



Linköping University

TDDE01 MACHINE LEARNING

Lab 1 - Report

Lawrence Thanakumar Rajappa (lawra776)

November 30, 2019

Assignment 1

2. Confusion Matrix and Misclassification Rate for $p > 0.5$

Confusion Matrix

Confusion Matrix - Training Data			Confusion Matrix - Test Data		
	0	1		0	1
0	803	81	0	791	97
1	142	344	1	146	336

Misclassification Rate

Misclassification Rate - Training Data	Misclassification Rate - Test Data
0.1627737 ~ 16.277%	0.1773723 ~ 17.737%

3. Confusion Matrix and Misclassification Rate for $p > 0.8$

Confusion Matrix

Confusion Matrix - Training Data			Confusion Matrix - Test Data		
	0	1		0	1
0	941	335	0	926	367
1	4	90	1	11	66

Misclassification Rate

Misclassification Rate - Training Data	Misclassification Rate - Test Data
0.2474453 ~ 24.744%	0.2759124 ~ 27.591%

The new rule has increased the Misclassification rates for both training and test dataset. This is because of the threshold or probability limit which was set. In 0.5 probability scenario, the data points which are above this threshold line was classified as 1 and the data points below the line was classified as 0. But, when the threshold was increased to 0.8, the points which were actually observed as 1, was classified as 0, hence the Misclassification rate has increased and also the accuracy has reduced from 82% to 72%.

4. Misclassification Rate when $k = 30$

Confusion Matrix

Confusion Matrix - Training Data			Confusion Matrix - Test Data		
	0	1		0	1
0	810	96	0	671	189
1	135	329	1	266	244

Misclassification Rate

Misclassification Rate - Training Data	Misclassification Rate - Test Data
0.1686131 ~ 16.861%	0.3321168 ~ 33.211%

By comparing step 4 and step 2, we could see that there is a huge difference in correct predictions and Misclassification rates. Logistic Regression model with $p > 0.5$ suits very well for this dataset rather than knn.

5. Misclassification Rate when $k = 1$

Confusion Matrix

Confusion Matrix - Training Data			Confusion Matrix - Test Data		
	0	1		0	1
0	945	0	0	640	177
1	0	425	1	297	256

Misclassification Rate

Misclassification Rate - Training Data	Misclassification Rate - Test Data
0 ~ 0%	0.3459854 ~ 34.598%

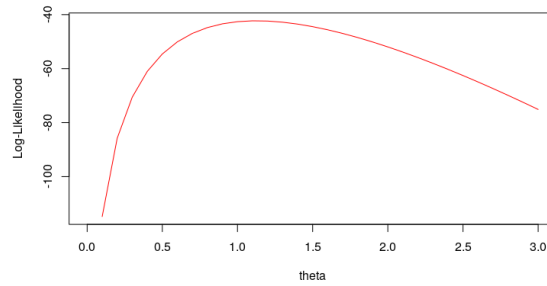
In terms of ***Bias-Variance trade off***, if $K = 1$, then the training data will have low bias hence it behaves well with training data. But, it fails to generalize the testing data and it will increase test data prediction error and leads to high variance. Low Bias and high variance leads to overfitting. Hence KNN model with $K = 1$ is not an admissible model to use. In the last lab group report, I have used `kknn()` function, hence I got weird results. But, when I used `train.kknn()` function, I got the expected results.

Assignment 2

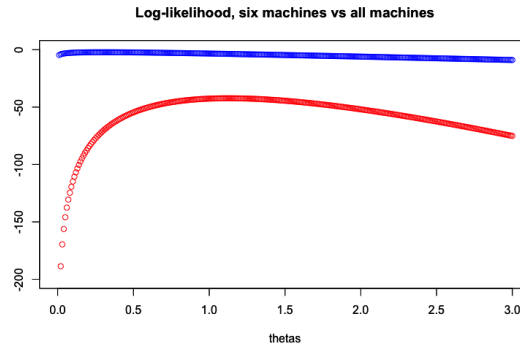
2. Based on the probability model, $P(x|\theta) = \theta e^{-\theta x}$, we can see that this data belongs to exponential distribution. We have used the below formula to calculate log-likelihood

$$l(\lambda; x_1, \dots, x_n) = n \ln(\lambda) - \lambda \sum_{j=1}^n x_j$$

and plotted the below graph and the maximum likelihood value of θ is 1.12

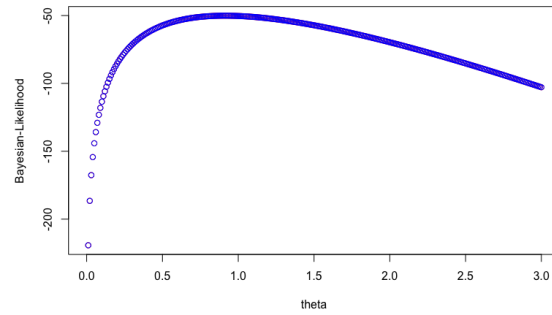


3. By using the same function but with only 6 set of observations, the generated plot is given below,



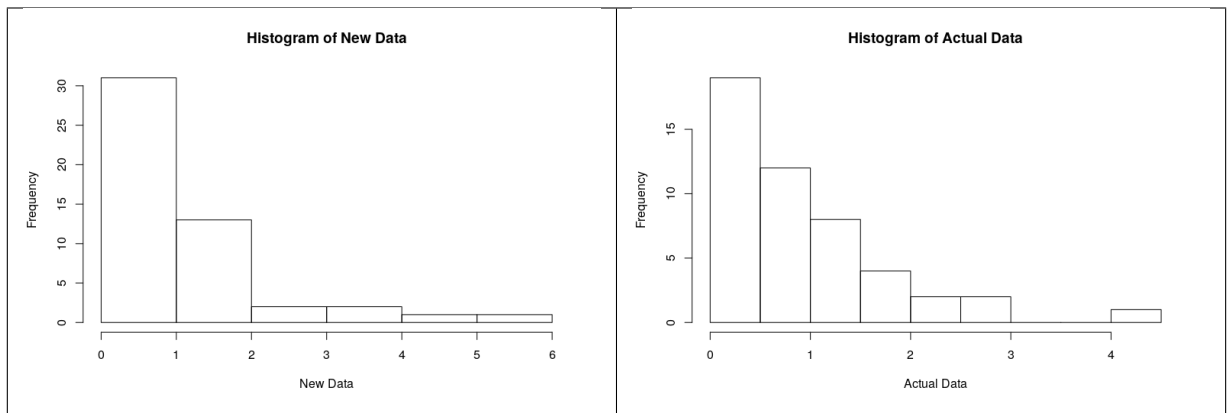
From the plot we can see that, blue curve is unreliable as it is using only first 6 observations of the data and we will miss out information. Comparing the plots, eventhough blue plot has higher θ , reliability is worse when data points are limited. The maximum log-likelihood value of θ is 1.126217 for full set of observations and 1.785681 for first 6 observations.

4. By using bayesian model $p(x|\theta) = \theta e^{-\theta x}$ and a prior $p(\theta) = \lambda e^{-\lambda \theta}$ and also $\lambda = 10$, we need to compute the function $l(\theta) = \log(p(x|\theta)p(\theta))$ and plot the corresponding curve.



The maximum likelihood value of θ is 0.91 compared to previous 1.12. This is used to measure how good the model fits the data.

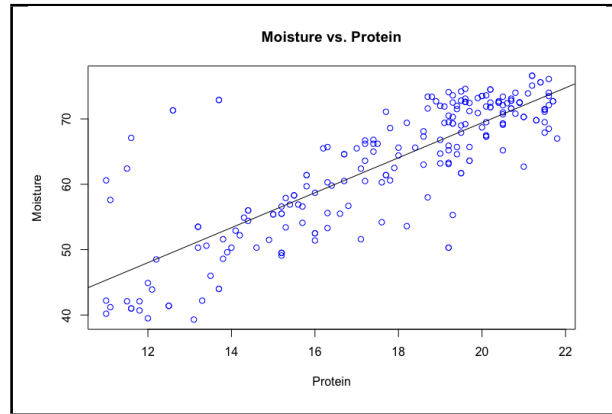
5.



From the above histograms, we can conclude that both histograms looks similar and follows exponential distribution and chosen model is a good model.

Assignment 4

1. Plot of Moisture VS Proteins



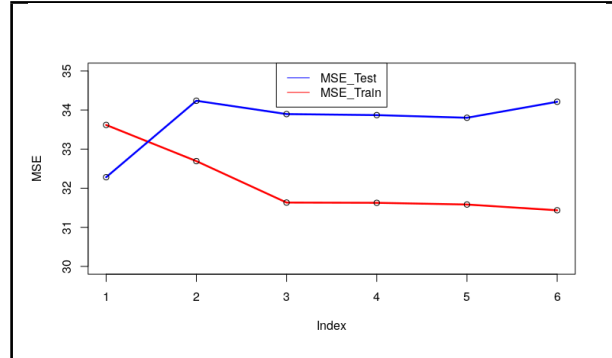
From the scatter plot, we can observe that there is a linearly increasing relationship between **'Moisture'** and **'Protein'** variables by a smoothing line. Moreover, linear regression concept is to have a linear relationship between response variable and dependent variables.

2. Now, let us consider a model m_1 where moisture is normally distributed and expected moisture is a polynomial function of protein. The probabilistic model is given below

$$\begin{aligned} \text{independent variable (X)} &= \text{Protein} \\ \text{dependent variable (Y)} &= \text{Moisture} \\ Y &\sim M_0 + M_1 * x + M_2 * x^2 + \dots + M_n * x^n \end{aligned}$$

MSE would be a better criterion in order to determine which model is best based on lower MSE.

3. MSE

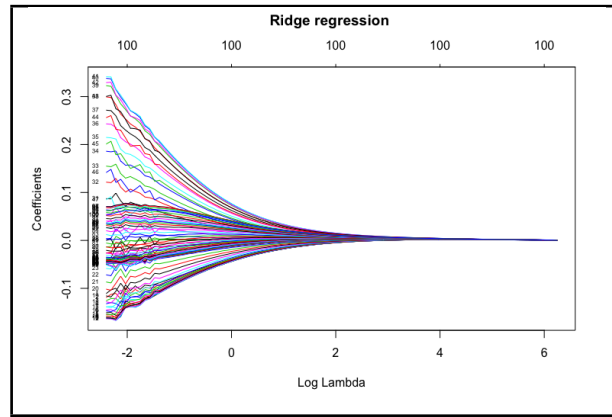


The above plot describes the training error and testing error for tecator dataset. We can observe that as the polynomial degrees increases, the MSE for test set increases and lower MSE for training set. In terms of Bias-Variance trade off, as the model complexity increases because of increase in polynomial degree, there is a high variance on training data and hence this will have higher error rates on test data as well as training set has low bias. Low Bias and High Variance leads to overfitting while training and the model performs poorer on test dataset. **Based on the plot, model_3 would be a better model when compared with other models, as it has optimum training and testing error when compared with other models.**

4. Now, we need to use stepAIC function in R for a variable selection on a linear model where *Fat* is response variable and *channel1-channel100* is independent variables. After running the function stepAIC, we get a total 63 variables which are given below,

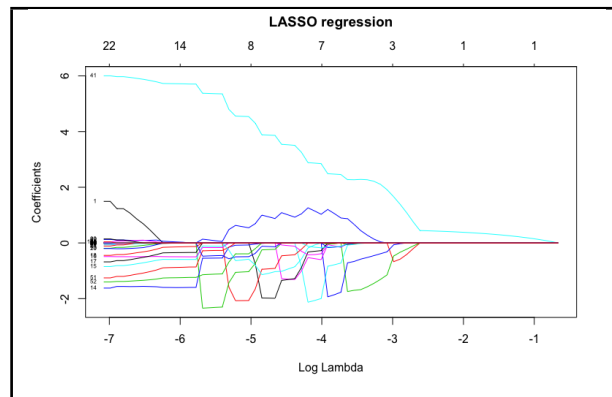
```
Final Model:
Fat ~ Channel1 + Channel14 + Channel16 + Channel18 + Channel19 +
Channel111 + Channel113 + Channel114 + Channel115 + Channel117 +
Channel118 + Channel120 + Channel121 + Channel123 + Channel124 +
Channel125 + Channel127 + Channel129 + Channel131 + Channel134 +
Channel135 + Channel136 + Channel137 + Channel144 + Channel145 +
Channel146 + Channel147 + Channel148 + Channel152 + Channel153 +
Channel154 + Channel155 + Channel156 + Channel157 + Channel158 +
Channel160 + Channel161 + Channel162 + Channel164 + Channel166 +
Channel167 + Channel169 + Channel170 + Channel171 + Channel172 +
Channel177 + Channel179 + Channel180 + Channel182 + Channel183 +
Channel188 + Channel189 + Channel191 + Channel192 + Channel195 +
Channel196 + Channel197 + Channel198 + Channel199 + Protein +
Moisture + Channel138 + Channel100
```

5. Now, we have applied Ridge regression to the scaled independent and the dependent variables, as values to be scaled before applying Ridge regression on them. Ridge regression is applied by using the glmnet function in R. The coefficients dependency on log of penalty factor λ is given below,



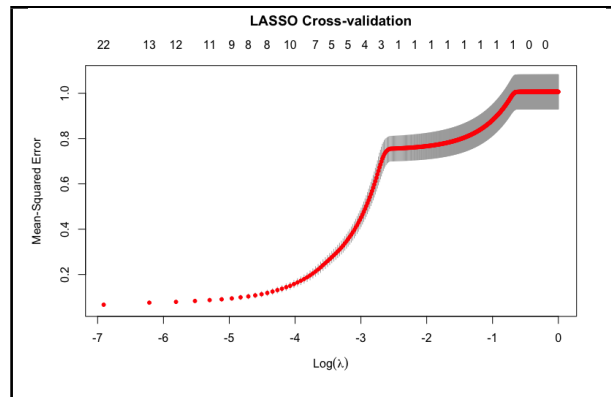
From the above graph, we can say that, if λ increases, all coefficients go to zero.

6. We do the same but it is for Lasso Regression,



From the above graph we can see that, most of the features have bigger impact and some of the features are completely ignored.

7. Now, we need to use cross-validation and find optimal LASSO Model. The plots are given below,



By interpreting the plot, we conclude that optimal λ value is 0. The number of features selected were 22 according to the plot for that specific lambda value. Moreover, LASSO gives lesser MSE than stepAIC eventhough, stepAIC selected 63 features than LASSO. In conclusion, it is not always better to use more features while modeling but at the same time it depends on the dataset and the number of features in the dataset.

Code Appendix

Assignment 1

```
library(readxl) #Library to read spreadsheet based files
library(kknn) #Library to implement KNN algorithm
options(scipen=999) #To avoid scientific notations
RNGversion('3.5.1')
#Assignment 1
#Reading from excel file
data = read_excel("spambase.xlsx",sheet = "spambase_data")
#1. Splitting the data
n=dim(data)[1]
set.seed(12345)
id=sample(1:n, floor(n*0.5))
#Converting target variable "Spam" to factor
data$Spam = as.factor(data$Spam)
train=data[id,]
test=data[-id,]

#2. Logistic Regression with P(Y|X)>0.5
logisticModel_1 = glm(Spam~.,family = binomial,data = train)
summary(logisticModel_1)
```

```

#Function to calculate misclassification rate
missclass=function(actualData,predictedData){
  n=length(actualData)
  return(1-sum(diag(table(actualData,predictedData)))/n)
}

#0.5 classification principle
predicted_training_prob_1 = predict(logisticModel_1,newdata = train,type="response")
predicted_training_1 = ifelse(predicted_training_prob_1>0.5,1,0)
table(as.factor(predicted_training_1),train$Spam)
missclass(train$Spam,as.factor(predicted_training_1))

predicted_test_prob_1 = predict(logisticModel_1,newdata = test,type = "response")
predicted_test_1 = ifelse(predicted_test_prob_1>0.5,1,0)
table(as.factor(predicted_test_1),test$Spam)
missclass(test$Spam,as.factor(predicted_test_1))

#0.8 classification principle
predicted_training_prob_2 = predict(logisticModel_1,newdata = train,type="response")
predicted_training_2 = ifelse(predicted_training_prob_2>0.8,1,0)
table(as.factor(predicted_training_2),train$Spam)
missclass(train$Spam,as.factor(predicted_training_2))

predicted_test_prob_2 = predict(logisticModel_1,newdata = test,type = "response")
predicted_test_2 = ifelse(predicted_test_prob_2>0.8,1,0)
table(as.factor(predicted_test_2),test$Spam)
missclass(test$Spam,as.factor(predicted_test_2))

#3. KNN

knnModel_1 = train.kknn(Spam~.,data = train,kmax = 30)

predicted_3_training_data = predict(knnModel_1,newdata = train)
table(as.factor(predicted_3_training_data),train$Spam)

predicted_3_testing_data = predict(knnModel_1,newdata = test)
table(as.factor(predicted_3_testing_data),test$Spam)

missclass(train$Spam,as.factor(predicted_3_training_data))
missclass(test$Spam,as.factor(predicted_3_testing_data))

knnModel_2 = train.kknn(Spam~.,data=train,kmax = 1)

predicted_4_training_data = predict(knnModel_2,newdata = train)
table(as.factor(predicted_4_training_data),train$Spam)

predicted_4_testing_data = predict(knnModel_2,newdata = test)
table(as.factor(predicted_4_testing_data),test$Spam)

missclass(train$Spam,as.factor(predicted_4_training_data))
missclass(test$Spam,as.factor(predicted_4_testing_data))

```

Assignment 2

```
#Assignment - 2
library(readxl) #Library to read spreadsheet based files
options(scipen=999) #To avoid scientific notations
set.seed(12345)
RNGversion('3.5.1')
#1. Reading the data
machineData = read_excel("machines.xlsx",sheet = "machines")

#Distribution
hist(machineData$Length,probability = TRUE,xlab = "Length", main = "Length Vs Density")
lines(density(machineData$Length),col="blue", lwd=2)

#Log-likelihood function
theta = seq(from=0,to=3,by=0.01)
logLikelihood = function(theta,dataVector)
{
  return(length(dataVector)*log(theta)-theta*sum(dataVector))
}

maximumLikelihood = function(theta,dataVector)
{
  return(length(dataVector)/sum(dataVector))
}

plot(theta, logLikelihood(theta,machineData$Length), ylim = c(-200,0), col = 'red',
      xlab="thetas", ylab = "",
      main="Log-likelihood, six machines vs all machines")
par(new = TRUE)
plot(theta, logLikelihood(theta,machineData[1:6,]), ylim = c(-200,0), col='blue',
      xlab="thetas", ylab = "",
      main="Log-likelihood, six machines vs all machines")

maximumLikelihood(theta,machineData$Length)
maximumLikelihood(theta,machineData$Length[1:6])

#4.
bayesian <- function(data, theta,lambda) {
  return( logLikelihood(theta, data) + log(lambda*exp(-lambda*theta)))
}

plot(theta,bayesian(machineData$Length,theta,10),col="red",xlab="theta",
      ylab = "Bayesian-Likelihood")
par(new=TRUE)
points(theta,bayesian(machineData$Length,theta,10),col="blue")
theta[which.max(bayesian(machineData$Length,theta,10))]

#5.
theta[which.max(logLikelihood(theta,machineData$Length))]
new_observation_exp = (rexp(50,
  theta[which.max(logLikelihood(theta,machineData$Length))]))
hist(new_observation_exp,main = "Histogram of New Data",xlab="New Data")
```

```
hist(machineData$Length, main = "Histogram of Actual Data", xlab = "Actual Data")
par(new = TRUE)
```

Assignment 4

```
#Assignment - 3
library(readxl) #Library to read spreadsheet based files
library(ggplot2) #For visualisation
options(scipen=999) #To avoid scientific notations
set.seed(12345)
#Loading data
tecatorData = read_excel("tecator.xlsx", sheet = "data")

#1. plotting Moisture VS Protein
plot(tecatorData$Protein, tecatorData$Moisture, main="Moisture vs. Protein", xlab =
     "Protein", ylab = "Moisture", col="blue")
abline(lm(formula = Moisture ~ Protein, data=tecatorData))

#Subsetting data
requiredData = tecatorData[,103:104]
id = sample(1:nrow(requiredData), floor(nrow(requiredData)*0.5))
train = requiredData[id,]
test = requiredData[-id,]

#Linear Regression
#M1
tecatorModel_1 = lm(formula = Moisture ~ Protein, data=train)
sm1 = summary(tecatorModel_1)
sm1

#M2
tecatorModel_2 = lm(formula = Moisture ~ Protein+I(Protein^2), data=train)
sm2 = summary(tecatorModel_2)
sm2

#M3
tecatorModel_3 = lm(formula = Moisture ~ Protein+I(Protein^2)+I(Protein^3), data=train)
sm3 = summary(tecatorModel_3)
sm3

#M4
tecatorModel_4 = lm(formula = Moisture ~ Protein+I(Protein^2)+I(Protein^3)+I(Protein^4),
                    data=train)
sm4 = summary(tecatorModel_4)
sm4

#M5
tecatorModel_5 = lm(formula = Moisture ~
                    Protein+I(Protein^2)+I(Protein^3)+I(Protein^4)+I(Protein^5), data=train)
sm5 = summary(tecatorModel_5)
```

```

sm5

#M6
tecatorModel_6 = lm(formula = Moisture ~
  Protein+I(Protein^2)+I(Protein^3)+I(Protein^4)+I(Protein^5)+I(Protein^6), data=train)
sm6 = summary(tecatorModel_6)
sm6

MSE_train = numeric(6)
MSE_train[1] = mean((train$Moisture-predict.lm(tecatorModel_1,train[,1]))^2)
MSE_train[2] = mean((train$Moisture-predict.lm(tecatorModel_2,train[,1]))^2)
MSE_train[3] = mean((train$Moisture-predict.lm(tecatorModel_3,train[,1]))^2)
MSE_train[4] = mean((train$Moisture-predict.lm(tecatorModel_4,train[,1]))^2)
MSE_train[5] = mean((train$Moisture-predict.lm(tecatorModel_5,train[,1]))^2)
MSE_train[6] = mean((train$Moisture-predict.lm(tecatorModel_6,train[,1]))^2)

MSE_test = numeric(6)
MSE_test[1] = mean((test$Moisture-predict.lm(tecatorModel_1,test[,1]))^2)
MSE_test[2] = mean((test$Moisture-predict.lm(tecatorModel_2,test[,1]))^2)
MSE_test[3] = mean((test$Moisture-predict.lm(tecatorModel_3,test[,1]))^2)
MSE_test[4] = mean((test$Moisture-predict.lm(tecatorModel_4,test[,1]))^2)
MSE_test[5] = mean((test$Moisture-predict.lm(tecatorModel_5,test[,1]))^2)
MSE_test[6] = mean((test$Moisture-predict.lm(tecatorModel_6,test[,1]))^2)

plot(1:6,MSE_train,type="l",ylim = c(20,45),col="red",lwd=2.5,xlab = "Index",ylab = "MSE")
lines(1:6,MSE_test,col="blue",lwd=2.5)
legend(x="center",legend = c("MSE_Test", "MSE_Train"),lwd=1,col=c("Blue", "Red"),lty=1)

print(anova(tecatorModel_1,tecatorModel_2,tecatorModel_3,tecatorModel_4,tecatorModel_5,tecatorModel_6))

#4. Variable Selection
library(MASS)
aicData = tecatorData
aicData = aicData[,-c(103:104)]
aicData = aicData[,-c(1)]
stepAIC = stepAIC(lm(Fat~.,data = aicData))
stepAIC$anova

#5. Ridge Regression
library(glmnet)
covariates = scale(tecatorData[, 2:101])
response = scale(tecatorData$Fat)
ridge_model = glmnet(as.matrix(covariates),
  response, alpha = 0, family="gaussian")
plot(ridge_model, xvar="lambda", label=TRUE, main="Ridge regression \n\n")

#6. Lasso Regression
lasso_model = glmnet(as.matrix(covariates),
  response, alpha = 1, family="gaussian")
plot(lasso_model, xvar="lambda", label=TRUE, main="LASSO regression\n\n")

```

```
#7. Cross-Validation
lasso_model_cv = cv.glmnet(as.matrix(covariates), response, alpha=1, family="gaussian",
    lambda=seq(0,1,0.001))
plot(lasso_model_cv, xvar="lambda", label=TRUE, main="LASSO Cross-validation\n\n")
coef(lasso_model_cv, s="lambda.min")
print(lasso_model_cv$lambda.min)
```
