

Confidence Intervals for Mean for Exponential Distribution

$$P(c_1 < \chi_{2n}^2 < c_2) = \gamma$$

$$c_2 = (\chi_{2n}^2)^{-1} \left[\frac{\gamma+1}{2} \right] \quad \text{and} \quad c_1 = (\chi_{2n}^2)^{-1} \left[\frac{1-\gamma}{2} \right]$$

$$P(2 \sum X_i / c_2 < \mu < 2 \sum X_i / c_1) = \gamma$$

$$\text{Expected length is } E[L] = 2n\mu \left(\frac{1}{c_1} - \frac{1}{c_2} \right).$$

Attempt to optimize c_1 and c_2 in both cases above using simple grid search. Start with c_1 and c_2 as defined above, then decrease both probabilities by 0.0001 until $\left[\frac{1-\gamma}{2} \right]$ is 0, then pick c_1 and c_2 with smallest confidence interval. For example for $\gamma = 0.95$ this will give 250 (0.025/0.0001) pairs of c_1 and c_2 to search. Among those 250 pairs the one that has the smallest $c_2 - c_1$ is selected.