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1 Data Structure

1.1 Binary Search

```

1 int binary_search(int arr[maxn], int lef, int rig,
2   int target){
3   if(lef > rig) return 0x3f3f3f3f;
4   int mid = (lef + rig) >> 1;
5   if(arr[mid] == target) return mid;
6   else if(arr[mid] > target){
7       return binary_search(arr, lef, mid - 1,
8         target);
9   }
10  else{
11      return binary_search(arr, mid + 1, rig,
12        target);
13  }
14 }
```

1.2 BIT

```

1 #define lowbit(k) (k & -k)
2 void add(vector<int> &tr, int id, int val) {
3     for (; id <= n; id += lowbit(id)) {
4         tr[id] += val;
5     }
6 }
7 int sum(vector<int> &tr, int id) {
8     int ret = 0;
9     for (; id >= 1; id -= lowbit(id)) {
10        ret += tr[id];
11    }
12    return ret;
13 }
```

1.3 Segment tree

```

1 int dfs(int lef, int rig){
2     if(lef + 2 == rig){
3         if(num[lef] > num[rig-1]){
4             return lef;
5         }
6         else{
7             return rig-1;
8         }
9     }
10    int mid = (lef + rig)/2;
11    int p1 = dfs(lef, mid);
12    int p2 = dfs(mid, rig);
13    if(num[p1] > num[p2]){
14        return p1;
15    }
16    else{
17        return p2;
18    }
19 }
```

1.4 Trie

```

1 const int MAXL = ; // 自己填
2 const int MAXC = ;
3 struct Trie {
4     int nex[MAXL][MAXC];
5     int len[MAXL];
6     int sz;
7     void init() {
8         memset(nex, 0, sizeof(nex));
9         memset(len, 0, sizeof(len));
10        sz = 0;
11    }
12    void insert(const string &str) {
13        int p = 0;
14        for (char c : str) {
15            int id = c - 'a';
16            if (!nex[p][id]) {
17                nex[p][id] = ++sz;
18            }
19            p = nex[p][id];
20        }
21        len[p] = str.length();
22    }
23    vector<int> find(const string &str, int i) {
24        int p = 0;
25        vector<int> ans;
26        for (; i < str.length(); i++) {
27            int id = str[i] - 'a';
28            if (!nex[p][id]) {
29                return ans;
30            }
31            p = nex[p][id];
32            if (len[p]) {
33                ans.pb(len[p]);
34            }
35        }
36    }
37 }
```

```

34     }
35 }
36 return ans;
37 }
38 };

```

2 Divide and Conquer

2.1 count inversions

```

1  /*逆序數對*/
2  int arr[maxn], buf[maxn];
3  int count_inversions(int lef, int rig){
4      if(rig - lef <= 1) return 0;
5      int mid = (lef + rig)/2;
6      int ans = count_inversions(lef, mid) +
7                count_inversions(mid, rig);
8      int i = lef, j = mid, k = lef;
9      while(i < mid || j < rig){
10         if(i >= mid) buf[k] = arr[j++];
11         else if(j >= rig) buf[k] = arr[i++];
12         else{
13             if(arr[i] <= arr[j]) buf[k] = arr[i++];
14             else{
15                 buf[k] = arr[j++];
16                 ans += mid - i;
17             }
18         }
19         k++;
20     }
21     for(int k = lef; k < rig; ++k) arr[k] = buf[k];
22     return ans;
23 }

```

3 DP

3.1 Doubling

```

1  /* 倍增 */
2  int LOG = sqrt(N); // 2^LOG >= N
3  vector<int> arr(N);
4  vector<vector<int>> dp(N, vector<int>(LOG));
5  for(int i = 0; i < N; ++i) cin >> arr[i];
6  int L, Q, a, b;
7  cin >> L >> Q;
8  for(int i = 0; i < N; ++i){
9      dp[i][0] = lower_bound(arr.begin(), arr.end(),
10                             arr[i] + L) - arr.begin();
11      if(dp[i][0] == N || arr[i] + L < arr[dp[i][0]])
12          dp[i][0] = -1;
13  }
14  for(int i = 1; i < LOG; ++i)
15      for(int j = 0; j < N; ++j)
16          dp[j][i] = dp[dp[j][i-1]][i-1];
17  for(int i = 0; i < Q; ++i){
18      cin >> a >> b;
19      a--; // 要減減是因為arr的index從0開始但題目從1開始
20      b--;
21      if(a > b) swap(a, b);
22      int ans = 0;
23      for(int i = LOG - 1; i >= 0; --i){ // 從後往回推
24          if(dp[a][i] < b){
25              ans += (1 << i);
26              a = dp[a][i];
27          }
28      }
29      cout << ans + 1 << endl;
30  }

```

3.2 Josephus

```

1  int josephus (int n, int k) {
2      // 有 n 個人圍成一圈，每 k 個一次
3      return n > 1 ? (josephus(n-1, k) + k) % n : 0;
4  }
5  // 回傳最後一人的編號，0 index

```

3.3 LCS

```

1  int LCS(string s1, string s2) {
2      int n1 = s1.size(), n2 = s2.size();
3      int dp[n1+1][n2+1] = {0};
4      // dp[i][j] = s1的前i個字元和s2的前j個字元
5      for (int i = 1; i <= n1; i++) {
6          for (int j = 1; j <= n2; j++) {
7              if (s1[i-1] == s2[j-1]) {
8                  dp[i][j] = dp[i-1][j-1] + 1;
9              } else {
10                 dp[i][j] = max(dp[i-1][j], dp[i][j-1]);
11             }
12         }
13     }
14     return dp[n1][n2];
15 }

```

3.4 LIS

```

1  int LIS(vector<int> &a) { // Longest Increasing
2      Subsequence
3      vector<int> s;
4      for (int i = 0; i < a.size(); i++) {
5          if (s.empty() || s.back() < a[i]) {
6              s.push_back(a[i]);
7          } else {
8              *lower_bound(s.begin(), s.end(), a[i],
9                           [](int x, int y) {return x < y;}) = a[i];
10         }
11     }
12     return s.size();
13 }

```

4 Enumerate

4.1 Halfcut Enumerate

```

1  /* 折半枚舉 */
2  void dfs(set<long long int> &s, int depth, int T,
3          long long int sum){
4      if(depth >= T){
5          s.insert(sum);
6          return;
7      }
8      dfs(s, depth + 1, T, sum); // 取或不取的概念
9      dfs(s, depth + 1, T, sum + A[depth]);
10 }
11 int main(){
12     int N, T;
13     set<long long int> s1, s2;
14     cin >> N >> T;
15     for(int i = 0; i < N; ++i) cin >> A[i];
16     dfs(s1, 0, N/2, 0); // 折半枚舉
17     dfs(s2, N/2, N, 0);
18     long long int ans = 0;
19     // 題目:枚舉集合 Sx 的數字 Sxi, 找出 Sy
20     // 集合內小於等於 T-Sxi 中最大的數 Syj
21     for(auto &x : s1){
22         auto it = s2.upper_bound(T - x);
23         long long int y = *(--it);
24     }

```

```

22     if(x + y <= T) ans = max(ans, x + y);
23 }
24 cout << ans << endl;
25 }

```

5 Graph

5.1 SPFA

```

1 bool SPFA(int s){
2     // 記得初始化這些陣列
3     int cnt[1000+5], dis[1000+5];
4     bool inqueue[1000+5];
5     queue<int> q;
6
7     q.push(s);
8     dis[s] = 0;
9     inqueue[s] = true;
10    cnt[s] = 1;
11    while(!q.empty()){
12        int now = q.front();
13        q.pop();
14        inqueue[now] = false;
15
16        for(auto &e : G[now]){
17            if(dis[e.t] > dis[now] + e.w){
18                dis[e.t] = dis[now] + e.w;
19                if(!inqueue[e.t]){
20                    cnt[e.t]++;
21                    if(cnt[e.t] > m){
22                        return false;
23                    }
24                    inqueue[e.t] = true;
25                    q.push(e.t);
26                }
27            }
28        }
29    }
30    return true;
31 }

```

5.2 Dijkstra

```

1 struct Item{
2     int u, dis;
3     // 取路徑最短
4     bool operator < (const Item &other) const{
5         return dis > other.dis;
6     }
7 };
8 int dis[maxn];
9 vector<Edge> G[maxn];
10 void dijkstra(int s){
11     for(int i = 0; i <= n; i++){
12         dis[i] = inf;
13     }
14     dis[s] = 0;
15     priority_queue<Item> pq;
16     pq.push({s, 0});
17     while(!pq.empty()){
18         // 取路徑最短的點
19         Item now = pq.top();
20         pq.pop();
21         if(now.dis > dis[now.u]){
22             continue;
23         }
24         // 鬆弛更新，把與 now.u 相連的點都跑一遍
25         for(Edge e : G[now.u]){
26             if(dis[e.v] > now.dis + e.w){
27                 dis[e.v] = now.dis + e.w;
28                 pq.push({e.v, dis[e.v]});
29             }
30         }
31     }
32 }

```

```

30     }
31 }
32 }

```

5.3 Floyd Warshall

```

1 void floyd_warshall(){
2     for(int i = 0; i < n; i++){
3         for(int j = 0; j < n; j++){
4             G[i][j] = INF;
5         }
6         G[i][i] = 0;
7     }
8     for (int k = 0; k < n; k++){ // 嘗試每一個中繼點
9         for (int i = 0; i < n; i++){ // 計算每一個i點與每一個j點
10            for (int j = 0; j < n; j++){
11                G[i][j] = min(G[i][j], G[i][k] + G[k][j]);
12            }
13        }
14    }
15 }

```

5.4 Disjoint set Kruskal

```

1 struct Edge{
2     int u, v, w;
3     // 用權重排序 由大到小
4     bool operator < (const Edge &other) const{
5         return w > other.w;
6     }
7 }edge[maxn];
8 // disjoint set
9 int find(int x){
10    if(parent[x] < 0){
11        return x;
12    }
13    else{
14        return parent[x] = find(parent[x]);
15    }
16 }
17 void unite(int a, int b){
18     a = find(a);
19     b = find(b);
20
21     if(a != b){
22         if(parent[a] < parent[b]){
23             parent[a] += parent[b];
24             parent[b] = a;
25         }
26         else{
27             parent[b] += parent[a];
28             parent[a] = b;
29         }
30     }
31 }
32 void kruskal(){
33     memset(parent, -1, sizeof(parent));
34     sort(edge, edge + m);
35     int i, j;
36     for(i = 0, j = 0; i < n - 1 && j < m; i++){
37         // 如果 u 和 v 的祖先相同，則 j++
38         // (祖先相同代表會產生環 所以不要)
39         while(find(edge[j].u) == find(edge[j].v)) j++;
40         // 若部會產生環 則讓兩點之間產生橋
41         // (連接兩顆子生成樹)
42         unite(edge[j].u, edge[j].v);
43         j++;
44     }
45 }

```

5.5 KM

```

1 const int X = 50; // x的點數，等於y的點數
2 const int Y = 50; // y的點數
3 int adj[X][Y]; // 精簡過的adjacency matrix
4 int lx[X], ly[Y]; // vertex labeling
5 int mx[X], my[Y]; //
    x各點的配對對象、y各點的配對對象
6 int q[X], *qf, *qb; // BFS queue
7 int p[X]; // BFS
    parent，交錯樹之偶點，指向上一個偶點
8 bool vx[X], vy[Y]; // 記錄是否在交錯樹上
9 int dy[Y], pdy[Y]; // 表格
10
11 void relax(int x){ // relaxation
12     for (int y=0; y<Y; ++y)
13         if (adj[x][y] != 1e9)
14             if (lx[x] + ly[y] - adj[x][y] < dy[y]){
15                 dy[y] = lx[x] + ly[y] - adj[x][y];
16                 pdy[y] = x; //
                    記錄好是從哪個樹葉連出去的
17             }
18 }
19 void reweight(){ // 調整權重、調整表格
20     int d = 1e9;
21     for (int y=0; y<Y; ++y) if (!vy[y]) d = min(d,
        dy[y]);
22     for (int x=0; x<X; ++x) if ( vx[x]) lx[x] -= d;
23     for (int y=0; y<Y; ++y) if ( vy[y]) ly[y] += d;
24     for (int y=0; y<Y; ++y) if (!vy[y]) dy[y] -= d;
25 }
26 void augment(int x, int y){ // 擴充路徑
27     for (int ty; x != -1; x = p[x], y = ty){
28         ty = mx[x]; my[y] = x; mx[x] = y;
29     }
30 }
31 bool branch1(){ // 延展交錯樹：使用既有的等邊
32     while (qf < qb)
33         for (int x=*qf++, y=0; y<Y; ++y)
34             if (!vy[y] && lx[x] + ly[y] == adj[x][y]){
35                 vy[y] = true;
36                 if (my[y] == -1){
37                     augment(x, y);
38                     return true;
39                 }
40                 int z = my[y];
41                 *qb++ = z; p[z] = x; vx[z] = true;
42                 relax(z);
43             }
44     return false;
45 }
46 bool branch2(){ // 延展交錯樹：使用新添的等邊
47     for (int y=0; y<Y; ++y){
48         if (!vy[y] && dy[y] == 0){
49             vy[y] = true;
50             if (my[y] == -1){
51                 augment(pdy[y], y);
52                 return true;
53             }
54             int z = my[y];
55             *qb++ = z; p[z] = pdy[y]; vx[z] = true;
56             relax(z);
57         }
58     }
59     return false;
60 }
61 int Hungarian(){
62     // 初始化vertex labeling
63     // memset(lx, 0, sizeof(lx)); // 任意值皆可
64     memset(ly, 0, sizeof(ly));
65     for (int x=0; x<X; ++x)
66         for (int y=0; y<Y; ++y)
67             lx[x] = max(lx[x], adj[x][y]);
68     // x側每一個點，分別建立等邊交錯樹。

```

```

68     memset(mx, -1, sizeof(mx));
69     memset(my, -1, sizeof(my));
70     for (int x=0; x<X; ++x){
71         memset(vx, false, sizeof(vx));
72         memset(vy, false, sizeof(vy));
73         memset(dy, 0x7f, sizeof(dy));
74         qf = qb = q;
75         *qb++ = x; p[x] = -1; vx[x] = true; relax(x);
76         while (true){
77             if (branch1()) break;
78             reweight();
79             if (branch2()) break;
80         }
81     }
82     // 計算最大權完美匹配的權重
83     int weight = 0;
84     for (int x=0; x<X; ++x)
85         weight += adj[x][mx[x]];
86     return weight;
87 }

```

5.6 Dinic

```

1 // Maximum Flow
2 const int V = 100, E = 1000;
3 int adj[V]; // adjacency lists，初始化為-1。
4 struct Element {int b, r, next;} e[E*2];
5 int en = 0;
6 void addedge(int a, int b, int c){
7     e[en] = (Element){b, c, adj[a]}; adj[a] = en++;
8     e[en] = (Element){a, 0, adj[b]}; adj[b] = en++;
9 }
10 int d[V]; // 最短距離
11 bool visit[V]; // BFS/DFS visit record
12 int q[V]; // queue
13 int BFS(int s, int t){ // 計算最短路徑，求出容許圖
14     memset(d, 0x7f, sizeof(d));
15     memset(visit, false, sizeof(visit));
16     int qn = 0;
17     d[s] = 0;
18     visit[s] = true;
19     q[qn++] = s;
20
21     for (int qf=0; qf<qn; ++qf){
22         int a = q[qf];
23         for (int i = adj[a]; i != -1; i = e[i].next){
24             int b = e[i].b;
25             if (e[i].r > 0 && !visit[b]){
26                 d[b] = d[a] + 1;
27                 visit[b] = true;
28                 q[qn++] = b;
29                 if (b == t) return d[t];
30             }
31         }
32     }
33     return V;
34 }
35 int DFS(int a, int df, int s, int t){ //
    求出一條最短擴充路徑，並擴充流量
36     if (a == t) return df;
37     if (visit[a]) return 0;
38     visit[a] = true;
39     for (int i = adj[a]; i != -1; i = e[i].next){
40         int b = e[i].b;
41         if (e[i].r > 0 && d[a] + 1 == d[b]){
42             int f = DFS(b, min(df, e[i].r), s, t);
43             if (f){
44                 e[i].r -= f;
45                 e[i^1].r += f;
46                 return f;
47             }
48         }
49     }
50     return 0;
51 }

```

```

52 int dinitz(int s, int t){
53     int flow = 0;
54     while (BFS(s, t) < V)
55         while (true){
56             memset(visit, false, sizeof(visit));
57             int f = DFS(s, 1e9, s, t);
58             if (!f) break;
59             flow += f;
60         }
61     return flow;
62 }

```

5.7 Bipatirate

```

1  const int maxn = 300 + 5;
2  int n, color[maxn];
3  vector<vector<int>> v(maxn);
4  bool dfs(int s){
5      for(auto it : v[s]){
6          if(color[it] == -1){
7              color[it] = 3 - color[s];
8              if(!dfs(it)){
9                  return false;
10             }
11         }
12         if(color[s] == color[it]){
13             return false;
14         }
15     }
16     return true;
17 }
18 void isBipatirate(){
19     bool flag = true;
20     for(int i = 1; i <= n; ++i){
21         if(color[i] == -1){
22             color[i] = 1;
23             flag &= dfs(i);
24         }
25     }
26     if(flag){
27         cout << "YES" << endl;
28     }
29     else{
30         cout << "NO" << endl;
31     }
32 }
33 int main(){
34     while(cin >> n && n){
35         for(int i = 1; i <= n; ++i) v[i].clear();
36         memset(color, -1, sizeof(color));
37         int a, b;
38         while(cin >> a >> b && (a || b)){
39             v[a].emplace_back(b);
40             v[b].emplace_back(a);
41         }
42         isBipatirate();
43     }
44 }

```

5.8 Hungarian algorithm

```

1  const int maxn = 500+5;
2  int t, N, bn, gn, match[maxn];
3  bool visited[maxn];
4  vector<vector<int>> G(maxn);
5  struct People{
6      int h;
7      string music, sport;
8      People(){
9          People(int h, string music, string sport){
10             this->h = h;
11             this->music = music;
12             this->sport = sport;

```

```

13     }
14 }lef[maxn], rig[maxn];
15 bool check(People boy, People girl){
16     if(abs(boy.h - girl.h) <= 40 && boy.music ==
17         girl.music && boy.sport != girl.sport) return
18         true;
19     return false;
20 }
21 bool dfs(int s){
22     for(int i = 0; i < G[s].size(); ++i){
23         int v = G[s][i];
24         if(visited[v]) continue;
25         visited[v] = true;
26         if(match[v] == -1 || dfs(match[v])){
27             match[v] = s;
28             return true;
29         }
30     }
31     return false;
32 }
33 int Hungarian(){
34     int cnt = 0;
35     memset(match, -1, sizeof(match));
36     for(int i = 0; i < bn; ++i){
37         memset(visited, false, sizeof(visited));
38         if(dfs(i)) cnt++;
39     }
40     return cnt;
41 }
42 int main(){
43     cin >> t;
44     while(t--){
45         cin >> N;
46         bn = 0, gn = 0;
47         for(int i = 0; i <= N; ++i) G[i].clear();
48         int h;
49         string sex, music, sport;
50         for(int i = 0; i < N; ++i){
51             cin >> h >> sex >> music >> sport;
52             if(sex == "M") lef[bn++] = People(h, music, sport);
53             else rig[gn++] = People(h, music, sport);
54         }
55         for(int i = 0; i < bn; ++i){
56             for(int j = 0; j < gn; ++j)
57                 if(check(lef[i], rig[j]))
58                     G[i].emplace_back(j);
59         }
60         cout << N - Hungarian() << endl;
61     }
62 }

```

5.9 LCA

```

1  /*最低共同祖先*/
2  // 此 node 下有幾顆 node
3  int dfs(int node, int dep){
4      depth[node] = dep + 1;
5      if(G[node].empty()){
6          siz[node] = 1;
7          return 1;
8      }
9      int total = 1;
10     for(auto i : G[node])
11         total += dfs(i.v, dep + 1);
12     siz[node] = total;
13     return siz[node];
14 }
15 // 找出每個節點的 2^i 倍祖先
16 // 2^20 = 1e6 > 200000
17 void find_parent(){
18     for(int i = 1; i < 20; i++){
19         for(int j = 0; j < N; j++){
20             parent[j][i] =
                parent[parent[j][i-1]][i-1];

```

```

21 }
22 // 求兩點的LCA (利用倍增法)
23 int LCA(int a, int b){
24     if (depth[b] < depth[a]) swap(a, b);
25     if (depth[a] != depth[b]){
26         int dif = depth[b] - depth[a];
27         for (int i = 0; i < 20; i++){
28             if (dif & 1) b = parent[b][i];
29             dif >>= 1;
30         }
31     }
32     if (a == b) return a;
33     for (int i = 19; i >= 0; i--){
34         if (parent[a][i] != parent[b][i]){
35             a = parent[a][i];
36             b = parent[b][i];
37         }
38     }
39     return parent[a][0];
40 }

```

```

21 memset(num, 0, sizeof(num));
22 cin >> n;
23 for(int i = 1; i <= n; i++){
24     cin >> num[i];
25 }
26 int mini = 2147483647; // 不知道為甚麼只有 2147483647
    給過
27 // 1 << n = n * 2
28 for(int i = 0; i < (1 << n); i++){
29     int XOR = 0, OR = 0;
30     for(int j = 1; j <= n; j++){
31         OR |= num[j];
32         if((i & (1 << j))){
33             XOR ^= OR;
34             OR = 0;
35         }
36     }
37     XOR ^= OR;
38     mini = min(mini, XOR);
39 }
40 cout << mini << endl;

```

6 Other

6.1 Bubble Sort Expect Value

```

1 /* 期望值算法:
2 擲一枚公平的六面骰子, 其每次「點數」的期望值是 3.5
3  $E(x) = 1 * 1/6 + 2 * 1/6 + 3 * 1/6 + 4 * 1/6 + 5 * 1/6 + 6 * 1/6$ 
4  $= (1 + 2 + 3 + 4 + 5 + 6)/6 = 3.5$ 
5 bubble sort 每兩兩之間交換機率是 1/2
6 總共會做  $C(n, 2)$  次
7  $E(x) = C(n, 2) * 1/2 = (n * (n - 1))/2 * 1/2$  */
8 int t, ca = 1;
9 cin >> t;
10 while(t--){
11     long long int n;
12     cin >> n;
13     cout << "Case " << ca++ << ": ";
14     // 如果  $(n * (n - 1))$  可以被 4 整除
        代表最後答案會是整數, 否則會是分數
15     if((n * (n - 1)) % 4){
16         cout << ( (n * (n - 1)) / 2 ) << "/2" << endl;
17     }
18     else{
19         cout << ( (n * (n - 1)) / 2 ) / 2 << endl;
20     }
21 }

```

6.2 ORXOR

```

1 /* 如何切區段, 之所以要  $1 << n$  是為了可以跑 000~111
2  $i = 0$ , binary  $i = 000$ 
3  $0 : 1 \ 5 \ 7$ 
4  $i = 1$ , binary  $i = 001$ 
5  $1 : 1 \ 5 \ 7$ 
6  $i = 2$ , binary  $i = 010$ , 看得出來切了一刀
7  $2 : 1 \ | \ 5 \ 7$ 
8  $i = 3$ , binary  $i = 011$ 
9  $3 : 1 \ | \ 5 \ 7$ 
10  $i = 4$ , binary  $i = 100$ , 為了要切在 index=2, 所以才要  $1 << j$ 
11  $4 : 1 \ 5 \ | \ 7$ 
12  $i = 5$ , binary  $i = 101$ 
13  $5 : 1 \ 5 \ | \ 7$ 
14  $i = 6$ , binary  $i = 110$ 
15  $6 : 1 \ | \ 5 \ | \ 7$ 
16  $i = 7$ , binary  $i = 111$ 
17  $7 : 1 \ | \ 5 \ | \ 7$ 
18 可以觀察出來, 前兩位 bit 是 1 時代表的意義是切在哪裡*/
19 int n;
20 int num[20+7];

```

6.3 Race to 1

```

1 const int N = 1000000;
2 bool sieve[N+5];
3 vector<int> pri;
4 double dp[N+5];
5 void Linear_Sieve(){ // 線性篩
6     for (int i = 2; i < N; i++){
7         if (!sieve[i])
8             pri.push_back(i);
9         for (int p: pri){
10             if (i * p >= N){
11                 break;
12             }
13             sieve[i * p] = true;
14             if (i % p == 0){
15                 break;
16             }
17         }
18     }
19 }
20 double dfs(int n){
21     if(dp[n] != -1) return dp[n];
22     dp[n] = 0;
23     if(n == 1) return dp[n];
24     int total = 0, prime = 0;
25     for(int i = 0; i < pri.size() && pri[i] <= n; i++){
26         total++;
27         if(n % pri[i]) continue;
28         prime++;
29         dp[n] += dfs(n/pri[i]);
30     }
31     dp[n] = (dp[n] + total)/prime; // 算期望值
32     return dp[n];
33 }
34 int main(){
35     int t;
36     int num;
37     int ca = 1;
38     for(int i = 0; i <= N; i++){
39         dp[i] = -1;
40     }
41     Linear_Sieve();
42     cin >> t;
43     while(t--){
44         cin >> num;
45
46         cout << "Case " << ca++ << ": " << fixed <<
            setprecision(10) << dfs(num) << endl;
47     }
48 }

```

6.4 X drawing

```

1 long long int n, a, b, p, q, r, s;
2 cin >> n >> a >> b;
3 cin >> p >> q >> r >> s;
4 for(long long int i = p; i <= q; i++){
5     for(long long int j = r; j <= s; j++){
6         if(abs(i - a) == abs(j - b)){
7             cout << '#';
8         }
9         else{
10            cout << '.';
11        }
12    }
13    cout << endl;
14 }

```

6.5 Big Mod

```

1 '''
2 Mod
3 pow(x, y, z) = x^y % z
4 '''
5 # python 如何讀取直到 EOF 用 try except
6 try:
7     while True:
8         # input().split() 用空格切開讀取一整行
9         # map (型態, input().split()) 才能把值全讀成
10            int
11            B, P, M = map(int, input().split())
12            print(pow(B, P, M))
13 except EOFError:
14     exit

```

6.6 Crested Ibis vs Monster

```

1 /* dp 背包 - 重量/價值/可重複使用
2 因為這題可以重複使用同一條魔法
3 所以可以這樣dp*/
4 int h, n;
5 cin >> h >> n;
6 for(int i = 1; i <= n; i++){
7     cin >> a[i] >> b[i];
8 }
9 memset(dp, 0x3f3f3f3f, sizeof(dp));
10 dp[0][0] = 0;
11 for(int i = 1; i <= n; i++){
12     for(int j = 0; j <= h; j++){
13         dp[i][j] = min(dp[i-1][j], dp[i][max(0, j -
14             a[i])] + b[i]);
15     }
16 }
17 cout << dp[n][h] << endl;

```

6.7 dpd Knapsack 1

```

1 // dp 背包 - 時間/數量/價值 - 第幾分鐘符合
2 int N, W;
3 cin >> N >> W;
4 int w[100000+5];
5 int v[100000+5];
6 for(int i = 0; i < N; i++){
7     cin >> w[i] >> v[i];
8 }
9 long long int dp[100000+5];
10 memset(dp, 0, sizeof(dp));
11 for(int i = 0; i < N; i++){
12     for(int j = W; j >= w[i]; j--){
13         dp[j] = max(dp[j], dp[j - w[i]] + v[i]);
14     }

```

```

15 }
16 cout << dp[W] << endl;

```

6.8 Fraction Floor Sum

```

1 /* [N/i] == M
2 -> M <= N/i < M + 1
3 -> N/(M+1) < i <= N/M */
4 long long int N;
5 cin >> N;
6 long long int ans = 0;
7 for(long long int i = 1; i <= N; i++){
8     long long int M = N / i;
9     long long int n = N / M;
10    // 總共會有 n - i 個的 [N/i] 值都是 M
11    ans += (n - i + 1) * M;
12    // 更新跳過 以免重複計算
13    i = n;
14 }
15 cout << ans << endl;

```

6.9 Homer Simpson

```

1 // dp 背包 - 時間/數量 - 漢堡
2 int m, n, t;
3 while(cin >> m >> n >> t){
4     int dp[10000+5];
5     memset(dp, -1, sizeof(dp));
6     dp[0] = 0;
7     for(int i = m; i <= t; i++){
8         if(dp[i - m] != -1){
9             dp[i] = max(dp[i], dp[i - m] + 1);
10        }
11    }
12    for(int i = n; i <= t; i++){
13        if(dp[i - n] != -1){
14            dp[i] = max(dp[i], dp[i - n] + 1);
15        }
16    }
17    if(dp[t] == -1){ // 時間無法剛好吃滿的時候
18        for(int i = t; i >= 0; i--){
19            if(dp[i] != -1){
20                cout << dp[i] << " " << t - i << endl;
21                break;
22            }
23        }
24    }
25    else{
26        cout << dp[t] << endl;
27    }
28 }

```

6.10 Let Me Count The Ways

```

1 // dp - 時間/數量 - 硬幣排序
2 long long int n, dp[30000+5];
3 int coin[] = {1, 5, 10, 25, 50};
4 memset(dp, 0, sizeof(dp));
5 dp[0] = 1;
6 for(int i = 0; i < 5; i++){
7     for(int j = coin[i]; j < 30000+5; j++){
8         if(dp[j - coin[i]] != -1){
9             dp[j] += dp[j - coin[i]];
10        }
11    }
12 }
13 while(cin >> n){
14     if(dp[n] == 1){
15         cout << "There is only " << dp[n] << " way to
16             produce " << n << " cents change." <<
17             endl;

```

```

16     }
17     else{
18         cout << "There are " << dp[n] << " ways to
           produce " << n << " cents change." <<
           endl;
19     }
20 }

```

6.11 Luggage

```

1 // dp 背包 - 重量/是否成立
2 int t;
3 cin >> t;
4 cin.ignore();
5 while(t--){
6     string str;
7     getline(cin, str);
8     vector<int> v;
9     stringstream ss;
10    int num, cnt = 0, sum = 0;;
11    bool dp[4000+5];
12    memset(dp, false, sizeof(dp));
13    ss << str;
14    while(ss >> num){
15        cnt++;
16        sum += num;
17        v.emplace_back(num);
18    }
19    if(sum & 1){
20        cout << "NO" << endl;
21        continue;
22    }
23    dp[0] = true;
24    for(int i = 0; i < v.size(); i++){
25        for(int j = sum; j >= v[i]; j--){
26            if(dp[j - v[i]]){
27                dp[j] = true;
28            }
29        }
30    }
31    cout << (dp[sum/2] ? "YES" : "NO") << endl;
32 }

```

6.12 Number of Pairs

```

1 /* upper_bound ex:
2 10 20 30 30 40 50
3 upper_bound for element 30 is at index 4
4 lower_bound ex:
5 10 20 30 40 50
6 lower_bound for element 30 at index 2 */
7 int t;
8 cin >> t;
9 while(t--){
10     int n, l, r;
11     vector<int> v;
12     cin >> n >> l >> r;
13     int num;
14     for(int i = 0; i < n; i++){
15         cin >> num;
16         v.emplace_back(num);
17     }
18     sort(v.begin(), v.end());
19     long long int ans = 0;
20     for(int i = 0; i < n; i++){
21         ans += (upper_bound(v.begin() + i + 1,
           v.end(), r - v[i]) -
           lower_bound(v.begin() + i + 1, v.end(), l
           - v[i]));
22     }
23     cout << ans << endl;
24 }

```

6.13 SuperSale

```

1 // dp 背包 - 重量/價值/不可重複使用 - 舉重
2 int t;
3 cin >> t;
4 while(t--){
5     int n;
6     cin >> n;
7     for(int i = 0; i < n; i++){
8         cin >> edge[i].p >> edge[i].w;
9     }
10    int g, total = 0;
11    cin >> g;
12    for(int i = 0; i < g; i++){
13        int pw, dp[30+5];
14        cin >> pw;
15        memset(dp, 0, sizeof(dp));
16        for(int j = 0; j < n; j++){
17            for(int k = pw; k >= edge[j].w; k--){
18                dp[k] = max(dp[k], dp[k - edge[j].w]
               + edge[j].p);
19            }
20        }
21        total += dp[pw];
22    }
23    cout << total << endl;
24 }

```

6.14 Walking on the Safe Side

```

1 // dp - 地圖更新
2 int t;
3 bool space = false;
4 cin >> t;
5 while(t--){
6     if(space){
7         cout << endl;
8     }
9     else{
10        space = true;
11    }
12    int r, c;
13    cin >> r >> c;
14    cin.ignore();
15    memset(mp, false, sizeof(mp));
16    memset(dp, 0, sizeof(dp));
17    string str;
18    for(int i = 0; i < r; i++){
19        getline(cin, str);
20        int n, num;
21        stringstream ss(str);
22        ss >> n;
23        while(ss >> num){
24            mp[n][num] = true;
25        }
26    }
27    dp[1][1] = 1;
28    for(int i = 1; i <= r; i++){
29        for(int j = 1; j <= c; j++){
30            if(mp[i][j]){
31                continue;
32            }
33            if(i > 1){
34                dp[i][j] += dp[i-1][j];
35            }
36            if(j > 1){
37                dp[i][j] += dp[i][j-1];
38            }
39        }
40    }
41    cout << dp[r][c] << endl;
42 }

```


6.15 Cutting Sticks

```

1 while(cin >> l && l){
2     cin >> n;
3     vector<int> s(n+2);
4     s[0] = 0;
5     for(int i = 1; i <= n; ++i) cin >> s[i];
6     s[++n] = 1; // 從現在開始 n 的數量變為 n + 1
7     int dp[n+5][n+5];
8     memset(dp, 0, sizeof(dp));
9     for(int r = 2; r <= n; ++r){ // r: 切幾段 b: 起點
10         c: 中間點 e: 終點
11         for(int b = 0; b < n; ++b){
12             if(b + r > n) break;
13             int e = b + r;
14             dp[b][e] = 0x3f3f3f3f;
15             for(int c = b + 1; c < e; ++c){
16                 dp[b][e] = min(dp[b][e], dp[b][c] +
17                                 dp[c][e] + s[e] - s[b]);
18             }
19         }
20     }
21     cout << "The minimum cutting is " << dp[0][n] <<
22     "." << endl;
23 }

```

6.16 Partitioning by Palindromes

```

1 /*string & dp - 字串長度判斷迴文*/
2 bool check_palindromes(int lef, int rig){
3     // 比較字串兩端都是迴文
4     while(lef < rig){
5         if(str[lef] != str[rig]) return 0;
6         lef++;
7         rig--;
8     }
9     return 1;
10 }
11 int main(){
12     int t;
13     cin >> t;
14     while(t--){
15         cin >> str;
16         memset(dp, 0x3f3f3f3f, sizeof(dp));
17         dp[0] = 0;
18         for(int i = 0; i < str.size(); ++i)
19             for(int j = 0; j <= i; ++j)
20                 if(str[i] == str[j])
21                     if(check_palindromes(j, i))
22                         if(dp[i+1] > dp[j] + 1)
23                             dp[i+1] = dp[j] + 1;
24         cout << dp[str.size()] << endl;
25     }
26 }

```

6.17 Ants Colony

```

1 /*LCA 最低共同祖先*/
2 const int maxn = 1e5 + 5;
3 struct Edge{
4     int v;
5     int w;
6 };
7 int N;
8 vector<Edge> G[maxn];
9 int parent[maxn][20+5];
10 int depth[maxn], siz[maxn];
11 // 此 node 下有幾顆 node
12 int dfs(int node, int dep){
13     depth[node] = dep + 1;
14     if(G[node].empty()){
15         siz[node] = 1;

```

```

16         return 1;
17     }
18     int total = 1;
19     for(auto i : G[node])
20         total += dfs(i.v, dep + 1);
21     siz[node] = total;
22     return siz[node];
23 }
24 // 找出每個節點的 2^i 倍祖先
25 // 2^20 = 1e6 > 200000
26 void find_parent(){
27     for(int i = 1; i < 20; i++){
28         for(int j = 0; j < N; j++){
29             parent[j][i] =
30                 parent[parent[j][i-1]][i-1];
31         }
32     }
33     // 求兩點的LCA (利用倍增法)
34     int LCA(int a, int b){
35         if(depth[b] < depth[a]) swap(a, b);
36         if(depth[a] != depth[b]){
37             int dif = depth[b] - depth[a];
38             for(int i = 0; i < 20; i++){
39                 if(dif & 1) b = parent[b][i];
40                 dif >>= 1;
41             }
42             if(a == b) return a;
43             for(int i = 19; i >= 0; i--){
44                 if(parent[a][i] != parent[b][i]){
45                     a = parent[a][i];
46                     b = parent[b][i];
47                 }
48             }
49             return parent[a][0];
50         }
51         long long int dist[maxn];
52         // 從 0 開始到每個點的距離
53         void distance(){
54             for(int u = 0; u < N; ++u){
55                 for(int i = 0; i < G[u].size(); ++i){
56                     dist[G[u][i].v] = dist[u] + G[u][i].w;
57                 }
58             }
59         }
60         int main(){
61             while(cin >> N && N){
62                 memset(dist, 0, sizeof(dist));
63                 memset(parent, 0, sizeof(parent));
64                 memset(depth, 0, sizeof(depth));
65                 memset(siz, 0, sizeof(siz));
66                 for(int i = 0; i <= N; ++i){
67                     G[i].clear();
68                 }
69                 for(int i = 1; i < N; ++i){
70                     int u, w;
71                     cin >> u >> w;
72                     G[u].push_back({i, w});
73                     parent[i][0] = u;
74                 }
75                 find_parent();
76                 dfs(0, 0);
77                 distance();
78                 int s; cin >> s;
79                 bool space = false;
80                 for(int i = 0; i < s; ++i){
81                     int a, b;
82                     cin >> a >> b;
83                     int lca = LCA(a, b);
84                     if(space) cout << " ";
85                     space = true;
86                     cout << (dist[a] + dist[b]) - (dist[lca]
87                         * 2);
88                 }
89                 cout << endl;
90             }
91         }
92     }

```

6.18 Fill the Containers

```

1  /*binary search 變形*/
2  int binary_search(int arr[maxn], int lef, int rig,
3      int mini){
4      if(lef > rig) return mini;
5      int amount = 1, fill = 0;
6      int mid = (lef + rig) >> 1;
7      for(int i = 0; i < n; ++i){
8          if(amount > m) break;
9          fill += arr[i];
10         if(fill > mid){
11             fill = arr[i];
12             amount++;
13         }
14     }
15     if(!flag && amount <= m) mini = mid;
16     if(flag && amount == m) mini = mid;
17     if(amount == m){
18         flag = true;
19         return binary_search(arr, lef, mid - 1, mid);
20     }
21     else if(amount < m){
22         return binary_search(arr, lef, mid - 1, mini);
23     }
24     else{
25         return binary_search(arr, mid + 1, rig, mini);
26     }
27 }
28 int main(){
29     int ca = 1;
30     while(cin >> n >> m){
31         flag = false;
32         int arr[maxn];
33         int maxi = 0, sum = 0;
34         for(int i = 0; i < n; ++i){
35             cin >> arr[i];
36             sum += arr[i];
37             maxi = max(maxi, arr[i]);
38         }
39         cout << binary_search(arr, maxi, sum, maxi)
40             << endl;
41     }
42 }

```

7 Function

7.1 strstr

```

1  #include <stdio.h>
2  #include <string.h>
3
4  int main(){
5      char * c;
6      char str1[1005], str2[1005];
7      scanf("%s %s", str1, str2);
8      c = strstr(str1, str2);
9      if (c != NULL){
10         printf("Yes\n");
11     }
12     else printf("No\n");
13 }
14 // Input : Hello eLl
15 // Output : No

```

7.2 substr

```

1  int main(){
2      string str; //abcdef
3      cin >> str;
4      string tmp;
5      tmp = str.substr(0, 2); //ab

```

```

6      str = str.substr(2); //cdef
7      cout << tmp << " " << str;
8      return 0;
9  }

```

7.3 map set

```

1  .begin( ) // Return iterator to beginning
2  .end( ) // Return iterator to end
3  .empty( ) // 檢查是否為空
4  .size( ) // 回傳大小
5  mp.insert(pair<char, int>('a', 100))
6  st.insert(100) // 插入key、value
7  .erase( ) // 刪掉指定key和他的value
8  .clear( ) // 清空整個 map
9  m.find( )
10 cout << "a => " << mymap.find('a')->second << endl;
11 // 找出 map 裡 key
12 // 有沒有在裡面，如果有的話會回傳元素所在的iterator，否則傳
13 // 沒有
14 s.count() // 返回某個值元素在set的個數
15 while( !mymap.empty()){
16     cout << mymap.begin()->first << " => " <<
17         mymap.begin()->second << endl;
18     mymap.erase(mymap.begin());
19 }
20 for (auto it = mymap.begin(); it != mymap.end(); ++it)
21     cout << it->first << " => " << it->second << endl;

```

7.4 vector

```

1  v.erase(v.begin() + 5) //拿掉第六個數
2  v.erase(v.begin(), v.begin() + 3); //拿掉前三個數

```

7.5 setprecision

```

1  // 將數字的小數部分設定為固定長度
2  cnt = 3.5555;
3  cout << fixed << setprecision(3) << cnt ;
4  // output : 3.555

```

7.6 GCD LCM

```

1  int gcd(int a, int b){
2      return (b == 0 ? a : gcd(b, a % b));
3  }
4  int lcm(int a, int b){
5      return a * b / gcd(a, b);
6  }
7
8  /* 輾轉相除法 - 求兩數是否互質
9  如果兩數互質 最終結果其中一方為0時 另一方必為1
10 若兩數有公因數 最終結果其中一方為0時 另一方必不為1 */
11 while ( ( num1 % num2 ) != 0 && ( num2 % num1 ) != 0 );

```

7.7 reverse

```

1  int a[10] = {0, 1, 2, 3, 4, 5, 6, 7, 8, 9};
2  reverse(a, a+5) // 轉換0~5
3
4  vector<int> v;
5  reverse(v.begin(), v.end());
6
7  string str = "123";
8  reverse(str.begin(), str.end());
9  cout << str << endl; //321

```

7.8 CHAR

```

1 isdigit()
2 isalnum() //判斷字母 // 數字
3 isalpha()
4 islower()
5 isupper()
6 isblank() //判斷是否為空格，或者 tab 健制表符，即
   space 和 \t
7 toupper()
8 tolower()

```

7.9 sort

```

1 priority_queue<int, vector<int>, less<int>> //大到小
2 priority_queue<int, vector<int>, greater<int>>
   //小到大
3
4 int arr[] = {4, 5, 8, 3, 7, 1, 2, 6, 10, 9};
5 sort(arr, arr+10);
6
7 vector<int> v;
8 sort(v.begin(), v.end()); //小到大
9
10 int cmp(int a, int b){
11     return a > b;
12 }
13 sort(v.begin(), v.end(), cmp); //大到小

```

7.10 struct

```

1 struct area{
2     int a, b;
3     bool operator<(const area rhs) const{
4         return a > rhs.a || ( a == a && b > rhs.b);
5     }
6     bool operator!=(const area rhs) const{
7         return a != rhs.a || b != rhs.b;
8     }
9 };

```

7.11 deque

```

1 deque <int> que;
2 que.push_back(10);
3 que.push_front(20);
4 que.front()
5 que.back()
6 que.pop_front()
7 que.pop_back()
8 cout << "Element at position 2 : " << que.at(2) <<
   endl;

```

7.12 python template

```

1 import math
2 import operator
3
4 try:
5     while(1):
6         listx = []
7         listx.append("...")
8         list_s = sorted(listx) # 小到大
9         list_s = sorted(listx, reverse = True) #
           大到小
10         # max(listx)
11         # min(listx)
12         # sum(listx)

```

```

13         # len(listx)
14         dicty = {}
15         dicty[key] = "value"
16         dicty= sorted(dicty.items()) # by key
17         dicty= sorted(dicty.items(),
           key=operator.itemgetter(1)) # by value
18         # EOF寫法
19         # 階層 math.factorial(3) == 6
20         # 絕對值 math.fabs(x)
21         # 無條件進位 math.ceil(3.1) == 3
22         # 無條件捨去 math.floor(2.9) == 2
23         # C n 取 k math.comb(n, k)
24         # math.gcd
25         # math.lcm
26         # e 次 x 冪 math.exp(x)
27 except EOFError:
28     pass

```