

# Topics to be covered

1) Reflection from plane mirror and spherical mirrors

2) Refraction of Light

3) TIR

4) Prism

5) Refraction from spherical surfaces

6) Thin lenses

7) Questions



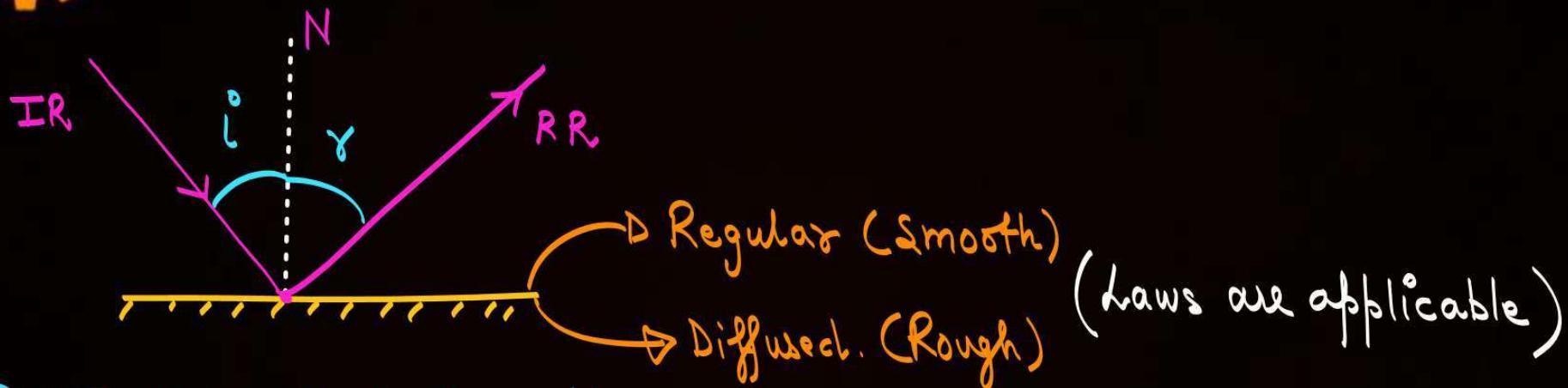
7 - 8 hours

# younity.pw.live

| doubts  
o  
| doubt

| Notes  
| Note

## Reflection and laws of Reflection



\* IR, N, RR lie in same plane.

$$\angle i = \angle r$$

Vector form:-

$$\hat{I} = \hat{R} + 2(\hat{I} \cdot \hat{n})\hat{n}$$

dir of IR      dir of RR      dir of normal.

Yes it is Imp!

## Plane Mirror

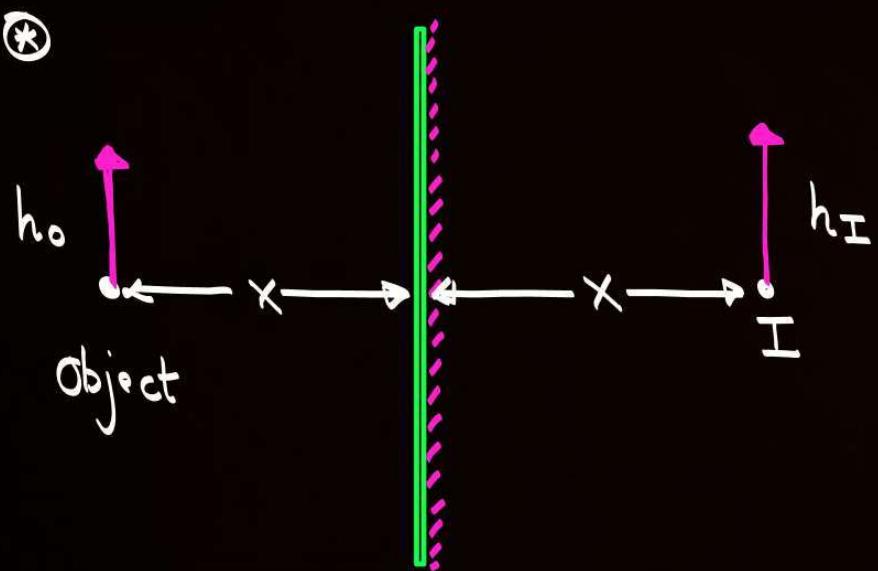
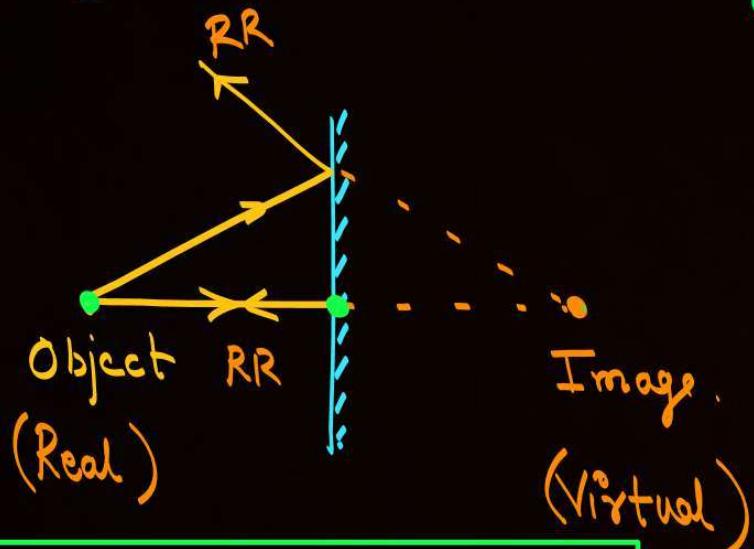


Image distance = object distance.

Size of Image = Size of object

$$|h_o| = |h_I|.$$

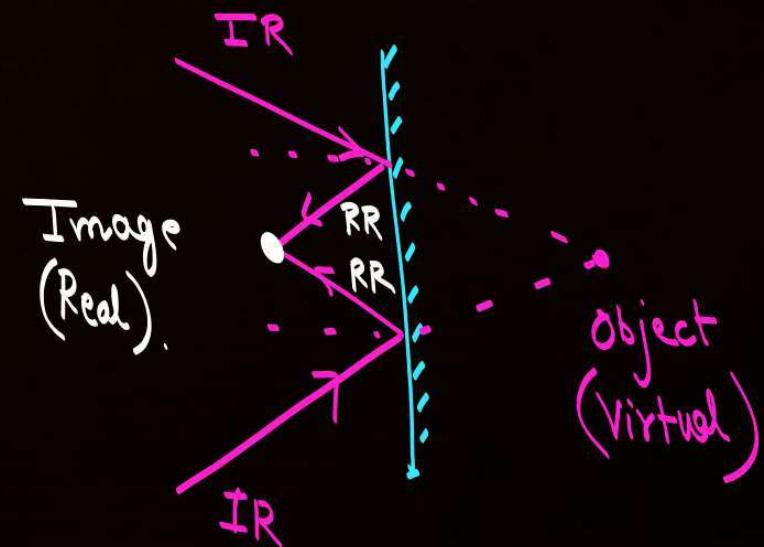
⊗ Object & Image are always of opp Nature.



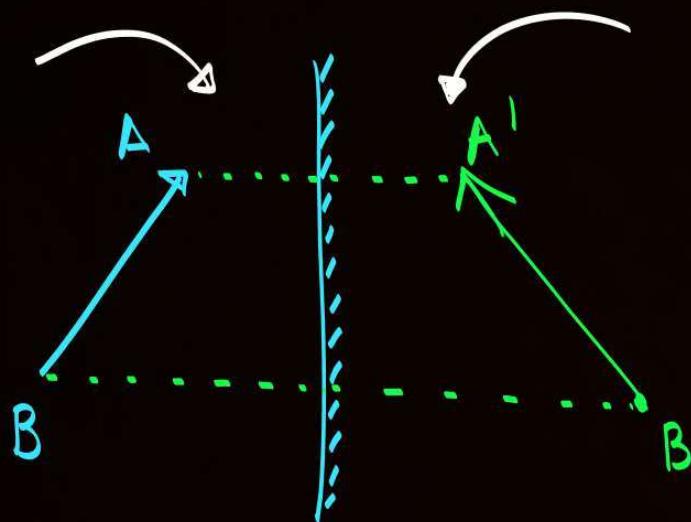
"Plane Mirror is  $\perp$  bisector to line joining O & I".

Image  $\rightarrow$  Intersection of RR

Object  $\rightarrow$  Intersection of IR



\* *Laterally Inverted.*



Clock Problems :-

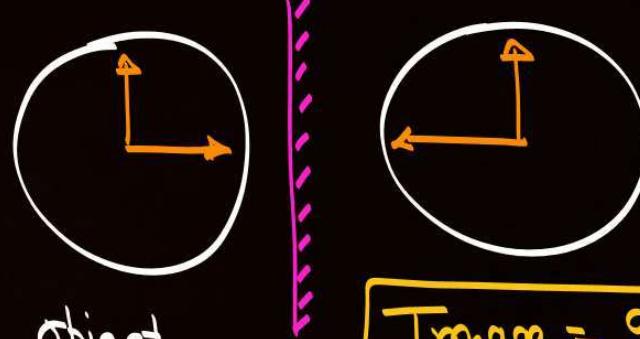


Image = 9      Ans. (12-3)

Ex:- Clock 8:50

$$\text{Image time} \Rightarrow 11:60 - 8:50 = \underline{\quad}$$

Ex:- Clock 5:20:35

$$\text{Image} = 11:59:60 - 5:20:35$$

$$= \underline{\quad}$$



## Plane mirror



- **Image Distance is equal to object distance**
- **Nature of Image is opposite to that of object**
- **Image is laterally Inverted**



## Plane mirror



- Rotation of object in front of plane mirror

Case.1. Object is Rotated.

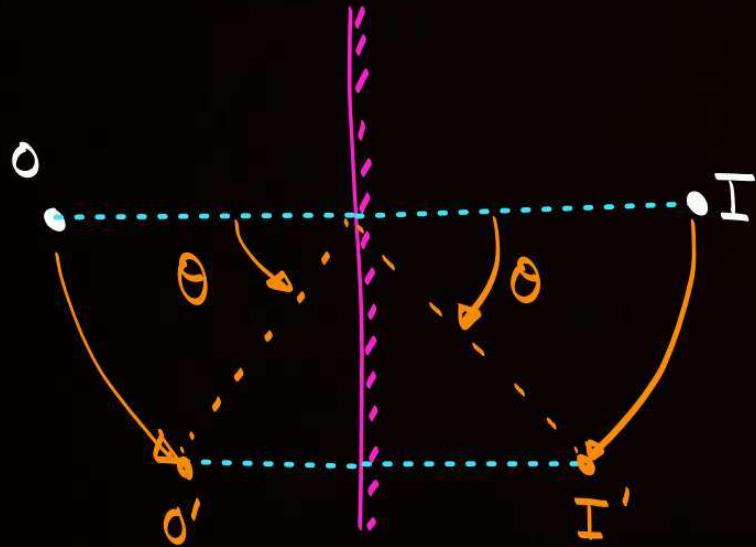
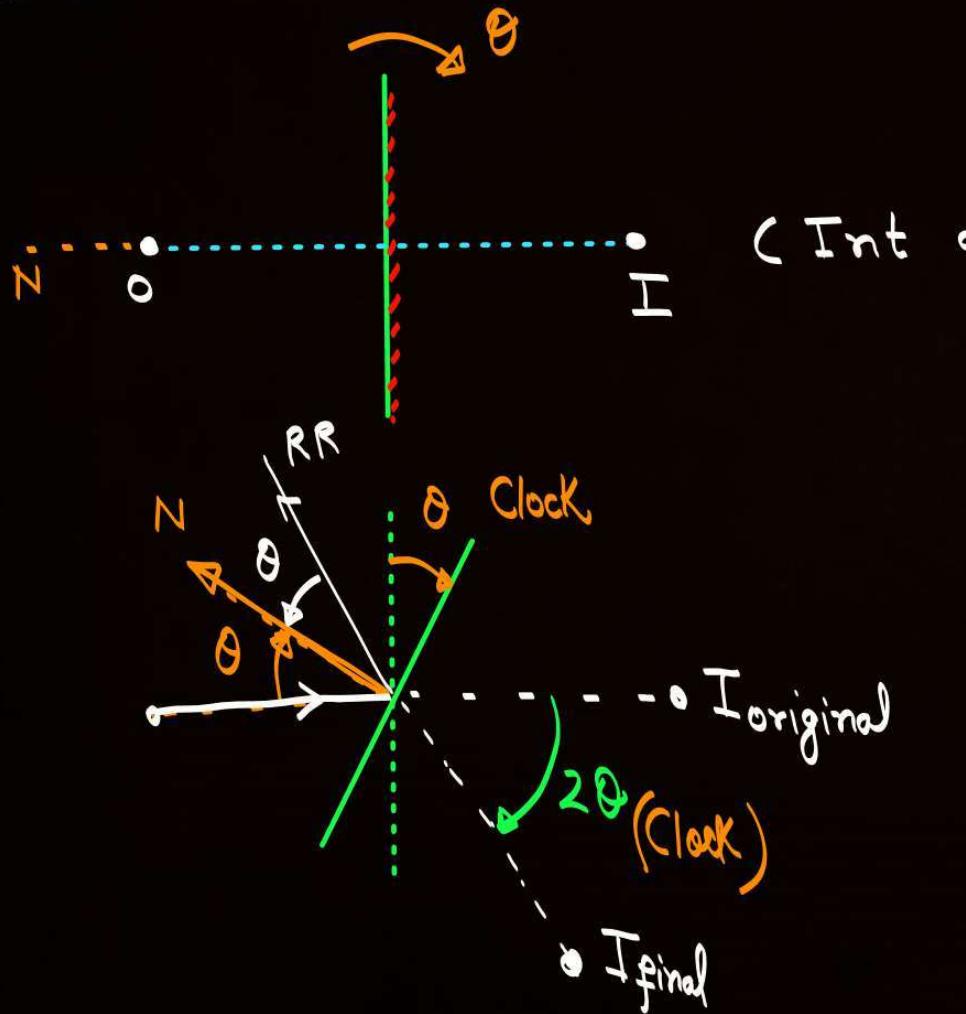


Image Rot by Same Angle in opp Sense.

## \* Case 2. Mirror is Rotated.



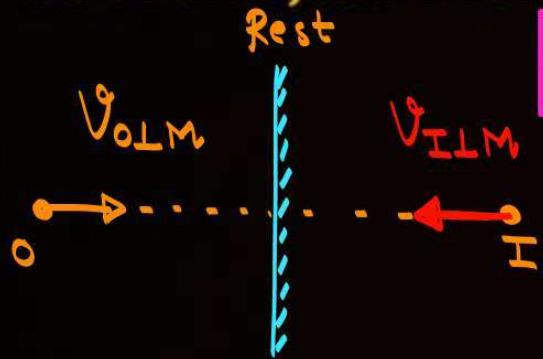
If Mirror is Rot by  $\theta$   
Image Rotates by  $2\theta$  in Same Sense.



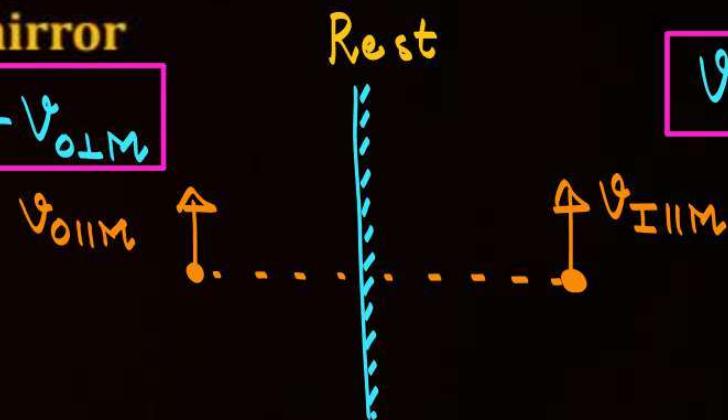
## Plane mirror



- Motion of object in front of plane mirror

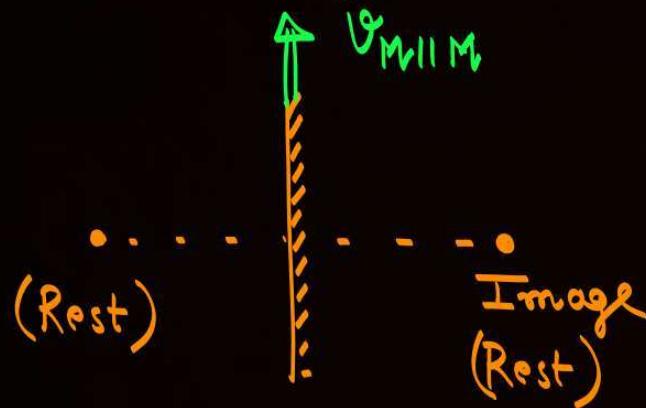


$$\textcircled{R} \quad v_{ILM} = -v_{OLM}$$



$$v_{IIM} = v_{OIM}$$

Case 2. Object Rest / M.  $\rightarrow$  Moving.



No Impact Velocity  
of Image.

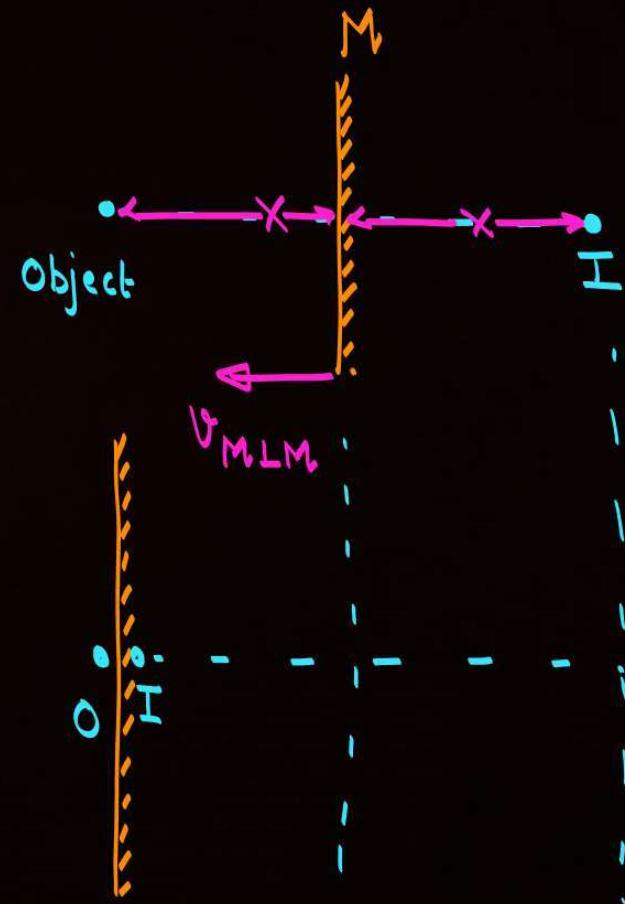
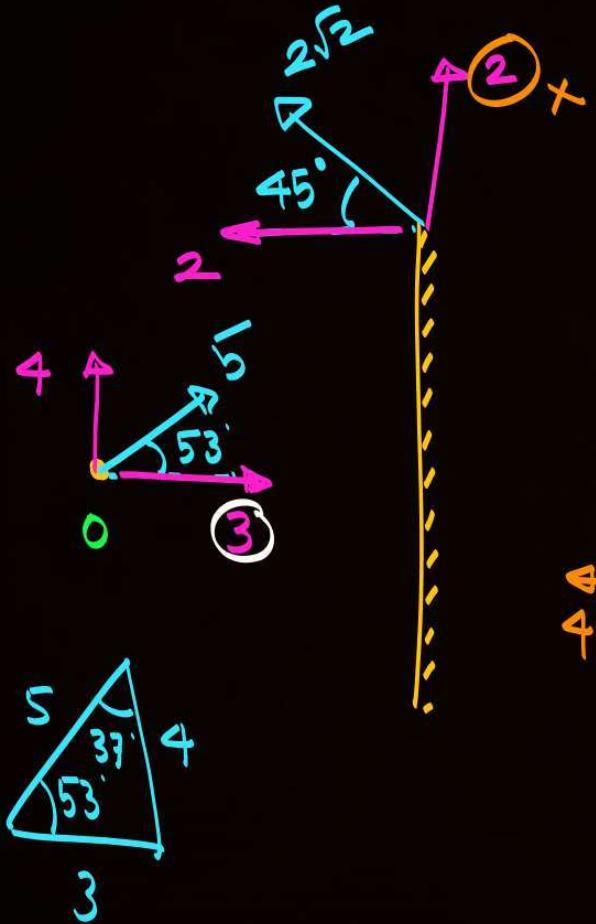
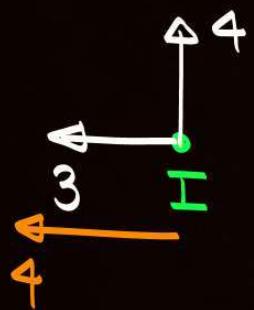


Image moves  
with  $2v$   
wrt ground  
in same dir  
of Mirror.

$\hat{e}_x, \hat{e}_y$ 


$V_{\text{Image w.r.t ground}} = ?$

$$\vec{V}_{I/g} = -7\hat{i} + 4\hat{j}$$



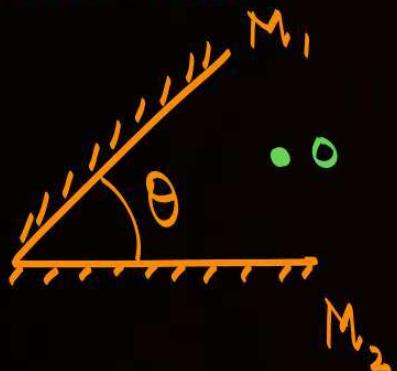
$$\begin{aligned}
 \oplus \quad \vec{V}_{I/O} &= \vec{V}_{I/g} - \vec{V}_{o/g} \\
 &= (-7\hat{i} + 4\hat{j}) - (3\hat{i} + 4\hat{j}) \\
 &= -10\hat{i} =
 \end{aligned}$$



## Plane Mirror



❖ No of images



1. Calculate  $\frac{360}{\theta}$

Even

odd

$$\text{No of Image} = \left( \frac{360}{\theta} - 1 \right)$$

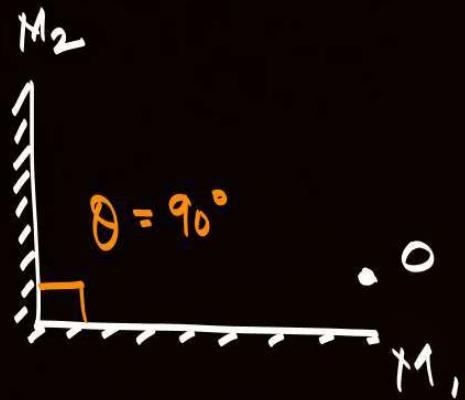
Object Symmetric

$$\left( \frac{360}{\theta} - 1 \right)$$

Object Asymmetric

$$\left( \frac{360}{\theta} \right)$$

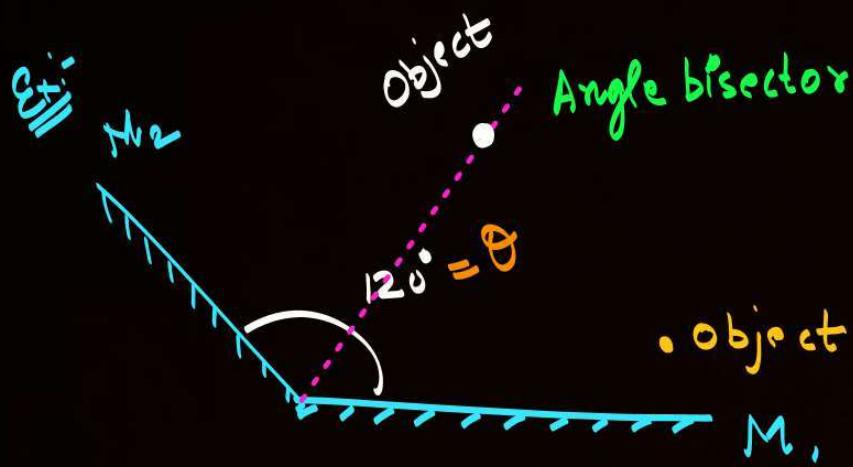
Ex:-



No of Images.

$$\textcircled{S} \quad \frac{360}{90} = 4 \quad (\text{Even})$$

No of Images = 3



Angle bisector (In this Case : No of I =  $\frac{360}{\theta}$ )

$$= 3 - 1 = \boxed{2}$$



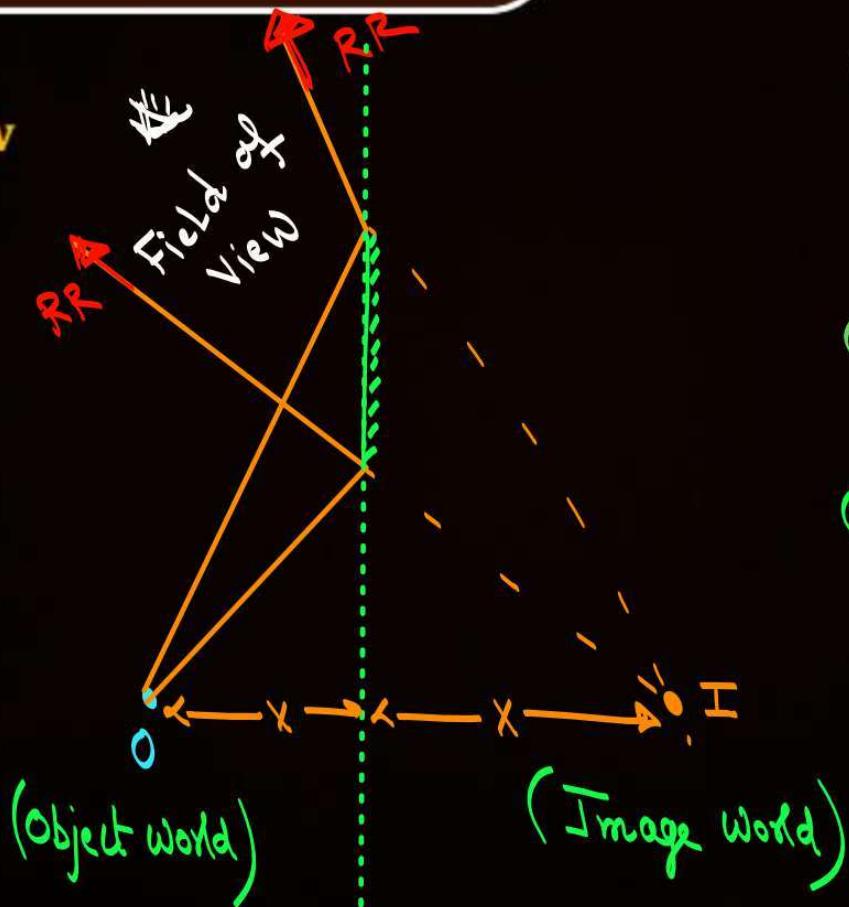
No of Images =

$$\textcircled{*} \quad \frac{360}{\theta} = \frac{360}{120} = 3 \quad (\text{odd})$$

No of Images = 3

# Plane Mirror

## ❖ Field of View



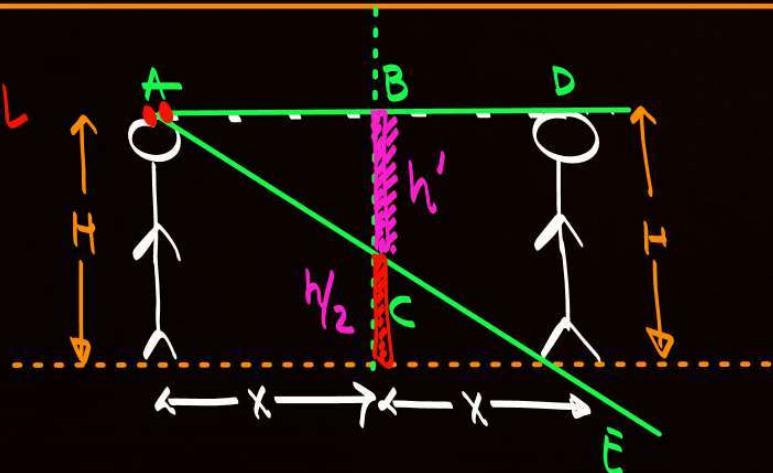
- ④ Whatever may be the Size / Location of Mirror Image is always formed.
- ④ Draw an Extended Mirror Object dist = Image dist.
- ④ Size of Mirror will decide the portion of Image Visible.

Ex:- Minimum Size of Mirror to form Complete Image.

"Point Size".

Ex:- Minimum Size of Mirror to See Complete Self

Eye Level



$$ABC \sim ADE \quad \textcircled{1}$$

$$\frac{AB}{AD} = \frac{h'}{H}$$

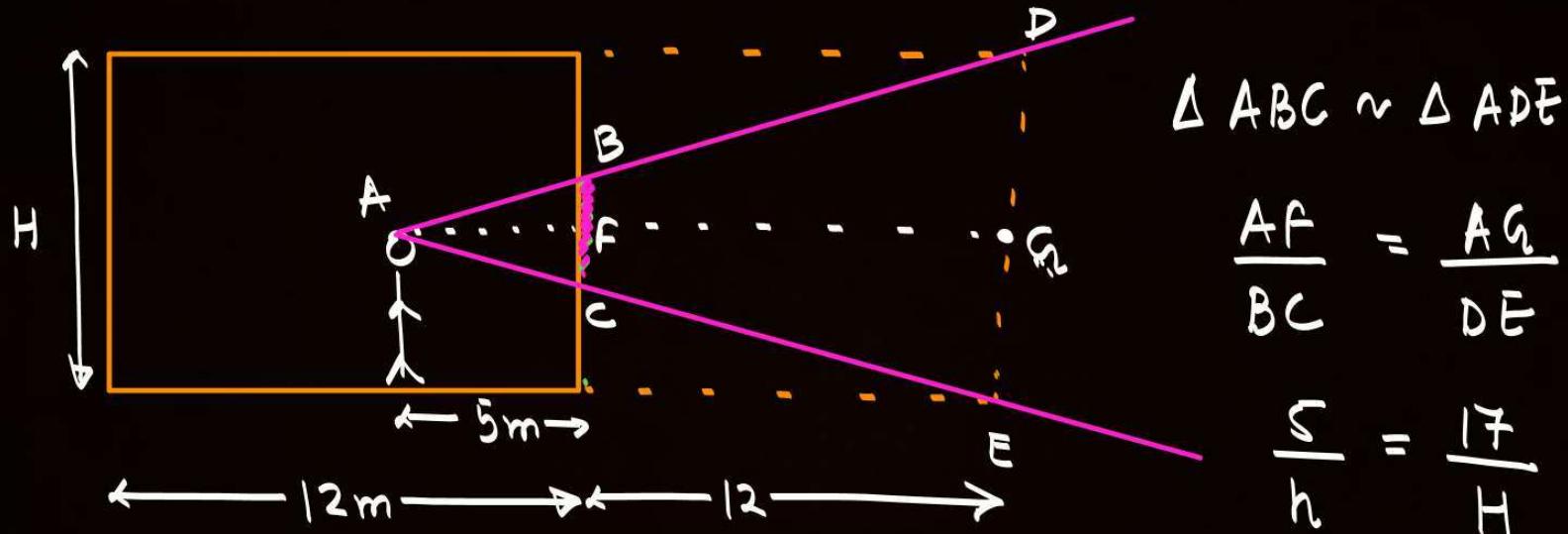
$$\frac{x}{2x} = \frac{h'}{H}$$

$$h' = H/2$$

Mirror should be placed  
at distance  $\frac{H}{2}$  from  
ground

Q3

Min Size of Mirror to See Complete back Wall.



$$\triangle ABC \sim \triangle ADE$$

$$\frac{AF}{BC} = \frac{AG}{DE}$$

$$\frac{5}{h} = \frac{17}{H}$$

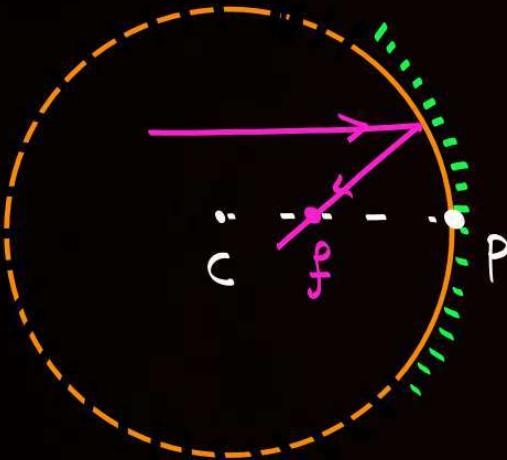
$$h = \frac{5H}{17}$$



# Spherical Mirror

④ all Para-axial Rays

PW



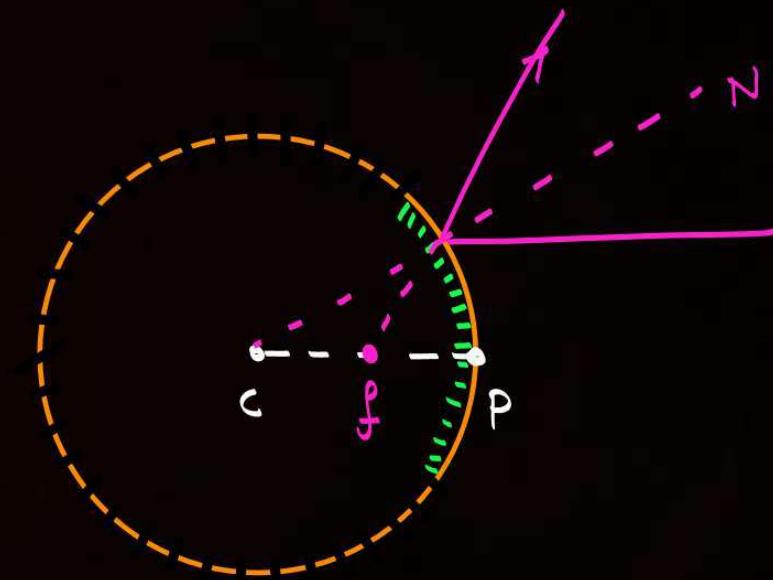
Concave Mirror

"Converging"

Sphere Radius = R

$$f = R/2$$

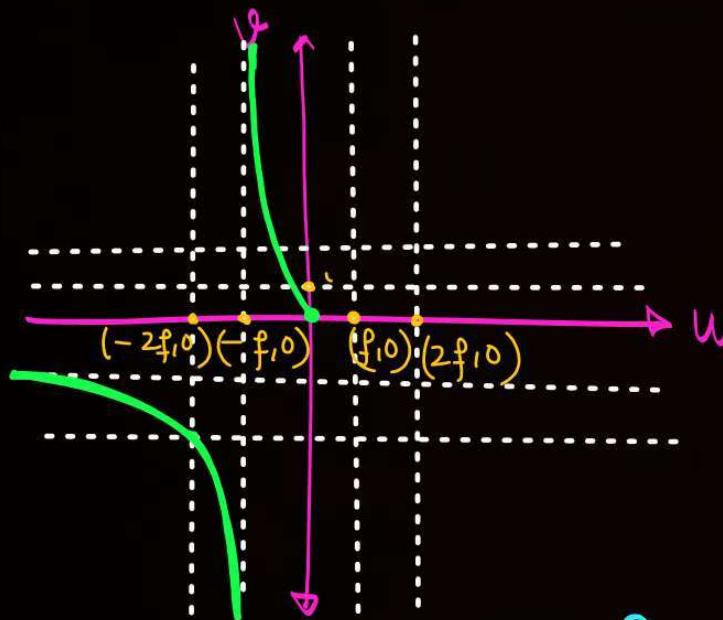
④ Independent of Med.



Convex Mirror

Diverging Mirror.

# Ray diagrams



$$\begin{aligned}
 u &\rightarrow -\infty & v &\Rightarrow -f & u &\rightarrow -f^{\ominus} & v &= +\text{ve.} \\
 u &\rightarrow -2f & v &= -2f & & & \\
 u &\rightarrow -f & v &= -\infty & & &
 \end{aligned}$$

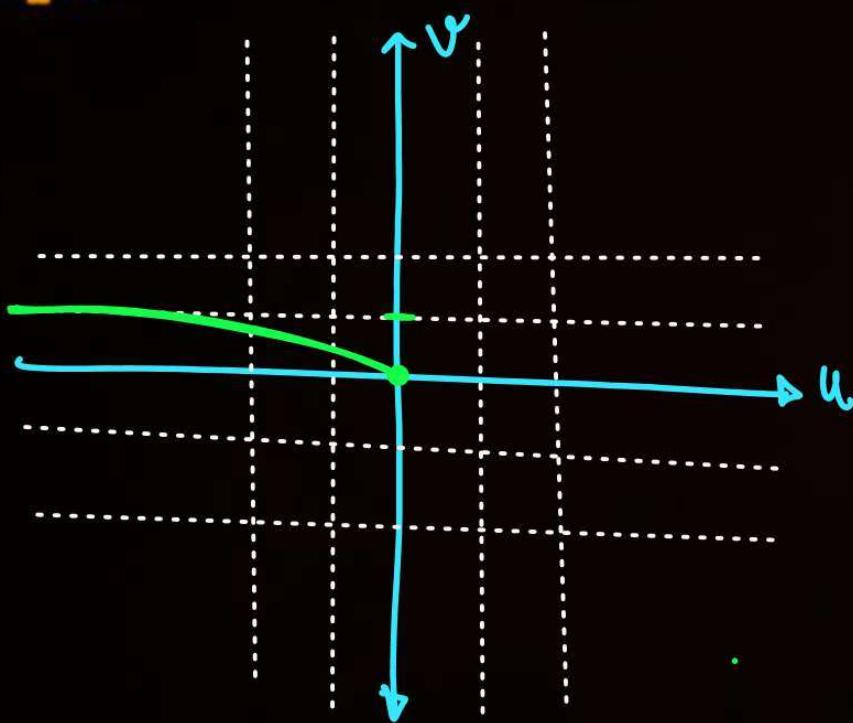
Real

Virtual.

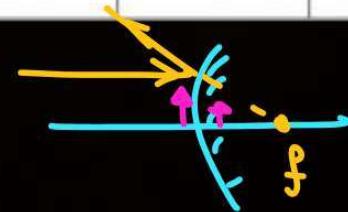
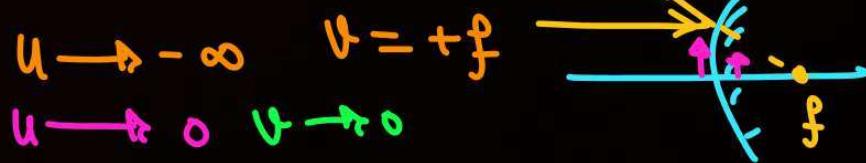
1. At infinity		At the principal focus or in the focal plane	Real, inverted, extremely diminished in size
2. Beyond the centre of curvature		Between the principal focus and centre of curvature	Real, inverted and diminished
3. At the centre of curvature		At the centre of curvature	Real, inverted and equal to object
4. Between focus and centre of curvature		Beyond centre of curvature	Real, inverted and bigger than object.
5. At the principal focus		At infinity	Extremely magnified
6. Between the pole and principal focus		Behind the mirror	Virtual, erect and magnified

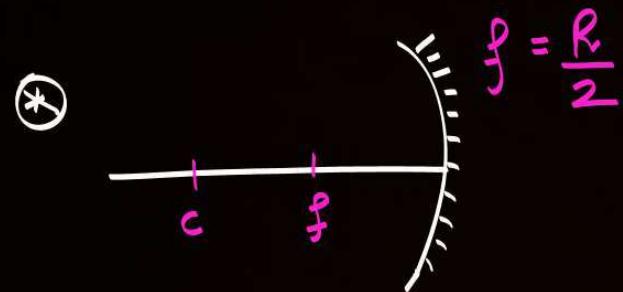


# Ray diagrams



(a)	<p>Diagram (a) shows a converging lens forming a real image. An object <math>B</math> is at position <math>B</math> on the left. A green horizontal ray from <math>B</math> is parallel to the axis and refracts as if it originated from the focal point <math>F</math>. A red vertical ray from <math>B</math> passes straight through the lens. A blue vertical ray from <math>B</math> is directed towards the focal point <math>F</math> and refracts parallel to the axis. The three refracted rays converge at a point <math>B'</math> on the right, which is the real image of <math>B</math>. The image is inverted and has the same height as the object.</p>	Between infinity and the pole	Behind the mirror between the focus and the pole	Virtual, smaller and erect
(b)	<p>Diagram (b) shows a converging lens forming a real image. An object <math>B</math> is at position <math>B</math> on the left. A green horizontal ray from <math>B</math> is parallel to the axis and refracts as if it originated from the focal point <math>F</math>. A red vertical ray from <math>B</math> passes straight through the lens. A blue vertical ray from <math>B</math> is directed towards the focal point <math>F</math> and refracts parallel to the axis. The three refracted rays converge at a point <math>B'</math> on the right, which is the real image of <math>B</math>. The image is inverted and has the same height as the object.</p>	At infinity	Behind the mirror at the focus $F$	Virtual, point-sized and erect





\* If object is placed Near to Mirror, Image is formed.

$$\frac{1}{f} = \frac{1}{v} + \frac{1}{u}$$

\* Mirror formula.

$u$  = Object dist from P

$v$  = Image dist from P

$f$  = focal length from P.

Lateral Magnification =  $m_{Lat} = \frac{h_I}{h_o} = -\frac{v}{u}$

magnifications

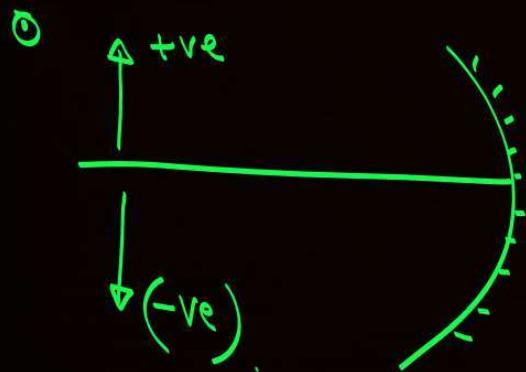
Longitudinal Magnification =  $m_{long} = \frac{t_I}{t_o} = \boxed{\frac{-v^2}{u^2}}$

\* Small thickness.

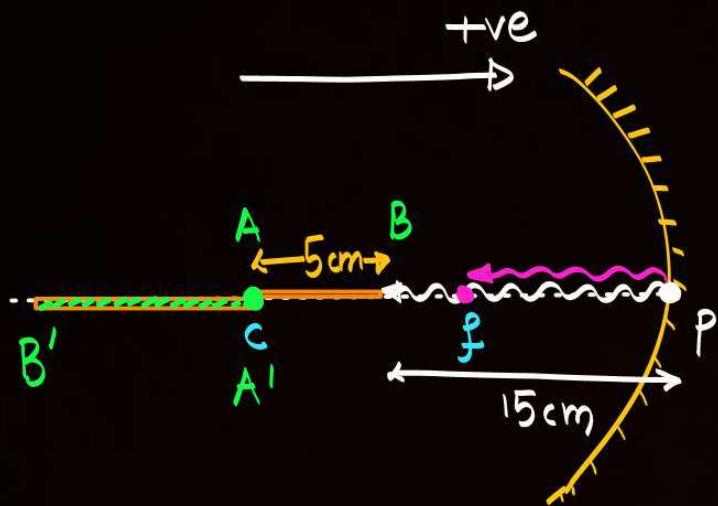
## # Sign Convention.



- dir of IR  $\rightarrow$  (positive)
- all distances are measured from Pole.
- distance measured in dir of IR (+ve)
- " " " opp dir of IR (-ve)



\*



\* find Length of Image

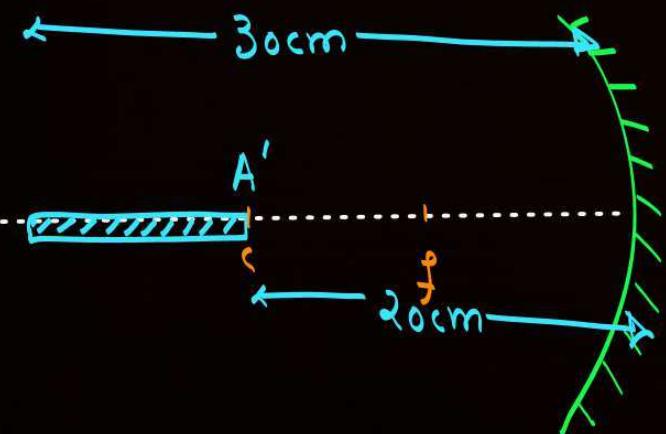
Sol:- Image of A  $\rightarrow$  at C.

(B) Object distance =  $-15\text{cm}$

$$f = -10$$

$$\frac{1}{f} = \frac{1}{V} + \frac{1}{U}$$

$$-\frac{1}{10} = \frac{1}{V} - \frac{1}{15} \Rightarrow \frac{1}{V} = \frac{1}{15} - \frac{1}{10} = \frac{2-3}{30}$$

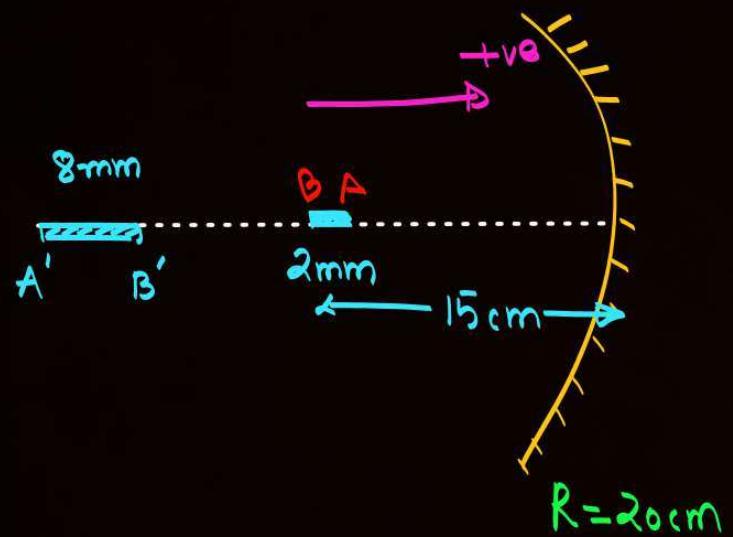


length of Image =  $10\text{cm}$

Ans.

$V = -30\text{cm}$

# Previous Ques.



$$u = -15$$

$$f = -10$$

$$\frac{1}{f} = \frac{1}{v} + \frac{1}{u}$$

$$V = -30\text{cm}$$

\* find thickness of Image .

for Small thickness

$$m_{\text{long}} = \frac{t_I}{t_o} = -\frac{v^2}{u^2}$$

$$= \frac{t_I}{2\text{mm}} = -\frac{(30 \times 30)}{18 \times 18}$$

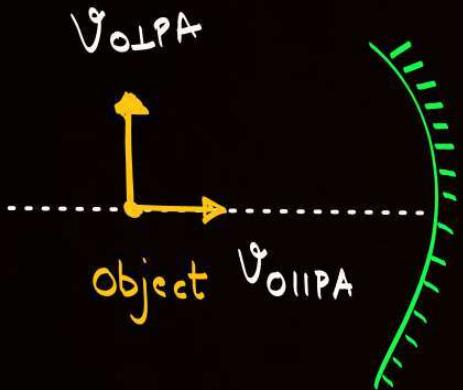
$$t_I = -8\text{mm}$$

↓  
Inverted.

Length along PA = thickness

length  $\perp$  to PA = height

## # Velocity Magnifications for both Mirrors.



Object move Karega  $\rightarrow$  Image move Karegi.

$$v_{Image \perp PA} = (m_{Lat}) v_{Object \perp PA}$$

$$v_{Image \parallel PA} = (m_{Long}) v_{Object \parallel PA}$$

$$m_{Lat} = -\frac{v}{u}$$

$$m_{Long} = -\frac{v^2}{u^2}$$

## Question 1



When one light ray is reflected from a plane mirror with  $30^\circ$  angle of reflection, the angle of deviation of the ray after reflection is

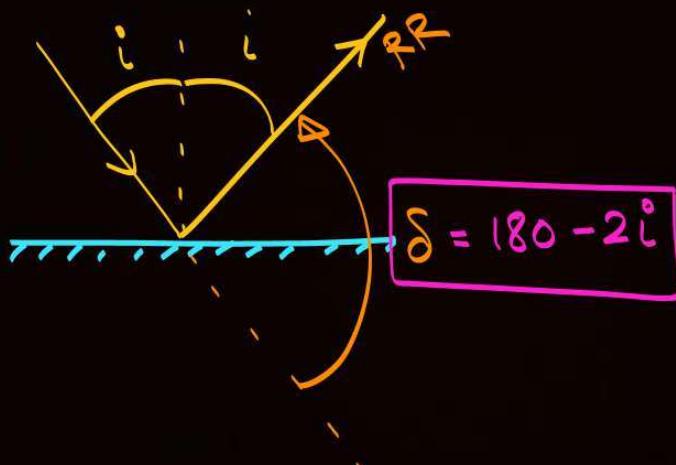
[Main 11<sup>th</sup> April 2<sup>nd</sup> Shift 2023]

1  $130^\circ$

2  $120^\circ$  Ans

3  $110^\circ$

4  $140^\circ$   $\angle i = \angle r = 30^\circ$



Initial dir of IR

$$\text{Ans} = 180 - 2 \times 30$$

$$= 120^\circ$$

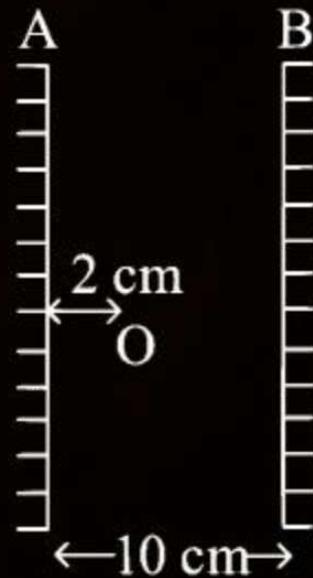
[Ans: 2]

## Question 2

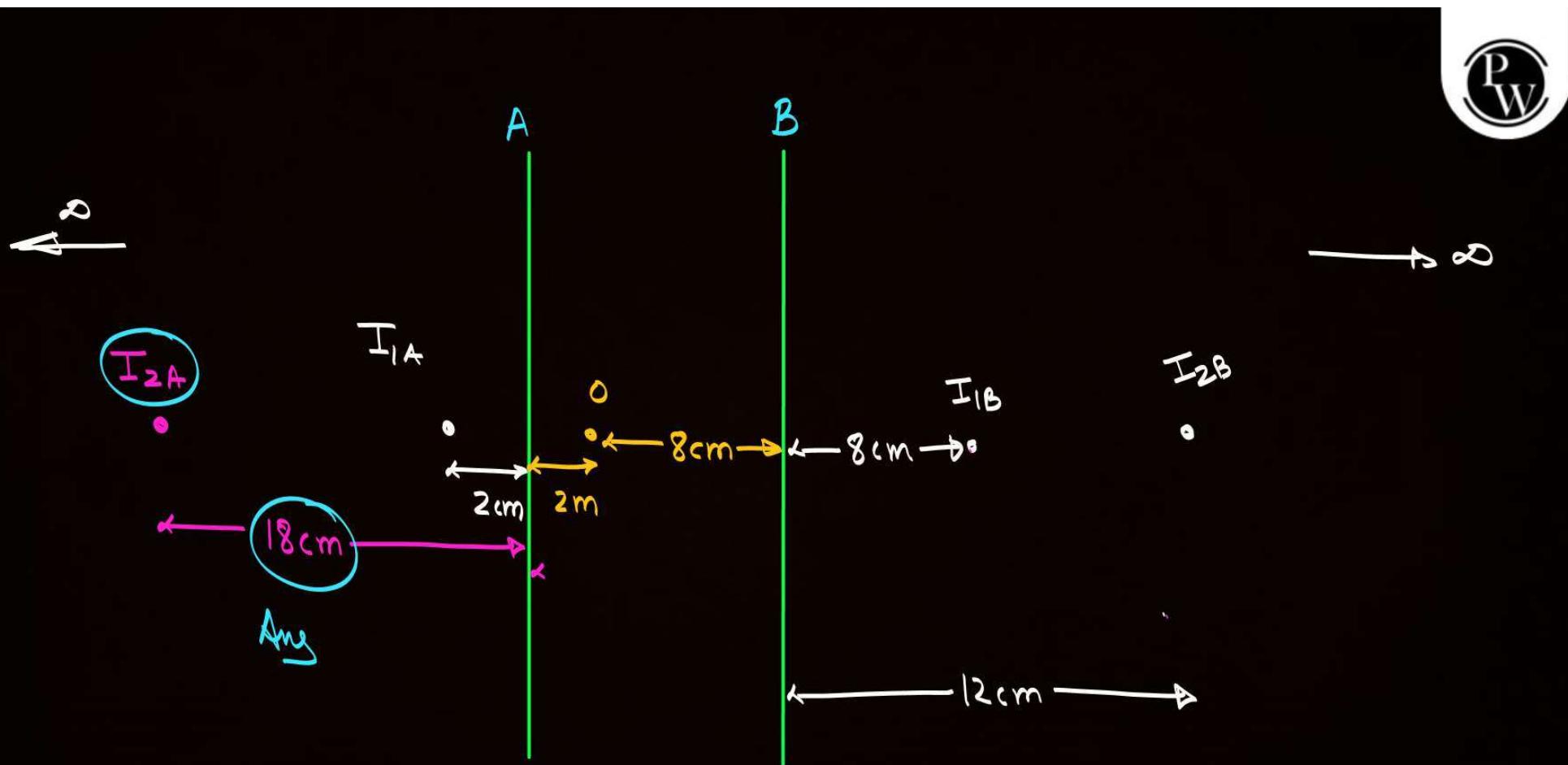


Two vertical parallel mirrors  $A$  and  $B$  are separated by 10 cm. A point object  $O$  is placed at a distance of 2 cm from mirror  $A$ . The distance of the second nearest image behind mirror  $A$  from the mirror  $A$  is ..... cm. [Main 6<sup>th</sup> April 1<sup>st</sup> Shift 2023]

$$\boxed{\text{No of Image} = \infty}$$



[Ans: 18]



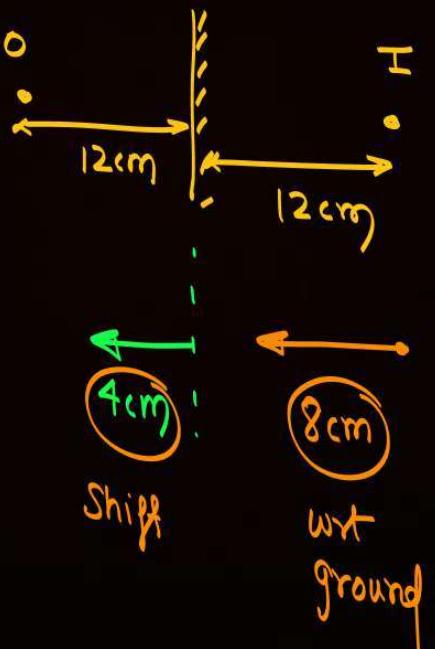
### Question 3



An object is placed at a distance of  $12\text{ cm}$  in front of a plane mirror. The virtual and erect image is formed by the mirror. Now the mirror is moved by  $4\text{ cm}$  towards the stationary object. The distance by which the position of image would be shifted, will be

[Main 10<sup>th</sup> April 1<sup>st</sup> Shift 2023]

- 1 ~~4 cm towards mirror~~
- 2  4 cm towards mirror
- 3 8 cm ~~away from mirror~~
- 4 ~~8 cm towards mirror~~



**Question 4**

The incident ray, reflected ray and the outward drawn normal are denoted by the unit vectors  $\vec{a}$ ,  $\vec{b}$  and  $\vec{c}$  respectively. Then choose the correct relation for these vectors

[JEE (Main) 2021 (24<sup>th</sup> Feb Shift 2)]

**1**

$$\vec{b} = 2\vec{a} + \vec{c}$$

$$\begin{aligned}\text{I.R} &= \vec{a} \\ R &= \vec{b}\end{aligned}$$

**2**

$$\vec{b} = \vec{a} - \vec{c}$$

$$n = \vec{c}$$

$$\hat{\vec{I}} = \hat{R} + 2(\hat{I} \cdot \hat{n})\hat{n}$$

**3**

$$\vec{b} = \vec{a} + 2\vec{c}$$

$$\vec{a} = \vec{b} + 2(\vec{a} \cdot \vec{c})\vec{c}$$

**4**

$$\vec{b} = \vec{a} - 2(\vec{a} \cdot \vec{c})\vec{c}$$

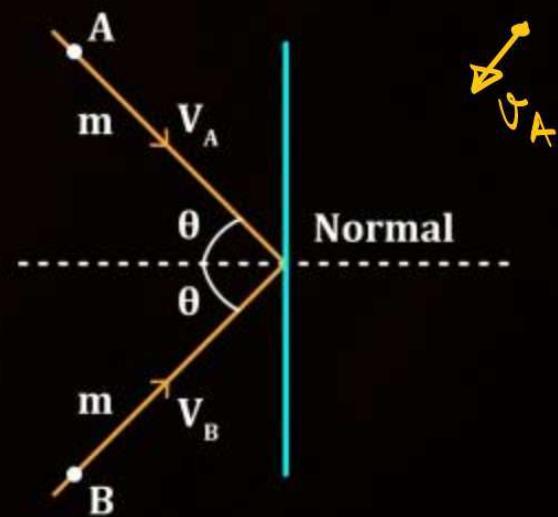
~~Ans~~

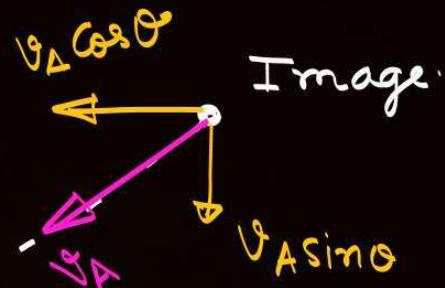
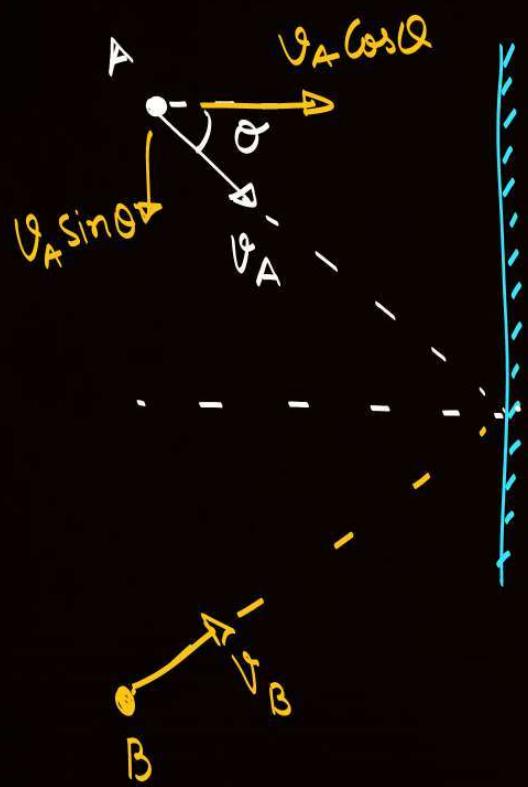
## Question 5



Two bodies  $A$  and  $B$  are moving towards a plane mirror with speeds  $V_A$  and  $V_B$  respectively as shown in the figure. The speed of image of  $A$  with respect to the body  $B$  is:

- 1  $V_A + V_B$  Ans
- 2  $|V_A - V_B|$
- 3  $\sqrt{V_A^2 + V_B^2}$
- 4  $\sqrt{V_A^2 - V_B^2}$





$$v_{\text{Image A wrt B}} = v_A + v_B$$

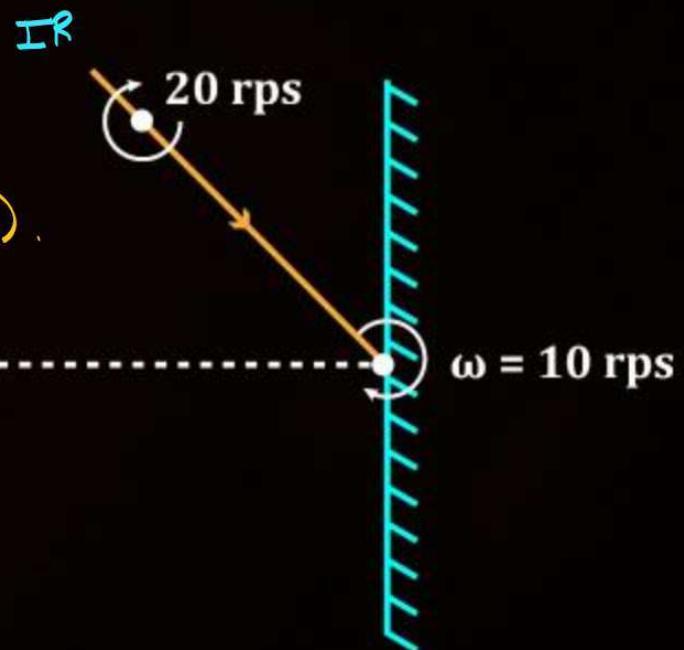
## Question 6



For the arrangement shown below, determine the angular speed with which the reflected beam will rotate.

- 1 40 rps
- 2 20 rps
- 3 30 rps
- 4 0 rps

Object (IR) Rotates  
 $\omega_{\text{Image}} = \text{anticlock } (20 \text{ rps})$ .  
Mirror (clock 10 rps)  
Image = (clockwise 20 rps)  
Ans  
0 rps.



## Question 7



A boy is walking under an inclined mirror at a constant velocity  $v$  m/s along the  $X$ -axis as shown in figure. If the mirror is inclined at an angle  $\theta$  with the horizontal then what is the velocity of the image?

[IIT-JEE 2002]

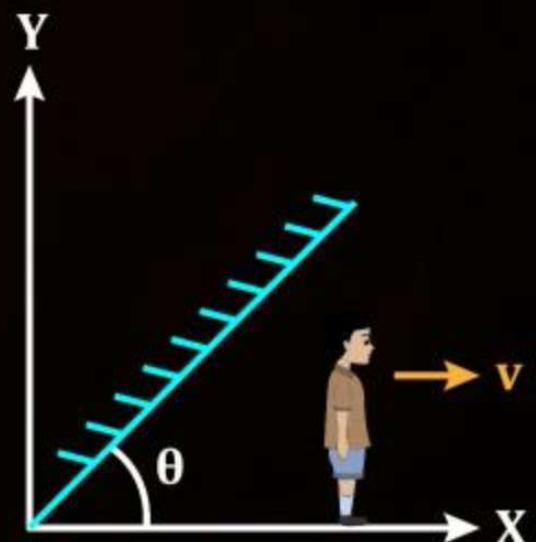
1  $v \sin \theta i + v \cos \theta j$

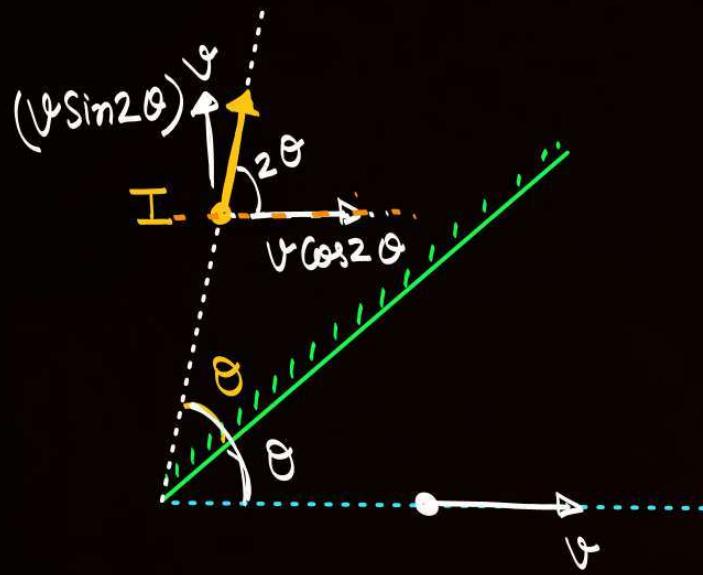
2  $v \cos \theta i + v \sin \theta j$

3  $v \sin 2\theta i + v \cos 2\theta j$

4  $v \cos 2\theta i + v \sin 2\theta j$

*Ans*



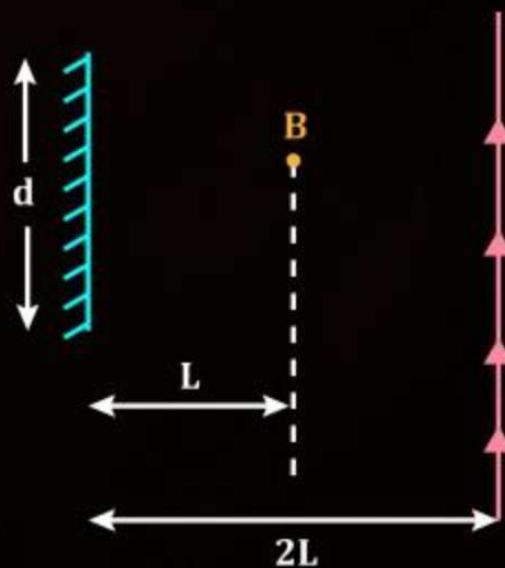


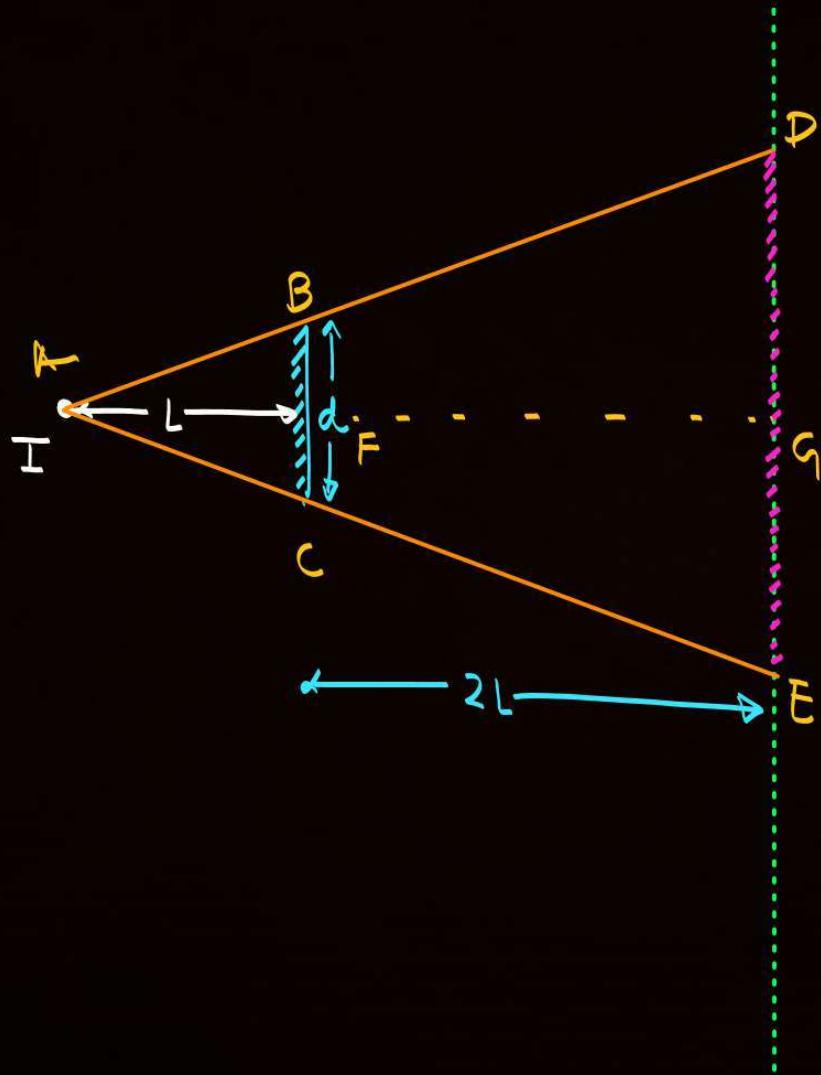
$$\text{Ans} = v \cos 2\theta \hat{i} + v \sin 2\theta \hat{j}$$

**Question 8**

A point source of light  $B$  is placed at a distance  $L$  in front of the centre of a mirror of width  $d$  hung vertically on a wall. A man walks in front of the mirror along a line parallel to the mirror at a distance  $2L$  from it as shown. The greatest distance over which he can see the image of the light source in the mirror is: [IIT-JEE 2002]

- 1**  $d/2$
- 2**  $d$
- 3**  $2d$
- 4**  $3d$  *Ans*





$\triangle ABC \sim \triangle ADE$

$$\frac{AF}{AG} = \frac{BC}{DE}$$

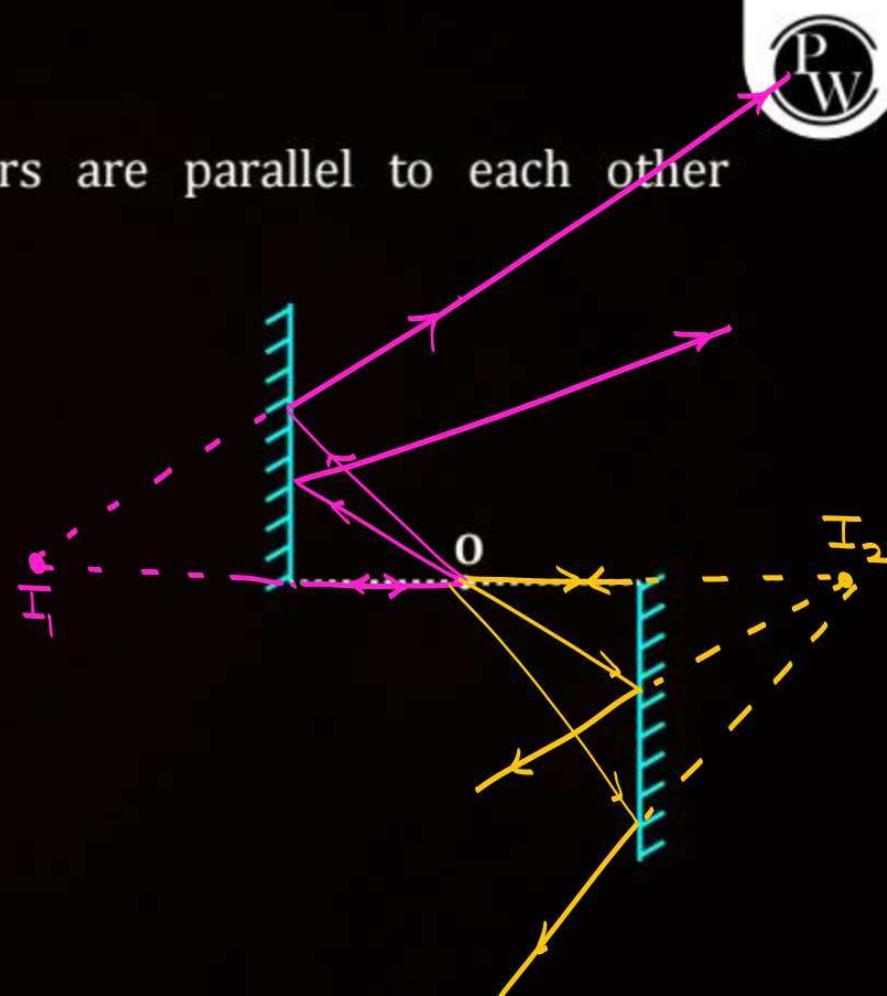
$$\frac{L}{3L} = \frac{d}{d'}$$

$$d' = 3d$$

## Question 9

Find no of image formed, When two mirrors are parallel to each other  
 $\theta = 180^\circ$

- 1 2. Ans
- 2 3
- 3 4
- 4  $\infty$



## Question 10



Find no of image formed, When two mirrors are  $\perp$  to each other  $\theta = 90^\circ$

1

Ans

2

$I_{m_1}$

3

4

3

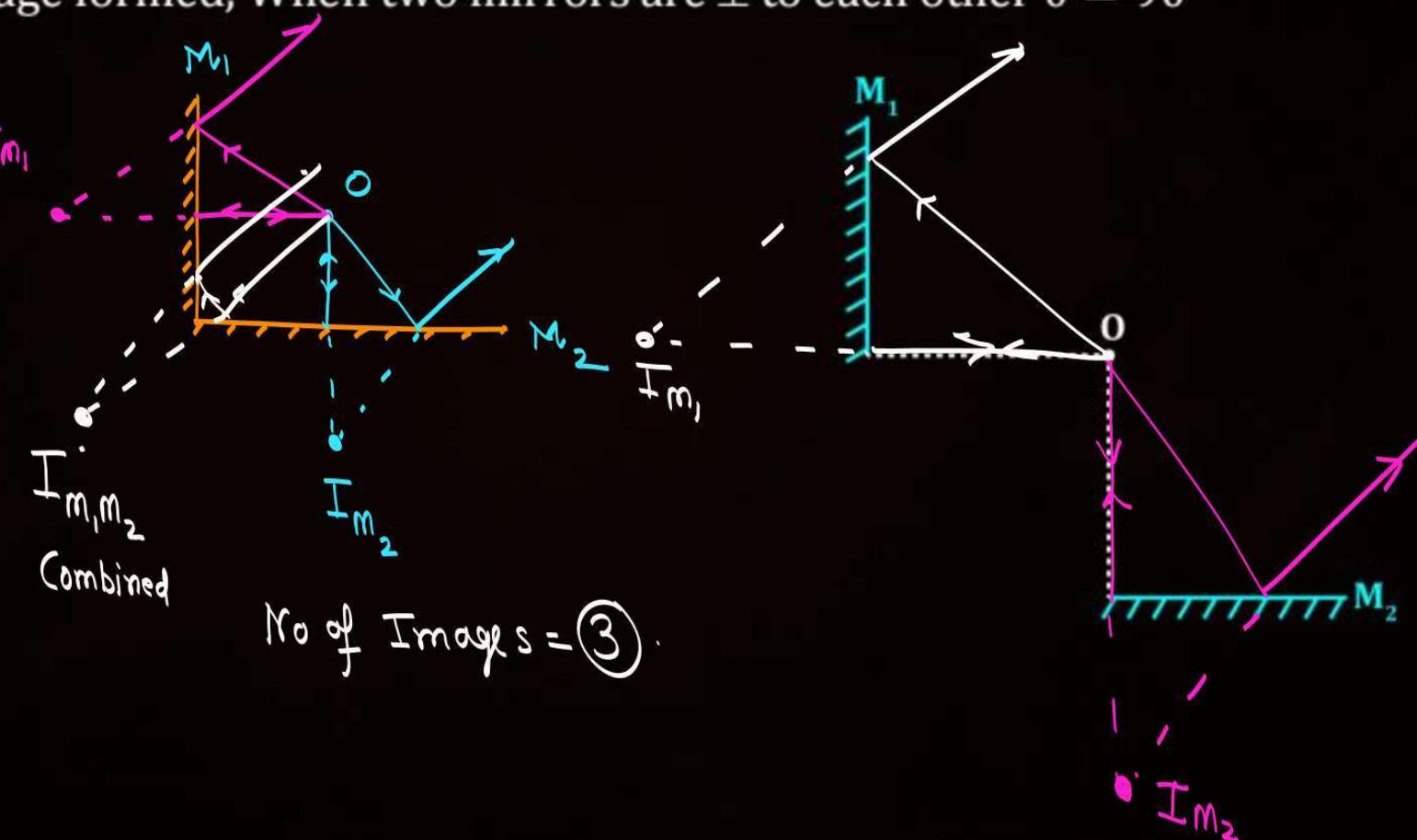
4

4

$\infty$

$I_{m_1, m_2}$   
Combined

No of Images = ③



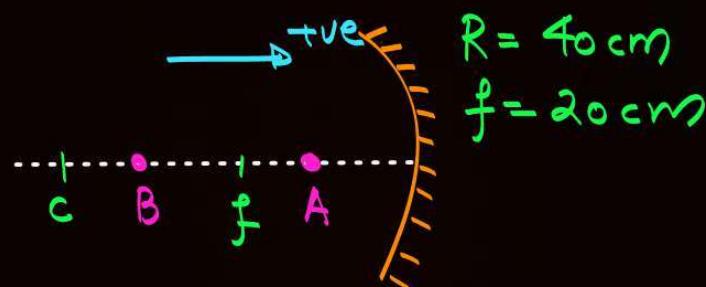
## Question 11



Two objects  $A$  and  $B$  are placed at 15 cm and 25 cm from the pole in front of a concave mirror having radius of curvature 40 cm. The distance between images formed by the mirror is

[Main 1<sup>st</sup> Feb 2<sup>nd</sup> Shift 2023]

- 1 40 cm
- 2 160 cm
- 3 60 cm
- 4 100 cm



$$\frac{1}{f} = \frac{1}{V} + \frac{1}{U}$$

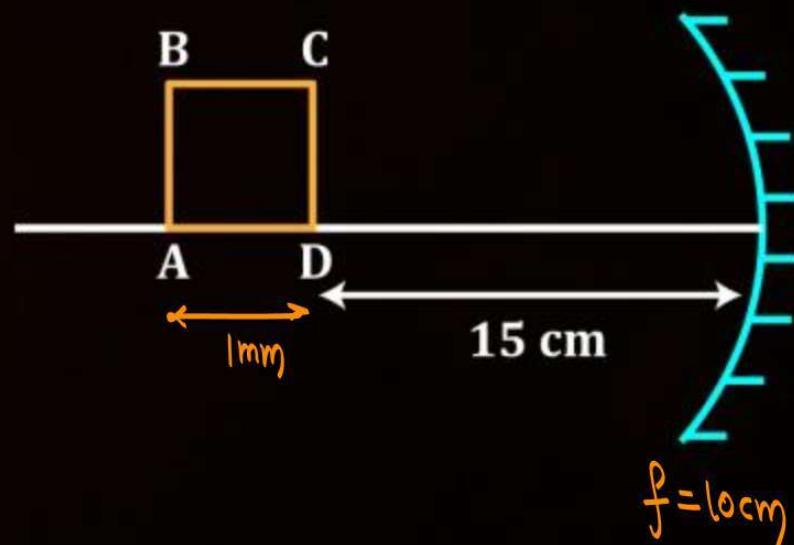
$$\left| \begin{array}{l} \frac{1}{V} = \frac{1}{15} - \frac{1}{20} \\ V_A = \dots \end{array} \right.$$

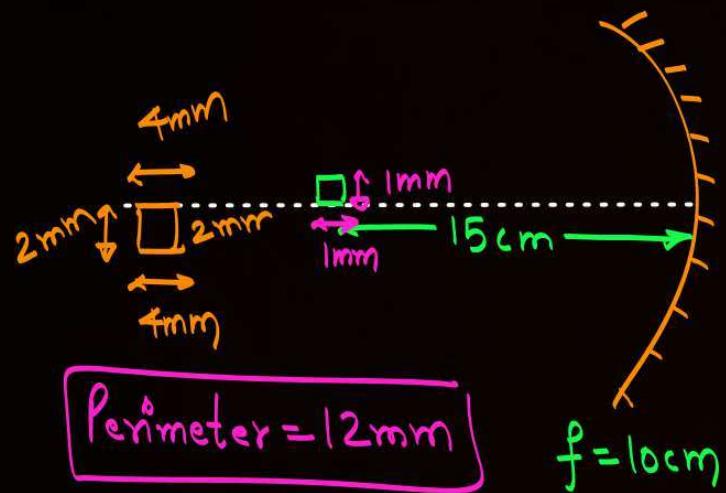
$$\left| \begin{array}{l} \frac{1}{f} = \frac{1}{V} + \frac{1}{U} \\ -\frac{1}{20} = \frac{1}{V} - \frac{1}{25} \\ -\frac{1}{20} + \frac{1}{25} = \frac{1}{V} = \dots \\ V_B = \dots \end{array} \right.$$

**Question 12**

A square ABCD of side 1 mm is kept at distance 15 cm in front of the concave mirror as shown in the figure. The focal length of the mirror is 10 cm. The length of the perimeter of its image will be approximately:

- 1** 8 mm
- 2** 2 mm
- 3** 12 mm *Ans*
- 4** 6 mm





$$\boxed{\text{Perimeter} = 12 \text{ mm}}$$

$$u = -15$$

$$f = -10$$

$$\frac{1}{f} = \frac{1}{v} + \frac{1}{u}$$

$$-\frac{1}{10} + \frac{1}{15} = \frac{1}{v} = \frac{-3+2}{30}$$

$$\boxed{v = -30}$$

$$m_{\text{Lat}} = \frac{h_I}{h_o} = -\frac{v}{u}$$

$$h_I = \frac{30}{15} \times 1 \text{ mm} = 2 \text{ mm}$$

$$m_{\text{long}} = \frac{t_I}{t_o} = -\frac{v^2}{u^2}$$

$$t_I = 4 \times 1 \text{ mm} = 4 \text{ mm}$$

### Question 13

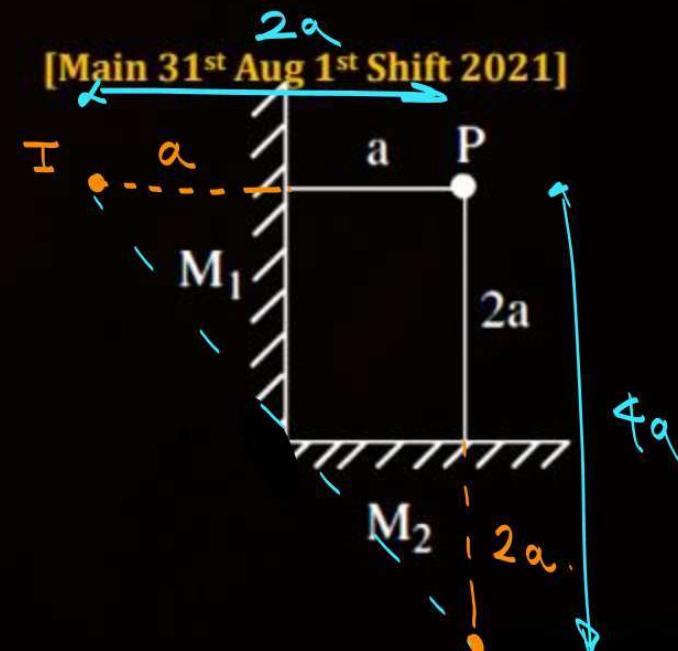


Two plane mirrors  $M_1$  and  $M_2$  are at right angle to each other as shown. A point source P is placed at  $a$  and  $2a$  meter away from  $M_1$  and  $M_2$  respectively. The shortest distance between the images thus formed individually by each mirror is (Take  $\sqrt{5} = 2.3$ )

- 1  $2.3a$
- 2  $2\sqrt{10}a$
- 3  $4.6a$
- 4  $3a$

$$\text{dist} = \sqrt{(4a)^2 + (2a)^2}$$

$$\boxed{\text{dist} = 4.3a}$$



## Question 14



Variation of  $v$  with  $u$  for a spherical mirror is as shown in figure. This curve is a hyperbola. A straight line of unit slope intersects the hyperbola at point 'A'. If the focal length of mirror is 20 cm, coordinates of point A are:

- 1 20 cm, 10 cm
- 2 40 cm, 40 cm
- 3 40 cm, 20 cm
- 4 20 cm, 20 cm

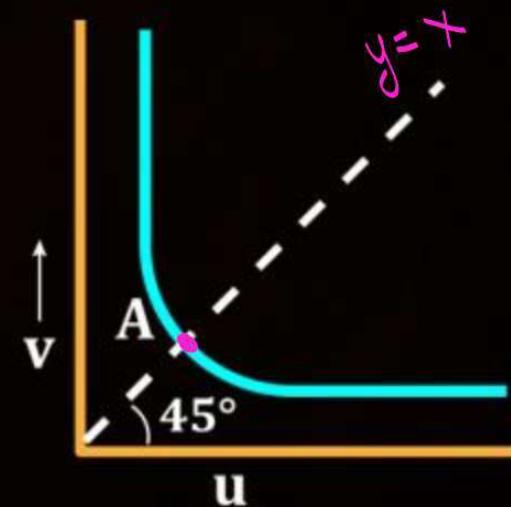
$$(f = 20 \text{ cm})$$

When  $v = u$

When object at C.

$$u = 40 \text{ cm}$$

$$v = 40 \text{ cm}$$



## Question 15



In a three dimensional coordinate system (OXYZ), a concave mirror of radius of curvature 40 cm is placed at  $x = 80$  cm. An object placed at origin is given a velocity  $\vec{v}_0 = (9\hat{i} + 6\hat{j} + 3\hat{k})$  cm/s. Find out the magnitude of velocity of its image.

1  $\sqrt{46}$  cm/s

$$u = -80$$

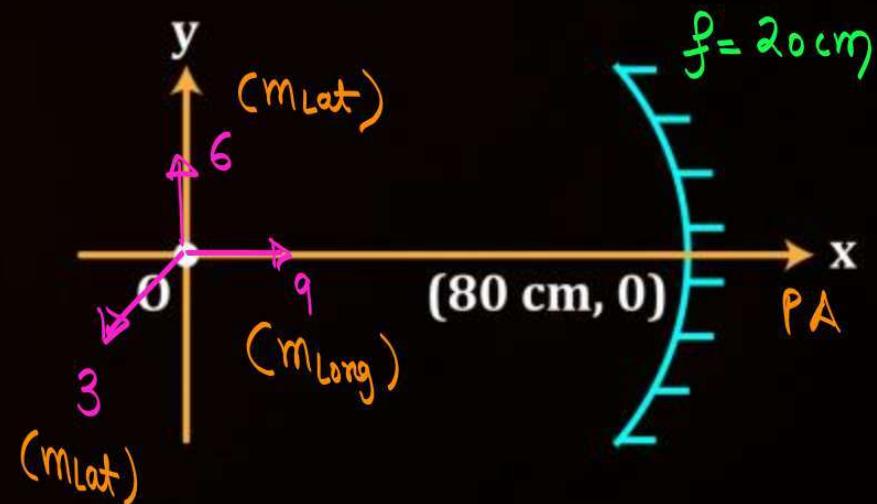
2  $\sqrt{6}$  cm/s  
Ans

$$f = -20$$

$$\frac{1}{f} = \frac{1}{v} + \frac{1}{u}$$

$$-\frac{1}{20} + \frac{1}{80} = \frac{1}{v} = \frac{-4+1}{80}$$

3  $\frac{\sqrt{14}}{3}$  cm/s



4 None of these

$$V = -\frac{80}{3}$$

$$m_{Lat} = -\frac{v}{u} = -\left(-\frac{80}{3x-80}\right) = \frac{1}{3}$$

$$m_{Long} = -m_{Lat}^2 = -\frac{1}{9}.$$

$$\vec{V_I} = -\hat{i} - 2\hat{j} - \hat{k}$$

$$|V_I| = \sqrt{1+4+1} = \sqrt{6},$$

Concept -  $V_{I||PA} = m_{Long} V_{0||PA}$

along X =  $V_I = -\frac{1}{9} \times 9\hat{i} = -\hat{i},$

$V_{I||PA} = m_{Lat} V_{0||PA}$  along Y =  $V_I = -\frac{1}{3} \times 6\hat{j} = -2\hat{j}.$

along Z =  $V_I = -\frac{1}{3} \times 3\hat{k} = -\hat{k}.$

## Question (Homework)



The light rays from an object have been reflected towards an observer from a standard flat mirror, the image observed by the observer are

- A. Real
- B. Erect
- C. Smaller in size than object
- D. Laterally inverted

[Main 25<sup>th</sup> Jan 2<sup>nd</sup> Shift 2023]

Choose the most appropriate answer from the options given below

1 B and C only

2 A, C and D only

3 B and D only

4 A and D only

[Ans: 3]

## Question (Homework)



A short straight object of height 100 cm lies before the central axis of a spherical mirror whose focal length has absolute value  $|f| = 40 \text{ cm}$ . The image of object produced by the mirror is of height 25 cm and has the same orientation of the object. One may conclude from the information

[Main 26<sup>th</sup> Feb 1<sup>st</sup> Shift 2021]

- 1** Image is virtual, opposite side of convex mirror.
- 2** Image is real, same side of concave mirror.
- 3** Image is virtual, opposite side of concave mirror.
- 4** Image is real, same side of convex mirror.

[Ans: 1]

## Question (Homework)



An object is placed between two plane mirrors inclined at an angle to each other. If the number of images formed is 7 then the angle of inclination is:

[JEE (Main) 2020]

1  $15^\circ$

2  $30^\circ$

3  $45^\circ$

4  $60^\circ$

## Question (Homework)

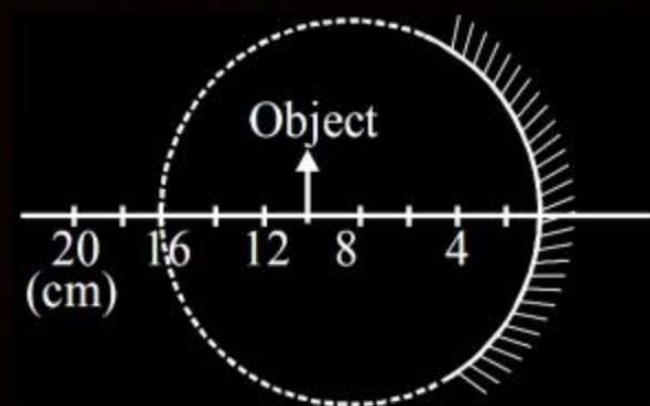


A spherical mirror is obtained as shown in the figure from a hollow glass sphere. If an object is positioned in front of the mirror, what will be the nature and magnification of the image of the object?

(Figure drawn as schematic and not to scale)

[Main 2<sup>nd</sup> Sept 1<sup>st</sup> Shift 2020]

- 1** Inverted, real and magnified
- 2** Erect, virtual and magnified
- 3** Erect, virtual and unmagnified
- 4** Inverted, real and unmagnified



[Ans: 4]

## Question (Homework)



A thin cylindrical rod of length 10 cm is placed horizontally on the principle axis of a concave mirror of focal length 20 cm. The rod is placed in a such a way that mid point of the rod is at 40 cm from the pole of mirror. The length of the image formed by the mirror will be  $x/3$  cm. The value of  $x$  is

[Main 1<sup>st</sup> Feb 1<sup>st</sup> Shift 2023]

[Ans: 32]

## Question (Homework)



An object 'O' is placed at a distance of 100 cm in front of a concave mirror of radius of curvature 200 cm as shown in the figure. The object starts moving towards the mirror at a speed 2 cm/s. The position of the image from the mirror after 10 s will be at ..... cm

[Main 28<sup>th</sup> July 22<sup>nd</sup> Shift 2022]

[Ans: 400]

## Question (Homework)



When an object is kept at a distance of 30 cm from a concave mirror, the image is formed at a distance of 10 cm from the mirror. If the object is moved with a speed of  $9 \text{ cm}^{-1}$ , parallel to axis, the speed (in  $\text{cms}^{-1}$ ) with which image moves at that instant is:

[JEE (Main) 2020 (3<sup>rd</sup> Sep Evening)]

## Refraction of Light

Phenomenon of bending of light

- ④  $\nu = \text{freq of light}$  (Source dependent)  
(Never changes)

$\Rightarrow$  Velocity & wavelength of light changes.

- ⑤ Refractive Index =  $\mu$

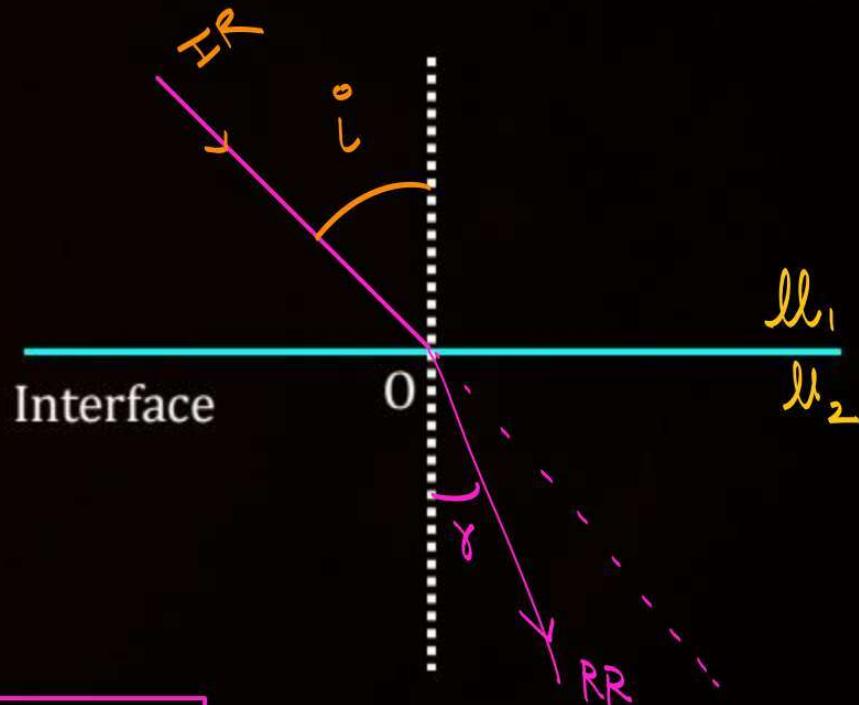
absolute      relative

$$\mu = \frac{c}{v} = \frac{\nu \times \lambda_0}{\nu \times \lambda_m} = \frac{\lambda_0}{\lambda_m}$$

$$\mu > 1$$

$$\mu = \frac{\mu_2}{\mu_1} = \frac{c}{v_2} \times \frac{v_1}{c} = \frac{v_1}{v_2}$$

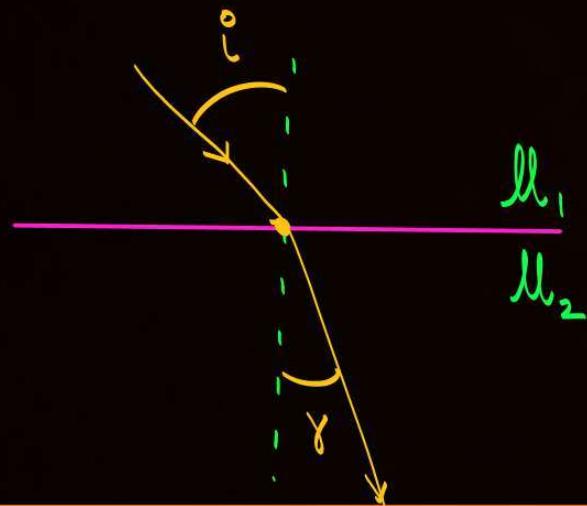
may or may not be greater than 1.



## laws of Refraction

\* IR, Normal, RR all lies in Same plane.

\*



$$\text{Snell's Law} = \mu_1 \sin i = \mu_2 \sin r$$

$$\mu \sin(\theta) = \text{const}$$

\*

$$\begin{matrix} \mu \uparrow & \theta \downarrow \\ \mu_b & \theta \uparrow \end{matrix}$$

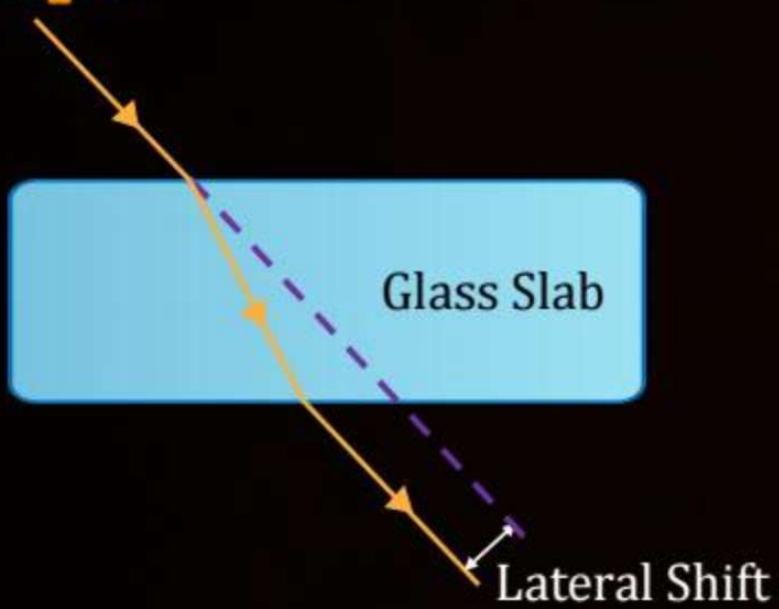
$R \rightarrow D$  Shift towards Normal  
 $D \rightarrow R$  Shift away from Normal



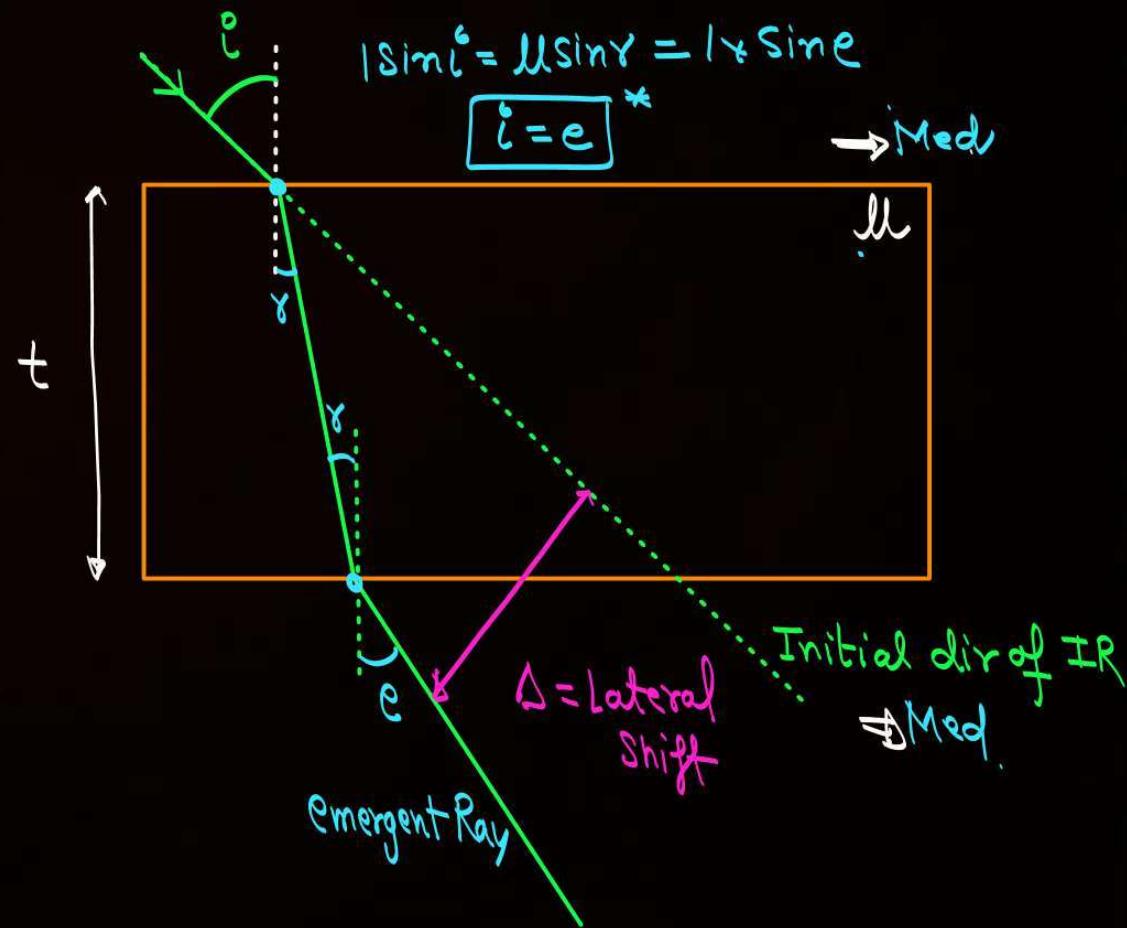


## Refraction of Light from Glass Slab

(Sirf Shift Karata hai)



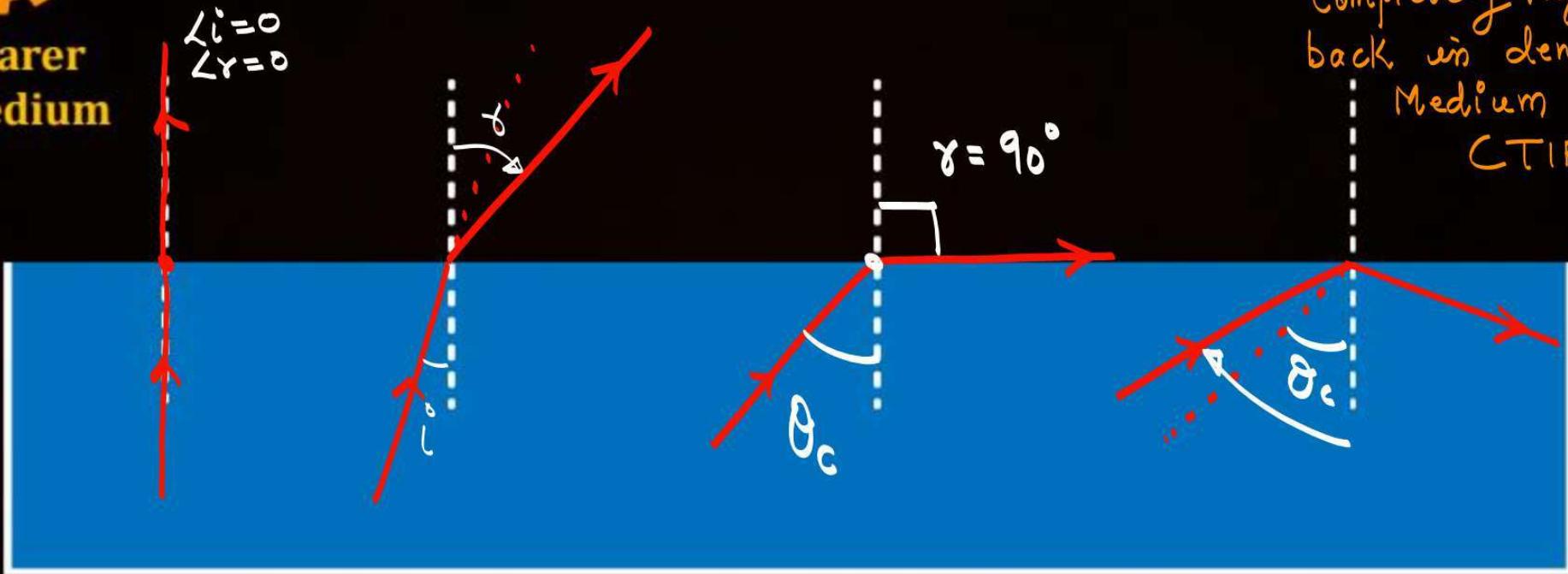
$$\Delta = \frac{t \sin(i - r)}{\cos r}$$





## Total Internal Reflection

④ Denser  $\rightarrow$  Rarer



Denser  
Medium

Normal  
Incidence

Critical Condition

$i > \theta_c$  (TIR)

Completely Reflected  
back in denser  
Medium  
(TIR).



## Total Internal Reflection (TIR)

### Calculation of critical angle in TIR

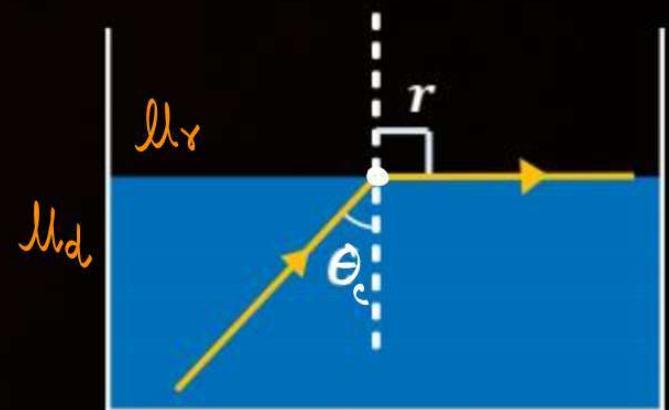
at Critical Angle. (Denser  $\rightarrow$  Rarer)

$$\mu_d \sin \theta_c = \mu_r \sin 90$$

$$\theta_c = \sin^{-1} \left( \frac{\mu_r}{\mu_d} \right)$$

Air  $\rightarrow$  Rarer

$$\theta_c = \sin^{-1} \left( \frac{1}{\mu} \right)$$



## Question 16



Light propagates 2 cm distance in glass of refractive index 1.5 in time  $t_0$ . In the same time  $t_0$ , light propagates a distance of 2.25 cm in medium. The refractive index of the medium is

1  $\frac{4}{3}$  Ans

$$\mu = \frac{c}{v_m}$$

2  $\frac{3}{2}$

3  $\frac{8}{3}$

4 None

$$\text{Speed} = \frac{\text{dist}}{\text{time}}$$

$$\frac{2C}{3} = \frac{2}{t_0}$$

Ratio

$$\frac{9/4}{2} = \frac{t_0}{\mu}$$

$$\frac{C}{\mu} = \frac{9}{4t_0}$$

$$\frac{2C}{3} \times \frac{\mu}{2} = \frac{t_0}{\mu} \times \frac{4t_0}{9/3}$$

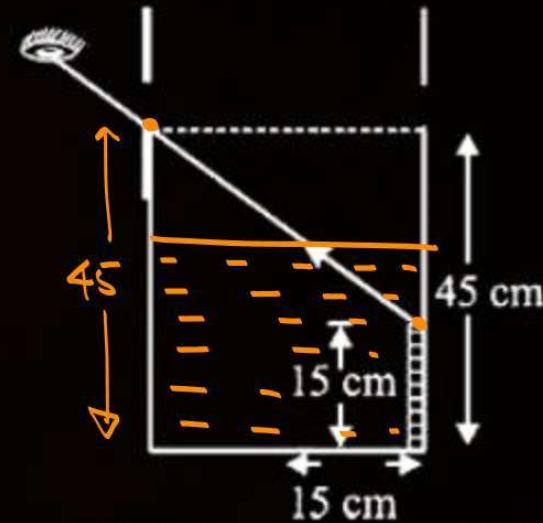
$$\mu = \frac{4}{3}$$

$$\mu = \frac{c}{v_{\text{med}}} = \frac{c}{\frac{c}{\mu}} = \mu$$

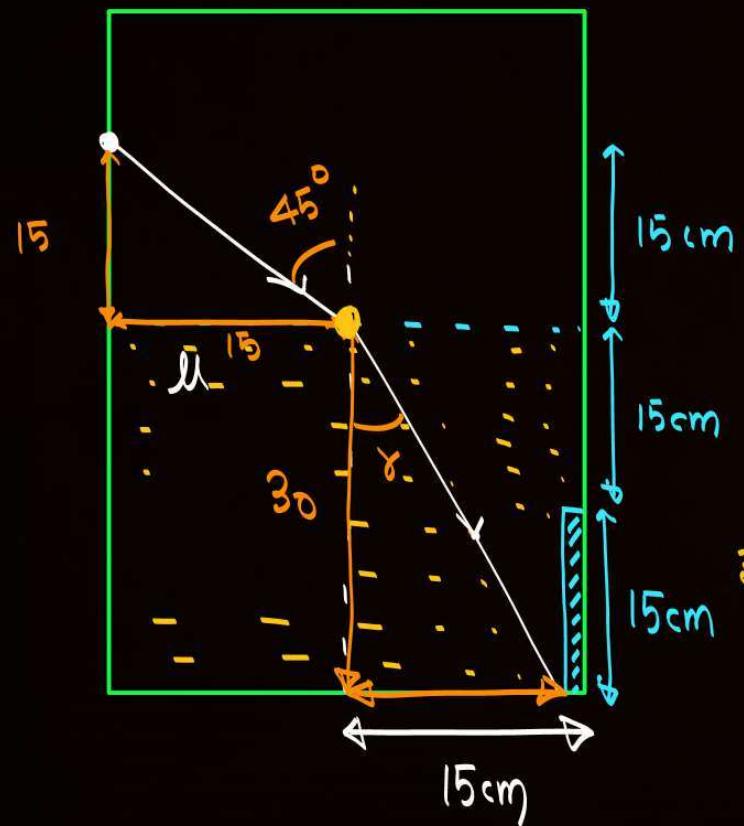
**Question 17**

An observer can see through a small hole on the side of a jar (radius 15 cm) at a point at height of 15 cm from the bottom (see figure). The hole is at a height of 45 cm. When the jar is filled with a liquid up to a height of 30 cm, the same observer can see the edge at the bottom of the jar. If the refractive index of the liquid is  $N/100$ , where N is an integer, the value of N is \_\_\_\_\_.

[Main 3<sup>rd</sup> Sept 1<sup>st</sup> Shift 2020]



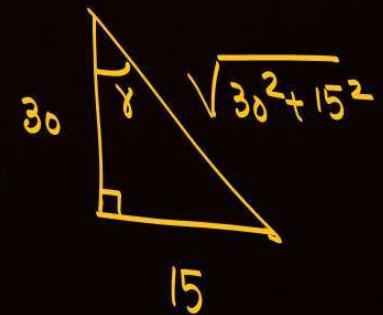
[Ans: 158]



$$fx \sin 45^\circ = mx \sin \gamma$$

$$\sin 45^\circ = M \times \frac{15}{\sqrt{30^2 + 15^2}}$$

$$M = \underline{1.058}$$



$$Ans = \frac{N}{100} = 1.058$$

$$N = 158$$

## Question 18



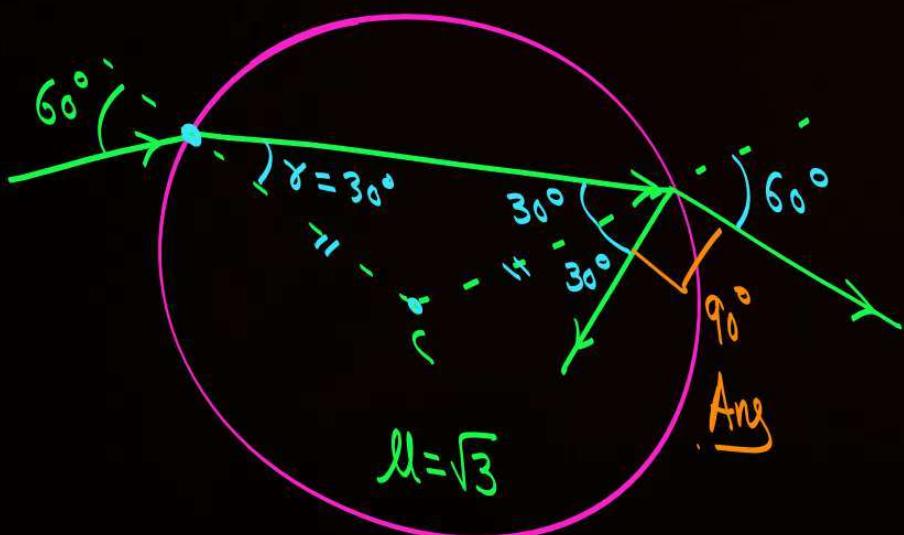
A light ray enters a solid glass sphere of refractive index  $\mu = \sqrt{3}$  at an angle of incidence  $60^\circ$ . The ray is both reflected and refracted at the further surface of the sphere. The angle (in degrees) between the refracted and reflected rays at this surface is \_\_\_\_\_

[Main 2<sup>nd</sup> Sept 2<sup>nd</sup> Shift 2020]

$$1 \times \sin 60^\circ = \sqrt{3} \sin r$$

$$\frac{\sqrt{3}}{2} = \sqrt{3} \sin r$$

$$r = 30^\circ$$



[Ans: 90]

## Question 19



A light beam travels at a speed of  $1.94 \times 10^8$  m/s in quartz. The wavelength found in quartz is 355 nm. The wavelength of light in air will be?

1 590 nm

$$V_m = 1.94 \times 10^8$$

2 549 nm Ans

$$\lambda_m = 355 \times 10^{-9} \text{ m}$$

3 460 nm

$$\lambda_0 = \frac{c}{V} = \frac{\lambda_0}{\lambda_m}$$

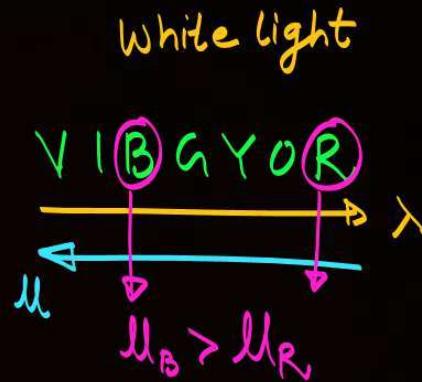
4 707 nm

$$\lambda_0 = \frac{c}{V} \lambda_m = \frac{3 \times 10^8 \times 355 \times 10^{-9}}{1.94 \times 10^8} = 548.9 \times 10^{-9}$$

**Question 20**

A ratio of the RI of red light to blue light in air is

- 1** Less than one Ans
- 2** Greater to one
- 3** Greater than one
- 4** Depends on surrounding condition



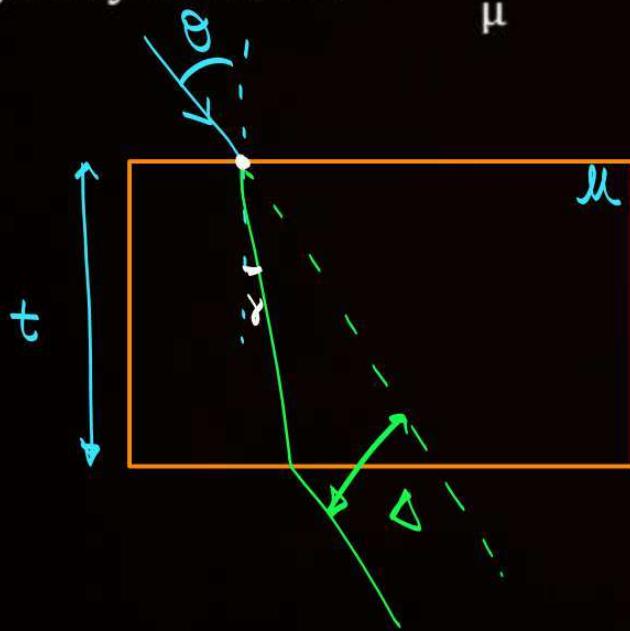
$$\frac{\mu_{\text{Red}}}{\mu_{\text{Blue}}} = < 1,$$

$$\mu \propto \frac{1}{\lambda}$$

## Question 21



A ray of light is incident on a parallel slab of thickness  $t$  and refractive index  $\mu$ . If the angle of incidence is  $\theta$  then for small  $\theta$  show that the lateral displacement of light ray will be  $\Delta = \frac{t\theta(\mu-1)}{\mu}$



$$\Delta = \frac{t \sin(i - r)}{\cos r}$$

$$\Delta = t(i - r)$$

$$= t\left(\theta - \frac{\theta}{\mu}\right)$$

for small angle.

$$\sin \theta \approx \tan \theta \approx \theta$$

$$\cos \theta \approx 1$$

$$i \approx \theta$$

$$i \approx \mu r$$

$$r \approx \theta/\mu$$

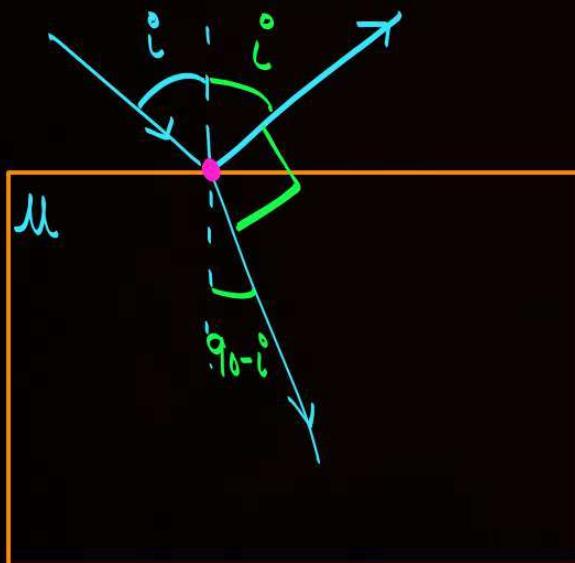
$$\boxed{\Delta = t\theta\left(\frac{\mu-1}{\mu}\right)}$$

## Question 22

### Brewster's Law.



Monochromatic light falls at an angle of incidence ' $i$ ' on a slab of a transparent material, refractive index of this material being ' $\mu$ ' for the given light. What should the relation between  $i$  and  $\mu$  be so that the reflected and the refracted rays are mutually perpendicular?



$$i \times \sin i = \mu \sin (90^\circ - i)$$

$$\sin i = \mu \cos i$$

$$\boxed{\tan i = \mu}$$

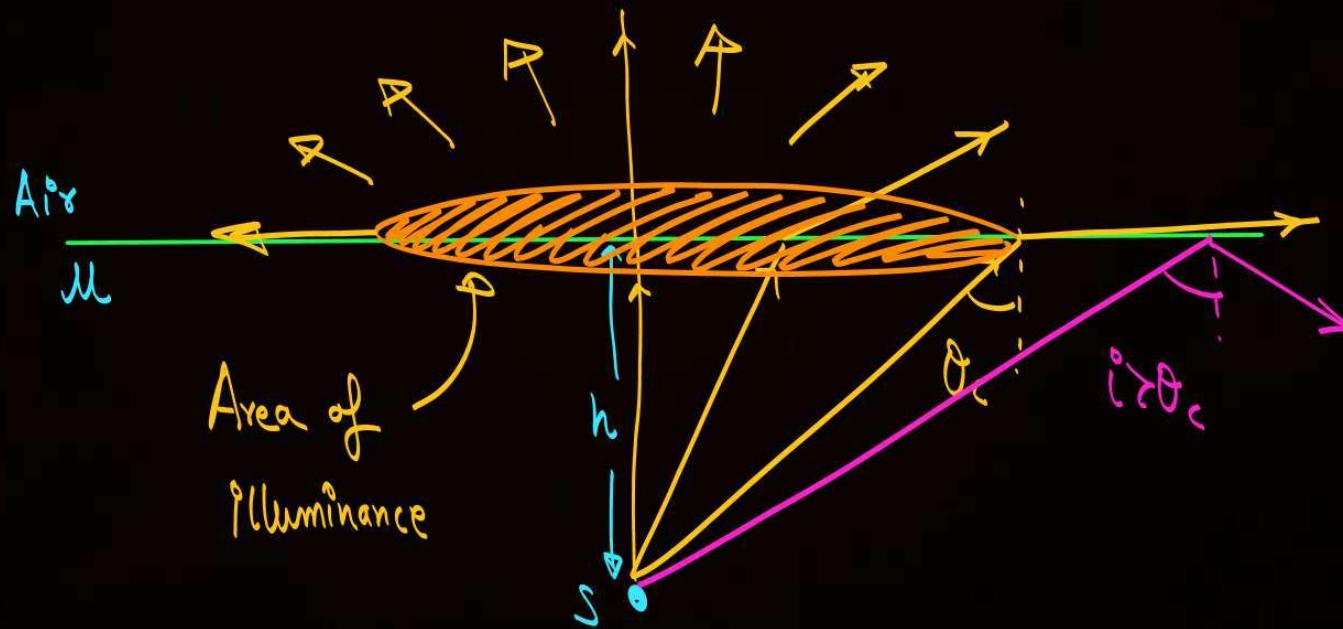
$i$  = Brewster's Angle.

**Question 23**

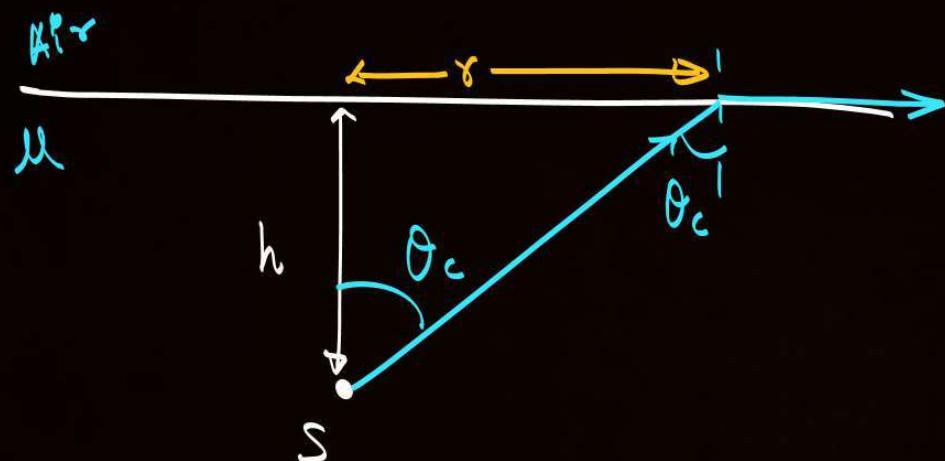
(NCERT) + (PYQ)

Area of Illuminance.

A point source of light is placed directly below the surface of a lake at a distance  $h$  from the surface. Find the area on water from which the light will come out from water.



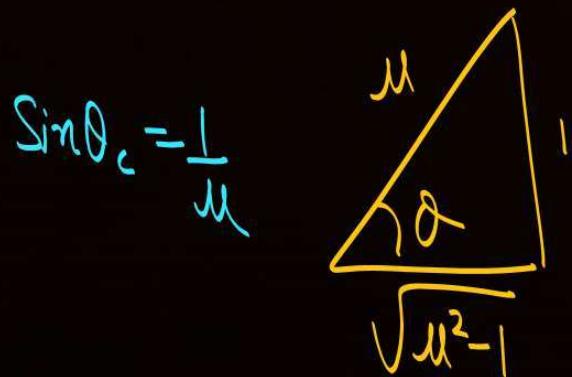
\*



$$\tan \theta_c = \frac{r}{h}$$

$$h \tan \theta_c = r$$

$\sqrt{\frac{h}{\mu^2 - 1}} = r = \text{radius of area of Illuminance}$



$$\sin \theta_c = \frac{1}{\mu}$$

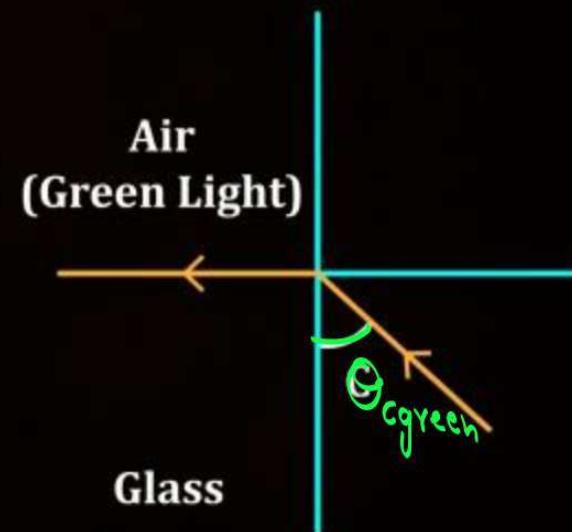
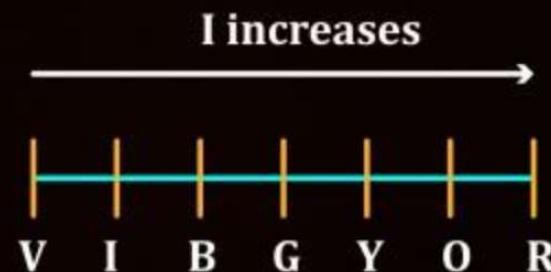
$$\text{Area} = \pi r^2 = \frac{\pi h^2}{\mu^2 - 1}$$

## Question 24

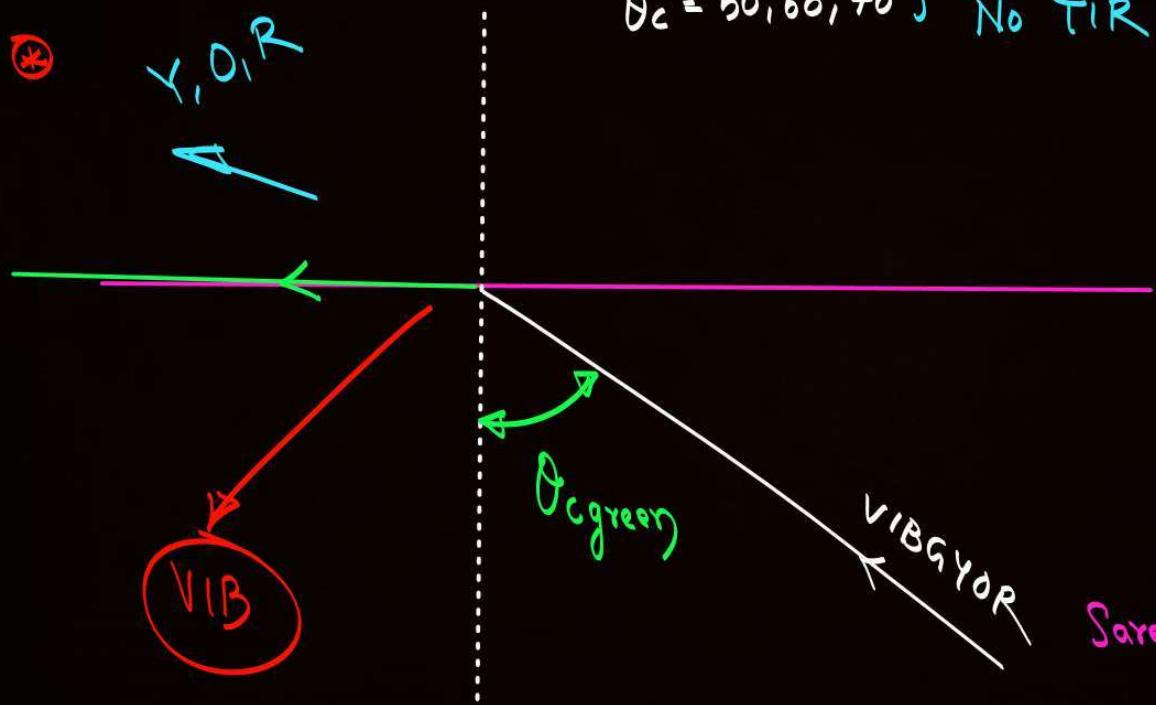
VIBGYOR

A beam of white light is incident on glass -air interface from glass to air such that green light just suffers total internal reflection. The colors of the light which will come out to air are

- 1 Violet, Indigo, Blue
- 2 All colors except green
- 3 Yellow, Orange, Red *Ans*
- 4 White light



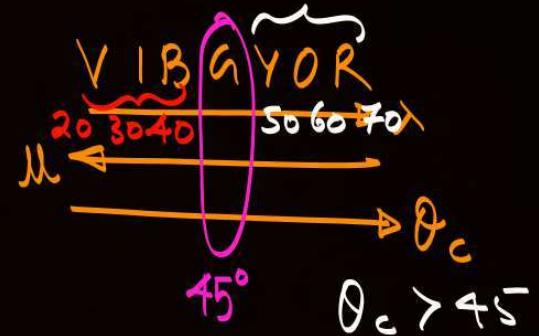
④



$$\left. \begin{array}{l} YOR \\ \angle i = 45^\circ \\ \theta_c = 50, 60, 70 \end{array} \right\} \begin{array}{l} \angle i < \theta_c \\ \text{No TIR} \end{array}$$

$$\sin \theta_c = \frac{1}{\mu}$$

$$\theta_c > \theta_{c\text{green}}$$



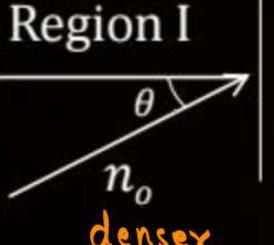
$$\begin{array}{ll} VIB & \angle i > \theta_c \\ \angle i = 45^\circ & \theta_c = 20, 30, 40 \\ \text{TIR} & \end{array}$$

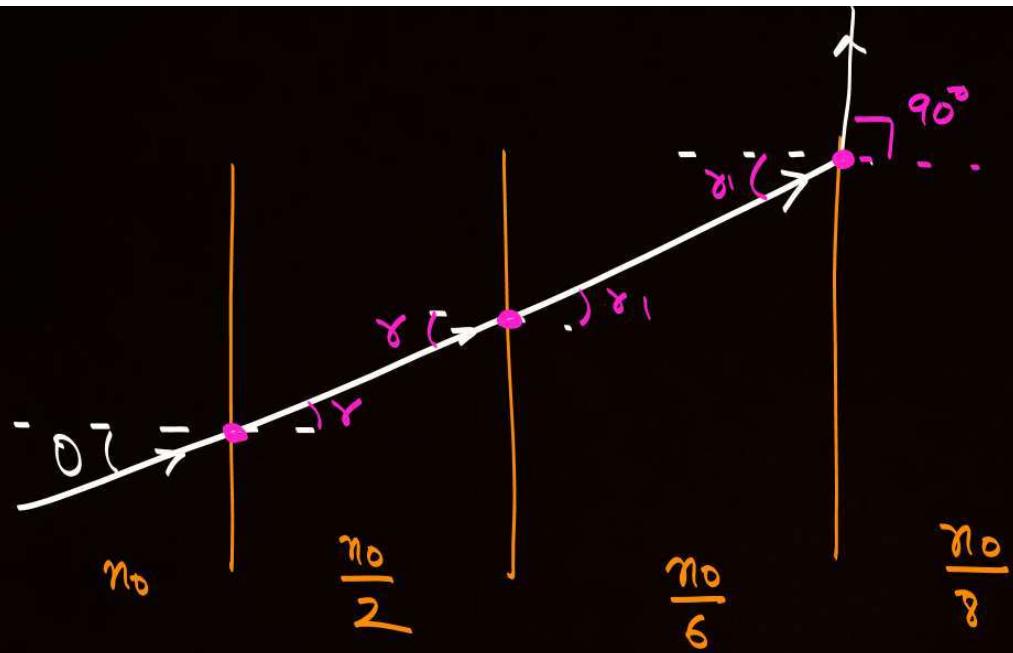
$$\text{Same colors } \angle i = \theta_{c\text{green}}$$

## Question 25



A light beam is travelling from region I to region IV. The refractive index in regions I, II, III and IV are  $n_0$ ,  $\frac{n_0}{2}$ ,  $\frac{n_0}{6}$ ,  $\frac{n_0}{8}$  respectively. The angle of incidence  $\theta$  for which the beam just misses entering region IV is:

- |  |                 |                 |                 |
|--|-----------------|-----------------|-----------------|
| Region I   | Region II       | Region III      | Region IV       |
|  | $\frac{n_0}{2}$ | $\frac{n_0}{6}$ | $\frac{n_0}{8}$ |
| <i>denser</i>  |                 |                 | <i>Rarer</i>    |
- 1**  $\sin^{-1} \left( \frac{3}{4} \right)$
- 2**  $\sin^{-1} \left( \frac{1}{8} \right)$
- 3**  $\sin^{-1} \left( \frac{1}{4} \right)$
- 4**  $\sin^{-1} \left( \frac{1}{3} \right)$



$$n_0 \sin \theta_0 = \frac{n_0}{2} \sin \gamma = \frac{n_0}{6} \sin \gamma_1 = \frac{n_0}{8} \sin 90$$

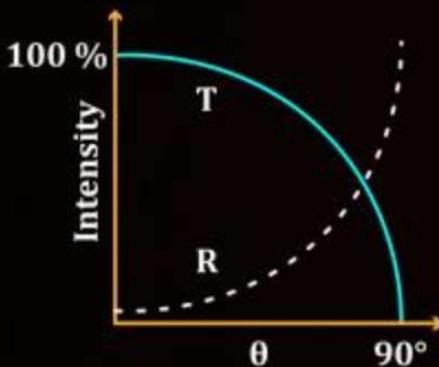
$$\theta_0 = \sin^{-1}\left(\frac{1}{8}\right)$$

## Question 26

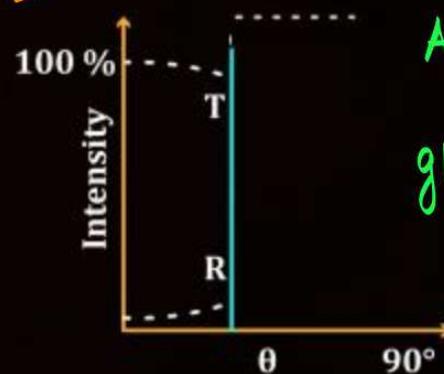


A light ray travelling in glass medium is incident on glass-air interface at an angle of incidence  $\theta$ . The reflected (R) and transmitted (T) intensities, both as function of  $\theta$ , are plotted. The correct sketch is: (Refracted)

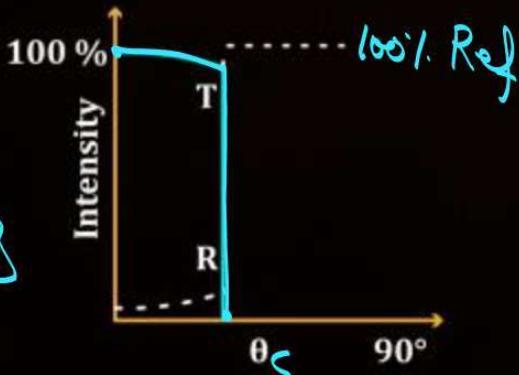
~~1~~



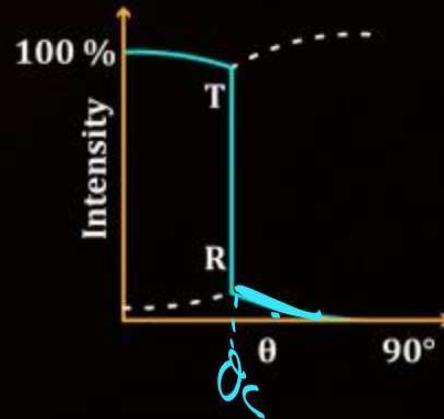
~~2~~



~~3~~



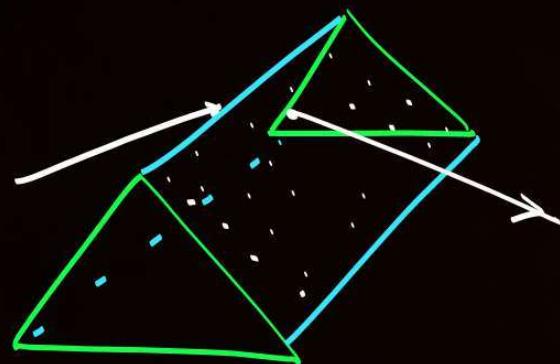
~~4~~



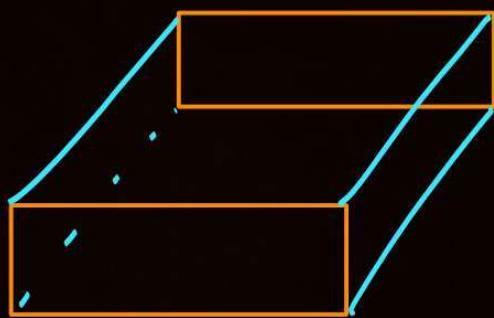
$\theta = 0^\circ$  Reflect ✓  
 Refract ✓  
 (More)  
 $\theta > \theta_c$  (TIR)  
 Refraction = 0  
 100% Reflection

Prism → Refracting Med bounded by 2 polygons of

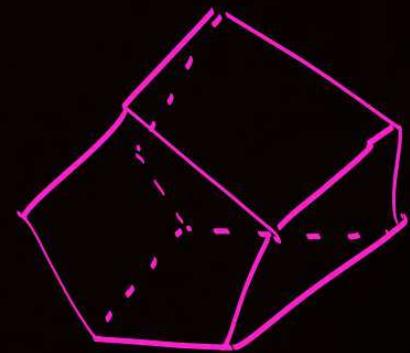
Rectangular Matt  
Surfaces.



Trihedral  
prism.



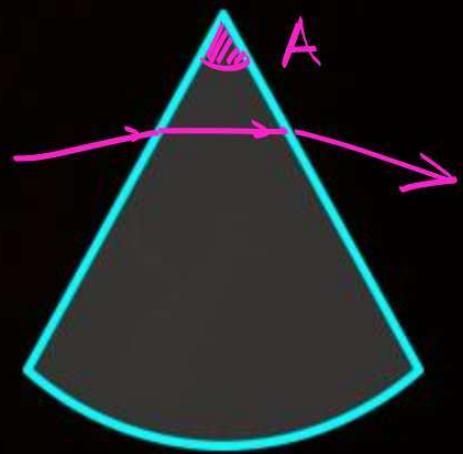
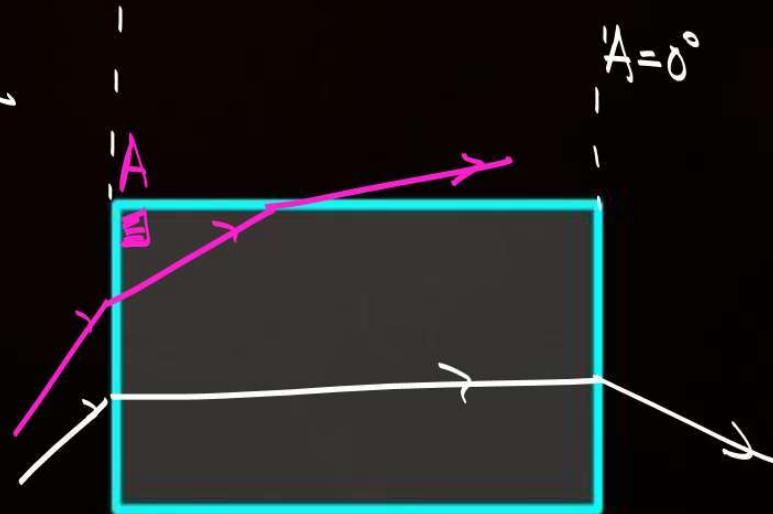
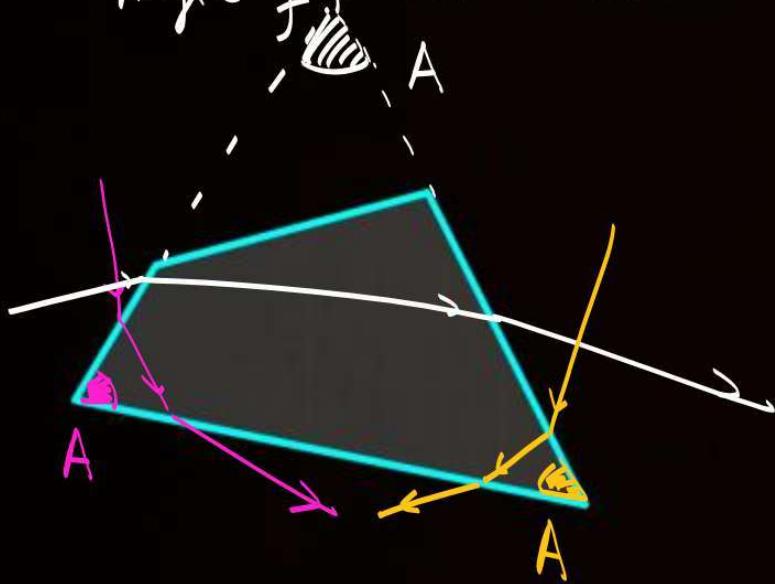
Rectangular Prism  
Slab.



Pentahedral Prism

## Prism and its Types

Angle of prism  $\rightarrow$   $\angle$  between two Matt Surfaces about which Refraction is Occuring.



## Deviation of Prism

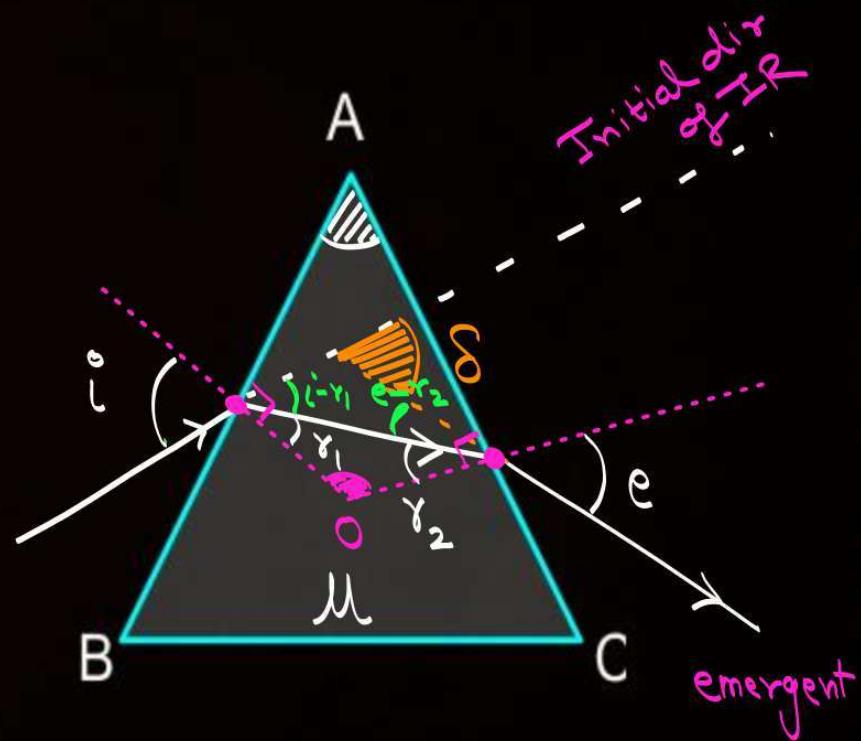
$$1. \sin i = \mu \sin r_1$$

$$2. \mu \sin r_2 = \sin e$$

$$3. \begin{cases} \angle A + \angle O = 180^\circ \\ r_1 + r_2 + \angle O = 180^\circ \end{cases} \quad A = r_1 + r_2$$

$$4. \text{deviation} = \delta = i - r_1 + e - r_2$$

$$\delta = i + e - A$$





## Minimum & Maximum Deviation



$\delta$  = Representation of  $\delta$ .

Condition for  $\delta_{\min}$ .

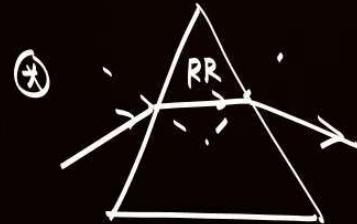
$$(*) \quad i = e \text{ then } \delta_{\min}$$

$$(*) \quad \delta_{\min} = 2i - A$$

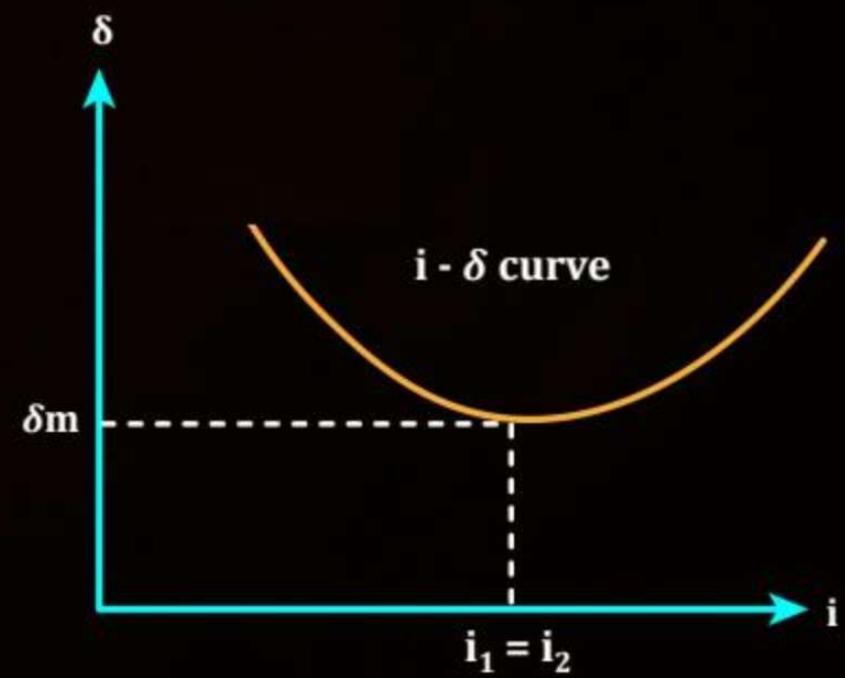
$$(*) \quad \gamma_1 = \gamma_2 = \frac{A}{2}$$

$$(*) \quad i \sin i = \mu \sin \frac{A}{2}$$

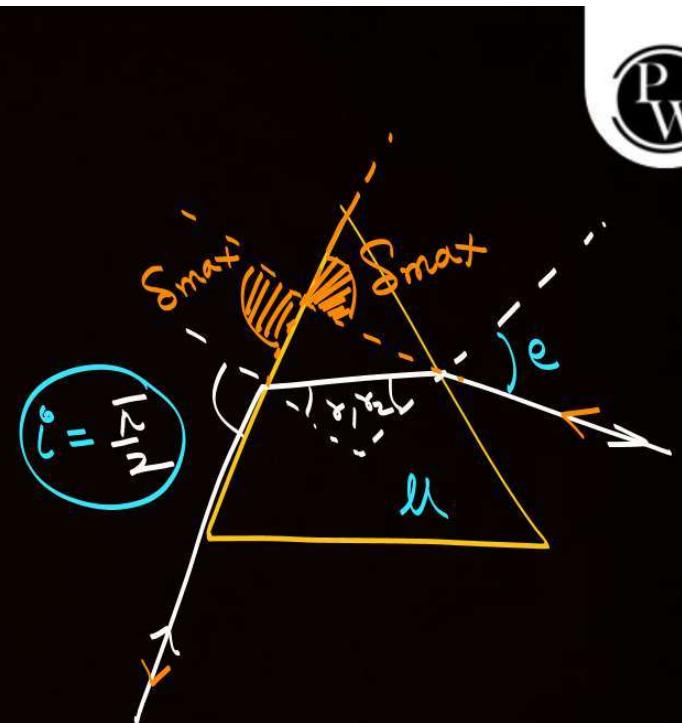
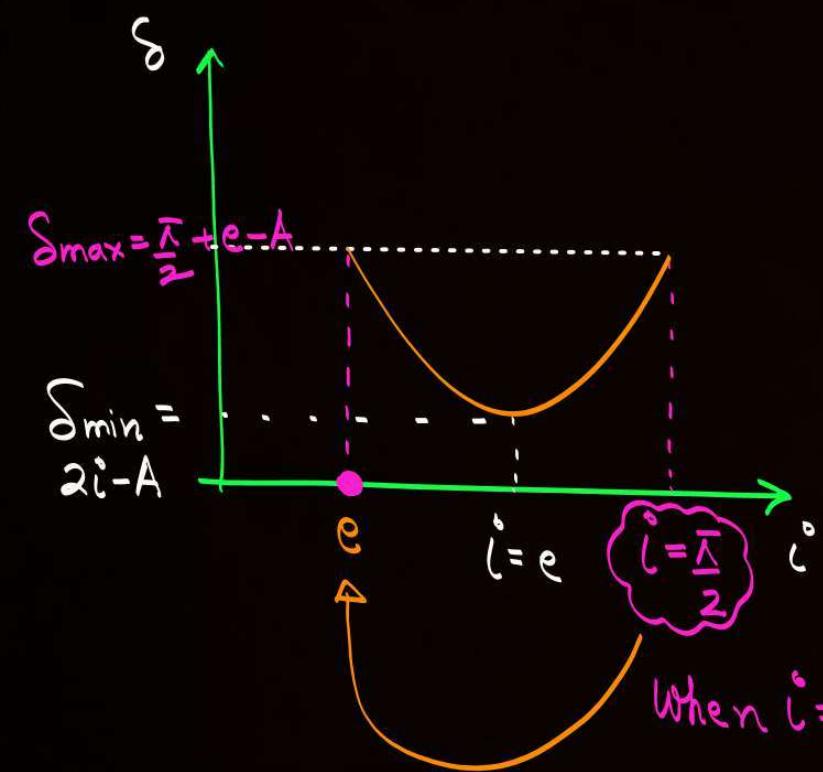
$$\frac{\sin(\delta_{\min} + A)}{\sin(A/2)} = \mu$$



Parallel to base.



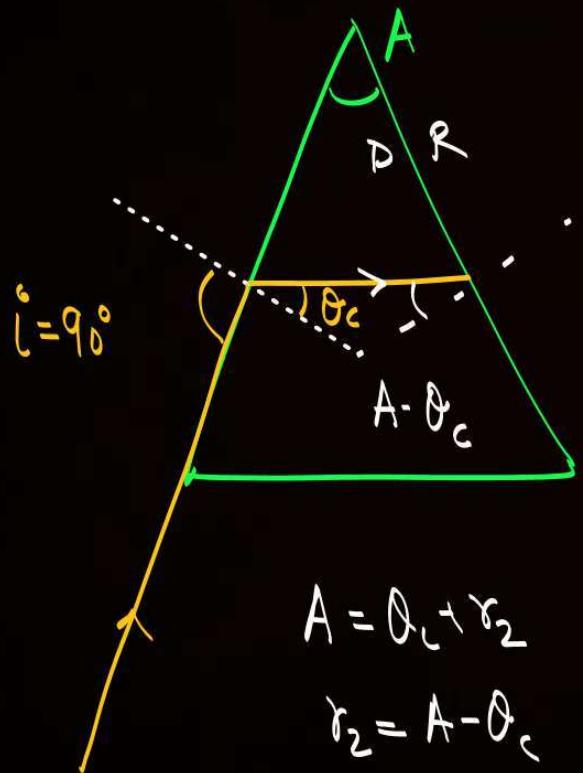
## "Assymetrical Graph"



Whatever will be  
le in this case

is the second angle at which  $\delta_{\max}$ .

## TIR In prism



What is the condition for which

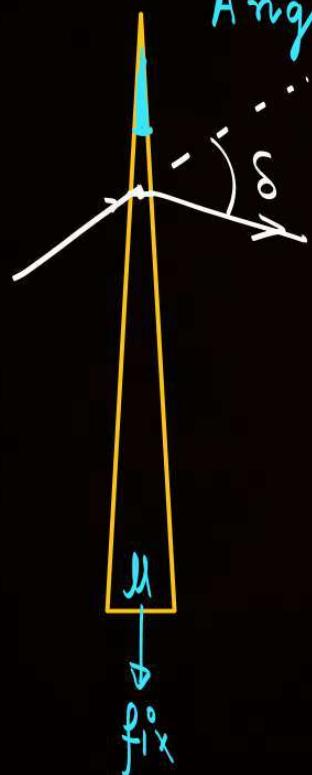
- ⊗  $\gamma_2 \geq \theta_c$  (TIR) light is always reflected from Second Matt Surface

$$A - \theta_c \geq \theta_c$$

$$A \geq 2\theta_c$$

$$A \geq 2 \sin^{-1}\left(\frac{1}{\mu}\right) \quad (\text{TIR})$$

## Thin prism and Dispersion



Angle of prism less than  $10^\circ$  = Thin Prism

$$A \rightarrow \text{Small} = r_1 + r_2$$

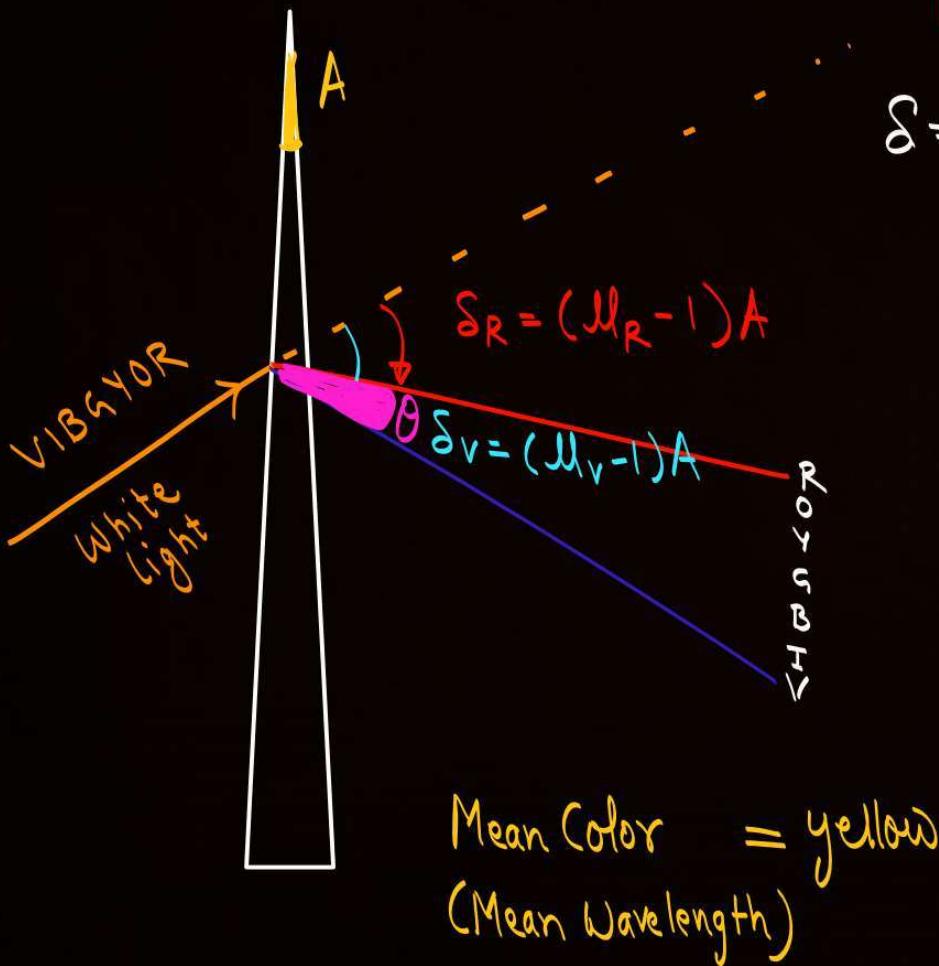
$r_1$  &  $r_2 \rightarrow \text{Small}$  (i.e.)  $\Rightarrow$  Small.  
(Small angle Appr)

$\downarrow \text{fix}$        $\downarrow \text{fix}$

$$\delta = (\mu - 1)A$$

$\delta$  by thin prism  $\Rightarrow$  fix. (for Monochromatic)

Thin Prism



## Dispersion

$$\delta = (\mu - 1)A$$

$$\frac{VIBGYOR}{\mu} \xrightarrow{\delta}$$

$$\theta = \text{Angle of dispersion} = \delta_V - \delta_R$$

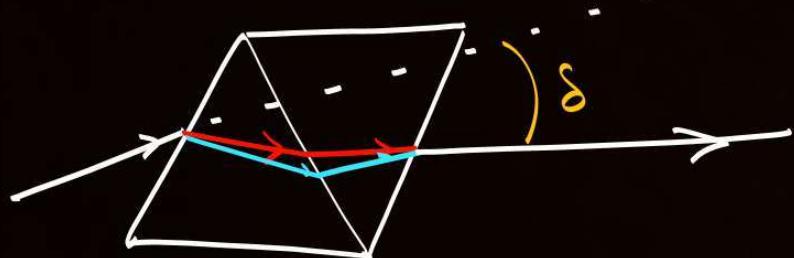
$$\theta = (\mu_v - \mu_r)A$$

$$\text{dispersive Power} = \omega = \frac{\theta}{\delta_{\text{mean}}} = \frac{\mu_v - \mu_r}{\mu_y - 1}$$

## Combination of prism.

#

deviation without dispersion



⊗

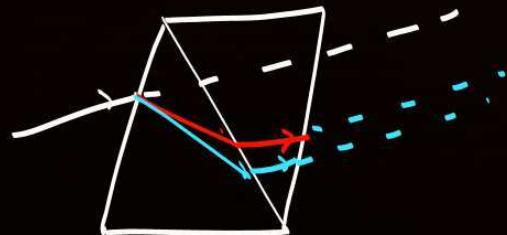
No dispersion

$$\theta_{\text{Prism}_1} + \theta_{\text{Prism}_2} = 0$$

$$(\mu_{v_1} - \mu_{R_1})A_1 + (\mu_{v_2} - \mu_{R_2})A_2 = 0$$

$$A_2 = -\frac{(\mu_{v_1} - \mu_{R_1})A_1}{(\mu_{v_2} - \mu_{R_2})}$$

# dispersion without deviation



$$\delta_{\text{Total}} = 0 = (\mu_1 - 1)A_1 + (\mu_2 - 1)A_2 = 0$$

$$A_2 = -\frac{(\mu_1 - 1)A_1}{(\mu_2 - 1)}$$

## Question 28



The refracting angle of a prism is  $A$  and refractive index of the material of the prism is  $\cot(A/2)$ . Then the angle of minimum deviation will be (Main 28<sup>th</sup> June 1<sup>st</sup> Shift 2022)

1  $180 - 2A$

$$\mu = \frac{\sin\left(\frac{A + \delta_{\min}}{2}\right)}{\sin\left(\frac{A}{2}\right)}$$

2  $90 - A$

$$\frac{\cos\left(\frac{A}{2}\right)}{\sin\left(\frac{A}{2}\right)} = \frac{\sin\left(\frac{A + \delta_{\min}}{2}\right)}{\sin\left(\frac{A}{2}\right)}$$

3  $180 + 2A$

4  $180 - 3A$

$$\frac{\pi}{2} - \frac{A}{2} = \frac{A}{2} + \frac{\delta_{\min}}{2}$$

$$\delta_{\min} = 180 - 2A$$

[Ans: 1]

## Question 29

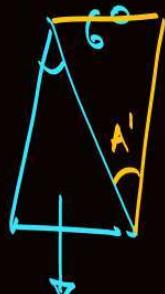


A thin prism  $P_1$  with an angle  $6^\circ$  and made of glass of refractive index 1.54 is combined with another prism  $P_2$  made from glass of refractive index 1.72 to produce dispersion without average deviation. The angle of prism  $P_2$  is

(Main 30<sup>th</sup> Jan 2<sup>nd</sup> Shift 2023)

$$\delta_{\text{net}} = 0$$

1  $7.8^\circ$



$$(\mu_1 - 1)A_1 + (\mu_2 - 1)A_2 = 0$$

2  $4.5^\circ$  Ans

$$A_2 = - \frac{(\mu_1 - 1)A_1}{\mu_2 - 1} = - \frac{0.54 \times 6^\circ}{0.72} = 4.5^\circ$$

3  $6^\circ$

$$\mu = 1.54$$

4  $1.3^\circ$

Second Prism  $\rightarrow$  Inverted.

[Ans: 2]

### Question 30



A prism of refractive index  $\mu$  and angle of prism  $A$  is placed in the position of minimum angle of deviation. If minimum angle of deviation is also  $A$ , then in terms of refractive index, value of  $A$  is

(Main 25<sup>th</sup> July 2<sup>nd</sup> Shift 2021)

- 1  $2\cos^{-1}\left(\frac{\mu}{2}\right)$ . Ans
- 2  $\sin^{-1}\left(\frac{\mu}{2}\right)$
- 3  $\cos^{-1}\left(\frac{\mu}{2}\right)$
- 4  $\sin^{-1}\left(\sqrt{\frac{\mu-1}{2}}\right)$

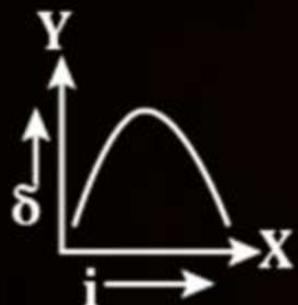
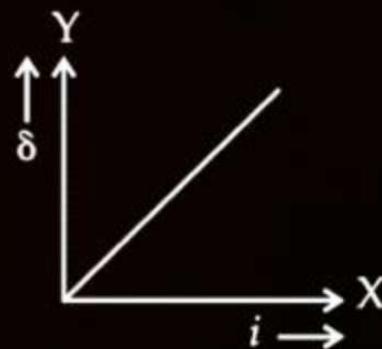
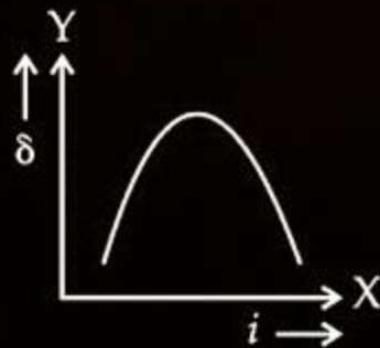


$$\mu = \frac{\sin\left(\frac{\delta_{\min} + A}{2}\right)}{\sin\left(\frac{A}{2}\right)} = \frac{\sin(A)}{\sin(A/2)} = 2 \sin\left(\frac{A}{2}\right) \cos\left(\frac{A}{2}\right)$$
$$\frac{\mu}{2} = \log\left(\frac{A}{2}\right)$$
$$A = 2 \log^{-1}\left(\frac{\mu}{2}\right)$$

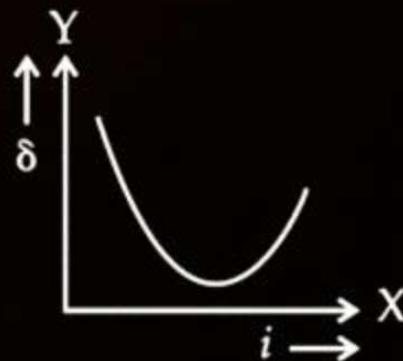
[Ans: 1]

**Question 31**

The expected graphical representation of the variation of angle of deviation  $\delta$  with angle of incidence  $i$  in a prism is  
**(Main 27<sup>th</sup> July 2<sup>nd</sup> Shift 2021)**

**1****2****3**

Ans  
**4**



[Ans: 4]

## Question 32



The angle of deviation through a prism is minimum when

(Main 16<sup>th</sup> March 1<sup>st</sup> Shift 2021)

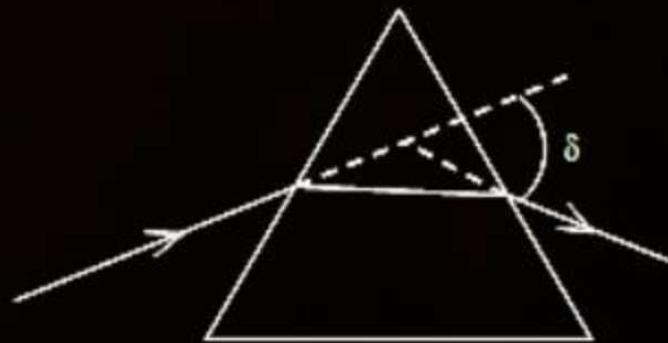
- (A) incident ray and emergent ray are symmetric to the prism
- (B) the refracted ray inside the prism becomes parallel to its base
- (C) angle of incidence is equal to that of the angle of emergence
- (D) when angle of emergence is double the angle of incidence.

1 Only statements (A) and (B) are true.

2 Statements (B) and (C) are true.

3 *Ans* Statements (A), (B) and (C) are true.

4 Only statement (D) is true.



[Ans: 3]

### Question 33



A monochromatic light is incident at a certain angle on an equilateral triangular prism and suffers minimum deviation. If the refractive index of the material of the prism is  $\sqrt{3}$ , then the angle of incidence is

(Main 11<sup>th</sup> Jan 2<sup>nd</sup> Shift 2019)

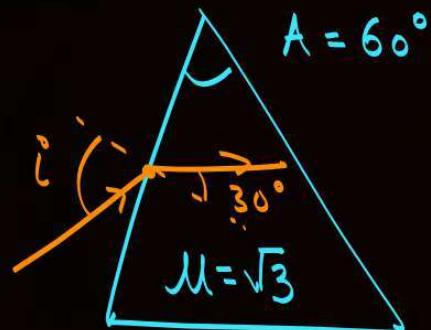
1

~~60°~~

Ans

2

45°



3

90°

4

30°

$$l \times \sin i = \sqrt{3} \sin 30^\circ$$

$$i = 60^\circ$$

$$r_1 + r_2 = A$$

$$\delta_{\min}$$

$$r = \frac{A}{2}$$

[Ans: 1]

## Question 34



A ray of light is incident at an angle of  $60^\circ$  on one face of a prism of angle  $30^\circ$ . The emergent ray of light makes an angle of  $30^\circ$  with incident ray. The angle made by the emergent ray with second face of prism will be

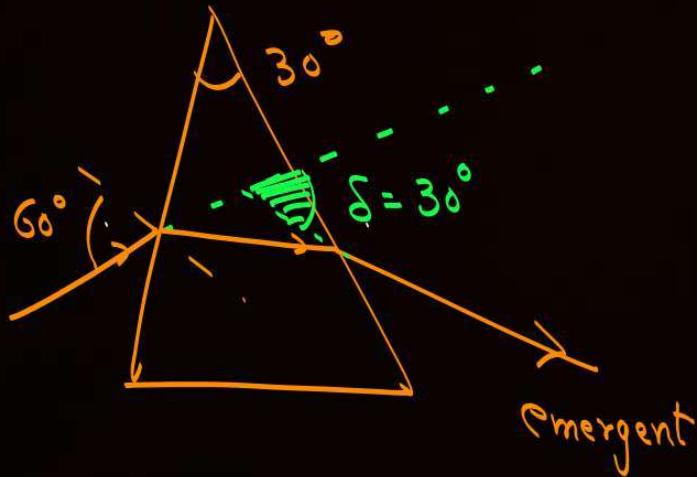
(Main Online 2018)

1  $0^\circ$

2  $45^\circ$

3  $90^\circ$   
Ans

4  $30^\circ$

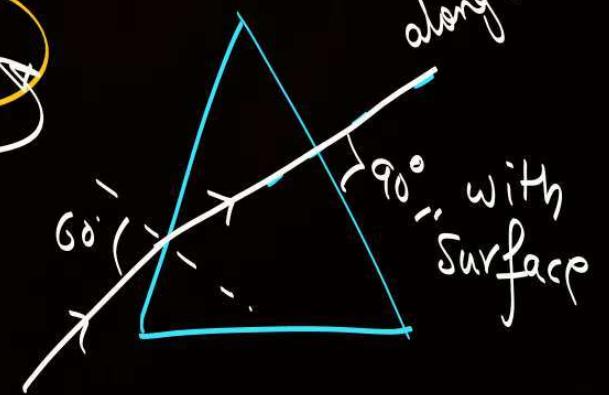


$$\delta = i + e - A$$

$$30 = 60 + e - 30$$

$$e = 0$$

with Normal

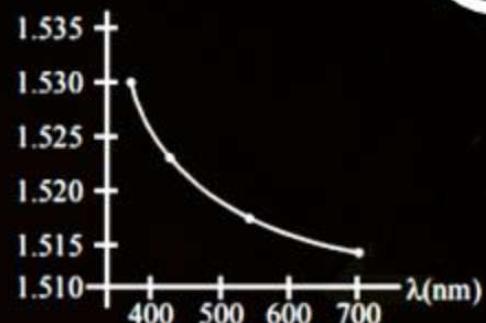


[Ans: 3]

## Question 35

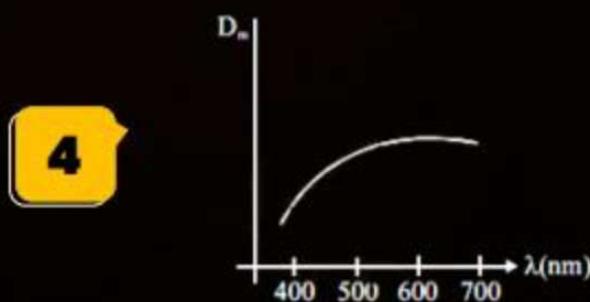
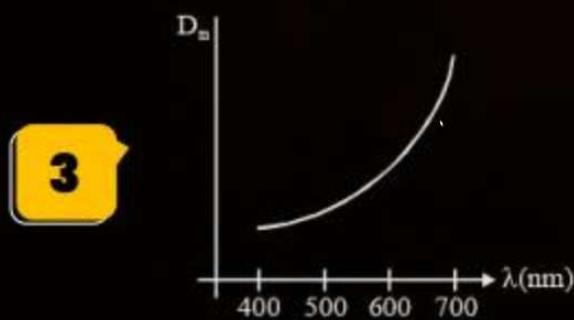
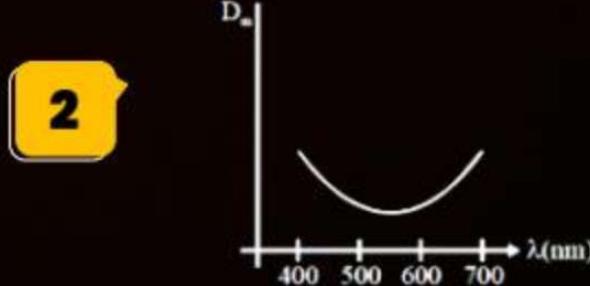
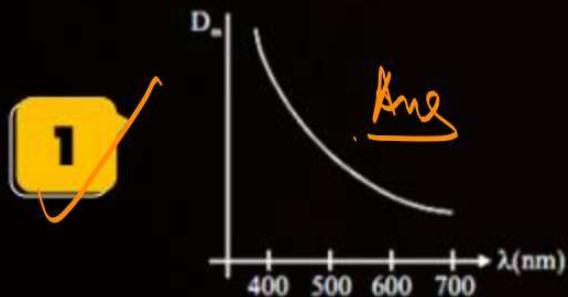
The variation of refractive index of a crown glass thin prism with wavelength of the incident light is shown. Which of the following graphs is the correct one, if  $D_m$  is the angle of minimum deviation?

(Main 11<sup>th</sup> Jan 1<sup>st</sup> Shift 2019)



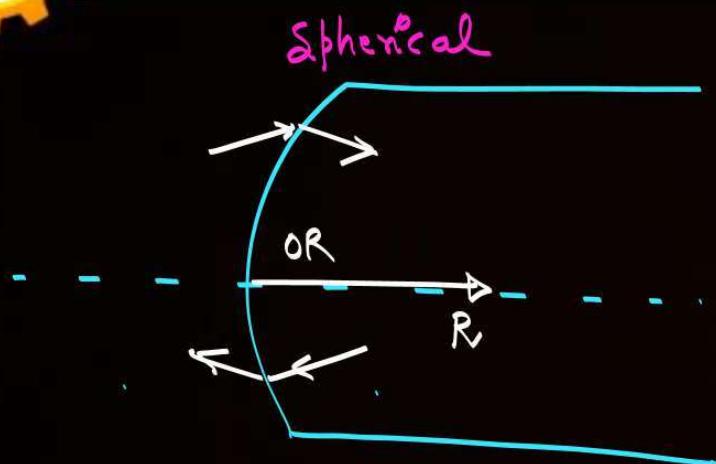
$$\delta = (\mu - 1) A$$

$\Delta \delta \uparrow \mu \uparrow \delta \downarrow$



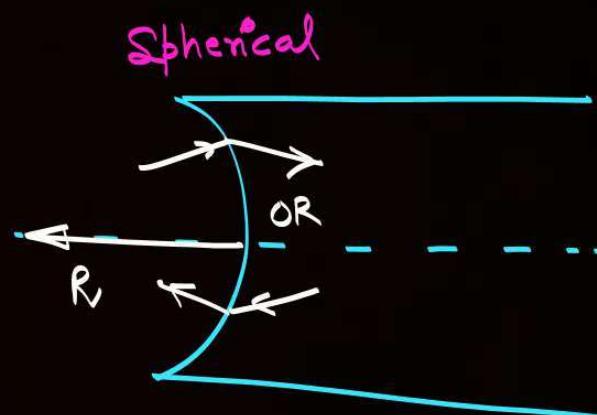
[Ans: 1]

# Refraction from Spherical Surfaces



Convex Surface.

1. Object  $\rightarrow$  Intersection of IR  
Image  $\rightarrow$  " " " RR's.



Concave

2. Refraction formula:

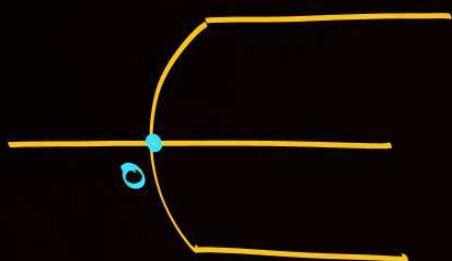
$$M_f = \text{Ja Rahi hai}$$

$$M_i = \text{Aa Rahi hai}$$

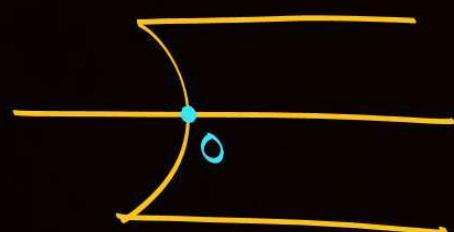
$$\frac{M_f}{v} - \frac{M_i}{u} = \frac{M_f - M_i}{R}$$

$v =$  Int of IR       $R =$  Radius of Curvature  
 $u =$  Int of RR

\* Same Sign Convention.



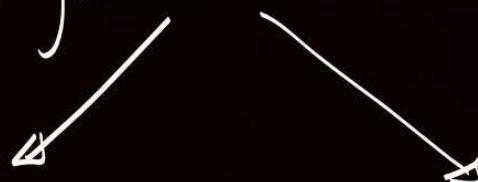
OR



all distances measured from O.

\*

magnification



$$m_{\text{lat}} = \frac{h_I}{h_O} = \frac{M_i}{M_f} \frac{v}{u}$$

$$m_{\text{long}} = \frac{t_I}{t_O} = \frac{M_i}{M_f} \frac{v^2}{u^2}$$

\* Velocity of I || PA = ( $m_{\text{long}}$ )  $V_{O \parallel PA}$

Velocity of I ⊥ PA = ( $m_{\text{lat}}$ )  $V_{O \perp PA}$ .

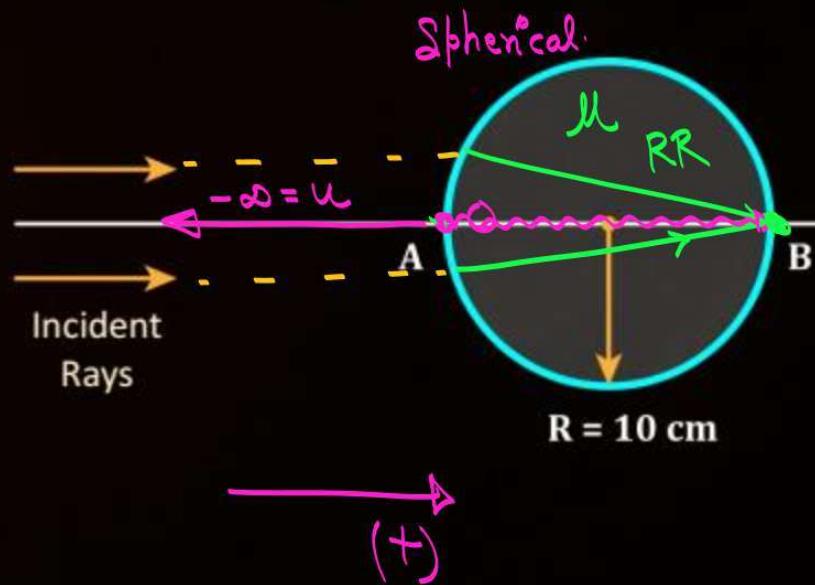
## Question 36



Figure shows a glass sphere of radius 10 cm. Along its diameter  $AB$  from one side a parallel beam of paraxial rays incident on it. What should be the refractive index of glass so that after refraction all rays will converge at opposite end  $B$ .

$$\frac{\mu_f}{v} - \frac{\mu_i}{u} = \frac{\mu_f - \mu_i}{R}$$

$$\begin{aligned}\mu_f &= \mu \\ \mu_i &= 1 \\ u &= -\infty \\ v &= +2R = +20 \\ R &= +R = +10\end{aligned}$$



## Question 37

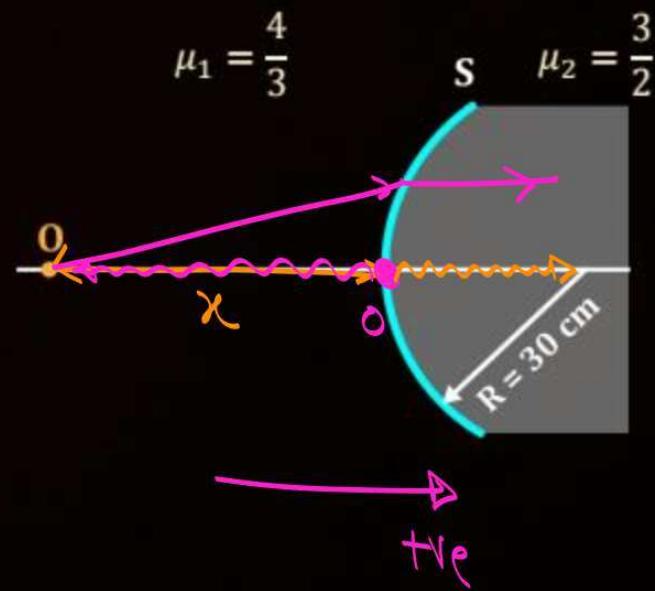


A spherical surface  $S$  separates two media 1 and 2 as shown in figure. Find where an object  $O$  is placed in medium-I so that the light rays from object after refraction becomes parallel to optics axis of this system.

Spherical

$$\frac{\mu_f}{v} - \frac{\mu_i}{u} = \frac{\mu_f - \mu_i}{R}$$

$\mu_f = 3/2$
$\mu_i = 4/3$
$u = -x$
$v = +\infty$
$R = +30$



## Question 38



Figure shows a small object M of length 1 mm which lies along a diametrical line of a glass sphere of radius 10 cm and  $\mu = 3/2$  which is viewed by an observer as shown. Find the size of object as seen by the observer.

$$\frac{t_I}{t_0} = \frac{\mu_i}{\mu_f} \frac{v^2}{u^2}$$

$$t_I = \frac{\mu_i}{\mu_f} \frac{v^2}{u^2} \times t_0$$

1 mm

$$\mu_i = 3/2$$

$$\mu_f = 1$$

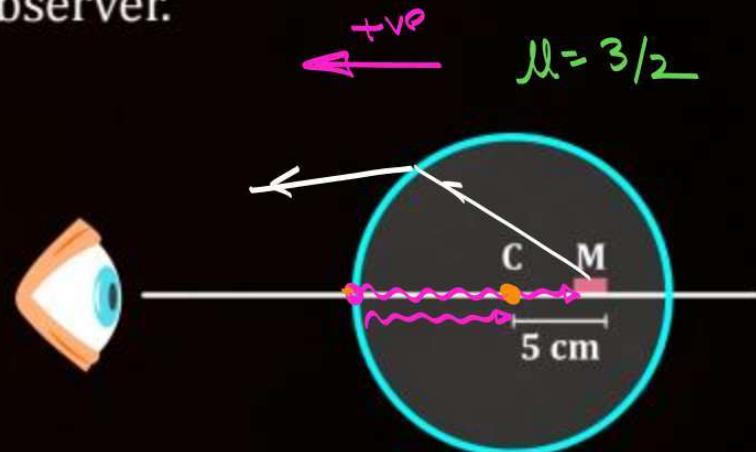
$$u = -15$$

$$v = +v$$

$$R = -10$$

$$\frac{\mu_f}{v} - \frac{\mu_i}{u} = \frac{\mu_f - \mu_i}{R}$$

$$v = \underline{\hspace{2cm}}$$



$$R = 10 \text{ cm}$$

## Question 39



The figure shows a fish bowl of radius 10 cm in which along a diametrical line a fish F is moving at speed 2 mm/sec. Find the speed of fish as observed by an observer outside along same line when fish is at a distance of 5 cm from the centre of bowl to right of it.

$$V_{I \parallel PA} = (\mu_{long}) V_{O \parallel PA}$$

$$V_{I \parallel PA} = \left( \frac{\mu_i}{\mu_f} \frac{u^2}{u^2} \right) 2 \frac{\text{mm}}{\text{s}}$$

$$\mu_i = \frac{4}{3}$$

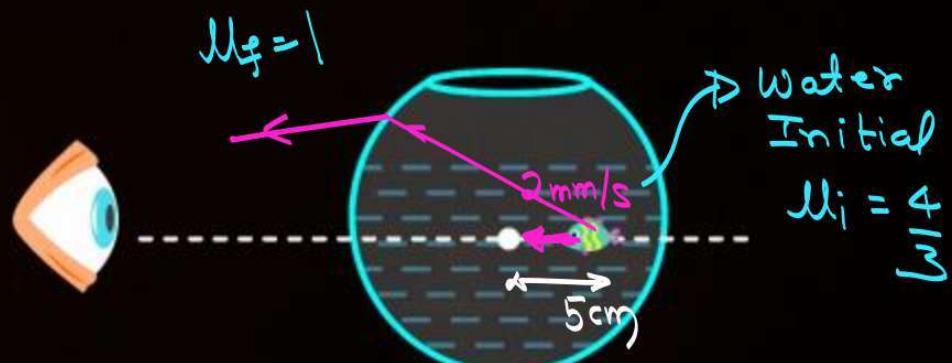
$$\mu_f = 1$$

$$u = -15$$

$$R = -10$$

$$v = +v$$

$$\frac{\mu_f - \mu_i}{u} = \frac{\mu_f - \mu_i}{R}$$



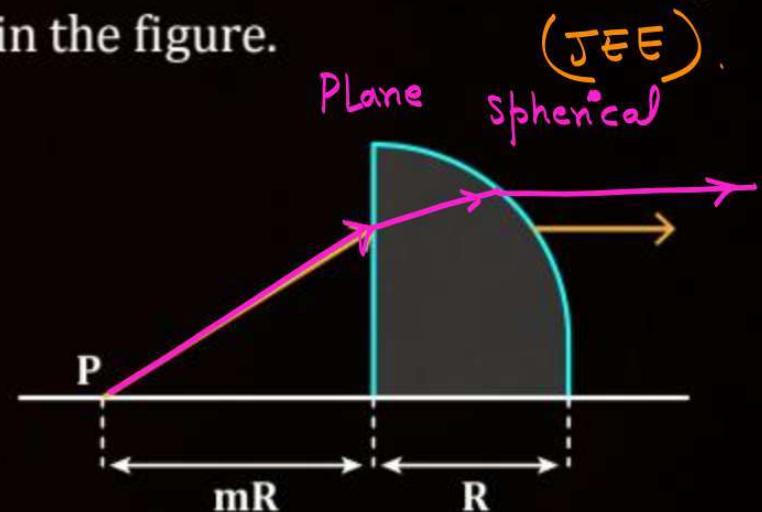
$$R = 10 \text{ cm}$$

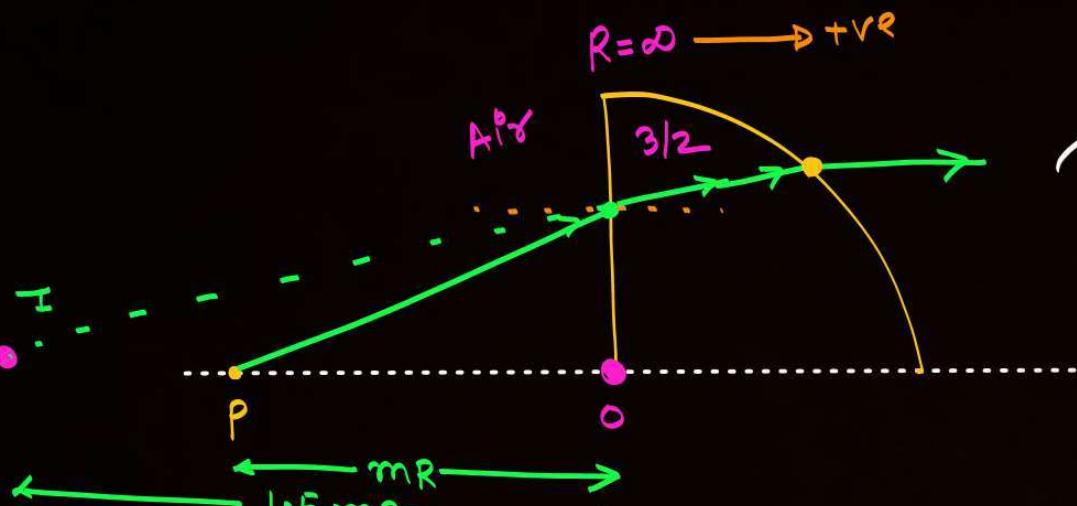
$$v = \underline{\hspace{2cm}}$$

## Question 40



A quarter cylinder of radius  $R$  and refractive index 1.5 is placed on a table. A point object  $P$  is kept at a distance of  $mR$  from it. Find the value of  $m$  for which a ray from  $P$  will emerge parallel to the table as shown in the figure.





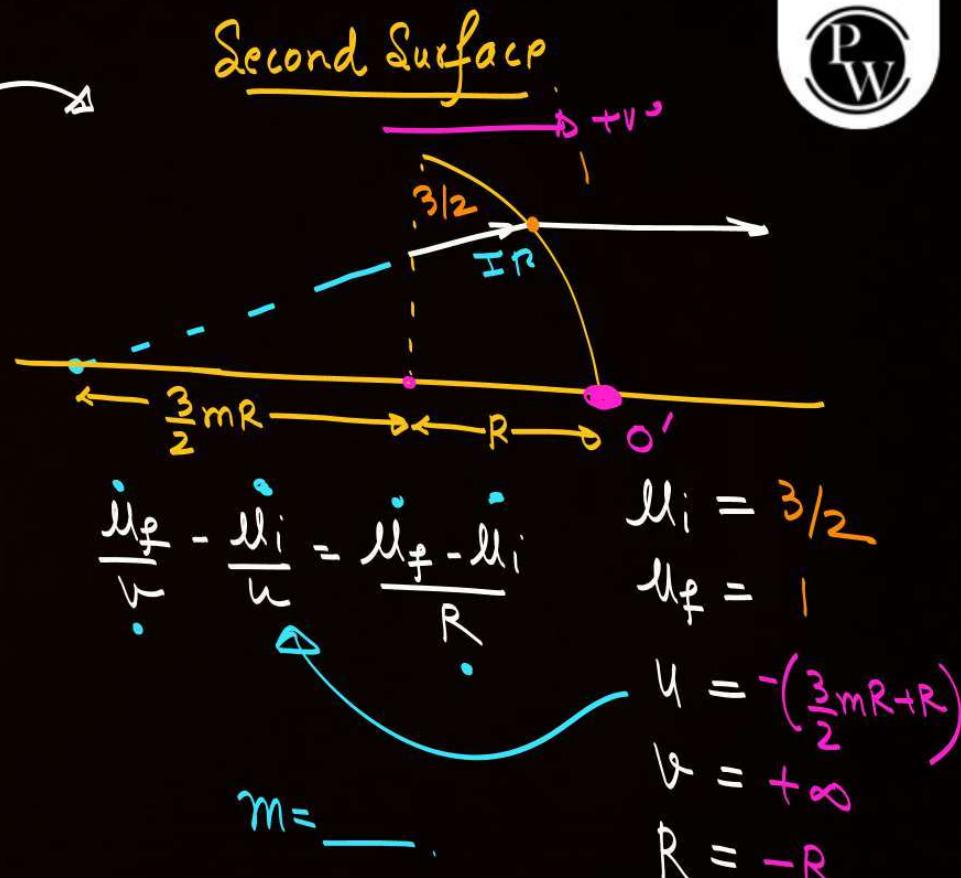
Plane

$$\frac{\mu_f}{v} - \frac{\mu_i}{u} = \frac{\mu_f - \mu_i}{R}$$

$$\frac{3}{2v} - \frac{1}{mR} = 0$$

$$\frac{3}{2v} = -\frac{1}{mR}$$

$$v = -\frac{3}{2}mR$$

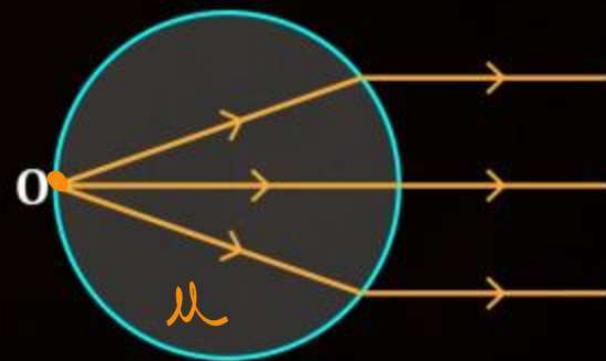


### Question 41

HW

P  
W

An object  $O$  is stuck on the surface of a transparent solid sphere of radius 20 cm. Find refractive index of the sphere such that rays from the object after refraction from the opposite side emerge as a parallel beam, as shown. Also prove that refractive index has the same value, in the given situation, for any value of radius of sphere.



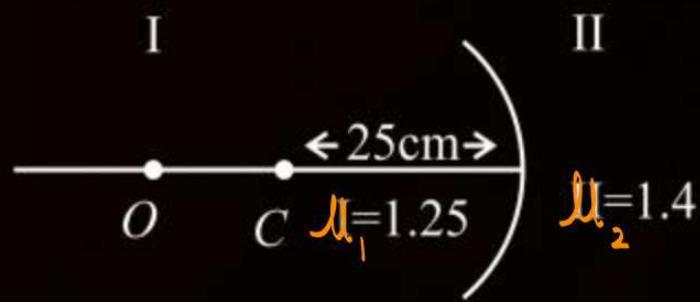
## Question (Homework)



Region I and II are separated by a spherical surface of radius 25 cm. An object is kept in region I and at a distance of 40 cm from the surface. The distance of the image from the surface is

[Main 20<sup>th</sup> July 1<sup>st</sup> Shift 2021]

- 1 9.52 cm
- 2 37.58 cm
- 3 55.44 cm
- 4 18.23 cm



[Ans: 2]

# Shift and Apparent Depth

**Shift of object due to Refraction at Plane Surface**

**Case-1:- When O is in denser medium**

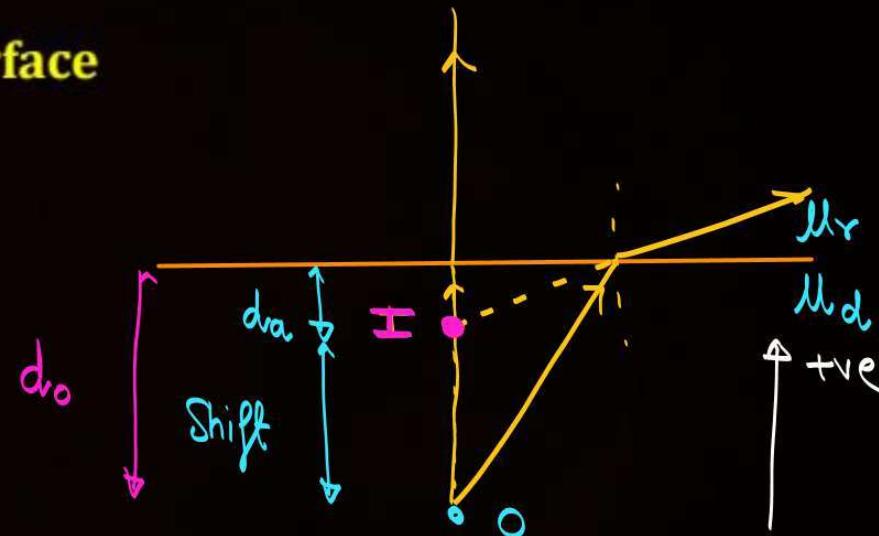
$$\begin{aligned} \mu_f &= \mu_r & \frac{\mu_f}{v} - \frac{\mu_i}{u} &= \frac{\mu_f - \mu_i}{R} \\ \mu_i &= \mu_d & & \\ u &= -d_o & \frac{\mu_r}{-d_o} + \frac{\mu_d}{d_o} &= 0 \\ v &= -d_a & -\frac{\mu_r}{d_a} &= \frac{\mu_d}{d_o} \end{aligned}$$

$$R = \infty$$

$$d_a = \frac{\mu_r d_o}{\mu_d}$$

$$\text{if } \mu_r = 1$$

$$d_{app} = \frac{d_o}{\mu}$$



$$\text{Shift} = d_o - \frac{d_o}{\mu} = d_o \left[ 1 - \frac{1}{\mu} \right]$$



## Shift and Apparent Depth



**Shift of object due to Refraction at Plane Surface**

**Case-2:- When O is in rarer medium**

$$\mu_i = \mu_r$$

$$\frac{\mu_f}{v} - \frac{\mu_i}{u} = \frac{\mu_f - \mu_i}{R}$$

$$\mu_f = \mu_d$$

$$u = -h_o$$

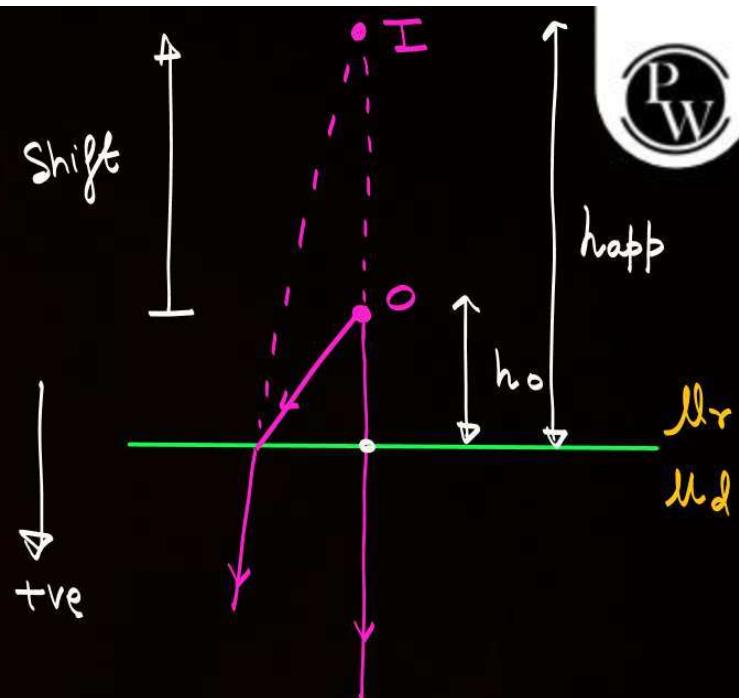
$$v = -h_a$$

$$R = \infty$$

$$\mu_r = 1$$

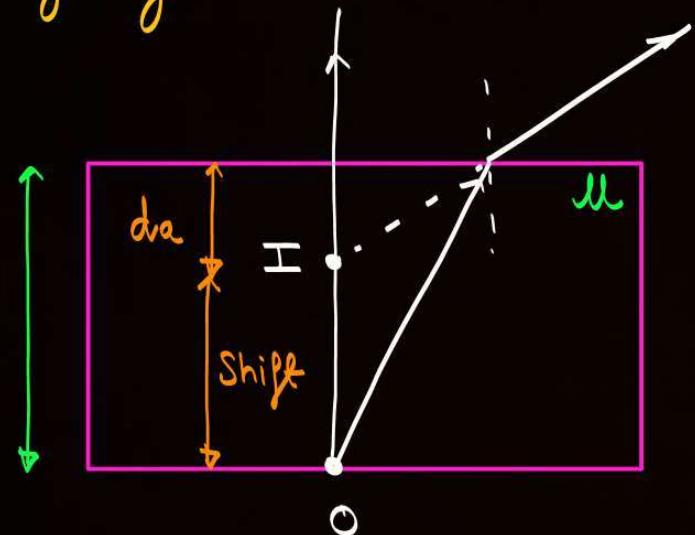
$$h_{app} = \mu_d h_o$$

$$\text{Shift} = \mu h - h = (\mu - 1) h$$



## \* Shift by Slab

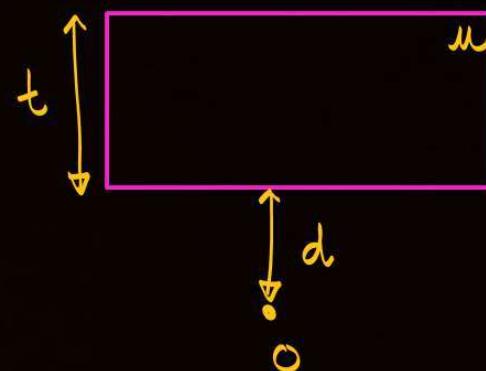
(a)



$$d_m = \frac{d_{\text{act}}}{\mu} = \frac{t}{\mu}$$

$$\text{Shift} = t - \frac{t}{\mu} = t \left[ 1 - \frac{1}{\mu} \right]$$

(b)



Shift by the Slab is  $= t \left[ 1 - \frac{1}{\mu} \right]$

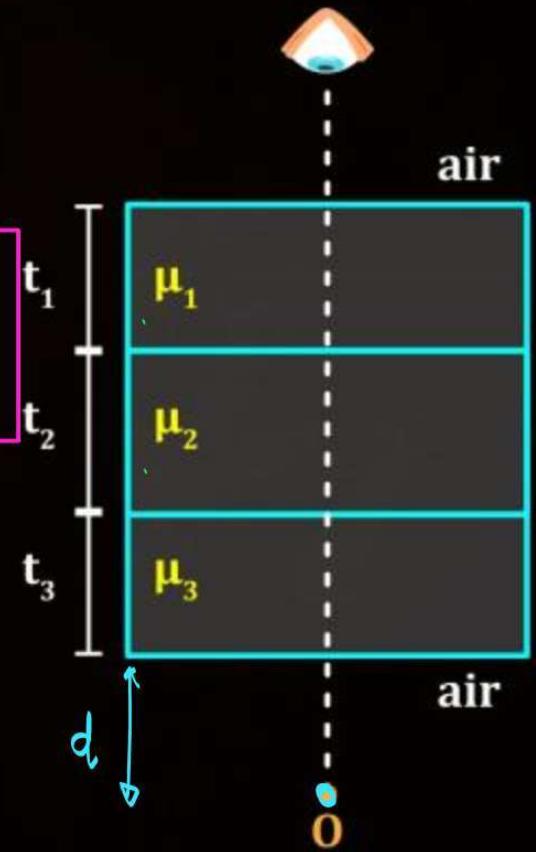
(Independent of d)



## Shift by slabs and multiple slabs

Total Shift =  $\sum$  Individual Shift.

$$\text{Total Shift} = t_1 \left[ 1 - \frac{1}{\mu_1} \right] + t_2 \left[ 1 - \frac{1}{\mu_2} \right] + t_3 \left[ 1 - \frac{1}{\mu_3} \right]$$



## Question 42



Find the apparent depth of an object O placed at the bottom of a beaker as shown in which two layers of transparent liquids are filled.

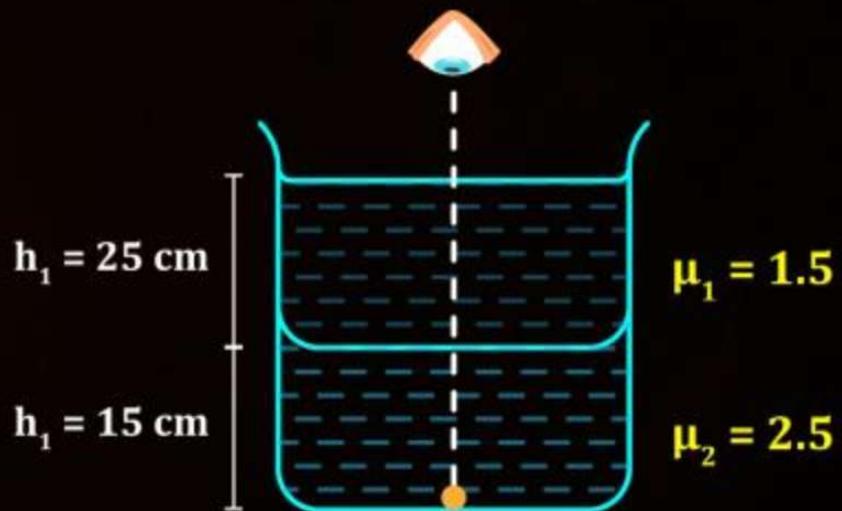
(two - slab)

$$\text{Total Shift} = h_1 \left[ 1 - \frac{1}{\mu_1} \right] + h_2 \left[ 1 - \frac{1}{\mu_2} \right]$$

$$\text{actual depth} = h_1 + h_2 = 25 + 15 = 40 \text{ cm}$$

④ Apparent depth = d.actual - Shift

$$= 40 - [\text{Shift}]$$



### Question 43



A converging beam of light rays incident on a glass-air interface as shown. Find where these rays will meet after refraction.

$$m_i = 1$$

$$m_f = 3/2$$

$$u = (\text{Intersection of IR}) = +20$$

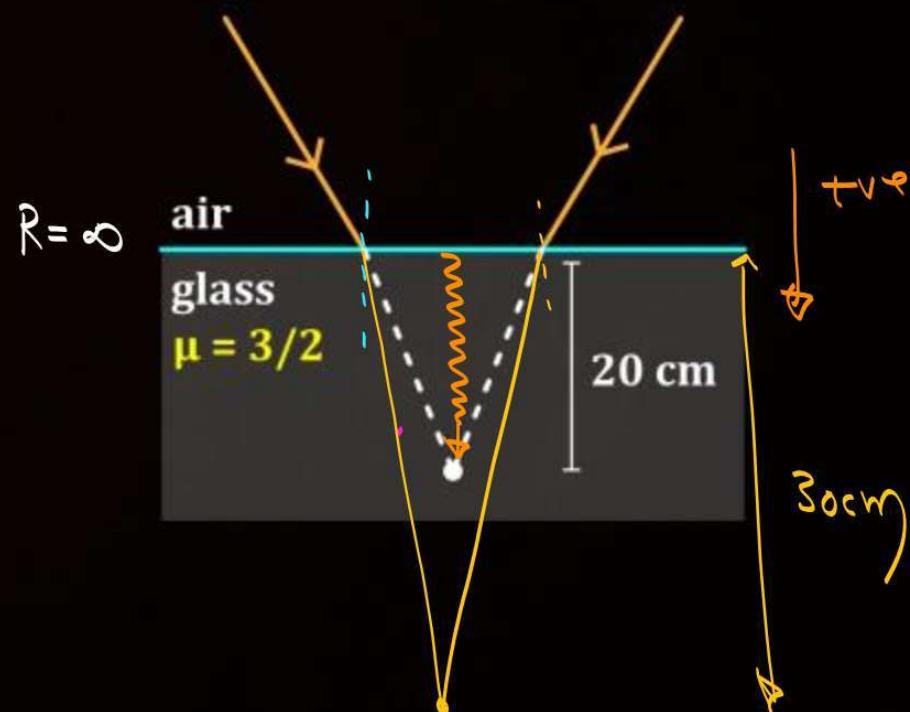
$$v = +v$$

$$R = \infty$$

$$\frac{m_f}{v} - \frac{m_i}{u} = \frac{m_f - m_i}{R}$$

$$\frac{3}{2v} - \frac{1}{+20} = 0$$

$$v = +30\text{ cm}$$

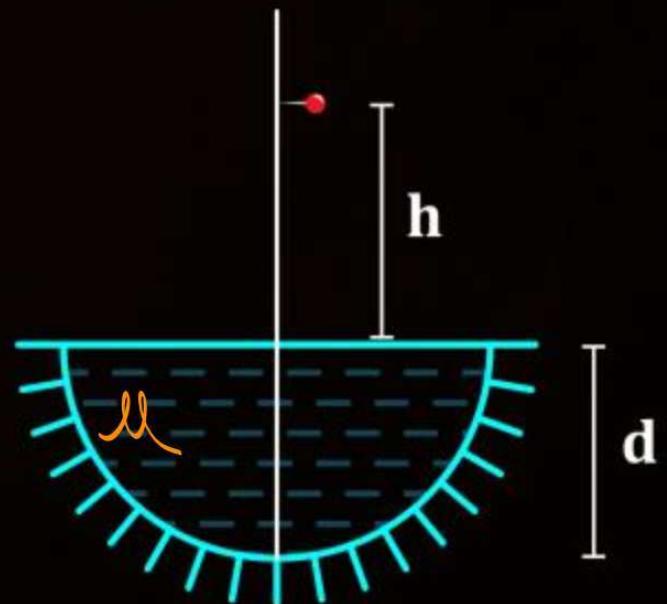


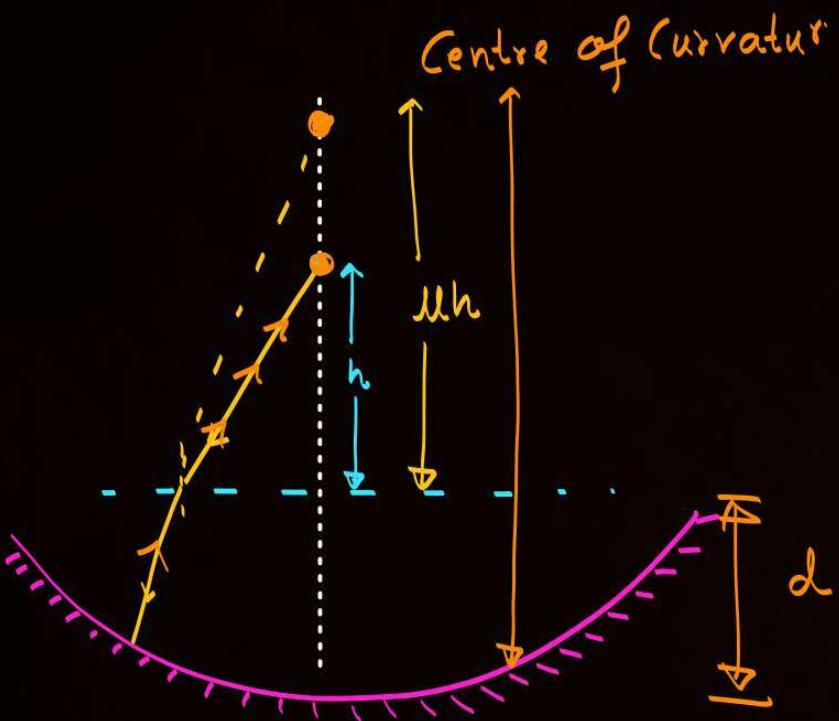
## Question 44



Figure shows a concave mirror of focal length  $F$  with its principal axis vertical. In mirror a transparent liquid of refractive index  $\mu$  is filled upto height  $d$ . Find where on axis of mirror a pin should be placed so that its image will be formed on itself.

Concept:- whenever Image has to be  
formed on object itself  
(Retrace light)



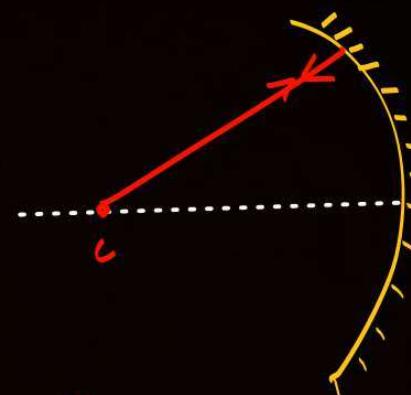


$$m_h + d = R$$

$$m_h + d = 2f$$

$$m_h = 2f - d$$

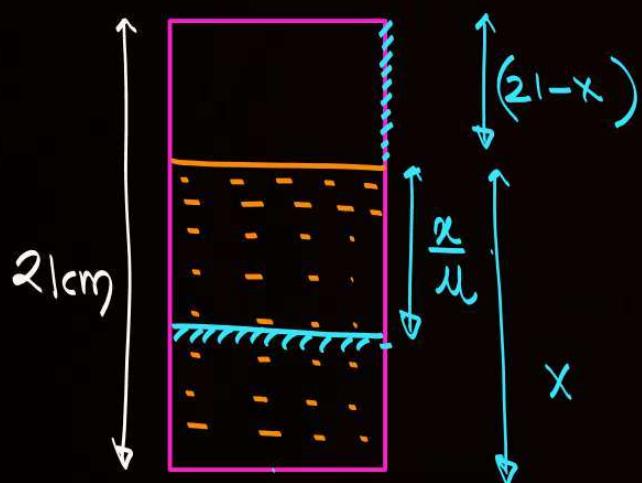
$$h = \frac{2f - d}{m_h}$$



## Question 45



How much water should be filled in a container of height 21 cm so that it will appear half filled when viewed along normal to water surface. (Take  $\mu_w = 4/3$ )



length of air column = length of Water column

$$21 - x = \frac{x}{\mu}$$

$$21 - x = \frac{3x}{4}$$

$$x = \underline{\hspace{2cm}}$$

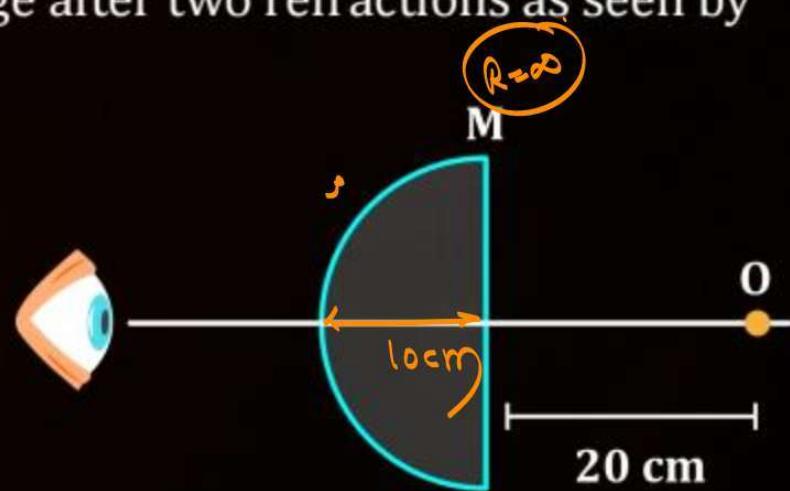
**Question 46**

HW

Thick lens

PW

Figure shows a glass hemisphere M of  $\mu = 3/2$  and radius 10 cm. A point object O is placed at a distance 20 cm behind the flat face which is viewed by an observer from the curved side. Find location of final image after two refractions as seen by observer.



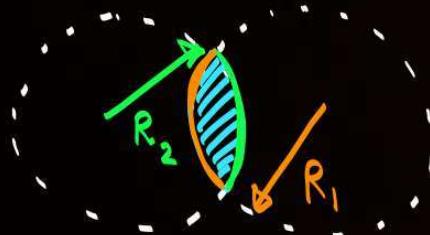


## Thin Lenses and its Types

→ Beech se Mota hota hai!

Case-1:- Convex Lenses (Intersecting surface lenses)

Biconvex lens



Bi-Convex

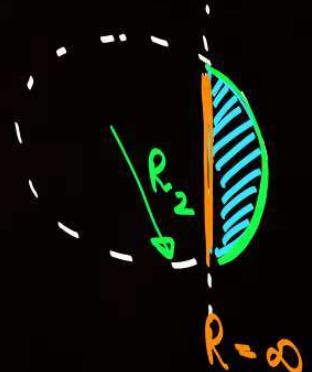
$$R_1 = R_2$$

Equi-Convex lens.

Concavo-convex lens



Plano-convex lens

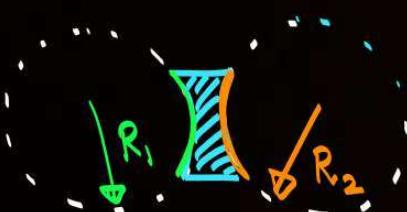


## Thin Lenses and its Types

→ Beech Se Patla hota hai.

Case-2:- Concave Lenses (Non-Intersecting surface lenses)

Bi-Concave



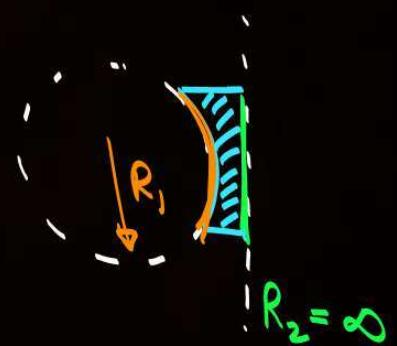
$$\text{if } R_1 = R_2$$

Equi-Concave.

Convexo-Concave



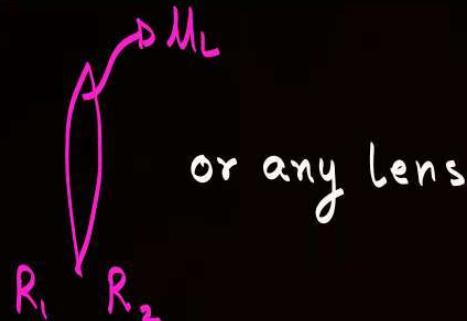
Plano-Concave





## Lens Makers Formula

⇒ derive focal length of thin lenses



or any lens

$$\frac{1}{f} = \left( \frac{\mu_L - 1}{\mu_s} \right) \left[ \frac{1}{R_1} - \frac{1}{R_2} \right]$$

Lens Maker formula.

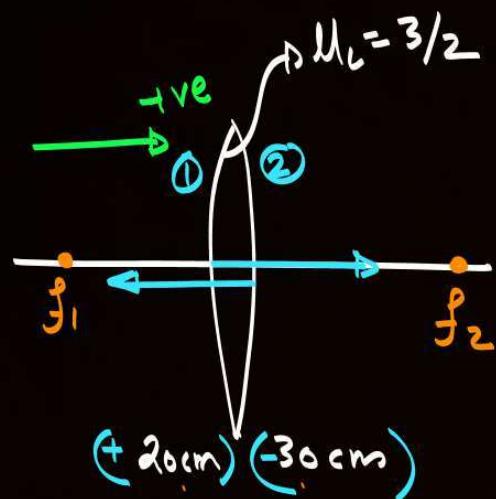
R<sub>1</sub> = first Surface light is incident

R<sub>2</sub> = Second Surface .. .. ..

Please take time  
→ to consider R<sub>1</sub> & R<sub>2</sub>

- Focus will be same on both side of lens even if radius is different
- Calculation of focal length using lens maker formula is independent of direction of incident ray
- We have to use the same sign convention used before. Light incident on first surface will be considered for first surface.
- For thick lenses we have to use the refraction formula separately for two surfaces keeping in consideration of thickness

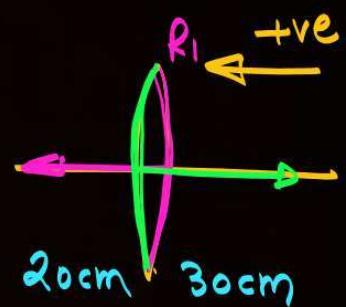
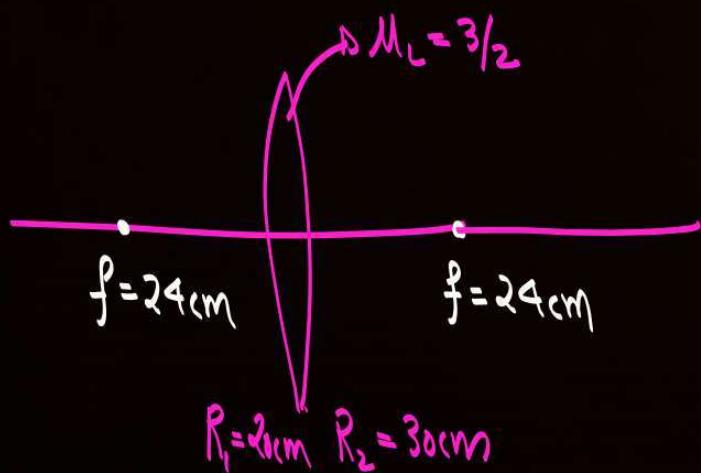
\*



$$\frac{1}{f} = \left(\frac{3}{2} - 1\right) \left[ \frac{1}{+20} - \frac{1}{-30} \right]$$

$$\frac{1}{f} = \frac{1}{2} \times \frac{8}{60/12}$$

$$f = 24 \text{ cm}$$



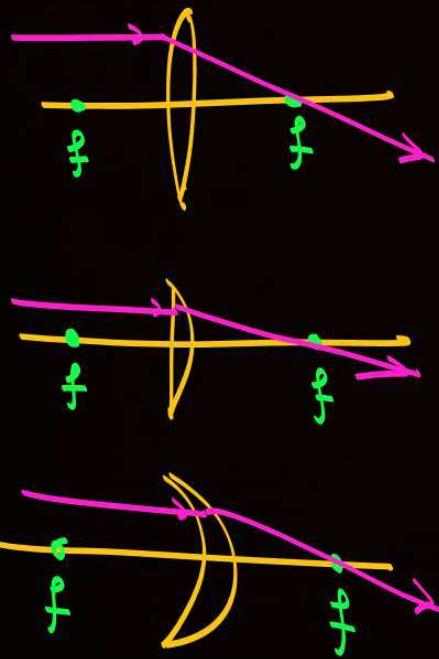
$$\frac{1}{f} = \left(\frac{3}{2} - 1\right) \left[ \frac{1}{+30} - \frac{1}{-20} \right]$$

$$\frac{1}{f} = \frac{1}{2} \times \frac{5}{60}$$

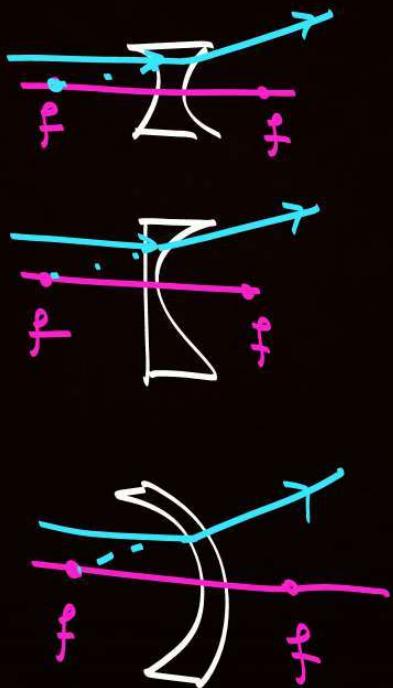
$$f = +24 \text{ cm}$$

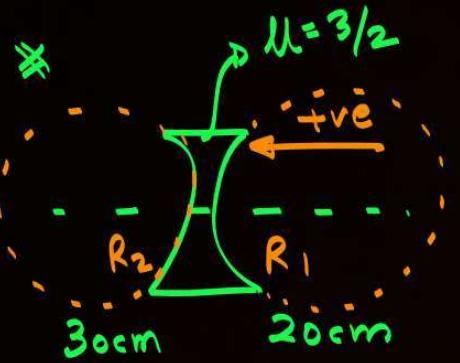
④ After lens Maker formula  $f = +ve$  (converging) (Main focus in dir of IR) PW

$f = -ve$  (diverging) (Main focus in opp dir of IR)



Converging.



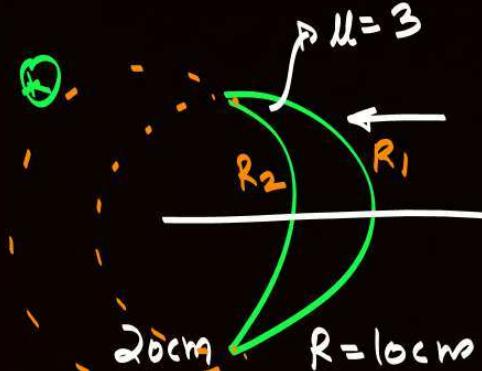
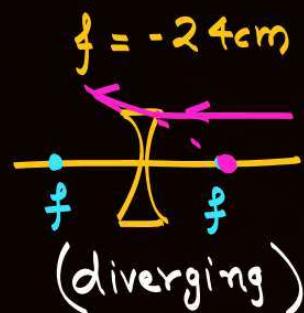


$$\frac{1}{f} = \left( \frac{3}{2} - 1 \right) \left[ \frac{1}{-20} - \frac{1}{30} \right]$$

★

$$R_1 = +10$$

$$R_2 = -20$$

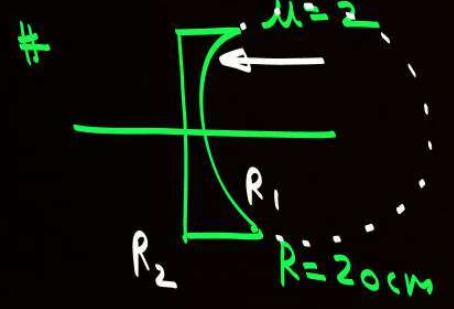


$$\frac{1}{f} = (3-1) \left[ \frac{1}{+10} - \frac{1}{+20} \right]$$

$$f = +ve \text{ } 10\text{cm}$$



Converging.



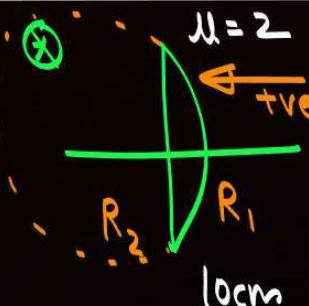
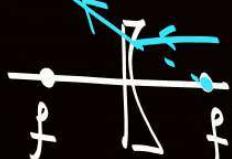
$$\frac{1}{f} = (2-1) \left[ \frac{1}{-20} - \frac{1}{\infty} \right]$$

$$f = -20\text{cm}$$

diver

$$R_1 = -20$$

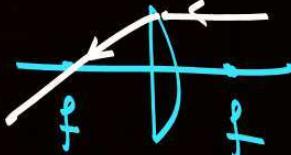
$$R_2 = \infty$$



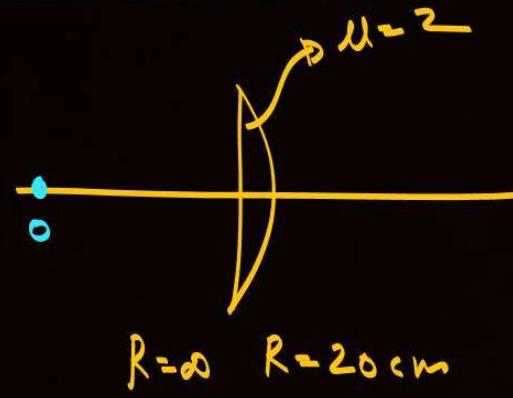
$$\frac{1}{f} = (2-1) \left[ \frac{1}{+10} - \frac{1}{+20} \right]$$

$$f = +10\text{cm}$$

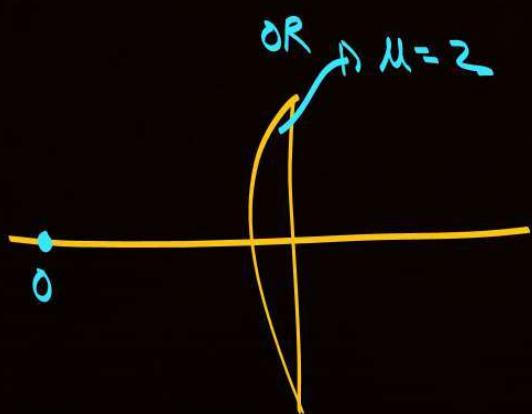
Converging.



# for Thin lenses.



$$R=\infty \quad f=20 \text{ cm}$$



$$R=20 \text{ cm} \quad f=\infty$$



Both are Same.

" $f$  is indep of orientation"  
of Thin lenses .

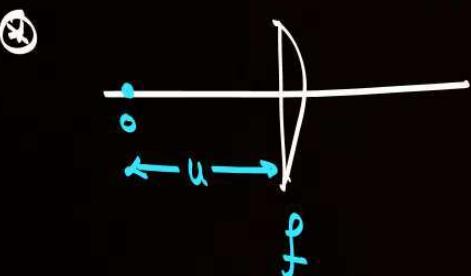
Light path plane par give ya Curve  
par koi difference nahi hai .

## Lens Formula

for any lens

$$\frac{1}{f} = \left( \frac{\mu_L}{\mu_s} - 1 \right) \left[ \frac{1}{R_1} - \frac{1}{R_2} \right]$$

↳ lens Maker formula.



$$\text{Lens formula} = \frac{1}{f} = \frac{1}{v} - \frac{1}{u}$$

↳ Same Sign Convention

$u$  = object dist

$v$  = Image dist

$f$  = focal length

$$\text{↳ } V_{I||PA} = (m_{long}) V_{o||PA}$$

$$V_{ILPA} = (m_{lat}) V_{OLPA}$$

magnifications

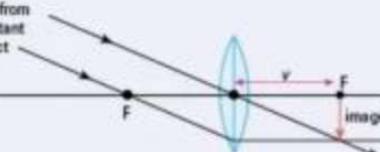
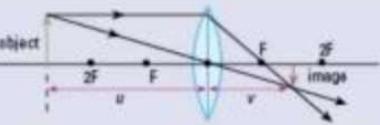
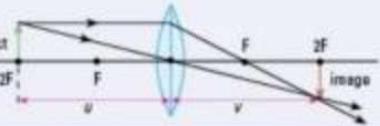
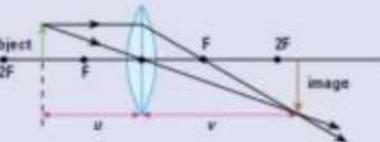
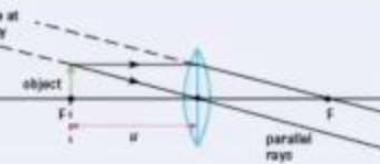
$$m_{lat} = \frac{h_I}{h_o} = \frac{v}{u}$$

$$m_{long} = \frac{t_I}{t_o} = \frac{v^2}{u^2}$$



# Ray Diagrams

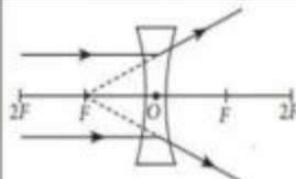
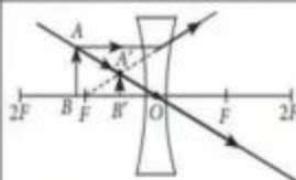


$U = \infty$		- inverted - real - diminished	$v = f$ - opposite side of the lens
$u > 2f$		- inverted - real - diminished	$f < v < 2f$ - opposite side of the lens
$u = 2f$		- inverted - real - same size	$v = 2f$ - opposite side of the lens
$f < u < 2f$		- inverted - real - magnified	$v > 2f$ - opposite side of the lens
$u = f$		- upright - virtual - magnified	- image at infinity - same side of the lens
$u < f$		- upright - virtual - magnified	- image is behind the object - same side of the lens



# Ray Diagrams

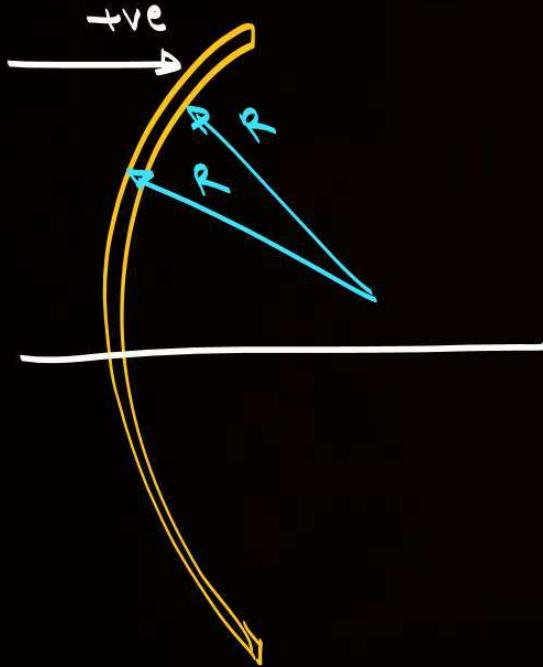


Concave lens				
	Ray diagram	Position of object	Position of image	Nature of image
(a)	 $u = -ve, v = -ve \text{ and } f = -ve$	At infinity	At $F$	Virtual, erect and highly diminished
(b)	 $u = -ve, v = -ve \text{ and } f = -ve$	Between infinity and $O$	Between $F$ and $O$	Virtual, erect and diminished

## Question 47



Prove that a hollow equiconvex lens of glass will behave like a glass plate.

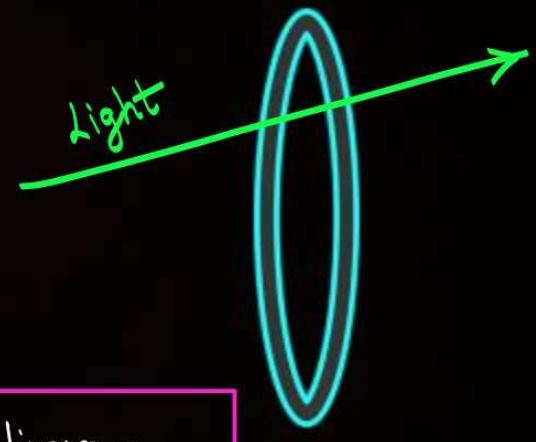


$$\frac{1}{f} = (\mu - 1) \left[ \frac{1}{R} - \frac{1}{R} \right]$$

$$\frac{1}{f} = 0$$

$$f = \infty$$

No Convergence & No divergence



Thin hollow equi-convex

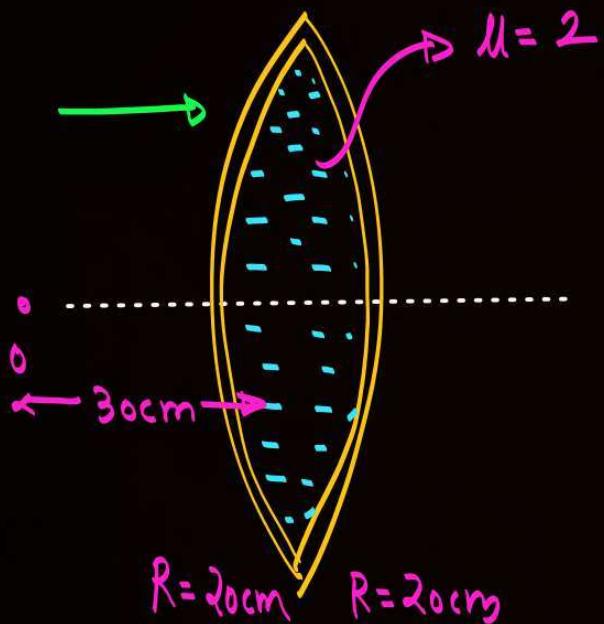


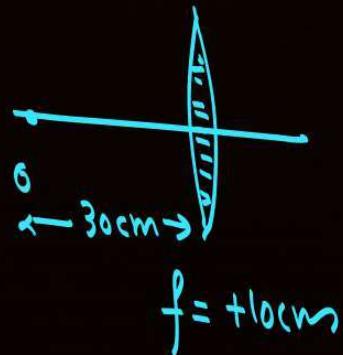
Image location = ?

"Liquid lens"

$$\frac{1}{f} = (2-1) \left[ \frac{1}{+20} - \frac{1}{-20} \right]$$

$$\frac{1}{f} = \frac{2}{20}$$

$$f = +10 \text{ cm} \quad \text{X}$$



$$u = -30 \quad f = +10 \quad \frac{1}{f} = \frac{1}{v} - \frac{1}{u} \quad v = +15 \text{ cm}$$



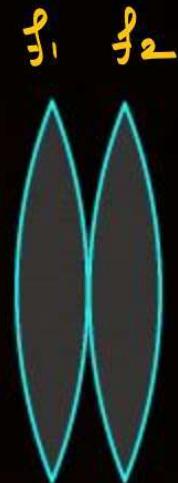
## Combination of Lenses



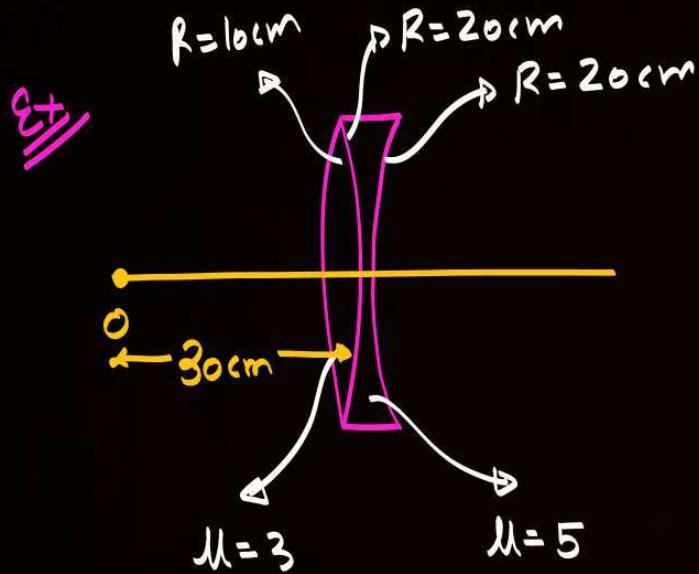
When two thin are in Contact  
we Can replace them with an equivalent  
lens

$$\frac{1}{f_{eq}} = \frac{1}{f_1} + \frac{1}{f_2}$$

with Sign



$f_{eq}$  = +ve Converging lens will Replace both  
= -ve diverging " "



$$\frac{1}{f_{eq}} = \frac{1}{f_1} + \frac{1}{f_2} = \frac{3}{10} - \frac{2}{5}$$

$$= \frac{3-4}{10}$$

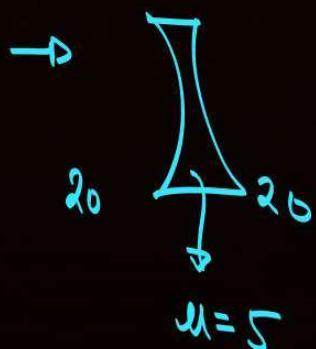
$$f_{eq} = -10$$

location of Image

Convex lens  $\frac{1}{f} = (S-1) \left[ \frac{1}{+10} - \frac{1}{-20} \right]$

$$\frac{1}{f} = 2 \left[ \frac{2+1}{20} \right] \Rightarrow f = +\frac{10}{3}$$

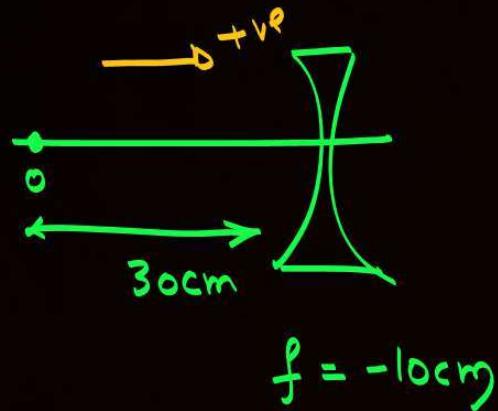
Concave lens :-



$$\frac{1}{f_2} = (S-1) \left[ -\frac{1}{20} - \frac{1}{20} \right]$$

$$\frac{1}{f_2} = -\frac{4 \times 2}{20}$$

$$f_2 = -\frac{5}{2}$$



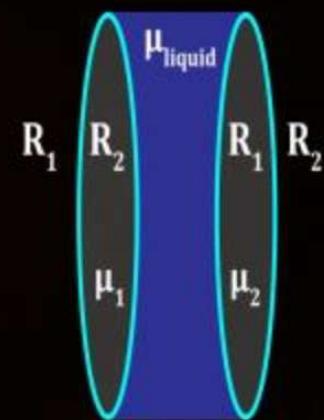
$$\frac{1}{f} = \frac{1}{v} - \frac{1}{u}$$

$$-\frac{1}{10} = \frac{1}{v} - \frac{1}{-30}$$

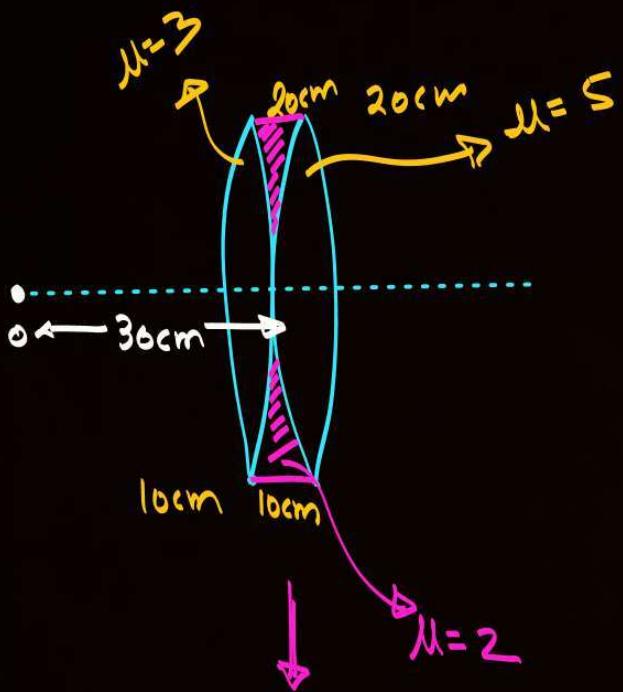
$$v = \underline{\hspace{2cm}}$$

## Combination of Lenses

Two convex lenses are placed, the gap between them is filled with a liquid of refractive index  $\mu_{\text{liquid}}$ . This combination is placed in the air then. The system is equal to combination of three thin lenses in contact, then



E+



$$\frac{1}{f_{eq}} = \frac{3}{5} + \frac{2}{5} - \frac{3}{20}$$

$$\frac{1}{f_{eq}} = \frac{8+8-3}{20} = \frac{13}{20}$$

$$f_{eq} = +\frac{20}{13}$$

Three thin lenses Pn Contact.

① lens  $\frac{1}{f_1} = (3-1) \left[ \frac{1}{+10} - \frac{1}{-10} \right]$

$$\frac{1}{f_1} = 2 \times \frac{2}{10}$$

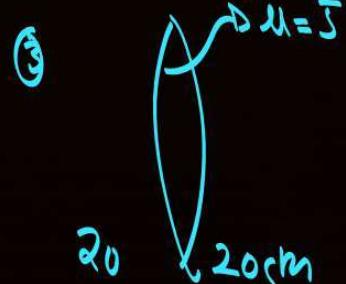
$$f_1 = +\frac{5}{2}$$



②  $\frac{1}{f_2} = (2-1) \left[ -\frac{1}{10} - \frac{1}{20} \right]$

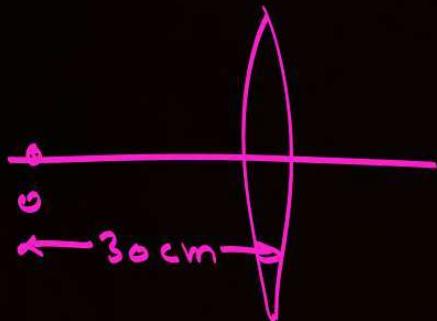
$$\frac{1}{f_2} = -\frac{3}{20}$$

$$f_2 = -\frac{20}{3}$$



③  $\frac{1}{f_3} = (5-1) \left[ \frac{1}{20} - \frac{1}{-20} \right] \quad \frac{1}{f_3} = \frac{4 \times 2}{20} = \frac{4}{5}$

$$f_3 = 5/4$$



$$f = +\frac{20}{13}$$

$$\frac{1}{f} = \frac{1}{v} - \frac{1}{u}$$

$$u = -30$$
$$f = +\frac{20}{13}$$

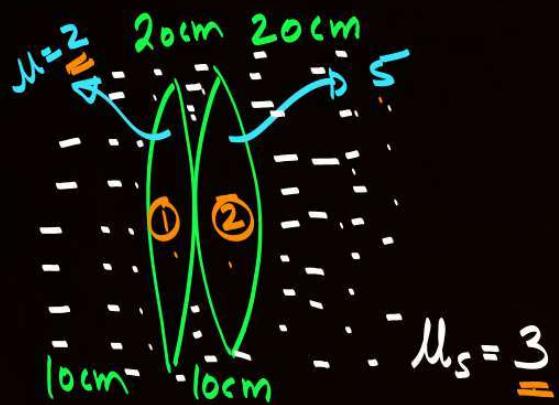
$$v = \underline{\hspace{2cm}}$$

## Combination of Lenses

Two convex lenses are kept in contact and the whole arrangement is placed in a liquid of refractive index  $\mu_{\text{liquid}}$  then this is equivalent to combination of two lenses kept in contact in a medium.



Ex



$$\mu_s = \underline{3}$$

↓

Combination

$$\frac{1}{f_{eq}} = \frac{1}{+15} + \frac{1}{-15} = 0$$

$$f_{eq} = \infty$$

Kisi Kaam Ke Nahi hai ye Jond.

Lens - ①

$$\frac{1}{f_1} = \left( \frac{2}{3} - 1 \right) \left[ \frac{1}{10} - \frac{1}{-10} \right]$$

$$\frac{1}{f_1} = -\frac{1}{3} \times \frac{2}{10}$$

$$f_1 = -15 \text{ cm}$$

divergin

Lens - ②

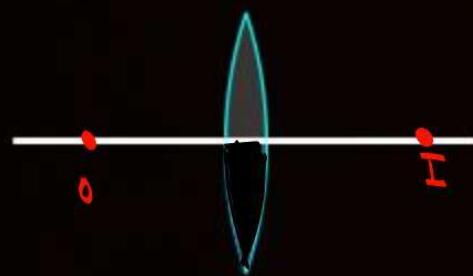
$$\frac{1}{f_2} = \left( \frac{5}{3} - 1 \right) \left[ \frac{1}{+20} - \frac{1}{-20} \right]$$

$$\frac{1}{f_2} = \frac{2}{3} \times \frac{2}{20} = \boxed{f_2 = +15 \text{ cm}} \quad (\text{Converging})$$



## Important Points

Every part of a lens forms complete image. If a portion of lens is obstructed full image will be formed but the intensity will be reduced.



Mirror | lens  
Image  $\rightarrow$  complete  
Brightness  $\rightarrow \frac{1}{2}$ .

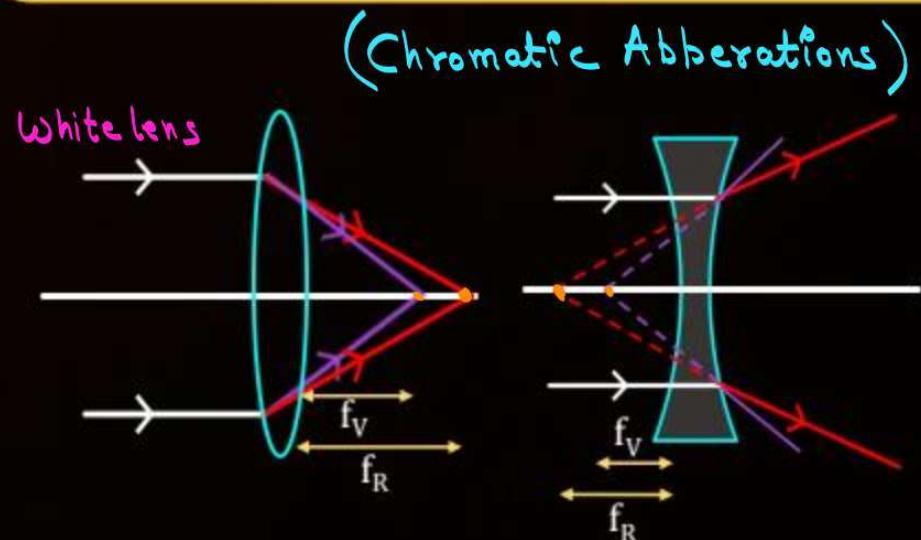
White Light (VIBGYOR)

$$\frac{1}{f} = (\mu - 1) \left[ \frac{1}{R_1} - \frac{1}{R_2} \right]$$

$$f_R > f_V$$

The focal length of a lens depends on its refractive index i.e.,

$$\frac{1}{f} \propto (\mu - 1)$$



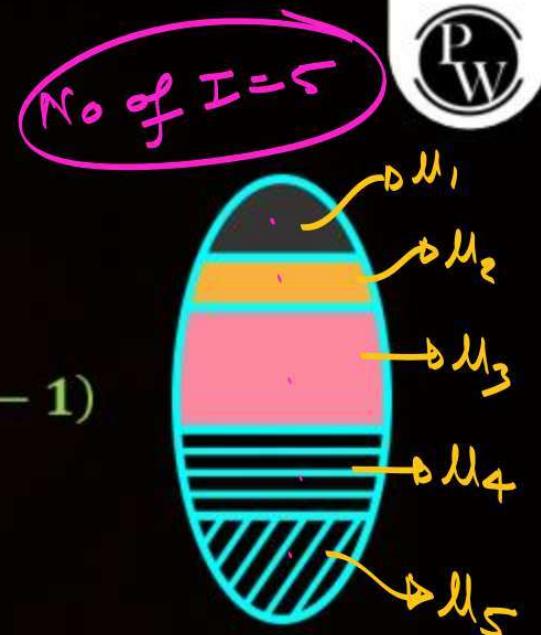


## Important Points

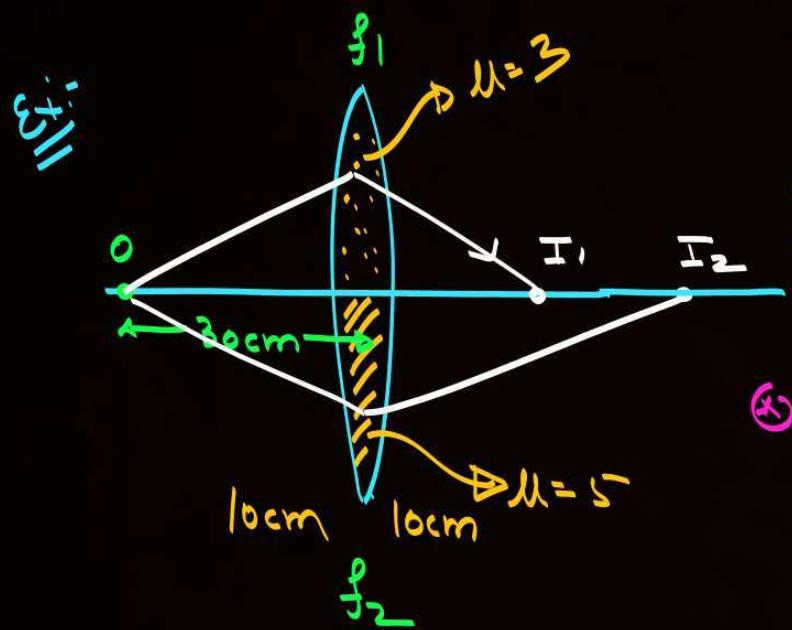
### Filling up of a lens

If a lens made a number of layers of different refractive indices as shown in figure for a given wavelength of light it will have many focal lengths

$$\frac{1}{f} \propto (\mu - 1)$$



No of Images = No of RI



$$U_1 = -30 \text{ cm}$$

$$f_1 = +5 \text{ cm}$$

$$V_1 = \underline{\quad}$$

$$U_2 = -30 \text{ cm}$$

$$f_2 = +5/4 \text{ cm}$$

$$V_2 = \underline{\quad}$$

$\Rightarrow$  No of Images = 2

$$\frac{1}{f} = (\mu_e - 1) \left[ \frac{1}{R_1} - \frac{1}{R_2} \right]$$

Same.

$$\oplus \frac{1}{f_1} = (3-1) \left[ \frac{1}{10} - \frac{1}{-10} \right] = \frac{1}{f_1} = 2 \times \frac{2}{10}$$

$$f_1 = \frac{5}{2}$$

$$\oplus \frac{1}{f_2} = (5-1) \left[ \frac{1}{10} - \frac{1}{-10} \right]$$

$$\frac{1}{f_2} = 4 \times \frac{2}{10}$$

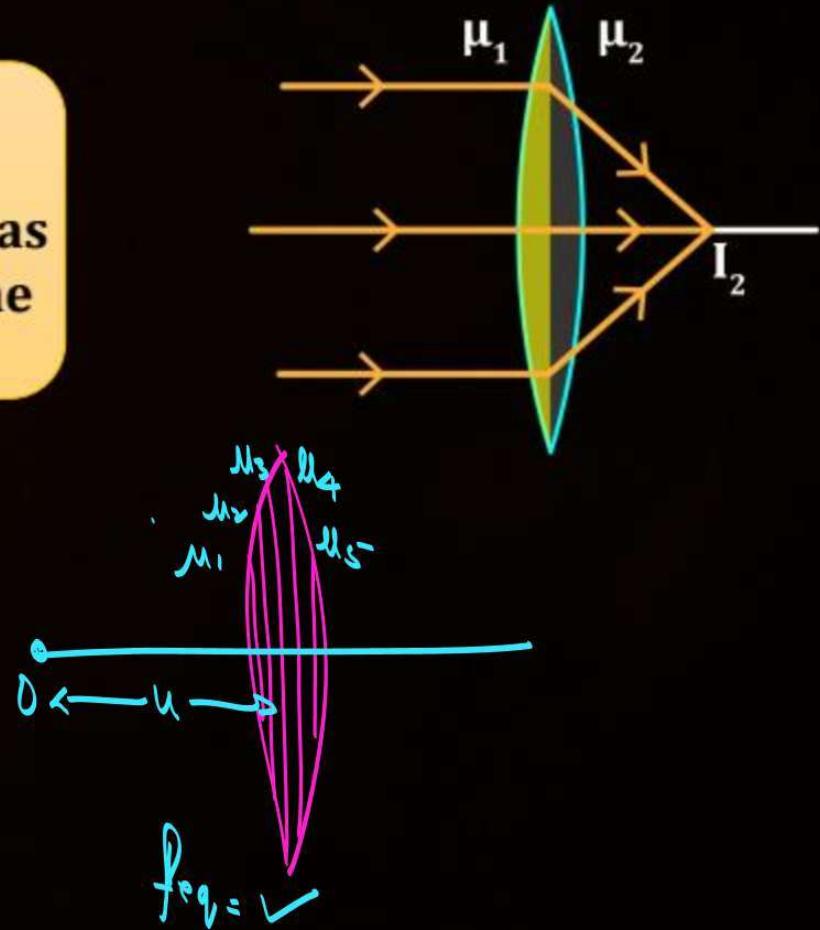
$$f_2 = 5/4$$

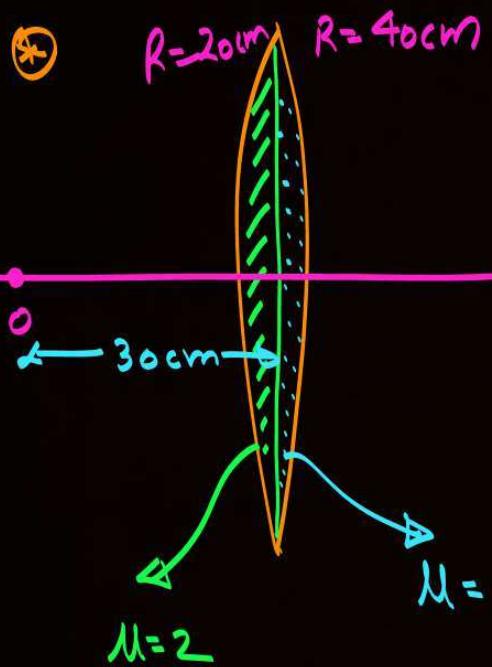
## Important Points

### Filling up of a lens

If a lens is made of two or more materials and are placed side by side as shown in figure, then there will be one focal length and hence one image.

$$\text{No of } I = 1$$





No of Images = 1

$$u = -30$$

$$f = +20/3 \quad v = \underline{\hspace{2cm}}$$

Two thin lenses in Contact



$$\frac{1}{f} = (2-1) \left[ \frac{1}{+20} - \frac{1}{\infty} \right]$$

$$f_1 = +20$$

$$\frac{1}{f_2} = (5-1) \left[ \frac{1}{\infty} - \frac{1}{-40} \right]$$

$$f_2 = +10\text{cm}$$

Contact

$$\frac{1}{f_{eq}} = \frac{1}{20} + \frac{1}{10} = \frac{3}{20}$$

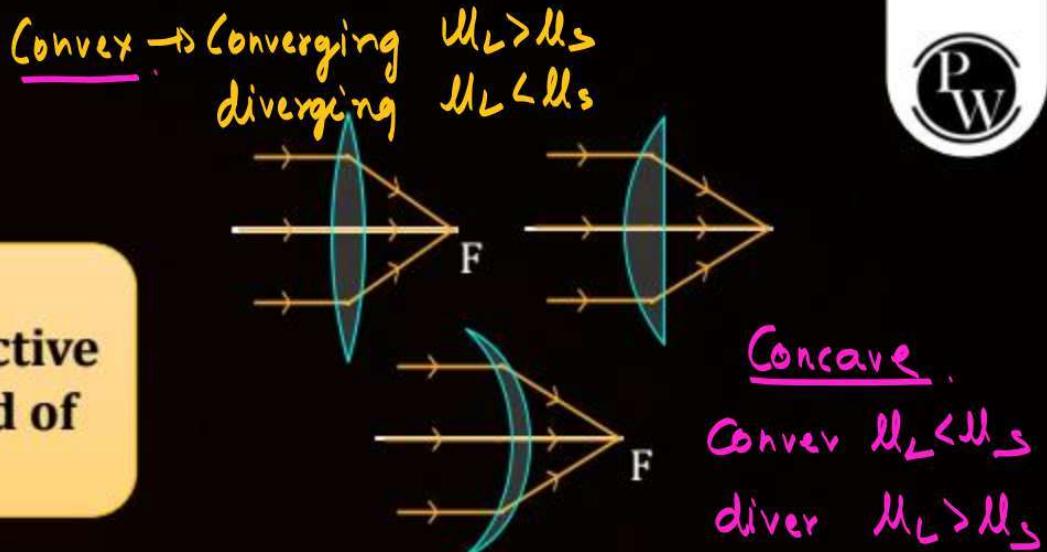
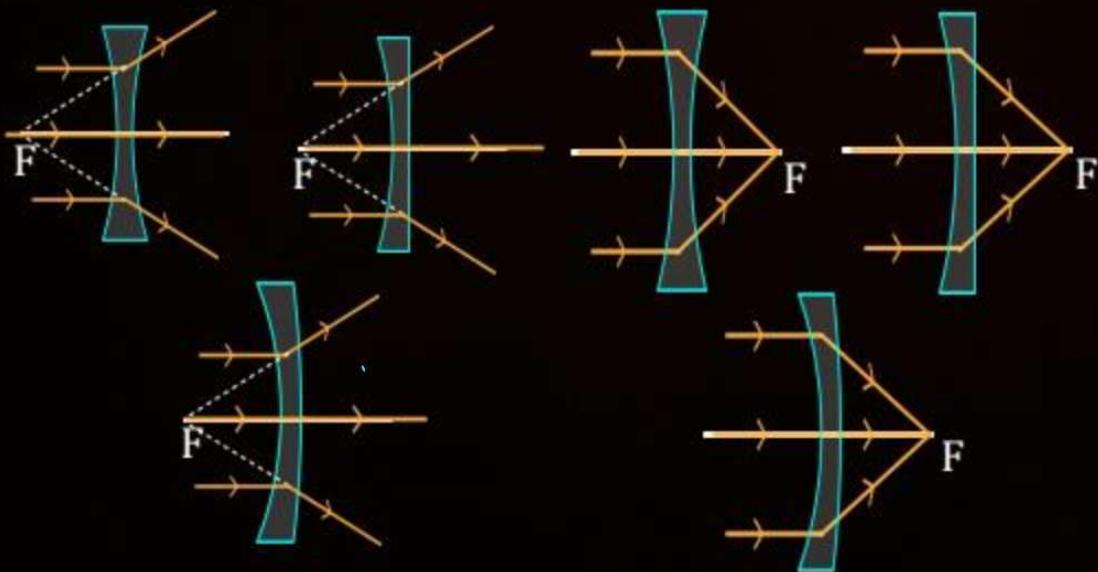
$$f_{eq} = 20/3$$





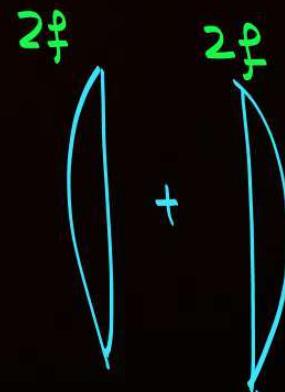
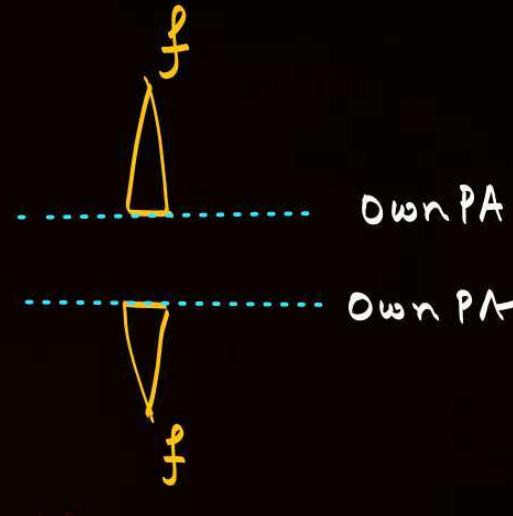
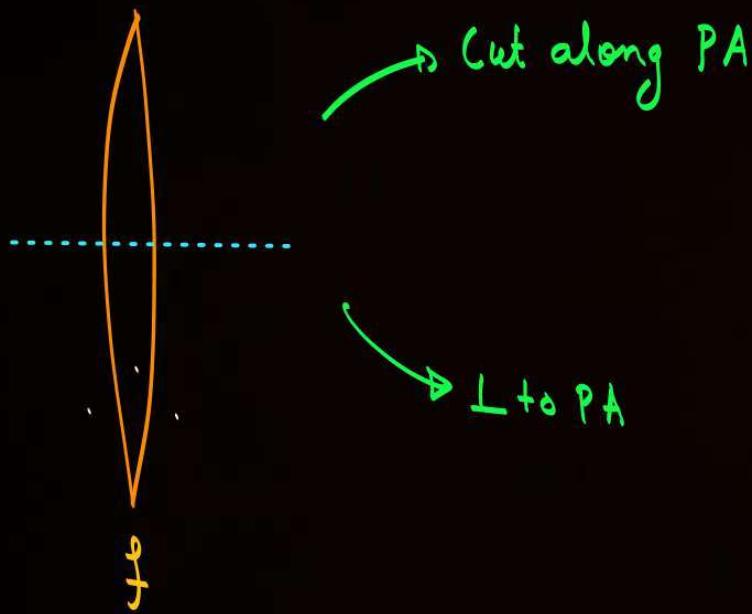
## Important Points

**Lens immersed in a liquid**  
If a lens made of material of refractive index  $\mu_{\text{lens}}$  is immersed in a liquid of refractive index  $\mu_{\text{liquid}}$ ,





## Cutting of a Lens



when Combined back

$$\frac{1}{f_{eq}} = \frac{1}{2f} + \frac{1}{2f}$$
$$f_{eq} = f$$

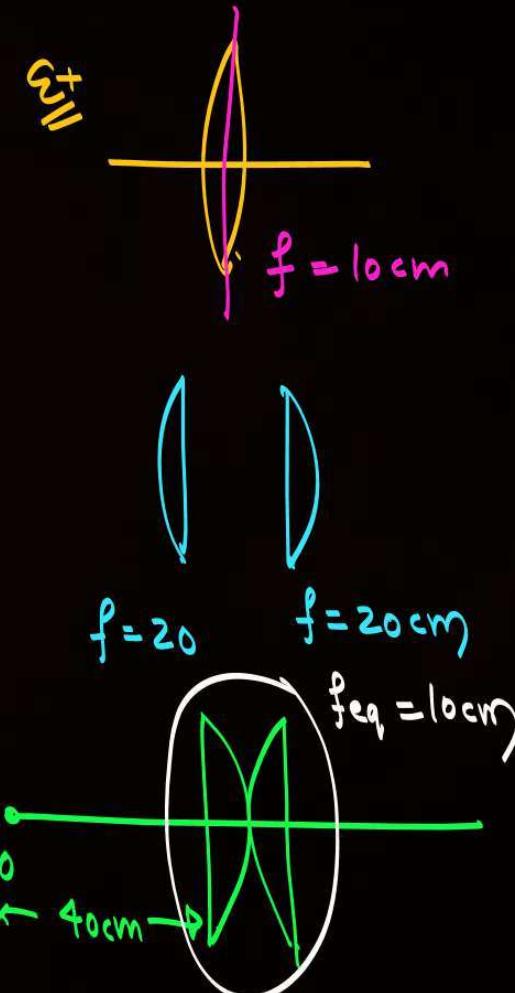


## Cutting of a Lens



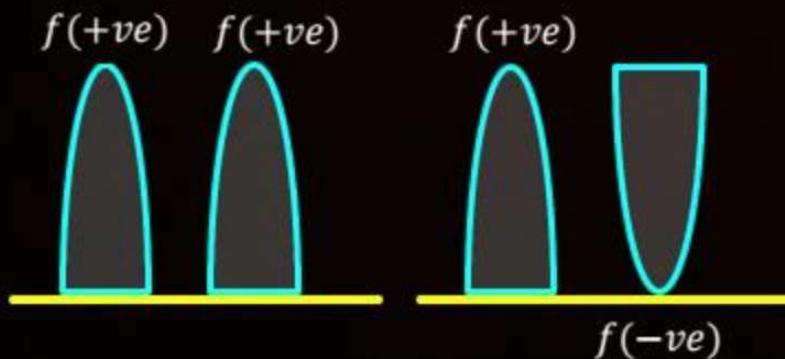
Equi-convex lens is divided into two equal parts transverse to the principal axis. The focal length of each part is  $2f$ . If these two parts are put in contact in a different combination, then

$$2f \quad 2f \quad + \quad \text{or} \quad 2f \quad 2f \quad + \quad \text{or} \quad 2f \quad 2f \quad +$$
$$\begin{array}{c} \text{f}_{eq} = f \\ \text{f}_{eq} = f \\ \text{f}_{eq} = f \end{array}$$

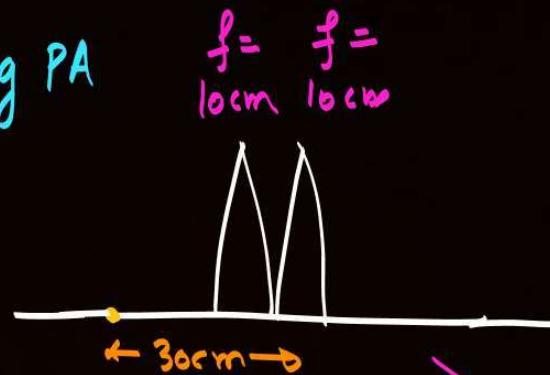
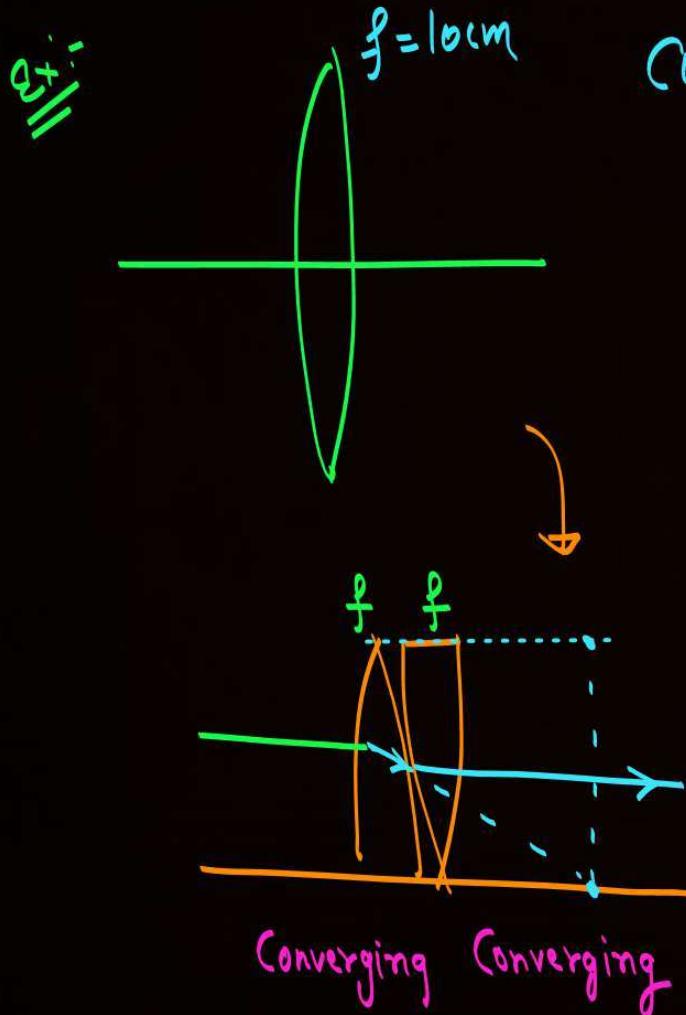


## Cutting of a Lens

Equi-convex lens is divided into two equal parts along its principal axis, the focal length of each part is  $f$ . If these two parts are put in contact in different combination, then



find Location  
of Image.



Two thin lenses in Contact

$u = -30\text{cm}$

$f = +5^-$

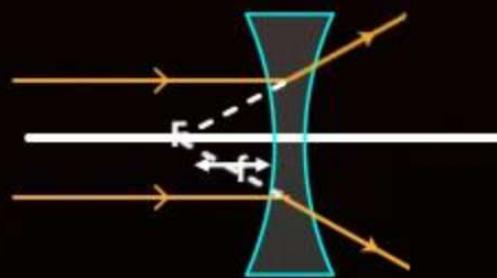
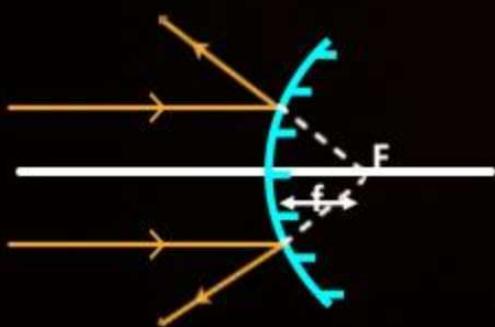
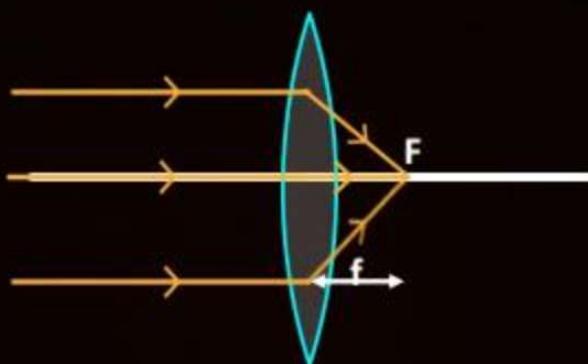
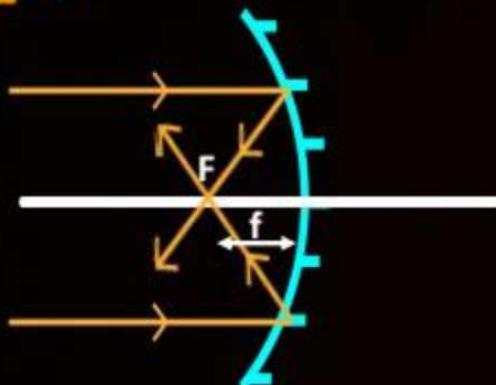
$v = \dots$

$\frac{1}{f_{eq}} = \frac{1}{10} + \frac{1}{10}$

$f_{eq} = 5$

Effect Cancelled out.  $f_{eq} = \infty$

## Power of Concave Mirror and Convex Lens



$$P_M = -\frac{1}{f(m)}$$

$$P_L = \frac{1}{f(m)}$$

Converging Mirror/lens  $P = +ve$   
diverging Mirror/lens  $P = -ve$

### Question 48

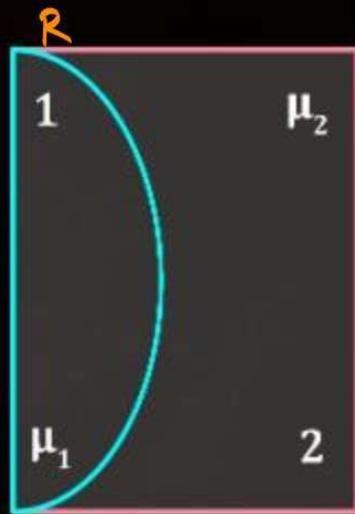
One plano-convex and one plano-concave lens of same radius of curvature R but of different materials are joined side by side as shown in figure. If the refractive index of the material 1 is  $\mu_1$  and that of 2 is  $\mu_2$ , then the focal length of the combination is

1  $\frac{2R}{\mu_1 - \mu_2}$

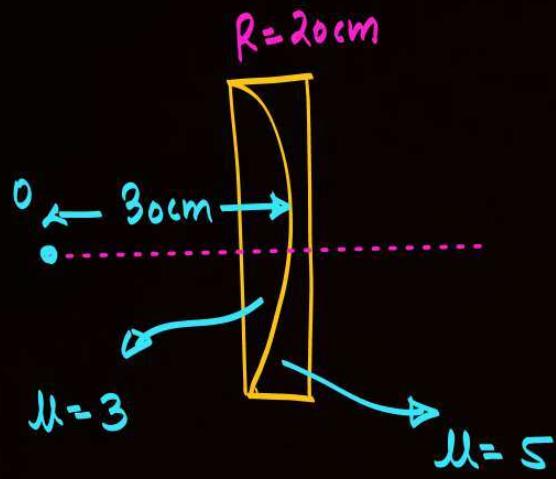
2  $\frac{R}{2 - (\mu_1 - \mu_2)}$

3  $\frac{R}{2(\mu_1 - \mu_2)}$

4  $\frac{R}{\mu_1 - \mu_2}$



Ex

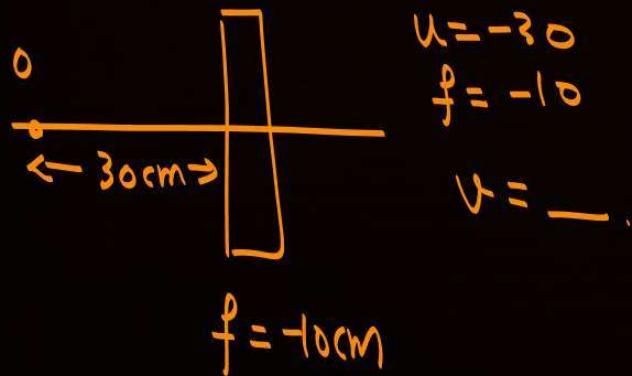


### Plano Concave & Plano Convex lens

$$\left| \frac{1}{f_1} = (3-1) \left[ \frac{1}{\infty} - \frac{1}{-20} \right] \right| \quad f_1 = 10\text{ cm}$$

$$\left| \frac{1}{f_2} = (5-1) \left[ -\frac{1}{20} - \frac{1}{\infty} \right] \right| \quad f_2 = -5\text{ cm}$$

Find Location of Image =



Combination  $\rightarrow$  Slab

$$\frac{1}{f_{eq}} = \frac{1}{f_1} + \frac{1}{f_2} = \frac{1}{10} - \frac{1}{5} = \frac{1-2}{10}$$

$$f_{eq} = -10$$

diverging

### Question 49



An equi-convex lens of refractive index  $(3/2)$  and focal length  $10\text{ cm}$  is held with its axis vertical and its lower surface immersed in water ( $\mu = 4/3$ ), the upper surface being in air. At what distance from the lens, will a vertical beam of parallel light incident on the lens be focused?

## Question 50

LW

When a beam of white light is allowed to pass through convex lens parallel to principal axis, the different colours of light converge at different point on the principle axis after refraction. This is called

[Main 24<sup>th</sup> Jan 2<sup>nd</sup> Shift 2023]

- 1 scattering
- 2 chromatic aberration
- 3 spherical aberration
- 4 polarisation

[Ans: 2]

## Question 51



The power of a lens (biconvex) is  $1.25 \text{ m}^{-1}$  in particular medium. Refractive index of the lens is 1.5 and radii of curvature are 20 cm and 40 cm respectively. The refractive index of surrounding medium

[Main 28<sup>th</sup> July 2<sup>nd</sup> Shift 2022]

1 1.0

$$P_L = 1.25 \quad D = \frac{100}{f(\text{cm})}$$

$$\frac{1}{f} = \left( \frac{\mu_L - 1}{\mu_S} \right) \left[ \frac{1}{R_1} - \frac{1}{R_2} \right]$$

2  $\frac{9}{7}$

$$\mu_L = 1.5$$

3  $\frac{3}{2}$

$$R_1 = 20$$

$$R_2 = 40 \text{ cm}$$

4  $\frac{4}{3}$

[Ans: 2]

## Question 52



A convex lens has power P. It is cut into two halves along its principal axis. Further one piece (out of the two halves) is cut into two halves perpendicular to the principal axis (as shown in figure). Choose the incorrect option for the reported pieces.

1 Power of  $L_1 = \frac{P}{2}$



[Main 27<sup>th</sup> June 2<sup>nd</sup> Shift 2022]

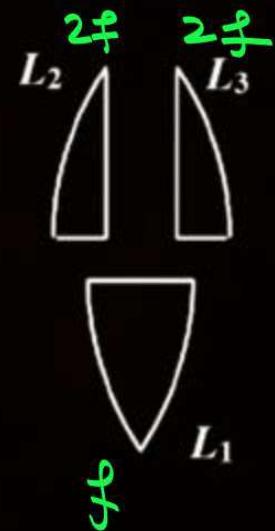
2 Power of  $L_2 = \frac{P}{2}$



3 Power of  $L_3 = \frac{P}{2}$



4 Power of  $L_1 = P$



[Ans: 1]

## Question 53



Find the distance of the image from object O, formed by the combination of lenses in the figure.

[Main 27<sup>th</sup> Aug 1<sup>st</sup> Shift 2021]

**1** 75cm *Ans*

$$\frac{1}{f} = \frac{1}{v} - \frac{1}{u}$$

$$\frac{1}{+10} = \frac{1}{v} - \frac{1}{-30}$$

$$\frac{1}{10} - \frac{1}{30} = \frac{1}{v}$$

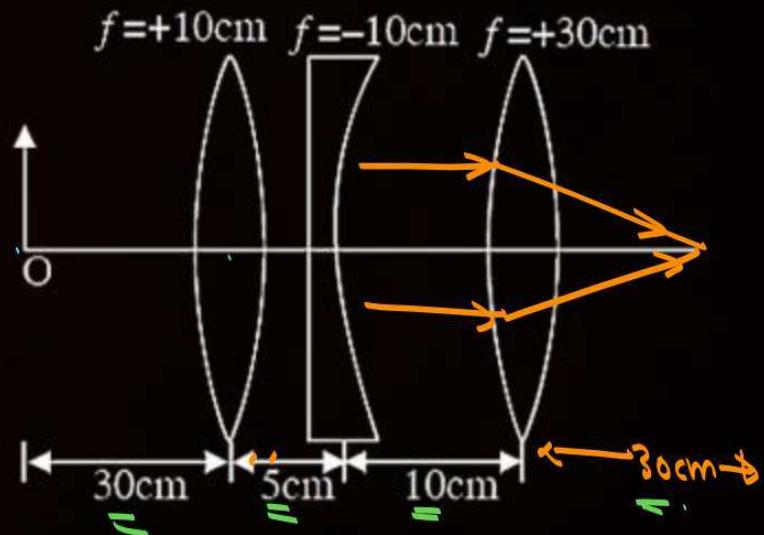
$$\frac{3-1}{30} = \frac{1}{v}$$

$$v = +15$$

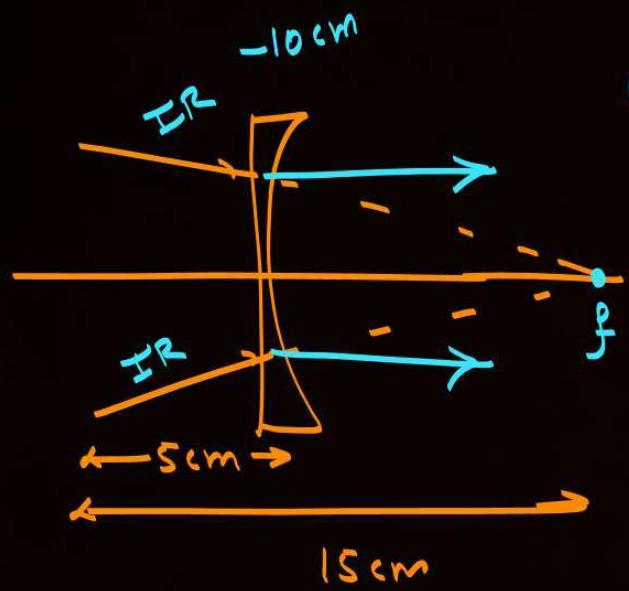
**2** 10 cm

**3** infinity

**4** 20 cm



[Ans: 1]



I

$$u = +10 \text{ cm}$$

$$\frac{1}{f} = \frac{1}{v} - \frac{1}{u}$$

$$-\frac{1}{15} = \frac{1}{v} - \frac{1}{+10}$$

$$v = \infty$$

## Question 54

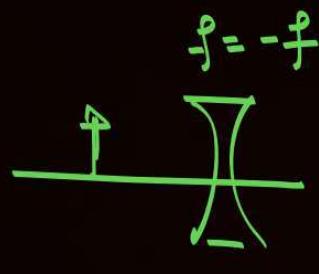
HW

P  
W

An object is placed at the focus of concave lens having focal length  $f$ . What is the magnification and distance of the image from the optical centre of the lens?

[Main 31<sup>th</sup> Aug 1<sup>st</sup> Shift 2021]

1  $\frac{1}{4}, \frac{f}{4}$



2  $\frac{1}{2}, \frac{f}{2}$

3 Very high,  $\infty$

4 1,  $\infty$

[Ans: B]

## Question 55



The refractive index of a converging lens is 1.4. What will be the focal length of this lens if it is placed in a medium of same refractive index? Assume the radii of curvature of the faces of lens are  $R_1$  and  $R_2$  respectively.

[Main 16<sup>th</sup> March 2<sup>nd</sup> Shift 2021]

1 Zero

$$\mu_L = \mu_S$$

$$f = \infty$$

2  $\frac{R_1 R_2}{R_1 - R_2}$

3 1

4 Infinite

[Ans: D]

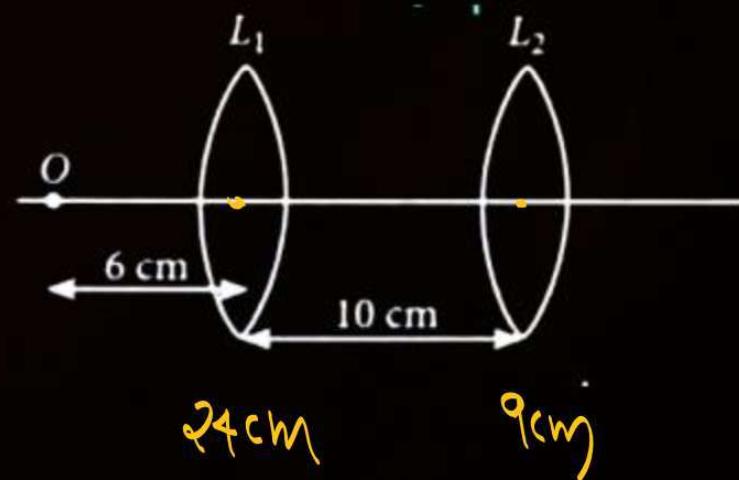
## Question 56

HQ

P  
W

A point object, 'O' is placed in front of two thin symmetrical coaxial convex lenses  $L_1$  and  $L_2$  with focal length 24 cm and 9 cm respectively. The distance between two lenses is 10 cm and the object is placed 6 cm away from lens  $L_1$  as shown in the figure. The distance between the object and the image formed by the system of two lenses is \_\_\_\_\_ cm.

[Main 10<sup>th</sup> April 2<sup>nd</sup> Shift 2023]



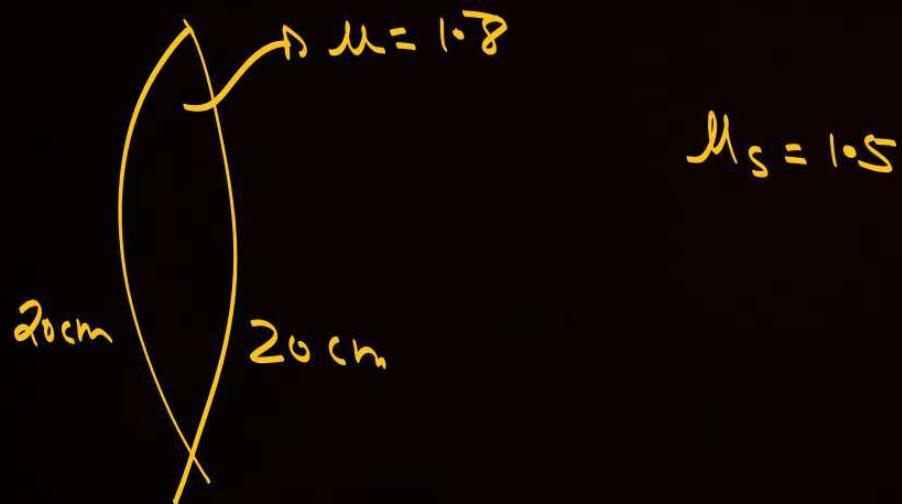
[Ans: 34]

### Question 57



The radius of curvature of each surface of a convex lens having refractive index 1.8 is 20 cm. The lens is now immersed in a liquid of refractive index 1.5. The ratio of power of lens in air to its power in the liquid will be  $x : 1$ . The value of  $x$  is \_\_\_\_\_.

[Main 11<sup>th</sup> April 1<sup>st</sup> Shift 2023]



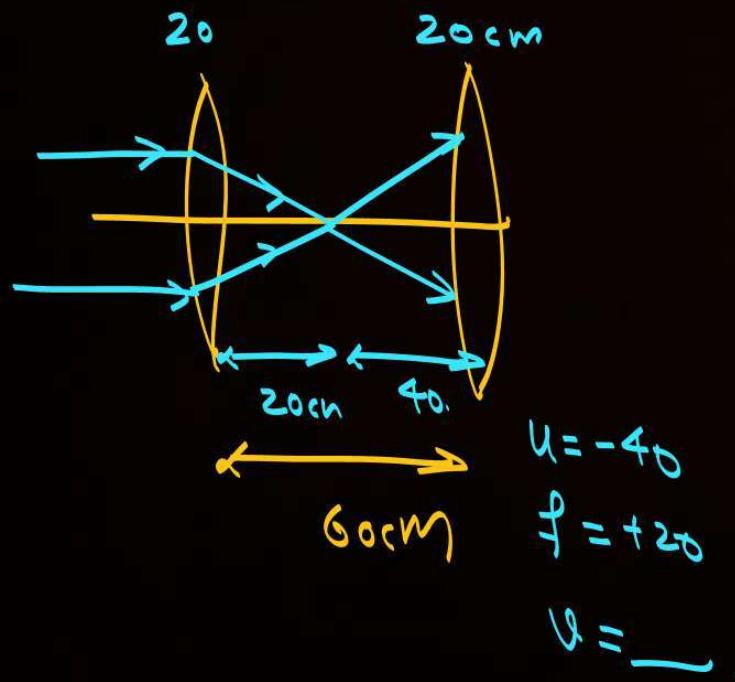
[Ans: 4]

## Question 58



Two convex lenses of focal length 20 cm each are placed coaxially with a separation of 60 cm between them. The image of the distant object formed by the combination is at \_\_\_\_\_ cm from the first lens.

[Main 12<sup>th</sup> April 1<sup>st</sup> Shift 2023]



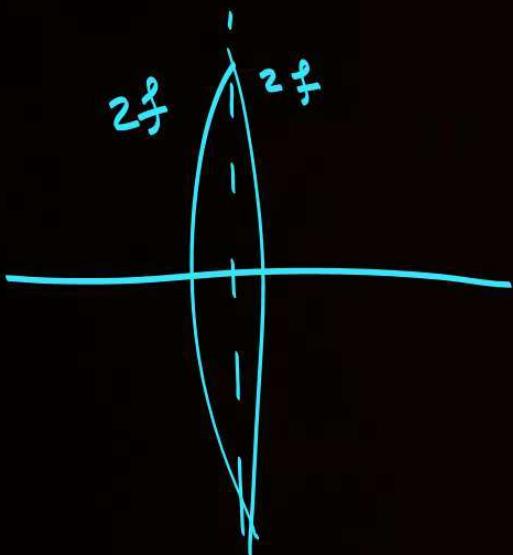
[Ans: 100]

### Question 59



A bi convex lens of focal length 10 cm is cut in two identical parts along a plane perpendicular to the principal axis. The power of each lens after cut is \_\_\_\_ D.

[Main 13<sup>th</sup> April 2<sup>nd</sup> Shift 2023]



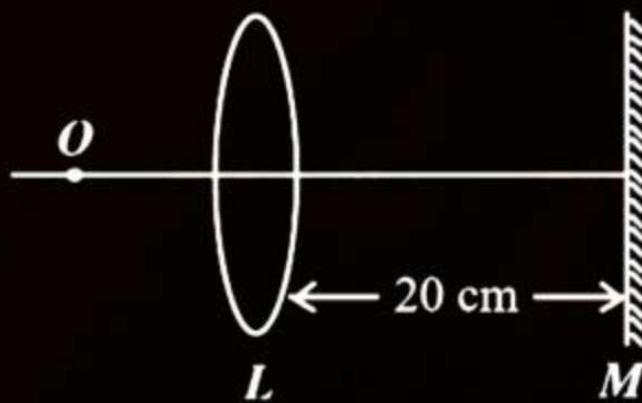
[Ans: 5]

## Question 60



An object is placed on the principal axis of convex lens of focal length 10 cm as shown. A plane mirror is placed on the other side of lens at a distance of 20 cm. The image produced by the plane mirror is 5 cm inside the mirror. The distance of the object from the lens is \_\_\_\_\_ cm.

[Main 25<sup>th</sup> Jan 2<sup>nd</sup> Shift 2023]



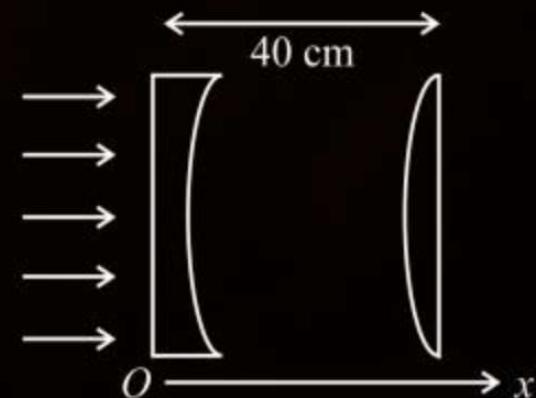
[Ans: 30]

## Question (Homework)



As shown in the figure, a combination of a thin plano concave lens and a thin plano convex lens is used to image an object placed at infinity. The radius of curvature of both the lenses is 30 cm and refraction index of the material for both the lenses is 1.75. Both the lenses are placed at distance of 40 cm from each other. Due to the combination, the image of the object is formed at distance  $x = \text{_____ cm}$ , from concave lens.

[Main 24<sup>th</sup> Jan 1<sup>st</sup> Shift 2023]



[Ans: 120]

## Question (Homework)



A convex lens of focal length 20 cm is placed in front of a convex mirror with principal axis coinciding each other. The distance between the lens and mirror is 10 cm. A point object is placed on principal axis at a distance of 60 cm from the convex lens. The image formed by combination coincides the object itself. The focal length of the convex mirror is \_\_\_\_\_ cm.

[Main 25<sup>th</sup> July 2<sup>nd</sup> Shift 2022]

[Ans: 10]

## Question (Homework)



For an object placed at a distance 2.4 m from a lens, a sharp focused image is observed on a screen placed at a distance 12 cm from the lens. A glass plate of refractive index 1.5 and thickness 1 cm is introduced between lens and screen such that the glass plate faces parallel to the screen. By what distance should the object be shifted so that a sharp focused image is observed again on the screen?

[Main 25<sup>th</sup> July 2<sup>nd</sup> Shift 2022]

1 0.8 m

2 3.2 m

3 1.2 m

4 5.6 m

[Ans: 2]

## Question (Homework)



Curved surfaces of a plano-convex lens of refractive index  $\mu_1$  and a plano-concave lens of refractive index  $\mu_2$  have equal radius of curvature as shown in figure. Find the ratio of radius of curvature to the focal length of the combined lenses.

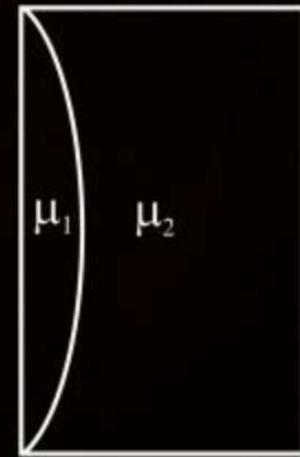
[Main 27<sup>th</sup> Aug 2<sup>nd</sup> Shift 2021]

1  $\frac{1}{\mu_2 - \mu_1}$

2  $\frac{1}{\mu_1 - \mu_2}$

3  $\mu_2 - \mu_1$

4  $\mu_1 - \mu_2$



[Ans: D]



## Homework



- ❖ Complete Homework Questions