

## Codeforces Round #326 (Div. 1)

### A. Duff and Weight Lifting

time limit per test: 1 second  
 memory limit per test: 256 megabytes  
 input: standard input  
 output: standard output

Recently, Duff has been practicing weight lifting. As a hard practice, Malek gave her a task. He gave her a sequence of weights. Weight of  $i$ -th of them is  $2^{w_i}$  pounds. In each step, Duff can lift some of the remaining weights and throw them away. She does this until there's no more weight left. Malek asked her to minimize the number of steps.

Duff is a competitive programming fan. That's why in each step, she can only lift and throw away a sequence of weights  $2^{a_1}, \dots, 2^{a_k}$  if and only if there exists a non-negative integer  $X$  such that  $2^{a_1} + 2^{a_2} + \dots + 2^{a_k} = 2^X$ , i. e. the sum of those numbers is a power of two.

Duff is a competitive programming fan, but not a programmer. That's why she asked for your help. Help her minimize the number of steps.

#### Input

The first line of input contains integer  $n$  ( $1 \leq n \leq 10^6$ ), the number of weights.

The second line contains  $n$  integers  $w_1, \dots, w_n$  separated by spaces ( $0 \leq w_i \leq 10^6$  for each  $1 \leq i \leq n$ ), the powers of two forming the weights values.

#### Output

Print the minimum number of steps in a single line.

#### Examples

<b>input</b>
5 1 1 2 3 3
<b>output</b>
2
<b>input</b>
4 0 1 2 3
<b>output</b>
4

#### Note

In the first sample case: One optimal way would be to throw away the first three in the first step and the rest in the second step. Also, it's not possible to do it in one step because their sum is not a power of two.

In the second sample case: The only optimal way is to throw away one weight in each step. It's not possible to do it in less than 4 steps because there's no subset of weights with more than one weight and sum equal to a power of two.

## B. Duff in Beach

time limit per test: 2 seconds  
memory limit per test: 256 megabytes  
input: standard input  
output: standard output

While Duff was resting in the beach, she accidentally found a strange array  $b_0, b_1, \dots, b_{l-1}$  consisting of  $l$  positive integers. This array was strange because it was extremely long, but there was another (maybe shorter) array,  $a_0, \dots, a_{n-1}$  that  $b$  can be build from  $a$  with formula:  $b_i = a_{i \bmod n}$  where  $a \bmod b$  denoted the remainder of dividing  $a$  by  $b$ .



Duff is so curious, she wants to know the number of subsequences of  $b$  like  $b_{i_1}, b_{i_2}, \dots, b_{i_x}$  ( $0 \leq i_1 < i_2 < \dots < i_x < l$ ), such that:

- $1 \leq x \leq k$
- For each  $1 \leq j \leq x - 1$ ,  $\lfloor \frac{b_j}{n} \rfloor + 1 = \lfloor \frac{b_{j+1}}{n} \rfloor$
- For each  $1 \leq j \leq x - 1$ ,  $b_j \leq b_{j+1}$ . i.e this subsequence is non-decreasing.

Since this number can be very large, she want to know it modulo  $10^9 + 7$ .

Duff is not a programmer, and Malek is unavailable at the moment. So she asked for your help. Please tell her this number.

### Input

The first line of input contains three integers,  $n, l$  and  $k$  ( $1 \leq n, k, n \times k \leq 10^6$  and  $1 \leq l \leq 10^{18}$ ).

The second line contains  $n$  space separated integers,  $a_0, a_1, \dots, a_{n-1}$  ( $1 \leq a_i \leq 10^9$  for each  $0 \leq i \leq n - 1$ ).

### Output

Print the answer modulo 1 000 000 007 in one line.

### Examples

input
3 5 3 5 9 1
output
10

input
5 10 3 1 2 3 4 5
output
25

### Note

In the first sample case,  $b = \langle 5, 9, 1, 5, 9 \rangle$ . So all such sequences are:  $\langle b_0 \rangle = \langle 5 \rangle$ ,  $\langle b_1 \rangle = \langle 9 \rangle$ ,  $\langle b_2 \rangle = \langle 1 \rangle$ ,  $\langle b_3 \rangle = \langle 5 \rangle$ ,  $\langle b_4 \rangle = \langle 9 \rangle$ ,  $\langle b_0, b_3 \rangle = \langle 5, 5 \rangle$ ,  $\langle b_0, b_4 \rangle = \langle 5, 9 \rangle$ ,  $\langle b_1, b_4 \rangle = \langle 9, 9 \rangle$ ,  $\langle b_2, b_3 \rangle = \langle 1, 5 \rangle$  and  $\langle b_2, b_4 \rangle = \langle 1, 9 \rangle$ .

## C. Duff in the Army

time limit per test: 4 seconds  
memory limit per test: 512 megabytes  
input: standard input  
output: standard output

Recently Duff has been a soldier in the army. Malek is her commander.

Their country, Andarz Gu has  $n$  cities (numbered from  $1$  to  $n$ ) and  $n - 1$  bidirectional roads. Each road connects two different cities. There exist a unique path between any two cities.

There are also  $m$  people living in Andarz Gu (numbered from  $1$  to  $m$ ). Each person has an ID number. ID number of  $i$ -th person is  $i$  and he/she lives in city number  $C_i$ . Note that there may be more than one person in a city, also there may be no people living in the city.



Malek loves to order. That's why he asks Duff to answer to  $q$  queries. In each query, he gives her numbers  $v$ ,  $u$  and  $a$ .

To answer a query:

Assume there are  $x$  people living in the cities lying on the path from city  $v$  to city  $u$ . Assume these people's IDs are  $p_1, p_2, \dots, p_x$  in increasing order.

If  $k = \min(x, a)$ , then Duff should tell Malek numbers  $k, p_1, p_2, \dots, p_k$  in this order. In other words, Malek wants to know  $a$  minimums on that path (or less, if there are less than  $a$  people).

Duff is very busy at the moment, so she asked you to help her and answer the queries.

### Input

The first line of input contains three integers,  $n$ ,  $m$  and  $q$  ( $1 \leq n, m, q \leq 10^5$ ).

The next  $n - 1$  lines contain the roads. Each line contains two integers  $v$  and  $u$ , endpoints of a road ( $1 \leq v, u \leq n, v \neq u$ ).

Next line contains  $m$  integers  $C_1, C_2, \dots, C_m$  separated by spaces ( $1 \leq C_i \leq n$  for each  $1 \leq i \leq m$ ).

Next  $q$  lines contain the queries. Each of them contains three integers,  $v$ ,  $u$  and  $a$  ( $1 \leq v, u \leq n$  and  $1 \leq a \leq 10$ ).

### Output

For each query, print numbers  $k, p_1, p_2, \dots, p_k$  separated by spaces in one line.

### Examples

input
5 4 5 1 3 1 2 1 4 4 5 2 1 4 3 4 5 6 1 5 2 5 5 10 2 3 3 5 3 1
output
1 3 2 2 3 0 3 1 2 4 1 2

### Note

Graph of Andarz Gu in the sample case is as follows (ID of people in each city are written next to them):



## D. Duff in Mafia

time limit per test: 6 seconds  
memory limit per test: 256 megabytes  
input: standard input  
output: standard output

Duff is one of the heads of Mafia in her country, Andarz Gu. Andarz Gu has  $n$  cities (numbered from 1 to  $n$ ) connected by  $m$  bidirectional roads (numbered by 1 to  $m$ ).

Each road has a destructing time, and a color.  $i$ -th road connects cities  $v_i$  and  $u_i$  and its color is  $c_i$  and its destructing time is  $t_i$ .

Mafia wants to destruct a *matching* in Andarz Gu. A *matching* is a subset of roads such that no two roads in this subset has common endpoint. They can destruct these roads in parallel, i. e. the total destruction time is a maximum over destruction times of all selected roads.

They want two conditions to be satisfied:

1. The remaining roads form a *proper coloring*.
2. Destructing time of this matching is minimized.

The remaining roads after destructing this matching form a *proper coloring* if and only if no two roads of the same color have same endpoint, or, in the other words, edges of each color should form a *matching*.

There is no programmer in Mafia. That's why Duff asked for your help. Please help her and determine which matching to destruct in order to satisfied those conditions (or state that this is not possible).

### Input

The first line of input contains two integers  $n$  and  $m$  ( $2 \leq n \leq 5 \times 10^4$  and  $1 \leq m \leq 5 \times 10^4$ ), number of cities and number of roads in the country.

The next  $m$  lines contain the the roads.  $i$ -th of them contains four integers  $v_i, u_i, c_i$  and  $t_i$  ( $1 \leq v_i, u_i \leq n, v_i \neq u_i$  and  $1 \leq c_i, t_i \leq 10^9$  for each  $1 \leq i \leq m$ ).

### Output

In the first line of input, print "Yes" (without quotes) if satisfying the first condition is possible and "No" (without quotes) otherwise.

If it is possible, then you have to print two integers  $t$  and  $k$  in the second line, the minimum destructing time and the number of roads in the matching ( $0 \leq k \leq \lfloor \frac{m}{2} \rfloor$ ).

In the third line print  $k$  distinct integers separated by spaces, indices of the roads in the matching in any order. Roads are numbered starting from one in order of their appearance in the input.

If there's more than one solution, print any of them.

### Examples

input
5 7 2 1 3 7 3 1 1 6 5 4 1 8 4 5 1 1 3 2 2 3 4 5 2 5 2 3 2 4
output
Yes 3 2 4 5

  

input
3 5 3 2 1 3 1 3 1 1 3 2 1 4 1 3 2 2 1 3 2 10
output
No

### Note

Graph of Andarz Gu in the first sample case is as follows:

A solution would be to destruct the roads with crosses.



Graph of Andarz Gu in the second sample case is as follows:



## E. Duff as a Queen

time limit per test: 7 seconds  
memory limit per test: 256 megabytes  
input: standard input  
output: standard output

Duff is the queen of her country, Andarz Gu. She's a competitive programming fan. That's why, when he saw her minister, Malek, free, she gave her a sequence consisting of  $n$  non-negative integers,  $a_1, a_2, \dots, a_n$  and asked him to perform  $q$  queries for her on this sequence.



There are two types of queries:

1. given numbers  $l, r$  and  $k$ , Malek should perform  $a_i = a_i \oplus k$  for each  $l \leq i \leq r$  ( $a \oplus b = a \text{ xor } b$ , bitwise exclusive OR of numbers  $a$  and  $b$ ).
2. given numbers  $l$  and  $r$  Malek should tell her the score of sequence  $a_l, a_{l+1}, \dots, a_r$ .

Score of a sequence  $b_1, \dots, b_k$  is the number of its different Kheshtaks. A non-negative integer  $w$  is a Kheshtak of this sequence if and only if there exists a subsequence of  $b$ , let's denote it as  $b_{i_1}, b_{i_2}, \dots, b_{i_x}$  (possibly empty) such that  $w = b_{i_1} \oplus b_{i_2} \oplus \dots \oplus b_{i_x}$  ( $1 \leq i_1 < i_2 < \dots < i_x \leq k$ ). If this subsequence is empty, then  $w = 0$ .

Unlike Duff, Malek is not a programmer. That's why he asked for your help. Please help him perform these queries.

### Input

The first line of input contains two integers,  $n$  and  $q$  ( $1 \leq n \leq 2 \times 10^5$  and  $1 \leq q \leq 4 \times 10^4$ ).

The second line of input contains  $n$  integers,  $a_1, a_2, \dots, a_n$  separated by spaces ( $0 \leq a_i \leq 10^9$  for each  $1 \leq i \leq n$ ).

The next  $q$  lines contain the queries. Each line starts with an integer  $t$  ( $1 \leq t \leq 2$ ), type of the corresponding query. If  $t = 1$ , then there are three more integers in that line,  $l, r$  and  $k$ . Otherwise there are two more integers,  $l$  and  $r$ . ( $1 \leq l \leq r \leq n$  and  $0 \leq k \leq 10^9$ )

### Output

Print the answer of each query of the second type in one line.

### Examples

input
5 5 1 2 3 4 2 2 1 5 1 2 2 8 2 1 5 1 1 3 10 2 2 2
output
8 16 1

### Note

In the first query, we want all Kheshtaks of sequence 1, 2, 3, 4, 2 which are: 0, 1, 2, 3, 4, 5, 6, 7.

In the third query, we want all Kheshtaks of sequence 1, 10, 3, 4, 2 which are:  
0, 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15.

In the fifth query, we want all Kheshtaks of sequence 0 which is 0.

## F. Duff is Mad

time limit per test: 4 seconds  
memory limit per test: 256 megabytes  
input: standard input  
output: standard output

Duff is mad at her friends. That's why she sometimes makes Malek to take candy from one of her friends for no reason!



She has  $n$  friends. Her  $i$ -th friend's name is  $S_i$  (their names are not necessarily unique).  $q$  times, she asks Malek to take candy from her friends. She's angry, but also she acts with rules. When she wants to ask Malek to take candy from one of her friends, like  $k$ , she chooses two numbers  $l$  and  $r$  and tells Malek to take exactly  $\sum_{i=l}^r \text{occur}(s_i, s)$  candies from him/her, where  $\text{occur}(t, s)$  is the number of occurrences of string  $t$  in  $S$ .

Malek is not able to calculate how many candies to take in each request from Duff. That's why she asked for your help. Please tell him how many candies to take in each request.

### Input

The first line of input contains two integers  $n$  and  $q$  ( $1 \leq n, q \leq 10^5$ ).

The next  $n$  lines contain the names.  $i$ -th of them contains a string  $S_i$ , consisting of lowercase English letters ( $1 \leq \sum_{i=1}^n |S_i| \leq 10^6$ ).

The next  $q$  lines contain the requests. Each of them contains three integers,  $l$ ,  $r$  and  $k$  (says that Malek should take  $\sum_{i=l}^r \text{occur}(s_i, s_k)$  candies from Duff's  $k$ -th friend).

### Output

Print the answer to each request in one line.

### Examples

input
5 5 a ab abab ababab b 1 5 4 3 5 4 1 5 2 1 5 3 1 4 1
output
12 6 3 7 1