## Lecture 4: Point Groups

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http://ffgroup.chem.uci.edu

#### **Definition**

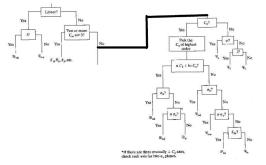
Point groups are groups of symmetry operations that keep at least one point in Euclidean space fixed.

Symmetry element of point groups:

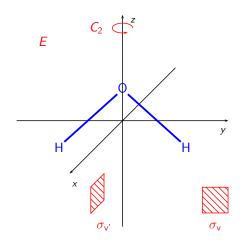
- (i) Identity E
- (ii) n-fold rotation or symmetry axes  $C_n$
- (iii) Reflection or symmetry or mirror planes  $\sigma$
- (iv) *n*-fold rotation-reflection axis  $S_n$  (includes  $i \equiv S_2$ )
  - All point groups are subroups of orthogonal group O(N) (N is dimension)
  - Molecular point groups: N = 3
    - ▶ 7 axial group families:  $C_n$ ,  $S_{2n}$ ,  $C_{nh}$ ,  $C_{nv}$ ,  $D_n$ ,  $D_{nd}$ ,  $D_{nh}$
    - ▶ 7 polyhedradal group families: T,  $T_d$ ,  $T_h$ , O,  $O_h$ , I,  $I_h$

## **Determining Point Group Symmetry**

- 1. Visualize the molecule (e.g. using a simple web-based renderer)
- 2. Determine all symmetry elements
- 3. Follow the flow chart:



### Water Molecule



- Symmetry elements of water:  $\{E, C_2, \sigma_v, \sigma_{v'}\}$
- Point group C<sub>2v</sub>

# Group Multiplication Table

- Product of two symmetry operations  $c = a \cdot b$ : Apply b followed by a
- $C_{2\nu}$  group (multiplication) table:

a	Ε	$C_2$	$\sigma_{\sf v}$	$\sigma_{v'}$
b				
Ε	Ε	$C_2$ $E$ $\sigma_{v'}$ $\sigma_{v}$	$\sigma_{\sf v}$	$\sigma_{v'}$
$C_2$	$C_2$	Ε	$\sigma_{v'}$	$\sigma_{\sf v}$
$\sigma_{\sf v}$ $\sigma_{\sf v'}$	$\sigma_{\sf v}$	$\sigma_{v'}$	Ε	$C_2$
$\sigma_{v'}$	$\sigma_{v'}$	$\sigma_{\sf v}$	$C_2$	Ε

#### Web Resources

- Otterbein Symmetry: Visualize symmetry operations in 3D
- Achim Gelessus' Website: Character tables for chemically important point groups