

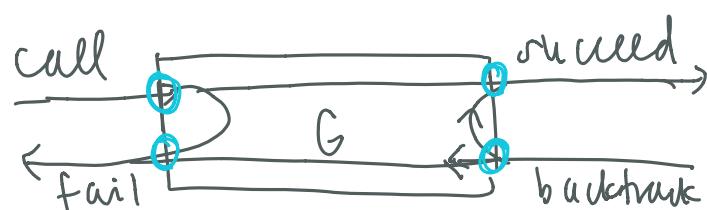
Prolog debugging

? - ask A

A = 5 Q

A = 2 + 7 Q

Prolog 4-part debugging model



- accessed through ?- true
- use only at the beginning to understand how Prolog works

Vocabulary

clause:

- fact
- rule
- query

To run, Prolog:

- starts with query
- backwards chaining from query
- ↳ starts with what you're trying to prove and goes backward from it

↳ from rules to facts

↳ goal oriented

- left-to-right
- AND. ↳ tries leftmost goals first within a query/clause
- OR ↳ for heads of clauses

Problems with Prolog

①

? - true

yes

? - fail.

no

? - precedence(A, B)

(message) // extra check

no.

source code
for true

source code
for fail

(doesn't have
source code)

②

? - loop



? - repeat

yes.

loop :- loop

repeat.
repeat:- repeat.

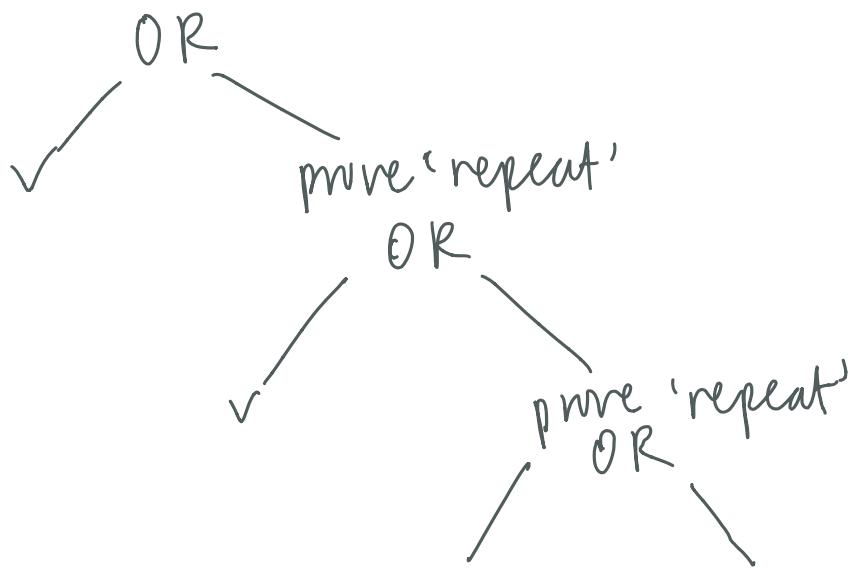
irresistible
force

? - repeat, read(x), write(x), nl, fail.

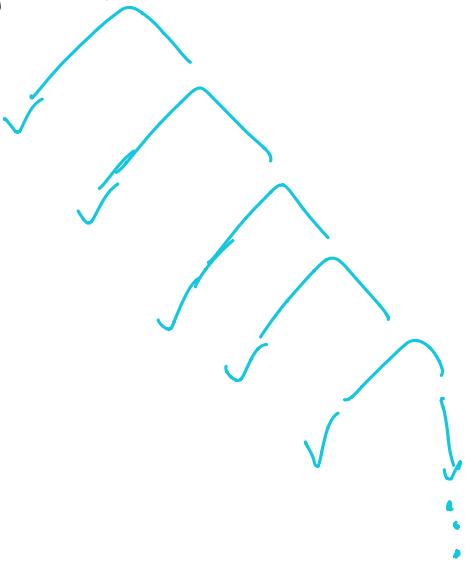
immutable
object

infinite loop, continuously copies data from terminal
to display.

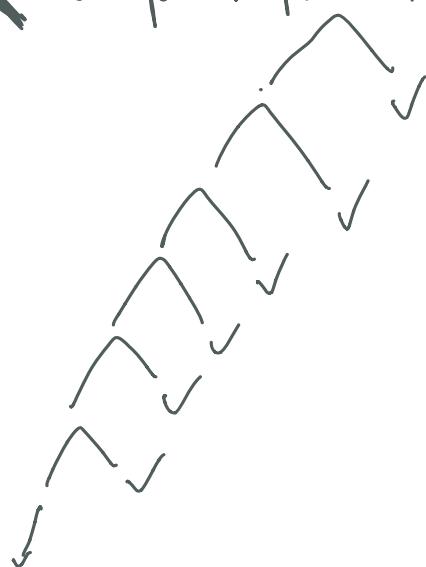
How to prove repeat



repeat proof tree



X creapeat proof tree



creapeat :- creapeat
creapeat.

Moral of the story: order matters

Prolog unification

= Two-way pattern matching

? - $p(x, f(x))$
 data structure
 $f(x) \neq g(B)$

$p(A, g(B)) :- q_1(B, A).$

$p(A, f(c)) :- q(g(c, A))$

$p(h(I), J) :- q(J, I)$

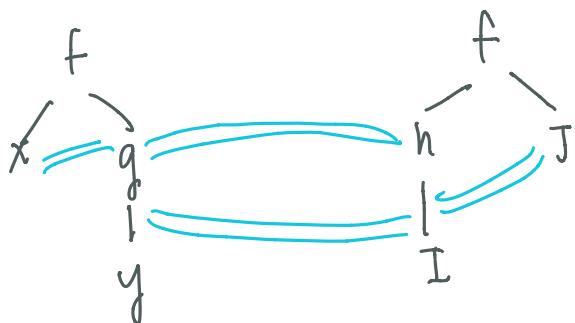
$x = h(E), f(y) = J$

Unification

- make 2 terms identical by replacing them / by substituting values for variables uniformly

$$\begin{array}{ccc} f(x, g(x)) & & f(h(J), I) \\ \Downarrow & \left\{ \begin{array}{l} x : h(J), I : g(y) \\ \text{maps logical variables to terms} \end{array} \right\} & \Downarrow \\ f(h(W), g(Y)) & & f(h(J), g(Y)) \end{array}$$

(partial function)



$$p(X, X) \quad ? - p(f(g(A)), h(J)), f(X, h(g(z))))$$

works! unification

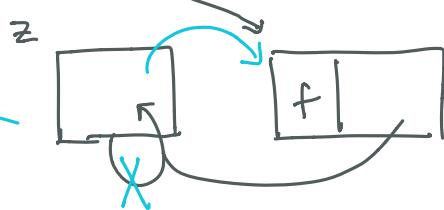
$p(X, X)$

? - $p(f(g(A)), h(J)), f(X, \textcircled{u} g(z)))$

wouldn't work

$p(x, x)$

? - $p(z, f(z)).$



- will give unbound variable a pointer to bound value
- $f(f(f(\dots$ goes on forever
↳ infinite term, a common problem in Prolog

? - $p(L, [-|L]),$

? - $L = [-|L],$

$=^1 (x, x).$ infinite loop

$X = X.$

addition in Prolog from last week errr:

? - $lA(A, A).$

$A = \text{succ}(\text{succ}(\text{succ}(\dots)) \dots$ infinity

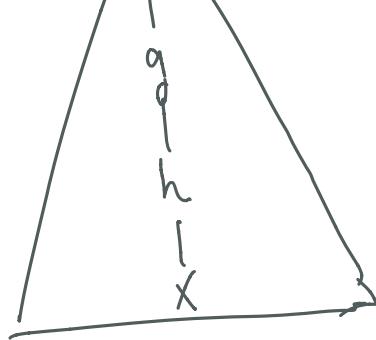
* don't write solution that leads to infinite terms

unify-with-occurs-check($X, f(\overbrace{g(h, Cx)}^B))$

$A = B$, except it returns to create infinite terms



checks that x
doesn't appear



$$\text{unify-with-owners_check}(A, B) = O(\max(|A|, |B|))$$
$$A = B \quad = O(\min(|A|, |B|))$$

- solution: never write (x, x) , always use unique variables
 - very expensive to implement checking

Transitive closure of a relation

$\text{pr}(\text{cs}32, \text{cs}131)$

$\text{pr}(\text{cs}33, \text{cs}131)$

$\text{pr}(\text{cs}35l, \text{cs}131)$

\vdots

$\times 30,000$

$\text{ipr}(A, C) :- \text{pr}(A, B), \text{pr}(B, C).$

$\text{ipr}(A, Z) :- \text{pr}(A, B), \text{ipr}(B, Z).$

Even more efficiently:

$\text{ipr}(A, Z) :- \text{pr}(A, B), (\text{pr}(B, Z); \text{ipr}(B, Z)).$

Equivalent without semicolon:

$\text{ipr}(A, Z) :- \text{pr}(A, B), \text{prh}(B, Z).$

$\text{prh}(A, B) :- \text{pr}(A, B).$

$\text{prh}(A, B) :- \text{ipr}(A, B).$

?- $\text{ipr}(\text{cs}31, Z)$

$Z = \text{cs}131;$

$Z = \text{cs}111;$

:

?- $\text{ipr}(A, \text{cs}231).$

$\left\{ \begin{array}{l} \text{pr}(A, B) \\ \text{prh}(B, \text{cs}231) \end{array} \right.$

runs really slowly
should not issue this goal

can you prove this
if false

?- $\neg \text{pr}(\text{dance}101, \text{cs}131).$ -

Yes.

- no way in Prolog to say "not"
- can only tell Prolog true things, not false

CWA = closed world assumption

- "everything that I don't tell you is true must be false"
- can't make this assumption in Prolog

How to make Prolog program go faster

$p(X, Y, Z, W) :- \text{gen}(X, Z, W, Q), \text{member}(X, W),$

$\text{test}(Y, Z, Q, X)$

filter

expensive

always
of ground terms { $W = [a, b, c, d, e]$
 $X = b$

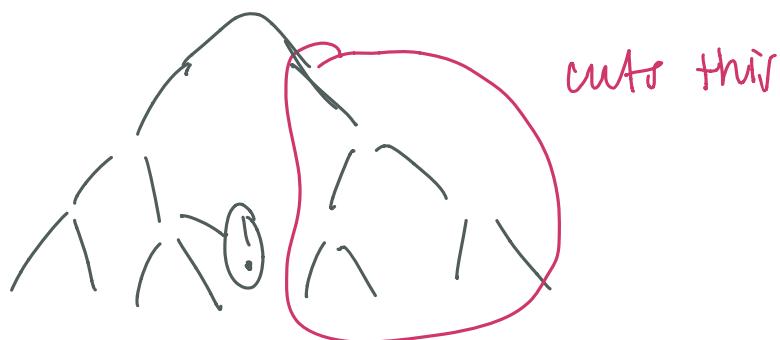
- still not as fast as possible
- member only needs to be run once

`member(X, [X | _])`

`member(X, [_ | L]) :- member(X, L).`

`memberchk(X, [X | _]) :- !.` cut - if we backtrack to this we immediately skip the predicate

`memberchk(X, [_ | L]) :- memberchk(X, L).`



- now memberchk only runs once, if we backtrack to it, we skip the calling predicate
- go to caller's caller predicate

alternative implementation to memberchk

`once(P) :- P, !.`

`memberchk(X, L) :- once(member(X, L)).`

meta-predicate: fails when P succeeds, succeeds when P fails

$\text{not}(P) :- P, !, \text{fail}$

$\text{not}(_)$.

?- $\text{not}(3 \text{ is } 4 + 7)$
 fail

Yes.

?- $\text{not}(\text{pr(dance101, cs131)})$.

Yes.

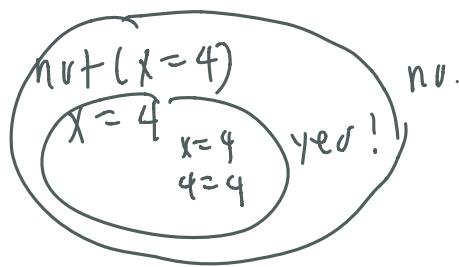
* this implementation of not doesn't always work

?- $X=3, \text{not}(X=4)$

Yes.

?- $\underbrace{\text{not}(X=4)}, X=3$

No.



- $\text{not} \neq \text{not}$
- $\backslash + P :- P, !, \text{fail}$ is built into prolog

Mathematical philosophy: $\vdash \equiv \models$

$\models P \equiv "P \text{ is true}"$

$\vdash P \equiv "P \text{ is provable}"$

$X \equiv Y \equiv "X \text{ is the same as } Y"$

$\nvdash P \equiv "P \text{ is not provable}"$

★ \+ (_) f(p) \+ p