

Session 16 Assignment 1 Question

Problem Statement 1:

A test is conducted which is consisting of 20 MCQs (multiple choices questions) with every MCQ having its four options out of which only one is correct. Determine the probability that a person undertaking that test has answered exactly 5 questions wrong.

Solution:

$$n = 20, n - k = 5, k = 20 - 5 = 15$$

The probability of success = probability of giving a right answer = $s = \frac{1}{4}$

Hence, the probability of failure = probability of giving a wrong answer = $1 - s$

$$= 1 - \frac{1}{4} = \frac{3}{4}$$

When we substitute these values in the formula for Binomial distribution we get,

$$\text{So, } P(\text{exactly 5 out of 20 answers incorrect}) = C(20, 5) * \left(\frac{1}{4}\right)^{15} * \left(\frac{3}{4}\right)^5$$

$$P(5 \text{ out of } 20) = \frac{(20*19*18*17*16)}{(5*4*3*2*1)} * \left(\frac{1}{4}\right)^{15} * \left(\frac{3}{4}\right)^5$$

$$= 0.0000034 \text{ (approximately)}$$

Thus the required probability is 0.0000034 approximately.

Problem Statement 2:

A die marked A to E is rolled 50 times. Find the probability of getting a “D” exactly 5 times.

Solution:

$$n = 50, k = 5, n - k = 45.$$

The probability of success = probability of getting a “D” = $s = 1/5$

Hence, the probability of failure = probability of not getting a “D” = $1 - s = 4/5$.

Problem Statement 3:

Two balls are drawn at random in succession without replacement from an urn containing 4 red balls and 6 black balls.

Find the probabilities of all the possible outcomes.

Solution:

First determine the probabilities of the events.

Events	Probability
RR	$(4/10)(3/9) = 2/15$
RB	$(4/10)(6/9) = 4/15$
BR	$(6/10)(4/9) = 4/15$
BB	$(6/10)(5/9) = 1/3$

The probability of 0 black balls (RR) is $2/15$

The probability of 1 black ball is (RB or BR) is $4/15 + 4/15 = 8/15$

The probability of 2 black balls (BB) is $\frac{1}{3}$

If Z is the random variable representing the number black balls. The probability distribution will be :

Z	P(z)
0	$\frac{2}{15}$
1	$\frac{8}{15}$
2	$\frac{1}{3}$

Notice that the sum of the probabilities = $\frac{2}{15} + \frac{8}{15} + \frac{1}{3} = 1$