

HOME WORK № 4

Instructions

1. Under any circumstances the deadline will NOT be extended.
2. Code should be written in python language in a Jupyter notebook .
3. Unless mentioned in the questions, feel free to use built-in python functions
4. Upload Jupyter notebook and html file of the Jupyter notebook in canvas. No other forms submissions is considered as valid submission. Make sure to have the output of the required cells of the jupyter notebook and its html version before making submission.
5. Plagiarism is unacceptable and we have ways to find it. So do not do it.
6. There is one problem in this assignment for 100 points.
7. The code should readable with variables named meaningfully.
8. Write test cases wherever required so that they cover all scenarios.

Problem 1

Fill in the methods of the Tree class. All the methods that change the tree should maintain the Binary Search Tree (BST) invariant.

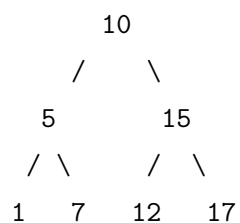
Note:

1. Diameter of a tree is the length of the longest path in the tree.
2. The `__contains__` "dunder" method returns True if an element is present in the tree and False otherwise.
By writing the `__contains__` "dunder" method you can use Python's 'in' syntax: '7 in tree' and '11 not in tree'.
3. `insert()` and `delete()` don't return anything--they just update the tree. In Python, returning None corresponds to returning nothing.

4. You may assume all inputs are valid, and you don't have to perform any error handling. In particular, you may assume that all elements inserted into the tree are distinct.

Example 1:

```
>>> node1 = Node(5, Node(1), Node(7))
>>> noder = Node(15, Node(12), Node(17))
>>> t = BST (Node(10, node1, noder))
```



```
>>> t.max()
17
```

```
>>> 15 in t
True
```

```
>>> 100 not in t
True
```

```
>>> t.height()
2
```

```
>>> t.diameter()
4
```

```
>>> t.inorder()
[1, 5, 7, 10, 12, 15, 17]
```

```
>>> t.preorder()
[10, 5, 1, 7, 15, 12, 17]
```

```
>>> t.postorder()
[1, 7, 5, 12, 17, 15, 10]
```

```
>>> t.level_order()
[10, 5, 15, 1, 7, 12, 17]
```

Example 2:

```
t2 = BST (Node (10, None, Node(15)))
```

```

  10
   \
   15

```

```
t2.insert(12)
```

```

  10
   \
   15
  /
 12

```

```
>>> t2.insert(16)
>>> t2.insert(9)
>>> t2.insert(11)
```

```

  10
 /  \
9    15
 /  \
12   16
 /
11

```

```
>>> t2.level_order()
[10, 9, 15, 12, 16, 11]
```

```
>>> t2.inorder()
[9, 10, 11, 12, 15, 16]
```

```
>>> t2.preorder()
```

```
[10, 9, 15, 12, 11, 16]
```

```
>>> t2.postorder()
```

```
[9, 11, 12, 16, 15, 10]
```

```
>>> t2.diameter()
```

```
4
```

```
>>> t2.delete(10)
```

```
    11
   /  \
  9    15
   /  \
  12   16
```

Write code following the below format:

```
1
2 class Node:
3
4     def __init__(self, data, left=None, right=None):
5         self.data = data
6         self.left = left
7         self.right = right
8
9
10 class BST:
11
12     def __init__(self, node):
13         self.root = node
14
15     def __contains__(self, data):
16         pass
17
18     def insert(self, data):
19         pass
20
21     def delete(self, data):
22         pass
23
24     def preorder(self):
25         pass
```

```
26
27     def postorder(self):
28         pass
29
30     def inorder(self):
31         pass
32
33     def level_order(self):
34         pass
35
36     def diameter(self):
37         pass
38
39     def height(self):
40         pass
41
42     def max(self):
43         pass
```
