Wave Motion

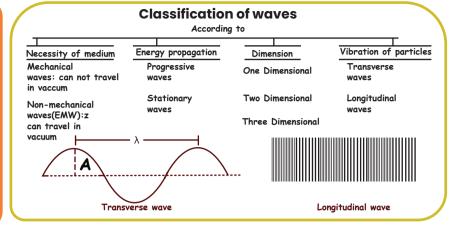
Waves

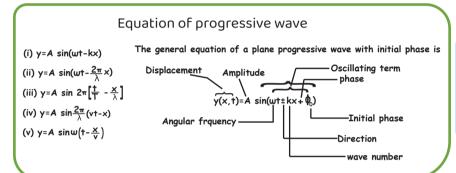
Wave is a disturbance which carries energy and momentum from one place to another without the transport of medium.

=> The medium should have elasticity and inertia

Characteristics of Wave

- The particles of the medium are executing simple harmonic motion.
- ⇒ The phase of vibration of the particle keeps on changing.
- > Wave carries energy and momentum.
- The velocity of the particle is not equal to velocity of wave.





Important Terms

A= Amplitude f= Frequency

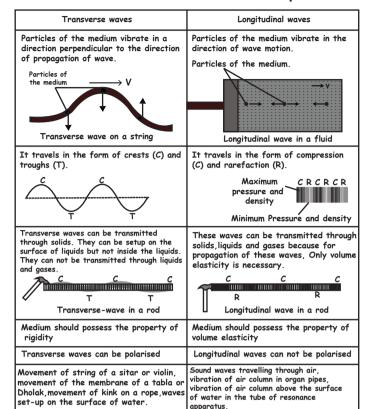
v= wave velocity

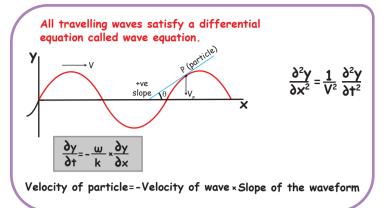
w= Angular frequency K=Wave number

 $\omega = \frac{2\pi}{T}$ or $2\pi f$

 $K = \frac{2\pi}{\lambda}$

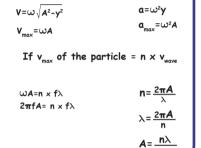
Classification of waves based on vibration of particles



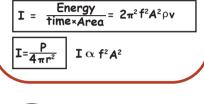


Acceleration

of particle



velocity of particle

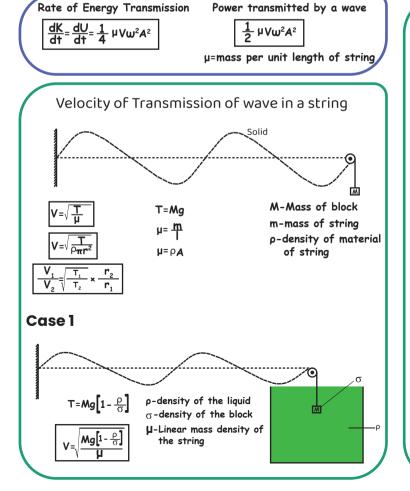


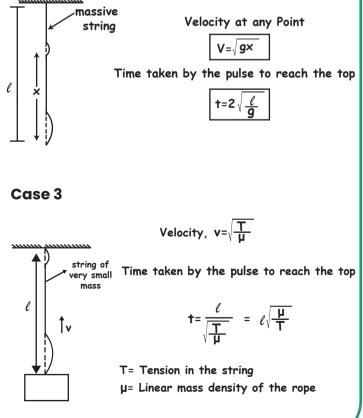
Intensity of wave

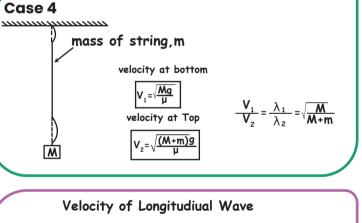


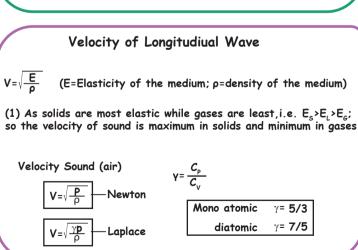
WAVES

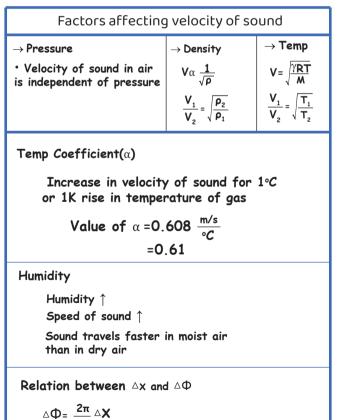
Case 2





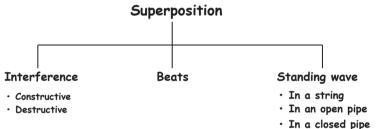






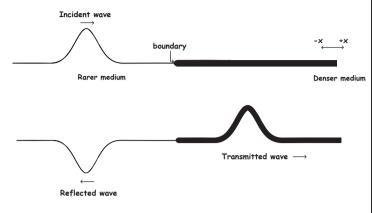
Principle of superposition

The displacement at any time due to number of waves meeting simulatoneously at a point in a medium is the vector sum of individual displacements due each one of the waves at that point at same time

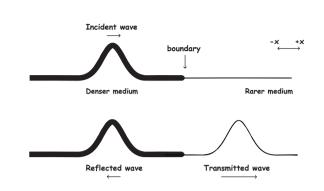


Waves on combination of strings

1) From rarer to denser medium



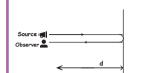
Incident wave $y_1 = a_1 \sin(\omega t - k_1 x)$ Reflected wave $y_r = a_r \sin(\omega t - k_1 (-x) + \pi)$ $= -a_r \sin(\omega t + k_1 x)$ Transmitted wave $y_s = a_s \sin(\omega t - k_2 x)$ 2) From rarer to denser medium



Incident wave $y_1 = a_1 \sin(\omega t - k_1 x)$

Reflected wave $y_r = a_r \sin(\omega t - k_1(-x) + 0)$ = $a_r \sin(\omega t + k_1 x)$ Transmitted wave $y_r = a_r \sin(\omega t - k_r x)$

Echo



Source at distance "d" from screen $t = \frac{d}{v} + \frac{d}{v} = \frac{2d}{v}$

Persistence of hearing for human ear is 0.1 sec

Conditions for echo: if $+ > 0.1 \Rightarrow \frac{2d}{} > 0.1 \Rightarrow d > -1$

if
$$t > 0.1 \Rightarrow \frac{2d}{V} > 0.1 \Rightarrow d > \frac{V}{20}$$

PHYSICS WALLAH

Interference of sound wave

Condition: -

- ·Two waves of same frequency, same wavelength, same velocity
- \cdot Resultant intensities will be different from the sum of intensities of each wave seperately
- ·This is due to the interference of waves

$$y_1 = a_1 \sin \omega t$$
, $y_2 = a_2 \sin(\omega t + \phi)$

φ-Phase difference between two waves

$$\vec{y} = \vec{y}_1 + \vec{y}_2 \Rightarrow y = A \sin(\omega t + \theta)$$

$$A = \sqrt{a_1^2 + a_2^2 + 2a_1a_2\cos\phi}$$

$$tan\theta = \frac{a_2 sin\phi}{a_1 + a_2 cos\phi}$$

Intensity ∞ A^2

$$A^2 = a_1^2 + a_2^2 + 2a_1a_2 \cos \phi$$

 $I = I_1 + I_2 + 2\sqrt{I_1 I_2} \cos \Phi$

$\frac{\overline{I}_{1}}{\overline{I}_{2}} = \left(\frac{a_{1}}{a_{2}}\right)^{2} \cdot \frac{\overline{I}_{max}}{\overline{I}_{min}} = \frac{(a_{1} + a_{2})^{2}}{(a_{1} - a_{2})^{2}} = \frac{(\overline{I}_{1} + \overline{I}_{2})^{2}}{(\overline{I}_{1} - \overline{I}_{2})^{2}}$

i) For Constructive interference:-

$$\Phi$$
 = 0, 2π , 4π , ---, OR Φ =2n π ; where n = 0, 1, 2, --- Δ x=0, λ , 2λ , --- , OR Δ x= n λ ; where n= 0, 1, 2,---

$$\mathbf{I}_{\text{max}} = \mathbf{I}_1 + \mathbf{I}_2 + 2\sqrt{\mathbf{I}_1\mathbf{I}_2}$$
$$= (\sqrt{\mathbf{I}}_1 + \sqrt{\mathbf{I}}_2)^2 \propto (\mathbf{A}_1 + \mathbf{A}_2)^2$$

ii) For Destructive interference:-

$$\phi = \pi$$
, 3π , 5π , --- OR $\Phi = (2n-1)\pi$; where $n=1,2,3,---$

$$\triangle x = \frac{\lambda}{2}, \frac{3\lambda}{2}, \dots = OR \triangle x = (2n-1)\frac{\lambda}{2}; \text{ where, n=1,2,3,----}$$

$$I_{\min} = I_1 + I_2 - 2\sqrt{I_1 I_2}$$

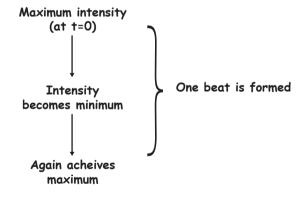
$$\Longrightarrow$$
 $\mathbf{I}_{\min} = (\sqrt{\mathbf{I}_1} - \sqrt{\mathbf{I}_2})^2 \propto (\mathbf{A}_1 - \mathbf{A}_2)^2$

Beats:-

- sound waves travelling in same medium with slightly different frequencies superimpose on each other.
- The intensity of resultant sound at particular position rises and falls regularly with time.
- The phenomenon of variation of intensity of sound with time at a particular position is called beats.

Point to remember: -

1) One beat:-



Beat period:-

Time interval between two sucessive beats (ie.two sucessive maximum of sound) is called beat period.

Beat frequency:-

No. of beats produced per second

Beat frequency:- n=|n₁-n₂|

Beat period: -T =
$$\frac{1}{\text{Beat frequency}} = \frac{1}{|n_1 - n_2|}$$

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Determination of Unknown Frequency

Let n_2 is the unknown frequency of tuning fork B, and this tuning fork B produce x beats per second with another tuning fork of known frequency n₁.

As number of beat/sec is equal to the difference in frequencies of two sources, therefore n2 = n1 \pm x

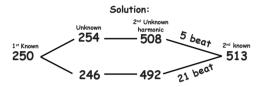
By waxing	By filing
If B is loaded with wax, its frequency decreases	If B is filed, its frequency increases

Q) A source of unknown frequency produces 4 beats/s when sounded with a source of known frequency 250 Hz. The second harmonic of the source of unknown frequency gives 5 beat/s when sounded with a source of frequency 513 Hz. The unknown frequency is?

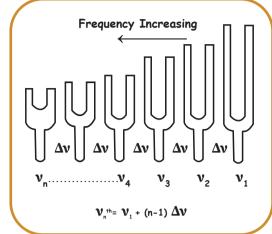
a) 254 Hz

b) 246 Hz c) 240 Hz

d) 260 Hz

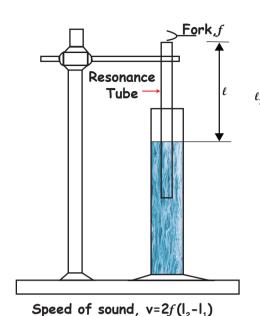


Hence unknown frequency is 254 Hz

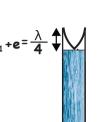


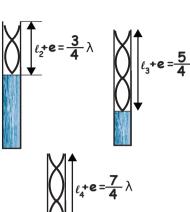


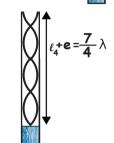
Resonance tube experiment



End correction: $e=\frac{1}{2}\left(\ell_2-3\ell_1\right)$

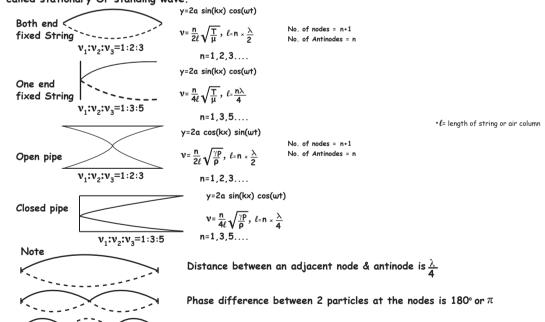






Standing Waves:

·When two progressive waves (both longitudinal and transverse) having same amplitude, time period, frequency moving along a straight line in opposite direction superpose, a new wave is formed. It is called stationary Or standing wave.



Both end fixed string/open pipe	One end fixed string/closed pipe		
n=1⇒ Fundamental frequency / 1 st harmonic n=2⇒ First overtone/ 2 nd harmonic n=3⇒ Second overtone / 3 rd harmonic	n=1⇒ Fundamental frequency / 1 st harmonic n=3⇒ First overtone/ 2 nd harmonic n=5⇒ Second overtone / 3 rd harmonic		

Strain and pressure is maximum at node and minimum at antinode

Octave: The tone whose frequency is double the fundamental frequency is called as Octave. (i) If $n_2 = 2n_1$, it means n_2 is an octave higher than n_1 or n_1 is an octave lower than n_2 .

(ii) If n₂ = 2³n₁, it means n₁ is 3-octave higher than n₂ or n₁ is 3-octave lower than n₂

(iii) Similarly if $n_2 = 2^n n_1$, it means n_2 is n-octave higher than n_1 or n_1 is n octave lower.

Unison: If the two frequencies are equal then vibrating bodies are said to be in unison.

Resonance: The phenomenon of making a body vibrate with it's natural frequency under the influence of another vibrating body having same frequency is called resonance.

Comparative Study of Stretched Strings, Open Organ Pipe and Closed Organ Pipe

5 . NO	Parameter	Stretched string		Open organ pipe	Closed organ pipe
1	Fundamental frequency or 1st harmonic	Both ends fixed $n_1 = \frac{v}{2l}$	one ends fixed $n_1 = \frac{v}{4l}$	$n_1 = \frac{v}{2l}$	n ₁ =
2	Frequency of or 2 nd harmonic	n ₂ = 2n ₁ 1 st overtone	n ₂ = 3n ₁ 1 st overtone	n ₂ = 2n ₁ 1 st overtone	n ₂ = 3n ₁ 1 st overtone
3	Frequency of or 3 rd harmonic	n ₃ = 3n ₁ 2 nd overtone	n ₃ = 5n ₁ 2 nd overtone	n ₃ = 3n ₁ 2 nd overtone	n ₃ = 5n ₁ 2 nd overtone
4	Frequency ratio of overtones	2:3:4	3:5:7	2:3:4	3:5:7
5	Frequency ratio of harmonics	1:2:3:4	1:3:5:7	1:2:3:4	1:3:5:7
6	Nature of waves	Transverse stationary	Transverse stationary	Longitudinal stationary	Longitudinal stationary

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Relation between loudness and intensity

 $L \propto \log_{10}$ (Intensity) unit(dB) unit W/m2

 $I_0 = 10^{-12} \text{W/m}^2$

 $dB=10 \times log_{10} \frac{I}{T}$

I_=Threshold intensity

 $L_2 = 10 \times \log_{10} \frac{I_2}{I_2} \qquad I_2 \longrightarrow L_2$

 $\triangle L = 10 \log \left(\frac{I_2}{T} \right)$

Doppler Effect

Whenever there is a relative motion between a source of sound and the listener, the apparent frequency of sound heard by the listener is different from the actual frequency of sound emitted by the source.

General equation (when both source & listener are moving)

$$v^{l} = \left(\frac{V \pm V_{L}}{V \mp V_{S}}\right) v \qquad \qquad b \downarrow \qquad b \downarrow$$

Case 1 (listener is stationary & source is approaching the listener)

$$v^{l} = \left(\frac{V}{V - V_{s}}\right)v$$

Case 2 (The source is stationary & listener is approaching the source)

Case 3 (source & listener are approaching each other)

$$V_{L}$$
 V_{S}

$$v^{\dagger} = \left(\frac{V + V_{L}}{V - V_{s}} \right)$$

Case 4

(source is stationary, listener is moving away from the source)

$$v^{I} = \left(\frac{V - V_{L}}{V}\right)v$$

Case 5

(source is moving away from the listener, listener is stationary)

$$v^{l} = \left(\frac{V}{V + V_{s}}\right)v$$

Case 6

(source and listener moving in same direction)

Case 7 (source and listener moving away from each other)

$$v^{l} = \left(\frac{V - V_{L}}{V + V_{s}}\right) v$$

Case 8 (source approaching a stationary wall)

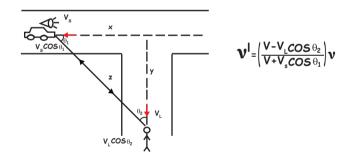


$$v^{l} = \frac{V + V_s}{V - V_s} v$$

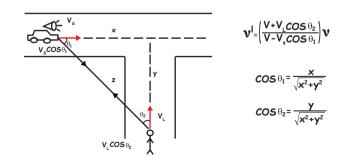
Case 9 (source is moving away from stationary wall)

$$V_s$$
 $V-V_s$

Case 10



Case 11



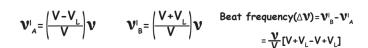


Note:



$$\mathbf{v}_{A} = \left(\frac{\mathbf{V} - \mathbf{V}_{L}}{\mathbf{V}}\right)\mathbf{v}$$

$$\mathbf{v}_{B}^{I} = \left(\frac{\mathbf{V} + \mathbf{V}_{L}}{\mathbf{V}}\right) \mathbf{v}$$
 Be



$$\Delta v = \frac{2V_L v}{V}$$

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