

MATHEMATICS

SECTION - A

Multiple Choice Questions: This section contains 20 multiple choice questions. Each question has 4 choices (1), (2), (3) and (4), out of which **ONLY ONE** is correct.

Choose the correct answer:

1. If
$$\sum_{r=1}^{9} \left(\frac{r+3}{2^r}\right) \cdot {}^9C_r = \alpha \left(\frac{3}{2}\right)^9 - \beta$$
, α , $\beta \in \mathbb{N}$, then

 $(\alpha + \beta)^2$ is equal to

(1) 18

(2) 27

(3) 81

(4) 9

Answer (3)

Sol.
$$\sum_{r=1}^{9} \left(\frac{r+3}{2^r}\right) \cdot {}^{9}C_r = \sum_{r=1}^{9} \frac{r}{2^r} \cdot \frac{9}{r} \cdot {}^{8}C_{r-1} + \sum_{r=1}^{9} 3 \cdot {}^{9}C_r \left(\frac{1}{2}\right)^r$$

$$= \frac{9}{2} \sum_{r=1}^{9} {}^{8}C_{r-1} \left(\frac{1}{2}\right)^{r-1} + 3 \sum_{r=1}^{9} {}^{9}C_r \left(\frac{1}{2}\right)^r$$

$$= \frac{9}{2} \sum_{r=0}^{8} {}^{8}C_{r-1} \left(\frac{1}{2}\right)^r + 3 \sum_{r=1}^{9} {}^{9}C_r \left(\frac{1}{2}\right)^r$$

$$= \frac{9}{2} \left(1 + \frac{1}{2}\right)^8 + 3 \left[\left(1 + \frac{1}{2}\right)^9 - {}^{9}C_0 \left(\frac{1}{2}\right)^0\right]$$

$$= \frac{9}{2} \cdot \frac{3^8}{2^8} + 3 \left[\frac{3^9}{2^9} - 1\right]$$

$$= \frac{3^{10}}{2^9} + \frac{3^{10}}{2^9} - 3 = 4 \cdot \frac{3^{10}}{2^{10}} - 3$$

$$= 4 \left(\frac{3}{2}\right)^{10} - 3$$

$$= 6 \left(\frac{3}{2}\right)^9 - 3$$

$$\alpha = 6, \beta = 3 \Rightarrow (\alpha + \beta)^2 = 81$$

- Let $z \in \mathbb{C}$ be such that $\frac{z^2 + 3i}{z 2 + i} = 2 + 3i$. Then the sum of all possible values of z^2 is
 - (1) -19 2i
- (2) -19 + 2i
- (3) 19 2i
- (4) 19 + 2i

Answer (1)

Sol.
$$\frac{z^2 + 3i}{z - 2 + i} = 2 + 3i$$

$$z^2 + 3i = (z - 2 + i)(2 + 3i)$$

$$z^2 + 3i = 2z - 4 + 2i + 3iz - 6i - 3i$$

$$z^2 + 3i = (2z - 7) + i(3z - 4)$$

$$z^2 - (2 + 3i)z + (7 + 7i) = 0$$

This is a quadratic in z.

$$z_1 + z_2 = 2 + 3i$$

$$z_1 + z_2 = 7 + 7i$$

$$z_1^2 + z_2^2 = (z_1 + z_2)^2 - 2z_1z_2$$

$$= (2 + 3i)^2 - 2(7 + 7i)$$

$$=4-9+12i-14-14i$$

- Let a line passing through the point (4, 1, 0) intersect the line $L_1: \frac{x-1}{2} = \frac{y-2}{3} = \frac{z-3}{4}$ at the point $A(\alpha, \beta, \gamma)$ and the line $L_2: x - 6 = y = -z + 4$ at the point B(a, b, c). Then $\begin{vmatrix} 1 & 0 & 1 \\ \alpha & \beta & \gamma \\ a & b & c \end{vmatrix}$ is equal to
 - (1) 16

(2) 6

- (3) 12
- (4) 8

Answer (4)

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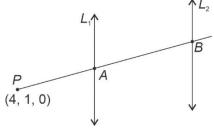








Sol.



$$A = (\alpha, \beta, 4) = (2\lambda + 1, 3\lambda + 2, 4\lambda + 3)$$

and
$$B = (a, b, c) = (\mu + 6, \mu, -\mu + 4)$$

$$\therefore \frac{\mu+2}{2\lambda-3} = \frac{\mu-1}{3\lambda+1} = \frac{-\mu+4}{4\lambda+3}$$

$$\therefore \lambda \mu + 8 \lambda + 4 \mu = 1$$
 ...(1)

and
$$7\lambda\mu - 16\lambda + 4\mu = 7$$
 ...(2)

from equation (1) and (2)

$$\lambda$$
 = -1 and μ = 3

Or
$$\lambda = -\frac{1}{3}$$
 and $\mu = 1$

By taking, $\lambda = -1$ and $\mu = 3$, we get

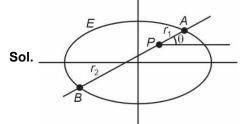
$$\therefore$$
 $A(\alpha, \beta, 4) = (-1, -1, -1)$

and B(a, b, c) = (9, 3, 1)

$$\begin{vmatrix} 1 & 0 & 1 \\ -1 & -1 & -1 \\ 9 & 3 & 1 \end{vmatrix} = 8$$

- 4. A line passing through the point $P(\sqrt{5}, \sqrt{5})$ intersects the ellipse $\frac{x^2}{36} + \frac{y^2}{25} = 1$ at A and B such that $(PA)\cdot(PB)$ is maximum. Then $5(PA^2 + PB^2)$ is equal to
 - (1) 377
- (2) 218
- (3) 338
- (4) 290

Answer (3)



$$\frac{x-\sqrt{5}}{\cos\theta} = \frac{y-\sqrt{5}}{\sin\theta} = r$$

$$x = r\cos\theta + \sqrt{5}$$

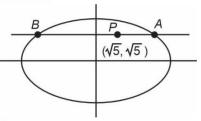
$$y = r \sin \theta + \sqrt{5}$$

$$25x^2 + 36y^2 = 900$$
, (x, y) lie on E

$$r^{2} \Big[25\cos^{2}\theta + 36\sin^{2}\theta \Big] + r \Big[50\sqrt{5}\cos\theta + 72\sqrt{5}\sin\theta \Big]$$

$$r_1 r_2 = \frac{900 - 305}{25 + 11 \sin^2 \theta}, (r_1 r_2)_{\text{max}} = \frac{595}{25} = \frac{119}{5}$$

$$|r_1 \cdot r_2|_{\text{max}} = \left(\frac{595}{25}\right) = \left(\frac{119}{5}\right) \text{ at } \theta = 0$$



$$\frac{x^2}{36} + \frac{y^2}{25} = 1$$

At
$$v = \sqrt{5}$$

$$\frac{x^2}{36} + \frac{1}{5} = 1$$

$$\Rightarrow \frac{x^2}{36} = \frac{4}{5} \Rightarrow x = \pm \frac{12}{\sqrt{5}}$$

$$PA^{2} + PB^{2} = (PA + PB)^{2} - 2PA \cdot PB = \left(\frac{24}{\sqrt{5}}\right)^{2} - 2 \cdot \frac{119}{5}$$

$$5(PA^2 + PB^2) = 5\left(\frac{24^2}{5} - \frac{2.119}{5}\right) = 24^2 - 238$$

= 338.

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JEE Main (Session-1) 202

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- 5. Let A = (-3, -2, -1, 0, 1, 2, 3). Let R be a relation on A defined by xRy if and only if $0 \le x^2 + 2y \le 4$. Let I be the number of elements in R and m be the minimum number of elements required to be added in R to make it a reflexive relation. Then I + m is equal to
 - (1) 18

(2) 19

(3) 17

(4) 20

Answer (1)

Sol. $0 \le x^2 + 2y \le 4$

For
$$y = -3$$
, $x = \{3, -3\}$

For
$$y = -2$$
, $x = \{-2, 2\}$

For
$$y = -1$$
, $x = \{-2, 2\}$

For
$$y = 0$$
, $x = \{-2, -1, 0, 1, 2\}$

For
$$y = 1$$
, $x = \{-1, 0, 1\}$

For
$$y = 2$$
, $x = \{0\}$

$$R = \{(3, -3), (-3, -3), (-2, -2), (2, -2), (-2, -1), (2, -1), (-2, 0), (-1, 0), (0, 0), (1, 0), (2, 0), (-1, 1), (2, 0), (1, 0), (2,$$

I = 15

We need to add (-1, -1), (2, 2), (3, 3) to make it reflexive

$$m = 3 \Rightarrow I + m = 18$$

- 6. Let A be a matrix of order 3×3 and |A| = 5. If $|2adj(3A \ adj(2A))| = 2^{\alpha} \cdot 3^{\beta} \cdot 5^{\gamma}$, α , β , $\gamma \in \mathbb{N}$, then $\alpha + \beta + \gamma$ is equal to
 - (1) 25

(2) 26

(3) 27

(4) 28

Answer (3)

Sol. $|2adj(3A \ adj(2A))| = 2^3|3A(adj(2A))|^2$

$$=2^{3}(3^{3})^{2}|A|^{2}|adj(2A)^{2}|$$

$$=2^3 \cdot 3^6 \cdot 5^2 (|(2A)|^2)^2$$

$$= 2^3 \cdot 3^6 \cdot 5^2 |2A|^4$$

$$=2^3 \cdot 3^6 \cdot 5^2 \cdot (2^3)^4 \cdot |A|^4$$

$$=2^{15}\cdot 3^6\cdot 5^6$$

7. Let
$$f(x) = \begin{cases} (1+ax)^{1/x} &, x < 0 \\ 1+b &, x = 0 \end{cases}$$
$$\frac{(x+4)^{1/2}-2}{(x+c)^{1/3}-2}, x > 0$$

be continuous at x = 0. Then e^abc is equal to:

(1) 48

(2) 72

(3) 36

(4) 64

Answer (1)

Sol.
$$f(x) = \begin{cases} (1+ax)^{1/x} &, x < 0\\ 1+b &, x = 0\\ \frac{(x+4)^{1/2}-2}{(x+c)^{1/3}-2} &, x > 0 \end{cases}$$

Hence, f(0) = 1 + 6

RHL =
$$\lim_{x \to 0^+} \frac{(x+4)^{1/2} - 2}{(x+c)^{1/3} - 2}$$
 For $\frac{0}{0}$ form, $c = 8$

$$= \lim_{x \to 0} \frac{2\left(1 + \frac{x}{4}\right)^{1/2} - 2}{\left(1 + \frac{x}{8}\right)^{1/3} - 2}$$

$$= \lim_{x \to 0} \frac{1 + \frac{x}{8} - 1}{1 + \frac{x}{8} \cdot \frac{1}{3} - 1} = \frac{\frac{1}{8}}{\frac{1}{8} \cdot \frac{1}{3}} = 3$$

$$\therefore 1+b=3$$

$$\Rightarrow b = 2$$

LHL =
$$\lim_{x\to 0} (1+ax)^{1/x} = \lim_{x\to 0} e^{\frac{1+ax-1}{x}} = e^a = 3$$

$$e^{a} \cdot bc = 3.2.8 = 48$$

8. A line passes through the origin and makes equal angles with the positive coordinate axes. It intersects the lines $L_1: 2x + y + 6 = 0$ and $L_2: 4x + 2y - p = 0$, p > 0, at the points A and B, respectively.

If
$$AB = \frac{9}{\sqrt{2}}$$
 and the foot of the perpendicular from

the point A on the line L_2 is M, then $\frac{AM}{BM}$ is equal to

(1) 3

(2) 5

(3) 2

(4) 4

Answer (1)

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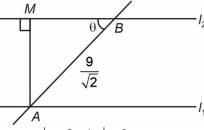




JEE (Main)-2025: Phase-2 (03-04-2025)-Morning



Sol.



$$\tan \theta = \left| \frac{-2-1}{1+(-2)(1)} \right| = \frac{3}{1}$$

$$\sin\theta = \frac{3}{\sqrt{10}}$$

$$AM = \frac{3}{\sqrt{10}} \times \frac{9}{\sqrt{2}} = \frac{27}{2\sqrt{5}}$$

Dist. between
$$I_1 \& I_2$$
, $AM = \left| \frac{P}{2} + 6 \right| = \frac{27}{2\sqrt{5}}$

$$\frac{P}{2}+6=\pm\frac{27}{2}$$

$$\frac{P}{2} = \frac{27}{2} - 6 \Rightarrow P = 15$$
, As $P > 0$

$$BM = \sqrt{\frac{81}{2} - \left(\frac{27}{2\sqrt{5}}\right)^2}$$

$$=\sqrt{\frac{810-729}{20}}=\sqrt{\frac{81}{20}}=\frac{9}{2\sqrt{5}}$$

Now,
$$\frac{AM}{BM} = \frac{\frac{27}{2\sqrt{5}}}{\frac{9}{2\sqrt{5}}} = 3$$

9. The sum of all rational terms in the expansion of

$$\left(2+\sqrt{3}\right)^8$$
 is

- (1) 3763
- (2) 18817
- (3) 33845
- (4) 16923

Answer (2)

Sol.
$$S = {}^8C_0(2)^8 + {}^8C_12^7(\sqrt{3}) + ... + {}^8C_8(\sqrt{3})^8$$

Sum of rational terms

$$={}^{8}C_{0}\left(2\right)^{8}+{}^{8}C_{2}2^{6}\left(\sqrt{3}\right)^{2}+{}^{8}C_{4}\left(2\right)^{4}\left(\sqrt{3}\right)^{4}+$$

$${}^{8}C_{6}\left(2\right)^{2}\left(\sqrt{3}\right)^{2}+{}^{8}C_{8}\left(\sqrt{3}\right)^{8}$$

= 18,817

- 10. Line L_1 passes through the point (1, 2, 3) and is parallel to z-axis. Line L_2 passes through the point $(\lambda, 5, 6)$ and is parallel to y-axis. Let for $\lambda = \lambda_1, \lambda_2, \lambda_2 < \lambda_1$, the shortest distance between the two lines be 3. Then the square of the distance of the point $(\lambda_1, \lambda_2, 7)$ from the line L_1 is
 - (1) 32

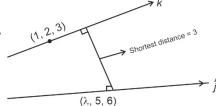
(2) 25

(3) 37

(4) 40

Answer (2)

Sol.

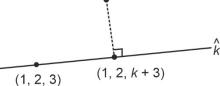


$$3 = \frac{\left| [(\lambda - 1) \hat{i} + 3 \hat{j} + 3 \hat{k}] \cdot (\hat{k} \times \hat{j}) \right|}{\left| \hat{k} \times \hat{j} \right|} = |\lambda - 1| = 3$$

$$\Rightarrow \lambda = 4 \text{ or } -2, \lambda_2 < \lambda_1 \Rightarrow \lambda_2 = -2$$

$$\lambda_1 = 4$$

L₁:
$$\frac{x-1}{0} = \frac{y-2}{0} = \frac{z-3}{1} = k$$
(4, -2, 7)



$$(3,-4,4-k)\perp\hat{k}$$

$$4-k=0 \Rightarrow k=4$$

 \Rightarrow Distance between (4, -2, 7) & (1, 2, 7)

$$\Rightarrow \sqrt{3^2 + 4^2} = 5$$

- 11. The radius of the smallest circle which touches the parabolas $y = x^2 + 2$ and $x = y^2 + 2$ is
 - (1) $\frac{7\sqrt{2}}{4}$
- (2) $\frac{7\sqrt{2}}{16}$
- (3) $\frac{7\sqrt{2}}{2}$
- (4) $\frac{7\sqrt{2}}{8}$

Answer (4)

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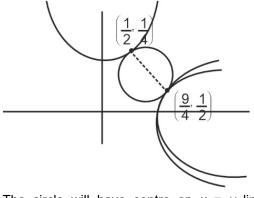
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Sol.



The circle will have centre on x = y line since parabolas are symmetric about y = x line

The slope of tangent at closest point $y^2 = x - 2$

$$\Rightarrow 2y \left(\frac{dy}{dx}\right) = 1 \Rightarrow y = \frac{1}{2} \Rightarrow \text{point will be } \left(\frac{9}{4}, \frac{1}{2}\right)$$

Similarly, on $x^2 = y - 2 \Rightarrow 2x = \frac{dy}{dx} = 1 \Rightarrow \left(\frac{1}{2}, \frac{9}{4}\right)$

$$2r = \sqrt{\left(\frac{9}{4} - \frac{1}{2}\right)^2 + \left(\frac{1}{2} - \frac{9}{4}\right)^2} = \sqrt{2}. \left|\frac{9}{4} - \frac{1}{2}\right|$$

$$=\frac{14}{8}\sqrt{2}=\frac{7\sqrt{2}}{4}$$

$$\Rightarrow r = \frac{7\sqrt{2}}{8}$$

- 12. The sum 1 + 3 + 11 + 25 + 45 + 71 +...upto 20 terms, is equal to
 - (1) 8124
- (2) 7240
- (3) 7130
- (4) 6982

Answer (2)

Sol. $T_r = 3r^2 - 7r + 5$ using second order difference

$$\sum_{r=1}^{20} (3r^2 - 7r + 5) = 3 \Sigma r^2 - 7\Sigma r + 5\Sigma(1)$$

$$=\frac{3(n)(n+1)(2n+1)}{6}-\frac{7n(n+1)}{2}-5n, n=20$$

$$= 7240$$

13. The number of solutions of the equation $2x + 3\tan x = \pi$,

$$x \in [-2\pi, 2\pi] - \left\{\pm \frac{\pi}{2}, \pm \frac{3\pi}{2}\right\}$$
 is:

(1) 5

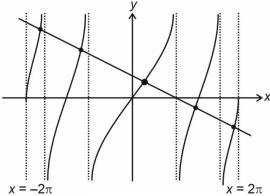
(3) 4

(4) 6

Answer (1)

Sol. $2x + 3\tan x = \pi$

$$\Rightarrow \tan x = \frac{\pi - 2x}{3}, x \in [-2\pi, 2\pi] - \left\{ \pm \frac{\pi}{2}, \pm \frac{3\pi}{2} \right\}$$



5 solutions

Let the domain of the function

$$f(x) = \log_2 \log_4 \log_6 (3 + 4x - x^2)$$
 be (a, b) . If $\int_0^{b-a} [x^2] dx = p - \sqrt{q} - \sqrt{r}$, $p, q, r \in \mathbb{N}$, $gcd(p, q, r) =$

1, where [] is the greatest integer function, then p + q + r is equal to

(1) 8

(2) 10

(3) 11

(4) 9

Answer (2)

Sol. $f(x) = \log_2(\log_4(\log_6(3 + 4x - x^2)))$

$$\log_4(\log_6(3 + 4x - x^2)) > 0$$

$$\Rightarrow \log_6(3 + 4x - x^2) > 1$$

$$\Rightarrow$$
 3 + 4x - x² > 6

$$\Rightarrow x^2 - 4x + 3 < 0$$

$$\Rightarrow$$
 $(x-1)(x-3)<0$

$$\Rightarrow x \in (1, 3)$$

$$a = 1 \ b = 3$$

$$\int_{1}^{2} [x^{2}] dx = \int_{1}^{\sqrt{2}} 1 dx + \int_{\sqrt{2}}^{\sqrt{3}} 2 dx + \int_{\sqrt{3}}^{2} 3 dx = 5 - \sqrt{2} - \sqrt{3}$$

$$p + q + r = 10$$

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99.99 Amogh Bansal

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15. If the domain of the function

$$f(x) = \log_e\left(\frac{2x-3}{5+4x}\right) + \sin^{-1}\left(\frac{4+3x}{2-x}\right)$$
 is $[\alpha, \beta)$, then

 α^2 + 4 β is equal to

(1) 3

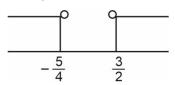
(2) 7

(3) 4

(4) 5

Answer (3)

Sol.
$$\frac{2x-3}{4x+5} > 0$$



$$\therefore x \in \left(-\infty, -\frac{5}{4}\right) \cup \left(\frac{3}{2}, \infty\right) \quad \dots (i)$$

$$-1 \le \frac{3x+4}{2-x} \le 1$$

$$\frac{3x+4}{2-x} \le 1$$

$$\Rightarrow \frac{3x+4}{2-x}-1\leq 0$$

$$\Rightarrow \frac{3x+4-2+x}{x-2} \ge 0$$

$$\Rightarrow \frac{4x+2}{x-2} \ge 0$$

$$\Rightarrow x \in \left(-\infty, -\frac{1}{2}\right] \cup (2, \infty)$$
 ...(ii)

$$\frac{3x+4}{2-x} \ge -1$$

$$\Rightarrow \frac{3x+4}{2-x}+1\geq 0$$

$$\Rightarrow \frac{3x+4+2-x}{2-x} \ge 0$$

$$\Rightarrow \frac{2x+6}{x-2} \le 0$$

 $\therefore x \in [-3, 2)$

...(iii)

Taking intersection of (i), (ii) and (iii)

$$x \in \left[-3, -\frac{5}{4}\right]$$

$$\alpha = -3, \, \beta = -\frac{5}{4}$$

$$\alpha^2 + 4\beta = 4$$

- 16. Let $f(x) = \int x^3 \sqrt{3 x^2} dx$. If $5f(\sqrt{2}) = -4$, then f(1)
 - (1) $-\frac{6\sqrt{2}}{5}$
- (2) $-\frac{4\sqrt{2}}{5}$
- (3) $-\frac{2\sqrt{2}}{5}$
- (4) $-\frac{8\sqrt{2}}{5}$

Answer (1)

Sol.
$$\int x^3 \sqrt{3-x^2} dx$$

$$3 - x^2 = t^2$$

$$-2xdx = 2tdt$$

$$= -\int t^2 (3 - t^2) dt = \int t^4 - 3t^2 dt$$

$$=\frac{t^5}{5}-t^3+c$$

$$f(x) = \frac{(3-x^2)^{\frac{5}{2}}}{5} - (3-x^2)^{\frac{3}{2}} + c$$

$$f(\sqrt{2}) = -\frac{4}{5}$$

$$\Rightarrow -\frac{4}{5} = \frac{1}{5} - 1 + c \Rightarrow c = 0$$

$$\therefore f(x) = \frac{(3-x^2)^{\frac{5}{2}}}{5} - (3-x^2)^{\frac{3}{2}}$$

Now
$$f(1) = \frac{2^{\frac{5}{2}}}{5} - 2^{\frac{3}{2}} = 2^{\frac{3}{2}} \left[\frac{2}{5} - 1 \right]$$

$$=2\sqrt{2}\left(-\frac{3}{5}\right)=-\frac{6}{5}\sqrt{2}$$

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AIR JEE (Adv.) 2020







- 17. Let a₁, a₂, a₃, ... be a G.P of increasing positive numbers. If $a_3a_5 = 729$ and $a_2 + a_4 = \frac{111}{4}$, then $24(a_1 + a_2 + a_3)$ is equal to
 - (1) 130
- (2) 131
- (3) 129
- (4) 128

Answer (3)

Sol.
$$a_2 + a_4 = \frac{111}{4}$$

$$a_3a_5 = 729$$

$$[ar^2][ar^4] = 729 = (27)^2$$

$$\Rightarrow$$
 ar³ = 27

$$\Rightarrow$$
 $a_4 = 27$

Now
$$a_2 = \frac{111}{4} - 27$$

$$a_2 = \frac{3}{4} = ar$$

$$r^2 = \frac{4 \times 27}{3} = 4 \times 9 = 36$$

$$\Rightarrow r = 6$$

(:: increasing GP)

$$a=\frac{1}{8}$$

Now $24[a_1 + a_2 + a_3] = 24[a + ar + ar^2]$

=
$$24 \times \frac{1}{8} [1 + r + r^2] = 3[1 + 6 + 6^2] = 3 \times 43 = 129$$

18. Let α and β be the roots of $x^2 + \sqrt{3}x - 16 = 0$, and γ and δ be the roots of $x^2 + 3x - 1 = 0$. If $P_n = \alpha^n + 1$ β^n and $Q^n = \gamma^n + \delta^n$, then $\frac{P_{25} + \sqrt{3}P_{24}}{2P_{23}} + \frac{Q_{25} - Q_{23}}{Q_{24}}$

is equal to

(1) 4

(3) 7

Answer (4)

Sol.
$$x^2 + 3x - 1 = 0$$
 $\Rightarrow \chi^2 - 1 = -3x$
 $\Rightarrow P^n = \gamma^n + \delta^n$
 $P_{25} - P_{23} = (\gamma^{25} - \gamma^{23}) + (\delta^{25} - \delta^{23})$
 $= \gamma^{23}(\gamma^2 - 1) + \delta^{23}(\delta^2 - 1)$
 $= \gamma^{23}(-3\gamma) + \delta^{23}(-3\delta) = -3[\gamma^{24} + \delta^{24}]$

$$\Rightarrow \frac{P_{25} - P_{23}}{P_{24}} = (-3)$$

$$x^{2} + \sqrt{3}x - 16 = 0 \Longrightarrow_{\beta}^{\alpha} Q_{n} = \alpha^{n} + \beta^{n}$$

$$\Rightarrow Q_{25} + \sqrt{3}Q_{24} = (\alpha^{25} + \sqrt{3}\alpha^{24}) + (\beta^{25} + \sqrt{3}\beta^{24})$$

$$= \alpha^{23}(\alpha^{2} + \sqrt{3}\alpha) + \beta^{23}(\beta^{2} + \sqrt{3}\beta)$$

$$= \alpha^{23}(16) + 16\beta^{23}$$

$$\Rightarrow \frac{Q_{25} + \sqrt{3}Q_{24}}{2 \cdot Q_{23}} = \frac{16(\alpha^{23} + \beta^{23})}{2(\alpha^{23} + \beta^{23})} = 8$$

$$\Rightarrow \frac{Q_{25} + \sqrt{3}Q_{24}}{2Q_{23}} + \frac{(P_{25} - P_{23})}{P_{24}} = 8 + (-3) = 5$$
19. Let *g* be a differentiable function such that

 $\int g(t)dt = x - \int tg(t)dt$, $x \ge 0$ and let y = y(x) satisfy

the differential equation $\frac{dy}{dx} - y \tan x = 2(x + 1) \sec x$

$$g(x), x \in \left[0, \frac{\pi}{2}\right]$$
. If $y(0) = 0$, then $y\left(\frac{\pi}{3}\right)$ is equal to

- (1) $\frac{2\pi}{3}$ (2) $\frac{4\pi}{3}$ (3) $\frac{2\pi}{3\sqrt{3}}$ (4) $\frac{4\pi}{3\sqrt{3}}$

Answer (2)

Sol.
$$\int_{0}^{x} g(t)dt = x - \int_{0}^{x} tg(t)dt$$

Differentiate both sides w.r.t x.

$$g(x) = 1 - xg(x)$$

$$g(x)(1+x)=1$$

$$g(x) = \frac{1}{1+x}$$

Now
$$\frac{dy}{dx} - y \tan x = 2(x+1)\sec xg(x)$$

$$LF = e^{-\int \tan x dx}$$

$$I.F = e^{-(-\ln\cos x)}$$

$$I.F = \cos x$$

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$$y.\cos x = \int 2(x+1)\sec x \cdot \frac{1}{(1+x)}\cos x dx$$

$$y\cos x = 2x + c$$

$$y(0) = 0$$

$$\Rightarrow$$
 $c = 0$

$$\therefore y\cos x = 2x$$

Put
$$x = \frac{\pi}{3}$$

$$\Rightarrow y\left(\frac{1}{2}\right) = \frac{2\pi}{3} \Rightarrow y = \frac{4\pi}{3}$$

20. If
$$y(x) = \begin{vmatrix} \sin x & \cos x & \sin x + \cos x + 1 \\ 27 & 28 & 27 \\ 1 & 1 & 1 \end{vmatrix}$$
, $x \in \mathbb{R}$

then
$$\frac{d^2y}{dx^2} + y$$
 is equal to

(1) 28

(2) 1

(3) -1

(4) 27

Answer (3)

Sol.
$$f(x) = \begin{vmatrix} \sin x & \cos x & \sin x + \cos x + 1 \\ 27 & 28 & 27 \\ 1 & 1 & 1 \end{vmatrix}$$

$$f(x) = \sin x(1) - \cos x(0) + (\sin x + \cos x + 1)(-1)$$

- $f(x) = \sin x \sin x \cos x 1$
- $f(x) = -\cos x 1$
- $f'(x) = \sin x$
- $f'(x) = \cos x$

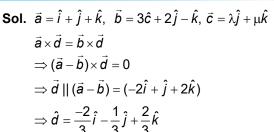
$$\Rightarrow f'(x) + f(x) = -\cos x - 1 + \cos x = -1$$

SECTION - B

Numerical Value Type Questions: This section contains 5 Numerical based questions. The answer to each question should be rounded-off to the nearest integer.

21. Let
$$\vec{a} = \hat{i} + \hat{j} + \hat{k}$$
, $\vec{b} = 3\hat{i} + 2\hat{j} - \hat{k}$, $\vec{c} = \lambda\hat{j} + \mu\hat{k}$ and \hat{d} be a unit vector such that $\vec{a} \times \hat{d} = \vec{b} \times \hat{d}$ and $\vec{c} \cdot \hat{d} = 1$. if \vec{c} is perpendicular to \vec{a} , then $\left| 3\lambda\hat{d} + \mu\vec{c} \right|^2$ is equal to _____

Answer (5)



Given $\hat{c} \cdot \hat{d} = 1$

$$\frac{-\lambda}{3} + \frac{2\mu}{3} = 1$$

$$\Rightarrow -\lambda + 2\mu = 3$$

Also \vec{a} is perpendicular to \vec{c}

$$\Rightarrow \vec{c} \cdot \vec{a} = 0$$

$$\Rightarrow \lambda + \mu = 0$$

$$\Rightarrow \lambda = -\mu$$

Put in (i)

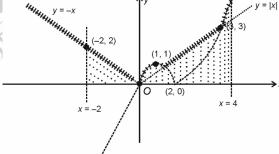
$$\mu + 2\mu = 3 \implies 3\mu = 3$$

$$\Rightarrow \mu = 1 \Rightarrow \lambda = -1$$

22. The area of the region bounded by the curve $y = \max\{|x|, x | x - 2|\}$, the x-axis and the lines x = -2 and x = 4 is equal to

Answer (12)

Sol.



Area =

$$\frac{1}{2} \times 2 \times 2 + \int_0^1 (2x - x^2) dx + \int_1^3 x dx + \int_3^4 (x^2 - 2x) dx$$

$$= 2 + \left[\frac{2x^2}{2} - \frac{x^3}{3} \right]_0^1 + \left[\frac{x^2}{2} \right]_1^3 + \left[\frac{x^3}{3} - \frac{2x^2}{2} \right]_0^4$$

= 12 square units

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23. Let the product of the focal distances of the point $P(4,2\sqrt{3})$ on the hyperbola $H: \frac{x^2}{a^2} - \frac{y^2}{b^2} = 1$ be 32. Let the length of the conjugate axis of H be p and the length of its latus rectum be q. Then $p^2 + q^2$ is equal to

Answer (120)

Sol.
$$P(4,2\sqrt{3})$$
 lies on $\frac{x^2}{a^2} - \frac{y^2}{b^2} = 1 \Rightarrow \frac{16}{a^2} - \frac{12}{b^2} = 1...(i)$

$$SP = e\left(4 - \frac{a}{e}\right), S'P = e\left(4 + \frac{a}{e}\right)$$

$$\Rightarrow$$
 SP · S'P = $16e^2 - a^2 = 32$

$$\because e^2 = 1 + \frac{b^2}{a^2}$$

$$\Rightarrow 16\left(1+\frac{b^2}{a^2}\right)-a^2=32 \qquad ...(ii)$$

From (i) and (ii), $a^2 = 8$, $b^2 = 12$

$$\Rightarrow : p^2 + q^2 = (2b)^2 + \left(\frac{2b^2}{9}\right)^2 = 4b^2 + \frac{4b^4}{a^2}$$

$$=48\left(1+\frac{12}{8}\right)=120$$

24. All five letter words are made using all the letters A. B, C, D, E and arranged as in an English dictionary with serial numbers. Let the word at serial number n be denoted by W_n . Let the probability $P(W_n)$ of choosing the word W_n satisfy $P(W_n) = 2P(W_n-1)$, *n* > 1.

If
$$P(CDBEA) = \frac{2^{\alpha}}{2^{\beta} - 1}$$
, $\alpha, \beta \in \mathbb{N}$, then $\alpha + \beta$ is equal to : ____

Answer (183)

Sol. We are given that the probability of choosing W_n

$$P(W_n) = 2P(W_{n-1})$$
 for $n > 1$

$$\Rightarrow P(W_1) = p, P(W_2) = 2p, P(W_3) = 4p, ..., P(W_n) = 2^{n-1}p$$

To find the value of p, we use:

$$\sum_{n=1}^{120} P(W_n) = 1 \text{ (total probability)}$$

So,
$$p(1+2+2^2+...+2^{119})=1$$

$$p(2^{120}-1)=1 \Rightarrow p=\frac{1}{2^{120}-1}$$

Thus,
$$P(W_n) = \frac{2^{n-1}}{2^{120} - 1}$$
 ...(i)

Since the first letter of CDBEA is C

Words starting with A: 4! = 24

Words starting with B: 4! = 24

Total before CDBEA = 63

Position of CDBEA = 64th

Putting in (i)

$$P(CDBEA) = P(W_{64}) = \frac{2^{63}}{2^{120} - 1}$$

Compare with the given form:

$$P(CDBEA) = \frac{2^{\alpha}}{2^{\beta} - 1}$$

So,
$$\alpha$$
 = 63, β = 120

$$\alpha$$
 + β = 63 +120 = 183

25. If the number of seven-digit numbers, such that the of their digits $m \cdot n \cdot 10^n$, $m, n \in \{1, 2, 3, ..., 9\}$, then m + n is equal

Answer (14)

Sol. When numbers are uniformly distributed, half of them have even digit sums and half have odd digits sums.

Number of 7-digit numbers with even digit sum =

$$\frac{1}{2} \cdot 9 \cdot 10^6 = 4.5 \cdot 10^6$$

Note that $9.5 \cdot 10^5 = 4.5 \cdot 10^6$

$$m + n = 9 + 5 = 14$$

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PHYSICS

SECTION - A

Multiple Choice Questions: This section contains 20 multiple choice questions. Each question has 4 choices (1), (2), (3) and (4), out of which **ONLY ONE** is correct.

Choose the correct answer:

26. Match the List-I with List-II

	List-I		List-II
A.	$ \begin{array}{l} 1 \\ 0 \\ 0 \\ 140 \\ 54 \end{array} Xe + \frac{94}{38}Sr + 2\frac{1}{0}n $	I.	Chemical reaction
B.	$2H_2 + O_2 \rightarrow 2H_2O$	II.	Fusion with +ve Q value
C.	$^{2}_{1}\text{H} + ^{2}_{1}\text{H} \rightarrow ^{3}_{2}\text{He} + ^{1}_{0}\text{n}$	III.	Fission
D.	$^{1}_{1}H + ^{3}_{1}H \rightarrow ^{2}_{1}H + ^{2}_{1}H$	IV.	Fusion with –ve Q value

Choose the **correct** answer from the options given below:

- (1) A-III, B-I, C-IV, D-II
- (2) A-II, B-I, C-IV, D-III
- (3) A-III, B-I, C-II, D-IV
- (4) A-II, B-I, C-III, D-IV

Answer (3)

Sol. (A) is fission reaction

- (B) is a chemical reaction
- (C) deuteron + deuteron → helium 3 is exothermic process
- (D) H + 3He → 2deuteron is endothermic process

- 27. A particle is released from height S above the surface of the earth. At certain height its kinetic energy is three times its potential energy. The height from the surface of the earth and the speed of the particle at that instant are respectively.
 - (1) $\frac{S}{2}$, $\sqrt{\frac{3gS}{2}}$
- $(2) \quad \frac{S}{4}, \sqrt{\frac{3gS}{2}}$
- (3) $\frac{S}{4}, \frac{3gS}{2}$
- (4) $\frac{S}{2}, \frac{3gS}{2}$

Answer (2)

Sol. PE = mgh

$$KE = mg(S - h)$$

given mg(S-h) = 3mgh

$$S = 4h$$

$$h = \frac{S}{4}$$

$$U = \sqrt{\frac{2g(3S)}{4}} = \sqrt{\frac{3gS}{2}}$$

- 28. Consider following statements for refraction of light through prism, when angle of deviation is minimum.
 - A. The refracted ray inside prism becomes parallel to the base.
 - B. Larger angle prisms provide smaller angle of minimum deviation.
 - C. Angle of incidence and angle of emergence becomes equal.
 - D. There are always two sets of angle of incidence for which deviation will be same except at minimum deviation setting.
 - E. Angle of refraction becomes double of prism angle.

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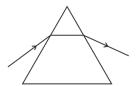
Choose the **correct** answer from the options given below:

- (1) A, B and E only
- (2) B, D and E only
- (3) B, C and D only
- (4) A, C and D only

Answer (4)

Sol. Because of symmetry where i = r, and $r = \frac{A}{2}$

$$\delta = (\mu - 1)A$$



- (A) is correct
- (B) is incorrect
- (C) is correct
- (D) is correct as $\delta = i + e A$
- (E) is incorrect
- 29. The radiation pressure exerted by a 450 W light source on a perfectly reflecting surface placed at 2 m away from it, is
 - (1) 1.5×10^{-8} Pascals (2) 0
 - (3) 3×10^{-8} Pascals (4) 6×10^{-8} Pascals

Answer (4)

Sol.
$$P = \frac{2I}{C}$$

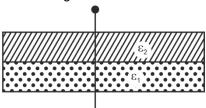
$$I = \frac{P}{A} = \frac{2 \times 450}{4 \pi \times 2^2}$$

$$Pressure = \frac{2 \times 450}{16\pi \times 3 \times 10^8}$$

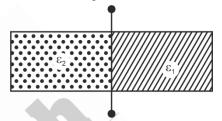
$$\approx 6 \times 10^{-8}$$

30. A parallel plate capacitor is filled equally (half) with two dielectrics of dielectric constants ϵ_1 and ϵ_2 , as shown in figures. The distance between the plates is d and area of each plate is A. If capacitance in first configuration and second configuration are C₁ and C_2 respectively, then $\frac{C_1}{C}$ is

First Configuration



Second Configuration



$$(1) \quad \frac{4\varepsilon_1\varepsilon_2}{\left(\varepsilon_1+\varepsilon_2\right)^2}$$

$$(2) \quad \frac{\varepsilon_0 \left(\varepsilon_1 + \varepsilon_2\right)}{2}$$

(3)
$$\frac{\varepsilon_1 \varepsilon_2}{\varepsilon_1 + \varepsilon_2}$$

$$(4) \ \frac{\varepsilon_1 \varepsilon_2^2}{\left(\varepsilon_1 + \varepsilon_2\right)^2}$$

Answer (1)

Sol.
$$C = \frac{k\epsilon_0 A}{d}$$

$$C_{1} = \frac{\varepsilon_{0}A}{\frac{d}{2\varepsilon_{1}} + \frac{d}{2\varepsilon_{2}}} = \frac{\varepsilon_{0}A}{d} \left\{ \frac{1}{\frac{\varepsilon_{2} + \varepsilon_{1}}{2\varepsilon_{1}\varepsilon_{2}}} \right\}$$

$$C_2 = \frac{\varepsilon_0}{d} \left(\varepsilon_1 \frac{A}{2} + \varepsilon_2 \frac{A}{2} \right) = \frac{\varepsilon_0 A}{d} \left\{ \frac{\varepsilon_1}{2} + \frac{\varepsilon_2}{2} \right\}$$

$$\frac{C_1}{C_2} = \frac{2\varepsilon_1\varepsilon_2}{(\varepsilon_2 + \varepsilon_1)\frac{(\varepsilon_1 + \varepsilon_2)}{2}} = \frac{4\varepsilon_1\varepsilon_2}{(\varepsilon_1 + \varepsilon_2)^2}$$

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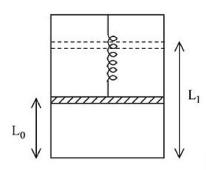








31. A piston of mass M is hung from a massless spring whose restoring force law goes as $F = -kx^3$, where k is the spring constant of appropriate dimension. The piston separates the vertical chamber into two parts, where the bottom part is filled with 'n' moles of an ideal gas. An external work is done on the gas isothermally (at a constant temperature T) with the help of a heating filament (with negligible volume) mounted in lower part of the chamber, so that the piston goes up from a height L_0 to L_1 , the total energy delivered by the filament is: (Assume spring to be in its natural length before heating)



(1)
$$nrT \ln \left(\frac{L_1}{L_0}\right) + Mg(L_1 - L_0) + \frac{k}{4}(L_1^4 - L_0^4)$$

(2)
$$3nrT \ln \left(\frac{L_1}{L_0}\right) + 2Mg(L_1 - L_0) + \frac{k}{3}(L_1^3 - L_0^3)$$

(3)
$$nrT \ln \left(\frac{L_1^2}{L_0^2}\right) + \frac{Mg}{2}(L_1 - L_0) + \frac{k}{4}(L_1^4 - L_0^4)$$

(4) $nrT \ln \left(\frac{L_1}{L_0}\right) + Mg(L_1 - L_0) + \frac{3k}{4}(L_1^4 - L_0^4)$

(4)
$$nrT \ln \left(\frac{L_1}{L_0}\right) + Mg(L_1 - L_0) + \frac{3k}{4}(L_1^4 - L_0^4)$$

Answer (None option matches)

Sol. From energy conservation

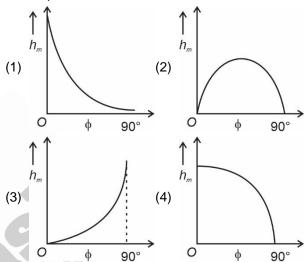
heat given = $(\Delta U + \Delta W)$ for gas + change in G.P.E. of piston + energy stored in spring

$$= 0 + \mu RT \ln \frac{V_2}{V_1} + Mg(h_2 - h_1) + \frac{1}{4}k(x_2^4 - x_1^4)$$

$$= nRT \ln \frac{L_1}{L_0} + Mg(L_1 - L_0) + \frac{1}{4}k(L_1 - L_0)^4$$

None option matches.

The angle of projection of a particle is measured from the vertical axis as of and the maximum height reached by the particle is h_m . Here h_m as function of ϕ can be presented as



Answer (4)

Sol.
$$h = \frac{u^2 \sin^2 \theta}{2g}$$
 $\theta = 90^\circ - \phi$

$$\Rightarrow h = \frac{u^2 \cos^2 \theta}{2g}$$

From $\phi = 0$ to $\phi = 90$

h decreases with cos² function.

- 33. A person measures mass of 3 different particles as 435.42 g, 226.3 g and 0.125 g. According to the rules for arithmetic operations with significant figures, the addition of the masses of 3 particles will be
 - (1) 661.8 g
- (2) 661.84 g
- (3) 662 g
- (4) 661.845 g

Answer (1)

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Sol. 435.42

226.3

0.125

661.845

For addition, minimum decimal number is considered for reporting the measured value

- ⇒ 661.8
- 34. During the melting of a slab of ice at 273 K at atmospheric pressure:
 - (1) Internal energy of ice-water system remains unchanged
 - (2) Internal energy of the ice-water system decreases
 - (3) Positive work is done by the ice-water system on the atmosphere
 - (4) Positive work is done on the ice-water system by the atmosphere

Answer (4)

Sol. Melting of ice requires heat therefore internal energy increases.

But because of decrease in volume the work done on atmosphere is negative or atmosphere does positive work on ice-water system.

- 35. The work function of a metal is 3 eV. The color of the visible light that is required to cause emission of photoelectrons is
 - (1) Red
- (2) Yellow
- (3) Green
- (4) Blue

Answer (4)

Sol.
$$\lambda = \frac{12400}{3} \text{ Å} = 4133 \text{ Å}$$

and
$$\lambda_{\text{visible}} \in (3800 - 7600) \text{ Å}$$

Therefore, most appropriate response is blue.

36. Match the List-I with List-II

	List-I		List-II
A.	Gravitational constant	I.	[LT ⁻²]
В.	Gravitational potential energy	II.	[L ² T ⁻²]
C.	Gravitational potential	III.	[ML ² T ⁻²]
D.	Acceleration due to gravity	IV.	[M ⁻¹ L ³ T ⁻²]

Choose the **correct** answer from the options given below:

- (1) A-II, B-IV, C-III, D-I
- (2) A-IV, B-III, C-II, D-I
- (3) A-I, B-III, C-IV, D-II
- (4) A-III, B-II, C-I, D-IV

Answer (2)

Sol. (A)
$$F = \frac{Gm^2}{r^2} \equiv G = \frac{Fr^2}{m^2} \equiv \frac{MLT^{-2}L^2}{M^2} = M^{-1}L^3T^{-2}$$

$$A \rightarrow IV$$

(B)
$$G.P E \equiv \text{Energy} \equiv ML^2T^{-2}$$

$$B \rightarrow III$$

(C)
$$G.P = \frac{mgh}{m} = gh = V^2 = L^2T^{-2}$$

$$C \rightarrow II$$

(D)
$$g \equiv LT^{-2}$$

 $D \rightarrow I$

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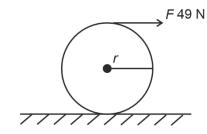
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37. A force of 49 N acts tangentially at the highest point of a sphere (solid) of mass 20 kg, kept on a rough horizontal plane. If the sphere rolls without slipping, then the acceleration of the center of the sphere is



- (1) 2.5 m/s²
- (2) 0.25 m/s²
- (3) 3.5 m/s²
- (4) 0.35 m/s²

Answer (3)

Sol.
$$\tau = I\alpha \Rightarrow 49 \times 2r = \frac{7}{5}mr^2\alpha$$

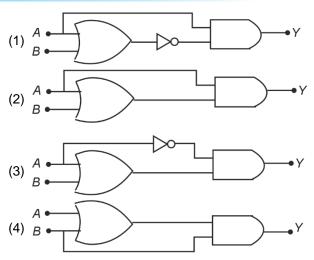
$$49 \times 2r = \frac{7}{5} mr a$$

$$\frac{49 \times 2 \times 5}{7 \times 20} = a$$

 $a = 3.5 \text{ m/s}^2$

38. Choose the correct logic circuit for the given truth table having inputs *A* and *B*.

Inputs		Output
А	В	Υ
0	0	0
0	1	0
1	0	1
1	1	1



Answer (2)

Sol. Option (1) =
$$(\overline{A+B}) \cdot A$$

$$=(\overline{A}+\overline{B})\cdot A\equiv 0$$

Option (2) =
$$(A + B) \cdot A$$

$$A \cdot A + A \cdot B = A$$

Option (3)
$$(A+B)\cdot \overline{A}$$

$$A \cdot \overline{A} + \overline{A} \cdot B = \overline{A}B$$

Option (4)

$$(A + B) \cdot (B)$$

$$A \cdot B + B \cdot B = B$$

- ⇒ option 2 matches the truth table
- 39. The electrostatic potential on the surface of uniformly charged spherical shell of radius R = 10 cm is 120 V. The potential at the centre of shell, at a distance r = 5 cm from centre, and at a distance r = 15 cm from the centre of the shell respectively, are:
 - (1) 120V, 120V, 80V
- (2) 40V, 40V, 80V
- (3) 0V, 120V, 40V
- (4) 0V, 0V, 80V

Answer (1)

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Sol. For
$$r \le R$$
 $V = \frac{kQ}{R}$

For
$$r > R$$
 $V = \frac{kQ}{r}$

(i) For r = 0 and r = 5 cm

$$(< R = 10 \text{ cm})$$

$$V = 120 \text{ V}$$

(ii) For
$$r = 15$$
 cm $V = \frac{kQ}{R} \frac{R}{r}$

$$= 120 \times \frac{10}{15}$$

$$= 80 \text{ V}$$

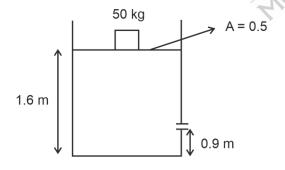
40. Consider a completely full cylindrical water tank of height 1.6 m and of cross-sectional area 0.5 m². It has a small hole in its side at a height 90 cm from the bottom. Assume, the cross-sectional area of the hole to be negligibly small as compared to that of the water tank. If a load 50 kg is applied at the top surface of the water in the tank then the velocity of the water coming out at the instant when the hole is opened is:

$$(g = 10 \text{ m/s}^2)$$

- (1) 3 m/s
- (2) 2 m/s
- (3) 5 m/s
- (4) 4 m/s

Answer (4)

Sol.



$$\Delta P = \frac{1}{2}\rho v^2$$

$$\frac{mg}{A} + \rho g \Delta h = \frac{1}{2} \rho v^2$$

$$\frac{500}{0.5} + 10^3 \times 10 \times 0.7 = \frac{1}{2} \times 10^3 v^2$$

$$1 + 7 = \frac{1}{2}v^2$$

$$v = 4 \text{ m/s}$$

41. A gas is kept in a container having walls which are thermally non-conducting. Initially the gas has a volume of 800 cm³ and temperature 27°C. The change in temperature when the gas is adiabatically compressed to 200 cm3 is:

(Take $\gamma = 1.5$; γ is the ratio of specific heats at constant pressure and at constant volume)

- (1) 300 K
- (3) 327 K (4) 600 P

Answer (1)

Sol. Being adiabatic process PV' = constant, where $\gamma =$ 1.5 and also TV^{r-1} = constant

$$300\{800\}^{0.5} = T\{200\}^{0.5}$$

$$T = 300 \times 2 = 600 \text{ K}$$

$$\Delta T = 600 - 300 = 300 \text{ K}$$

42. Two blocks of masses m and M, (M > m) are placed on a frictionless table as shown in figure. A massless spring with spring constant k is attached with the lower block. If the system is slightly displaced and released, then

 $(\mu = \text{coefficient of friction between the two blocks})$

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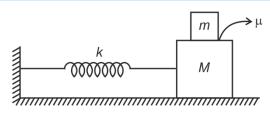












- A. The time period of small oscillation of the two blocks is $T = 2\pi \sqrt{\frac{(m+M)}{k}}$
- B. The acceleration of the blocks is $a = -\frac{kx}{M+m}$ (x = displacement of the blocks from the mean position)
- C. The magnitude of the frictional force on the upper block is $\frac{m\mu|x|}{M+m}$
- D. The maximum amplitude of the upper block, if it does not slip, is $\frac{\mu(M+m)g}{k}$
- E. Maximum frictional force can be $\mu(M+m)g$ Choose the **correct** answer from the options given below :
- (1) B, C, D only
- (2) A, B, C only
- (3) A, B, D only
- (4) C, D, E only

Answer (3)

- **Sol.** A. Assuming no slipping, $T = 2\pi \sqrt{\frac{m_{\text{total}}}{k}}$ A is correct.
 - B. Assuming no slipping, $a = \frac{|F|}{m}$ B is correct.
 - C. $f = (m)(a) = \frac{m \times kx}{m+M}$

C is correct.

D. For no slipping $\frac{kx_0}{m+M} \le \mu g$

D is correct.

E. $f_{\text{max}} = \mu \, mg$

E is incorrect.

- 43. The radii of curvature for a thin convex lens are 10 cm and 15 cm respectively. The focal length of the lens is 12 cm. The refractive index of the lens material is
 - (1) 1.5
- (2) 1.2
- (3) 1.4
- (4) 1.8

Answer (1)

Sol. For biconvex

$$R_1 = 10$$

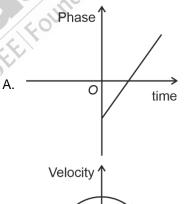
$$R_2 = 15$$

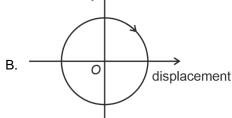
$$\frac{1}{f} = \left(\mu - 1\right) \left(\frac{1}{R_1} + \frac{1}{R_2}\right)$$

$$\frac{1}{12} = \left(\mu - 1\right) \left(\frac{1}{10} + \frac{1}{15}\right) = \left(\mu - 1\right) \left(\frac{1}{6}\right)$$

$$\mu - 1 = \frac{1}{2} \Rightarrow \mu = 1.5$$

44. Which of the following curves possibly represent onedimensional motion of a particle?





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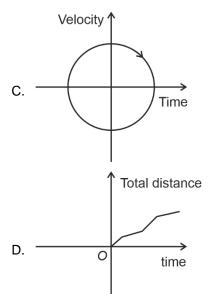
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Choose the **correct** answer from the options given below:

- (1) A and B only
- (2) A, C and D only
- (3) A, B and C only (4) A, B and D only

Answer (4)

Sol. A. Phase increase with time in SHM

- Correct
- B. Velocity and displacement are related in elliptical/circular relation

i.e.
$$\frac{v^2}{v_0^2} + \frac{x^2}{x_0^2} = 1$$

- Correct
- C. At same time particle can't have two velocities

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- Incorrect
- D. Distance always increases
 - Correct

- 45. A wire of length 25 m and cross-sectional area 5 mm² having resistivity 2 x $10^{-6} \Omega$ m is bent into a complete circle. The resistance between diametrically opposite points will be
 - (1) 100Ω

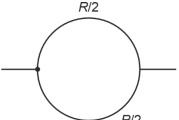
(2) 50Ω

(3) 12.5Ω

(4) 25Ω

Answer (None matches the options)

Sol.



Let R be total resistance across ends of wire, then

$$R_{\text{eq}} = \frac{R}{4} = \frac{\rho \ell}{4A} = \frac{2 \times 10^{-6} \times 25}{4 \times 5 \times 10^{-6}}$$

 $= 2.5 \Omega$

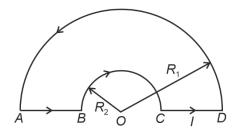
None matches the options.

SECTION - B

Numerical Value Type Questions: This section contains 5 Numerical based questions. The answer to each question should be rounded-off to the nearest integer.

46. A loop ABCDA, carrying current I = 12 A, is placed in a plane, consists of two semi-circular segments of radius $R_1 = 6\pi$ m and $R_2 = 4\pi$ m. The magnitude of the resultant magnetic field at center O is $k \times 10^{-7}$ T. The value of k is _

(Given $\mu_0 = 4\pi \times 10^{-7} \text{ Tm A}^{-1}$)



Answer (1)

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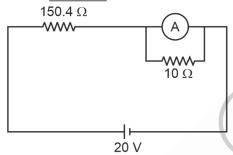


Sol.
$$B = \frac{\mu_0 I}{2r} \frac{\theta}{2\pi}$$
 for an arc

For semicircle
$$B = \frac{\mu_0 I}{4r}$$

$$B_{\text{het}} = \frac{\mu_0 I}{4\{4\pi\}} - \frac{\mu_0 I}{4\{6\pi\}}$$
$$= \frac{4_0 I}{4\pi} \left\{ \frac{1}{4} - \frac{1}{6} \right\}$$
$$= 10^{-7} \times 12 \times \frac{2}{24} = 10^{-7} \text{T} \Rightarrow k = 1$$

47. In the figure shown below, a resistance of 150.4 Ω is connected in series to an ammeter A of resistance 240 Ω . A shunt resistance of 10 Ω is connected in parallel with the ammeter. The reading of the ammeter is



Answer (5)

Sol.
$$i_0 = \frac{20}{150.4 + \frac{240 \times 10}{250}}$$

= $\frac{20}{150.4 + 9.6} = \frac{20}{160} = \frac{1}{8}$ A
 $i_A = \frac{1}{8} \times \frac{10}{250} \times 1000$ mA

48. Three identical spheres of mass m, are placed at the vertices of an equilateral triangle of length a. When released, they interact only through gravitational force and collide after a time T = 4 seconds. If the sides of the triangle are increased to length 2a and also the masses of the spheres are made 2m, then they will collide after seconds.

Answer (8)

Sol. As limiting case of elliptical path is straight line therefore proportionality $T^2 \propto \frac{a^3}{M}$ will holds from

$$\left(T^2 = \frac{4\pi^2}{GM}r^3\right)$$

$$\frac{4^2}{T^2} = \frac{a^3}{m} \frac{2m}{(2a)^3} = \frac{2}{8} = \frac{1}{4}$$

$$\frac{4}{T} = \frac{1}{2}$$

T = 8 seconds

49. Two coherent monochromatic light beams of intensities 41 and 91 are superimposed. The difference between the maximum and minimum intensities in the resulting interference pattern is xl. The value of x is

Answer (24)

Sol.
$$I_{\text{max}} = \left(\sqrt{4I} + \sqrt{9I}\right)^2 = 25I$$

$$I_{\min} = \left(\sqrt{4I} - \sqrt{9I}\right)^2 = I$$

$$\Delta I = 24I$$

50. A 4.0 cm long straight wire carrying a current of 8 A is placed perpendicular to a uniform magnetic field of strength 0.15 T. The magnetic force on the wire is mN.

Answer (48)

Sol.
$$F = i / B$$

$$= 8 \times 4 \times 10^{-2} \times 0.15$$
 newton

$$= 8 \times 4 \times 10^{-2} \times 0.15 \times 10^{3} \text{ mN}$$

$$= 32 \times 1.5 \text{ mN}$$

= 48 mN

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CHEMISTRY

SECTION - A

Multiple Choice Questions: This section contains 20 multiple choice questions. Each question has 4 choices (1), (2), (3) and (4), out of which **ONLY ONE** is correct.

Choose the correct answer:

51. 2 moles each of ethylene glycol and glucose are dissolved in 500 g of water. The boiling point of the resulting solution is:

(Given : Ebullioscopic constant of water = 0.52 K kg mol⁻¹)

- (1) 377.3 K
- (2) 375.3 K
- (3) 379.2 K
- (4) 277.3 K

Answer (1)

Sol. $\Delta T_b = K_b(m)$

$$= \left(0.52\right) \! \left(\frac{4}{0.5}\right)$$

- = (0.52)(8)
- = 4.16 K

 $T_b = 373.15 + 4.16$

= 377.3 K

52. Which compound would give 3-methyl-6-oxoheptanal upon ozonolysis?

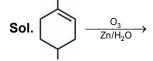


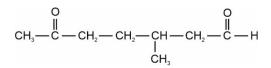






Answer (3)





3-methyl-6-oxoheptanal

53. In the following reactions, which one is NOT correct?

(1)
$$N = NCI^{\ominus}$$

$$EtOH$$

$$OEt$$

(2)
$$\stackrel{\oplus}{N} = NC1^{\ominus}$$

$$\stackrel{CuCN/KCN}{\longrightarrow}$$

$$(3) \qquad \stackrel{\oplus}{\stackrel{N=NC1}{\longrightarrow}} NC1^{\ominus}$$
Potassium Iodide
$$I = I$$

Answer (1)

Sol. N₂*CI⁻

Option (1) is incorrect

54. Among 10⁻⁹ g (each) of the following elements, which one will have the highest number of atoms?

Element: Pb, Po, Pr and Pt

(1) Po

(2) Pb

- (3) Pt
- (4) Pr

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Answer (4)

- **Sol.** Highest atoms in case where atomic mass is lowest
 - Po = 209
 - Pb = 207
 - Pt = 195
 - Pr = 140
- 55. Correct order of limiting molar conductivity for cations in water at 298 K is :
 - (1) $H^+ > Na^+ > K^+ > Ca^{2+} > Mg^{2+}$
 - (2) $Mg^{2+} > H^+ > Ca^{2+} > K^+ > Na^+$
 - (3) $H^+ > Ca^{2+} > Mg^{2+} > K^+ > Na^+$
 - (4) $H^+ > Na^+ > Ca^{2+} > Mg^{2+} > K^+$

Answer (3)

- **Sol.** λ_m^0 order
 - $H^+ > Ca^{2+} > Mg^{2+} > K^+ > Na^+$
- 56. Which of the following postulate of Bohr's model of hydrogen atom is not in agreement with quantum mechanical model of an atom?
 - (1) The electron in a H atom's stationary state moves in a circle around the nucleus
 - (2) An atom in a stationary state does not emit electromagnetic radiation as long as it stays in the same state.
 - (3) When an electron makes a transition from a higher energy stationary state to a lower energy stationary state, then it emits a photon of light.
 - (4) An atom can take only certain distinct energies E₁, E₂, E₃, etc. These allowed states of constant energy are called the stationary states of atom.

Answer (1)

Sol. The electron in a H-atom's stationary state moves in a circle around the nucleus. This is not in agreement with Quantum Mechanical model of an atom.

- 57. Number of molecules from below which cannot give iodoform reaction is:
 - Ethanol, Isopropyl alcohol, Bromoacetone, 2-Butanol, 2-Butanone, Butanal, 2-Pentanone, 3-Pentanone, Pentanal and 3-Pentanol.
 - (1) 2

(2) 5

(3) 3

(4) 4

Answer (4)

- **Sol.** The compounds which doesn't give iodoform test are
 - Butanal, 3-pentanone, pentanal, 3-pentanol
- 58. Given below are two statements:
 - **Statement (I)**: A catalyst cannot alter the equilibrium constant (K_C) of the reaction, temperature remaining constant.
 - **Statement (II)**: A homogenous catalyst can change the equilibrium composition of a system, temperature remaining constant.
 - In the light of the above statements, choose the **correct** answer from the options given below.
 - (1) Both Statement-I and Statement-II are false
 - (2) Both Statement-I and Statement-II are true
 - (3) Statement-I is true but Statement-II is false
 - (4) Statement-I is false but Statement-II is true

Answer (3)

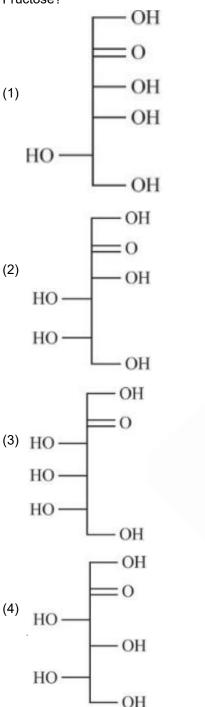
Sol. Catalyst doesn't change K_{eq} catalyst doesn't change composition statement-I is true But statement-II is false.



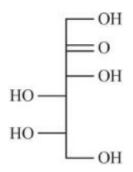


Answer (2)

59. Which of the following is the correct structure of L-Fructose?



Sol.



60. Match the LIST-I with LIST-II

		LIST-I (Molecules/ion)		LIST-II (Hybridisation of central atmn)
	A.	PF ₅	I.	dsp ²
	B.	SF ₆	II.	sp³d
	C.	Ni(CO) ₄	III.	sp³d²
	D.	[PtCl ₄] ²⁻	IV.	sp ³

Choose the *correct* answer from the options given below:

- (1) A-III, B-I, C-IV, D-II (2) A-II, B-III, C-IV, D-I
- (3) A-I, B-II, C-III, D-IV (4) A-IV, B-I, C-II, D-III

Answer (2)

- **Sol.** (A) $PF_5 sp^3d$ (II)
- (B) $SF_6 sp^3d^2$ (III)
- (C) $Ni(CO)_4 sp^3(IV)$
- (D) $[PtCl_4]^{2-} dsp^2(I)$
- 61. In the following system, PCl₅(g) ⇒ PCl₃(g) + Cl₂(g) at equilibrium, upon addition of xenon gas at constant T & p, the concentration of
 - (1) Cl₂ will decrease
 - (2) PCl₃ will increase
 - (3) PCI₅ will increase
 - (4) PCl₅, PCl₃ & Cl₂ remain constant

Answer (2)

Sol. According to Le-Chatelier's principle

Reaction will shift in forward direction.

Cl₂ will increase

PCl₃ will increase

PCI₅ will decrease

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62. Identify the correct statements from the following.



D.
$$NH_2$$
 and NH

are homologous

Choose the *correct* answer from the options given below:

- (1) A, B & C Only
- (2) B & C Only
- (3) A & B Only
- (4) C & D Only

Answer (3)

- **Sol.** A and B are correct. C ⇒ Homologous
- 63. In a reaction A + B \rightarrow C, initial concentrations of A and B are related as $[A]_0 = 8[B]_0$. The half lives of A and B are 10 min and 40 min, respectively, If they start to disappear at the same time, both following first order kinetics, after how much time will the concentration of both the reactants be same?
 - (1) 40 min
- (2) 20 min
- (3) 80 min
- (4) 60 min

Answer (1)

$$\textbf{Sol.} \ \ \underset{8B_0}{A} \xrightarrow{10} 4B_0 \xrightarrow{10} 2B_0 \xrightarrow{10} B_0 \xrightarrow{10} \frac{B_0}{2}$$

$$B_{B_0} \xrightarrow{40} \frac{B_0}{2}$$

t = 40

64. The least acidic compound, among the following is

EiO OH SO
$$_3$$
H COOH EiO $_2$ C $=$ H

(1) A

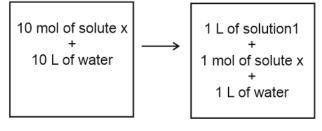
(2) D

(3) C

(4) B

Answer (2)

- **Sol.** Terminal alkyne is least Acidic among given compound
- 65. Which of the following properties will change when system containing solution 1 will become solution 2



(Solution 1)

(Solution 2)

- (1) Density
- (2) Concentration
- (3) Gibbs free energy
- (4) Mol heat capacity

Answer (3)

- **Sol.** Gibbs free energy will change.
- 66. The metal ions that have the calculated spin only magnetic moment value of 4.9 B.M. are
 - A. Cr²⁺
- B Fe²⁺
- C. Fe3+
- D. Co2+
- E. Mn³⁺

Choose the correct answer from the options given below:

- (1) B and E only
- (2) A, B and E only
- (3) A, D and E only
- (4) A, C and E only

Answer (2)

Sol. $\mu = 4.9 \text{ BM}$

n = 4 for Cr^{2+} ; Fe^{2+} ; Mn^{3+} (where n = unpairedelectron)

67. Given below are two statements:

Statement I: The N – N single bond is weaker and longer than that of P – P single bond.

Statement II: Compounds of group 15 elements in + 3 oxidation states readily undergo disproportionation reactions.

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In the light of the above statements, choose the correct answer from the options given below

- (1) Statement I is false but Statement II is true
- (2) Statement I is true but Statement II is false
- (3) Both Statement I and Statement II are true
- (4) Both Statement I and Statement II are false

Answer (4)

Sol. Bond energy : (N - N) < (P - P)

Bond length : (N - N) < (P - P)

Statement-I is false.

Not all elements of Group-15 undergo disproportionation reaction.

Statement-II is false.

- 68. Which of the following statements are correct?
 - A. The process of adding an electron to a neutral gaseous atom is always exothermic.
 - B. The process of removing an electron from an isolated gaseous atom is always endothermic.
 - C. The 1st ionization energy of boron is less than that of beryllium.
 - D. The electronegativity of C is 2.5 in CH₄ and CCl₄
 - E. Li is the most electropositive among elements of group I.

Choose the correct answer from the options given below:

- (1) B and D Only
- (2) B, C and E Only
- (3) A, C and D Only
- (4) B and C Only

Answer (4)

Sol. B and C are correct

IE:B<Be

- 69. The correct order of the complexes $[\text{Co}(\text{NH}_3)_5(\text{H}_2\text{O})]^{3+} \text{ (A), } [\text{Co}(\text{NH}_3)_6]^{3+} \text{ (B), } [\text{Co}(\text{CN})_6]^{3-}$ (C) and $[\text{CoCl}(\text{NH}_3)_5]^{2+} \text{ (D) in terms of wavelength of light absorbed is}$
 - (1) C > B > A > D
- (2) D > C > B > A
- (3) C > B > D > A

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(4) D > A > B > C

Answer (4)

Sol. D > A > B > C

$$\Delta_o = \frac{hc}{\lambda}$$

More the value of Δ_0 more energy will be obseved Δ_0 increases and λ decreases.

70. Identify [A], [B] and [C], respectively in the following reaction sequence:

[A]
$$\xrightarrow{\text{NaNO}_{2r} \text{HCl}}$$
 $\xrightarrow{\text{NaNO}_{2r} \text{HCl}}$ $\xrightarrow{\text{NH}_2}$ $\xrightarrow{\text{NN}_2 \text{Cl}}$ \xrightarrow

Answer (4)

Sol.

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SECTION - B

Numerical Value Type Questions: This section contains 5 Numerical based questions. The answer to each question should be rounded-off to the nearest integer.

71. The number of optical isomers exhibited by the iron complex (A) obtained from the following reaction is

FeCl₃ + KOH +
$$H_2C_2O_4 \rightarrow A$$

Answer (2)

Sol. Complex obtained is $[Fe(C_2O_4)_3]^{3-}$ Total isomers = 2 (d/l form)

72. During estimation of nitrogen by Dumas' method of compound X (0.42 g)



____ mL of N₂ gas will be liberated at STP. (nearest integer)

(Given molar mass in g mol-1 : C : 12, H : 1, N : 14)

Answer (109)

Sol. Formula of compound = $C_4H_{10}N_2$

= 86

Moles of compound = 0.00488

Moles of $N_2 = 0.00488$

Volume of $N_2 = 0.1093 L$

= 109.3 mL

Nearest integer = 109

73. Given:

 $\Delta H_{\text{sub}}^{\Theta}[C(\text{graphite})] = 710 \text{ kJ mol}^{-1}$

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 $\Delta_{C-H}H^{\Theta} = 414 \text{ kJ mol}^{-1}$

 $\Delta_{H_-H}H^{\Theta} = 436 \text{ kJ mol}^{-1}$

 $\Delta_{C-C}H^{\Theta} = 611 \text{ kJ mol}^{-1}$

The ΔH_f^{Θ} for $CH_2 = CH_2$ is ____ kJ mol⁻¹ (nearest integer value)

Answer (25)

Sol. $\Delta H_r^{\Theta} = 2(710) + 2 \times 436 - 611 - 4(414)$

= 1420 + 872 - 611 - 1656

= 25 kJ mole⁻¹

74. 0.5 g of an organic compound on combustion gave 1.46 g of CO₂ and 0.9 g of H₂O. The percentage of carbon in the compound is _____. (Nearest integer)

[Given : Molar mass (in g mol $^{-1}$) C : 12, H : 1, O : 16]

Answer (80)

Sol. Mass of C = $\frac{1.46}{44} \times 12 = 0.398 \text{ g}$

% by mass of $C = \frac{0.398}{0.5} \times 100$

= 79.63%

Nearest integer = 80

75. Consider the following reactions

 $\begin{array}{c} {\rm A} + {\rm NaCl} + {\rm H_2SO_4} \rightarrow {\rm CrO_2Cl_2} + {\rm Side\ Products} \\ {\rm Little} \\ {\rm amount} \end{array}$

CrO₂Cl_{2(Vapour)} + NaOH → B + NaCl + H₂O

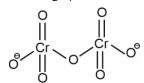
 $B + H^+ \rightarrow C + H_2O$

The number of terminal 'O' present in the compound 'C' is _____.

Answer (6)

Sol. B : CrO_4^{2-}

 $C : Cr_2O_7^{2-}$



Terminal oxygen atoms = 6

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