional threshold below which SVD values are considered zero. If 'tol' is None, and "S" is an array with singular values for 'M', and "eps" is the epsilon value for datatype of "S", then 'tol' is set to "S.max() \* max(M.shape) \* eps" Broadcasted against the stack of matrices hermitian : bool, optional If True, 'M' is assumed to be Hermitian (symmetric if real-valued), enabling a more efficient method for finding singular values. Defaults to False.

**Returns** :

#### 1.N.2 tests

test\_simple\_case: a simple 3X3 eye matrix is tested

test\_scalar: the rank of a scalar input equates to 1.

test\_array: same as above but a scalar inside an array.

test\_zero\_rank: the rank of a matrix with zeros will equate to 0.

test\_1\_dimensional\_matrix: the rank of a 1 dimensional matrix should be 1.

These tests were written to test the functionality of matrix rank with various simple inputs.

### 1.O linalg.det, linalg.slogdet

#### 1.O.1 documentation

Determinants are used to define the characteristic polynomial of a matrix and whether it has a unique solution or not. This function computes the sign and (natural) logarithm of the determinant of an array. A number representing the sign of the determinant. For a real matrix, this is 1, 0, or -1. For a complex matrix, this is a complex number with absolute value 1 (i.e., it is on the unit circle), or else 0. The determinant is computed via LU factorization using the LAPACK routine z/dgetrf. The determinant of a 2-D array "[[a, b], [c, d]]" is "ad - bc". (sign, logdet) = np.linalg.slogdet(a)

**Parameters** : An array or matrix with single, double, complex single or complex double type.

**Returns** : A scalar.

### 1.O.2 tests

`test_det`: This tests that the determinant calculation works according to the above.

`test_size_zero`: This tests that the sign of the determinant an empty matrix is a complex number and that the determinant itself is 1.

`test_types`: This tests that the output type of the determinant is the same as the input type, i.e. single, double, csingle and cdouble.

These tests were written to test matrix determinants with various simple inputs.

## 1.P linalg.multidot (Black box tests)

### 1.P.1 documentation

Compute the dot product of two or more arrays in a single function call, while automatically selecting the fastest evaluation order. ‘multi\_dot’ chains ‘numpy.dot’ and uses optimal parenthesization of the matrices. Depending on the shapes of the matrices, this can speed up the multiplication a lot. If the first argument is 1-D it is treated as a row vector. If the last argument is 1-D it is treated as a column vector. The other arguments must be 2-D.

`TestCases`: Test cases are created so that vectors when multiplied share the same dimensions. When matrices are multiplied they need to be organized so that the first dimension of the first matrix is the same as the second dimension of the second matrix etc.

**Parameters** : Vectors or matrices. They must be organized so that the first dimension of the first matrix is the same as the second dimension of the second matrix etc.

**Returns** : A vector or matrix whose dimension depends on the inputs.

### 1.P.2 Tests

`test_three_inputs_vectors`: This tests the multidot function with three vectors. The assert is the following: `assert_almost_equal(multi_dot([A, B]), A.dot(B))`

`test_three_inputs_matrices`: This tests the multidot function with three matrices

`test_four_inputs_matrices`: This tests the multidot function with four matrices

`test_shape_vector_first`: This tests the multidot function with a vector with n rows as the first argument followed by three matrices with dimensions n, m and m, n. The shape result sought is the same as the vector, i.e. 1 dimensional with n rows.

`test_shape_vector_last`: This tests the multidot function with a n rows vector as the last argument preceded by three matrices with dimensions m, n and n, m. The shape result sought is

m.

`test_shape_vector_first_and_last`: This tests the `multidot` function with `n` rows vector as the first and last arguments with two matrices with dimensions `n, m` and `m, n` in the middle. The shape result sought is `()` since the result is a scalar. `assert_equal(multidot([A1d, B, C, D1d]).shape, ())`

`test_types`: This runs the `test_three_inputs_matrices` above using integers, doubles, complex numbers.

These tests were written to test the functionality of `multidot` with various inputs. All test cases are initialized with random values.

## 2 White-Box Test

In this section we aim to use what we can see from the functions themselves to satisfy some coverage criteria. To evaluate coverage we will use the `coverage.py` package. This can evaluate both statement and branch coverage and enumerate which statements or branches were not executed.

The function we have chosen to white box test is the `multi_dot()` function and it's subsidiary functions `_multi_dot()` and `multi_dot_three()`.

**Node Coverage** For node coverage we have the critereon that our tests cause all statements to be executed. Figure 1 shows the control flow graph for the functions under test.

**Edge Coverage** For edge coverage we have the critereon that our tests cause all branches to execute. In this case we have the set of edges  $\{(1,2),(1,3),(1,4),(4,5),(4,6),(5,6),(6,7),(6,8),(8,9),(8,10),(8,12),(12,10),(10,16),(9,11),(11,13),(13,14),(13,15),(15,16),(16,17),(16,18),(16,19)\}$ . Our test requirements are that every edge is contained in at least one of our test paths.

### 2.A Test: Arguments<sub>1</sub>=2

This test gives us node coverage for  $\{1,2\}$  and branch coverage for  $\{(1,2)\}$ . It returns a raises value error.

### 2.B Test: Arguments<sub>1</sub>=2

This test gives us node coverage for  $\{1,3\}$  and branch coverage for  $\{(1,3)\}$ . It returns the dot product of the two.

### 2.C Test: Arguments<sub>1</sub>=3,dimension of 1st argument = 1

This test gives us node coverage for  $\{1,4,5,6,8,9,11,13,14,16,17\}$  and branch coverage for  $\{(1,4),(4,5),(6,8),(8,9),(9,11),(11,13),(13,14),(14,16),(16,17)\}$ .

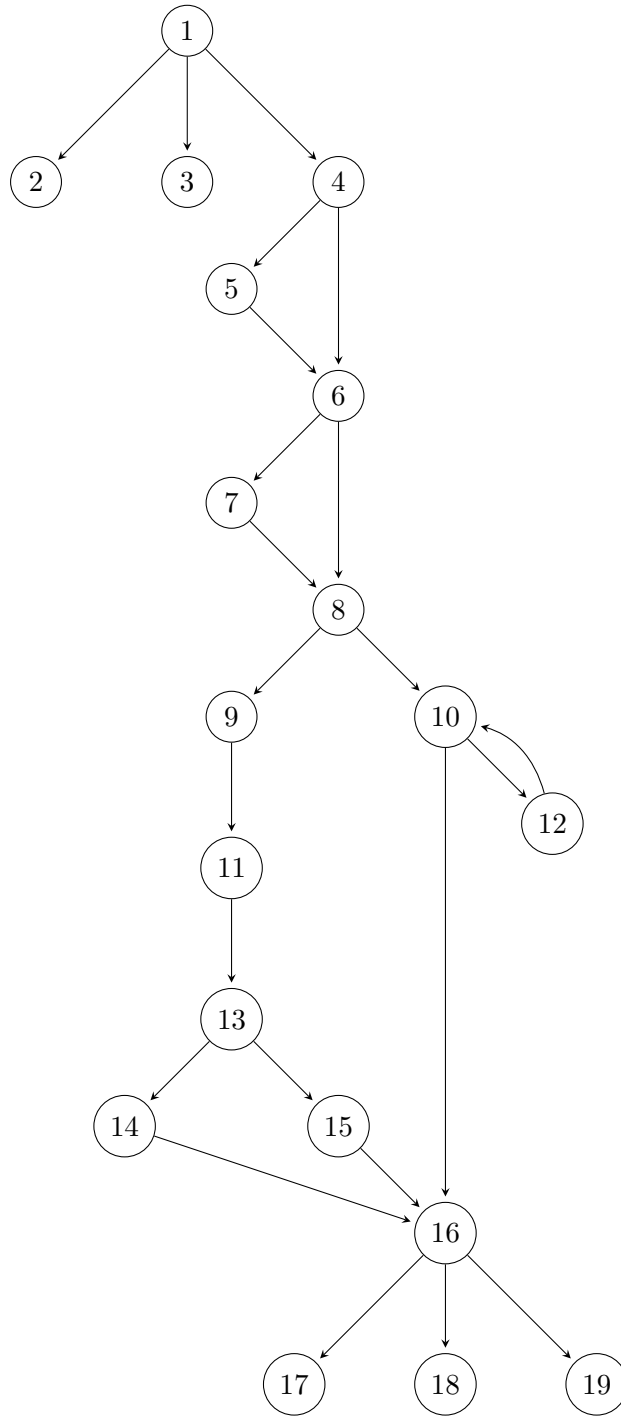


Figure 1: The control flow graph for `multi_dot()`, `multi_dot_three()` and `_multi_dot()`



**2.D Test: Arguments=3,dimension of last argument = 1**

**2.E Test: Arguments=3,dimension of first and last argument = 1**

## 3 Appendix

### 3.A whitebox

```
import numpy as np
import unittest
import random as rand
```

```
from numpy import array, single, double, csingle, cdouble, dot, identity, empty
from numpy import multiply, atleast_2d, inf, asarray, matrix
import linpy
#from linalg import matrix_power, norm, matrix_rank, multi_dot, LinAlgError
#from linalg import _multi_dot_matrix_chain_order
#from numpy.testing import (
#    assert_, assert_equal, assert_raises, assert_array_equal,
#    assert_almost_equal, assert_allclose, run_module_suite,
#    dec, SkipTest)
```

```
class WhiteBox(unittest.TestCase):
```

```
    def setUp(self):
```

```
        self.array_2_2_identity = np.identity(2)
        self.array_1 = np.array([[1,2],[3,4]])
        self.array_2 = np.array([[5,6],[7,8]])
        self.array_3 = np.array([[9,10,11],[12,13,14],[15,16,17]])
        self.array_4 = np.array([[6,5],[5,3],[12,15]])
        #self.array_multi_5 = np.rand.rand(3,2)
```

```
        """ Empty Test [1](http://gettingsharper.de/2011/11/30/vector-fun-dot-pr
        self.array_empty = np.empty([2,2])
```

```
        """ Linear Test [1] """
```

```
        self.array_com_3 = [12.4, -1.7, 3.15]
        self.scalar = 0.22
        self.sint = np.array([7,7])
        self.sfloat = np.array([6.6,6.6])
```

```
        """ Basic test no need to test with floats/ints/complex as this function
```

```
        """ Perpendicular Test [1] """
```

```
        self.array_per_1 = [2.0, 1.0, 4.0]
        self.array_per_2 = [1.0, -1.0, -0.25]
```

```
        """
```

```
        Testing numpy.linalg.dot() function
```

```
        """
```

```

def test_multi_dot_raises(self):
    with self.assertRaises(ValueError):
        actual = linpy.multi_dot([self.array_1])

#         try:
#             self.assertFalse(True)
#         except ValueError:
#             pass

#test 2
def test_multi_two(self):
    actual = linpy.multi_dot([self.array_1, self.array_2])
    expected1 = np.array([[19, 22], [43, 50]])
    self.assertTrue((actual == expected1).all())

def test_multi_ndim_01(self):
    actual = linpy.multi_dot([self.sint, self.array_1, self.array_2])
    expected = np.array([434, 504])
    self.assertTrue((actual == expected).all())

def test_multi_ndim_00(self):
    actual = linpy.multi_dot([self.array_4, self.array_1, self.array_2])
    expected = np.array([[329, 382], [224, 260], [873, 1014]])
    self.assertTrue((actual == expected).all())

def test_multi_ndim_end1(self):
    actual = linpy.multi_dot([self.array_1, self.array_2, self.sint])
    expected = np.array([287, 651])
    self.assertTrue((actual == expected).all())

def test_multi_ndim_11(self):
    actual = linpy.multi_dot([self.sint, self.array_1, self.array_2, self.sflo])
    expected = np.array([6190.8])
    self.assertAlmostEqual(actual, expected)

if __name__ == '__main__':
    unittest.main()

```

### 3.B linalg.dot

```
class numpy as np
import unittest

class TestLinAlg(unittest.TestCase):

    def setUp(self):
        """http://gettingsharper.de/2011/11/30/vector-fun-dot-product/"""

        Basic Identity Test / Square Test
        self.array_1 = [[1, 0], [0, 1]]
        self.array_2 = [[4, 1], [2, 2]]

        Zero Test
        self.array_zero = [0, 0]

        Commutative Test
        self.array_com_1 = [-3.22, 2.25, -0.13]
        self.array_com_2 = [0.0, -6.7, 10.0]

        Linear Test
        self.array_com_3 = [12.4, -1.7, 3.15]
        self.scalar = 0.22

        Perpendicular Test
        self.array_per_1 = [2.0, 1.0, 4.0]
        self.array_per_2 = [1.0, -1.0, -0.25]
```

```
def test_dot_corner(self):
    actual = np.dot([ ], [ ])
    expected = False
    self.assertEqual(actual, expected);
```

```
def test_dot_corner2(self):
    with self.assertRaises(ValueError):
        actual = np.dot([ ], [1, 2])
```

```
def test_dot_identity(self):
    actual = np.dot(self.array_1, self.array_2)
    expected = [[4, 1], [2, 2]]
    self.assertTrue((actual == expected).all())
```

```

def test_dot_zero(self):
    actual = np.dot(self.array_zero, self.array_2)
    expected = 0
    self.assertTrue((actual == expected).all())

```

```

def test_dot_commutative(self):
    actual = np.dot(self.array_com_1, self.array_com_2)
    expected = np.dot(self.array_com_2, self.array_com_1)
    self.assertTrue((actual == expected).all())

```

```

def test_dot_square(self):
    actual = np.dot(self.array_2, self.array_2)
    expected = [[18, 6], [12, 6]]
    self.assertTrue((actual == expected).all())

```

```

def test_dot_perpendicuar(self):
    actual = np.dot(self.array_per_1, self.array_per_2)
    expected = 0
    self.assertTrue((actual == expected).all())

```

```

def test_dot_raises(self):
    with self.assertRaises(ValueError):
        actual = np.dot([2, 2, 3], [2, 1])

```

### 3.C linalg.vdot

```

class TestLinAlg(unittest.TestCase):
    def setUp(self):
        self.array_a = np.array([[1, 4], [5, 6]])
        self.array_b = np.array([[4, 1], [2, 2]])

        self.array_a_float = np.array([1.0, 4.5])
        self.array_b_float = np.array([3.0, 2.5])

    def setUpForComplex(self):
        self.complex_a = np.array([1+2j, 3+4j])
        self.complex_b = np.array([5+6j, 7+8j])
        self.complex_c = np.array([-5-6j, -7-8j])

```

```

def test_vdot_square(self):
    actual = np.vdot(self.array_a, self.array_a)
    expected = 78
    self.assertTrue(actual == expected)

```

```
def test_vdot_complexSquare(self):
    self.setupForComplex()

    actual = np.vdot(self.complex_a, self.complex_a)
    expected = 30+0j

    self.assertTrue(actual == expected)
```

```
def test_vdot_normal(self):
    self.setupForComplex()
    actual = np.vdot(self.complex_a, self.complex_b)
    expected = 70-8j
    self.assertTrue(actual == expected)
```

```
def test_vdot_com(self):
    self.setupForComplex()
    actual = np.vdot(self.array_a, self.array_b)
    expected = np.vdot(self.array_b, self.array_a)
    self.assertTrue(actual == expected)
```

```
def test_vdot_negative(self):
    self.setupForComplex()
    actual = np.vdot(self.complex_c, self.complex_a)
    expected = -70-8j
    self.assertTrue(actual == expected)
```

```
def test_vdot_float(self):
    actual = np.vdot(self.array_a_float, self.array_b_float)
    expected = 14.25
    self.assertTrue(actual == expected)
```

```
def test_vdot_empty(self):
    actual = np.vdot([],[])
    self.assertFalse(actual)
```

### 3.D linalg.inner

```
def setUp(self):
```

```
    self.array_a = np.array([1, 2, 3])
    self.array_b = np.array([0, 1, 0])

    self.array_a_float = np.array([1.0, 2.0, 4.5])
    self.array_b_float = np.array([3.0, 3.5, 2.5])
```

*Inner Product Wolfram*

<http://mathworld.wolfram.com/InnerProduct.html>

```
    self.vector_u = np.array([1,2,3])
    self.vector_v = np.array([1,2,1])
    self.vector_w = np.array([4,5,6])
    self.scalar = 5
    self.vector_zero = np.array([0, 0, 0])
```

```
def test_inner_simple(self):
```

```
    actual = np.inner(self.array_a, self.array_b)
    expected = 2
    self.assertTrue(actual == expected)
```

```
def test_inner_zero(self):
```

```
    actual = np.inner(self.array_a, [0, 0, 0])
    expected = 0
    self.assertTrue(actual == expected)
```

```
def test_inner_float(self):
```

```
    actual = np.inner(self.array_a_float, self.array_b_float)
    expected = 21.25
    self.assertTrue(actual == expected)
```

```
def test_inner_prop1(self):
```

```
    actual = np.inner(np.add(self.vector_u, self.vector_v), self.vector_w)
    expected = np.add(np.inner(self.vector_u, self.vector_w),
np.inner(self.vector_v, self.vector_w))
    self.assertTrue(actual == expected)
```

```
def test_inner_prop2(self):
```

```
    actual = np.inner(self.scalar * self.vector_v, self.vector_w)
    expected = self.scalar * np.inner(self.vector_v, self.vector_w)
    self.assertTrue(actual == expected)
```

```
def test_inner_prop3(self):  
    actual = np.inner(self.vector_v, self.vector_w)  
    expected = np.inner(self.vector_w, self.vector_v)  
    self.assertTrue(actual == expected)
```

```
def test_inner_prop4(self):  
    actual = np.inner(self.vector_zero, self.vector_zero)  
    expected = 0  
    self.assertTrue(actual == expected)
```

```
def test_inner_raises(self):  
    with self.assertRaises(ValueError):  
        actual = np.inner([2, 2, 3], [2, 1])
```

### 3.E test\_multi\_dot

```
CASES = []

dimension1 = np.random.randint(1, 12)
dimension2 = np.random.randint(1, 12)

CASES += [np.random.random((dimension1, dimension2)), # 0
          np.random.random((dimension2, dimension1)),
          np.random.random((dimension1, dimension2)),
          np.random.random((dimension2, dimension1)),
          np.random.random(dimension1),
          np.random.random(dimension1), # 5]

class TestMultiDot(unittest.TestCase):

    def test_two_inputs_vectors(self):
        A = CASES[4]
        B = CASES[5]

        assert_almost_equal(multi_dot([A, B]), A.dot(B))
        assert_almost_equal(multi_dot([A, B]), np.dot(A, B))

    def test_three_inputs_vectors(self):
        A = CASES[4]
        B = CASES[5]
        C = CASES[2]

        # running multi-dot on three equal size vectors should result in a multi_dot error
        try:
            assert_almost_equal(multi_dot([A, B, C]), np.dot(np.dot(A, B), C))
        except Exception:
            pass

    def test_three_inputs_matrices(self):
        A = CASES[0]
        B = CASES[1]
        C = CASES[2]

        assert_almost_equal(multi_dot([A, B, C]), A.dot(B).dot(C))
        assert_almost_equal(multi_dot([A, B, C]), np.dot(A, np.dot(B, C)))

        #when the inputs are in the wrong order
        try:
            assert_almost_equal(multi_dot([A, C, B]), np.dot(np.dot(A, C), C))
        except Exception:
            pass

    def test_four_inputs_matrices(self):
        A = CASES[0]
        B = CASES[1]
        C = CASES[2]
        D = CASES[3]

        assert_almost_equal(multi_dot([A, B, C, D]), A.dot(B).dot(C).dot(D))

        # when the inputs are in the wrong order
        try:
            assert_almost_equal(multi_dot([A, C, B]), np.dot(np.dot(A, C), C))
        except Exception:
            pass

    def test_vector_as_first_argument(self):
        # The first argument can be 1-D
        A1d = np.random.random(2) # 1-D
        B = np.random.random((2, 6))
        C = np.random.random((6, 2))
        D = np.random.random((2, 2))

        # the result should be 1-D
        assert_equal(multi_dot([A1d, B, C, D]).shape, (2,))

    def test_vector_as_last_argument(self):
        # The last argument can be 1-D
        A = np.random.random((6, 2))
        B = np.random.random((2, 6))
        C = np.random.random((6, 2))
        D1d = np.random.random(2) # 1-D

        # the result should be 1-D
        assert_equal(multi_dot([A, B, C, D1d]).shape, (6,))

    def test_vector_as_first_and_last_argument(self):
        # The first and last arguments can be 1-D
        A1d = np.random.random(2) # 1-D
        B = np.random.random((2, 6))
        C = np.random.random((6, 2))
        D1d = np.random.random(2) # 1-D

        # the result should be a scalar
        assert_equal(multi_dot([A1d, B, C, D1d]).shape, ())
```



### 3.F test\_matrix\_rank

```
class TestMatrixRank(unittest.TestCase):

    def test_simple_case(self):
        # the rank of a 3X3 matrix is 3
        assert_equal(linalg.matrix_rank(np.eye(3)), 3)

    def test_scalar(self):
        assert_equal(matrix_rank(1), 1)

    def test_array(self):
        # the rank of an array with a single value should be one
        assert_equal(matrix_rank([1]), 1)

    def test_zero_rank(self):
        assert_equal(linalg.matrix_rank(np.zeros((4, 4))), 0)

    def test_1_dimensional_matrix(self):
        assert_equal(matrix_rank([1, 0, 0, 0]), 1)
```

### 3.G test\_matrix\_determinant

```
class TestDet(unittest.TestCase):
    def test_empty_simple(self):
        assert_equal(linalg.det([[0.0]]), 0.0)

    def test_det_empty_types(self):
        assert_equal(type(linalg.det([[0.0]])), double)
        assert_equal(linalg.det([[0.0j]]), 0.0)
        assert_equal(type(linalg.det([[0.0j]])), cdouble)

    def test_slogdet_empty_types(self):
        assert_equal(linalg.slogdet([[0.0j]]), (0.0j, -inf))
        assert_equal(type(linalg.slogdet([[0.0j]])[0]), cdouble)
        assert_equal(type(linalg.slogdet([[0.0j]])[1]), double)
        assert_equal(linalg.slogdet([[0.0]]), (0.0, -inf))
        assert_equal(type(linalg.slogdet([[0.0]])[0]), double)
        assert_equal(type(linalg.slogdet([[0.0]])[1]), double)

    def test_size_simple(self):
        # create an empty array
        empty_array = np.zeros((0, 0))
        # compute the determinant
        determinant_result = linalg.det(empty_array)
        # make sure the result is 1
        assert_equal(determinant_result, 1.)

        #do the same for slogdet
        determinant_result = linalg.slogdet(empty_array)

        #the result in this case should be (1, 0)
        assert_equal(determinant_result, (1, 0))
```

### 3.H test\_datatypes

```

# GLOBAL FUNCTIONS
def get_real_dtype(dtype):
    return {single: single, double: double,
            csingle: single, cdouble: double}[dtype]

class LinalgCase(object):
    def __init__(self, name, a, b, tags=set()):

        assert_(isinstance(name, str))
        self.name = name
        self.a = a
        self.b = b
        self.datatype = frozenset(tags) # prevent shared tags

CASES = []

CASES += [LinalgCase("single",
                    array([1., 1., 1.], dtype=single),
                    array([1., 1., 1.], dtype=single)),
         LinalgCase("double",
                    array([1., 2.], [3., 4.], dtype=double),
                    array([2., 1.], dtype=double)),
        ]

class TestDatatypes(unittest.TestCase):

    def test_invTypes(self):
        x = np.array([[1, 0.5], [0.5, 1]], dtype=single)
        assert_equal(linalg.solve(x, x).dtype, single)

    def test_EigvalTypes(self):
        def check(dtype):
            x = np.array([[1, 0.5], [0.5, 1]], dtype=dtype)
            assert_equal(linalg.eigvals(x).dtype, dtype)
        for dtype in [single, double, csingle, cdouble]:
            yield check, dtype

    def test_EigvalHermitianTypes(self):
        def check(dtype):
            x = np.array([[1, 0.5], [0.5, 1]], dtype=dtype)
            w = np.linalg.eigvalsh(x)
            assert_equal(w.dtype, get_real_dtype(dtype))
        for dtype in [single, double, csingle, cdouble]:
            yield check, dtype

    def test_EigTypes(self):
        def check(dtype):
            x = np.array([[1, 0.5], [0.5, 1]], dtype=dtype)
            w, v = np.linalg.eig(x)
            assert_equal(w.dtype, dtype)
            assert_equal(v.dtype, dtype)

        for dtype in [single, double, csingle, cdouble]:
            yield check, dtype

    def test_SVDtypes(self):
        def check(dtype):
            x = np.array([[1, 0.5], [0.5, 1]], dtype=dtype)
            u, s, vh = linalg.svd(x)
            assert_equal(u.dtype, dtype)
        for dtype in [single, double, csingle, cdouble]:
            yield check, dtype

    def test_determinantTypes(self):
        def check(dtype):
            x = np.array([[1, 0.5], [0.5, 1]], dtype=dtype)
            assert_equal(np.linalg.det(x).dtype, dtype)
        for dtype in [single, double, csingle, cdouble]:
            yield check, dtype

if __name__ == '__main__':
    unittest.main()

```