

Topics to be covered



- 1) Thermometry
- 2) Calorimetry
- 3) Thermal Expansion
- 4) Heat Transfer



Thermometry

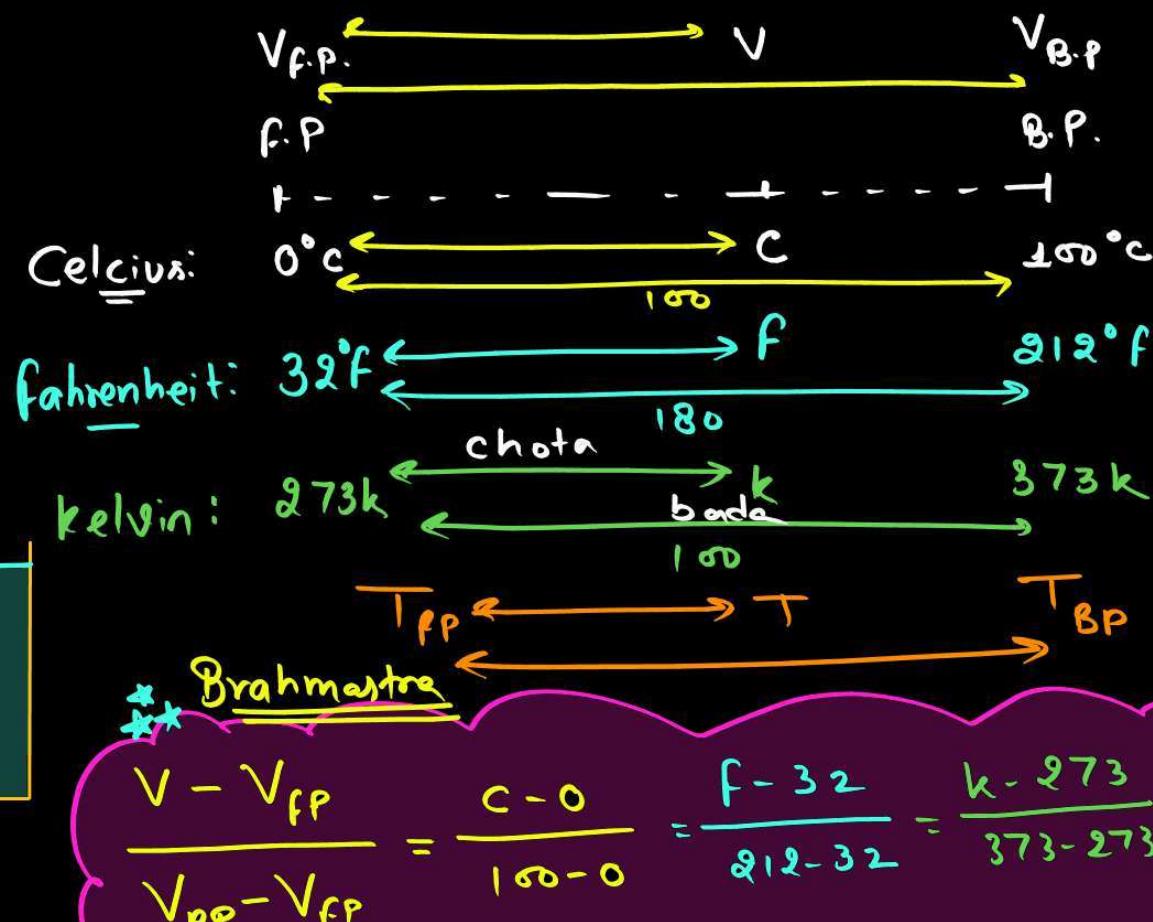
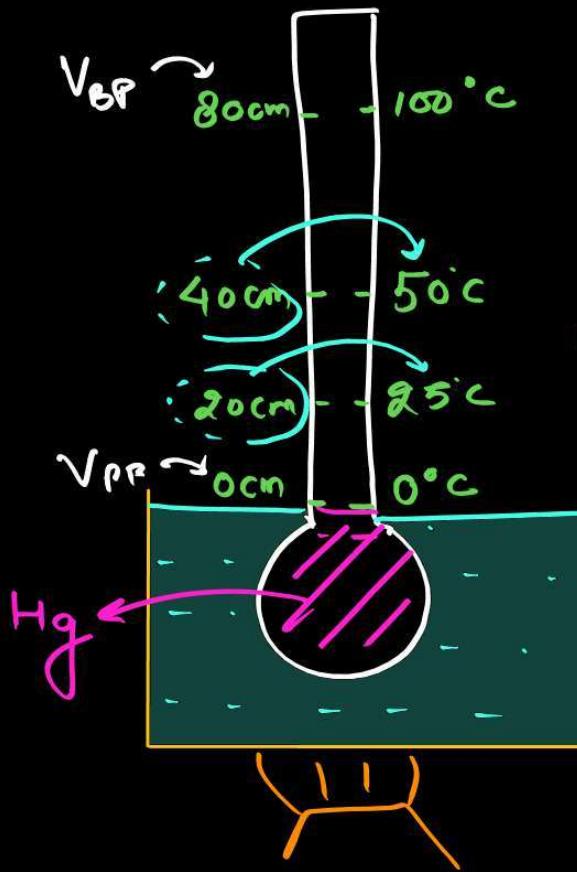


Measurement of Temperature

Phy. Qty. that vary with temp.

- Volume
- Pressure of gas at
Const vol.
$$\left\{ \begin{array}{l} PV = nRT \\ \Rightarrow P \propto T \end{array} \right.$$
- Density
- Electrical Resistance
- Thermal Radiation

fundamental physical Qty
↓
Degree of Hotness
{ Avg. k.e of molecules }



$f.p.$ = Freezing pt. of water.
 $B.P.$ = Boiling pt. of water.



$$\frac{C}{100} = \frac{F-32}{180}$$

$$C = \frac{5}{9}(F-32)$$

→ $\Delta C = \frac{5}{9} \Delta F$

$$\Delta C = \frac{5}{9} \times 45 = 25^{\circ}\text{C}$$

i) Convert 41°F into $^{\circ}\text{C}$

$$C = \frac{5}{9}(41-32)$$

$$= \frac{5}{9} \times 9 = 5^{\circ}\text{C}$$

ΔT

ii) Temp. of body risen by 45°F .
What is the temp. change in $^{\circ}\text{C}$?

$$C = \frac{5}{9}(F-32)$$

$$C + \Delta C = \frac{5}{9}(F+45-32)$$



$$\frac{C - 0}{\cancel{100.0}} = \frac{k - 273}{\cancel{100}}$$

$$C = k - 273$$

$$\Delta C = \Delta k$$

QUESTION



- (1) Convert 50°C into Fahrenheit.
- (2) At what temp, Fahrenheit scale & Celsius scale will give same reading.
- (3) A body is heated such that its temp. rises from 20° C to 50° C . Find the temp. change of body in Fahrenheits.

$$1) \frac{C-0}{100-0} = \frac{F-32}{212-32}$$

$$\cancel{\frac{50}{100}} = \frac{F-32}{180} \Rightarrow F = 90 + 32$$

$F = 122^{\circ}\text{F}$

2)

$$\frac{C-0}{100-0} = \frac{C-32}{212-32}$$

$$\Rightarrow \frac{C}{100} = \frac{C-32}{180}$$

$$\frac{9}{5}C = C - 32$$

$$\left(\frac{9}{5} - 1\right)C = -32$$

$C = -40^{\circ}\text{F}$

3) $\Delta C = 30^{\circ}\text{C}$

$$\frac{C-0}{100-0} = \frac{F-32}{212-32}$$

$$C = \frac{5}{9}(F-32)$$

$$\Delta C = \frac{5}{9} \Delta F$$

$$30 = \frac{5}{9} \Delta F \Rightarrow \Delta F = 54^{\circ}\text{F}$$

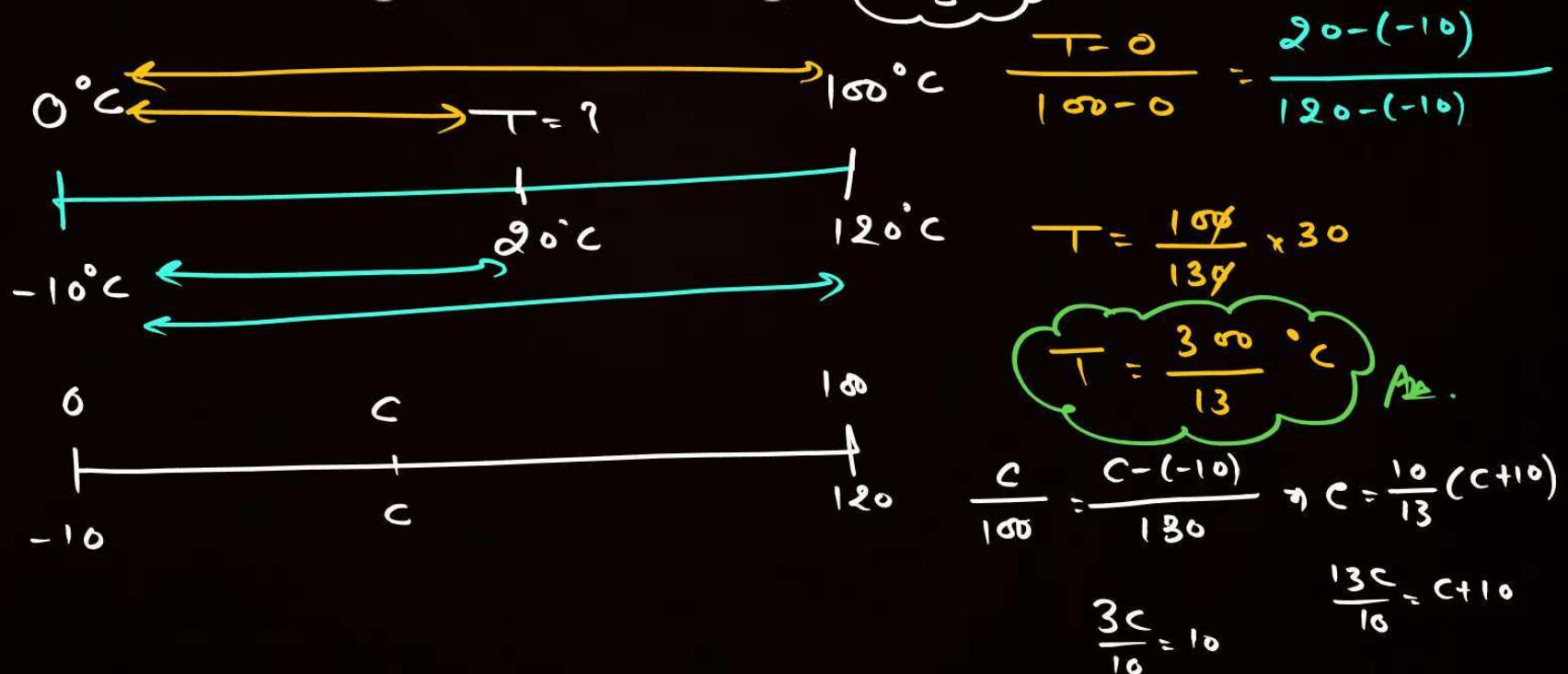
Ans.

QUESTION

Custom scale.



A faulty thermometer reads -10°C at freezing pt. of water & 120°C at boiling point of water when the thermometer reads 20°C what is the actual temp. of body? At what temp. will the thermometer give correct reading? $\rightarrow C = \frac{100}{3}^{\circ}\text{C}$

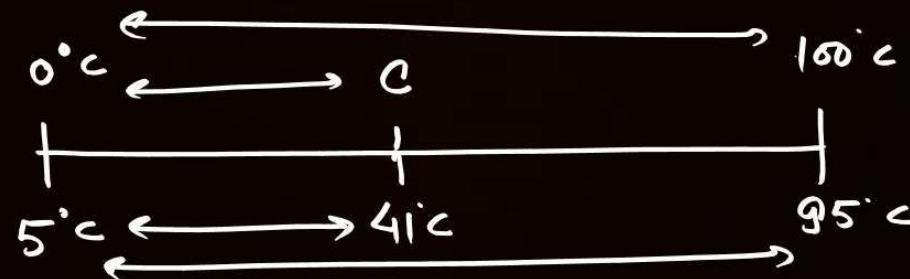


QUESTION (JEE Mains – Jan. 30, 2023 (II))



A faulty thermometer reads 5°C in melting ice and 95°C in steam. The correct temperature on absolute scale will be _____ K when the faulty thermometer reads 41°C .

kelvin



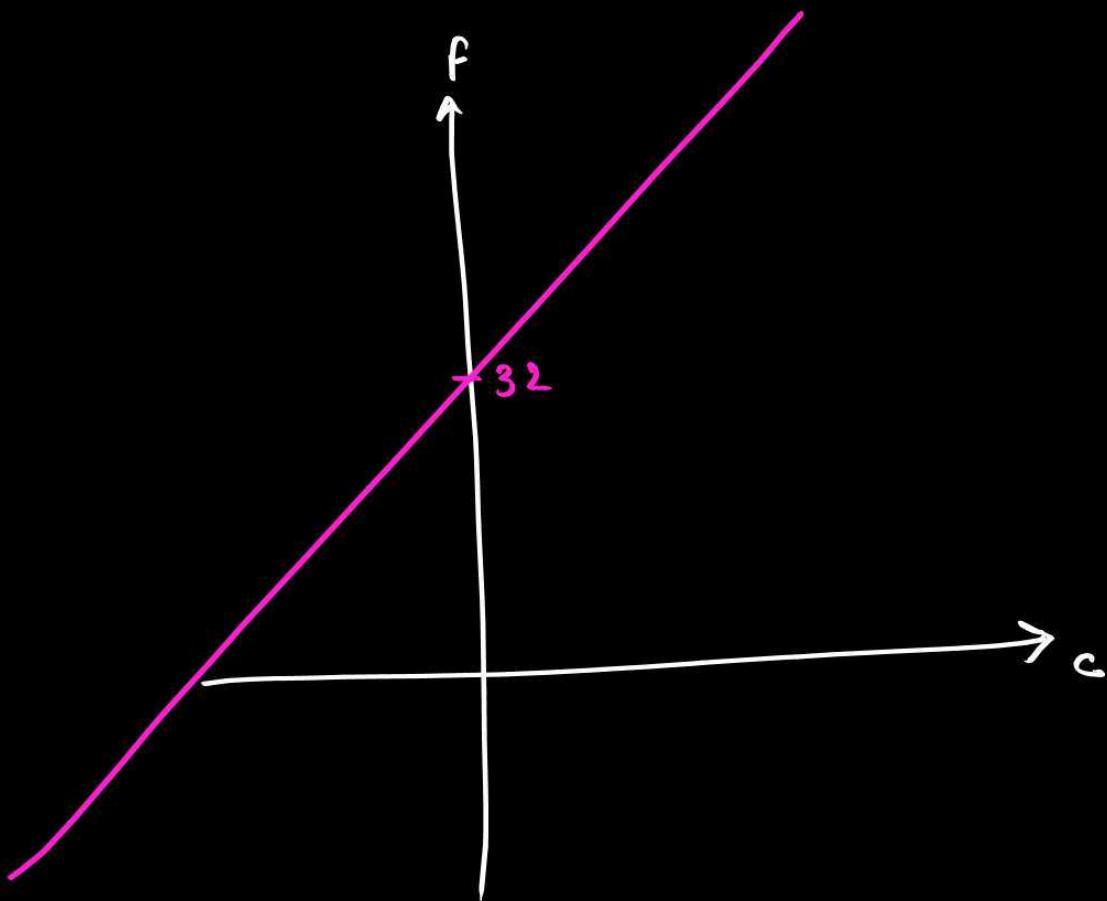
$$\frac{41 - 5}{95 - 5} = \frac{C - 0}{100 - 0}$$

$$C = \frac{364}{24} \times 100$$

$$C = 40^{\circ}\text{C}$$

$$k = 273 + 40$$

$$k = 313 \text{ K} \quad \text{Ans}$$



$$C = \frac{9}{5}(F - 32)$$

$$\begin{matrix} F = \frac{9}{5}C + 32 \\ \downarrow \qquad \downarrow \\ y \qquad x \end{matrix}$$

$$y = \frac{9}{5}x + 32$$

QUESTION (JEE Mains – Jan. 25, 2023 (II))

The graph between two temperature scales P and Q is shown in the figure. Between upper fixed point and lower fixed point there are 150 equal divisions of scale P and 100 divisions on scale Q. The relationship for conversion between the two scales is given by:

A

$$\frac{t_Q}{150} = \frac{t_p - 180}{100}$$

B

$$\frac{t_Q}{100} = \frac{t_p - 30}{150}$$

C

$$\frac{t_Q}{180} = \frac{t_p - 40}{100}$$

D

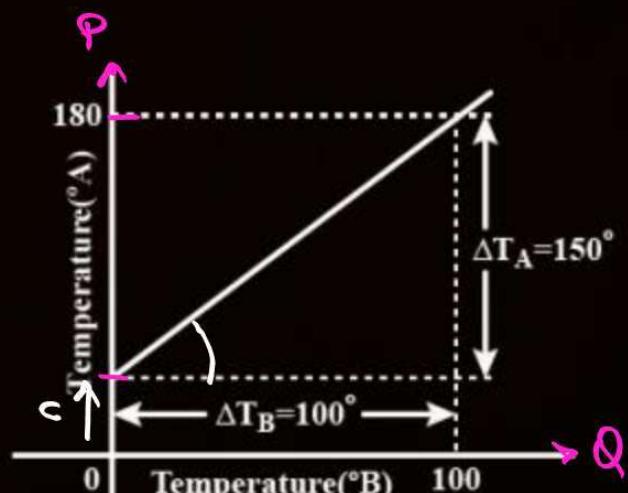
$$\frac{t_p}{100} = \frac{t_Q - 180}{150}$$

$$y = mx + c$$

$$P = \frac{150}{100} \times Q + 30$$

$$P - 30 = \frac{150}{100} Q$$

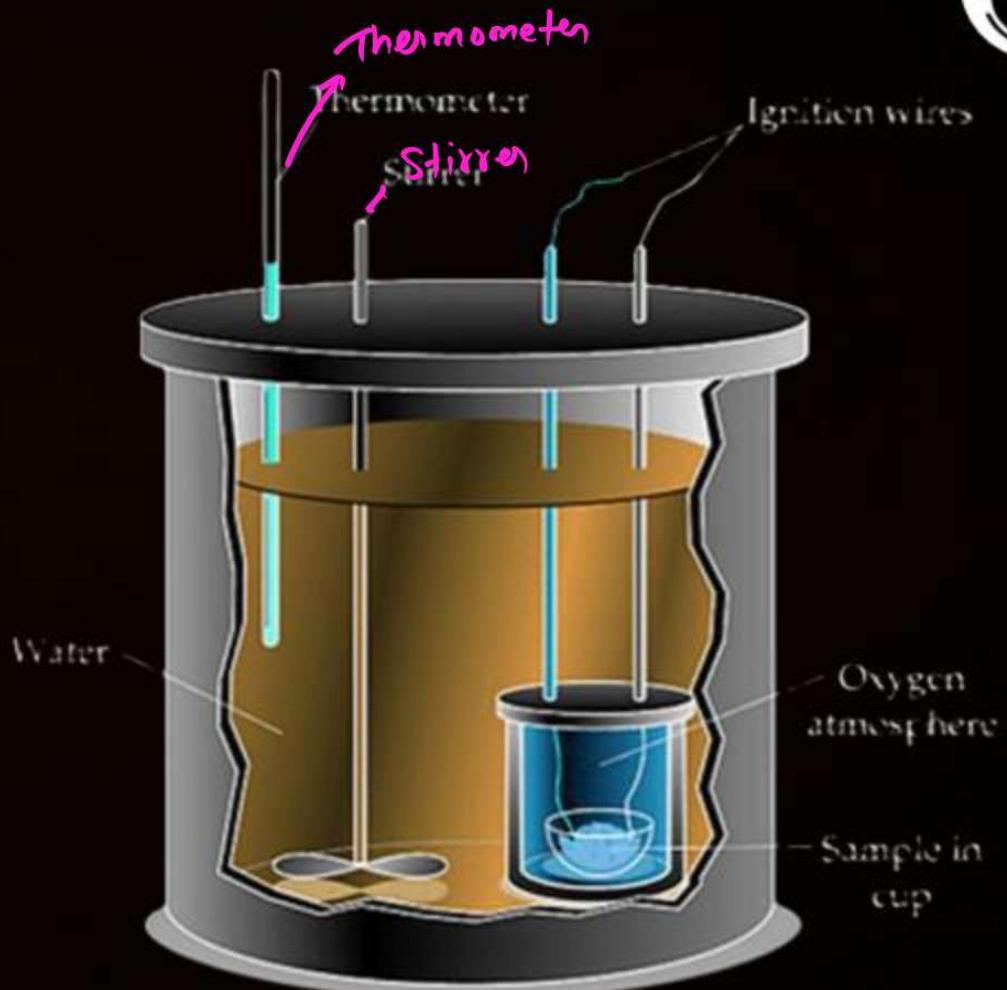
$$\frac{Q}{100} = \frac{P - 30}{150}$$





Calorimetry

Study of heat exchanged
b/w different materials
due to temp. difference





Specific Heat Capacity



$$\frac{\text{mass}}{1 \text{ g}} \xrightarrow{\Delta T} 1^\circ \text{C} \xrightarrow{Q} \text{Sp. Heat Capacity}$$

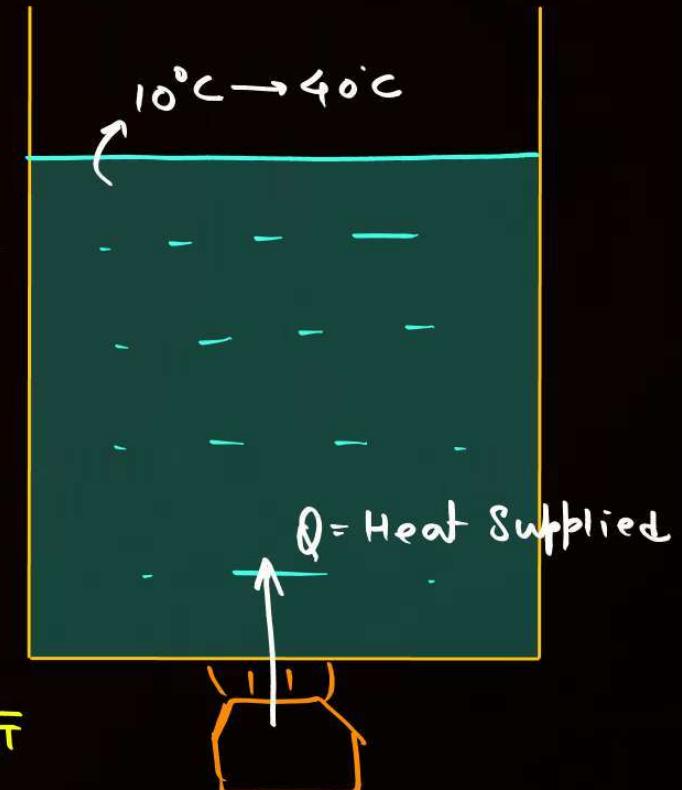
(S) cal.

$$m \text{ g} \longrightarrow 1^\circ \text{C} \longrightarrow m \text{ s}$$

$$m \text{ g} \longrightarrow \Delta T^\circ \text{C} \longrightarrow m \text{ s} \Delta T$$

$$Q = m \text{ s} \Delta T$$

$$S = \frac{Q}{2 \times m \Delta T}$$



$$1 \text{ cal} = 4.2 \text{ J}$$

- Sp. Heat capacity is the property of material only, it does not depend on mass & temp. change of body.

Very High

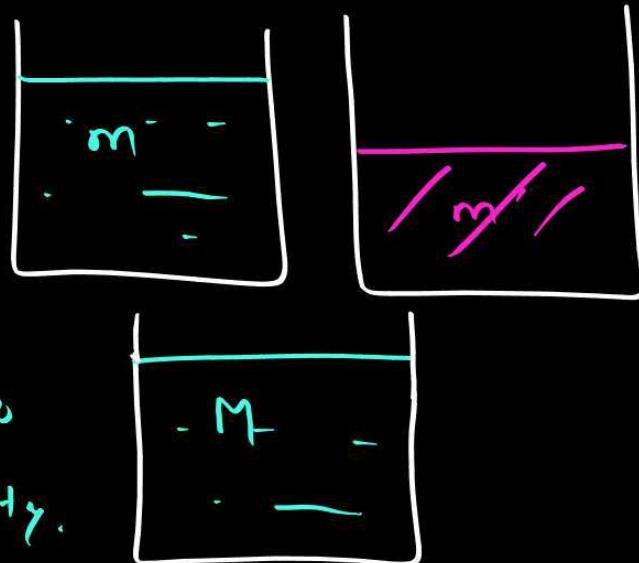
- $S_{\text{water}} = 1 \text{ Cal/g}^{\circ}\text{C}$

$$4200 \text{ J/kg.K}$$

$$S_{\text{Ice}} = \frac{1}{2} \text{ Cal/g}^{\circ}\text{C}$$

$$S_{\text{steam}} = \frac{1}{2} \text{ Cal/g}^{\circ}\text{C}$$

- Sp. Heat cap. is the heat req. to raise temp. of unit mass by unity.





High Sp. Heat cap. → गरम करने में
उच्चाधा Heat → गरम करना
लगाए गयी Better Coolant



Heat Capacity

Heat required to raise temp. of any mass by unity

$$Q = \underline{m s \Delta T}$$
$$Q = C \Delta T$$

$$C = m s$$

$$C \propto m$$

Unit : J/k
or Cal/ $^{\circ}$ C

$$1g \rightarrow 1^{\circ}C \rightarrow s$$
$$mg \rightarrow 1^{\circ}C \rightarrow ms$$
$$mg \rightarrow \Delta T \rightarrow ms \Delta T$$

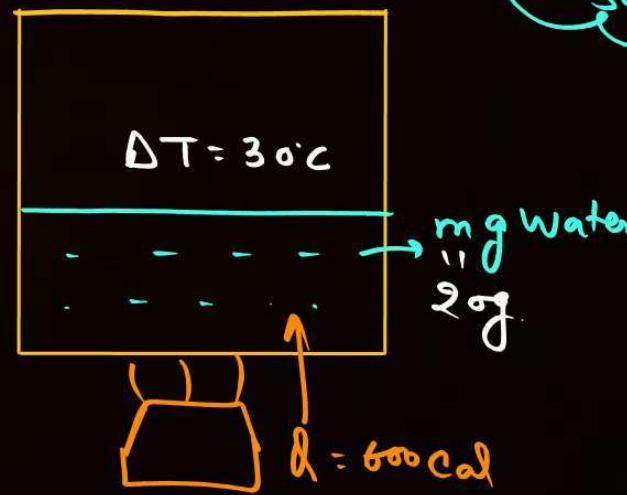
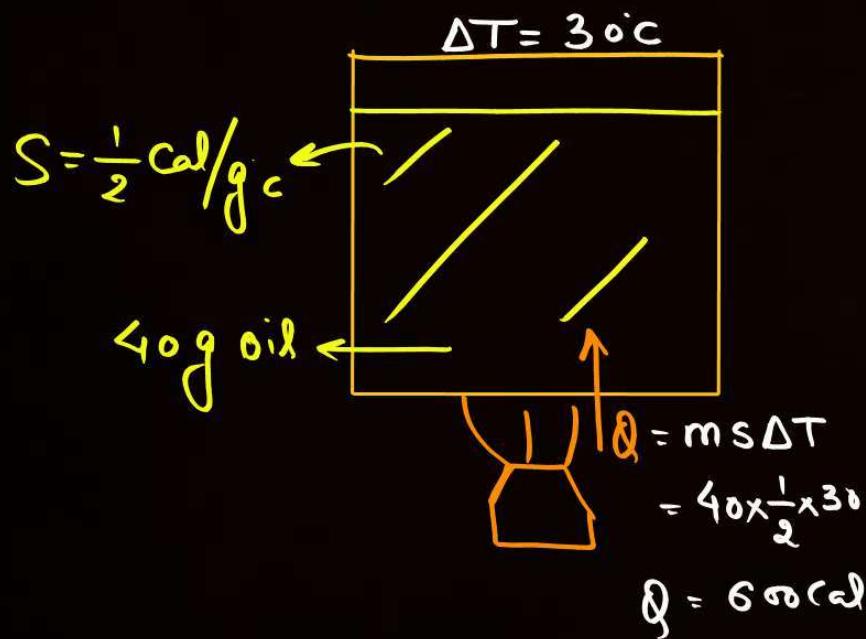




Water Equivalent



Amount of water which is thermally equivalent to given material.



$$Q = mS\Delta T$$
$$600 = m \times 1 \times 30$$

$$m = 20\text{ g}$$

Same Heat $\frac{1}{2} \times 42$
Same temp. change



$$Q = m s \Delta T$$

$$m_w \cdot S_w \cancel{\Delta T} = m s \cancel{\Delta T}$$

Water equivalent

$$m_w = m s$$

SI unit : kg
CGS unit : g

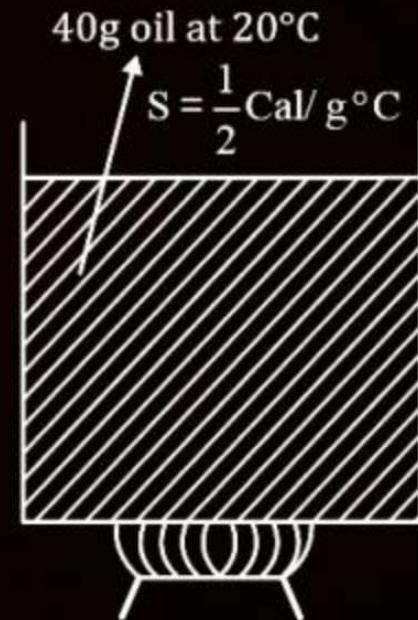
QUESTION

Find heat req to raise temp. of oil to 50°.

$$Q = m s \Delta T$$

$$= 40 \times \frac{1}{2} \times 30$$

$$Q = 600 \text{ cal}$$



QUESTION



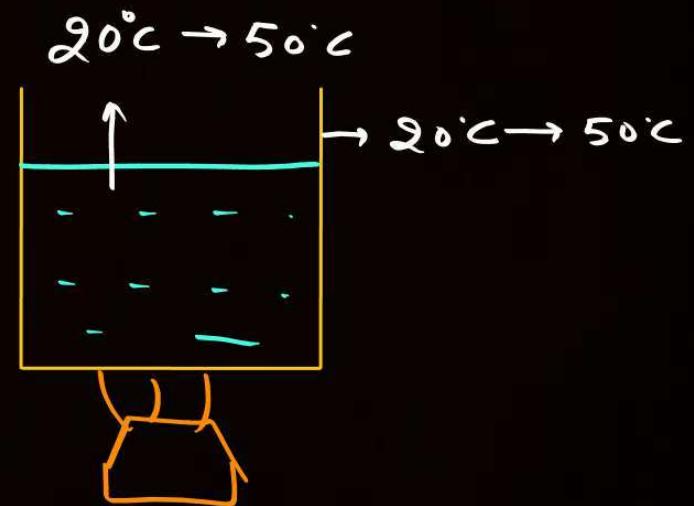
A container of mass 1 kg contains 40 g oil at $20^\circ C$. If the sp. Heat cap. of oil is $1/2 \text{ cal/g}^\circ \text{C}$. Find the heat req to raise temp. of oil to 50°C ($S_{\text{container}} = \underline{0.1 \text{ cal/g}^\circ \text{C}}$)

$$Q = m_1 s_1 \Delta T + m_2 s_2 \Delta T$$

$$= 40 \times \frac{1}{2} \times 30 + 1000 \times 0.1 \times 30$$

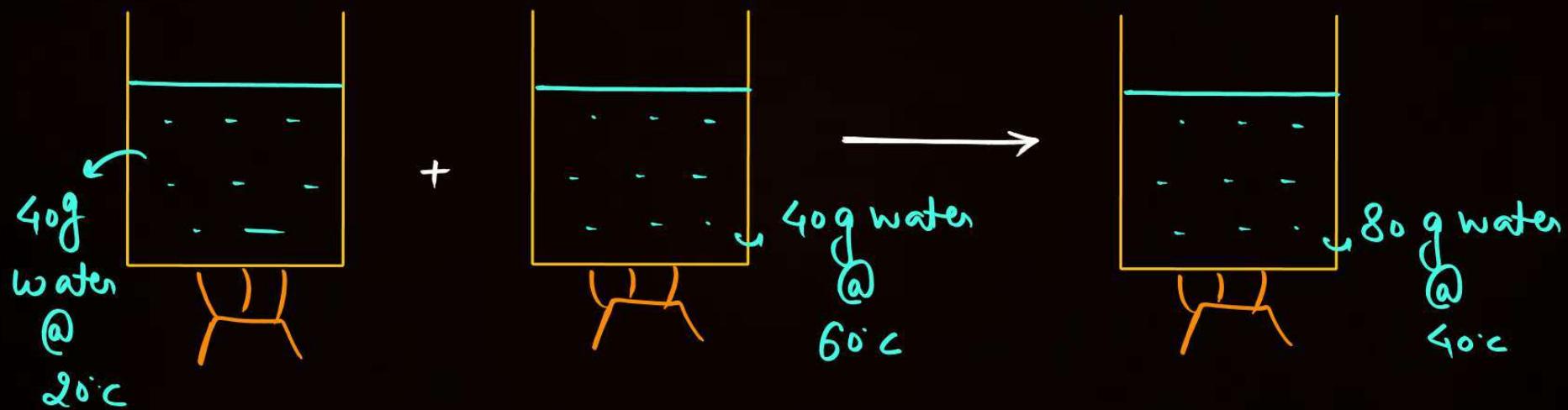
$$= 600 + 3000$$

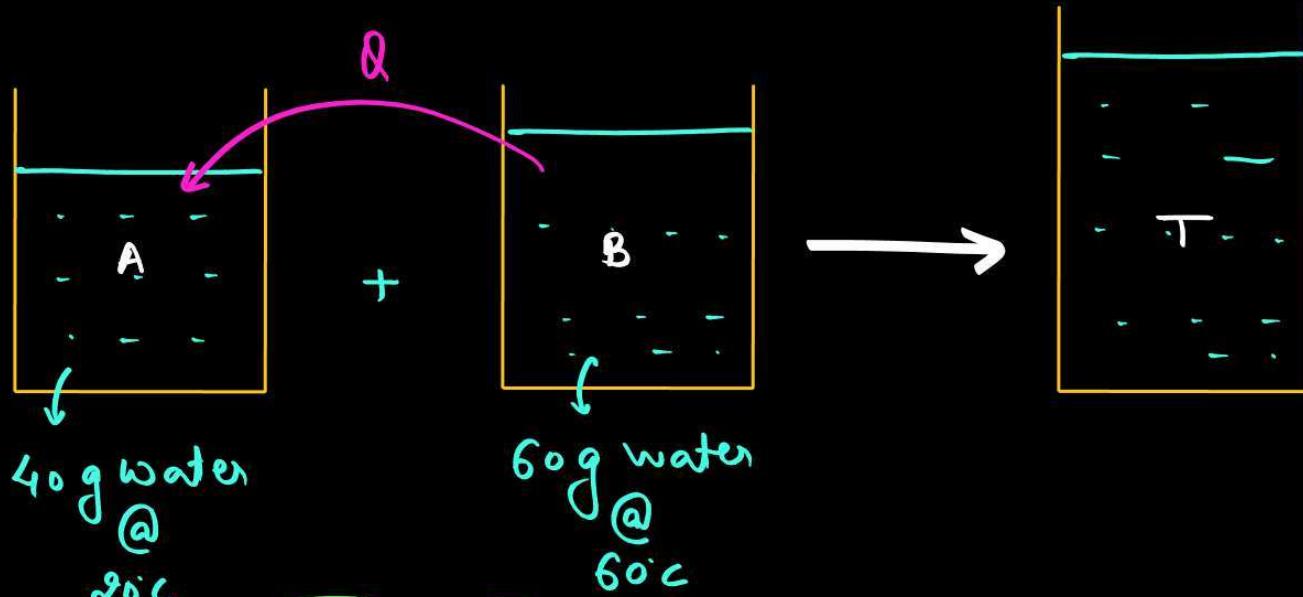
$$= 3600 \text{ cal}$$





Mixture of Liquids at Different Temperatures

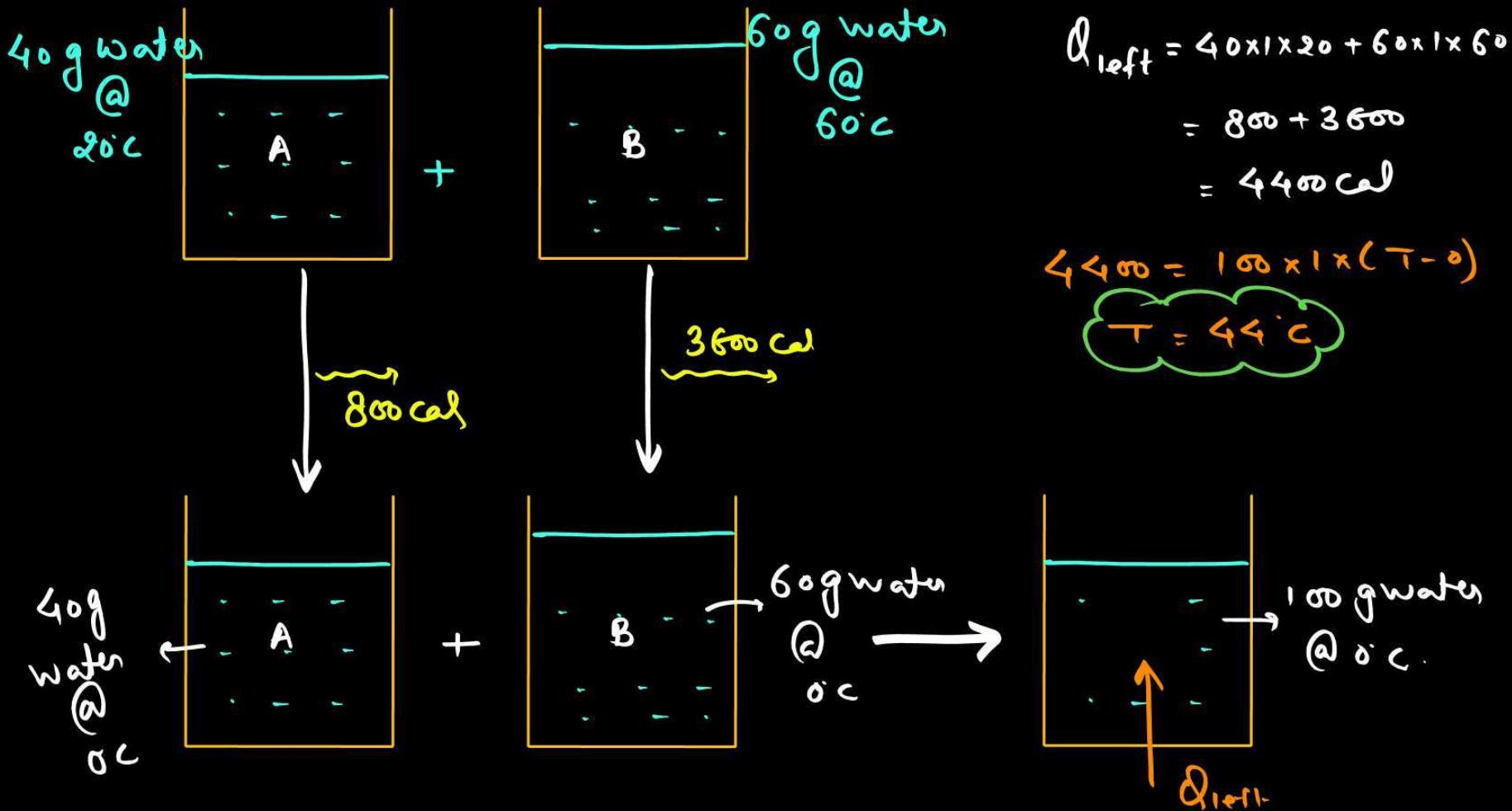




Flam Zinder

Heat lost by B = Heat gained by A

$$60 \times 1 \times (60 - T) = 40 \times 1 \times (T - 20) \Rightarrow 3600 - 60T = 40T - 800$$
$$100T = 4400$$
$$T = 44^\circ\text{C}$$

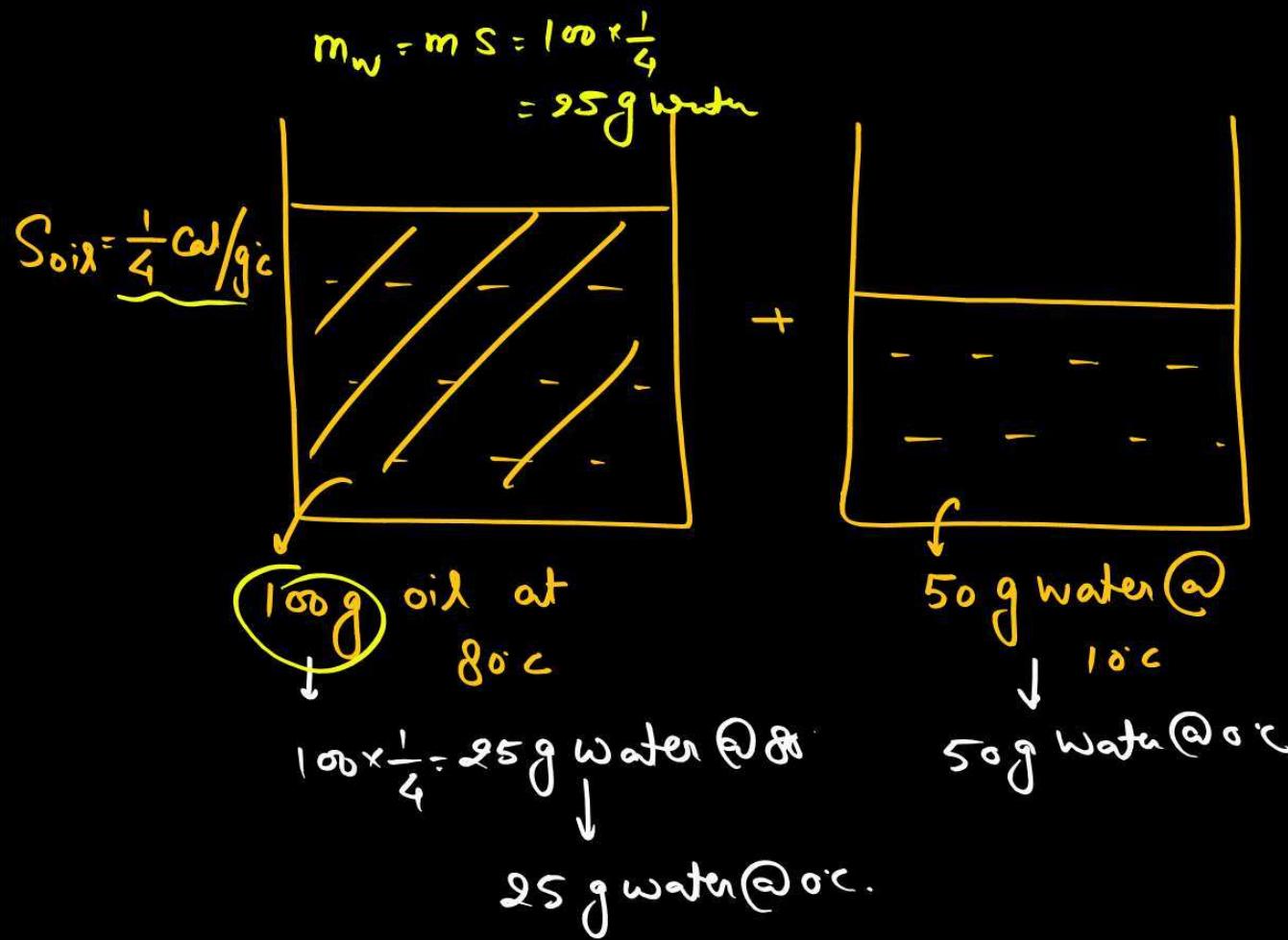




Brahmastra - 2

- Convert Everything into 0°C water equivalent.
- Find Q_{left} .
- Give back Q_{left} to entire water equivalent.

$$Q_{\text{left}} = m_{\text{total}} \times l \times (T - 0)$$



$$Q_{\text{left}} = 25 \times 80 + 50 \times 16$$

$$= 2000 + 500$$

$$= 2500 \text{ cal}$$

$$M_{\text{total}} = 25 + 50$$

$$= 75 \text{ g water.}$$

$$Q_{\text{left}} = M_{\text{total}} \cdot S \cdot \Delta T$$

$$2500 = 75 \times 1 \times T$$

$$T = \frac{2500}{75} = \frac{800}{18} = \frac{100}{3}^\circ\text{C}$$

QUESTION



Find final temperature if 130 grams water at 10°C is added to 60 grams liquid at 80°C kept in the shown container.

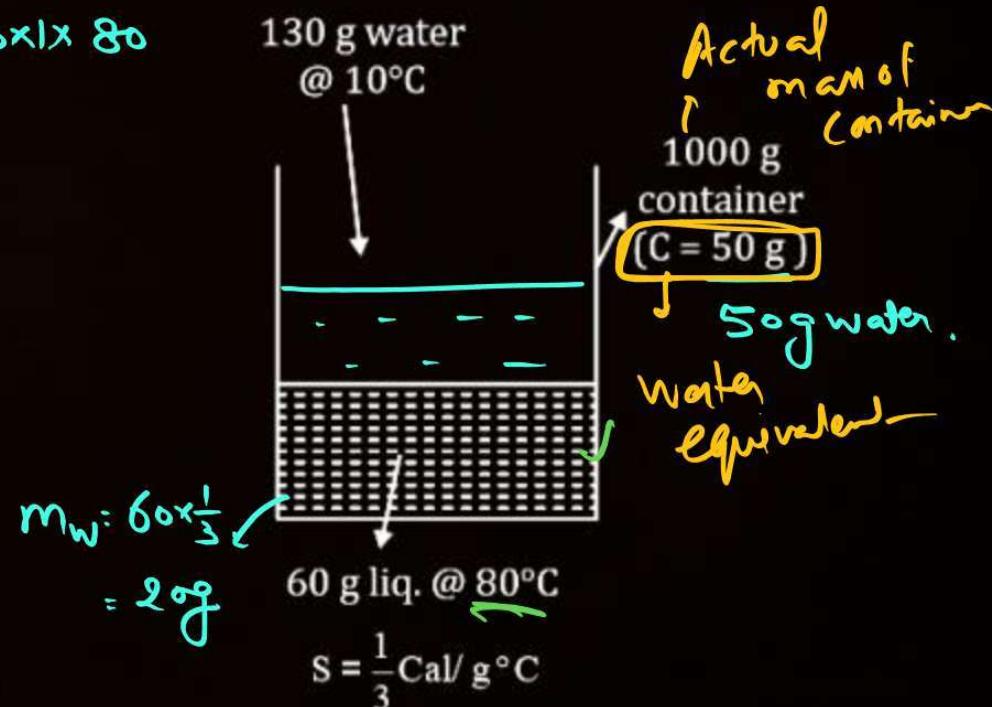
$$\begin{aligned} Q_{\text{left}} &= 130 \times 1 \times 10 + 20 \times 1 \times 80 + 50 \times 1 \times 80 \\ &= 1300 + 1600 + 4000 \\ &= 6900 \text{ cal.} \end{aligned}$$

$$m_{\text{total}} = 130 + 20 + 50 = 200 \text{ g}$$

$$Q_{\text{left}} = m_{\text{total}} \cdot S \cdot \Delta T$$

$$6900 = 200 \times 1 \times (T - 0)$$

$$T = \frac{69}{2} = 34.5^{\circ}\text{C} \text{ Ans.}$$



QUESTION



Find final temp. of mixture.

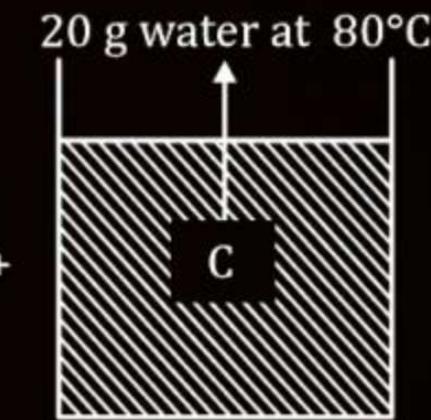
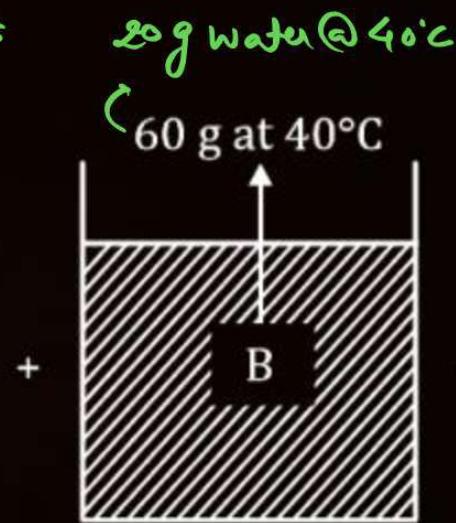
$$\frac{10 \times 20 + 20 \times 40 + 20 \times 80}{10 + 20 + 20}$$

$$\frac{200 + 800 + 1600}{50}$$

$$\frac{2600}{50} = 52^{\circ}\text{C}$$

Ans

10 g water @ 20°C
40 g @ 20°C



$$S_A = \frac{1}{4} \text{ Cal/g}^{\circ}\text{C}$$

$$S_B = \frac{1}{3} \text{ Cal/g}^{\circ}\text{C}$$



$$\overline{T_f} = \frac{m_1 S_1 T_1 + m_2 S_2 T_2 + \dots}{m_1 S_1 + m_2 S_2 + \dots}$$

मत याद करना



Equivalent Heat Capacity of Mixtures



$$S_{eq} = \frac{m_1 S_1 + m_2 S_2 + \dots}{m_1 + m_2 + \dots}$$



Latent Heat

Latent Heat of fusion

Solid \longrightarrow Liquid

mass

$1g$

$\longrightarrow L_f$

$m g$

$\longrightarrow m L_f$

L_f for water = 80 cal/g .

Latent Heat of vaporization.

Liquid \longrightarrow Gas

$1g \longrightarrow L_v$

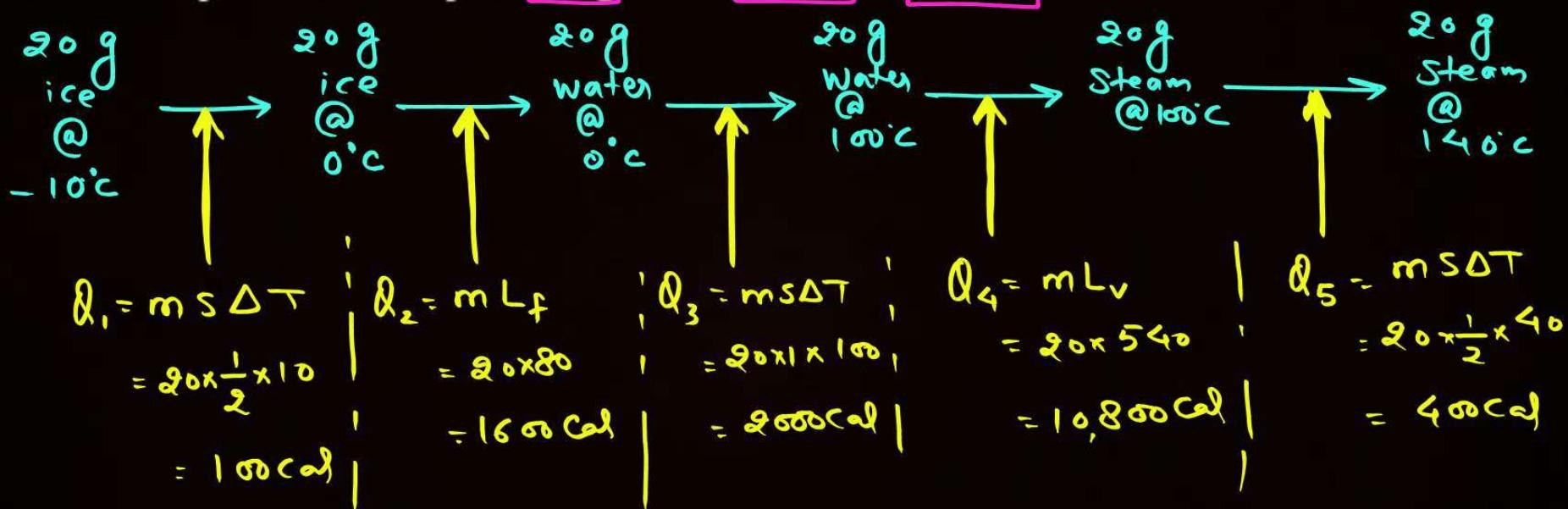
$m g \longrightarrow Q = m L_v$

L_v for water = 540 cal/g .

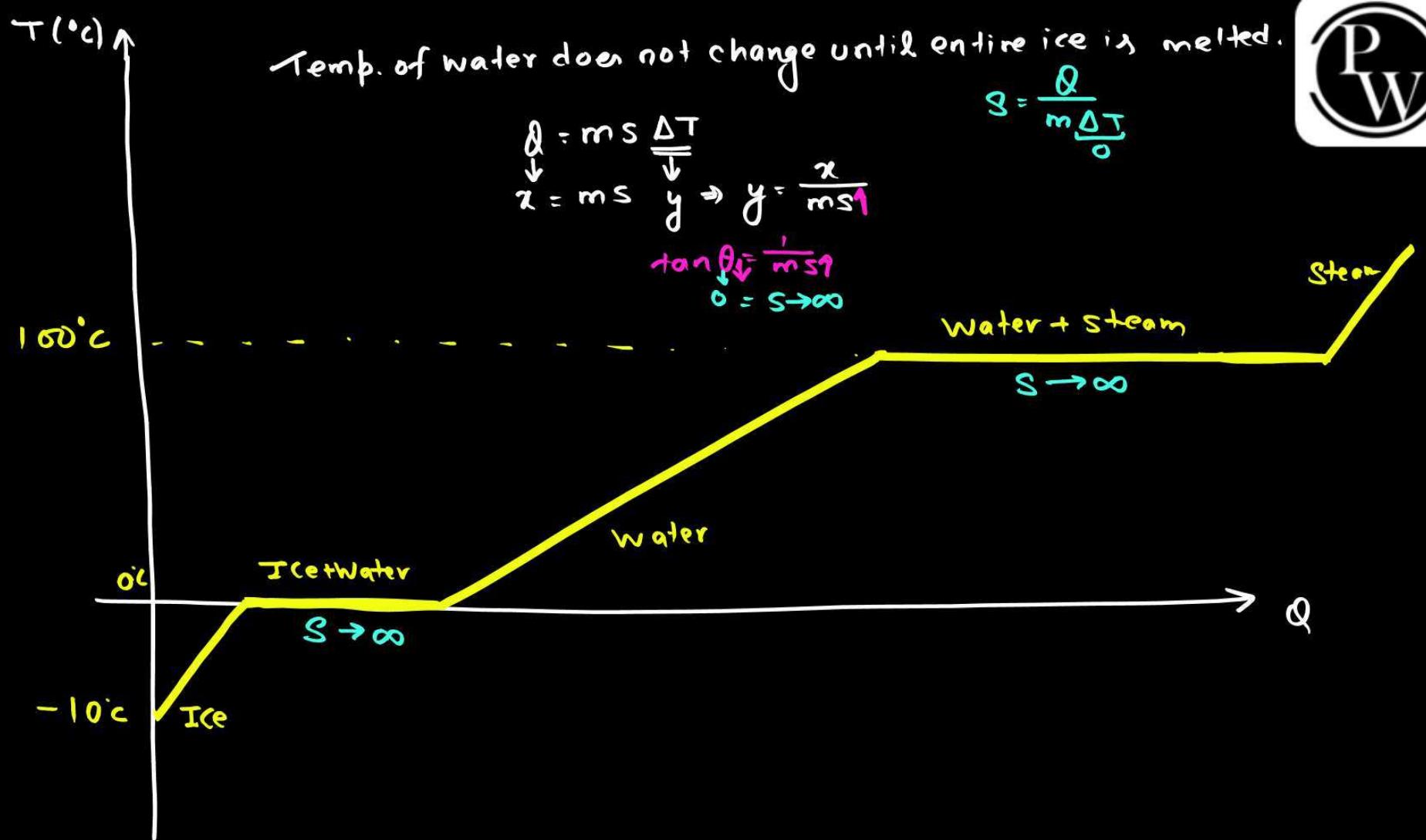
QUESTION



Find heat req to raise temp. of 20 g ice at -10°C to 140°C .

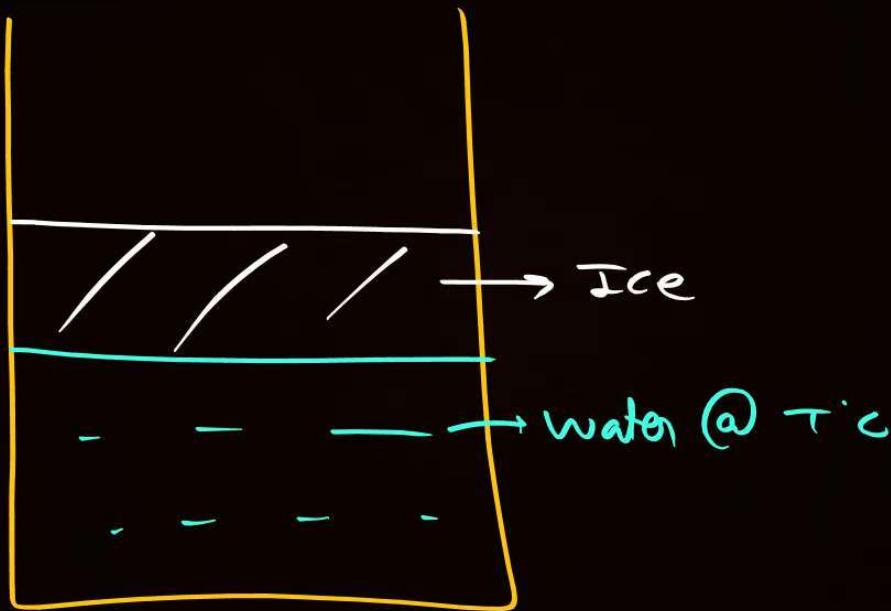


$$Q_{\text{total}} = Q_1 + Q_2 + Q_3 + Q_4 + Q_5 = 14,900 \text{ cal}$$





Ice Water Mixture





no. of friends = 20

Cost of one ticket = 80/-

Total money required = $20 \times 80 = 1600/-$

Papa में रुपये किये = 1,600/-

कातने दौरत picture देरवाही = 20

no. of friends = 20

Cost of one ticket = 80/-

Total money required = $20 \times 80 = 1600/-$

Papa में रुपये किये = 80/-

फिल्में रुपये कम पड़े = $1600 - 800 = 800/-$

फिल्में दौरत picture नहीं = $\frac{800}{80} = 10$
दूसरा पायेंगे

कातने दौरत picture देरवाही = $\frac{800}{80} = 10$
जो $20 - 10 = 10$



No. of friends = 20

Cost of one ticket = 80/-

Total money required = $20 \times 80 = 1600/-$

Papa के रुपये किये = 2000/-

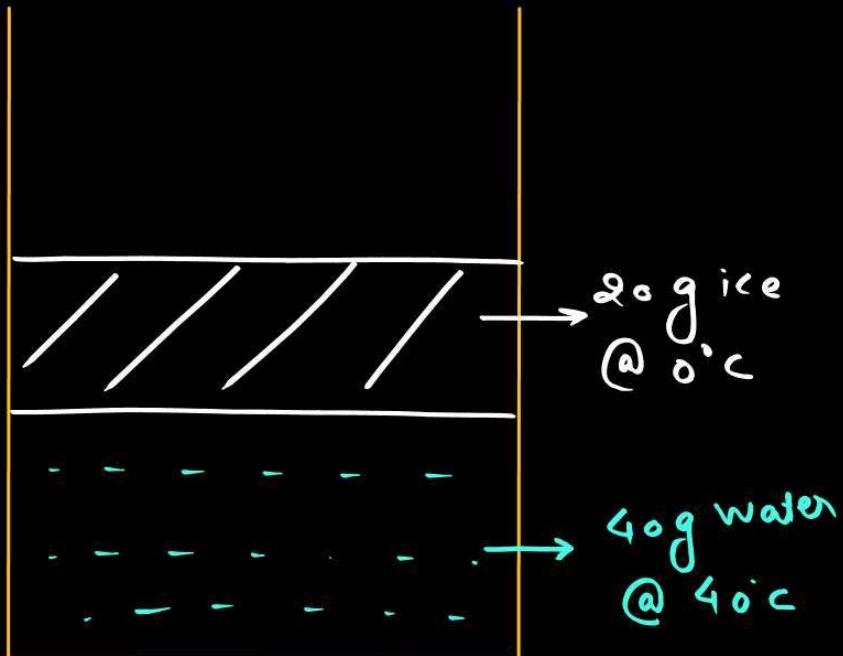
Ki तकनी रुपये extra मिले = $2000/- - 1600 = 400/-$

कंतेल फोटोट प्रिंटर द्वारा : 20

party के लिये extra रुपये = 400/-



⇒ Convert everything into 0°C water equivalent



$$Q_{\text{left}} = 40 \times 1 \times 40 - 20 \times 80$$

$$= 1600 - 1600$$

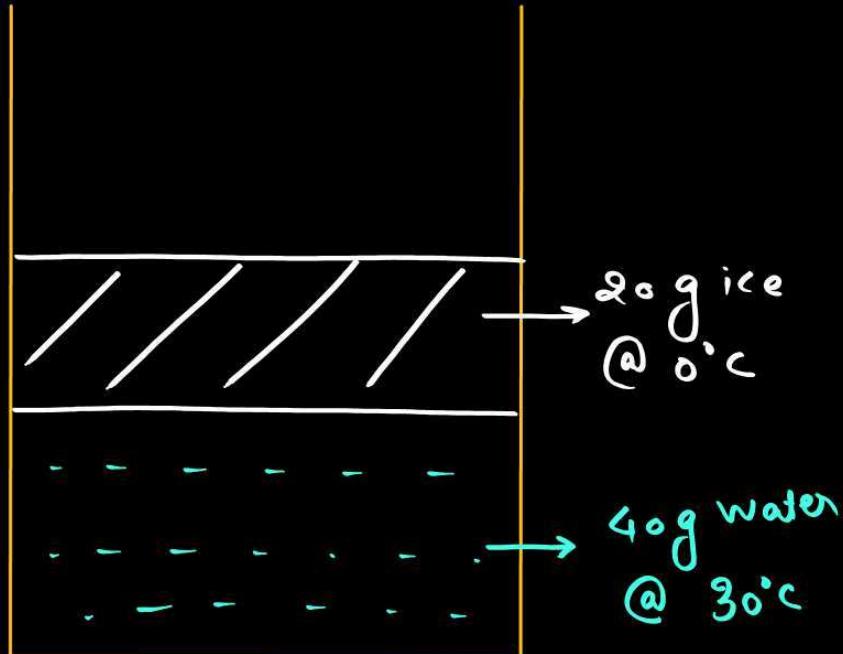
$$Q_{\text{left}} = 0 \text{ cal}$$

Entire ice has just melted.

$$T_{\text{final}} = 0^\circ\text{C}$$



⇒ Convert everything into 0°C water equivalent.



$$Q_{\text{left}} = 40 \times 1 \times 30 - 20 \times 80$$

$$= 1200 - 1600$$

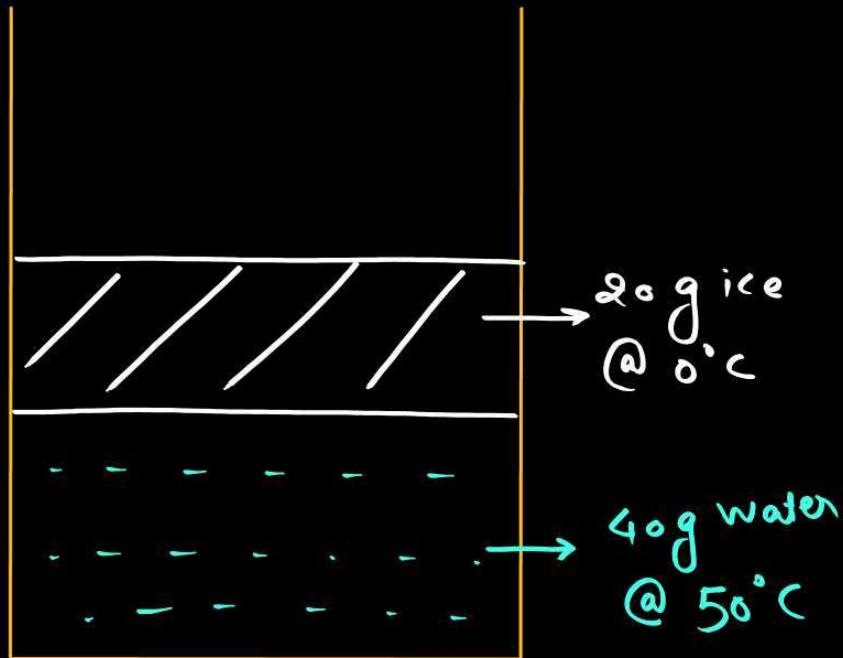
$$Q_{\text{left}} = (-400 \text{ cal}) \quad \begin{array}{l} \text{400 कम पर्याप्त है} \\ \text{पड़ गये} \end{array}$$

$$\text{Amt. of ice left} = \frac{400}{80} = 5 \text{ g}$$

$$\text{Amt. of water} = 15 + 40 = 55 \text{ g}$$

$$T_{\text{final}} = 0^\circ\text{C}$$

⇒ Convert everything into 0°C water equivalent.



$$Q_{\text{left}} = 40 \times 1 \times 50 - 20 \times 80 \\ = 2000 - 1600$$

$$Q_{\text{left}} = 400 \text{ cal.}$$

Entire ice has melted.

$$m_{\text{ice}} = 0$$

$$m_{\text{water}} = 40 + 20 = 60 \text{ g}$$

$$Q_{\text{left}} = m_{\text{total}} \cdot S \Delta T$$

$$400 = 60 \times 1 \times (T - 0) \\ T = \frac{400}{60} = \frac{20}{3}^{\circ}\text{C}$$

QUESTION



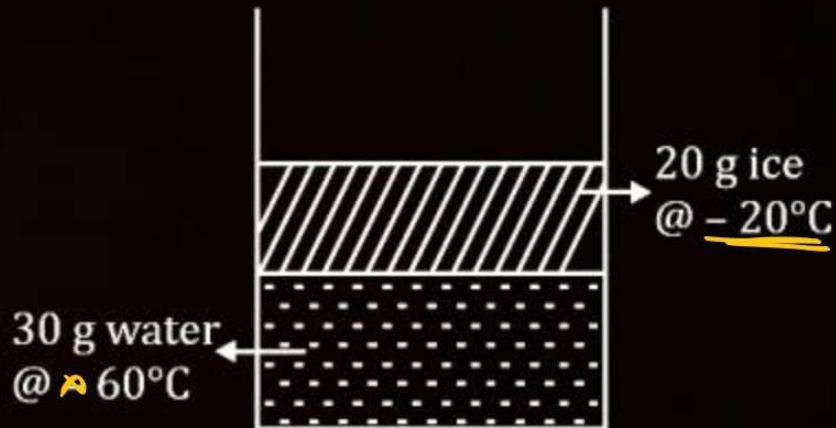
Find final temperature and composition.

$$\begin{aligned}Q_{\text{refl}} &= 30 \times 60 - 20 \times \frac{1}{2} \times 20 - 20 \times 80 \\&= 1800 - 200 - 1600\end{aligned}$$

$$= 0$$

Entire ice just melts.

$m_{\text{ice}} = 0$
 $m_{\text{water}} = 50 \text{ g}$
 $T_{\text{final}} = 0^\circ \text{C}$



QUESTION



Find final temperature & composition.

$$Q_{\text{left}} = 40 \times 50 - 20 \times \frac{1}{2} \times 10 - 20 \times 80$$

$$= 2000 - 100 - 1600$$

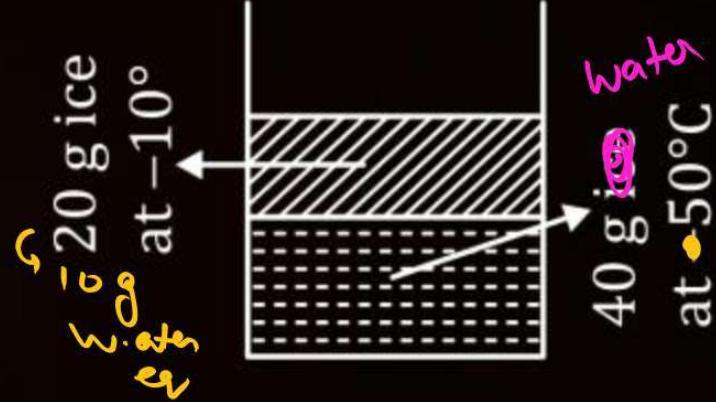
$$= 300 \text{ cal}$$

Entire ice melts.

$$Q_{\text{left}} = m_{\text{total}} \cdot s \cdot \Delta T$$

$$300 = 60 \times 1 \times T$$

$$(T = 5^{\circ}\text{C})$$





Ice Steam Mixture



Use same Brahmastra

QUESTION

$$L_v = 540 \text{ Cal/g}$$



Find min. amount of steam required to completely melt the entire ice.

$$Q_{\text{left}} = m \times 540 - 80 \times 80$$

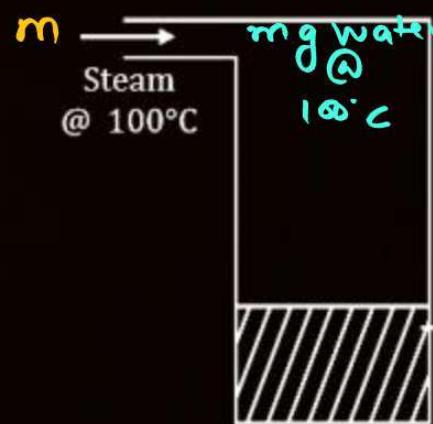
Common mistake

$$\Theta = m \times 540 - 6400$$

$$m = \frac{6400}{540} = \frac{640}{54} \text{ g}$$

$$Q_{\text{left}} = m \times 540 + m \times 1 \times 100 - 80 \times 80$$

$$\Theta = m \times 640 - 6400 + m \times 100$$



Steam @ 100°C



Water @ 100°C



Water @ 0°C

80 g Ice
@ 0°C

80 g ice
@ 0°C.



1 g steam @ 100°C can completely melt 8 g ice @ 0°C .

QUESTION



Find final temp. & composition.

$$Q_{\text{left}} = \underbrace{10 \times 540}_{\text{Q}_1} + \underbrace{10 \times 1 \times 100}_{\text{Q}_2} - \underbrace{80 \times \frac{1}{2} \times 40}_{\text{Q}_3} - \underbrace{80 \times 80}_{\text{Q}_4}$$

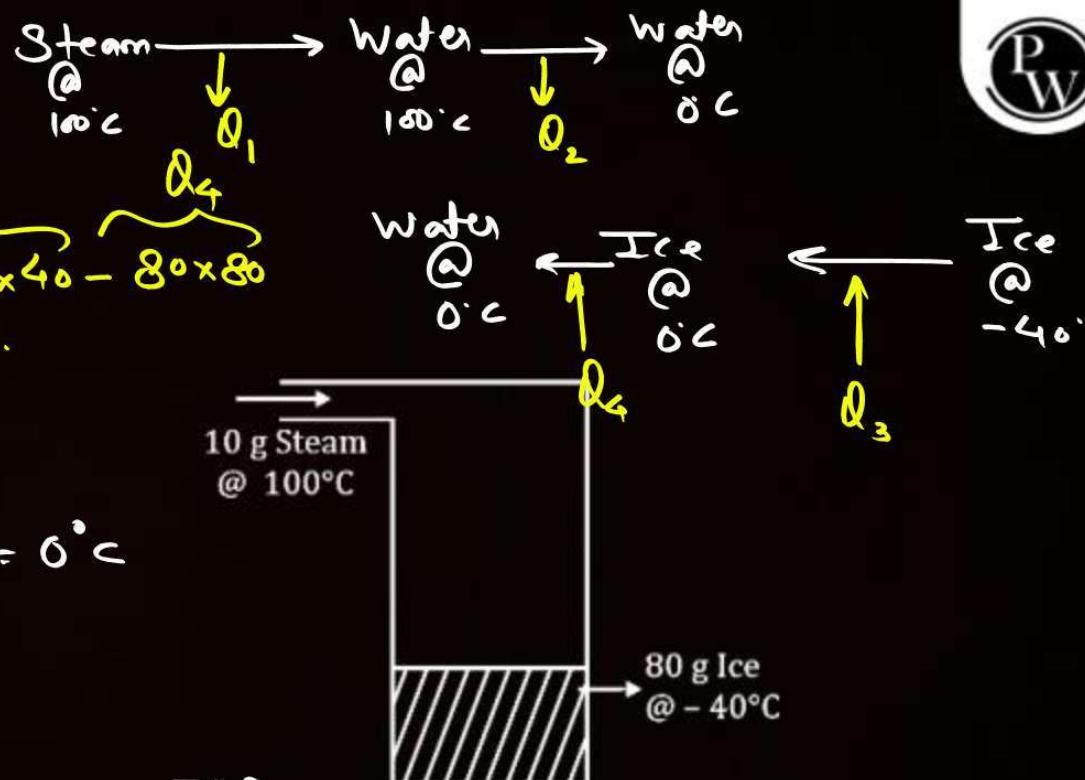
$$= \cancel{10 \times 640} - 1600 - \cancel{6400}$$

$$Q_{\text{left}} = -1600 \text{ cal} \quad | \quad T_{\text{final}} = 0^\circ\text{C}$$

$$m_{\text{ice}} = \frac{1600}{80}$$

$$\text{m}_{\text{ice}} = 20 \text{ g}$$

$$m_{\text{water}} = 90 - 20 = 70 \text{ g}$$



QUESTION (JEE Mains – Sep. 03, 2020 (II))

A calorimeter of water equivalent 20 g contains 180 g of water at 25°C. 'm' grams of steam at 100°C is mixed in it till the temperature of the mixture is 31°C. The value of 'm' is close to (Latent heat of water = 540 cal g⁻¹, specific heat of water = 1 cal.g⁻¹ °C⁻¹)

A 2

^{m g}
Steam → Water
@ 100°C @ 31°C

B 4

C 3.2

D 2.6

(180+20) g
water
@ 25°C

20 g water @ 25°C

$$\mathcal{Q}_{\text{loss}} = \mathcal{Q}_{\text{gain}}$$

$$m \times 540 + m \times 1 \times (100 - 31) = 200 \times 1 \times (31 - 25)$$

$$m \times (540 + 69) = 200 \times 6$$

$$m = \frac{1200}{609}$$



QUESTION (JEE Mains – Sep. 04, 2020 (I))

$$\frac{1700}{210} = 85 \text{ cal}$$

$$\frac{3.4 \times 10^5 \times}{4.2 \times 1000} \frac{\text{cal}}{\text{kg}} = \frac{340}{42} = \frac{340}{42}$$



The specific heat of water = $4200 \text{ J kg}^{-1} \text{ K}^{-1}$ and the latent heat of ice = $3.4 \times 10^5 \text{ J kg}^{-1}$.
 100 grams of ice at 0°C is placed in 200 g of water at 25°C . The amount of ice that will melt as the temperature of water reaches 0°C is close to (in grams):

- A** 61.7
- B** 63.8
- C** 69.3
- D** 64.6

$$Q_{\text{left}} = 200 \times 25 - 100 \times 85$$

$$= 5000 - 8500$$

$$Q_{\text{left}} = -3500$$

$$m_{\text{ice}} = \frac{-3500}{85} = \frac{700}{17} =$$

mass of ice melted -

$$100 - \frac{700}{17}$$

$$\frac{1700 - 700}{17}$$

$$= \frac{1000}{17}$$

$$= 5$$

QUESTION (JEE Mains – NA 7 Jan. 2020 II)

M grams of steam at 100°C is mixed with 200 g of ice at its melting point in a thermally insulated container. If it produces liquid water at 40°C [heat of vaporization of water is 540 cal/g and heat of fusion of ice is 80 cal/g], the value of M is $40g$.

$$\begin{array}{l} \text{Heat lost} \\ \text{by} \\ \text{steam} \end{array} = \begin{array}{l} \text{Heat gained} \\ \text{by} \\ \text{ice} \end{array}$$

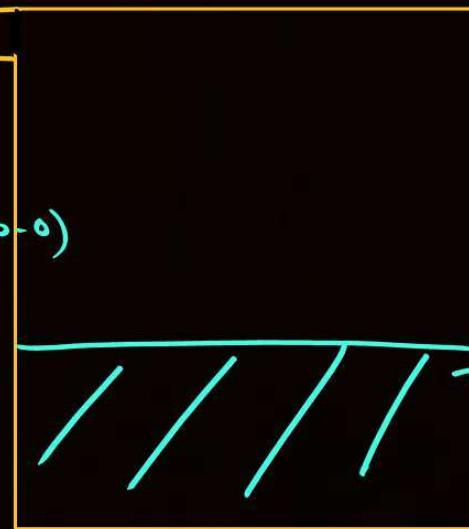
$\xrightarrow{\hspace{1cm}}$

 $m \text{ g steam}$
 $@ 100^\circ\text{C}$

$$m \times 540 + m \times 1 \times (100 - 40) = 200 \times 80 + 200 \times 1 \times (40 - 0)$$

$$\begin{aligned} 600m &= 16000 + 800 \\ &\quad - \underline{24000} = 400 \\ &\quad \cancel{-} \cancel{24000} = 400 \end{aligned}$$

T_{final}



200 g ice
 $@ 0^\circ\text{C}$

QUESTION (JEE Mains – 12 April 2019 I)

When M_1 gram of ice at -10°C (Specific heat = $0.5 \text{ cal g}^{-1} \text{ }^\circ\text{C}^{-1}$) is added to M_2 gram of water at 50°C , finally no ice is left and the water is at 0°C . The value of latent heat of ice, in cal g^{-1} is:

$$\text{Heat absorbed by ice} = \text{Heat lost by water}.$$

A $\frac{50M_2}{M_1} - 5$

$$M_1 \times \frac{1}{2} \times (10 - 0) + M_1 L = M_2 \times 1 \times 50$$

B $\frac{5M_1}{M_2} - 50$

$$5M_1 + L M_1 = 50M_2$$

C $\frac{50M_2}{M_1}$

$$(5 + L) M_1 = 50M_2$$

D $\frac{5M_2}{M_1} - 5$

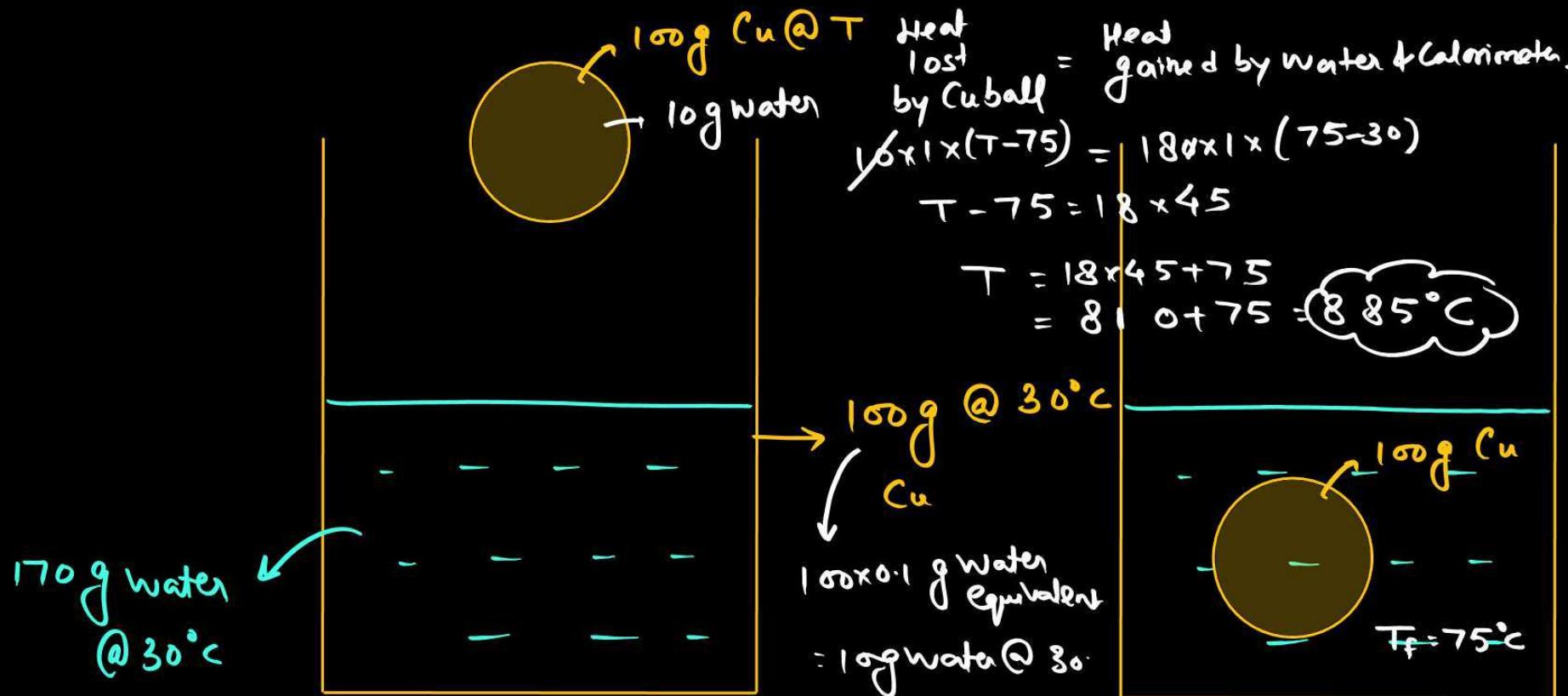
$$L = \frac{50M_2}{M_1} - 5$$

QUESTION (JEE Mains – 2017)

A copper ball of mass 100 gm is at a temperature T . It is dropped in a copper calorimeter of mass 100 gm, filled with 170 gm of water at room temperature. Subsequently, the temperature of the system is found to be 75°C. T is given by

(Given : room temperature = 30°C, specific heat of copper = 0.1 cal/gm°C)

- A** 1250°C
- B** 825°C
- C** 800°C
- D** 885°C



QUESTION (JEE Mains – Online April 8, 2017)



In an experiment a sphere of aluminium of mass 0.20 kg is heated upto 150°C. Immediately, it is put into water of volume 150 cc at 27°C kept in a calorimeter of water equivalent to 0.025 kg. Final temperature of the system is 40°C. The specific heat of aluminium is: (take 4.2 Joule=1 calorie)

25g

A $378 \text{ J/kg} - \text{ }^{\circ}\text{C}$

B $315 \text{ J/kg} - \text{ }^{\circ}\text{C}$

C $476 \text{ J/kg} - \text{ }^{\circ}\text{C}$

D $434 \text{ J/kg} - \text{ }^{\circ}\text{C}$

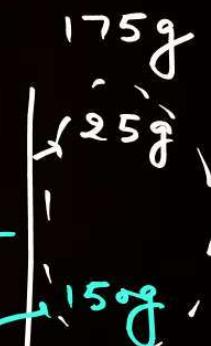
Heat lost by Al = Heat gained by Water

$$200 \times 8 \times (150 - 40) = 175 \times 1 \times (40 - 27)$$

$$S = \frac{175 \times 13}{200 \times 110} = \frac{13 \times 7}{110 \times 8} \text{ Cal/g } ^{\circ}\text{C}$$

200g Al

150g water



QUESTION



A ball of mass m falls from height 240 m. If after hitting the ground, entire K.E. of balls gets converted into thermal energy which heats up the ball. Find the change in temp. of ball ($S = 0.2 \text{ cal/g}^\circ\text{C}$)

$$\begin{aligned}
 & \text{Diagram: A ball of mass } m \text{ falls from height } 240 \text{ m.} \\
 & \text{Equation: } \frac{m}{g^\circ\text{C}} = \frac{0.2 \text{ cal}}{g^\circ\text{C}} \\
 & \quad 0.2 \times \frac{4.2 \text{ J}}{10^{-3} \text{ kg K}} \\
 & \quad 0.84 \times 10^3 \text{ J/kg K} \\
 & \quad 840 \\
 & \text{Equation: } k\epsilon = mgH \\
 & \quad \text{where } k\epsilon = \text{kinetic energy}
 \end{aligned}$$

$$mgH = mS\Delta T$$

$$\Delta T = \frac{gH}{S}$$

Common mistake.

$$\Delta T = \frac{10 \times 240}{0.2}$$

$$\Delta T = 12,000^\circ\text{C}$$

$$\Delta T = \frac{gH}{S} \times 10^6$$

$$= \frac{10 \times 240}{0.2} \times 10^6$$

$$= \frac{80 \times 10^6}{2} = \frac{20}{7}^\circ\text{C}$$

Ans



Share your JEE Reg. details

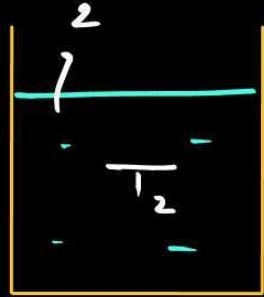
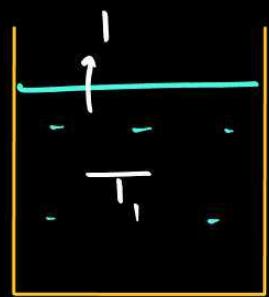
https://bit.ly/JEE_24Fa

QUESTION (JEE Mains – Jan. 08, 2020 (II))

Three containers C_1 , C_2 and C_3 have water at different temperatures. The table below shows the final temperature T when different amounts of water (given in liters) are taken from each container and mixed (assume no loss of heat during the process)

The value of θ (in $^{\circ}\text{C}$ to the nearest integer) is ____.

C_1	C_2	C_3	T
1l	2l	-	60°C
-	1l	2l	30°C
2l	-	1l	60°C
1l	1l	1l	θ



$$C_1: \frac{1 \times 1 \times T_1 + 2 \times 1 \times T_2}{3}$$
$$3 \times 60 = T_1 + 2T_2 - 0$$

$$C_2: \frac{1 \times T_2 + 2 \times T_3}{3}$$
$$T_2 + 2T_3 = 90 - ②$$

$$\frac{2T_1 + T_3}{3} = 60$$
$$2T_1 + T_3 = 180 - ③$$



$$\begin{array}{rcl} T_1 + 2T_2 & = 180 & - \textcircled{1} \\ T_2 + 2T_3 & = 90 & - \textcircled{2} \\ 2T_1 & + T_3 & = 180 - \textcircled{3} \\ \hline 3T_1 + 3T_2 + 3T_3 & = 450 \end{array}$$

$$\theta = \frac{T_1 + T_2 + T_3 = 150}{3}$$

$\theta = 50$

QUESTION (JEE Mains – Jan. 11, 2019 (II))

A metal ball of mass 0.1 kg is heated upto 500°C and dropped into a vessel of heat capacity 800 JK^{-1} and containing 0.5 kg water. The initial temperature of water and vessel is 30°C . What is the approximate percentage increment in the temperature of the water? [Specific heat Capacities of water and metal are, respectively $4200 \text{ J kg}^{-1} \text{ K}^{-1}$ and $400 \text{ J kg}^{-1} \text{ K}^{-1}$]

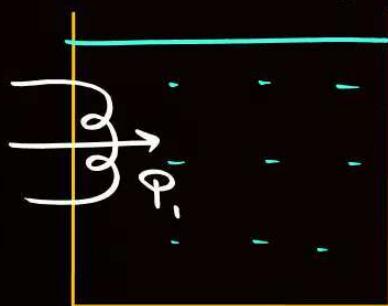
- A** 15 %
- B** 30 %
- C** 25 %
- D** 20 %

QUESTION (JEE Mains – June. 29, 2022 (I))



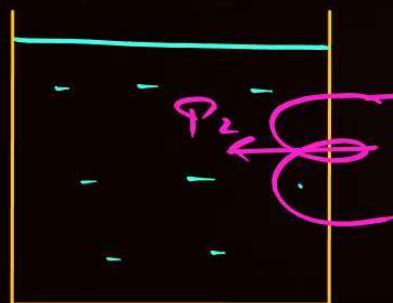
Two coils require 20 minutes and 60 minutes respectively to produce same amount of heat energy when connected separately to the same source. If they are connected in parallel arrangement to the same source; the time required to produce same amount of heat by the combination of coils, will be ____ min.

$$Q = \text{Heat req.}$$



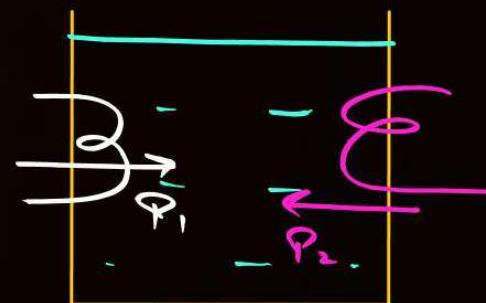
$$\frac{1}{T_1} = \frac{Q}{\Phi_1}$$

$$\Phi_1 = \frac{Q}{T_1}$$



$$\frac{1}{T_2} = \frac{Q}{\Phi_2}$$

$$\Phi_2 = \frac{Q}{T_2}$$



$$\frac{1}{T} = \frac{Q}{\Phi_1 + \Phi_2} \Rightarrow T = \frac{Q}{\frac{Q}{T_1} + \frac{Q}{T_2}}$$

$$\begin{aligned} \frac{1}{T} &= \frac{1}{T_1} + \frac{1}{T_2} \\ &= \frac{1}{30} + \frac{1}{60} \\ T &= 20 \text{ min} \end{aligned}$$

QUESTION (JEE Mains – JEE Adv, 2019)

$T = \text{temp}$
 $t = \text{time}$



A current carrying wire heats a metal rod. The wire provides a constant power (P) to the rod. The metal rod is enclosed in an insulated container. It is observed that the temperature (T) in the metal rod changes with time (t) as:

$$T(t) = T_0(1 + \beta t^{1/4})$$

$$T = T_0 + T_0 \beta t^{1/4}$$

$$T_0 \beta t^{1/4} = T - T_0$$

Where β is a constant with appropriate dimension while T_0 is a constant with dimension of temperature. The heat capacity of the metal is

A

$$\frac{4P(T(t)-T_0)^3}{\beta^4 T_0^4}$$

C

$$\frac{4P(T(t)-T_0)^4}{\beta^4 T_0^5}$$

B

$$\frac{4P(T(t)-T_0)}{\beta^4 T_0^2}$$

D

$$\frac{4P(T(t)-T_0)^2}{\beta^4 T_0^3}$$

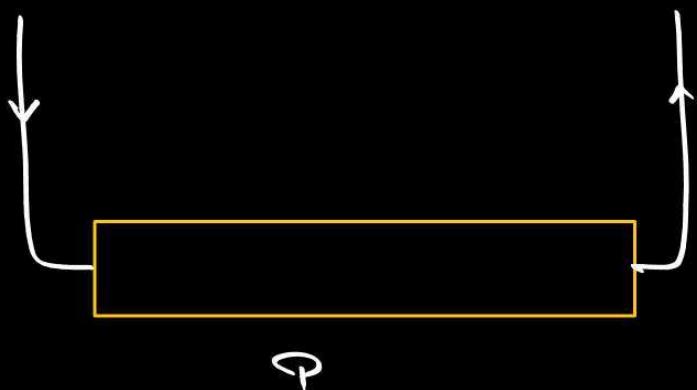
$$dQ = C dT$$

$$P dt = C dT$$

$$C = \frac{P}{dT/dt}$$

$$t^{1/4} = \frac{T - T_0}{\beta T_0}$$

$$t^{3/4} = \left[\frac{T - T_0}{\beta T_0} \right]^3$$



Heat supplied by wire in t sec.

$$Q = \varphi \times t$$

$$T = T_0 \left(1 + \beta T^{\frac{1}{4}} \right)$$

$$\frac{dT}{dt} = T_0 \times \beta \times \frac{1}{4} T^{-\frac{3}{4}}$$

$$\begin{aligned} C &= \frac{\varphi}{\left(\frac{dT}{dt} \right)} = \frac{\varphi}{\frac{T_0 \beta}{4} t^{-\frac{3}{4}}} \\ &= \frac{4 \varphi t^{\frac{3}{4}}}{T_0 \beta} \\ &= \frac{4 \varphi}{T_0 \beta} \left[\frac{T - T_0}{\beta t} \right]^{\frac{3}{4}} \end{aligned}$$

$$\frac{4 \varphi}{T_0^{\frac{1}{4}} \beta^{\frac{1}{4}}}$$

QUESTION (JEE Mains – Jan. 31, 2023 (II))



A water heater of power 2000 W is used to heat water. The specific heat capacity of water is $4200 \text{ J kg}^{-1} \text{ K}^{-1}$. The efficiency of heater is 70%, Time required to heat 2 kg of water from 10°C to 60°C is _____ S.

(Assume that the specific heat capacity of water remains constant over the temperature range of the water).

$$\begin{aligned}\text{Power delivered} &= 70\% \text{ of rated power} \\ &= 0.7 \times 2000 \\ &= 1400 \frac{\text{J}}{\text{s}}.\end{aligned}$$

$$\begin{aligned}Q &= m s \Delta T \\ Q \times t &= m s \Delta T \\ 1400 \times t &= 2 \times 4200 \times 50 \\ t &= \frac{84000}{1400} \\ t &= 300 \text{ s.}\end{aligned}$$

QUESTION (JEE Mains – June. 25, 2022 (II))

A copper block of mass $\underline{5.0 \text{ kg}}$ is heated to a temperature of 500°C and is placed on a large ice block. What is the maximum amount of ice that can melt? [Specific heat of copper: $0.39 \text{ J g}^{-1} \text{ }^\circ\text{C}^{-1}$ and latent heat of fusion of water: $335 \text{ J g}^{-1} \text{ }^\circ\text{C}^{-1}$]

- A** 1.5 kg
- B** 5.8 kg
- C** 2.9 kg
- D** 3.8 kg

$$T_f = 0^\circ\text{C}$$

*Heat supplied = Heat absorbed
by Cu by ice.*

$$5000 \times 0.39 \times (500 - 0) = m \times 335$$

$$5000 \times 39 \times 5 = m \times 335$$

$$m = \frac{500 \times 5 \times 39}{335} \text{ gram.}$$

$$= \frac{335}{335 \times 1000} \text{ kg} = \frac{195}{675} \text{ kg}$$

QUESTION (JEE Mains – Aug. 26, 2021 (II)) $s_1 \ s_2 \ s_3$ 

The temperature of equal masses of three different liquids x , y and z are 10°C , 20°C and 30°C respectively. The temperature of mixture when x is mixed with y is 16°C and that when y is mixed with z is 26°C . The temperature of mixture when x and z are mixed will be:

- A** 28.32°C
- B** 23.84°C
- C** 25.62°C
- D** 20.28°C

QUESTION (JEE Mains – Aug. 27, 2021 (II))

The height of victoria falls is 63 m. What is the difference in temperature of water at the top and at the bottom of fall?

[Given 1 cal = 4.2 J and specific heat of water = 1 cal g⁻¹ °C⁻¹]

$$\cancel{mgh = ms \Delta T}$$

- A** 0.147 °C
- B** 14.76 °C
- C** 1.476 °C
- D** 0.014 °C

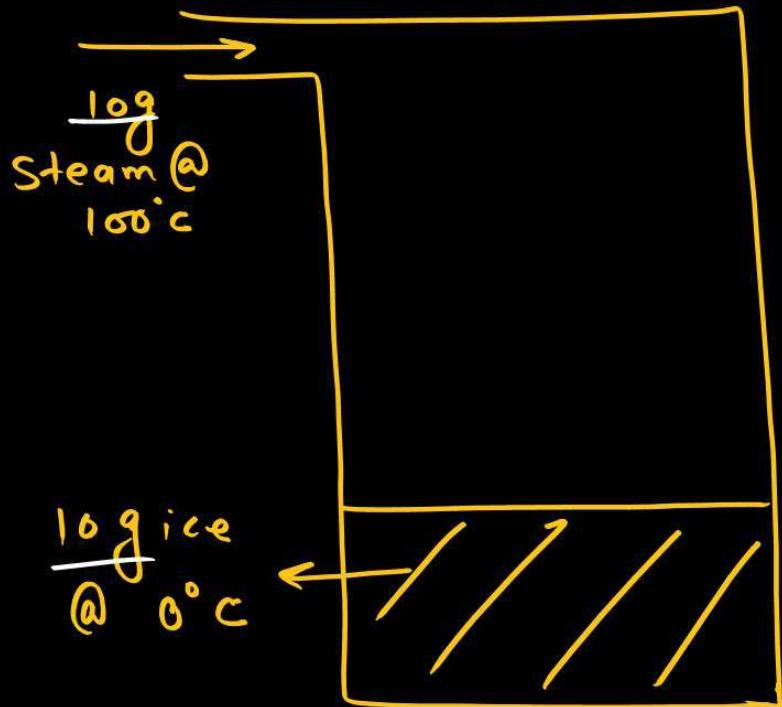
QUESTION (JEE Mains – July. 25, 2022 (II))

A block of ice of mass 120 g at temperature 0°C is put in 300 g of water at 25°C . The $x\text{g}$ of ice melts as the temperature of the water reaches 0°C . The value of x is _____. [Use specific heat capacity of water = $4200 \text{ J kg}^{-1} \text{ K}^{-1}$, Latent heat of ice = $3.5 \times 10^5 \text{ J kg}^{-1}$]



Q. Find final temp & comp.

$$T_f = 100^\circ C$$



$$Q_{\text{left}} = 10 \times 540 + 10 \times 1 \times 100 - 10 \times 80$$

$$= 10 \times 640 - 800$$

$$= 6400 - 800$$

$$Q_{\text{left}} = 5600 \text{ cal}$$

$$Q_{\text{left}} = m s \Delta T$$

$$5600 = 2 \times 1 \times (T - 0)$$

$$T = \frac{560}{2} = 280^\circ C > 100^\circ C$$

$$\begin{aligned} Q &= m s \Delta T \\ &= 2 \times 1 \times 100 \\ &= 2000 \text{ cal.} \end{aligned}$$

$$Q_{\text{left}} = 5600 - 2000 = 3600 \text{ cal}$$

$$m_{\text{steam}} = \frac{Q_{\text{left}}}{540} = \frac{3600}{540} \text{ g.}$$

QUESTION (JEE Mains – Sep. 05, 2020 (I))

A bullet of mass 5g, traveling with a speed of 210 m/s, strikes a fixed wooden target. One half of its kinetic energy is converted into heat in the bullet while the other half is converted into heat in the wood. The rise of temperature of the bullet if the specific heat of its material is $0.030 \text{ cal}/(\text{g} - \text{ }^{\circ}\text{C})$ ($1 \text{ cal} = 4.2 \times 10^7 \text{ ergs}$) close to:

A 83.3°C

$$\text{S} = 0.030 \times \frac{4.2 \text{ J}}{\text{g} \cdot \text{C}}$$

$$\begin{array}{c} m = 5\text{g} \\ \rightarrow \\ 210 \text{ m/s} \end{array}$$

B 38.4°C

C 87.5°C

D 119.2°C



$$k \cdot \epsilon = \frac{1}{2} m v^2$$

$$m s \Delta T = \frac{1}{2} k \cdot \epsilon$$

~~$$m s \Delta T = \frac{1}{4} m v^2$$~~

$$\Delta T = \frac{v^2}{4s}$$

QUESTION (JEE Mains – JEE Adv, 2019)



A liquid at 30°C is poured very slowly into a Calorimeter that is at temperature of 110°C . The boiling temperature of the liquid is 80°C . It is found that the first 5 gm of the liquid completely evaporates. After pouring another 80 gm of the liquid the equilibrium temperature is found to be 50°C . The ratio of the Latent heat of the liquid to its specific heat will be _____ $^{\circ}\text{C}$. [Neglect the heat exchange with surrounding]



Heat absorbed by liq. = Heat released by Calorimeter.

$$\text{Q} = 5 \times S \times (80 - 30) + 5 \times L = C \times (110 - 80)$$

$$\Rightarrow 250S + 5L = 30^\circ\text{C}$$

$$\Rightarrow 50S + L = 6^\circ\text{C} \quad \text{--- (1)}$$

Heat abs. by liq. = Heat supplied by Cal

$$80 \times S \times (50 - 30) = C \times (80 - 50)$$

$$80 \times S \times 20 = 30^\circ\text{C}$$

$$160S = 30^\circ\text{C}$$

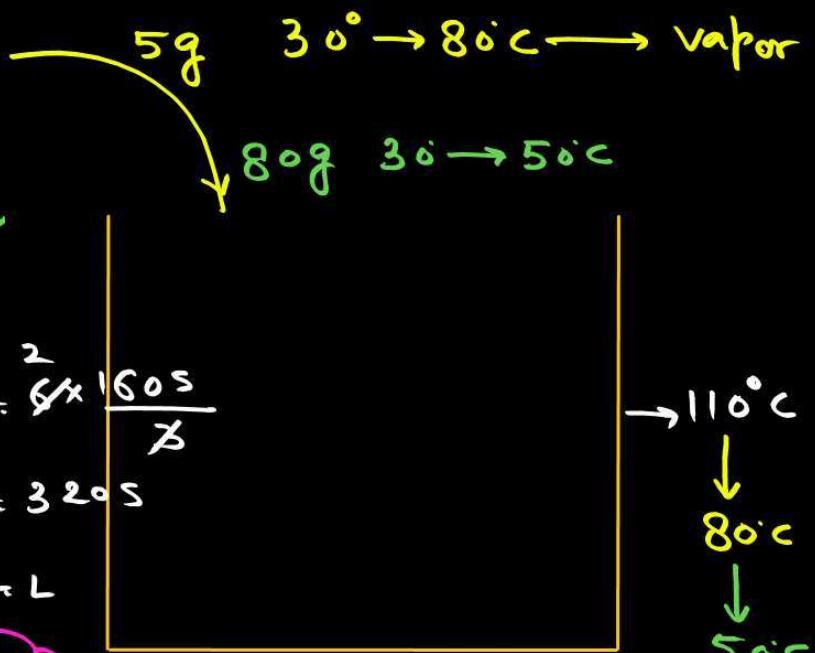
$$\therefore C = \frac{160S}{3} \quad \text{--- (2)}$$

$$\begin{aligned} 50S + L &= \frac{6 \times 160S}{3} \\ 50S + L &= 320S \end{aligned}$$

$$270S = L$$

$$\frac{L}{S} = 270$$

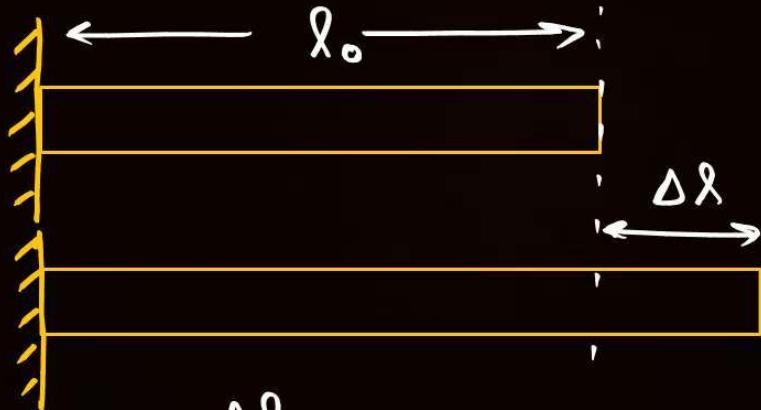
Any





Thermal Expansion

① Linear Thermal Expansion →



fractional change in length of rod $\rightarrow \frac{\Delta l}{l_0} = \alpha \Delta T$

$$\Delta l \propto \Delta T$$

$\propto l_0$ Prop. of material

$$\Delta l = l_0 \propto \Delta T$$

Prop. const.

(Thermal coeff. of linear expansion)

$$l = l_0 + \Delta l$$

Unit of $\alpha = ^\circ C$
 $[\alpha] = [T^{-1}]$

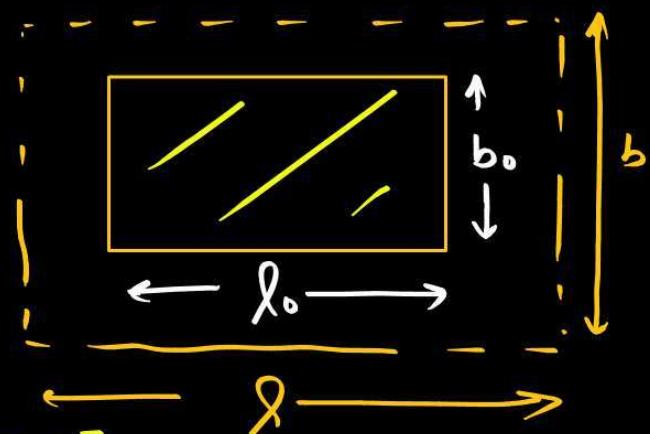
$$= l_0 + \alpha l_0 \Delta T$$

$$l = l_0 (1 + \alpha \Delta T)$$



Usually, α is very small.

② Areal Thermal Expansion \rightarrow



$$\sigma = \sigma_0 [1 - \beta \Delta T]$$

↓
Area density.

$$\Delta A = \beta A_0 \Delta T$$

$$\frac{\Delta A}{A_0} = \beta \Delta T$$

$$A_0 = l_0 b_0$$

$$A = l b$$

$$A = l_0 (1 + \alpha \Delta T) b_0 (1 + \alpha \Delta T)$$

$$A = l_0 b_0 (1 + \alpha \Delta T)^2$$

$$A = A_0 (1 + \underbrace{\alpha \Delta T}_{\text{very small}})^2$$

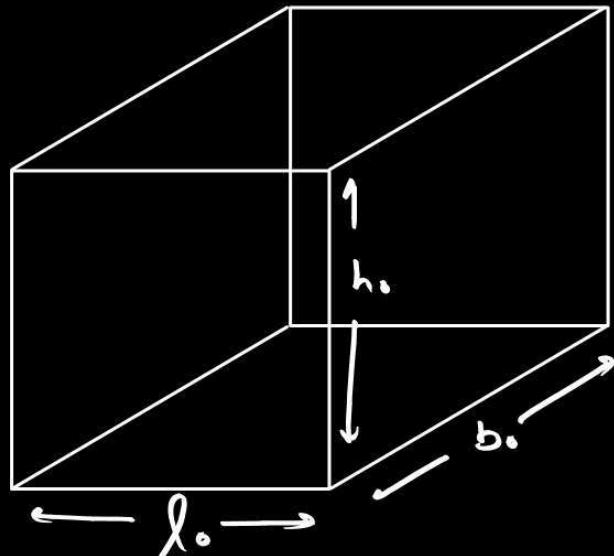
$$A = A_0 (1 + 2\alpha \Delta T)$$

$$A = A_0 (1 + \beta \Delta T)$$

\downarrow
Th. Coeff. of areal expansion
 $(\beta = 2\alpha)$

③ Volumetric Thermal Expansion \rightarrow

$$\gamma_0 = \frac{M}{V_0}$$



$$V = V_0(1 + \gamma \Delta T)$$

Th. coeff. of vol. expansion.

$$\gamma = 3\alpha$$

$$\Delta V = V_0 \gamma \Delta T$$

$$\frac{\Delta V}{V_0} = \gamma \Delta T$$

$$\gamma = \frac{M}{V} \Rightarrow \gamma = \frac{M}{V_0(1 + \gamma \Delta T)} = \frac{M}{V_0} (1 + \gamma \Delta T)^{-1}$$

$$\rho = \rho_0 (1 - \gamma \Delta T)$$





Effect on Shape

↓
Thermal Expansion is similar to zooming an image. It does not change the shape of object.

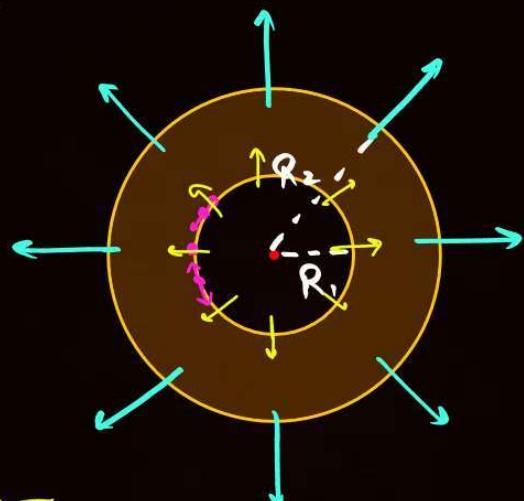


QUESTION

Find the effect of heating on-

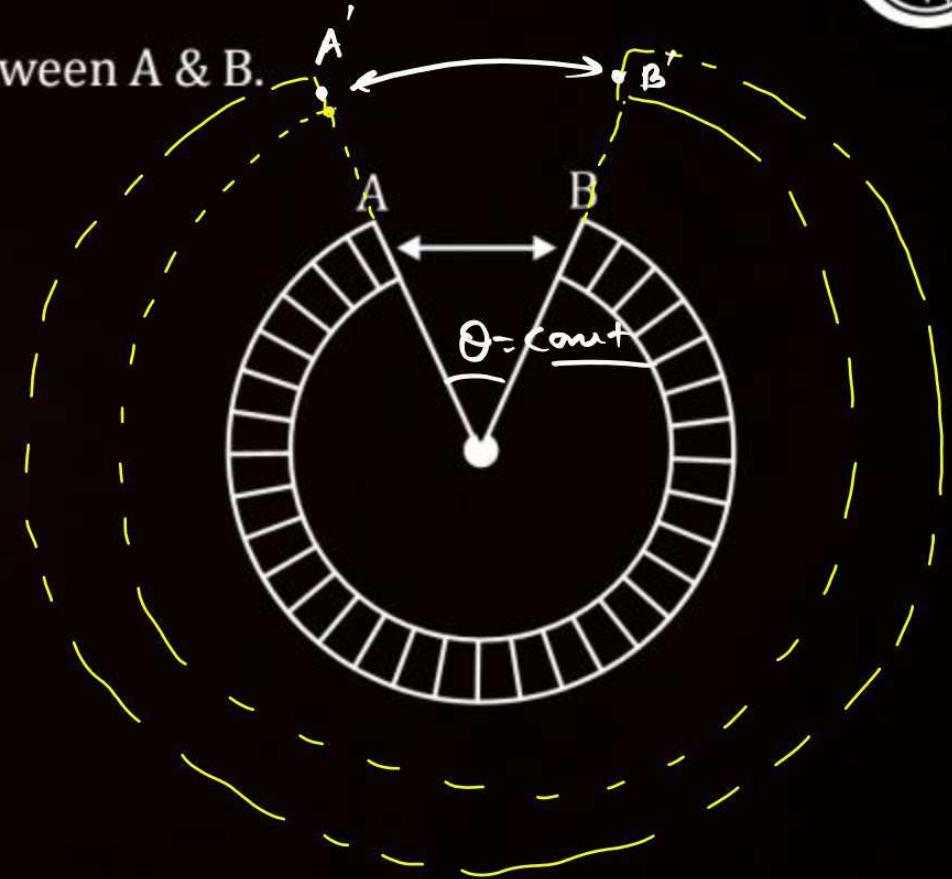
- (1) $R_1 \uparrow$
- (2) $R_2 \uparrow$
- (3) $R_2 - R_1 \uparrow$

$$\begin{aligned} & \lambda = \lambda_0 (1 + \alpha \Delta T) \\ & \Delta \lambda = \lambda_0 \alpha \Delta T \end{aligned}$$



QUESTION

What will be the effect of heating on dist. between A & B.



QUESTION

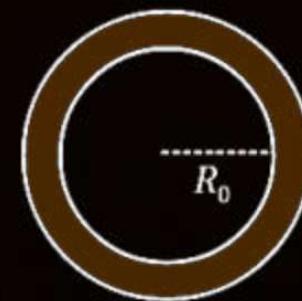
A rod of length l_0 & th. coeff. Of linear expansion α is bent to form a ring. If the ring is now heated, Find the change in radius of ring & area of ring (change in temp = ΔT).

$$l = l_0 (1 + \alpha \Delta T)$$

~~$$2\pi R = 2\pi R_0 (1 + \alpha \Delta T)$$~~

$$R = R_0 (1 + \alpha \Delta T)$$

$$A = A_0 (1 + 2\alpha \Delta T)$$



QUESTION~~0.8 m~~

An iron rim of radius ~~0.8~~ m is to be fitted on a wooden wheel of radius 1m. Find the temp. change in iron to perfectly fit the wooden wheal ($\alpha_{\text{iron}} = 0.002/\text{ }^{\circ}\text{C}$)

$$R = R_0(1 + \alpha \Delta T)$$

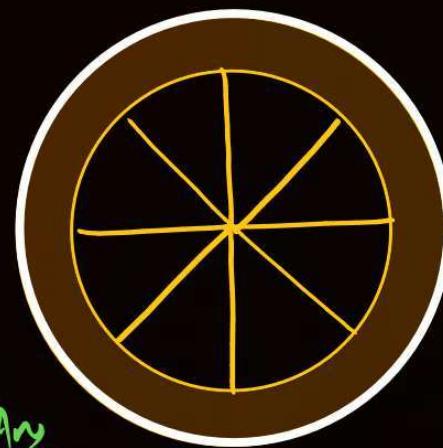
$$1 = 0.8(1 + 0.002 \times \Delta T)$$

$$\frac{1}{0.8} = 1 + 0.002 \Delta T$$

$$\frac{1}{4} = 0.002 \Delta T$$

$$\Delta T = \frac{1}{4 \times 0.002} = \frac{1000}{8} = \frac{500}{4}$$

$$\Delta T = 125\text{ }^{\circ}\text{C}$$



QUESTION (JEE Mains – Jan 24, 2023 (I))

$$\Delta T = 177 - 27 = 150^\circ\text{C}$$



A hole is drilled in a metal sheet. At 27°C , the diameter of hole is 5 cm. When the sheet is heated to 177°C , the change in the diameter of hole is $d \times 10^{-3} \text{ cm}$. The value of d will be _____ if coefficient of linear expansion of the metal is $1.6 \times 10^{-5}/^\circ\text{C}$.

$$d = d_0(1 + \alpha \Delta T)$$

$$\Delta d = d_0 \alpha \Delta T$$

$$= 5 \times 1.6 \times 10^{-5} \times 150$$

$$= 8 \times 150 \times 10^{-5} \text{ cm}$$

$$= 120 \times 10^{-4} \text{ cm}$$

$$\Delta d = 12 \times 10^{-3} \text{ cm}$$

QUESTION (JEE Mains – Sep. 02, 2020 (II))

$$V = l^3 \Rightarrow \frac{\Delta V}{V} = 3 \times \frac{\Delta l}{l}$$



When the temperature of metal wire is increase from 0°C to 10°C , its length increase by 0.02%. The percentage change in its mass density will be closed to:

- A** 0.008
- B** 0.8
- C** 0.06
- D** 2.3

$$\rho = \frac{m}{V}$$

$$\frac{\Delta l}{l} = 0.02\%$$

$$\frac{\Delta \rho}{\rho} = -\frac{\Delta V}{V}$$

$$= -0.06\%$$

$$\frac{\Delta V}{V} = 3 \times 0.02\% \\ = 0.06\%$$

QUESTION (JEE Mains – Sep. 05, 2020 (II))

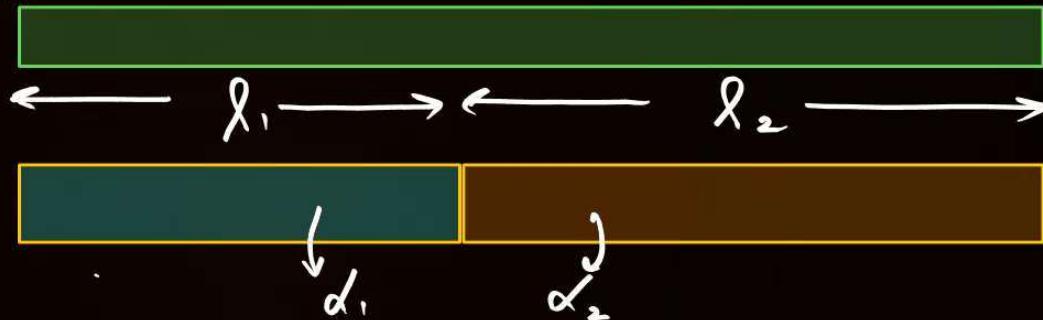
Two different wires having lengths L_1 and L_2 and respective temperature coefficient of linear expansion α_1 and α_2 , are joined end-to-end. Then the effective temperature coefficient of linear expansion is

A $\sqrt[2]{\alpha_1 \alpha_2}$

B $\frac{4\alpha_1 \alpha_2}{\alpha_1 + \alpha_2} \frac{L_2 L_1}{(L_2 + L_1)^2}$

C $\frac{\alpha_1 + \alpha_2}{2}$

D $\frac{\alpha_1 L_1 + \alpha_2 L_2}{L_1 + L_2}$



$$\Delta l_{\text{total}} = \Delta l_1 + \Delta l_2$$

$$(l_1 + l_2) \alpha_{\text{eq}} \Delta T = l_1 \alpha_1 \Delta T + l_2 \alpha_2 \Delta T$$

$$\alpha_{\text{eq}} = \frac{l_1 \alpha_1 + l_2 \alpha_2}{l_1 + l_2}$$



Non-Isotropic Thermal Expansion



$$\gamma = \alpha_1 + \alpha_2 + \alpha_3$$

अलंग - अलंग direction, में α अलंग - अलंग है।

QUESTION (JEE Mains – Jan. 07, 2020 (I))

A non-isotropic solid metal cube has coefficients of linear expansion as: $5 \times 10^{-5} /{}^\circ\text{C}$ along the x-axis and $5 \times 10^{-6} /{}^\circ\text{C}$ along the y and the z-axis. If the coefficient of volume expansion of the solid is $C \times 10^{-6} /{}^\circ\text{C}$ then the value of C is

$$\alpha_x = 5 \times 10^{-5} /{}^\circ\text{C} = 50 \times 10^{-6} /{}^\circ\text{C} \quad \gamma = \alpha_x + \alpha_y + \alpha_z$$

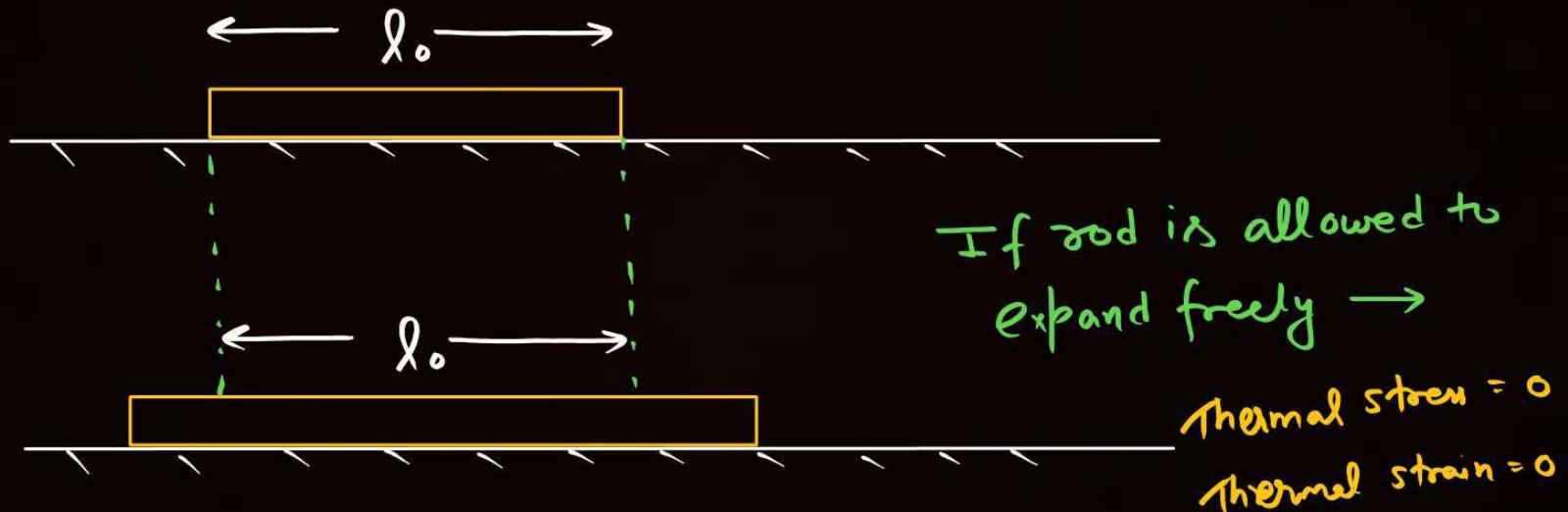
$$\alpha_y = \alpha_z = 5 \times 10^{-6} /{}^\circ\text{C}$$

$$\begin{aligned}\gamma &= 50 \times 10^{-6} + 2 \times 5 \times 10^{-6} \\ &= \underline{\underline{C}} \times 10^{-6} /{}^\circ\text{C}\end{aligned}$$



Thermal Stress and Strain

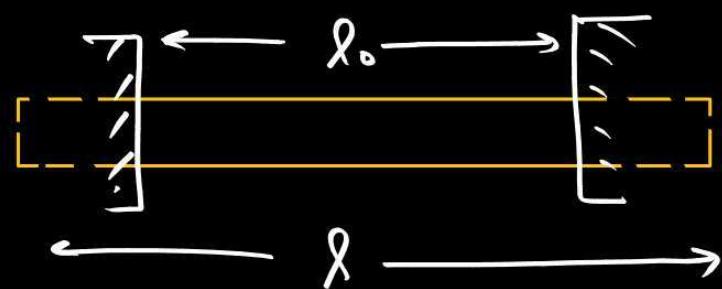
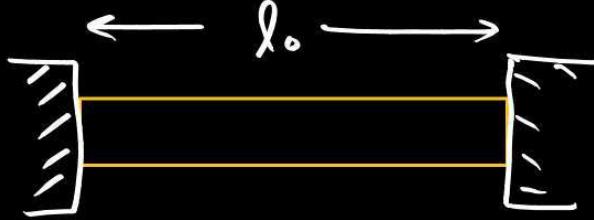
$$\text{Stress} = Y \times \text{Strain}$$



If rod is allowed to
expand freely →

Thermal stress = 0
Thermal strain = 0

$$\frac{\Delta l}{l_0} = \alpha \Delta T$$



→ Rod will be in compression.

Thermal Strain, $\epsilon = \frac{\Delta l}{l} \approx \frac{\Delta l}{l_0}$

Th. Stress = $\gamma \times$ Th. strain

$$\sigma = \gamma \left[\frac{\Delta l}{l_0} \right]$$

* $\sigma = \gamma \alpha \Delta T$



QUESTION (JEE Mains – 1 Sep, 2021 (S-II))



A steel rod with $\gamma = 2.0 \times 10^{11} \text{ Nm}$ and $\alpha = 10^{-5} \text{ }^{\circ}\text{C}^{-1}$ of length 4 m and area of cross-section 10 cm^2 is heated from 0°C to 400°C without being allowed to extend. The tension produced in the rod is $x \times 10^5 \text{ N}$ where the value of x is ____.

$$\sigma_{th.} = \gamma \alpha \Delta T$$

$$\frac{F}{A} = \gamma \alpha \Delta T$$

$$\begin{aligned} f &= \gamma \alpha \Delta T \cdot A \\ &= 2 \times 10^{11} \times 10^{-5} \times 400 \times 10 \times 10^{-4} \\ &= 8 \times 10^5 \text{ N} \end{aligned}$$

QUESTION (JEE Mains – 22 July, 2021 (S-II))



The area of cross-section of a railway track is 0.01 m^2 . The temperature variation is 10°C . Coefficient of linear expansion of material of track is $10^{-5}/^\circ\text{C}$. The energy stored per meter in the track is J/m . (Young's modulus of material of track is 10^{11} m^{-2})

$$\text{Energy density} = \frac{1}{2} \times \text{stress} \times \text{strain}$$

$$\frac{U}{\text{Vol.}} = \frac{1}{2} \times \sigma \times \epsilon$$

$$\frac{U}{l \times A} = \frac{1}{2} \times \sigma \times \epsilon$$

$$\frac{U}{l} = \frac{1}{2} \times \sigma \times \epsilon \times A$$

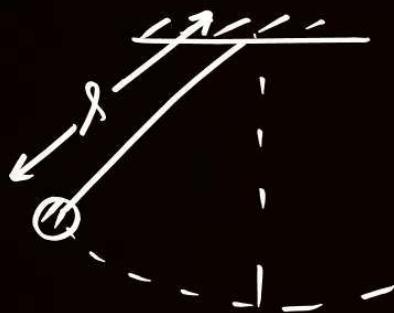
$$\frac{U}{l} = \frac{1}{2} (\gamma \alpha \Delta T) \times (\alpha \Delta T) \times A$$

$$= \frac{1}{2} \gamma \alpha^2 A (\Delta T)^2$$

$$= \frac{1}{2} \times 10^{11} \times (10^{-5})^2 \times 0.01 \times 10^2$$

$$= \frac{10}{2} = \boxed{5 \text{ J/m}}$$

Time Period of Simple Pendulum



$$T = 2\pi \sqrt{\frac{l}{g}}$$

$$\frac{\Delta T}{T} = \frac{1}{2} \left(\frac{\Delta l}{l} \right)$$

$$\frac{\Delta T}{T} = \frac{1}{2} \propto \Delta \theta$$

↓ Temp. change

fractional
Change in
time period of
Simple pendulum.



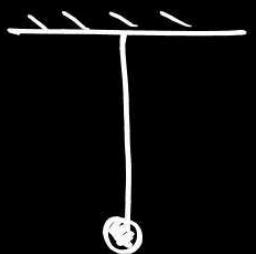
$$y = x^n$$

$$\frac{\Delta y}{y} = n \frac{\Delta x}{x}$$

for small change

$$\frac{\Delta T}{T} \rightarrow 1 \text{ day में कितना change होता है?}$$

$$\frac{\Delta T}{T} \rightarrow 1 \text{ day में कितना change होता है?}$$



Temp.

T_0 → correct time

1 tick → 1 sec

$T > T_0$ → Clock will

1 tick → > 1 sec

become slow & lose time.

$T < T_0$ → Clock will become fast
& will gain time

QUESTION

A clock working on simple pendulum principle is calibrated to run correctly at 10°C . If the clock is operated at 40°C , how much time it will lose/gain in a day? ($\alpha = 0.001/\text{ }^{\circ}\text{C}$)

$$\frac{\Delta T}{T} = \frac{1}{2} \alpha \Delta \theta$$

$$\frac{\Delta T}{T}$$

$$= \frac{1}{2} \times 0.001 \times (40 - 10)$$

$$\frac{\Delta T}{T} = 0.001 \times 15$$

$$\frac{\Delta T}{T} = 1.5 \times 10^{-3}$$

$$\Delta T = 1.5 \times 10^{-3} \times T$$
$$= 1.5 \times 10^{-3} \times 86400 \frac{\text{sec}}{\text{day}}$$

QUESTION



A clock gains 20 sec/day at 5°C & loses 10 sec/day at 35°C . Find temp at which clock will measure time correctly.

Method-1:—

$$\frac{\Delta T}{T_0} = \frac{1}{2} \alpha \Delta \theta$$

$$\frac{\Delta T}{T_0} = \frac{1}{2} \alpha (\theta - \theta_0)$$

$$-20 = \frac{1}{2} \alpha [5 - \theta_0] \quad \text{--- (1)}$$

$$+10 = \frac{1}{2} \alpha [35 - \theta_0] \quad \text{--- (2)}$$

$$\Rightarrow -2 = \frac{5 - \theta_0}{35 - \theta_0}$$

$$\Rightarrow -70 + 2\theta_0 = 5 - \theta_0$$

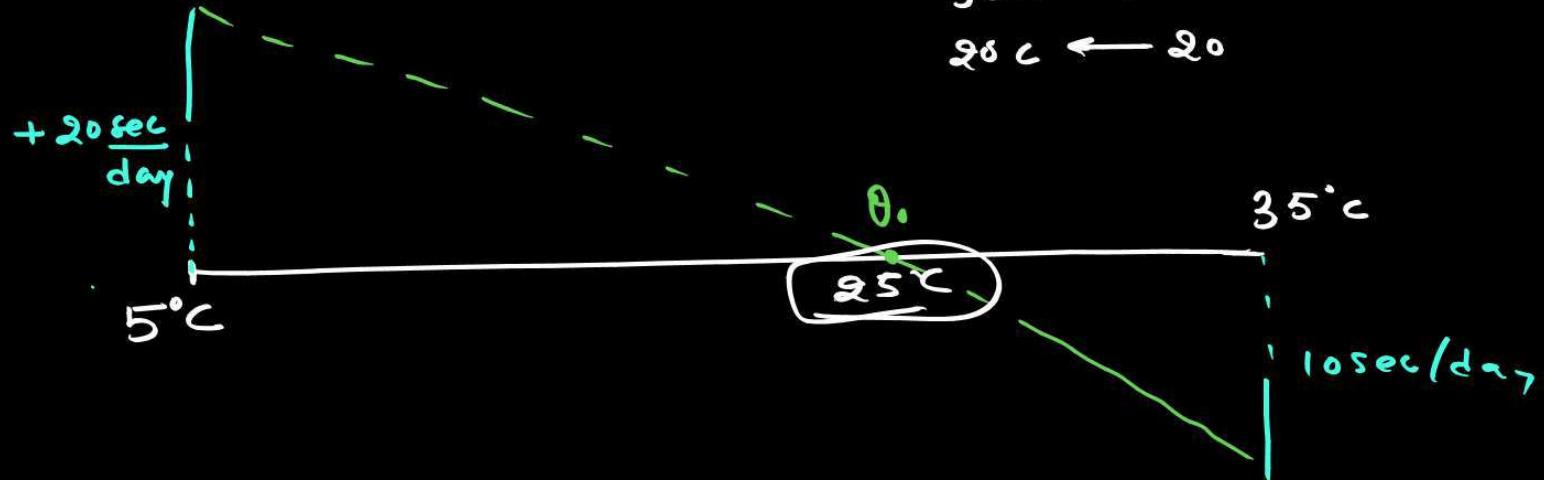
$$3\theta_0 = 75$$

$$\theta_0 = 25^\circ\text{C}$$

Ans

Method-2

$$\frac{\Delta T}{T} = \frac{1}{2} \propto \Delta \theta$$



$$\begin{array}{l} \Delta \theta \\ 30^{\circ}\text{C} \rightarrow 3^{\circ} \\ 20^{\circ}\text{C} \leftarrow 2^{\circ} \end{array}$$



QUESTION



A disc of mass M & radius R_0 is rotating abt. fixed axis passing through center with angle vel ω_0 . If due to change in temp ΔT . The disc expands, find the new angular vel. (Th. Coeff. of linear exp. = α)

$$I_1 \omega_0 = I_2 \omega$$

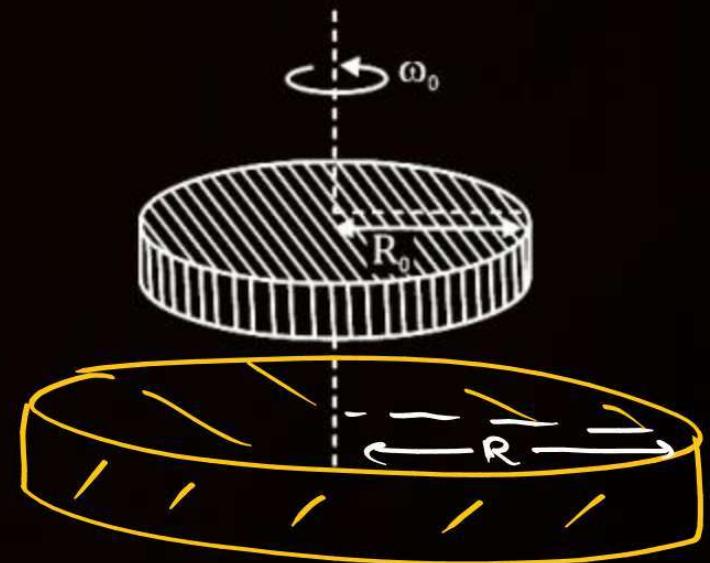
~~$$\frac{1}{2} M R^2 \omega_0 = \frac{1}{2} M [R_0(1+\alpha\Delta T)]^2 \omega$$~~

$$\omega_0 = (1 + \alpha \Delta T)^2 \omega$$

$$\omega = \frac{\omega_0}{(1 + \alpha \Delta T)^2}$$

$$\omega = \omega_0 (1 + \alpha \Delta T)^{-2}$$

Ans.

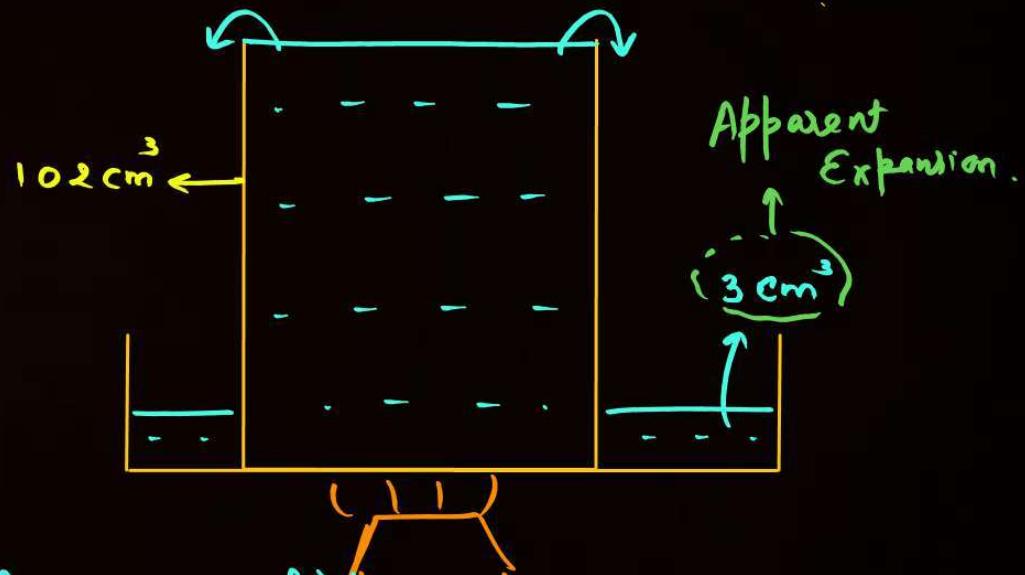
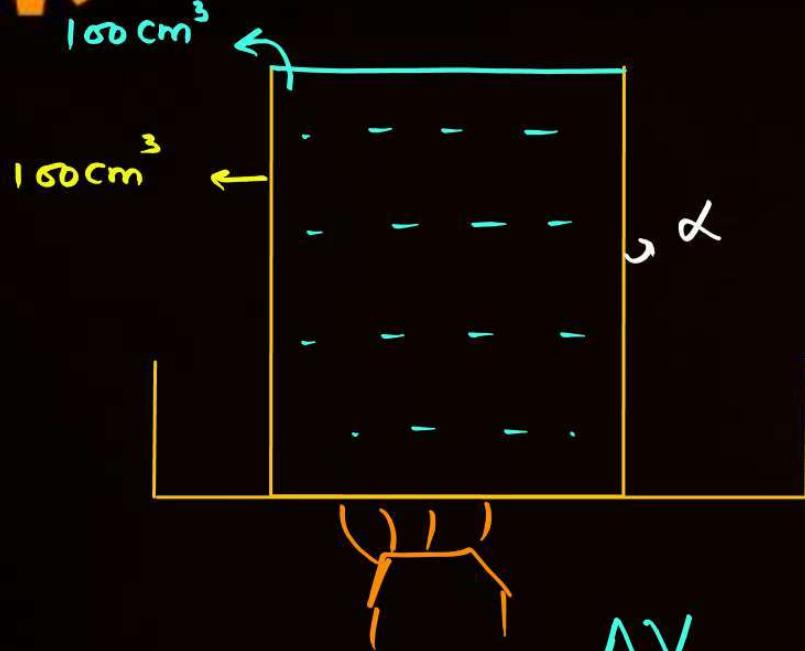




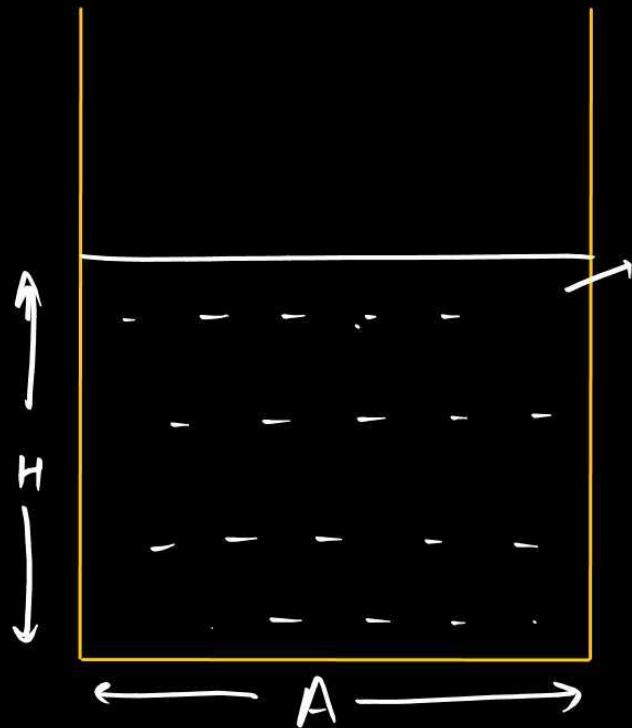
Apparent Expansion of Liquid



$$\gamma_{\text{liq.}} = 3 \alpha_{\text{cont.}} + \gamma_{\text{app.}}$$



$$\Delta V_{\text{actual}} = \Delta V_{\text{contained}} + \Delta V_{\text{apparent}}$$
$$V_0 \gamma \Delta T = V_0 (3\alpha) \Delta T + V_0 \gamma_{\text{app.}} \Delta T$$



$$V = A \cdot H$$

$$V_0(1 + \gamma \Delta T) = A_0(1 + 2\alpha \Delta T)^H$$

$$H = \frac{V_0}{A_0} \left(1 + (\gamma - 2\alpha) \Delta T \right)$$

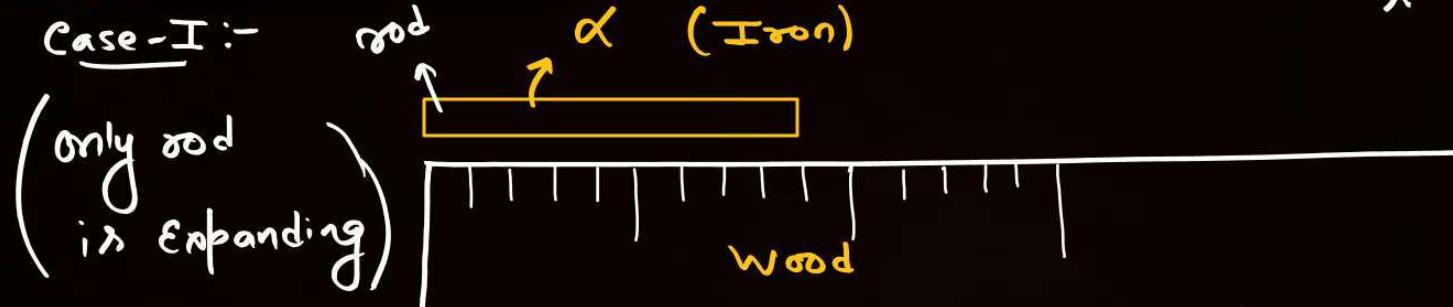
$$H = H_0 \left[1 + (\gamma - 2\alpha) \Delta T \right]$$



Measurement by Scale

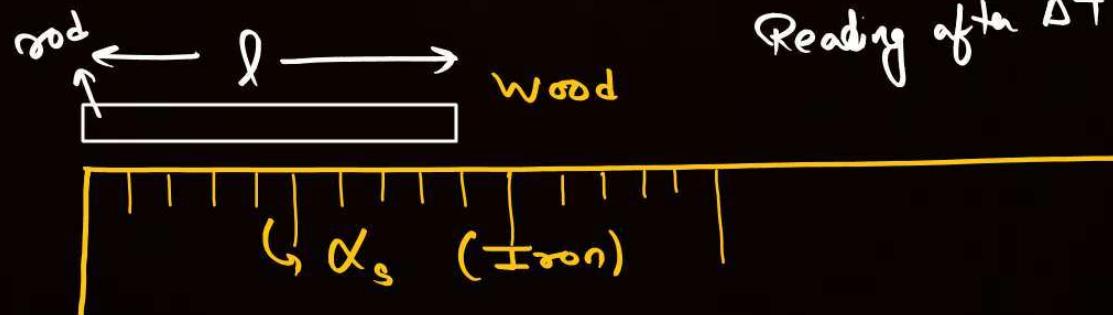


Case-I :-



Case-II :-

(Only scale
is
expanding)



Reading
at temp. $T \rightarrow$

$$l = l_0(1 + \alpha \Delta T)$$

Scale is reading correctly at $T_0 \rightarrow l_0$

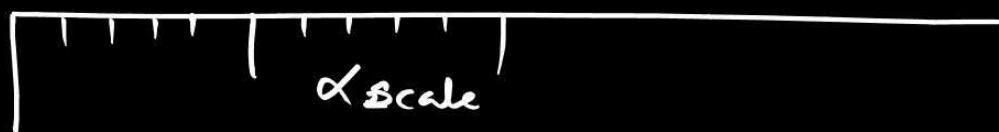
Reading after ΔT temp. increment \rightarrow

$$l = l_0(1 - \alpha_s \Delta T)$$



Case - III

(Both rod &
Scale can
Expand)



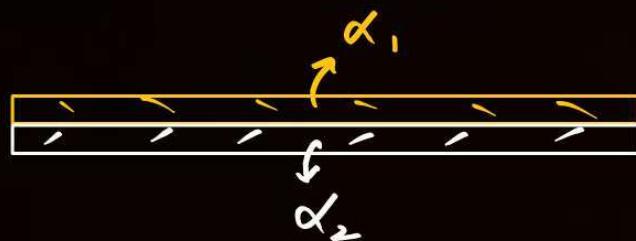
Correct reading at T_0 temp. $\rightarrow l_0$

Reading at temp $T_0 + \Delta T$ \rightarrow

$$l = l_0 [1 + (\alpha_{\text{rod}} - \alpha_{\text{scale}}) \Delta T]$$



Bimetallic Strip



$$\alpha_1 > \alpha_2$$



Strip उस Side bend hogi जिस
तरफ α कम होगा।

QUESTION (JEE Mains – July. 25, 2022 (I))



A unit scale is to be prepared whose length does not change with temperature and remains 20cm, using a bimetallic strip made of brass and iron each of different length. The length of both components would change in such a way that difference between their length remains constant. If length of brass is 40 cm and length of iron will be 60 cm. ($\alpha_{\text{iron}} = 1.2 \times 10^{-5} \text{ K}^{-1}$ and $\alpha_{\text{brass}} = 1.8 \times 10^{-5} \text{ K}^{-1}$).

$$\Delta l_1 - \Delta l_2 = 0$$

$$l_1 \alpha_1 \Delta T = l_2 \alpha_2 \Delta T$$

$$l_1 \alpha_1 = l_2 \alpha_2$$

~~$$40 \times 1.8 \times 10^{-5} = l \times 1.2 \times 10^{-5}$$~~

$$l = \frac{40 \times 1.8}{1.2} = 60 \text{ cm.}$$

$$l_1 - l_2 = \text{const.}$$

$$\Delta l_1 = \Delta l_2$$

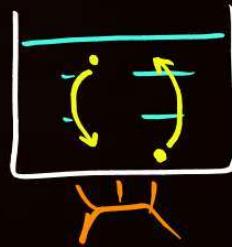
Heat Transfer



Thermal Conduction

- 
- Medium is required.
- only Heat transfer takes place, no matter is transferred
- In Solids.

Convection

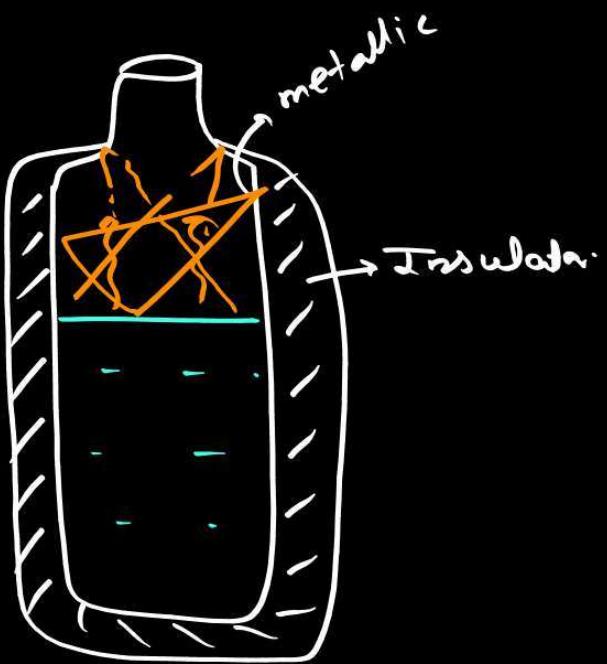


- Medium is required.
- Both mass & energy transfer takes place.
- In fluids

Radiation.

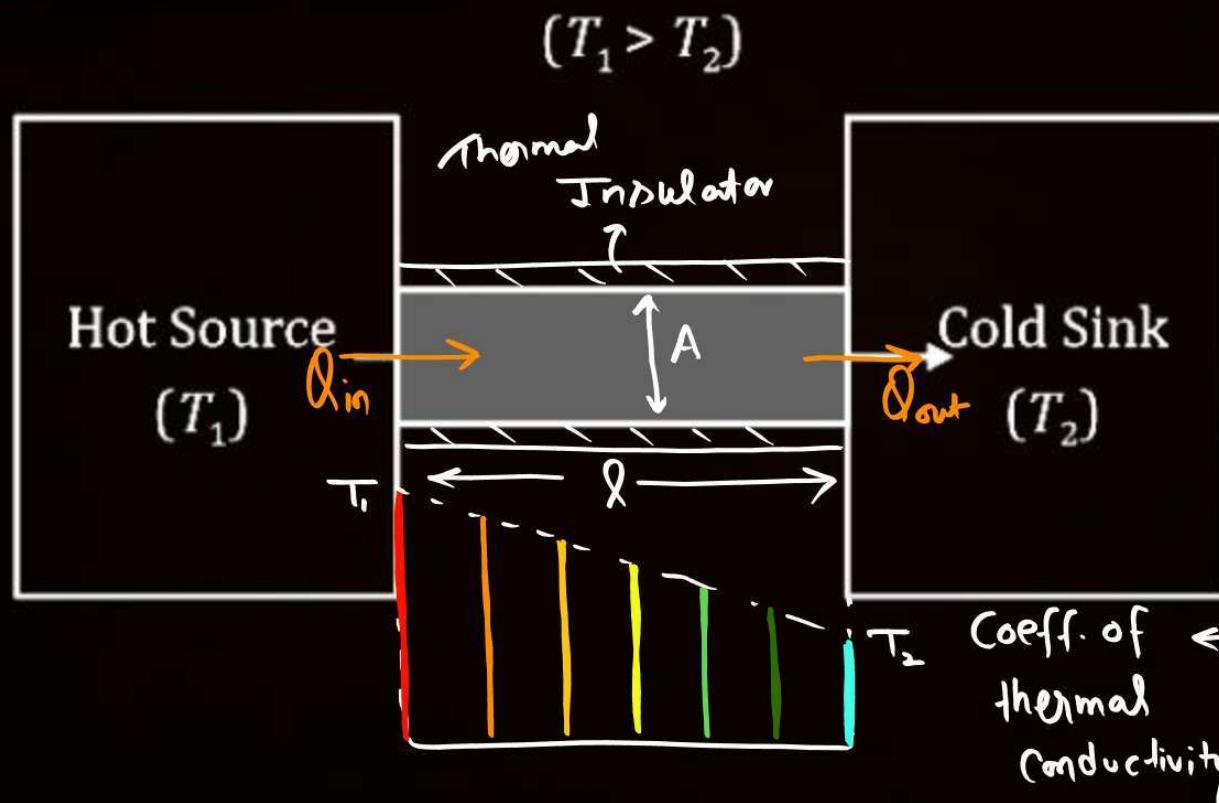


- fastest way of energy transfer.
- Medium is not required.
- No mass transfer happens.
- Happens in all bodies, (Solid, Liquid, gas)
- Happens at all temp





Thermal Conduction



In steady state \rightarrow

$$Q_{in} = Q_{out}$$

$\frac{dQ}{dt}$ = Rate of Heat flow

SI Unit: $\frac{J}{s}$ = watt \star

Temp. gradient

$$\frac{dQ}{dt} \propto T_1 - T_2 \quad \left. \begin{array}{l} \uparrow \\ \frac{T_1 - T_2}{\lambda} \end{array} \right\}$$

$$\propto \frac{1}{\lambda}$$

$$\frac{dQ}{dt} = \frac{kA}{\lambda} \Delta T$$

QUESTION

Find time in which entire ice will melt.



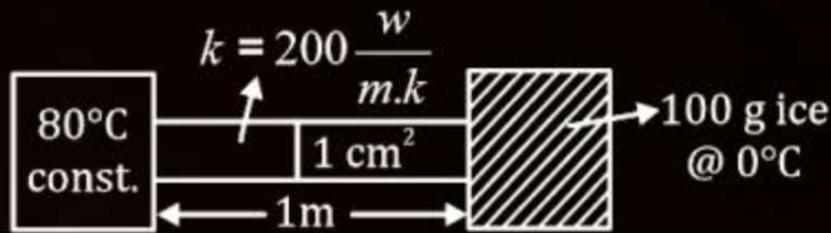
$$\frac{dQ}{dt} = k \frac{A}{\lambda} \Delta T \Rightarrow k = \frac{dQ/dt \cdot \lambda}{A \cdot \Delta T}$$

$$= \frac{\text{Watt} \cdot \text{m}^{-2}}{\text{m}^2 \cdot \text{K}}$$

$$\frac{dQ}{dt} = \frac{kA}{\lambda} \Delta T$$

$$\frac{dQ}{dt} = \frac{200 \times 1 \times 10^{-4}}{1} \times 80$$

$$= 1.6 \text{ J/s}$$

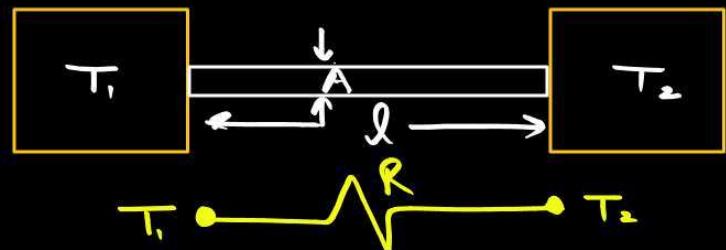


$$t = \frac{Q}{dQ/dt} = \frac{m L}{(dQ/dt)}$$

$$= \frac{100 \times 80 \text{ cal}}{1.6 \text{ J/s}}$$

$$= \frac{8000 \times 412 \text{ J}}{16 \text{ J/s}}$$

$$t = 21000 \text{ s}$$

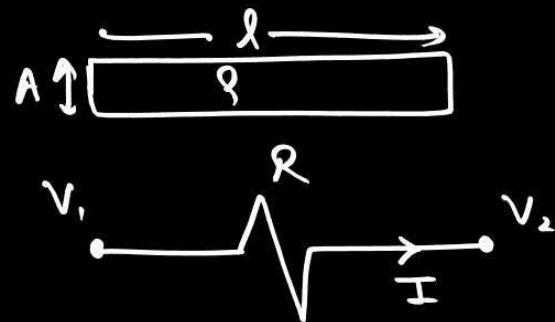


$$\frac{dQ}{dt} = \frac{kA}{l} \Delta T$$

$$\frac{dQ}{dt} = \frac{\Delta T}{\left(\frac{l}{kA}\right)} \quad \begin{matrix} \text{Thermal potential diff} \\ \text{Thermal Resistance} \end{matrix}$$

thermal current

$$R_{\text{th.}} = \frac{l}{kA}$$



$$V = IR$$

$$V_1 - V_2 = I \cdot R$$

$$I = \frac{V_1 - V_2}{R} \quad \text{Elec. Resistivity}$$

$$I = \frac{V_1 - V_2}{\left(\frac{\rho l}{A}\right)} = \frac{\Delta V}{\left(\frac{\rho l}{A}\right)} \quad \begin{matrix} \text{Electrical conductivity} \\ \text{Electric Resistance} \end{matrix}$$



QUESTION (JEE Mains – Jan. 10, 2019 (I))

A heat source at $T = 10^3 \text{ K}$ is connected to another heat reservoir at $T = 10^2 \text{ K}$ by a copper slab which is 1 m thick. Given that the thermal conductivity of copper is $0.1 \text{ WK}^{-1} \text{ m}^{-1}$, the energy flux through it in the steady state

A $90 \text{ Wm}^{-2} \frac{\text{W}}{\text{m}^2}$

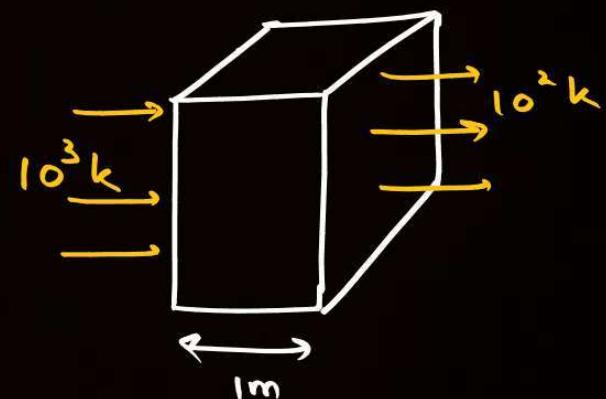
B 120 Wm^{-2}

C 65 Wm^{-2}

D 200 Wm^{-2}

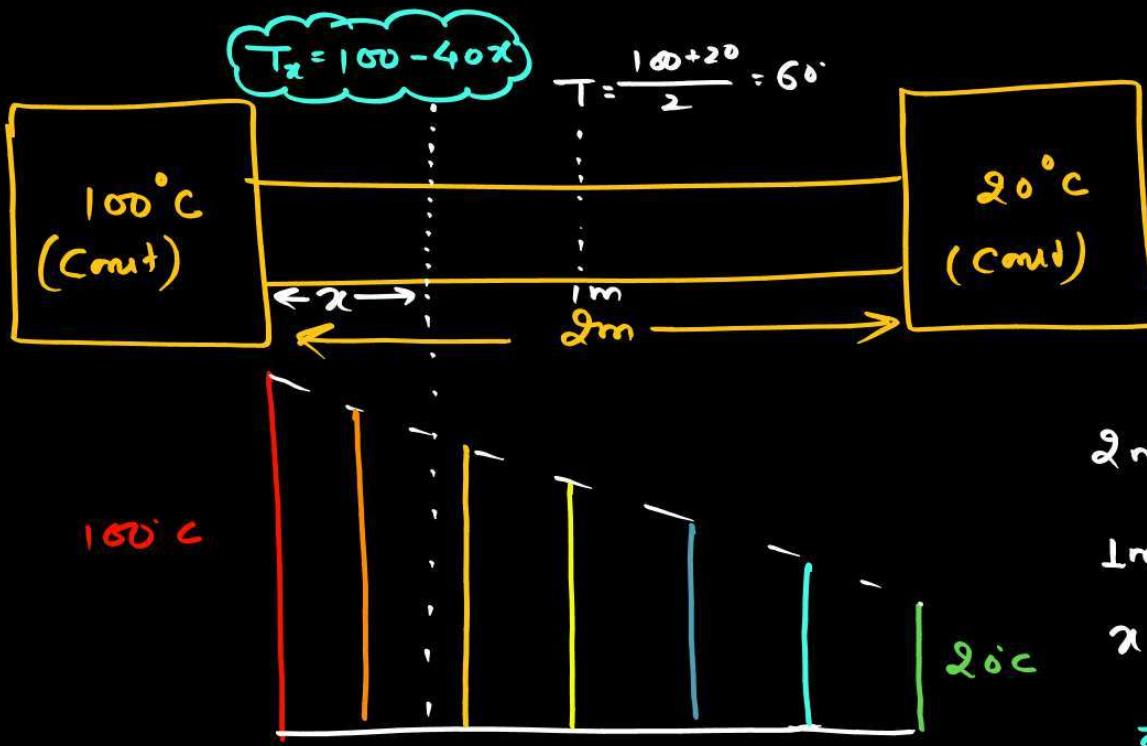
$$\frac{dQ}{dt} = \frac{kA}{\ell} \Delta T$$

$$\begin{aligned} \frac{dQ}{dt} &= \frac{k \Delta T}{\ell} \\ &= \frac{0.1 \times (1000 - 100)}{1} \\ &= 90 \times 0.1 = 90 \frac{\text{W}}{\text{m}^2}. \end{aligned}$$





Q.



$$\frac{\Delta T}{2m} \rightarrow 80^{\circ}\text{C}$$
$$1m \rightarrow 40^{\circ}\text{C}$$
$$xm \rightarrow (40 \times x)^{\circ}\text{C}$$

इतना temp. कम हुआ है।

QUESTION



Find temperature of junction between two conductors.

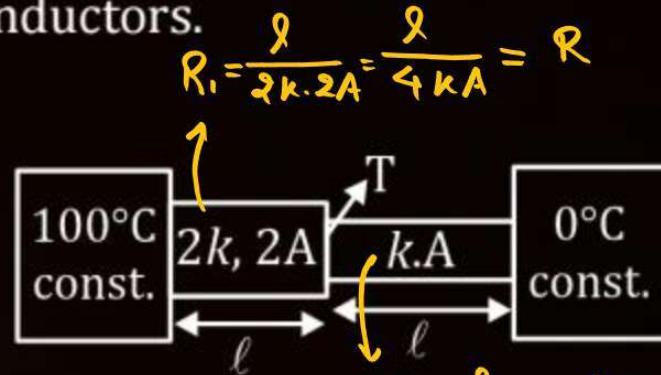
$$R = \frac{\rho l}{A} = \frac{\rho}{kA}$$

$$5R \xrightarrow{\Delta T} 100^\circ C$$

$$R \xrightarrow{\Delta T} \frac{100}{5} {}^\circ C = 20^\circ C$$

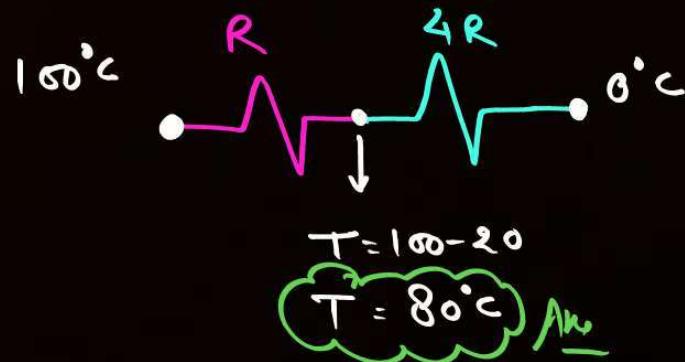
$$\frac{dQ}{dt} = \frac{V}{R_{eq}} = \frac{100}{5R} = \left(\frac{20}{4kA} \right)$$

$$\frac{dQ}{dt} = \frac{80 \text{ kA}}{\rho}$$



$$R_1 = \frac{\rho}{2k \cdot 2A} = \frac{\rho}{4kA} = R$$

$$R_2 = \frac{\rho}{kA} = 4R$$



$$T = 100 - 20$$

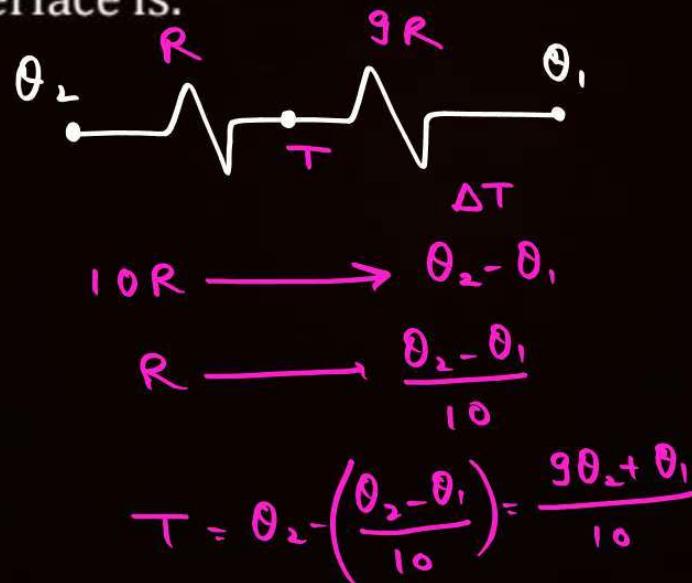
$$T = 80^\circ C$$

Ans

QUESTION (JEE Mains – Apr. 09, 2019 (II))

Two materials having coefficients of thermal conductivity '3K' and 'K' and thickness 'd' and '3d', respectively, are joined to form a slab as shown in the figure. The temperatures of the outer surfaces are ' θ_2 ' and ' θ_1 ' respectively, ($\theta_2 > \theta_1$). The temperature at the interface is:

- A** $\frac{\theta_2 + \theta_1}{2}$
- B** $\frac{\theta_1}{3} + \frac{2\theta_2}{3}$
- C** $\frac{\theta_1}{10} + \frac{9\theta_2}{10}$
- D** $\frac{\theta_1}{6} + \frac{5\theta_2}{6}$



$$\text{Left side: } R_1 = \frac{d}{3kA} \quad \text{Right side: } R_2 = \frac{3d}{kA} = 9R$$

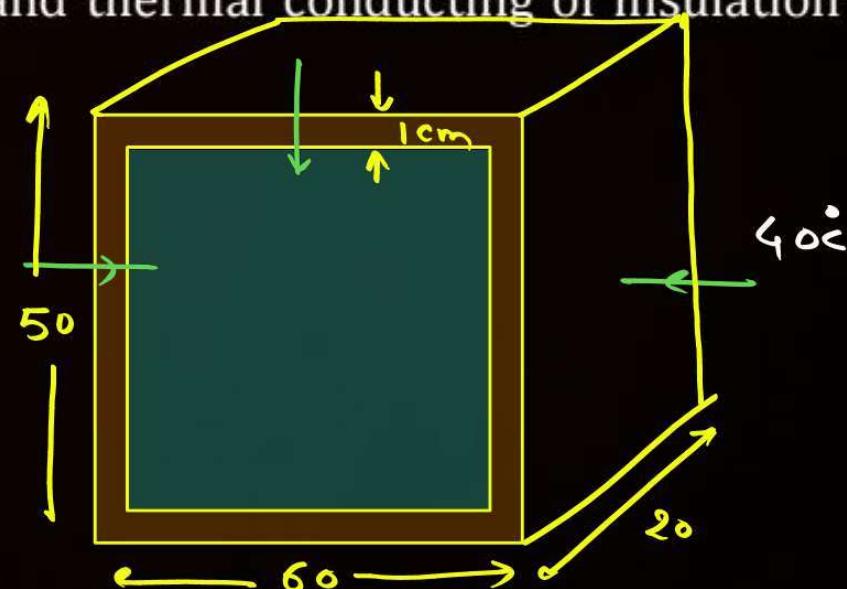
QUESTION (JEE Mains – July. 26, 2022 (II))



An ice cube of dimensions $60\text{cm} \times 50\text{cm} \times 20\text{cm}$ is placed in an insulation box of wall thickness 1 cm. The box keeping the ice cube at 0°C of temperature is brought to a room of temperature 40°C . The rate of melting of ice is approximately:

(Latent heat of fusion of ice is $3.4 \times 10^5 \text{ J kg}^{-1}$ and thermal conductivity of insulation wall is $0.05 \text{ Wm}^{-1} \text{ }^\circ\text{C}^{-1}$)

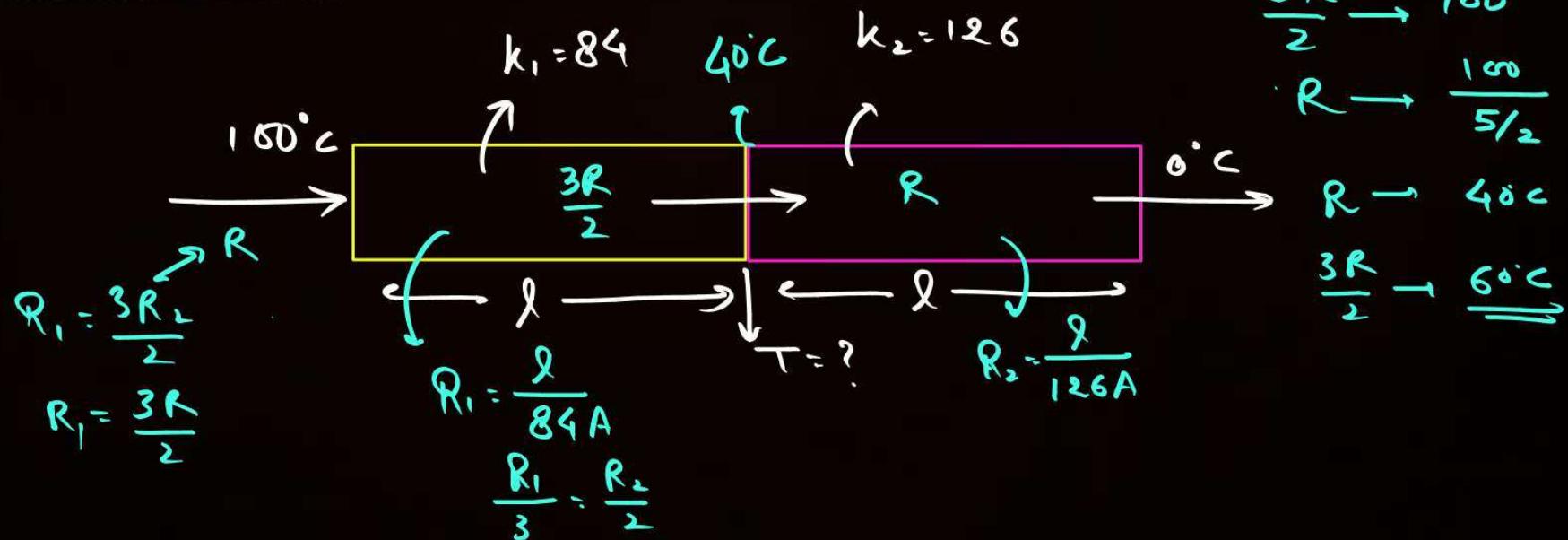
- A** $61 \times 10^{-3} \text{ kg s}^{-1}$ $\frac{dQ}{dt} =$
- B** $61 \times 10^{-5} \text{ kg s}^{-1}$
- C** 208 kg s^{-1}
- D** $30 \times 10^{-3} \text{ kg s}^{-1}$



QUESTION (JEE Mains – Apr. 13, 2023 (II))



Two plates A and B have thermal conductivities $84 \text{ Wm}^{-1}\text{K}^{-1}$ and $126 \text{ Wm}^{-1}\text{K}^{-1}$ respectively. They have same surface area and same thickness. They are placed in contact along their surfaces. If the temperatures of the outer surfaces of A and B are kept at 100°C and 0°C respectively, then the temperature of the surface of contact in steady state is 60 $^\circ\text{C}$.

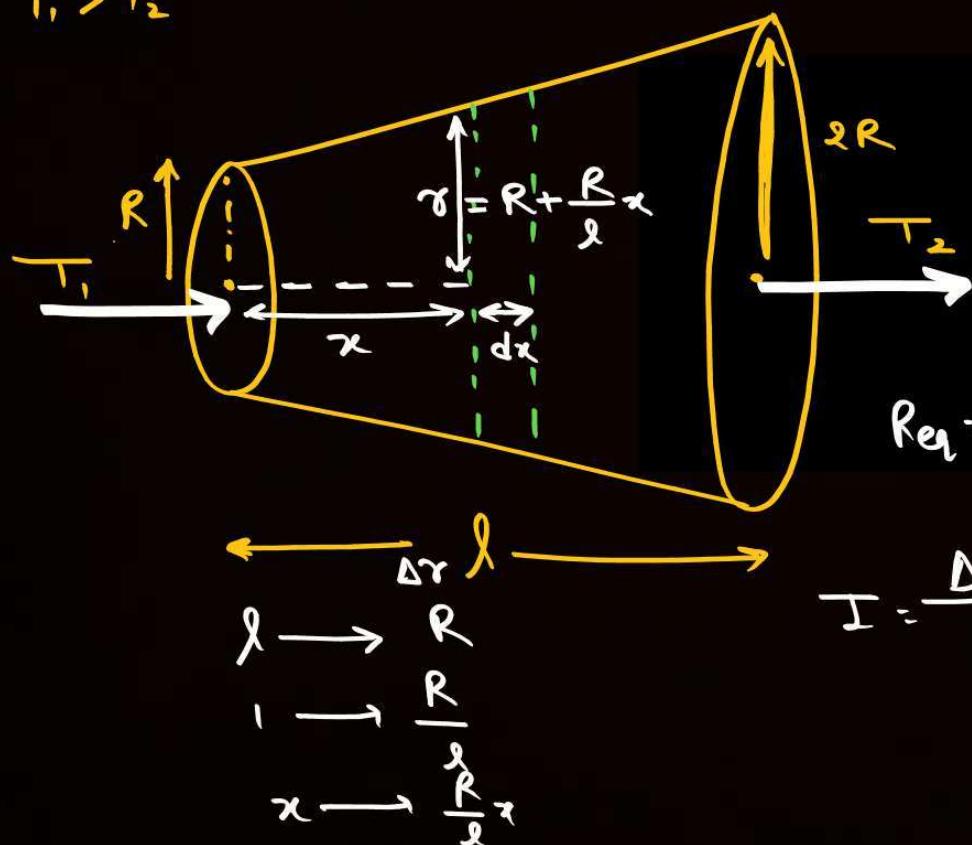


QUESTION



Find rate of heat flow between ends of frustum.

$$T_1 > T_2$$



$$\int dR = \int \frac{dx}{k \cdot A}$$

$$R_{eq} = \frac{1}{k} \int \frac{dx}{\pi r^2}$$

$$= \frac{1}{k\pi} \int \frac{dx}{r^2} = \frac{1}{\pi k} \int_0^l \frac{dx}{R^2 \left[1 + \frac{x}{l}\right]^2}$$

$$R_{eq} = \frac{l}{2\pi R^2 k}$$

$$I = \frac{\Delta T}{R_{eq}} = \frac{(T_1 - T_2) 2\pi R^2 k}{l}$$

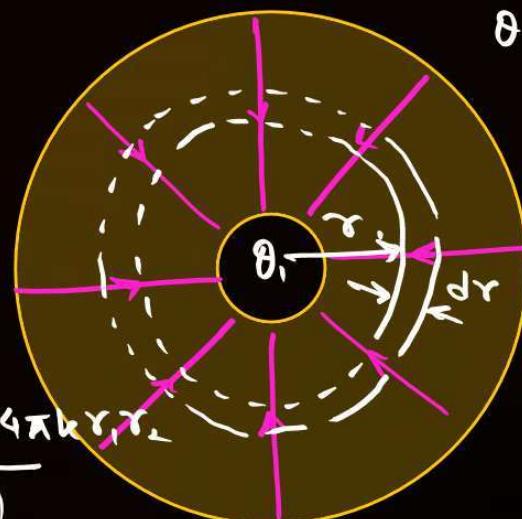
$$R_{eq} = \frac{l}{\pi R^2 k} \left[\left(1 + \frac{x}{l}\right)^{-1} \right]_0^l = \frac{l}{\pi R^2 k} \left(1 - \frac{1}{2} \right)$$

QUESTION (JEE Mains – Aug. 31, 2021 (II))

Two thin metallic spherical shells of radii r_1 and r_2 ($r_1 < r_2$) are placed with their centres coinciding. A material of thermal conductivity K is filled in the space between the shells. The inner shell is maintained at temperature θ_1 and the outer shell at temperature θ_2 ($\theta_1 < \theta_2$). The rate at which heat flows radially through the material is:

- A** $\frac{\pi r_1 r_2 (\theta_2 - \theta_1)}{r_2 - r_1}$
- B** $\frac{K(\theta_2 - \theta_1)(r_2 - r_1)}{4\pi r_1 r_2}$
- C** $\frac{K(\theta_2 - \theta_1)}{r_2 - r_1}$
- D** $\frac{4\pi K r_1 r_2 (\theta_2 - \theta_1)}{r_2 - r_1}$

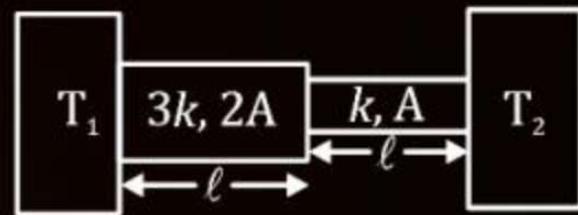
$$\begin{aligned} dR &= \int_{r_1}^{r_2} \frac{d\tau}{k(4\pi\tau^2)} \\ R_{eq} &= \frac{1}{4\pi k} \left[-\frac{1}{\tau} \right]_{r_1}^{r_2} \\ R_{eq} &= \frac{1}{4\pi k} \left[\frac{1}{r_1} - \frac{1}{r_2} \right] \\ \frac{dQ}{dt} &= \frac{\theta_2 - \theta_1}{R_{eq}} = \frac{(\theta_2 - \theta_1)4\pi k r_1 r_2}{(r_2 - r_1)} \end{aligned}$$



QUESTION

Find equivalent thermal conductivity-

$$\frac{2k}{7}$$



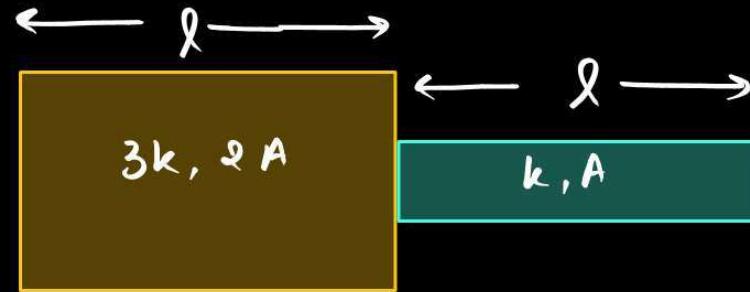


Geometry change

फिल्म विकला, मुम्हाई

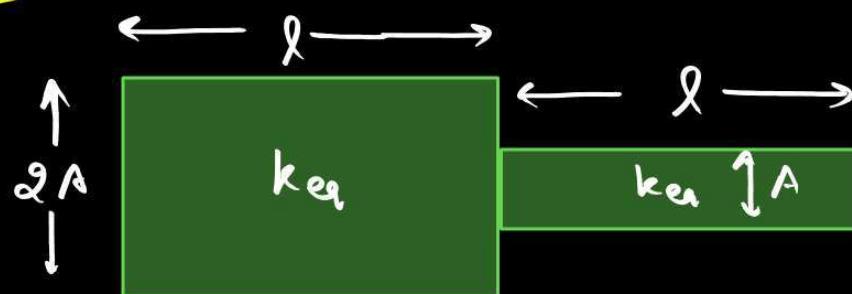
material रखो कि

Req. change नहीं है



$$R_{eq} = R_1 + R_2 = \frac{l}{6kA} + \frac{l}{kA}$$

$$R_{eq} = \frac{7l}{6kA}$$



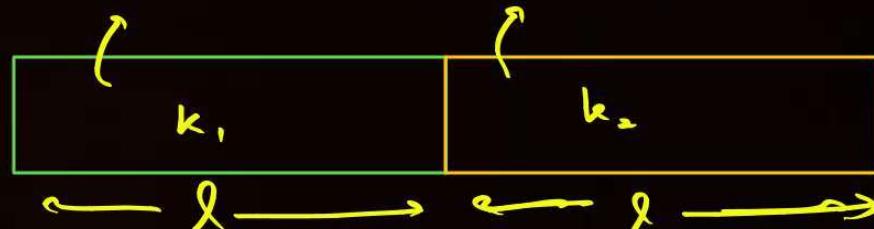
$$R_{eq} = \frac{l}{k_{eq} \cdot 2A} + \frac{l}{k_{eq} \cdot A}$$

$$\frac{7l}{6kA} = \frac{1}{k_{eq}} \times \frac{3l}{2A} \Rightarrow k_{eq} = \frac{9}{7} k_A$$

QUESTION (JEE Mains – March. 17, 2021 (I))

Two identical metal of thermal conductivities K_1 and K_2 respectively are connected in series. The effective thermal conductivity of the combination is:

$$R = \frac{\ell}{k_1 A} \quad R_2 = \frac{\ell}{k_2 A}$$



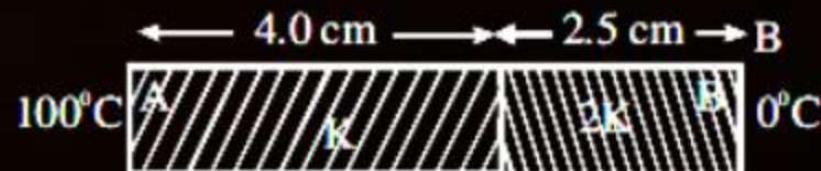
- A** $\frac{K_1 + K_2}{K_1 K_2}$
- B** $\frac{K_1 + K_2}{2K_1 K_2}$
- C** $\frac{2K_1 K_2}{K_1 + K_2}$
- D** $\frac{K_1 K_2}{K_1 + K_2}$

$$\frac{2\ell}{k_{eq} \cdot A} = \frac{\ell}{k_1 A} + \frac{\ell}{k_2 A}$$

$$k_{eq} = \frac{2k_1 k_2}{k_1 + k_2}$$

QUESTION (JEE Mains – June. 29, 2022 (I))

As per the given figure, two plates A and B of thermal conductivity K and $2K$ are joined together to form a compound plate. The thickness of plates are 4.0 cm and 2.5 cm respectively and the area of cross-section is 120 cm^2 for each plate. The equivalent thermal conductivity of the compound plate is $\left(1 + \frac{5}{\alpha}\right)K$, then the value of α will be _____.



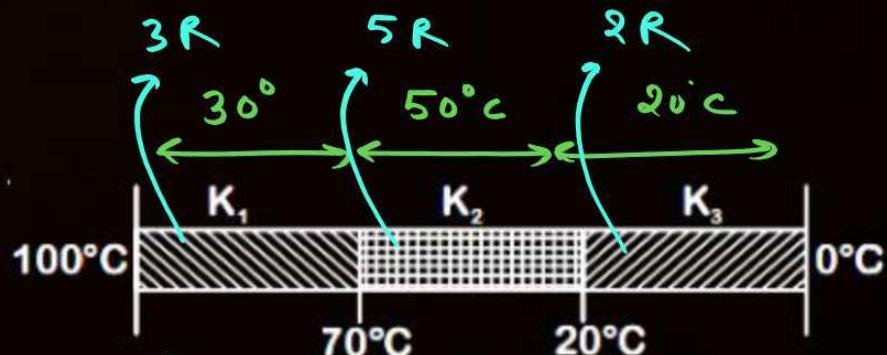
QUESTION (JEE Mains – Sep. 06, 2020 (II))

$$\uparrow V = \frac{I}{R} R \uparrow$$



Three rods of identical cross-section and lengths are made of three different materials of thermal conductivity K_1 , K_2 and K_3 respectively. They are joined together at their ends to make a long rod (see figure). One end of the long rod is maintained at 100°C and the other at 0°C (see figure). If the joints of the rod are at 70°C and 20°C in steady state and there is no loss of energy from the surface of the rod, the correct relationship between K_1 , K_2 and K_3 is

- A $K_1 : K_3 = 2 : 3 ; K_2 : K_3 = 2 : 5$
- B $K_1 < K_2 < K_3$
- C $K_1 : K_2 = 5 : 2 ; K_1 : K_3 = 3 : 5$
- D $K_1 > K_2 > K_3$



$$k_2 < k_1 < k_3 \quad \uparrow R = \frac{\Delta T}{\downarrow k \Delta}$$



$$\frac{\frac{\lambda}{k_1 A}}{\frac{\lambda}{k_2 A}} = \frac{3R}{5R}$$

$$\frac{k_2}{k_1} : \frac{3}{5} \Rightarrow \frac{k_1}{k_2} = \frac{5}{3}$$

QUESTION

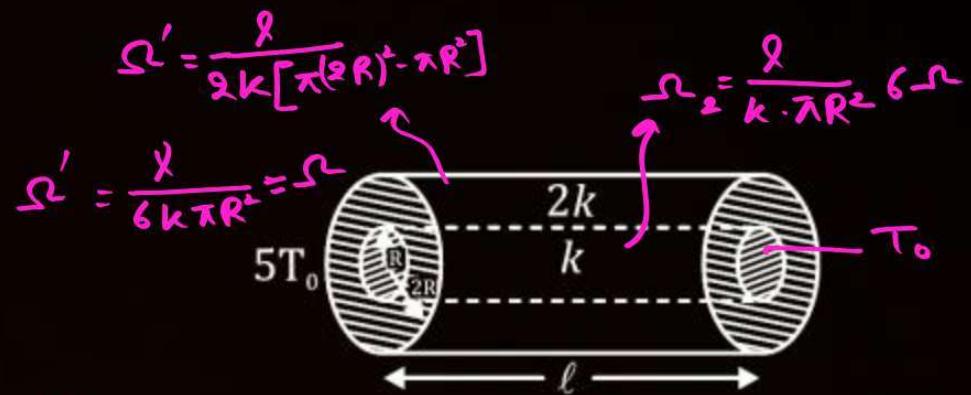


Find.

(1) Rate of heat flow

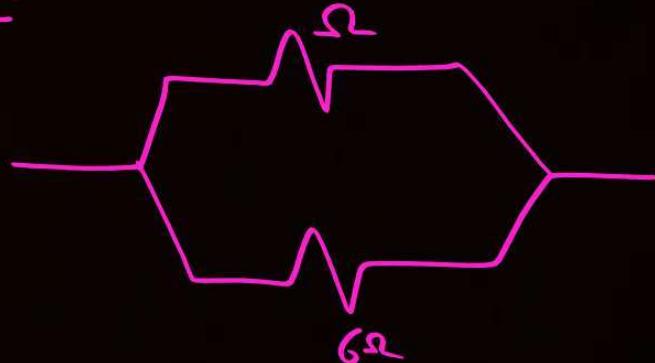
~~Y/W~~

(2) Equivalent thermal conductivity.



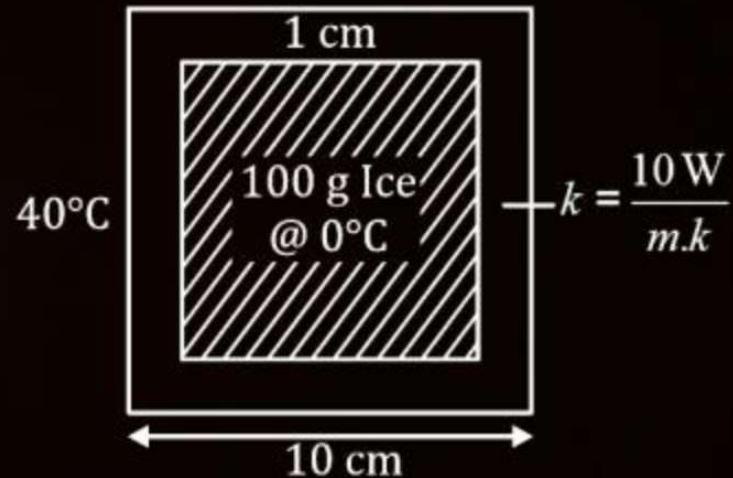
$$\Omega_{eq} = \frac{\Omega \times 6\Omega}{7\Omega} = \frac{6\Omega}{7}$$

$$\begin{aligned} \lambda &= \frac{V}{Rq} = \frac{5T_0 - T_0}{\frac{6}{7}\Omega} \\ &= 4T_0 \times \frac{7}{2} \times \frac{6k\pi R^2}{\delta} \\ &= \frac{28\pi R^2 k T_0}{\delta} \end{aligned}$$



QUESTIONH.W

Find time in which entire ice will melt.



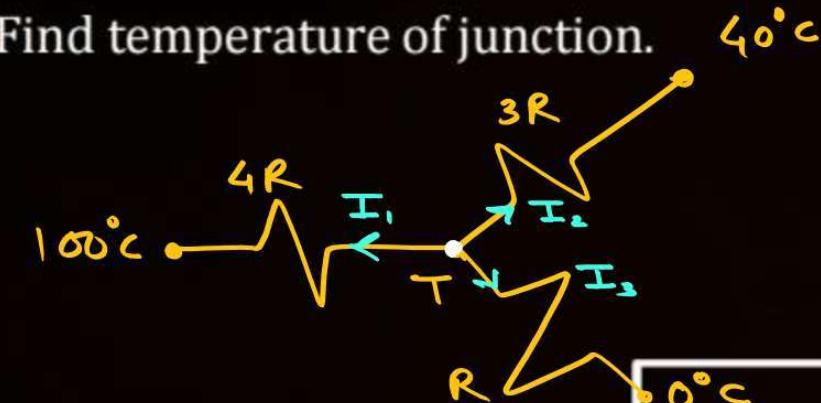
QUESTION

(kCL)

$$I = \frac{V}{R}$$



Find temperature of junction.

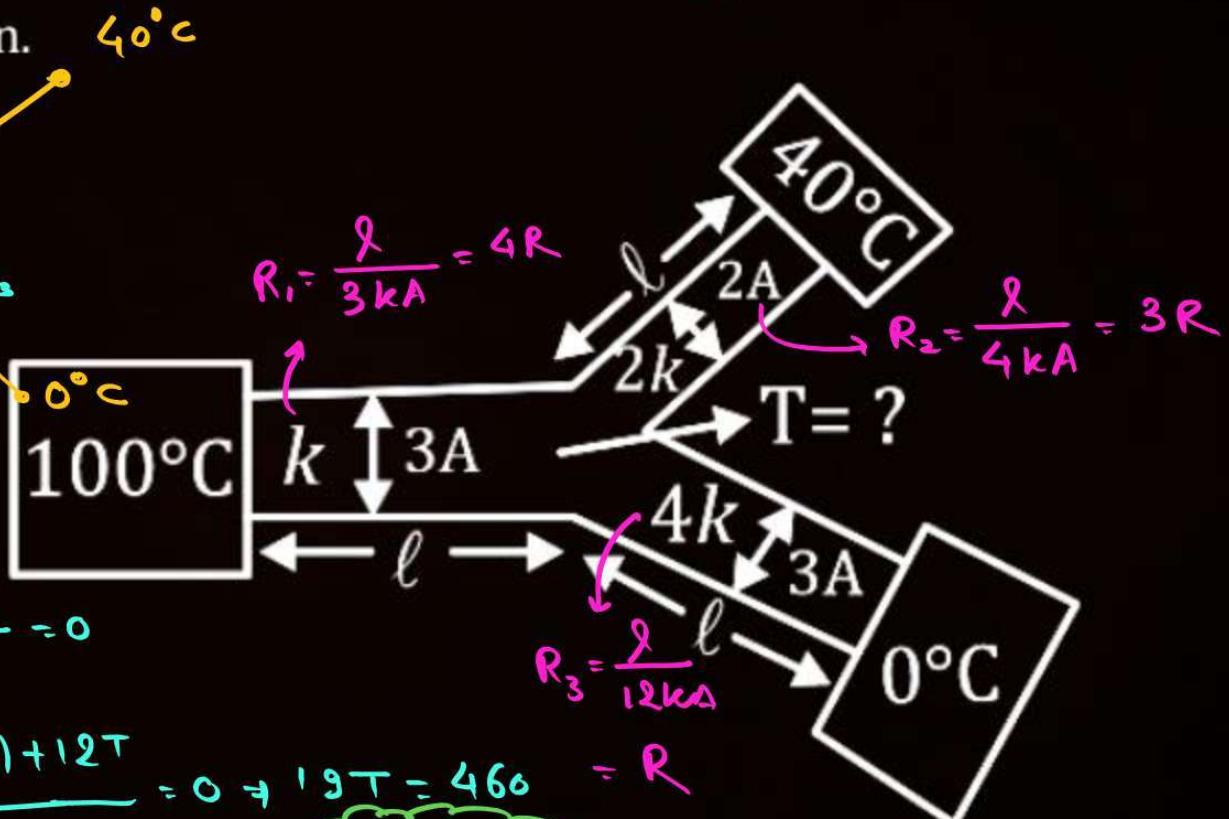


$$I_1 + I_2 + I_3 = 0$$

$$\frac{T-100}{4R} + \frac{T-40}{3R} + \frac{T-0}{R} = 0$$

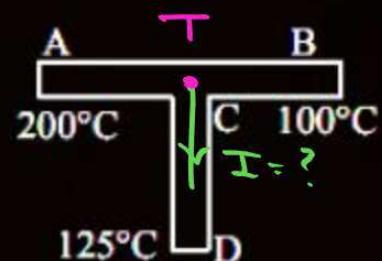
$$\frac{3(T-100) + 4(T-40) + 12T}{12R} = 0 \Rightarrow 19T = 460 = R$$

$$T = \frac{460}{19} \text{ Ans}$$



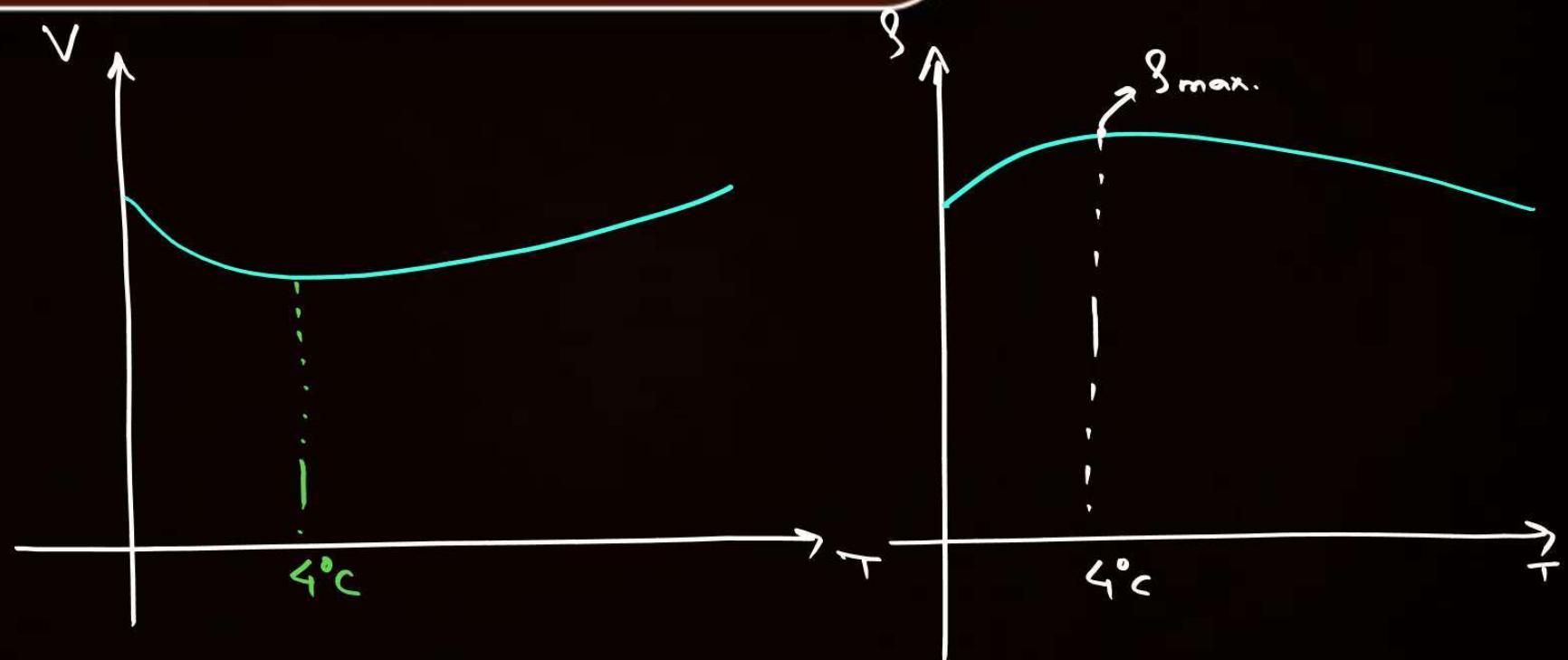
QUESTION (JEE Mains – Aug. 27, 2021 (I))

A rod CD of thermal resistance 10.0 kW^{-1} is joined at the middle of an identical rod AB as shown in figure. The end A, B and D are maintained at 200°C , 100°C and 125°C respectively. The heat current in CD is P watt. The value of P is



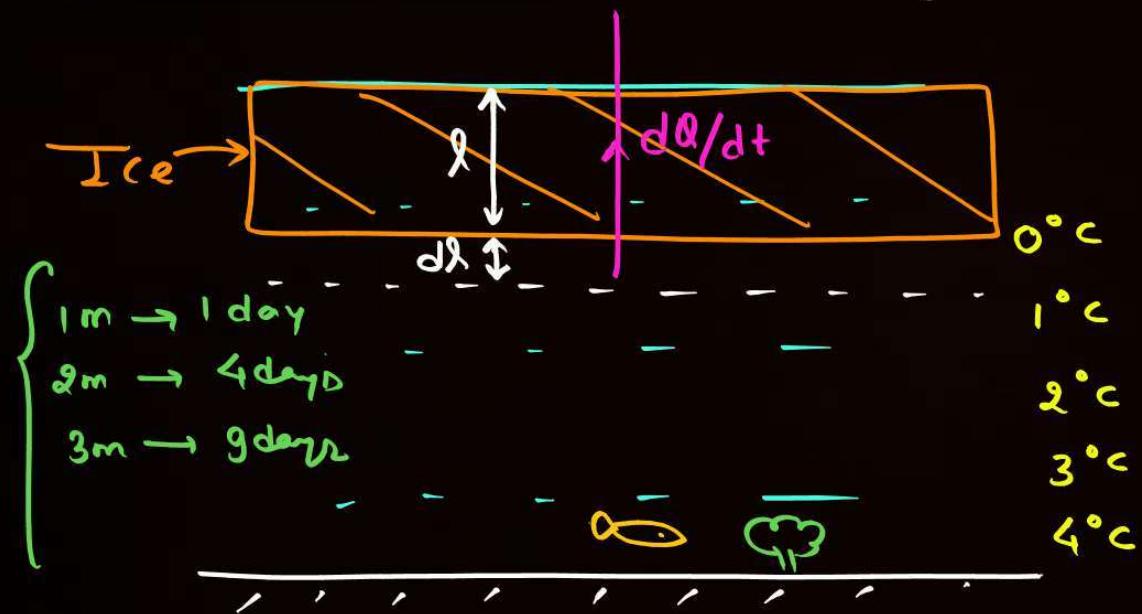


Anomalous Behaviour of Water





Freezing of Lake



$$\frac{dQ}{dt} = \frac{kA}{\lambda} \Delta T$$
$$dQ = dm L$$

$$\frac{dm \cdot L}{dt} = \frac{kA}{\lambda} T_0$$

$$\frac{\rho A d\lambda \cdot L}{dt} = \frac{kA}{\lambda} T_0$$

$$\rho L \frac{d\lambda}{dt} = \frac{k}{\lambda} T_0$$

$$\rho L \int \lambda d\lambda = k T_0 \int dt$$

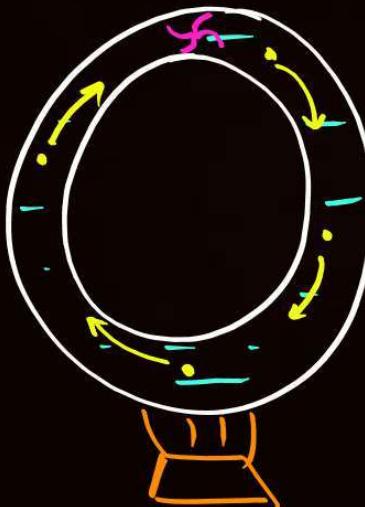
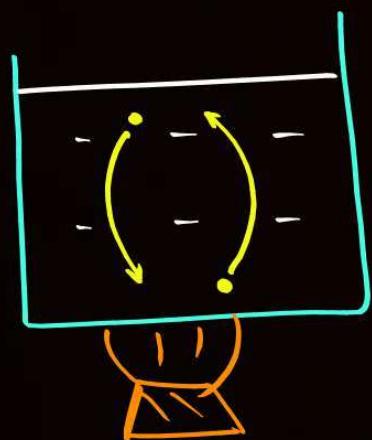
$$\frac{\rho L \lambda^2}{2} = k T_0 t$$
$$t \propto \lambda^2$$



Thermal Convection

Natural

Forced



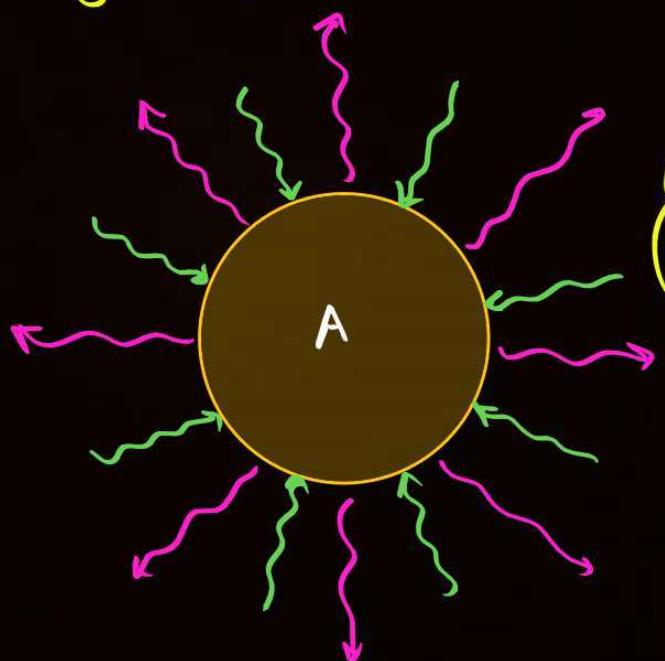


Thermal Radiation

Prevost
Theory
of
Heat
Exchange

{ Heat.

Any body that has temp. of above 0K radiates



In equilibrium \rightarrow

Heat
radiated
per
sec.

= Heat
absorbed
per
sec

Emissive Power, Absorptive Power



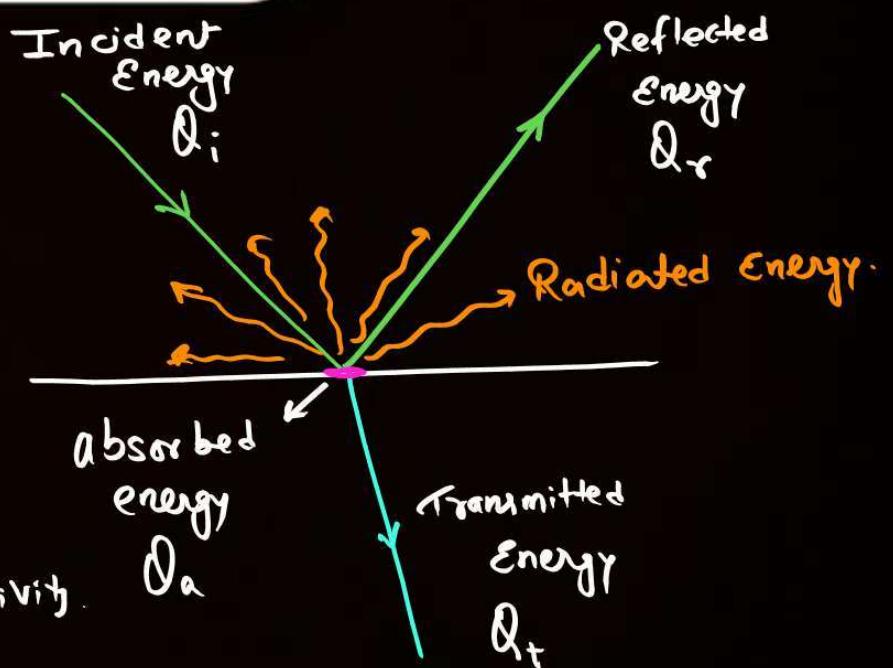
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$$Q_i = Q_r + Q_t + Q_a$$

$$\frac{Q_r}{Q_i} + \frac{Q_t}{Q_i} + \frac{Q_a}{Q_i} = 1$$

$$\gamma + t + \underline{\alpha} = 1$$

reflectivity transmittivity Absorptive power/absorptivity.





$$\text{Absorptive power} = \frac{\text{Total Energy absorbed}}{\text{Total Energy incident}}$$

(a) \downarrow unitless

$$\gamma + t + a = 1$$

for perfectly reflecting surface, $\gamma = 1, a, e = 0$

for perfectly transparent surface, $t = 1, a, e = 0$

for perfectly absorptive surface (Perfect Black Body), $a = 1, \gamma, t = 0$



Emissive Power, $E \rightarrow$

Total energy radiated per unit time per unit Area.

$$E = \frac{\text{Energy radiated}}{\text{Time} \times \text{Area}}$$

$$\text{Unit} = \frac{\text{Watt}}{\text{m}^2}$$

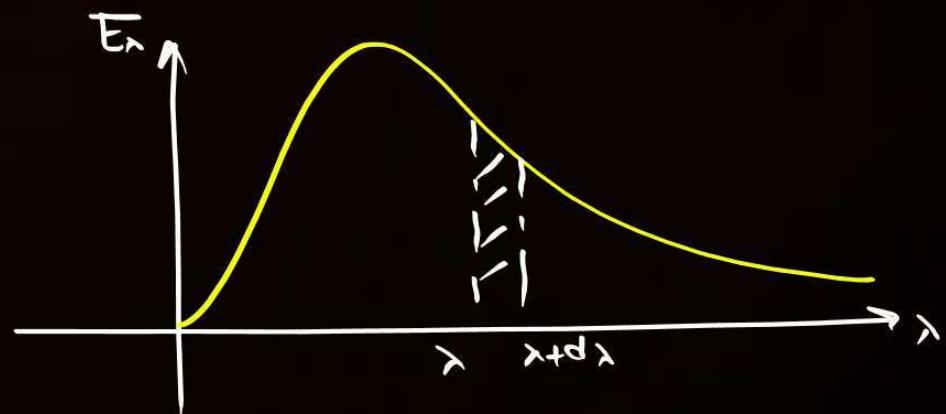


Spectral Emissive Power



$$\bar{E}_\lambda = \frac{dE}{d\lambda}$$

Total energy radiated per unit time per unit Area per unit wavelength





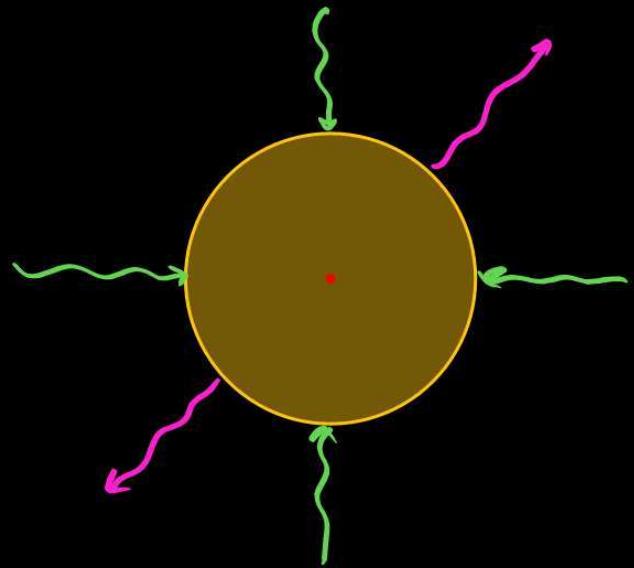
Perfect Black Body

$$\alpha = 1$$

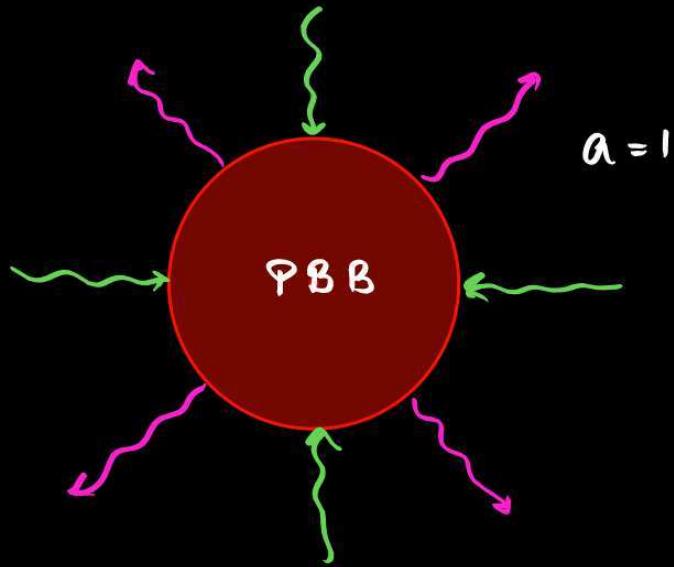




Thermal Equilibrium



$$E = E_0 \times Q$$



$$E_{PBB} = E_0$$

$$E = E_{PBB} \times Q$$



Kirchhoff's Law of Radiation

Emissive power of a body is a fraction of Emissive power
of PBB at same temp

$$E = E_{PBB} \times \alpha$$



Emissivity

$$e = \frac{E}{E_{\text{PBB}}}$$

$$\underline{0 < e \leq 1}$$

$$e = \alpha$$



Stefan-Boltzmann Law



$$\frac{dQ}{dt} = \sigma e A T^4$$

$\frac{dQ}{dt}$ = Rate of Heat radiated per sec

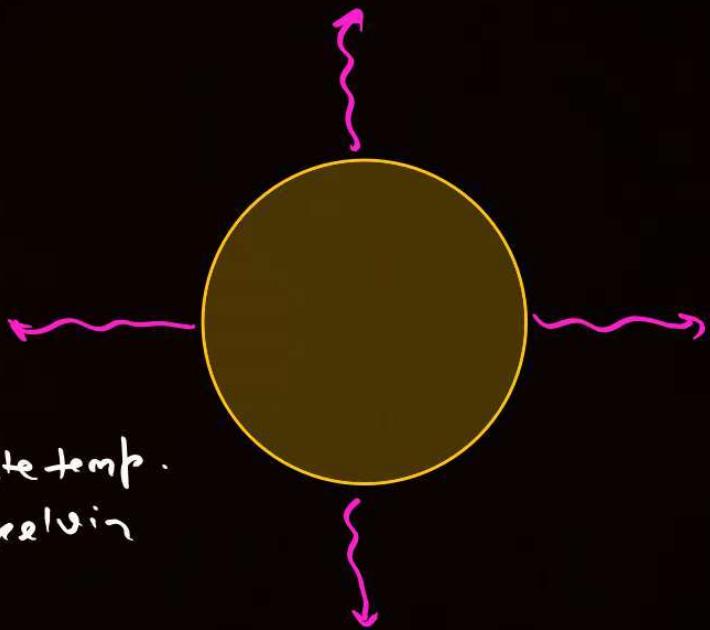
σ = Stefan's const

$$\sigma = 5.67 \times 10^{-8} \frac{\text{W}}{\text{m}^2 \cdot \text{K}^4}$$

e = emissivity

A = Surface area of body

T: Absolute temp.
in kelvin



QUESTION (JEE Mains – 2006)

Assuming the Sun to be a spherical body of radius R at a temperature of $T K$, evaluate the total radiant power incident on Earth at a distance r from the Sun

A $4\pi r_0^2 R^2 \sigma \frac{T^4}{r^2}$

B $\pi r_0^2 R^2 \sigma \frac{T^4}{r^2}$

C $r_0^2 R^2 \sigma \frac{T^4}{4\pi r^2}$

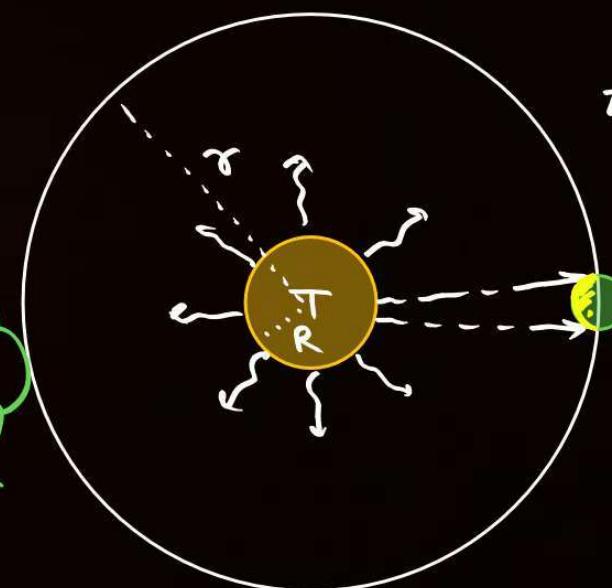
D $R^2 \sigma \frac{T^4}{r^2}$

Heat rad.
by sun \rightarrow

$$\frac{dQ}{dt} = \sigma e A T^4$$

$$P_o = \frac{dQ}{dt} = \sigma (\pi R^2) T^4$$

$$\frac{\sigma \pi R^2 T^4 \tau_0}{4\pi r^2}$$



$$\begin{aligned}
 4\pi r^2 &\rightarrow P_o \\
 1 &\rightarrow \frac{P_o}{4\pi r^2} \\
 \pi r_0^2 &\rightarrow \frac{P_o}{4\pi r^2} \pi r_0^2 \\
 \uparrow r_0 \quad A_{\text{eff}} = \pi r_0^2 & \\
 \frac{P_o \tau_0}{4\pi r^2} &
 \end{aligned}$$

where r_0 is the radius of the Earth and σ is Stefan's constant.

QUESTION (JEE Mains – Online May 7, 2012)

The heat radiated per unit area in 1 hour by a furnace whose temperature is 3000 K is
($\sigma = 5.7 \times 10^{-8} \text{ W m}^{-2} \text{ K}^{-4}$)

A $1.7 \times 10^{10} \text{ J}$

$$\frac{d\Phi}{dt} = \sigma T^4$$
$$= 5.7 \times 10^{-8} \times (3 \times 10^3)^4$$

B $1.1 \times 10^{12} \text{ J}$

$$= 5.7 \times 10^{-8} \times 81 \times 10^{12}$$

C $2.8 \times 10^8 \text{ J}$

$$= 5.7 \times 81 \times 10^8$$

D $4.6 \times 10^6 \text{ J}$

>

QUESTION (JEE Mains – 2004)

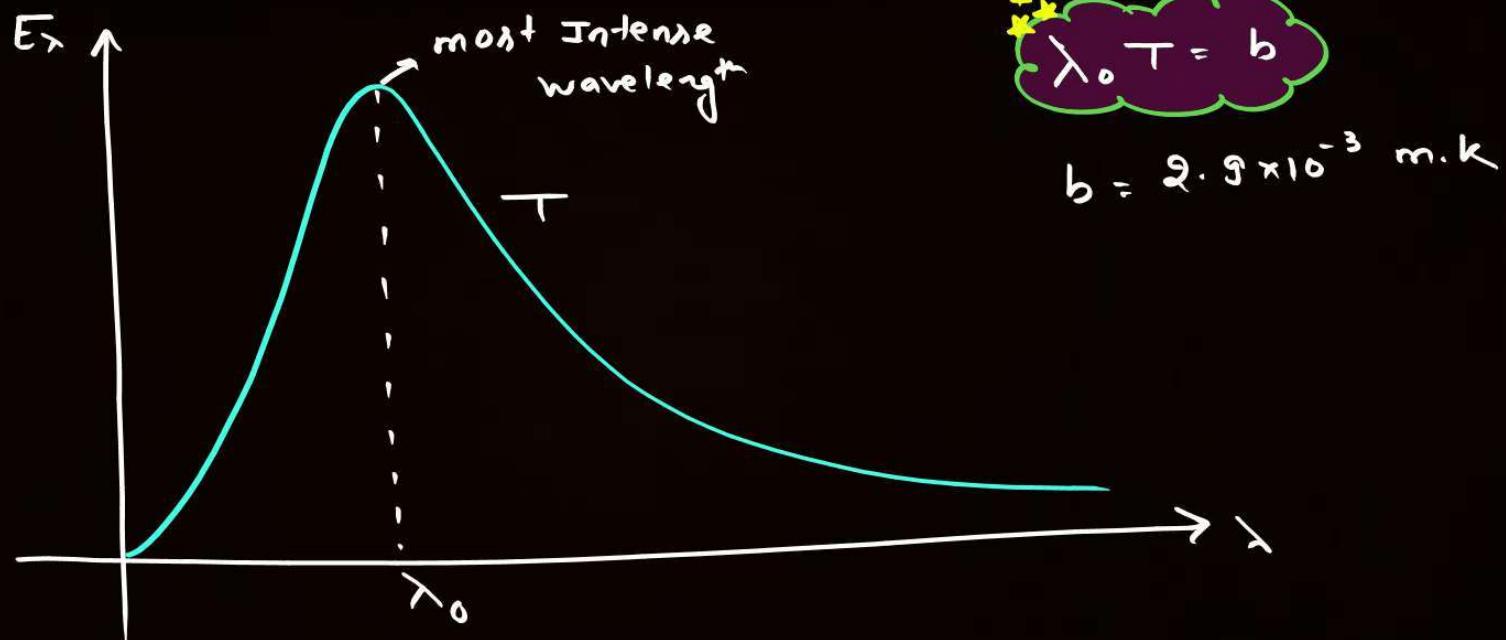
If the temperature of the sun were to increase from T to $2T$ and its radius from R to $2R$, then the ratio of the radiant energy received on earth to what it was previously will be

- A** 32
- B** 16
- C** 4
- D** 64

$$\frac{dQ}{dt} = \sigma e A T^4$$
$$\sigma e \cdot 4\pi(2R)^2 (2T)^4$$
$$4 \times 16 \times$$



Wein's Displacement Law



$$\lambda_0 T = \text{const.}$$

$$\lambda_0 T = b$$

$$b = 2.9 \times 10^{-3} \text{ m.k}$$

QUESTION (JEE Mains – JEE Adv, 2023)



$$\frac{T_0}{P_0} \longrightarrow 2^4 \quad T_0 \longrightarrow 2^4 P_0 = 16 P_0$$

Match the temperature of a black body given in List-I with an appropriate statement in List-II, and choose the correct option. [Given: Wien's constant as 2.9×10^{-3} m-K and $hc/e = 1.24 \times 10^{-6}$ V-m]

$$\lambda \propto T \text{ or } \lambda = \frac{\text{Const}}{T}$$

List - I	List - II
(P) 2000 K	(1) The radiation at peak wavelength can lead to emission of photoelectrons from a metal of work function 4 eV .
(Q) 3000 K	(2) The radiation at peak wavelength is visible to human eye. ($4000\text{-}7000\text{\AA}$)
(R) 5000 K	(3) The radiation at peak emission wavelength will result in the widest central maximum of a single slit diffraction. $\uparrow P \propto \frac{2 \lambda D}{a}$
(S) 10000 K	(4) The power emitted per unit area is $1/16$ of that emitted by a blackbody at temperature 6000 K.
	(5) The radiation at peak emission wavelength can be used to image human bones. X-ray

QUESTION (JEE Mains – JEE Adv, 2023)

A $p \rightarrow 3, q \rightarrow 5, r \rightarrow 2, s \rightarrow 3$

B $p \rightarrow 3, q \rightarrow 2, r \rightarrow 4, s \rightarrow 1$

C $p \rightarrow 3, q \rightarrow 4, r \rightarrow 2, s \rightarrow 1$

D $p \rightarrow 1, q \rightarrow 2, r \rightarrow 5, s \rightarrow 3$



Rate of Heat Loss

$$\text{At } T_{\text{body}} = T_0 \rightarrow$$

Heat rad. per sec. = Heat absorbed per sec.

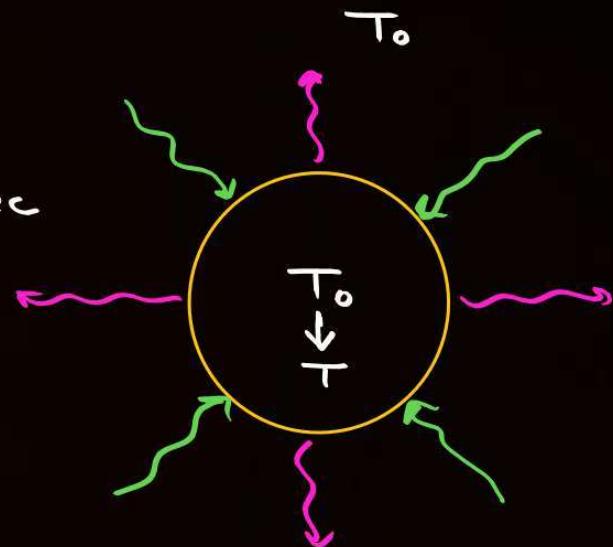
$$\sigma e A T_0^4 = \text{Heat absorbed per sec.}$$

$$\text{At } T_{\text{body}} = T$$

$$\text{Heat rad./sec} = \sigma e A T^4$$

$$\text{Heat absorbed/sec} = \sigma e A T_0^4$$

$$\text{Net rate of Heat loss} = \sigma e A (T^4 - T_0^4)$$





Rate of cooling ($-\frac{dT}{dt}$)

$$\frac{dQ_{\text{net}}}{dt} = \sigma e A (T^4 - T_0^4)$$

$$\frac{msdT}{dt} = \sigma e A (T^4 - T_0^4)$$

$$\frac{dT}{dt} = \frac{\sigma e A}{ms} (T^4 - T_0^4)$$

$$T = T_0 + \Delta T$$

$$\frac{dT}{dt} = \frac{\sigma e A}{ms} \left[(T_0 + \Delta T)^4 - T_0^4 \right]$$

$$= \frac{\sigma e A}{ms} \left[T_0^4 \left(1 + \frac{\Delta T}{T_0} \right)^4 - T_0^4 \right]$$

$$\Delta T \ll T_0 \rightarrow$$

$$\frac{\Delta T}{dt} = \frac{\sigma e A}{ms} \left[T_0^4 \left(1 + \frac{4\Delta T}{T_0} \right) - T_0^4 \right]$$

$$\frac{dT}{dt} = \frac{\sigma e A}{ms} \propto 4\Delta T \times T_0^3$$

$$\frac{dT}{dt} = \frac{4\sigma e A T_0^3}{ms} \Delta T \Rightarrow \frac{dT}{dt} \propto \Delta T$$

Newton's Law of Cooling



Newton's Law of Cooling

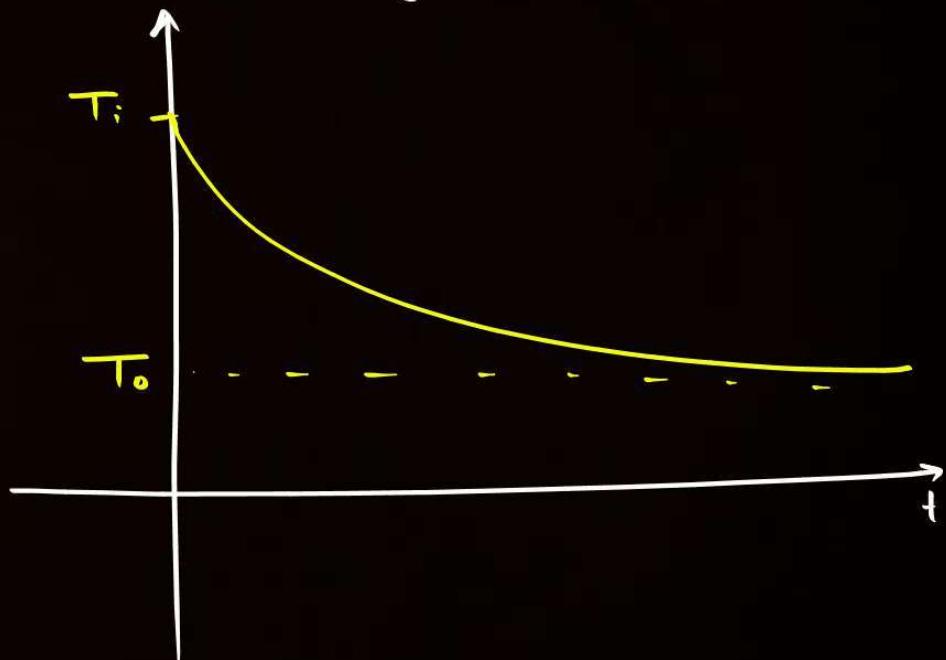


$$-\frac{dT}{dt} = k(T - T_0)$$

Rate of cooling

Temp. of body

Temp. of surrounding





$$-\frac{dT}{dt} = k(T - T_0)$$

$$\int_{T_i}^{T_f} \frac{dT}{T_0 - T} = \int_0^t k dt$$

$$\left[-\ln(T_0 - T) \right]_{T_i}^{T_f} = kt$$

$$\ln \left| \frac{T_i - T_0}{T_f - T_0} \right| = kt$$

QUESTION

$$T_0 = 20^\circ C$$

If $80^\circ C \rightarrow 70^\circ C = 100s$ then $70^\circ C \rightarrow 60^\circ C, t = ?$

$$\ln \left| \frac{T_i - T_0}{T_f - T_0} \right| = kt$$

$$\ln \left(\frac{80 - 20}{70 - 20} \right) = k \times 100 \Rightarrow \frac{\ln \frac{6}{5}}{k} = 100 \Rightarrow \frac{\ln \frac{6}{5}}{\ln \frac{5}{4}} = \frac{100}{t}$$

$$\ln \left(\frac{70 - 20}{60 - 20} \right) = k \times t \Rightarrow \frac{\ln \frac{5}{4}}{k} = t$$

$$t = 100 \frac{\ln \frac{5}{4}}{\ln \frac{6}{5}}$$

$$t = 100 \left[\frac{\ln 5 - \ln 4}{\ln 6 - \ln 5} \right]$$



Brahmastra

$$T_0 = 20$$

$$80^\circ \rightarrow 70^\circ : 100\lambda$$

$$70^\circ \rightarrow 60^\circ : t = ?$$

$$-\frac{dT}{dt} = k(T_{avg} - T_0)$$

$$\frac{\cancel{80-70}}{100} = k \left[\left(\frac{80+70}{2} \right) - 20 \right]$$
$$\frac{\cancel{70-60}}{t} = k \left[\left(\frac{70+60}{2} \right) - 20 \right]$$

$$\frac{t}{100} = \frac{55}{45}$$

$$t = \frac{11}{9} \times 100$$

QUESTION (JEE Mains – Sep. 03, 2020 (II))

A metallic sphere cools from 50°C to 40°C in 300 s. If atmospheric temperature around is 20°C , then the sphere's temperature after the next 5 minutes will be close to :

A 31°C

B 33°C

C 28°C

D 35°C

$$\ln \frac{T_i - T_0}{T_f - T_0} = k t$$

$$\frac{\ln \left(\frac{50 - 20}{40 - 20} \right)}{300} = k$$

$$\ln \left(\frac{40 - 20}{T_f - 20} \right) = k \times 300$$

$$\ln \frac{3}{2} = \ln \frac{20}{T_f - 20}$$

$$\frac{3}{2} = \frac{20}{T_f - 20} \Rightarrow T_f - 20 = \frac{40}{3}$$

$$T_f = \frac{100}{3}^{\circ}\text{C}$$

300 s

$$50 \rightarrow 40^{\circ}\text{C} : 300$$

$$40 \rightarrow T : 300$$

$$\frac{10}{300} = k [40 - 20]$$

$$\frac{40 - T}{300} = k \left[\frac{40 + T}{2} - 20 \right]$$

$$\frac{10}{40 - T} = \frac{25}{T}$$

$$10T = 50(40 - T) \Rightarrow 60T = 200$$

$$T = \frac{100}{3}^{\circ}\text{C}$$

QUESTION (JEE Mains – July. 27, 2021 (I))

A body takes 4 min. to cool from 61°C to 59°C . If the temperature of the surroundings is 30°C , the time taken by the body to cool from 51°C to 49°C is:

- A** 6 min
- B** 3 min
- C** 4 min
- D** 8 min

QUESTION (JEE Mains – 2014)

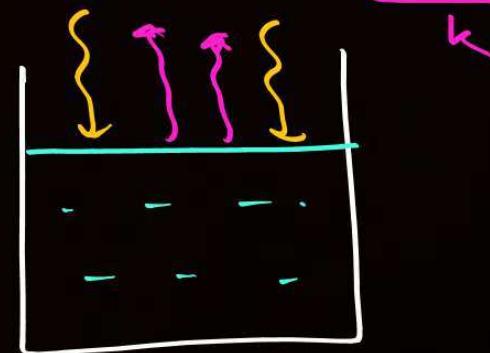
Hot water cools from 60°C to 50°C in the first 10 minutes and to 42°C in the next 10 minutes. The temperature of the surroundings is:

- A** 25°C
- B** 10°C
- C** 15°C
- D** 20°C

QUESTION (JEE Mains – JEE Adv, 2020)

A container with 1 kg of water in it is kept in sunlight, which causes the water to get warmer than the surroundings. The average energy per unit time per unit area received due to the sunlight is 700 Wm⁻² and it is absorbed by the water over an effective area of 0.05 m². Assuming that the heat loss from the water to the surroundings is governed by Newton's law of cooling, the difference (in °C) in the temperature of water and the surroundings after a long time will be $\frac{25}{3}$ °C (Ignore effect of the container, and take constant for Newton's law of cooling = 0.001 s⁻¹, Heat capacity of water = 4200 J kg⁻¹ K⁻¹)

$$Q_{in} = 700 \times 0.05 \\ = 35 \text{ J/s}$$





In steady state -

$$\frac{dT}{dt} \quad \text{Rate of cooling} = \text{Rate of Heating}$$

$$k \Delta T = \frac{35}{m s}$$

$$0.001 \times \Delta T = \frac{35}{1 \times 4200}$$

$$\Delta T = \frac{35}{4200 \times 0.001}$$

$$= \frac{350}{4200} \text{ } 50$$

$$= \frac{25}{3} {}^{\circ}\text{C}$$

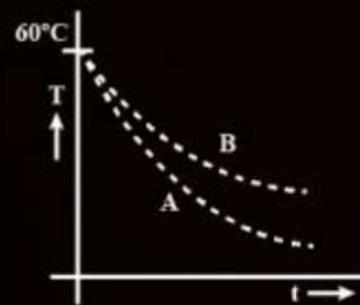
QUESTION (JEE Mains – Apr. 08, 2019 (I))

प्र०

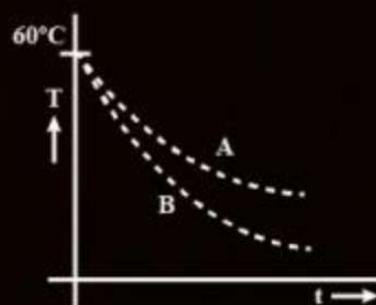


Two identical breakers A and B contain equal volumes of two different liquids at 60°C each and left to cool down. Liquid in A has density of $8 \times 10^2 \text{ kg/m}^3$ and specific heat of $2000 \text{ J kg}^{-1} \text{ K}^{-1}$ while liquid in B has density of $10^{-3} \text{ kg m}^{-3}$ and specific heat of $4000 \text{ J kg}^{-1} \text{ K}^{-1}$. Which of the following best describes their temperature versus time graph schematically? (assume the emissivity of both the beakers to be the same)

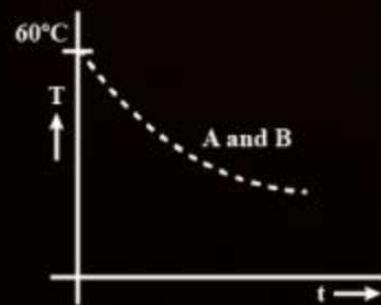
A



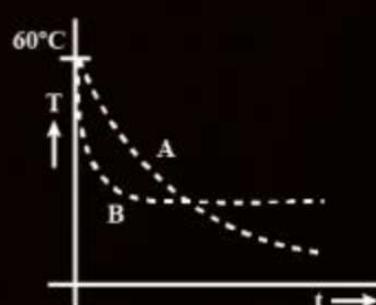
B



C



D





Homework



DPP + Class Q.