

## Math Review and Algorithm Analysis

Use empirical analysis methods and code analysis methods to determine running time complexity in Big O notation.

### Review of Common Math Functions.

- 1) Use Excel or some other graphing tool to graph the following equations.

$$y = x$$

$$y = 2x$$

$$y = x^2$$

$$y = 2^x$$

$$y = x^3$$

$$y = \log_2 x$$

- 2) Rank the graphs of the above equations by rate of growth, fastest (non-initial) growth first.
- 3) Match the shape of each graph with the closest common Big(O) curve and label them so.

### Empirical Analysis.

- 4) Complete the table for each of the following functions. For each foo, write a small program with a loop where n is a counter from 0 to at least 64. Call the foo within the loop, passing it each value of n, and getting the return value from foo. Fill out a table with each n and its corresponding return value. You can skip some values of n when n starts to get bigish. Capture your output and generate the tables.

```
int foo1(int n)
{
    int counter = 0;

    for(int i = 0; i < n; i++)
        counter++;

    return counter;
}

int foo2(int n)
{
    int counter = 0;

    for(int i = 0; i < n; i++)
        for(int j = 0; j < n; j++)
            counter++;

    return counter;
}

int foo3(int n)
{
    int counter = 0;
```

n	return value
0	
1	
2	
3	
4	
5	
6	
7	
8	
9	
10	
11	
12	
13	
14	
15	
16	
32	
64	

```

        for(int i = n; i > 0; i = i/2)
            counter++;

    return counter;
}

// note: you might not make it much past n = 32
int foo4(int n)
{
    static int counter = 0;
    counter++;

    if(n > 0)
    {
        foo4(n-1);
        foo4(n-1);
    }

    return counter;
}

```

- 5) Use Excel to GRAPH the data tables from the previous functions. Use the return value as a function of n. That means, put n on the horizontal axis (x) and put the return value on the vertical axis (y). Use Excel or some other graphics tool.
- 6) Rank the graphs above by rate of growth, fastest first.

### Code Analysis

- 7) **Implement** and test each of the following series for several different values of n and A. Present your output in a nice table of values. Use **iterative solutions**, do not use the equivalent (condensed) algebraic formula.

#### I. Arithmetic Series

Test for values of n from 1 to 10.

$$\sum_{i=1}^N i = 1 + 2 + 3 + \dots + N$$

Iterative code solution:

```

int sum = 0;
for(int i = 1; i <= n; i++)
    sum = sum + i;

```

#### II. Geometric Series

Test for values of n from 1 to 5 and A from 1 to 5 (25 rows total).

$$\sum_{i=1}^N A^i = A^1 + A^2 + A^3 + \dots + A^N$$

Iterative code solution:

```

int term, sum = 0;
for(int i = 1; i <= n; i++)
{
    term = A;

```

```

        for(int j = 1; j < i; j++)
            term = term * A;
        sum = sum + term;
    }

    return sum;

```

### III. A More Efficient Geometric Series

Redo the previous solution using only a single loop instead of the nested loop.

### IV. Another Series

Implement the following series and test for  $n = 1$  to 5 and  $A = 1$  to 5 (25 rows total).  
Produce a nice table of values.

$$\sum_{i=1}^N iA^i = 1A^1 + 2A^2 + 3A^3 + \dots + NA^N$$

- 8) For the previous series implementations, determine the BigO of each series by analysis of the source code. A code analysis using our Big O “rules of thumb” is sufficient; you do not need to perform an exact mathematical analysis. List the Big O answer and explain why it is so in English.