10

3

8

8

9

10

11

11

11 }

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## Data Structure

## 1.1 Binary Search

```
1 int binary_search(int arr[maxn], int lef, int rig,
      int target){
      if(lef > rig) return 0x3f3f3f3f;
      int mid = (lef + rig) >> 1;
3
      if(arr[mid] == target) return mid;
5
      else if(arr[mid] > target){
6
          return binary_search(arr, lef, mid - 1,
              target);
7
      }
8
9
          return binary_search(arr, mid + 1, rig,
              target):
```

```
1.2 BIT
```

}

```
#define lowbit(k) (k & -k)
  void add(vector<int> &tr, int id, int val) {
    for (; id <= n; id += lowbit(id)) {</pre>
      tr[id] += val;
5
6
  }
  int sum(vector<int> &tr, int id) {
7
    int ret = 0;
9
    for (; id >= 1; id -= lowbit(id)) {
10
      ret += tr[id];
    }
11
12
    return ret;
13 }
```

## Segment tree

```
1 int dfs(int lef, int rig){
       if(lef + 2 == rig){
           if(num[lef] > num[rig-1]){
               return lef;
           else{
 7
               return rig-1;
8
9
10
       int mid = (lef + rig)/2;
11
       int p1 = dfs(lef, mid);
12
       int p2 = dfs(mid, rig);
       if(num[p1] > num[p2]){
13
14
           return p1;
15
       }
       else{
16
17
           return p2;
18
19 }
```

# 1.4 Trie

```
const int MAXL = ; // 自己填
  const int MAXC = ;
  struct Trie {
    int nex[MAXL][MAXC];
    int len[MAXL];
    int sz;
     void init() {
      memset(nex, 0, sizeof(nex));
8
       memset(len, 0, sizeof(len));
10
11
12
     void insert(const string &str) {
13
       int p = 0;
       for (char c : str) {
14
         int id = c - 'a';
15
         if (!nex[p][id]) {
16
17
           nex[p][id] = ++sz;
18
19
         p = nex[p][id];
      }
20
21
      len[p] = str.length();
22
23
     vector<int> find(const string &str, int i) {
24
       int p = 0;
       vector<int> ans;
25
26
       for (; i < str.length(); i++) {</pre>
27
         int id = str[i] - 'a';
         if (!nex[p][id]) {
28
```

```
29
           return ans;
         }
30
         p = nex[p][id];
31
         if (len[p]) {
32
33
           ans.pb(len[p]);
34
35
       return ans;
37
38 };
  1.5 BWT
1 /* BWT 資料轉換演算法 */
```

```
void BWT(){
2
       for(int i = 0; i < n; ++i){
           if(back[i] == 0)
5
                mini[zero++] = i;
6
       for(int i = 0; i < n; ++i)</pre>
           if(back[i] == 1)
7
               mini[zero++] = i;
9
       int ptr = mini[0];
10
       for(int i = 0; i < n; ++i){</pre>
11
           cout << back[ptr] << " ";
```

# 2 Divide and Conquer

ptr = mini[ptr];

12

13

14

15 }

#### 2.1 count inversions

cout << endl;</pre>

```
1 /*逆序數對*/
2 int arr[maxn], buf[maxn];
3 int count_inversions(int lef, int rig){
       if(rig - lef <= 1) return 0;</pre>
4
5
       int mid = (lef + rig)/2;
       int ans = count_inversions(lef, mid) +
6
            count_inversions(mid, rig);
7
       int i = lef, j = mid, k = lef;
8
       while(i < mid || j < rig){</pre>
           if(i >= mid) buf[k] = arr[j++];
9
           else if(j >= rig) buf[k] = arr[i++];
10
           else{
11
12
                if(arr[i] <= arr[j]) buf[k] = arr[i++];</pre>
13
                else{
                    buf[k] = arr[j++];
14
                    ans += mid - i;
15
                }
16
           }
17
18
           k++;
19
       for(int k = lef; k < rig; ++k) arr[k] = buf[k];</pre>
20
21
       return ans;
22 }
```

# 3 DP

## 3.1 Doubling

```
1  /* 倍增 */
2  int LOG = sqrt(N); // 2^LOG >= N
3  vector<int> arr(N);
4  vector<vector<int>> dp(N, vector<int>(LOG));
5  for(int i = 0; i < N; ++i) cin >> arr[i];
6  int L, Q, a, b;
7  cin >> L >> Q;
8  for(int i = 0; i < N; ++i){
```

```
9
       dp[i][0] = lower_bound(arr.begin(), arr.end(),
           arr[i] + L) - arr.begin();
       if(dp[i][0] == N || arr[i] + L < arr[dp[i][0]])</pre>
10
           dp[i][0] -= 1;
11
  }
  for(int i = 1; i < LOG; ++i)</pre>
12
      for(int j = 0; j < N; ++j)
13
14
           dp[j][i] = dp[dp[j][i - 1]][i - 1];
  for(int i = 0; i < 0; ++i){
15
      cin >> a >> b;
16
      a--; // 要減減是因為arr的index從0開始但題目從1開始
17
      b--;
18
      if(a > b) swap(a, b);
19
20
       int ans = 0;
       for(int i = LOG - 1; i >= 0; --i){ // 從後往回推
21
           if(dp[a][i] < b){</pre>
22
               ans += (1 << i);
23
               a = dp[a][i];
24
25
26
      }
      cout << ans + 1 << endl;
27
28 }
```

## 3.2 Josephus

### 3.3 LCS

```
1 int LCS(string s1, string s2) {
    int n1 = s1.size(), n2 = s2.size();
    int dp[n1+1][n2+1] = \{0\};
    // dp[i][j] = s1的前i個字元和s2的前j個字元
    for (int i = 1; i <= n1; i++) {</pre>
      for (int j = 1; j <= n2; j++) {</pre>
        if (s1[i - 1] == s2[j - 1]) {
           dp[i][j] = dp[i - 1][j - 1] + 1;
           dp[i][j] = max(dp[i - 1][j], dp[i][j - 1]);
10
11
12
13
    }
14
    return dp[n1][n2];
15 3
```

## 3.4 LIS

```
1 int LIS(vector<int> &a) { // Longest Increasing
     vector<int> s;
     for (int i = 0; i < a.size(); i++) {</pre>
       if (s.empty() || s.back() < a[i]) {</pre>
         s.push_back(a[i]);
5
6
       } else {
7
         *lower_bound(s.begin(), s.end(), a[i],
8
           [](int x, int y) {return x < y;}) = a[i];
9
10
    }
11
     return s.size();
12 }
```

## **4 Enumerate**

#### 4.1 Halfcut Enumerate

```
1 /* 折半枚舉 */
  void dfs(set<long long int> &s, int depth, int T,
      long long int sum){
3
      if(depth >= T){
4
          s.insert(sum);
5
          return;
6
      }
7
      dfs(s, depth + 1, T, sum); // 取或不取的概念
8
      dfs(s, depth + 1, T, sum + A[depth]);
9
  }
10
  int main(){
11
      int N, T;
      set < long long int > s1, s2;
12
13
      cin >> N >> T;
      for(int i = 0; i < N; ++i) cin >> A[i];
14
15
      dfs(s1, 0, N/2, 0); // 折半枚舉
      dfs(s2, N/2, N, 0);
16
      long long int ans = 0;
17
      // 題目:枚舉集合 Sx 的數字 Sxi,找出 Sy
18
           集合內小於等於 T-Sxi 中最大的數 Syj
19
      for(auto &x : s1){
20
          auto it = s2.upper_bound(T - x);
          long long int y = *(--it);
21
22
          if(x + y \le T) ans = max(ans, x + y);
      }
23
24
      cout << ans << endl;</pre>
25 }
```

# 5 Graph

### 5.1 SPFA

```
1 bool SPFA(int s){
       // 記得初始化這些陣列
2
3
       int cnt[1000+5], dis[1000+5];
       bool inqueue[1000+5];
5
       queue < int > q;
6
7
       q.push(s);
       dis[s] = 0;
9
       inqueue[s] = true;
10
       cnt[s] = 1;
11
       while(!q.empty()){
           int now = q.front();
12
13
           q.pop();
14
           inqueue[now] = false;
15
16
           for(auto &e : G[now]){
                if(dis[e.t] > dis[now] + e.w){
17
                    dis[e.t] = dis[now] + e.w;
18
19
                    if(!inqueue[e.t]){
20
                         cnt[e.t]++;
21
                         if(cnt[e.t] > m){
                             return false;
22
23
                         inqueue[e.t] = true;
24
25
                         q.push(e.t);
                    }
26
27
               }
28
           }
       }
29
30
       return true;
31 }
```

## 5.2 Dijkstra

```
1 struct Item{
2 int u, dis;
3 // 取路徑最短
4 bool operator < (const Item &other) const{
return dis > other.dis;
```

```
7 };
  int dis[maxn];
  vector<Edge> G[maxn];
10
  void dijkstra(int s){
       for(int i = 0; i <= n; i++){</pre>
11
           dis[i] = inf;
12
13
       dis[s] = 0;
14
15
       priority_queue < Item > pq;
16
       pq.push({s, 0});
17
       while(!pq.empty()){
           // 取路徑最短的點
18
19
           Item now = pq.top();
20
           pq.pop();
21
           if(now.dis > dis[now.u]){
22
               continue;
23
           // 鬆弛更新,把與 now.u 相連的點都跑一遍
24
25
           for(Edge e : G[now.u]){
26
               if(dis[e.v] > now.dis + e.w){
27
                    dis[e.v] = now.dis + e.w;
28
                    pq.push({e.v, dis[e.v]});
29
           }
30
31
       }
32 }
```

## 5.3 Floyd Warshall

```
void floyd_warshall(){
       for(int i = 0; i < n; i++){</pre>
3
           for(int j = 0; j < n; j++){
4
               G[i][j] = INF;
5
6
           G[i][i] = 0;
7
8
       for (int k = 0; k < n; k++){
           嘗試每一個中繼點
9
           for (int i = 0; i < n; i++){ //</pre>
               計算每一個i點與每一個j點
               for (int j = 0; j < n; j++){
10
                   G[i][j] = min(G[i][j], G[i][k] +
11
                       G[k][j]);
               }
12
13
           }
      }
14
15 }
```

## 5.4 Disjoint set Kruskal

```
1 struct Edge{
2
       int u, v, w;
       // 用權重排序 由大到小
3
       bool operator < (const Edge &other) const{</pre>
5
           return w > other.w;
       }
6
7 } edge[maxn];
8
  // disjoint set
9
  int find(int x){
    if(parent[x] < 0){</pre>
10
11
       return x;
12
13
       return parent[x] = find(parent[x]);
14
15
16 }
17
  void unite(int a, int b){
    a = find(a);
18
    b = find(b);
19
20
21
     if(a != b){
       if(parent[a] < parent[b]){</pre>
```

```
23
        parent[a] += parent[b];
                                                            44 }
        parent[b] = a;
24
                                                              bool branch2(){ // 延展交錯樹:使用新添的等邊
                                                            45
25
      }
                                                                  for (int y=0; y<Y; ++y){</pre>
                                                            46
26
      else{
                                                                      if (!vy[y] && dy[y] == 0){
                                                            47
27
        parent[b] += parent[a];
                                                            48
                                                                          vy[y] = true;
28
        parent[a] = b;
                                                            49
                                                                          if (my[y] == -1){
29
                                                            50
                                                                               augment(pdy[y], y);
30
    }
                                                                               return true;
                                                            51
31 }
                                                            52
32
  void kruskal(){
                                                            53
                                                                          int z = my[y];
33
      memset(parent, -1, sizeof(parent));
                                                                          *qb++ = z; p[z] = pdy[y]; vx[z] = true;
      sort(edge, edge + m);
34
                                                                               relax(z):
35
      int i, j;
                                                                      }
                                                            55
      for(i = 0, j = 0; i < n - 1 && j < m; i++){
36
                                                            56
                                                                  }
          // 如果 u 和 v 的祖先相同, 則 j++
37
                                                                  return false;
                                                            57
               (祖先相同代表會產生環 所以不要)
                                                            58
                                                              }
          while(find(edge[j].u) == find(edge[j].v)) j++;
                                                            59 int Hungarian(){
38
           // 若部會產生環 則讓兩點之間產生橋
                                                            60
                                                                  // 初始化vertex labeling
39
                                                                     memset(lx, 0, sizeof(lx)); // 任意值皆可
               (連接兩顆子生成樹)
                                                            61
                                                            62
                                                                  memset(ly, 0, sizeof(ly));
40
          unite(edge[j].u, edge[j].v);
41
                                                            63
                                                                  for (int x=0; x<X; ++x)
          j++;
                                                                      for (int y=0; y<Y; ++y)</pre>
                                                            64
42
      }
                                                            65
                                                                           lx[x] = max(lx[x], adj[x][y]);
43 }
                                                            66
                                                                  // X側每一個點,分別建立等邊交錯樹。
                                                            67
                                                            68
                                                                  memset(mx, -1, sizeof(mx));
  5.5 KM
                                                                  memset(my, -1, sizeof(my));
                                                            69
                                                            70
                                                                  for (int x=0; x<X; ++x){</pre>
                                                            71
                                                                      memset(vx, false, sizeof(vx));
                      // X的點數,等於Y的點數
1 const int X = 50;
                                                            72
                                                                      memset(vy, false, sizeof(vy));
2 | const int Y = 50;
                      // Y的點數
                                                            73
                                                                      memset(dy, 0x7f, sizeof(dy));
                      // 精簡過的adjacency matrix
3 int adj[X][Y];
                                                            74
                                                                      qf = qb = q;
  int lx[X], ly[Y];
                      // vertex labeling
                                                            75
                                                                      *qb++ = x; p[x] = -1; vx[x] = true; relax(x);
5 int mx[X], my[Y];
                      //
                                                            76
                                                                      while (true){
       X各點的配對對象、Y各點的配對對象
                                                            77
                                                                          if (branch1()) break;
6 int q[X], *qf, *qb; // BFS queue
                                                                           reweight():
                                                            78
                       // BFS
7 int p[X];
                                                            79
                                                                          if (branch2()) break;
      parent,交錯樹之偶點,指向上一個偶點
                                                            80
8 bool vx[X], vy[Y]; // 記錄是否在交錯樹上
                                                            81
                                                                  }
9 int dy[Y], pdy[Y]; // 表格
                                                                  // 計算最大權完美匹配的權重
                                                            82
10
                                                                  int weight = 0;
                                                            83
11
  void relax(int x){ // relaxation
                                                            84
                                                                  for (int x=0; x<X; ++x)</pre>
      for (int y=0; y<Y; ++y)</pre>
12
                                                            85
                                                                      weight += adj[x][mx[x]];
          if (adj[x][y] != 1e9)
13
                                                            86
                                                                  return weight;
               if (lx[x] + ly[y] - adj[x][y] < dy[y]){
14
                                                            87 }
                  dy[y] = lx[x] + ly[y] - adj[x][y];
15
16
                  pdy[y] = x; //
                       記錄好是從哪個樹葉連出去的
                                                              5.6 Dinic
17
              }
18 }
                                                            1 // Maximum Flow
19
  void reweight(){ // 調整權重、調整表格
20
      int d = 1e9;
                                                              const int V = 100, E = 1000;
                                                              int adj[V]; // adjacency lists, 初始化為-1。
      for (int y=0; y<Y; ++y) if (!vy[y]) d = min(d,</pre>
21
           dy[y]);
                                                              struct Element {int b, r, next;} e[E*2];
      for (int x=0; x<X; ++x) if ( vx[x]) lx[x] -= d;</pre>
22
                                                            5
                                                              int en = 0;
23
      for (int y=0; y<Y; ++y) if ( vy[y]) ly[y] += d;</pre>
                                                              void addedge(int a, int b, int c){
24
      for (int y=0; y<Y; ++y) if (!vy[y]) dy[y] -= d;</pre>
                                                                  e[en] = (Element)\{b, c, adj[a]\}; adj[a] = en++;
25 }
                                                                  e[en] = (Element){a, 0, adj[b]}; adj[b] = en++;
                                                            8
26 void augment(int x, int y){ // 擴充路徑
                                                            9
                                                              }
27
      for (int ty; x != -1; x = p[x], y = ty){
                                                            10 int d[V];
                                                                               // 最短距離
                                                            11 bool visit[V]; // BFS/DFS visit record
          ty = mx[x]; my[y] = x; mx[x] = y;
28
                                                                              // queue
29
                                                            12
                                                              int q[V];
                                                              int BFS(int s, int t){ // 計算最短路徑,求出容許圖
30 }
                                                            13
31 bool branch1(){ // 延展交錯樹:使用既有的等邊
                                                            14
                                                                  memset(d, 0x7f, sizeof(d));
      while (qf < qb)</pre>
                                                                  memset(visit, false, sizeof(visit));
32
                                                            15
33
           for (int x=*qf++, y=0; y<Y; ++y)</pre>
                                                                  int qn = 0;
               if (!vy[y] && lx[x] + ly[y] == adj[x][y]){
                                                                  d[s] = 0:
34
                                                           17
35
                   vy[y] = true;
                                                            18
                                                                  visit[s] = true;
36
                  if (my[y] == -1){
                                                            19
                                                                  q[qn++] = s;
37
                       augment(x, y);
                                                            20
38
                       return true;
                                                            21
                                                                  for (int qf=0; qf<qn; ++qf){</pre>
                  }
                                                            22
                                                                      int a = q[qf];
39
40
                                                                      for (int i = adj[a]; i != -1; i = e[i].next){
                   int z = my[y];
                                                            23
```

24

25

26

27

int b = e[i].b;

if (e[i].r > 0 && !visit[b]){
 d[b] = d[a] + 1;

visit[b] = true;

41

42

43

\*qb++ = z; p[z] = x; vx[z] = true;

relax(z);

}

return false;

```
28
                    q[qn++] = b;
                   if (b == t) return d[t];
29
               }
30
31
           }
32
33
       return V;
34 }
35 int DFS(int a, int df, int s, int t){ //
       求出一條最短擴充路徑,並擴充流量
       if (a == t) return df;
36
       if (visit[a]) return 0;
37
38
       visit[a] = true;
       for (int i = adj[a]; i != -1; i = e[i].next){
39
40
           int b = e[i].b;
           if (e[i].r > 0 && d[a] + 1 == d[b]){
41
42
               int f = DFS(b, min(df, e[i].r), s, t);
               if (f){
43
44
                   e[i].r -= f;
45
                   e[i^1].r += f;
46
                    return f;
47
           }
48
49
50
       return 0;
51 }
  int dinitz(int s, int t){
52
       int flow = 0;
53
       while (BFS(s, t) < V)
55
           while (true){
56
               memset(visit, false, sizeof(visit));
57
               int f = DFS(s, 1e9, s, t);
               if (!f) break;
58
59
               flow += f;
           }
60
61
       return flow;
62 }
```

## 5.7 Bipatirate

```
1 const int maxn = 300 + 5;
2 int n. color[maxn]:
3 vector<vector<int>> v(maxn);
4 bool dfs(int s){
5
       for(auto it : v[s]){
6
           if(color[it] == -1){
7
                color[it] = 3 - color[s];
8
                if(!dfs(it)){
9
                    return false;
10
           }
11
           if(color[s] == color[it]){
12
13
                return false;
           }
14
15
16
       return true;
17 }
18 void isBipatirate(){
       bool flag = true;
19
20
       for(int i = 1; i <= n; ++i){
           if(color[i] == -1){
21
22
                color[i] = 1;
23
                flag &= dfs(i);
           }
24
25
       if(flag){
26
27
           cout << "YES" << endl;</pre>
       }
28
29
       else{
           cout << "NO" << endl;
30
31
32 }
33 int main(){
34
       while(cin >> n && n){
           for(int i = 1; i <= n; ++i) v[i].clear();</pre>
35
           memset(color, -1, sizeof(color));
36
```

```
int a, b;
while(cin >> a >> b && (a || b)){
    v[a].emplace_back(b);
    v[b].emplace_back(a);
}
isBipatirate();

41
}
```

## 5.8 Hungarian algorithm

```
1 const int maxn = 500+5;
2 int t, N, bn, gn, match[maxn];
3
  bool visited[maxn];
  vector<vector<int>> G(maxn);
  struct People{
       int h;
7
       string music, sport;
       People(){}
8
9
       People(int h, string music, string sport){
           this->h = h;
10
           this->music = music;
11
12
           this->sport = sport;
13
14
  }lef[maxn], rig[maxn];
  bool check(People boy, People girl){
15
       if(abs(boy.h - girl.h) <= 40 && boy.music ==</pre>
           girl.music && boy.sport != girl.sport) return
           true:
17
       return false;
18 }
19
  bool dfs(int s){
       for(int i = 0; i < G[s].size(); ++i){</pre>
20
21
           int v = G[s][i];
22
           if(visited[v]) continue;
           visited[v] = true;
23
24
           if(match[v] == -1 || dfs(match[v])){
25
               match[v] = s;
26
                return true;
           }
27
28
       }
29
       return false;
30
  }
31
  int Hungarian(){
32
       int cnt = 0;
33
       memset(match, -1, sizeof(match));
34
       for(int i = 0; i < bn; ++i){</pre>
35
           memset(visited, false, sizeof(visited));
36
           if(dfs(i)) cnt++;
37
       }
38
       return cnt;
39 }
40
  int main(){
41
       cin >> t;
42
       while(t--){
           cin >> N;
43
           bn = 0, gn = 0;
44
           for(int i = 0; i <= N; ++i) G[i].clear();</pre>
45
46
           int h;
47
           string sex, music, sport;
48
           for(int i = 0; i < N; ++i){
                cin >> h >> sex >> music >> sport;
49
                if(sex == "M") lef[bn++] = People(h,
50
                    music, sport);
51
                else rig[gn++] = People(h, music, sport);
52
           for(int i = 0; i < bn; ++i){</pre>
53
54
                for(int j = 0; j < gn; ++j)</pre>
                    if(check(lef[i], rig[j]))
55
                        G[i].emplace_back(j);
56
57
           cout << N - Hungarian() << endl;</pre>
58
       }
59 }
```

#### 5.9 LCA

```
1 /*最低共同祖先*/
2 // 此 node 下有機顆 node
3 int dfs(int node, int dep){
      depth[node] = dep + 1;
5
      if(G[node].empty()){
           siz[node] = 1;
6
7
           return 1;
9
      int total = 1;
10
      for(auto i : G[node])
           total += dfs(i.v, dep + 1);
11
      siz[node] = total;
12
13
      return siz[node];
14 }
15 // 找出每個節點的 2<sup>1</sup> 倍祖先
16 // 2^20 = 1e6 > 200000
17 void find_parent(){
      for(int i = 1; i < 20; i++)</pre>
18
19
           for (int j = 0; j < N; j++)
               parent[j][i] =
20
                   parent[parent[j][i-1]][i-1];
21 }
22 // 求兩點的LCA (利用倍增法)
23 int LCA(int a, int b){
       if (depth[b] < depth[a]) swap(a, b);</pre>
      if (depth[a] != depth[b]){
25
26
           int dif = depth[b] - depth[a];
           for (int i = 0; i < 20; i++){
27
               if (dif & 1) b = parent[b][i];
28
               dif >>= 1;
29
           }
30
31
      if (a == b) return a;
32
33
      for (int i = 19; i >= 0; i --){
           if (parent[a][i] != parent[b][i]){
34
35
               a = parent[a][i];
               b = parent[b][i];
36
37
           }
38
39
       return parent[a][0];
40 }
```

## 6 Other

### 6.1 Bubble Sort Expect Value

```
1 /* 期望值算法:
2 擲一枚公平的六面骰子,其每次「點數」的期望值是 3.5
|E(x)| = 1 * 1/6 + 2 * 1/6 + 3 * 1/6 + 4 * 1/6 + 5 *
      1/6 + 6 * 1/6
4 = (1 + 2 + 3 + 4 + 5 + 6)/6 = 3.5
5 bubble sort 每兩兩之間交換機率是 1/2
6| 總共會做 C(n, 2) 次
7 E(x) = C(n, 2) * 1/2 = (n * (n - 1))/2 * 1/2 */
8 int t, ca = 1;
9 cin >> t;
10 while(t--){
      long long int n;
11
      cin >> n;
12
      cout << "Case " << ca++ << ": ";
13
      // 如果 (n * (n - 1)) 可以被 4 整除
14
          代表最後答案會是整數,否則會是分數
15
      if((n * (n - 1)) % 4){
         cout << ((n * (n - 1)) / 2) << "/2" << endl;
16
17
      }
18
      else{
19
         cout << ( (n * (n - 1)) / 2 ) / 2 << endl;
20
21 }
```

### 6.2 ORXOR

```
1 /* 如何切區段,之所以要1<<n是為了可以跑000~111
  i = 0, binary i = 000
3 0 : 1 5 7
  i = 1, binary i = 001
5 1 : 1 5 7
6 \mid i = 2,binary i = 010,看得出來切了一刀
  2:1157
|i| = 3, binary |i| = 011
9 3 : 1 | 5 7
10 i = 4, binary i = 100, 為了要切在index=2, 所以才要1<<j
  4:1517
|12|i = 5, binary i = 101
13 5 : 1 5 | 7
|14| i = 6, binary i = 110
15 6 : 1 | 5 | 7
16
  i = 7, binary i = 111
17 7 : 1 | 5 | 7
18 可以觀察出來,前兩位 bit 是 1 時代表的意義是切在哪裡*/
19 int n:
20 int num[20+7];
21
  memset(num, 0, sizeof(num));
  cin >> n;
22
23 for(int i = 1; i \le n; i++){
      cin >> num[i];
25 }
26 int mini = 2147483647; // 不知道為甚麼只有 2147483647
      給過
27
  // 1 << n = n * 2
  for(int i = 0; i < (1 << n); i++){</pre>
28
29
      int XOR = 0, OR = 0;
      for(int j = 1; j <= n; j++){</pre>
31
          OR |= num[j];
          if((i & (1 << j))){</pre>
32
              XOR ^= OR;
33
              OR = 0;
34
35
          }
36
      XOR ^= OR;
37
      mini = min(mini, XOR);
38
39 }
40 cout << mini << endl;
```

### 6.3 Race to 1

```
1 const int N = 1000000;
2 bool sieve[N+5];
3 vector<int> pri;
  double dp[N+5];
  void Linear_Sieve(){ // 線性篩
       for (int i = 2; i < N; i++){</pre>
           if (!sieve[i])
8
               pri.push_back(i);
           for (int p: pri){
10
               if (i * p \ge N){
11
                    break:
12
13
               sieve[i * p] = true;
14
               if (i % p == 0){
15
                    break;
16
17
           }
18
  double dfs(int n){
20
21
       if(dp[n] != -1) return dp[n];
22
       dp[n] = 0;
       if(n == 1) return dp[n];
23
       int total = 0, prime = 0;
25
       for(int i = 0; i < pri.size() && pri[i] <= n;</pre>
           i++){
26
           total++;
27
           if(n % pri[i]) continue;
```

```
28
            prime++;
           dp[n] += dfs(n/pri[i]);
29
30
31
       dp[n] = (dp[n] + total)/prime; // 算期望值
32
       return dp[n];
33 }
34
  int main(){
       int t:
35
36
       int num:
       int ca = 1;
37
       for(int i = 0; i <= N; i++){</pre>
38
39
           dp[i] = -1;
40
41
       Linear_Sieve();
       cin >> t;
42
43
       while(t--){
           cin >> num;
44
45
           cout << "Case " << ca++ << ": " << fixed <<
46
                setprecision(10) << dfs(num) << endl;</pre>
47
48 }
```

## 6.4 X drawing

```
1 | long long int n, a, b, p, q, r, s;
2 cin >> n >> a >> b;
3 cin >> p >> q >> r >> s;
4
  for(long long int i = p; i <= q; i++){</pre>
       for(long long int j = r; j \le s; j++){
           if(abs(i - a) == abs(j - b)){
7
                cout << '#';
8
           }
9
           else{
                cout << '.';
10
11
       }
12
13
       cout << endl;</pre>
14 }
```

## 6.5 Big Mod

```
1 | ' ' '
2 Mod
3 \mid pow(x, y, z) = x^y \% z
5 # python 如何讀取直到 EOF 用 try except
6 try:
7
      while True:
          # input().split() 用空格切開讀取一整行
8
          # map (型態, input().split()) 才能把值全讀成
9
          B, P, M = map(int, input().split())
10
11
          print(pow(B, P, M))
12 except EOFError:
     exit
13
```

## 6.6 Crested Ibis vs Monster

## 6.7 dpd Knapsack 1

```
1 // dp 背包 - 時間/數量/價值 - 第幾分鐘符合
  int N, W;
  cin >> N >> W:
  int w[100000+5];
  int v[100000+5];
  for(int i = 0; i < N; i++){
      cin >> w[i] >> v[i];
8 }
9
  long long int dp[100000+5];
10 memset(dp, 0, sizeof(dp));
  for(int i = 0; i < N; i++){
11
      for(int j = W; j >= w[i]; j--){
12
13
          dp[j] = max(dp[j], dp[j - w[i]] + v[i]);
14
15 }
16 cout << dp[W] << endl;</pre>
```

#### 6.8 Fraction Floor Sum

```
1 / * [N/i] == M
  -> M <= N/i < M + 1
  -> N/(M+1) < i <= N/M */
4 long long int N;
  cin >> N;
5
6
  long long int ans = 0;
7
  for(long long int i = 1; i <= N; i++){</pre>
      long long int M = N / i;
9
      long long int n = N / M;
10
      // 總共會有 n - i 個的 [N/i] 值都是 M
      ans += (n - i + 1) * M;
11
12
      // 更新跳過 以免重複計算
13
14 }
15 cout << ans << endl;
```

## 6.9 Homer Simpson

```
1 // dp 背包 - 時間/數量 - 漢堡
  int m, n, t;
  while(cin >> m >> n >> t){
3
      int dp[10000+5];
      memset(dp, -1, sizeof(dp));
5
       dp[0] = 0;
7
       for(int i = m; i <= t; i++){</pre>
8
           if(dp[i - m] != -1){
9
               dp[i] = max(dp[i], dp[i - m] + 1);
10
11
       for(int i = n; i <= t; i++){</pre>
12
13
           if(dp[i - n] != -1){
               dp[i] = max(dp[i], dp[i - n] + 1);
14
15
16
17
       if(dp[t] == -1){ // 時間無法剛好吃滿的時候
           for(int i = t; i >= 0; i--){
18
19
               if(dp[i] != -1){
                    cout << dp[i] << " " << t - i << endl;
20
21
                    break;
               }
22
23
           }
24
      }
25
       else{
           cout << dp[t] << endl;</pre>
26
```

```
27
28 }
  6.10 Let Me Count The Ways
1 // dp - 時間/數量 - 硬幣排序
2 long long int n, dp[30000+5];
3 int coin[] = {1, 5, 10, 25, 50};
4 memset(dp, 0, sizeof(dp));
5|dp[0] = 1;
6
  for(int i = 0; i < 5; i++){
      for(int j = coin[i]; j < 30000+5; j++){</pre>
7
          if(dp[j - coin[i]] != -1){
9
              dp[j] += dp[j - coin[i]];
10
11
      }
```

cout << "There is only " << dp[n] << " way to</pre>

produce " << n << " cents change." <<

cout << "There are " << dp[n] << " ways to
 produce " << n << " cents change." <<</pre>

# 6.11 Luggage

13 while(cin >> n){

}

}

else{

 $if(dp[n] == 1){$ 

endl:

endl;

12 }

14

15

16

17

18

19

20 }

```
1 // dp 背包 - 重量/是否成立
2 int t;
3 cin >> t;
4 cin.ignore();
5 while(t--){
       string str;
7
       getline(cin , str);
       vector<int> v;
8
9
       stringstream ss;
10
       int num, cnt = 0, sum = 0;;
11
       bool dp[4000+5];
12
       memset(dp, false, sizeof(dp));
       ss << str;
13
       while(ss >> num){
14
15
           cnt++;
16
           sum += num;
           v.emplace_back(num);
17
18
       if(sum & 1){
19
           cout << "NO" << endl;
20
21
           continue;
22
23
       dp[0] = true;
       for(int i = 0; i < v.size(); i++){</pre>
24
           for(int j = sum; j >= v[i]; j--){
25
                if(dp[j - v[i]]){
26
27
                    dp[j] = true;
28
29
           }
30
       cout << (dp[sum/2] ? "YES" : "NO") << endl;</pre>
31
32 }
```

## 6.12 Number of Pairs

```
1  /* uper_bound ex:
2  10  20  30  30  40  50
3  upper_bound for element 30 is at index 4
4  lower_bound ex:
```

```
5 10 20 30 40 50
  lower_bound for element 30 at index 2 */
7
  int t;
  cin >> t;
8
  while(t--){
10
       int n, 1, r;
       vector<int> v;
11
12
       cin >> n >> 1 >> r;
13
       int num;
       for(int i = 0; i < n; i++){</pre>
14
15
           cin >> num;
           v.emplace_back(num);
16
17
       sort(v.begin(), v.end());
18
19
       long long int ans = 0;
       for(int i = 0; i < n; i++){</pre>
20
21
           ans += (upper_bound(v.begin() + i + 1,
                v.end(), r - v[i]) -
                lower_bound(v.begin() + i + 1, v.end(), 1
                - v[i]));
22
23
       cout << ans << endl;</pre>
24 }
```

## 6.13 SuperSale

```
1 // dp 背包 - 重量/價值/不可重複使用 - 舉重
2 int t;
  cin >> t;
4
  while(t--){
       int n;
       cin >> n;
6
7
       for(int i = 0; i < n; i++){
8
           cin >> edge[i].p >> edge[i].w;
9
10
       int g, total = 0;
11
       cin >> g;
       for(int i = 0; i < g; i++){
12
13
           int pw, dp[30+5];
           cin >> pw;
14
15
           memset(dp, 0, sizeof(dp));
           for(int j = 0; j < n; j++){</pre>
16
               for(int k = pw; k >= edge[j].w; k--){
17
                    dp[k] = max(dp[k], dp[k - edge[j].w]
18
                        + edge[j].p);
19
               }
           }
20
21
           total += dp[pw];
22
      }
23
       cout << total << endl;</pre>
24 }
```

## 6.14 Walking on the Safe Side

```
1 // dp - 地圖更新
  int t;
2
3
  bool space = false;
  cin >> t;
4
  while(t--){
6
       if(space){
7
           cout << endl;</pre>
       else{
9
10
           space = true;
       }
11
12
       int r, c;
13
       cin >> r >> c;
14
       cin.ignore();
15
       memset(mp, false, sizeof(mp));
16
       memset(dp, 0, sizeof(dp));
       string str;
17
       for(int i = 0; i < r; i++){</pre>
18
           getline(cin, str);
19
```

22

23

24

25

26 }

3

}

```
20
            int n, num;
21
            stringstream ss(str);
22
            ss >> n;
23
            while(ss >> num){
24
                 mp[n][num] = true;
25
       }
26
27
       dp[1][1] = 1;
       for(int i = 1; i <= r; i++){
28
29
            for(int j = 1; j <= c; j++){</pre>
30
                 if(mp[i][j]){
31
                     continue:
                 }
32
                 if(i > 1){
33
34
                     dp[i][j] += dp[i-1][j];
35
                 if(j > 1){
36
37
                      dp[i][j] += dp[i][j-1];
38
39
            }
40
41
       cout << dp[r][c] << endl;</pre>
42 }
```

## 6.15 Cutting Sticks

```
1 while (cin >> 1 && 1){
2
      cin >> n:
3
       vector<int> s(n+2);
      s[0] = 0;
       for(int i = 1; i <= n; ++i) cin >> s[i];
      s[++n] = 1; // 從現在開始 n 的數量變為 n + 1
7
      int dp[n+5][n+5];
      memset(dp, 0, sizeof(dp));
8
      for(int r = 2; r <= n; ++r){ // r: 切幾段 b: 起點
9
           c: 中間點 e: 終點
10
           for(int b = 0; b < n; ++b){
               if(b + r > n) break;
11
12
               int e = b + r;
               dp[b][e] = 0x3f3f3f3f;
13
14
               for(int c = b + 1; c < e; ++c){
15
                   dp[b][e] = min(dp[b][e], dp[b][c] +
                       dp[c][e] + s[e] - s[b]);
16
          }
17
18
       cout << "The minimum cutting is " << dp[0][n] <<</pre>
19
           "." << endl;
20 }
```

### 6.16 Partitioning by Palindromes

```
1 /*string & dp - 字串長度判斷迴文*/
2 bool check_palindromes(int lef, int rig){
       // 比較字串兩端都是迴文
3
       while(lef < rig){</pre>
5
           if(str[lef] != str[rig]) return 0;
6
           lef++;
           rig--;
8
      }
9
      return 1;
10 }
11 int main(){
12
       int t;
13
       cin >> t;
14
       while(t--){
           cin >> str;
15
           memset(dp, 0x3f3f3f3f, sizeof(dp));
16
17
           dp[0] = 0;
18
           for(int i = 0; i < str.size(); ++i)</pre>
19
               for(int j = 0; j <= i; ++j)</pre>
                   if(str[i] == str[j])
20
                        if(check_palindromes(j, i))
21
```

## **Ants Colony**

const int maxn = 1e5 + 5;

1 /\* LCA 最低共同祖先\*/

if(dp[i+1] > dp[j] + 1)dp[i+1] = dp[j] + 1;

cout << dp[str.size()] << endl;</pre>

```
struct Edge{
      int v;
      int w;
  };
  int N:
7
  vector < Edge > G[maxn];
  int parent[maxn][20+5];
10 int depth[maxn], siz[maxn];
  // 此 node 下有機顆 node
11
12
  int dfs(int node, int dep){
       depth[node] = dep + 1;
13
14
       if(G[node].empty()){
15
           siz[node] = 1;
16
           return 1;
17
      }
18
       int total = 1;
19
       for(auto i : G[node])
           total += dfs(i.v, dep + 1);
20
       siz[node] = total;
22
       return siz[node];
23 }
  // 找出每個節點的 2<sup>i</sup> 倍祖先
24
25
  // 2^20 = 1e6 > 200000
  void find_parent(){
26
       for(int i = 1; i < 20; i++)
27
           for (int j = 0; j < N; j++)
28
29
               parent[j][i] =
                   parent[parent[j][i-1]][i-1];
30 }
  // 求兩點的LCA (利用倍增法)
31
  int LCA(int a, int b){
33
       if (depth[b] < depth[a]) swap(a, b);</pre>
34
       if (depth[a] != depth[b]){
35
           int dif = depth[b] - depth[a];
           for (int i = 0; i < 20; i++){
36
37
               if (dif & 1) b = parent[b][i];
38
               dif >>= 1;
39
40
41
      if (a == b) return a;
42
       for (int i = 19; i >= 0; i--){
           if (parent[a][i] != parent[b][i]){
43
44
               a = parent[a][i];
               b = parent[b][i];
45
46
47
      }
48
       return parent[a][0];
49
50 long long int dist[maxn];
  // 從 ∅ 開始到每個點的距離
51
52
  void distance(){
53
       for (int u = 0; u < N; ++u){
           for(int i = 0; i < G[u].size(); ++i){</pre>
54
55
               dist[G[u][i].v] = dist[u] + G[u][i].w;
  }
56
  int main(){
       while(cin >> N && N){
58
59
           memset(dist, 0, sizeof(dist));
           memset(parent, 0, sizeof(parent));
60
           memset(depth, 0, sizeof(depth));
61
62
           memset(siz, 0, sizeof(siz));
63
           for(int i = 0; i <= N; ++i){
               G[i].clear();
64
65
           for(int i = 1; i < N; ++i){</pre>
66
```

```
67
                 int u, w;
                 cin >> u >> w;
68
                 G[u].push_back({i, w});
69
70
                 parent[i][0] = u;
71
72
            find_parent();
            dfs(0, 0);
73
74
            distance();
75
            int s; cin >> s;
            bool space = false;
76
77
            for(int i = 0; i < s; ++i){</pre>
78
                 int a, b;
79
                 cin >> a >> b;
                 int lca = LCA(a, b);
80
81
                 if(space) cout << " ";</pre>
                 space = true;
82
                 cout << (dist[a] + dist[b]) - (dist[lca]</pre>
83
                      * 2);
            }
84
85
            cout << endl;</pre>
        }
86
87 }
```

#### 6.18 Fill the Containers

```
1 /*binary search 變形*/
2 int binary_search(int arr[maxn], int lef, int rig,
       int mini){
       if(lef > rig) return mini;
       int amount = 1, fill = 0;
       int mid = (lef + rig) >> 1;
       for(int i = 0; i < n; ++i){</pre>
6
7
           if(amount > m) break;
8
           fill += arr[i];
           if(fill > mid){
9
10
                fill = arr[i];
11
                amount++;
12
13
       }
       if(!flag && amount <= m) mini = mid;</pre>
14
15
       if(flag && amount == m) mini = mid;
       if(amount == m){
16
           flag = true;
17
18
           return binary_search(arr, lef, mid - 1, mid);
19
20
       else if(amount < m){</pre>
           return binary_search(arr, lef, mid - 1, mini);
21
       }
22
       else{
23
24
           return binary_search(arr, mid + 1, rig, mini);
25
26 }
27 int main(){
       int ca = 1;
28
29
       while(cin >> n >> m){
           flag = false;
30
           int arr[maxn];
31
           int maxi = 0, sum = 0;
32
           for(int i = 0; i < n; ++i){</pre>
33
34
                cin >> arr[i];
                sum += arr[i];
35
36
                maxi = max(maxi, arr[i]);
37
38
           cout << binary_search(arr, maxi, sum, maxi)</pre>
                << endl;
39
       }
40 }
```

### 6.19 How Many O's

```
1 /*數論*/
2 int main(){
3 long long int n, m;
```

```
while(cin >> n >> m && (n >= 0) && (m >= 0)){
           long long int total1 = 0, total2 = 0;
5
           long long int ten = 1, tmp = n-1;
7
           while(tmp >= 10){
8
               if(tmp % 10 == 0){
9
                    tmp /= 10;
10
                    total1 += (tmp - 1) * ten + ((n-1) %
                         ten) + 1;
               }
11
12
                else{
13
                    tmp /= 10;
                    total1 += tmp * ten;
14
15
               ten *= 10:
16
17
           }
           ten = 1; tmp = m;
18
19
           while(tmp >= 10){
20
               if(tmp % 10 == 0){
                    tmp /= 10;
21
22
                    total2 += (tmp - 1) * ten + (m % ten)
                        + 1;
23
24
                else{
25
                    tmp /= 10;
26
                    total2 += tmp * ten;
               }
27
                ten *= 10;
28
           }
29
30
           if(n == 0) total1--;
31
           cout << total2 - total1 << endl;</pre>
       }
32
33 }
```

## 6.20 Binary codes

```
1 /*BWT 資料轉換演算法*/
  void BWT(){
3
       for(int i = 0; i < n; ++i){</pre>
4
           if(back[i] == 0){
                mini[zero++] = i;
       for(int i = 0; i < n; ++i){</pre>
6
           if(back[i] == 1){
8
                mini[zero++] = i;
9
       int ptr = mini[0];
10
       for(int i = 0; i < n; ++i){
           cout << back[ptr] << " ";</pre>
11
12
            ptr = mini[ptr];
       }
13
14
       cout << endl;</pre>
15 }
  int main(){
16
17
       cin >> n;
       for(int i = 0; i < n; ++i){</pre>
18
19
           cin >> back[i];
       zero = 0;
20
       BWT();
21
22 }
```

## 7 Function

### 7.1 strstr

```
1  #include <stdio.h>
2  #include <string.h>
3
4  int main(){
5  char * c;
6  char str1[1005], str2[1005];
7  scanf("%s %s", str1, str2);
8  c = strstr(str1, str2);
9  if (c != NULL){
    printf("Yes\n");
```

```
11    }
12    else printf("No\n");
13    }
14    // Input : Hello eLl
15    // Output : No
```

### 7.2 substr

```
1 int main(){
2     string str; //abcdef
3     cin >> str;
4     string tmp;
5     tmp = str.substr(0, 2); //ab
6     str = str.substr(2); //cdef
7     cout << tmp << " " << str;
8     return 0;
9 }</pre>
```

## 7.3 map set

```
1 .begin( ) // Return iterator to beginning
2 .end( ) // Return iterator to end
3 .empty() // 檢查是否為空
4 . size( ) // 回傳大小
5 mp.insert(pair<char,int>('a',100))
6 st.insert(100) // 插入key \ value
7 .erase( ) // 刪掉指定key和他的value
8 .clear( ) // 清空整個 map
9 m.find()
10 cout << "a => " << mymap.find('a')->second << endl;</pre>
      // 找出 map 裡 key
          有沒有在裡面,如果有的話會回傳元素所在的iterator
12 s.count() // 返回某個值元素在 set 的 個數
13 while( !mymap.empty()){
      cout << mymap.begin()->first << " => " <<</pre>
14
          mymap.begin()->second << endl;</pre>
      mymap.erase(mymap.begin());
15
16 }
17 for (auto it = mymap.begin(); it != mymap.end(); ++it)
      cout << it->first << " => " << it->second << endl;</pre>
```

### 7.4 vector

```
1 | v.erase(v.begin() + 5) //拿掉第六個數
2 | v.erase (v.begin(), v.begin() + 3); //拿掉前三個數
```

# 7.5 setprecision

```
1 // 將數字的小數部分設定為固定長度
2 cnt = 3.5555;
3 cout << fixed << setprecision(3) << cnt ;
4 // output : 3.555
```

#### 7.6 GCD LCM

```
      1
      int gcd(int a, int b){

      2
      return (b == 0 ? a : gcd(b, a % b));

      3
      }

      4
      int lcm(int a, int b){

      5
      return a * b / gcd(a, b);

      6
      }

      7
      /* 輾轉相除法 - 求兩數是否互質

      9
      如果兩數互質 最終結果其中一方為0時 另一方必為1

      10
      若兩數有公因數 最終結果其中一方為0時 另一方必不為1 */

      11
      while ((num1 %= num2)!= 0 && (num2 %= num1)!=

      0);
```

### 7.7 reverse

```
1 | int a[10] = {0, 1, 2, 3, 4, 5, 6, 7, 8, 9};
2 | reverse(a, a+5) // 轉換0~5
3 | vector<int> v;
reverse(v.begin(), v.end());
6 |
7 | string str = "123";
8 | reverse(str.begin(), str.end());
9 | cout << str << endl; //321</pre>
```

## 7.8 CHAR

#### 7.9 sort

#### 7.10 struct

```
1  struct area{
2    int a, b;
3    bool operator < (const area rhs) const{
4        return a > rhs.a || ( a == a && b > rhs.b);
5    }
6    bool operator!=(const area rhs) const{
7        return a != rhs.a || b != rhs.b;
8    }
9 };
```

## 7.11 deque

```
1 deque <int> que;
2 que.push_back(10);
3 que.push_front(20);
4 que.front()
5 que.back()
6 que.pop_front()
7 que.pop_back()
8 cout << "Element at position 2 : " << que.at(2) << end];</pre>
```

## 7.12 python template

```
1 import math
2 import operator
3
4
5
      while(1):
          listx = []
          listx.append("...")
7
          list_s = sorted(listx) # 小到大
8
9
          list_s = sorted(listx, reverse = True) #
              大到小
          # max(listx)
10
          # min(listx)
11
12
          # sum(listx)
          # len(listx)
13
14
          dicty = {}
          dicty[key] = "value"
15
          dicty= sorted(dicty.items()) # by key
16
          dicty= sorted(dicty.items(),
17
              key=operator.itemgetter(1)) # by value
          # EOF寫法
18
          # 階層 math.factorial(3) == 6
19
          # 絕對值 math.fabs(x)
20
          # 無條件進位 math.ceil(3.1) == 3
21
          # 無條件捨去 math.floor(2.9) == 2
22
          # C n 取 k math.comb(n, k)
23
24
          # math.gcd
          # math.lcm
25
          # e 次 x 幂 math.exp(x)
26
27 except EOFError:
28
      pass
```