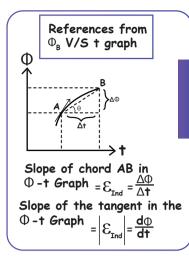
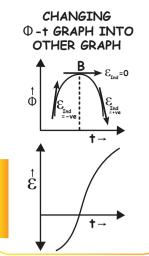


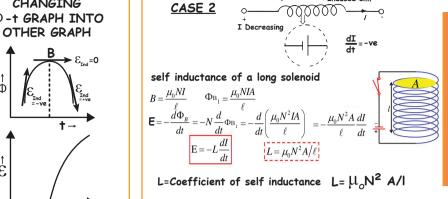
FARADAY'S LAW

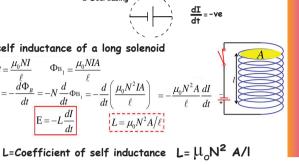
- 1) Whenever the amount of magnetic flux linked with a circuit changes, an emf is induced in the circuit 2) The induced EMF is given by rate of change of magnetic flux linked with the circuit $\mathcal{E}_{\text{Ind}} = -\frac{d\Phi_{\text{B}}}{dt}$
- Negative sign indicates that induced emf opposes the cause of flux change



ELECTROMAGNETIC







Unit of inductance: Henry [H] $=[ML^2T^{-2}A^{-2}]$

M is called as mutual inductance of the coils. $L = \mu_0 n^2 AI$

EMF induced.

 $\phi_{\rm g} \propto I$

currents I_1 and I_2 .

$$\mathcal{E}_{B} = -\frac{dt}{dt}$$

$$\Rightarrow$$
 $\varepsilon_{\rm B}$ =- $M \frac{{\sf dI}_{1}}{{\sf dt}}$

 $\phi_{\lambda} \propto I_{\lambda}$

 $\Rightarrow \phi_{\star} = MI_{\circ}$

MUTUAL INDUCTANCE

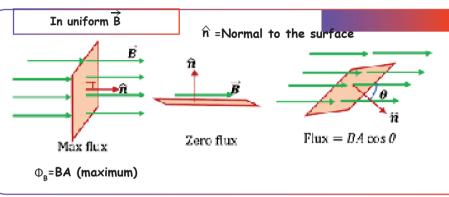
Change in current in one coil causes change

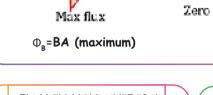
in flux in another coil and vice versa.

Let there be two coils A and B, having

$$\mathcal{E}_A = -\frac{d\phi}{dt}$$

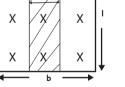
$$\Rightarrow$$
 $\epsilon_{A} = -M \frac{dI_{2}}{dt}$



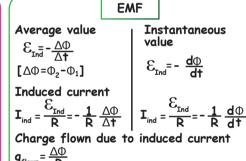




1) Steps of solving В /dx/ Χ



- 1. Take a small strip 'dx'
- 2. flux d⊕ =BdA [dA=ldx]
- 3. Total flux $\Phi = \int d\Phi = \int BdA$ =∫Bldx



Charge flown due to induced current depends only on change in flux

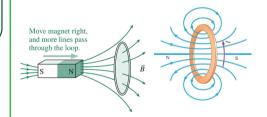
LENZ'S LAW & CONSERVATION OF ENERGY

INDUCTION

The direction of any induced magnetic effect is such as to oppose the change that produces it

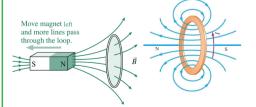
DIRECTION OF INDUCED **CURRENT**

- 1. If flux is decreasing, the magnetic field due to induced current will be along the existing magnetic field
- 2. If flux is increasing, the magnetic field due to induced current will be opposite to existing magnetic field



Field causing flux change

Induced Field



Field causing flux change

Induced Field

Self Inductance £ 1000000000 £

- Scalar quantity - Unit of inductance (H)

Inductance

- Dimension : ML2T-2A-2

Current I in the coil changes due to external source

INDUCTANCE

INDUCTANCE

Mutual

Inductance

Causes change in magnetic field inside

Results in change in magnetic flux inside the coil

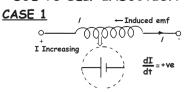
EMF is induced which opposes the changing magnetic flux

Creates an induced current which is opposing in nature

E=-LdI dt

where, L= Self Inductance I = Current in the coil

NATURE OF INDUCED CURRENT DUE TO SELF INDUCTION

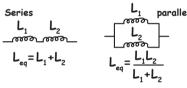


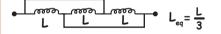
ENERGY STORED IN INDUCTOR $U_{R} = \frac{1}{2} LI^{2}$

MAGNETIC ENERGY STORED PER UNIT VOLUME ENERGY DENSITY

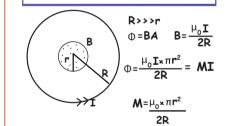
$$u = \frac{U_B}{V} = \frac{U_B}{AI} = \frac{\mu_O n^2 I^2}{2} = \frac{B^2}{2\mu_O}$$

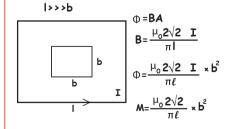
SERIES & PARALLEL COMBINATION OF INDUCTORS

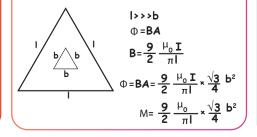




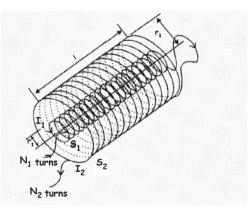
MUTUAL INDUCTANCE OF SOME STANDARD CASES







MUTUAL INDUCTANCE OF TWO CO-AXIAL SOLENOIDS



 I_2 = Current through outer coil

$$B = \mu_0 n_2 I_2$$

$$\Phi_{12} = \mu_0 n_2 I_2 \times \pi r_1^2 n_1 I$$

$$M = M_{12} = \mu_0 n_1 n_2 \times \pi r_1^2 |$$

$$= \frac{\mu_0 N_1 N_2}{r_1^2} \pi r_1^2$$



Relation between mutual inductance & self inductance

$$M=K \int_{1}^{\infty} L_{1}L_{2} \quad 0 \leq K \leq 1$$

K→coefficient of coupling If K=1, Perfect flux linkage



Otherwise → imperfect linkage

change of area in magnetic field region

 $A \longrightarrow A_1 \longrightarrow Area$ increases, current will be anticlockwise

 $A \rightarrow A_2 \rightarrow$ Area decreases, current will be

clockwise

() = BA

 $\triangle \Phi = B \triangle A$

- If K=0 no linkage
- ⇒M=0

DYNAMIC MOTIONAL EMF DUE TO TRANSLATORY MOTION

- Charges accumulate at the ends of the conductor due to its movement in external magnetic field
- · This separation of charges at the ends of the conductor causes a voltage difference

At steady state



Direction to find the positive terminal By using right hand rule,

Thumb - velocity

Fingers - Magnetic field Palm - Positive terminal of the rod

Modification

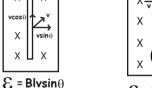
ii) Conductor of arbitrary shape

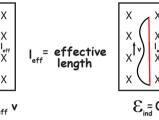
i) Velocity is not perpendicular

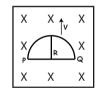
v Perpendicular to effective length

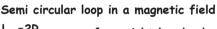
v Parallel to effective length











I_{eff}=2R S=Bletta E=Bx2Rv

from right hand rule, P is at higher potential Q is at lower potential

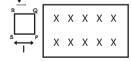
MOTIONAL EMF : FARADAY'S LAW

i) At t=0 → loop about to entre

Shrinking Loop

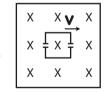
Loop shrinking at rate

 $\mathcal{E}_{Ind} = Bx2 \pi r x \frac{dr}{dt}$



iii) Loop has fully





iv) Loop exiting. Field

is decreasing

I clockwise

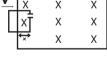
 $B_{ind} \times$

 $\epsilon_{_{\text{Ind}}}\text{-Blv}$

Χ

Χ

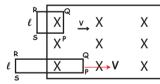
ii) At time t=t, 'x' length inside loop



A=lx $B_{ind} \rightarrow \bigcirc$

 $\mathbf{I}_{\text{ind}} \rightarrow \text{anticlockwise}$ $\bigcirc = BA = BIx$

MOTION OF A SQUARE, RECTANGLE, CIRCLE & ELLIPSE IN UNIFORM MAGNETIC FIELD



For square $PQ \rightarrow E = Blv = Constant$ RQ & SP-1 Parallel to velocity

For Rectangle -PQ → E = Blv = Constant RQ & SP - I Parallel to velocity

 $RS \rightarrow \xi = 0$ (Outside B) Q - Higher potential

P - Lower potential Current - Anticlockwise direction

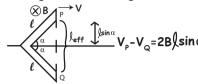
 $RS \rightarrow \xi = 0$ (Outside B) Q - Higher potential P - Lower potential Current - Anticlockwise direction

For Circle & Ellipse Χ

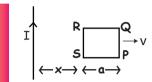
Effective length is constantly varying Induced EMF is varying. When loop is entering, EMF first increases reaches a maximum and then decreases induced current in anticlockwise direction Instantaneous Induced EMF = $B(I_{eff})_{inst}$ v

TRANSLATORY MOTION OF METALLIC FRAME IN UNIFORM / NON UNIFORM MAGNETIC FIELD

Metal frame of different shapes moving in uniform magnetic field



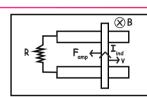
MOVING METAL FRAME IN NON UNIFORM MAGNETIC FIELD



 $B_{\text{at RS}} = \frac{\mu_o I}{2 \pi x}$, $E_{\text{RS}} = \frac{\mu_o I}{2 \pi x}$ av

 $B_{\text{at}} = \frac{\mu_{\text{o}} \mathbf{I}}{2\pi (\mathbf{x} + \mathbf{a})}, \ E_{\text{QP}} = \frac{\mu_{\text{o}} \mathbf{I}}{2\pi (\mathbf{x} + \mathbf{a})} \text{ av}$ $\xi_{\text{net}} = \xi_1 - \xi_2 = \frac{\mu_0 I a^2 v}{2 \pi x (x + a)}$

INDUCED CURRENT AND AMPERIAN FORCE



• Amperian force

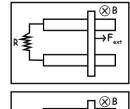
$$F_{amp} = \frac{B^2 \sqrt{V}}{R} \rightarrow Opposes motion$$

• Work done by amperian force

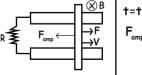
 $W = \triangle KE = 0 - \frac{1}{2} m v_0^2$ Final vel.=0

• Power developed in circuit

Terminal velocity

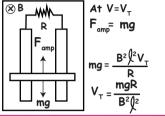


slider at rest

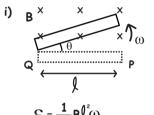


when is terminal velocity achieved **a=0**

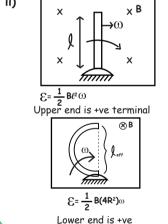
V=V=constant **A**† †=∞



MOTIONAL EMF DUE TO ROTATIONAL MOTION



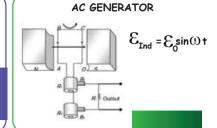
End Q is positive terminal

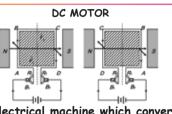


INSTANTANEOUS VALUE OF

 $\Phi = NBA \cos\theta$ = NBA cosot

 $\mathcal{E}_{\mathsf{Ind}}$ = NBA ω sin ω t E_= NBAW when t=0 $\mathcal{E}_{\mathsf{Ind}} = \mathcal{E}_{\mathsf{S}} \mathsf{sin} \omega \mathsf{t}$





electrical machine which converts electrical energy into mechanical

EQUATION FOR BACK EMF E-NBA@sin@t MECHANICAL POWER

& EFFICIENCY OF DC MOTOR

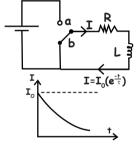
 $\eta = \frac{\mathsf{back} \; \mathsf{emf}}{\mathsf{supply} \; \mathsf{voltage}} = \frac{\mathsf{Pout}}{\mathsf{Pin}} = \frac{\mathsf{e}}{\mathsf{E}}$

L-R CIRCUIT

Steady state \rightarrow inductor \rightarrow zero resistance For current growth in a circuit

- at t=0 Inductor offers infinite resistance - at t=∞ Inductor offers zero resistance

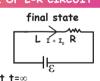
 $I=I_0(1-e^{\frac{-\tau}{\tau}})$



INITIAL & FINAL STATE OF L-R CIRCUIT

Initial state

Initial state - inductor open V= 3



final state -replace inductor with a wire

PERIODIC EMI

Average induced emf

- when coil is rotated from θ = 0° to 90° $E_{ind} = \frac{2NBA@}{II}$
- when coil is rotated from θ =90° to 180° ξ_{ind} =- $\frac{2NBA \odot}{\pi}$

