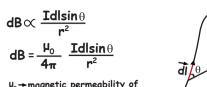
Biot-Savart's Law



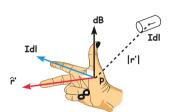
 $\mu_0 \rightarrow$ magnetic permeability of free space or vaccum $\mu_0 = 4\pi \times 10^{-7}$

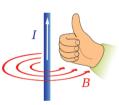
In vector form

$$\overrightarrow{dB} = \frac{\mu_0}{4\pi} I \frac{\overrightarrow{dl} \times r}{r^3}$$

 $d\overline{B}$ is perpendicular to both $d\overline{l}$ and \overline{r} . BY using right hand screw rule we can find direction of magnetic field

Here, B is into the plane





Magnetic field circulates around the current carrying wire

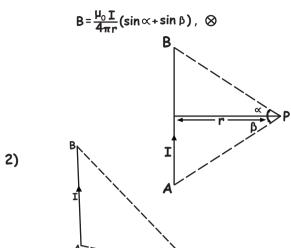
MOVING **CHARGES MAGNETISM**



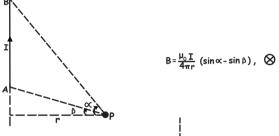
Formula of Field due to straight wire

1) At point P

B is into the plane



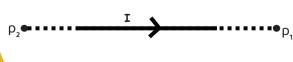
Extend AB downwards and draw a perpendicular from P



3) Wire of infinite length \propto =90 and β =90 ∝=90°_ r β=90° $B = \frac{\mu_0 I}{4\pi r}$ (sin 90 + sin 90)

4) Wire of semi infinite length

$$B = \frac{\mu_0 I}{4\pi r} \text{ (sin90+sin0)}$$
$$= \frac{\mu_0 I}{4\pi r}$$

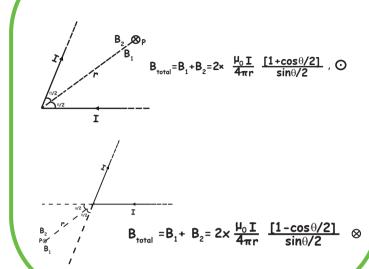


∝=**90**°

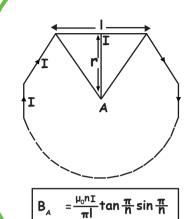
 $B(P_1) = B(P_2) = 0$



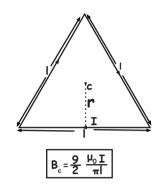
Field Due to bent wire



Field due to polygon

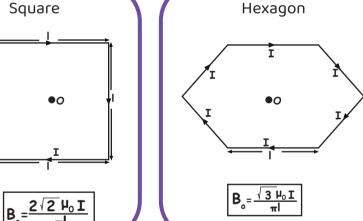


eg: equilateral triangle

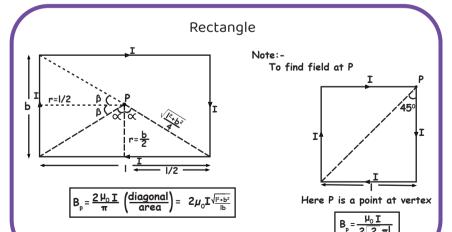


If a total lenght I is bent as an equilateral

$$B' = \frac{27}{2} \frac{\mu_0 I}{\pi l}$$

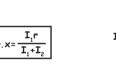


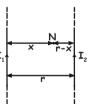
Hexagon $B_o = \frac{\sqrt{3} \mu_o I}{\pi I}$



Neutral Points

Points at which magnetic field becomes zero are called neutral points. Case 1: Parallel wires carrying current in same direction (I,>I₂)



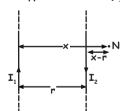


If y is the distance from 2nd conductor then

$$y = \frac{I_2 r}{I + I}$$

Case 2: Parallel wires carrying currents in opposite direction (I, >I,)

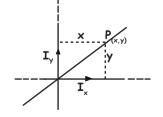




Case 3: Wires perpendicular to each other

Field wll be zero on all points of the line OP

Comparing with y=mx+C we get.



Wire perpendicular to plane

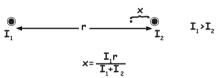
- 1) Current directed out of plane
 - ●I)B is in anticlockwise direction
- 2) Current directed into the plane



Direction of field

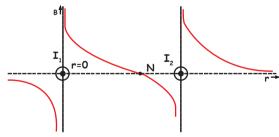
- 2) B-AntiClockwise

Neutral Point

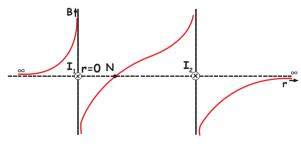


Graphs

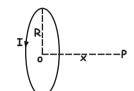
1) I out of the plane, I, > I,



2) I into the plane $[I_1 < I_2]$



Field due to a circular ring & Field at the axis of a ring



$$B_p = \frac{\mu_0 I R^2}{2(x^2 + R^2)^{3/2}}$$

Every current carrying loop acts as a magnetic dipole

Direction of A is determined using right hand thumb rule

Here, $M=IA \implies M=I\pi R^2$

$$B = \frac{\mu_0}{4\pi} \frac{2M}{(x^2 + R^2)^{3/2}}$$

If current is flowing in anticlockwise direction



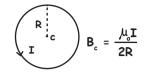
If current is flowing in clockwise direction



Magnetic field lines for a current loop

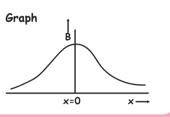
If there are N loops, B=

Field at the centre of ring



Field at the axis in terms of field at center

$$B_{axis} = \frac{B_c}{\left(1 + \frac{x^2}{R^2}\right)^{3/2}}$$



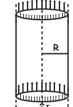
Percentage change in field with respect to centre

for the points on the axis

% change in B = 1-(1+ \times^2/R^2) × 100%

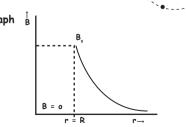
For change < 10% = $\left(\frac{3}{2} \times \frac{x^2}{R^2}\right) \times 100\%$

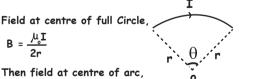
Hollow cylinder (pipe)





Inside : r < R





PHYSICS

WALLAH

Field at the Centre due to circular arc

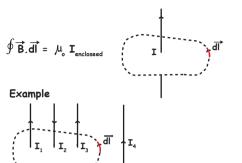
Then field at centre of arc,

where, θ is in radian

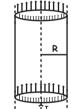
Example

Ampere's Cicutal Law

The line integral of magnetic field over a closed loop is equal to μ_o times the total current enclosed by the loop



$\oint \overrightarrow{B} \cdot \overrightarrow{dl} = \mu_0 \left[I_1 - I_2 + I_3 \right]$

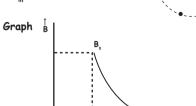


Outside : r > R



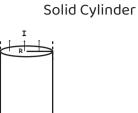
On the surface : r = R





CHARGES AND **MAGNETISM**





Outside : r > R



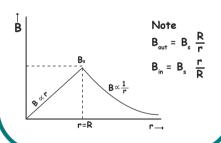


On the surface r = R

$$B_s = \frac{\mu_o I}{2\pi R}$$

Inside (r < R)





MOVING

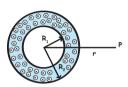


Annular pipe



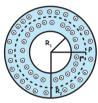


· Outside (r > R2)



$$B_{out} = \frac{\mu_o I}{2\pi r}$$

· In between R₁ < r < R₂

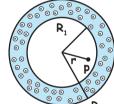


$$I_{enc} = \frac{I}{\pi (R_2^2 - R_1^2)} \times \pi (r^2 - R_1^2)$$

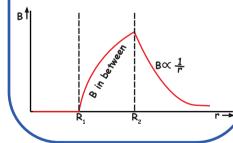
$$B_{btw} = \frac{\mu_o}{2\pi r} \times I \frac{(r^2 - R_1^2)}{(R_2^2 - R_2^2)}$$

Inside

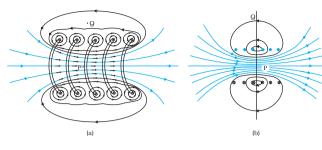
r<R₁ B₁=0

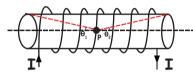


Graph



Solenoid





$$B_{p} = \frac{1}{2} \mu_{0} n I (\cos \theta_{1} + \cos \theta_{2})$$

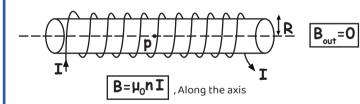
where $n \longrightarrow no.of$ turns per unit length

Tightly packed long solenoid

Long solenoid: Radius is small compared to the length of the solenoid

For a long solenoid the middle region will have a uniform magnetic field

1) At centre



2) End point

$$\theta_1 = 0$$
 $\theta_2 = 90^{\circ}$

$$B_{end} = \frac{1}{2} \mu_0 n I = \frac{B_{axis}}{2}$$

Charged particle in magnetic field

Magnetic Force on particle $\overrightarrow{F}_{n} = q(\overrightarrow{vxB})$

Case V⊥B Path: Circle

Radius of circular path

i)
$$F_m = \frac{mv^2}{r}$$

$$\Rightarrow qvB = \frac{mv^2}{r}$$

$$\Rightarrow r = \frac{mv}{qB}$$

ii) Momentum

p= mv=√2mk

$$\Rightarrow$$
 r= $\frac{\sqrt{2mk}}{qB}$

If charged particle at rest is accelerated by a voltage of 'V' volt then,

$$r = \frac{\sqrt{2mqV}}{qB}$$

If $K_i \neq 0$, then $K_f = qV + K_i$

$$r = \frac{\sqrt{2mK}}{qB} = \frac{\sqrt{2m(qV + K_i)}}{qB}$$

Time Period

$$T = \frac{2\pi m}{aB}$$

⇒ T∝r°
T∝v°

We have $\frac{q}{m}$ = specific charge

$$\Rightarrow \mathsf{T} \propto \frac{1}{\mathsf{specific charge}}$$

MOVING CHARGES AND MAGNETISM

Calculation of ratio of radii

1) All particles are projected with same speed:

V=Constant

$$r = \frac{mv}{qB} \Rightarrow r \propto \frac{m}{q}$$

$$r_{p} : r_{d} : r_{c} = \frac{1}{e} : \frac{2}{e} : \frac{4}{2e} = 1:2:2$$

2) All particles are projected with same momentum

$$r = \frac{p}{qB} \Rightarrow r \propto \frac{1}{q}$$

$$r_{p} : r_{d} : r_{\infty} = \frac{1}{e} : \frac{1}{e} : \frac{1}{2e} = 2:2:1$$

As radius ↑ Curvature ↓

3) All particles are projected with same kinetic energy

$$r = \frac{mv}{qB} = \frac{\sqrt{2mk}}{qB}$$

$$\Rightarrow r \propto \frac{\sqrt{m}}{q}$$

$$r_{p} : r_{d} : r_{x} = \frac{\sqrt{1}}{e} : \frac{\sqrt{2}}{e} : \frac{\sqrt{4}}{2e}$$

$$1 : \sqrt{2} : 1$$

4) All particles are projected by same accelerating potential

$$r = \frac{\sqrt{2mqV}}{qB} \implies r \propto \sqrt{\frac{m}{q}}$$

$$r_{p} : r_{d} : r_{\alpha} = \sqrt{\frac{1}{e}} : \sqrt{\frac{2}{e}} : \sqrt{\frac{4}{2e}} = 1 : \sqrt{2} : \sqrt{2}$$

Helical path & pitch

 \vec{V} makes angle θ with \vec{B} ($\theta \neq 0, \pi, \pi/2$)

Path of charge is Helical

$$\overrightarrow{V} < \overrightarrow{V}_{\parallel} \rightarrow \parallel \text{ to } \overrightarrow{B}$$

1) Radius

$$R = \frac{mv_{\perp}}{qB}$$

$$R = \frac{mvsin\theta}{qB} = \frac{\sqrt{2mqV}}{qB} sin\theta$$

2) Time period

$$T = \frac{2\pi m}{qB}$$

3) Pitch $=V_{\parallel} \times T$

$$=V\cos\theta\times\frac{2\pi m}{qB}$$

$$=2\pi\left(\frac{mv}{qB}\right)Cos\theta$$

$$=2\pi \frac{\sqrt{2mK}}{qB} \cos \theta$$

$$=2\pi \frac{\sqrt{2mqV}}{qB} \cos\theta$$



Toroid

r is the mean radius



D_{out} = U

$$\bm{B}_{\text{in between}} = \; \mu_0 \bm{n} \bm{I}$$

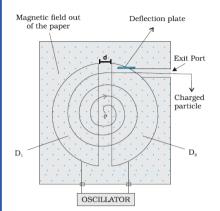
unit and dimension of B

F=qvBsinθ

$$B = \frac{F}{qvsin\theta}$$

[B] =
$$\frac{MLT^{-2}}{AT \times LT^{-1}} = MA^{-1}T^{-2}$$

Cyclotron



1) Maximum kinetic energy

$$K_{\text{max}} = \frac{q^2 B^2 R^2_{\text{dee}}}{2m}$$

2) Number of oscillations ,N

Work done=∆K

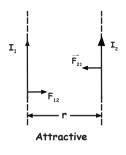
$$NxqEd = \frac{q^2B^2R^2}{2m}$$

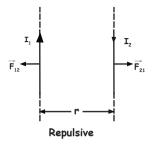
E is in the plane of the dees

- 3) Time period of revolution= $\frac{2\pi i}{aR}$
- 4) Cyclotron frequency $v_c = \frac{qB}{2\pi m}$

Force between parallel conductors

1) Force between two long parallel current conductors



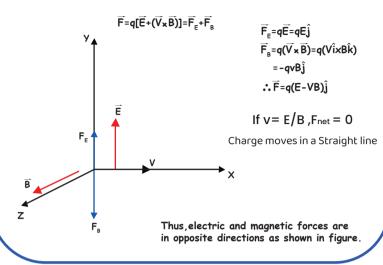


Parallel currents attract each other. Anti parallel currents repel each other. Force per unit length of conductor

$$F_{12} = F_{21} = \frac{\mu_0}{2\pi} - \frac{I_1I_2}{r}$$

Net force on 'l' length of conductor= $\frac{\mu_0}{4\pi} = \frac{2I_1I_2}{r} \times I$

Motion of charged particle in Crossed Electric and Magnetic field (B) velocity selector



MOVING **CHARGES** AND **MAGNETISM**

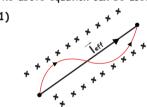


Force on current carrying Conductor in magnetic field

consider a small element dT of the conductor

| → . → → | | | | | |
|--|---|---|-----|-----|---|
| dF=I(dl×B) | × | × | × | × | × |
| To find resulting force | × | × | | ı × | × |
| ∫dF=∫I(di×B) | × | × | I × | × | × |
| =I∫dİ×B In uniform field | × | × | 1 × | × | × |
| $\vec{F} = \vec{I} (\int \vec{d}) \times \vec{B} = \vec{I} (\vec{I} \times \vec{B})$ | × | × | × | × | × |

The above equation can be used in the following situations



2) \vec{l}_{eff} perpendicular to \vec{B}

$$\theta = 90$$

$$F_{max} = I_{eff}B$$

For closed Loop in uniform field

Here,
$$I_{eff} = 0$$

 $\therefore \vec{F} = 0$



Lorentz force

A charge q in an electric field \overrightarrow{E} experiences the electric force

The magnetic force experienced by the charge q moving with velocity \overrightarrow{V} in the magnetic field \overrightarrow{B}

$$\vec{F} = q(\vec{V} \times \vec{B})$$

The total force, or the Lorentz force, experienced by the charge q due to both electric and magnetic field is given by

$$\vec{F} = q[\vec{E} + (\vec{V} \times \vec{B})]$$

 τ = NIABsin θ

Sensitivity of a Galvanometer

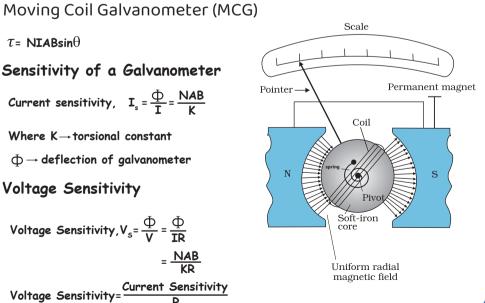
Current sensitivity,
$$I_s = \frac{\Phi}{I} = \frac{NAB}{K}$$

Where $K \rightarrow torsional$ constant $\Phi \rightarrow$ deflection of galvanometer

Voltage Sensitivity

Voltage Sensitivity,
$$V_s = \frac{\Phi}{V} = \frac{\Phi}{IR}$$

Voltage Sensitivity= Current Sensitivity



Magnetic dipole moment of a revolving electron

T is the time period of revolution

$$T = \frac{2\pi r}{V}$$

$$\tau_{-} eV$$



There will be a magnetic moment, usually denoted by μ associated with this circulating current

$$\mu = I \pi r^2 = \frac{eVr}{2}$$

$$\mu = \frac{e}{2m_e} (m_e vr) = \frac{e}{2m_e} L \qquad \overline{L} = \overrightarrow{r} \times \overline{P}$$
= rmvsin

In vector form

$$\overline{\mu} = \frac{-e}{2m} \overline{L}$$

The negative sign indicates that the angular momentum of the electron is opposite in direction to the magnetic moment

The ratio of magnetic moment to the angular momentum is called gyromagnetic ratio

$$\frac{\mu}{L} = \frac{e}{2m_e}$$

Its value is a constant and is equal to 8.8×10¹⁰ C/kg

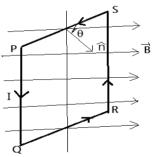
According to Bohr's quantization condition, angular momentum assumes a discrete set of values, namely.

$$L = \frac{nh}{2\pi} \text{ where } n=1, 2, 3..... \\ h \rightarrow \text{planck's constant}$$

$$\mu_{\text{min}} = \frac{e}{4\pi \, \text{m}_a} \, \text{h} = 9.27 \times 10^{-24} \, \text{Am}^2$$

PHYSICS

Torque on a current loop in a uniform magnetic field



Then $\tau = NIABsin\theta$

Special cases:

i) When () = 0°

 \mathcal{T} =0 , ie, the torque is minimum when the plane of the loop is perpendicular to the magnetic field

ii) When = 90°

 τ = NIAB ie, the torque is maximum when the plane of the loop is parallel to the magnetic field. Thus,

 $T_{\text{max}} = \text{NIAB}$

Note:

1) The constant, $\frac{K}{NAB}$ is called galvanometer constant or current reduction factor of the galvanometer.

2) Figure of merit of a galvanometer

$$G = \frac{\mathbf{I}}{\Phi} = \frac{K}{\mathsf{NAB}}$$