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Electrochemistry

Galvanic Cell

For a cell reaction in an electrochemical cell

$$Zn(s) + CuSO_4(aq) \Longrightarrow Cu(s) + ZnSO_4(aq)$$

Cell representation
$$\Rightarrow$$
 Zn | Zn²⁺(aq.) || Cu²⁺(aq.) |Cu Cathode(+)

For half cell reaction

$$M \to M^{n+}(aq.) + ne^{-}; E_{OX}^{o} = E_{M/M^{n+}}^{o}$$

$$M^{n+}(aq) + ne^{-} \rightarrow M; E^{o}_{red} = E^{o}_{M^{n+}/M}$$

Emf of cell,
$$E_{cell}^0 = E_{right}^0 - E_{left}^0 = E_{cathode}^0 - E_{anode}^0$$

(R.P. = Reduction potential)

* Oxidation potential for half cell reaction:

$$M \rightarrow M^{+n} + ne^{-}$$

$$E_{OX} = E_{OX}^{0} - \frac{2.303RT}{nE} log[M^{n+}]$$

* Reduction potential for half-cell reaction:

$$M^{n+} + ne^- \rightarrow M, \ E_{red} = E_{red}^0 + \frac{2.303 \, RT}{nF} log[M^{n+}]$$

Nernst's Equation

❖
$$\Delta G = -nFE_{cell} = -W$$

$$\Delta G = \Delta G^{\circ} + 2.303 \, RT \log O$$

$$\Delta G^{\circ} = -nFE_{cell}^{\circ}$$

$$E_{cell} = E_{cell}^{o} - \frac{2.303RT}{nF} log Q$$

 ΔG = Change in free energy

W = Useful work done

n = Number of electrons exchanged

F = Faraday constant (96500 coulomb)

Q = Reaction quotient

At room temperature (25°C)

⇒ Nernst's equation

$$\Rightarrow E_{cell} = E_{cell}^0 - \frac{0.0591}{n} \log Q$$

Concentration Cell

* For Electrode Concentration Cell

$$Pt \mid H_2(P_1) \mid H^+(cM) \parallel H^+(cM) \mid H_2(P_2) \mid Pt$$

$$E_{cell} = \frac{0.0591}{2} log \frac{P_1}{P_2}; (P = Pressure)$$

* For Electrolyte Concentration Cell

$$(Cu \mid \underset{anode(-)}{Cu^{2+}}(C_1) \parallel Cu^{2+} \underset{Cathode(+)}{(C_2)} \parallel Cu)$$

$$E_{cell} = \frac{0.0591}{2} log \frac{C_2}{C_1}$$

For concentration cells, $E_{cell}^0 = 0$

* At Equilibrium

$$E_{cell} = 0$$
 (as $\Delta G = 0$)

Thermodynamics for the Cell

* Temperature Coefficient (T.C.)

$$(T.C.) = \left(\frac{\partial E_{cell}}{\partial T}\right)_{0}$$

* Change in Entropy

$$\Delta S = nF \left(\frac{\partial E}{\partial T} \right)_n$$

* Relation Between E_{Cell} & (T.C.)

$$E_{cell} = \left(\frac{-\Delta H}{nF}\right) + T\left(\frac{\partial E}{\partial T}\right)_{p}$$

 $\{\Delta H = \text{Heat of cell reaction}\}\$

 $\left(\frac{\partial E}{\partial T}\right)_{n} > 0 \Rightarrow$ Cell reaction is endothermic and vice versa.

Quantitative Analysis

* Faraday's 1st Law of Electrolysis

m = 7I

m = mass of substance deposited

Z = electrochemical equivalent

I = current

t = time

$$Z = \frac{Atomic mass}{n \times F}$$

❖ Faraday's 2nd Law of Electrolysis (Q = constant)



$$\frac{\mathbf{m}_1}{\mathbf{m}_2} = \frac{\mathbf{E}_1}{\mathbf{E}_2}$$
 (E = equivalent weight)

Conductance

* Ohm's Law

$$V = RI$$

$$R = \rho \frac{\ell}{a}$$

V = Potential difference

R = Resistance

I = Current

 ρ = Specific resistance (resistivity)

 ℓ = length of conductor

a = cross-section area of conductor

* Conductance

$$G = \frac{1}{R}$$

* Specific Conductance (Conductivity)

$$\kappa = \frac{1}{\rho}$$

* Cell Constant

$$G^* = \frac{\ell}{a}$$

$$\kappa = G \times G^*$$

* Molar Conductance

$$\Lambda_{\rm m} = \frac{1000 \times \kappa}{\rm C(or\,M)}$$

{C = concentration of electrolyte in terms of molarity}

* Equivalent Conductance

$$\Lambda_{eq} = \frac{1000 \times \kappa}{N}$$

$${N = Normality}$$

$$\Lambda_{\rm eq} = \frac{\Lambda_{\rm M}}{(n - {\rm factor})}$$

$$\Lambda_0 = \lim_{C \to 0} \Lambda_C$$

 $\{\Lambda_0 = \text{equivalent conductance at infinite dilution}$ (or zero concentration) $\}$

* For Weak Electrolyte

$$\Lambda_{\rm C} \propto \frac{1}{\sqrt{C}}$$

For strong electrolyte, $\Lambda_{\rm C} = \Lambda_{\rm 0} - {\rm B(C)}^{\scriptscriptstyle 1/2}$ (B = constant)

* At Infinite Dilution, for an Electrolyte A_xB_y

$$A_x B_y \rightleftharpoons x A^{y+} + y B^{x-}$$

$$\Lambda^0_{A_x B_y} = x \lambda^0_{A^{y+}} + y \lambda^0_{B^{x-}}$$

 $\{\,\lambda_{A^{y_+}}^0,\,\lambda_{B^{x_-}}^0=\text{equivalent conductance at infinite dilution of cation and anion}\}$

* Ionic Mobility

$$\mu = \frac{Ionic \, Velocity}{Potential \, gradient}$$

Degree of Dissociation

* For a Weak Electrolyte

$$(CH_3COOH \rightleftharpoons CH_3COO^- + H^+)$$

$$\alpha = \frac{\Lambda_{\rm m}}{\Lambda_{\rm 0}}, \ K_{\rm a} = \frac{C(\Lambda_{\rm m}/\Lambda_{\rm 0})^2}{1-(\Lambda_{\rm m}/\Lambda_{\rm 0})}$$

Solubility Product

For solubility of salt $(AgCl(s) \rightleftharpoons Ag^{+}(aq) + Cl^{-}(aq))$

$$\mathbf{K}_{sp} = \left(\frac{1000\kappa}{\Lambda_0}\right)^2$$

