

# **Testing**

Advanced Functional Programming Summer School 2019

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#### Why testing?

- · Gain confidence in the correctness of your program
- Show that common cases work correctly
- Show that corner cases work correctly

# Why testing?

- · Gain confidence in the correctness of your program
- · Show that common cases work correctly
- Show that corner cases work correctly

Testing cannot prove the absence of bugs

#### When is a program correct?

- What is a specification?
- How to establish a relation between the specification and the implementation?
- · What about bugs in the specification?

#### QuickCheck

#### QuickCheck, an *automated* testing library/tool for Haskell

- Describe properties as Haskell programs using an embedded domain-specific language (EDSL)
- Automatic datatype-driven random test case generation
- Extensible, e.g. test case generators can be adapted
  - A default generator for list generates any list, but you may want only sorted lists

# Case study: insertion sort

# A buggy insertion sort

Let's try to debug it using QuickCheck

#### How to write a specification?

#### A good specification is

- as precise as necessary
- but no more precise than necessary

A good specification for a particular problem, such as sorting, should:

- 1. distinguish sorting from all other operations on lists,
- 2. without forcing us to use a particular sorting algorithm

#### A first approximation

Certainly, sorting a list should not change its length

```
sortPreservesLength :: [Int] -> Bool
sortPreservesLength xs =
  length (sort xs) == length xs
```

We can test by invoking the function:

```
> quickCheck sortPreservesLength
Failed! Falsifiable, after 4 tests:
[0,3]
```

QuickCheck gives back a counterexample

## Correcting the bug

Which branch does not preserve the list length?

#### A new attempt

> quickCheck sortPreservesLength
OK, passed 100 tests.

Looks better. But have we tested enough?

## Properties are first-class objects

```
(f `preserves` p) x = p x == p (f x)
sortPreservesLength = sort `preserves` length
idPreservesLength = id `preserves` length
```

#### Properties are first-class objects

```
(f `preserves` p) x = p x == p (f x)
sortPreservesLength = sort `preserves` length
idPreservesLength = id `preserves` length
So id also preserves the lists length:
> quickCheck idPreservesLength
```

We need to refine our specification

OK, passed 100 tests.

#### When is a list sorted?

We can define a predicate that checks if a list is sorted:

```
isSorted :: [Int] -> Bool
isSorted [] = True
isSorted [x] = True
isSorted (x:y:xs) = x < y && isSorted (y:xs)</pre>
```

And use this to check that sorting a list produces a list that isSorted

#### Testing again

```
sortEnsuresSorted :: [Int] -> Bool
sortEnsuresSorted xs = isSorted (sort xs)

> quickCheck sortEnsuresSorted
Falsifiable, after 5 tests:
[5,0,-2]
> sort [5,0,-2]
[0,-2,5]
```

We're still not quite there...

# Debugging sort

## What's wrong now?

```
sort :: [Int] -> [Int]
sort [] = []
sort (x:xs) = insert x xs

insert :: Int -> [Int] -> [Int]
```

# Debugging sort

What's wrong now?

```
sort :: [Int] -> [Int]
sort [] = []
sort (x:xs) = insert x xs

insert :: Int -> [Int] -> [Int]
```

We are not recursively sorting the tail in **sort**!

# Another bug

```
> quickCheck sortEnsuresSorted
Falsifiable, after 7 tests:
[4,2,2]
> sort [4,2,2]
[2,2,4]
```

This is correct. What is wrong?

# Another bug

```
> quickCheck sortEnsuresSorted
Falsifiable, after 7 tests:
[4,2,2]
> sort [4,2,2]
[2,2,4]
```

> isSorted [2,2,4]

This is correct. What is wrong?

False

## Fixing the specification

The isSorted specification reads:

Why does it return False? How can we fix it?

# Are we done yet?

Is sorting specified completely by saying that

- · sorting preserves the length of the input list,
- the resulting list is sorted?

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Is sorting specified completely by saying that

- · sorting preserves the length of the input list,
- · the resulting list is sorted?

Not really...

```
evilNoSort :: [Int] -> [Int]
evilNoSort xs = replicate (length xs) 1
```

This function fulfills both specifications, but does not sort

# Specifying sorting

```
permutes :: ([Int] -> [Int]) -> [Int] -> Bool
permutes f xs = f xs `elem` permutations xs

sortPermutes :: [Int] -> Bool
sortPermutes xs = sort `permutes` xs
```

This completely specifies sorting and our algorithm passes the corresponding tests

# QuickCheck in general

## The type of quickCheck

The type of is an overloaded type:

```
quickCheck :: Testable prop => prop -> IO ()
```

- The argument of is a property of type **prop**
- The only restriction on the type is that it is in the **Testable** *type class*.
- When executed, prints the results of the test to the screen hence the
   IO () result type.

## Which properties are Testable?

So far, all our properties have been of type:

```
sortPreservesLength :: [Int] -> Bool
sortEnsuresSorted :: [Int] -> Bool
sortPermutes :: [Int] -> Bool
```

When used on such properties, QuickCheck generates random integer lists:

- If the result is **True** for 100 cases, this success is reported in a message
- If the result is False for a test case, the input triggering the failure is printed

# Other example properties

```
appendLength :: [Int] -> [Int] -> Bool
appendLength xs ys =
  length xs + length ys == length (xs ++ ys)
plusIsCommutative :: Int -> Int -> Bool
plusIsCommutative m n = m + n == n + m
takeDrop :: Int -> [Int] -> Bool
takeDrop n xs = take n xs ++ drop n xs == xs
dropTwice :: Int -> Int -> [Int] -> Bool
dropTwice m n xs =
  drop m (drop n xs) == drop (m + n) xs
```

# Other forms of properties – contd.

```
> quickCheck takeDrop
OK, passed 100 tests.
> quickCheck dropTwice
Falsifiable after 7 tests.
-1
[0]
> drop (-1) [0]
[0]
> drop 1 (drop (-1) [0])
[]
```

#### **Nullary properties**

A property without arguments is also possible:

```
lengthEmpty :: Bool
lengthEmpty = length [] == 0
wrong :: Bool
wrong = False
> quickCheck lengthEmpty
OK, passed 100 tests.
> quickCheck wrong
Falsifiable, after 0 tests.
```

QuickCheck subsumes unit tests

#### **Properties**

Recall the type of quickCheck:

```
quickCheck :: Testable prop => prop -> IO ()
```

We can now say more about when types are **Testable**:

testable properties usually are functions (with any number of arguments)
 resulting in a Bool

What argument types are admissible?

 QuickCheck has to know how to produce random test cases of such types

#### Properties - continued

A **Testable** thing is something which can be turned into a **Property**:

```
class Testable prop where
  property :: prop -> Property
```

A Bool is testable:

```
instance Testable Bool where ...
```

If a type is testable, we can add a function argument, as long as we know how to generate and print test cases:

```
instance (Arbitrary a, Show a, Testable b) =>
    Testable (a -> b) where
```

#### Information about test data

We can show the actual data that is tested:

```
> quickCheck (\ xs -> collect xs (sPL xs))
OK, passed 100 tests:
6% []
1% [9,4,-6,7]
1% [9,-1,0,-22,25,32,32,0,9,...
...
```

Why is it important to have access to the test data?

#### **Implications**

The function insert preserves an ordered list:

```
implies :: Bool -> Bool -> Bool
implies x y = not x || y

insertPreservesOrdered :: Int -> [Int] -> Bool
insertPreservesOrdered x xs =
  sorted xs `implies` sorted (insert x xs)
```

#### Implications – contd.

```
> quickCheck insertPreservesOrdered
OK, passed 100 tests.
But:
> let iPO = insertPreservesOrdered
> quickCheck (\x xs -> collect (sorted xs)
                                 (iP0 \times xs))
OK, passed 100 tests.
88% False
12% True
```

For 88 test cases, insert has not actually been relevant!

Implications – contd.

The solution is to use the QuickCheck implication operator:

```
(==>) :: Testable prop => Bool -> prop -> Property
iPO :: Int -> [Int] -> Property
iPO x xs = sorted xs ==> sorted (insert x xs)
```

Now, lists that are not sorted are discarded and do not contribute towards the goal of 100 test cases

#### Implications - contd.

We can now easily run into a new problem:

We try to ensure that lists are not too short, but:

Arguments exhausted after 20 tests (100% True).

The chance that a random list is sorted is extremely small

# Custom generators

#### Generators

- · Generators belong to an abstract data type Gen
  - The only effect available to us is access to random numbers
  - Think of as a restricted version of IO
- We can define our own generators using another domain-specific language
  - The default generators for datatypes are specified by defining instances of class Arbitrary

```
class Arbitrary a where
  arbitrary :: Gen a
  ...
```

#### Generator combinators

```
choose :: Random a => (a,a) -> Gen a
oneof :: [Gen a] -> Gen a
frequency :: [(Int, Gen a)] -> Gen a
elements :: [a] -> Gen a
sized :: (Int -> Gen a) -> Gen a
```

```
instance Arbitrary Bool where
  arbitrary = choose (False, True)
instance (Arbitrary a, Arbitrary b)
      => Arbitrary (a,b) where
  arbitrary = do x <- arbitrary
                  y <- arbitrary
                  return (x,y)
  -- arbitrary = (,) <$> arbitrary <*> arbitrary
data Dir = North | East | South | West
instance Arbitrary Dir where
  arbitrary = elements [North, East, South, West]
```

## Generating random numbers

· A simple possibility:

```
instance Arbitrary Int where
  arbitrary = choose (-20,20)
```

· Better

```
instance Arbitrary Int where
  arbitrary = sized (\n -> choose (-n,n))
```

 ${\boldsymbol{\cdot}}$  QuickCheck automatically increases the size gradually

### How to generate sorted lists

#### Idea: Adapt the default generator for lists

The following function turns a list of integers into a sorted list of integers:

## Random generator

The generator can be adapted as follows:

### Using a custom generator

There is another function to construct properties provided by QuickCheck, passing an explicit generator:

This is how we use it:

## **Shrinking**

The other method in **Arbitrary** is:

```
shrink :: (Arbitrary a) => a -> [a]
```

- Maps each value to structurally smaller values
  - [2,3] is structurally smaller than [1,2,3]
- When a failing test case is discovered, QuickCheck shrinks repeatedly until no smaller failing test case can be obtained

#### Loose ends

- Haskell can deal with infinite values, and so can QuickCheck
  - Properties must not inspect infinitely many values
  - Solution: only inspect finite parts
- QuickCheck can also generate functional values
  - Tequires defining an instance of another class Coarbitrary
  - · Showing functional values is still problematic
- QuickCheck has facilities for testing properties that involve IO

## Program coverage

To assess the quality of your test suite, it can be very useful to use GHC's program coverage tool:

```
$ ghc -fhpc Suite.hs --make
$ ./Suite
$ hpc report Suite --exclude=Main --exclude=QC
   18% expressions used (30/158)
      0% boolean coverage (0/3)
          0% guards (0/3), 3 unevaluated
      100% 'if' conditions (0/0)
      100% qualifiers (0/0)
      ...
```

This also generates a .html file showing which code has (not) been executed.

<u>module</u>	Top Level Definitions			<u>Alternatives</u>			Expressions		
	%	cc	vered / total	%	c	overed / total	%	cov	/ered / total
module Prettify2	42%	9/21		23%	8/34		18%	30/158	
Program Coverage Total	42%	9/21		23%	8/34		18%	30/158	

Figure 1: screenshot

```
data Doc = Empty
25
26
27
28
29
30
31
32
33
34
35
36
37
38
39
40
41
42
43
44
45
46
47
48
50
51
                 | Char Char
                  Text String
                   Line
                   Concat Doc Doc
                 | Union Doc Doc
                 deriving (Show, Eq)
      {-- /snippet Doc --}
      instance Monoid Doc where
           mempty = empty
           mappend = (<>)
      {-- snippet append --}
      empty :: Doc
     (<>) :: Doc -> Doc -> Doc
      {-- /snippet append --}
      empty = Empty
      Empty <> y = y
      x \ll Empty = x
      x <> y = x `Concat` y
      char :: Char -> Doc
      char c = Char c
```

Figure 2: screenshot

#### **Summary**

QuickCheck is a great tool:

- · A domain-specific language for writing properties
- Test data is generated automatically and randomly
- Another domain-specific language to write custom generators

However, keep in mind that writing good tests still requires practice, and that tests can have bugs, too

## Correctness

## Correctness as a goal

Testing cannot prove the absence of bugs

· Only point at failing cases

Are there ways to prove your code correct?

## **Equational reasoning**

- 1. Write a bunch of properties that specify your algorithm
- 2. Prove that they hold using equational reasoning
- 3. You are done!

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#### Caveats

- Time-consuming, needs lots of manual work
- · Laziness and exceptions are not taken care of
  - Proofs only work for finite values

### Interactive theorem proving

Help you proving properties about your program

- · Check that every inference step is correct
- Fill in boring and obvious proofs

Some interactive theorem provers:

- · Coq (blame the French for the name!)
- · Isabelle/HOL

### More expressive types

Define the type of your function in such a way that only correct implementations are allowed

```
append :: List n a -> List m a -> List (n + m) a
```

- 1. Dependent types
  - Allow values to appear in types
  - Examples: Agda, Idris, Coq
- 2. Refinement types
  - · Attach predicates to types
  - Example: LiquidHaskell

#### Theorems for free

How many implementations are of these signatures?

```
f :: a -> a
g :: (a, b) -> (b, a)
```

#### Theorems for free

How many implementations are of these signatures?

```
f :: a -> a
g :: (a, b) -> (b, a)
```

Only one!

```
f x = x -- identity function g (x, y) = (y, x) -- swap pair
```

Types are enough to determine many properties of the implementation

• We call those *free theorems* 

### Further reading

- John Hughes. Building on developers' intuition to create effective property-based tests (video)
- · Chapter 11 of Real World Haskell
- Koen Claessen and John Hughes. QuickCheck: A Lightweight Tool for Random Testing of Haskell Programs (the original paper)

Note: the titles are links;)