

# Automata

## Take Home Assignment

Index: 16001354

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### Question1

For M1:

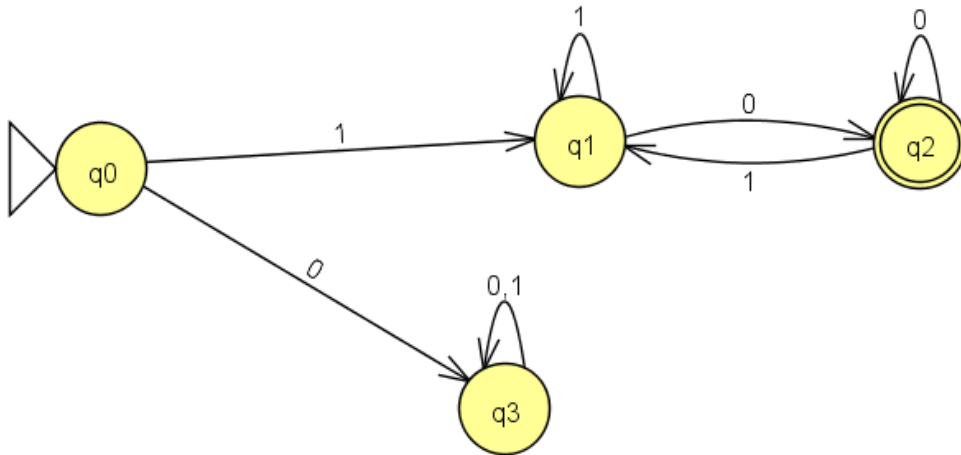
- a) Start state: q1
- b) Accept state: q2
- c)  $q1 \rightarrow q2 \rightarrow q3 \rightarrow q1 \rightarrow q1$
- d) No
- e) No

For M2:

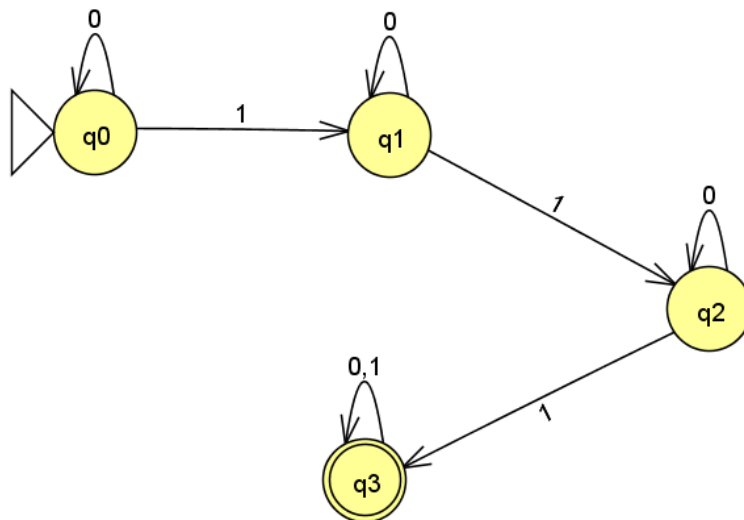
- a) Start state: q1
- b) Set of Accept states: {q1, q4}
- c)  $q1 \rightarrow q1 \rightarrow q2 \rightarrow q4$
- d) Yes
- e) Yes

Question2

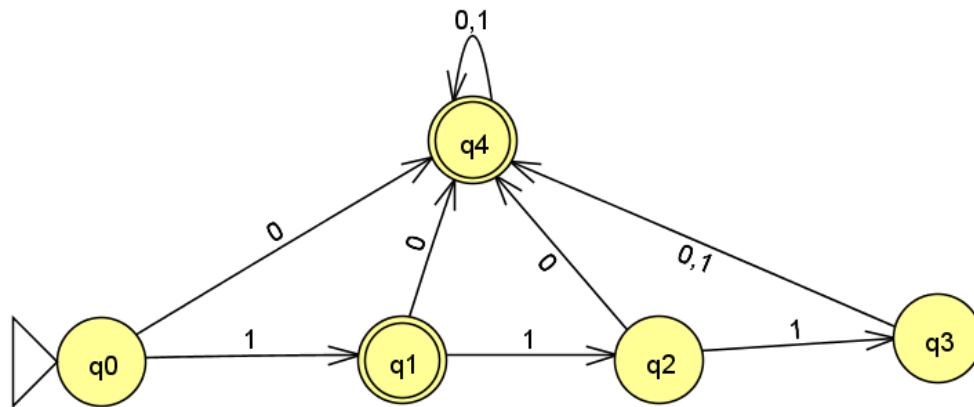
1.  $1(1)^* (1+0)^* 0(0)^*$

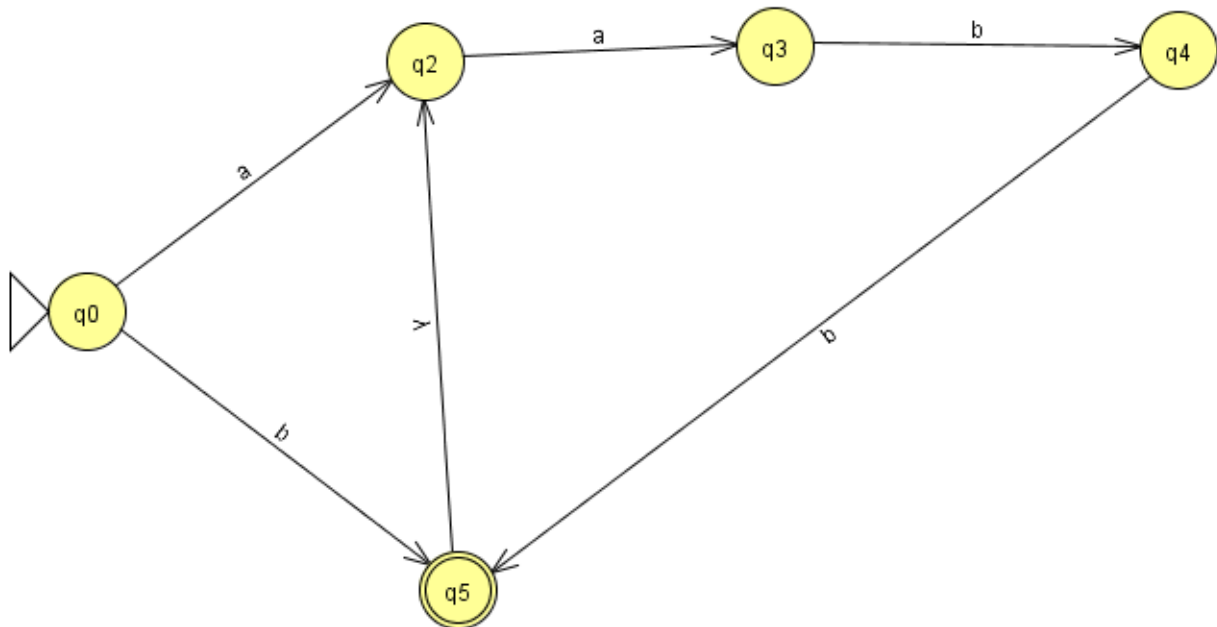
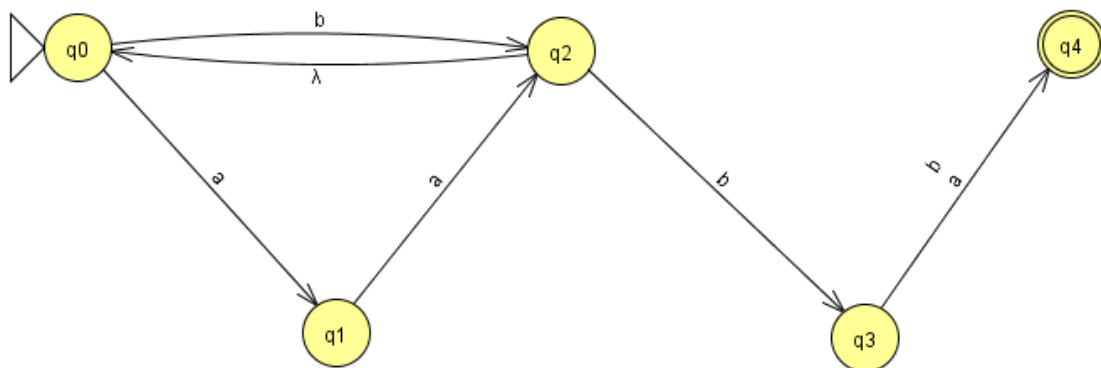


2)  $(0+1)^* 1(1)^* (0+1)^* 1(1)^* (0+1)^* 1(1)^* (0+1)^*$



3)  $0+(1(0+(1(0+(1(0+1)))))) (0+1)^*$



Question31)2)

Question 04question 4

$$L = \{0^m 1^m 2^m \mid m \geq 0\}.$$

assume  $L$  is regular.

Since  $L$  is infinite, we can use pumping Lemma.

let's take  $k$  as integer,

$$w = 0^k 1^k 2^k$$

$w \in L$ . Since  $w$  is regular  $0^k 1^k 2^k = xyz$

$$|xy| \leq k \quad |y| \geq 1.$$

$$xyz = 0^k 1^k 2^k$$

from pumping Lemma

$$xyz = \underbrace{0 \dots 0}_{x, |x| \leq k} \underbrace{0 \dots 0}_{y, |y| \leq k} \underbrace{1 \dots 1}_{z, |z| \leq k} \underbrace{2 \dots 2}_{k}$$

$$yz = 0^c \quad c \geq 1 \quad |xy| \leq k.$$

from pumping Lemma

$$xy^i z \in L \quad i = 0, 1, 2, \dots$$

let's take  $i = 0$ .

$$xz = 0^{k-c} 1^k 2^k \in L$$

Thus:

$$0^{k-c} 1^k 2^k \in L \quad k \geq 0.$$

But

$$L = \{0^m 1^m 2^m \mid m \geq 0\}.$$

$$0^{k-c} 1^k 2^k \notin L \quad \#$$

$\therefore L = \{0^m 1^m 2^m \mid m \geq 0\}$  is not a regular language.

### Question5

1.  $S \rightarrow 0A0 \mid 1A1$   
 $A \rightarrow 0A \mid 1A \mid \epsilon$

2.  $S \rightarrow 0T \mid 1T$   
 $T \rightarrow 0S \mid 1S \mid \epsilon$