Quiz 1 • Graded

Student

LAVESH GUPTA

Total Points

20 / 20 pts

Question 1

True False 9 / 9 pts

1.1 1 3 / 3 pts

- - - 1 pt Minor mistakes in proof -- cannot think of examples of minor mistakes :)
 - + 0 pts Totally wrong or else unanswered
 - + 0 pts Excessive Scratching / Overwriting

1.2 2 3 / 3 pts

- → + 1 pt Correct answer is F
- \checkmark + 2 pts Valid counter example where value of $\mathbf{w}^{\top}\mathbf{x} + b$ is strictly positive for both \mathbf{x}_0 and $-\mathbf{x}_0$, possibly with minor issues
 - **1 pt** Minor mistakes in example e.g. value of $\mathbf{w}^{\top}\mathbf{x} + b$ is zero for one/both the cases.
 - + 0 pts Totally wrong or else unanswered

3/3 pts

- → + 1 pt Correct answer is T
- \checkmark + 2 pts Valid example where value of x_0, x_1 is given in terms of a, b and universal constants, possibly with minor issues.
 - **1 pt** Minor issues e.g. examples are not given for general values of a, b, but for specific values of a, b, or if say cases of a > b and b > a are not discussed.
 - + 0 pts Totally wrong or else unanswered

Sliding Parabolas 7 / 7 pts

- + **0 pts** Give marks directly out of 7 using points adjustment. 1 mark per correct answer. No partial marking for incorrect sign etc.
- + 0 pts Completely wrong or else unanswered

Question 3

Vector Line-up 4 / 4 pts

- f + 0 pts Give marks directly out of 4 using points adjustment. 1 mark per correct answer. Deduct 0.5 marks per part for minor mistakes e.g. if answer violates at most one condition e.g. in part a, violating the condition that answer must be a non-zero vector, or if in part b, squared L_2 norm of the vector is an integer but L_2 norm is not an integer, etc. No marks if an answer is outright wrong.
- + 0 pts Completely wrong or else unanswered
- + 4 pts Point adjustment

CS 771A:	Intro to Machine Le	earning,	IIT Kanpur	Quiz I (24 Jan	2024)
Name	LAVESH GUPTA			20 m	arks
Roll No	210562	Dept.	ELECTRICAL ENGIGE.	Page 1	L of 2

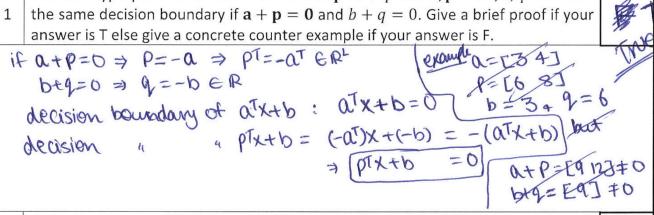
Instructions:

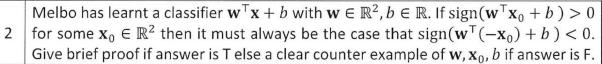
- 1. This question paper contains 1 page (2 sides of paper). Please verify.
- 2. Write your name, roll number, department above in block letters neatly with ink.
- 3. Write your final answers neatly with a blue/black pen. Pencil marks may get smudged.
- 4. Don't overwrite/scratch answers especially in MCQ such cases may get straight 0 marks.
- 5. Do not rush to fill in answers. You have enough time to solve this guiz.

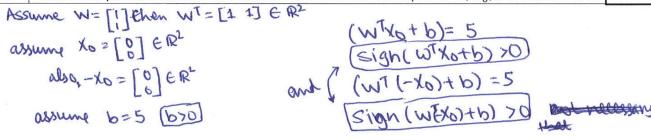


Q1. (True-False) Write T or F for True/False (write only in the box on the right-hand side). You must also give a brief justification for your reply in the space provided below.(3 x (1+2) = 9 marks)

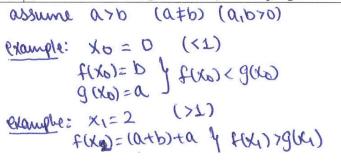
1	The two hyperplane classifiers $\mathbf{a}^{T}\mathbf{x} + b$ and $\mathbf{p}^{T}\mathbf{x} + q$ with $\mathbf{a}, \mathbf{p} \in \mathbb{R}^2, b, q \in \mathbb{R}$ have the same decision boundary if $\mathbf{a} + \mathbf{p} = 0$ and $b + q = 0$. Give a brief proof if your				
	answer is T else give a concrete counter example if your answer is F.				

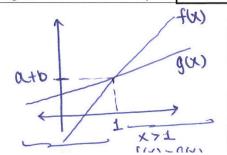






Consider $f, g: \mathbb{R} \to \mathbb{R}$ of the form f(x) = ax + b, g(x) = bx + a with a, b > 0. If $a \neq b$, there must exist $x_0, x_1 \in \mathbb{R}$ such that $f(x_0) < g(x_0)$ and $f(x_1) > g(x_1)$. If your answer is T, give example of x_0 , x_1 in terms of a, b, else give a counter example.





g(x1) = (a+b)+b J

ベくよ

しんしょうかい

f(x)<g(x)
if a 7b

if asb

Q2. (Sliding parabolas) Consider $f(x) = (x - a)^2 + b$, $g(x) = -(x - p)^2 + q$ and $h(x) = x^3/2$.

Find values of $a, b \in \mathbb{R}$ such that f and h share a tangent at $x = 1$.	$a = \frac{1}{4}$	$b = \frac{1}{16}$
Find values of $p, q \in \mathbb{R}$ such that g and h share a tangent at $x = 1$.	$p = \frac{\pi}{4}$	$q = \frac{17}{16}$
Find the value of $f+g$ at $x=1$ i.e., $(f+g)(1)$	(f+g)(1) =	1
Find the first derivative of $f+g$ at $x=1$ i.e., $(f+g)'(1)$	(f+g)'(1) =	3
Find second derivative of $f+g$ at $x=1$ i.e., $(f+g)^{\prime\prime}(1)$	(f+g)''(1) =	0

Write your answers only in the space provided.

(2+2+1+1+1=7 marks)

Q4. (Vector line-up) Give examples of 4D vectors (fill-in the 4 boxes) with the following properties. Any example will get full marks so long as it satisfies all the properties mentioned in the question. Your answers to the parts a, b, c, d, e may be same/different. (4 \times 1 = 4 marks)

- a. A vector $\mathbf{v} \in \mathbb{R}^4$ such that $\mathbf{v} \neq \mathbf{0}$ and \mathbf{v} is perpendicular to both the vectors (1,0,1,1) and (0,1,0,0).
- b. A vector $\mathbf{v} \in \mathbb{R}^4$ with only integer coordinates (at least 2 non-zero coordinates) whose L_2 norm is also an integer.
- c. A vector $\mathbf{v} \in \mathbb{R}^4$ that is perpendicular to its own negative i.e., $\mathbf{v} \perp -\mathbf{v}$.
- d. A point $\mathbf{v} \in \mathbb{R}^4$ with equal L_2 distance from the vectors (1,2,3,4) and (4,3,2,1).

0	0	1	-1
8	6	0	0
0	0	0	0
5/2	5/2	5/2	5/2

Anything written here will not be graded