



Linköping University

TDDC17 ARTIFICIAL INTELLIGENCE **Lab 3: Bayesian Networks**

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1 Task 2

1.1 What is the risk of melt-down in the power plant during a day if no observations have been made? What if there is icy weather?

The risk of melt-down if no observations have been made is 0.02578, this is done by just monitoring the Meltdown node. If there is icy weather then the risk is 0.03472, this is done by changing the IcyWeather node to true and then monitoring the Meltdown node.

1.2 Suppose that both warning sensors indicate failure. What is the risk of a meltdown in that case? Compare this result with the risk of a melt-down when there is an actual pump failure and water leak. What is the difference? The answers must be expressed as conditional probabilities of the observed variables, $P(\text{Meltdown}|\dots)$.

The risk of a meltdown when both warning sensors indicate failure is

$$P(\text{Meltdown}|\text{PumpFailureWarning} \wedge \text{WaterLeakWarning}) = 0.14535,$$

which is acquired by setting both warning nodes to true and then observing the Meltdown node. The risk of a meltdown when the failures actually occur is

$$P(\text{Meltdown}|\text{PumpFailure} \wedge \text{WaterLeak}) = 0.20000,$$

which is acquired by setting both failure nodes to true and then observing the Meltdown node. The difference is

$$\begin{aligned} &P(\text{Meltdown}|\text{PumpFailure} \wedge \text{WaterLeak}) - \\ &P(\text{Meltdown}|\text{PumpFailureWarning} \wedge \text{WaterLeakWarning}) = 0.05465. \end{aligned}$$

1.3 The conditional probabilities for the stochastic variables are often estimated by repeated experiments or observations. Why is it sometimes very difficult to get accurate numbers for these? What conditional probabilities in the model of the plant do you think are difficult or impossible to estimate?

The "IcyWeather" variable is probably hardest to try and estimate since you cannot rely on past data for weather. Weather in itself is so inconsistent that if there is icy weather one day it does not mean that the next day will also have icy weather.

1.4 Assume that the "IcyWeather" variable is changed to a more accurate "Temperature" variable instead (don't change your model). What are the different alternatives for the domain of this variable? What will happen with the probability distribution of $P(\text{WaterLeak}|\text{Temperature})$ in each alternative?

To get exactly the same behavior as with the "IcyWeather" variable then the domain for the "Temperature" variable could be "icy temperature" or "normal temperature", instead of "true" and

"false". In this case the probability distribution will be the same since the probability for "icy temperature" will be the same as the probability of "IcyWeather"'s "true" and the same goes for "normal temperature" and "false".

1.5 What does a probability table in a Bayesian network represent?

The table represents the conditional distributions

1.6 What is a joint probability distribution? Using the chain rule on the structure of the Bayesian network to rewrite the joint distribution as a product of $P(child|parent)$ expressions, calculate manually the particular entry in the joint distribution of $P(\text{Meltdown}=F, \text{PumpFailureWarning}=F, \text{PumpFailure}=F, \text{WaterLeakWarning}=F, \text{WaterLeak}=F, \text{IcyWeather}=F)$. Is this a common state for the nuclear plant to be in?

Joint probability calculates the likelihood of two events occurring together and at the same point in time.

$$\begin{aligned} P(\neg \text{Meltdown}, \neg \text{PumpFailureWarning}, \neg \text{PumpFailure}, \neg \text{WaterLeakWarning}, \neg \text{WaterLeak}, \neg \text{IcyWeather}) = \\ P(\neg \text{Meltdown} | \neg \text{PumpFailure} \wedge \neg \text{WaterLeak}) * P(\neg \text{PumpFailureWarning} | \neg \text{PumpFailure}) * P(\neg \text{PumpFailure}) \\ * P(\neg \text{WaterLeakWarning} | \neg \text{WaterLeak}) * P(\neg \text{WaterLeak} | \neg \text{IcyWeather}) * P(\neg \text{IcyWeather}) = \\ 0.999 * 0.95 * 0.9 * 0.95 * 0.9 * 0.95 = 0.69378 \end{aligned}$$

1.7 What is the probability of a meltdown if you know that there is both a water leak and a pump failure? Would knowing the state of any other variable matter? Explain your reasoning!

Since the probability is given by the following probability function:

$$P(\text{Meltdown} | \text{PumpFailure} \wedge \text{WaterLeak}) = 0.2$$

then we do not know the state of any other variable. However if the probability would be given by

$$P(\text{Meltdown}, \text{PumpFailure}, \text{WaterLeak}) = P(\text{Meltdown} | \text{PumpFailure} \wedge \text{WaterLeak})$$

then we would need to know the state of the "IcyWeather" variable.

- 1.8 Calculate manually the probability of a meltdown when you happen to know that $\text{PumpFailureWarning}=\text{F}$, $\text{WaterLeak}=\text{F}$, $\text{WaterLeakWarning}=\text{F}$ and $\text{IcyWeather}=\text{F}$ but you are not really sure about a pump failure.

$$\begin{aligned}
& P(\text{Meltdown}, \neg \text{PumpFailureWarning}, \neg \text{WaterLeak}, \neg \text{WaterLeakWarning}, \neg \text{IcyWeather}, \neg \text{PumpFailure}) + \\
& P(\text{Meltdown}, \neg \text{PumpFailureWarning}, \neg \text{WaterLeak}, \neg \text{WaterLeakWarning}, \neg \text{IcyWeather}, \text{PumpFailure}) = \\
& [P(\neg \text{Meltdown} | \neg \text{PumpFailure} \wedge \neg \text{WaterLeak}) * P(\neg \text{PumpFailureWarning} | \neg \text{PumpFailure}) * P(\neg \text{PumpFailure}) \\
& \quad * P(\neg \text{WaterLeakWarning} | \neg \text{WaterLeak}) * P(\neg \text{WaterLeak} | \neg \text{IcyWeather}) * P(\neg \text{IcyWeather})] + \\
& [P(\neg \text{Meltdown} | \text{PumpFailure} \wedge \neg \text{WaterLeak}) * P(\neg \text{PumpFailureWarning} | \text{PumpFailure}) * P(\text{PumpFailure}) \\
& \quad * P(\neg \text{WaterLeakWarning} | \neg \text{WaterLeak}) * P(\neg \text{WaterLeak} | \neg \text{IcyWeather}) * P(\neg \text{IcyWeather})] = \\
& \quad \quad \quad 0.001895
\end{aligned}$$

2 Task 3

- 2.1 During the lunch break, the owner tries to show off for his employees by demonstrating the many features of his car stereo. To everyone's disappointment, it doesn't work. How did the owner's chances of surviving the day change after this observation?

If we do not know if the radio is working then the probability of the owner surviving is 0.99010, this is achieved by just observing the "Survives" variable. If the radio is not working then the probability of the owner surviving is 0.98116, this is achieved by setting the "Radio" variable to "false" and then observing the "Survives" variable. The owner's chance of surviving decreased by

$$0.99010 - 0.98116 = 0.00885.$$

2.2 How does the bicycle change the owner's chances of survival?

The chance that the owner survives when it owns a bike as well is 0.99505, which is achieved by just observing the "Survives" variable after adding the "BicycleWorks" variable. The owner's chance of surviving increased by

$$0.99505 - 0.99010 = 0.00495,$$

compared to when he did not own the bike.

- 2.3** It is possible to model any function in propositional logic with Bayesian Networks. What does this fact say about the complexity of exact inference in Bayesian Networks? What alternatives are there to exact inference?

3 Task 4

- 3.1** The owner had an idea that instead of employing a safety person, to replace the pump with a better one. Is it possible, in your model, to compensate for the lack of Mr H.S.'s expertise with a better pump?

Yes since a better pump could reduce the probability of "PumpFailure" which also reduces the need for Mr H.S.'s expertise.

- 3.2** Mr H.S. fell asleep on one of the plant's couches. When he wakes up he hears someone scream: "There is one or more warning signals beeping in your control room!". Mr H.S. realizes that he does not have time to fix the error before it is too late (we can assume that he wasn't in the control room at all). What is the chance of survival for Mr H.S. if he has a car with the same properties as the owner?

Mr H.S.'s chance of survival is 0.61280.

- 3.3** What unrealistic assumptions do you make when creating a Bayesian Network model of a person?

We always assume that the person is healthy, but it is possible that the person is sick or just feeling unwell which may affect the chance of survival.

- 3.4** Describe how you would model a more dynamic world where for example the "IcyWeather" is more likely to be true the next day if it was true the day before. You only have to consider a limited sequence of days.

We could add a node that connects to "IcyWeather" and which represents the previous day's weather. This could also be done for several days. Then the probability for today's "IcyWeather" will be higher if the previous days had "IcyWeather".