1 Clustering problem

The Clustering problem is NP-hard [1]. It is defined as follows: There is a finite set X of objects (|X| = N), a distance $d(x, y) \in \mathbb{Z}_0^+$ for each pair $x, y \in X$, and two positive integers K and B. Is there a partition of X into disjoint sets X_1, X_2, \dots, X_K such that, for all pairs $x, y \in X_i$, $d(x, y) \leq B$, where $1 \leq i \leq K$?

2 Experiments

There were 10 randomly generated problem instances for each problem. Details of the generating procedure, as well as configurations, are described in the GitHub repository.¹. Problems' specification are depicted in relevant tables.

3 Results

Table 1 presents the experiment results of the Clustering problem. DLV achieved the best results in all problems. WMaxSAT was the second losing against Clingo in the first two problems only. Similarly, cmodels outperformed Clingo for larger problems but lost completly againts WMaxSAT. Eventually, smodel performed very poorly compared to other solvers.

Note that in Table 1, 2, 3, 4, and 5, TL denotes the time limit that was 240 s in every experiment. The best results are marked in bold.

Table 1: The Clustering problems' specification and the results. *Dec.* denotes a *decision*.

| Problem | N | K | В | Dec. | Clingo | DLV | smodels | cmodels | ${\bf WMaxSAT}$ |
|---------|------|---|----|------|---------------------|---------------------|---------------|-------------|-----------------|
| p1 | 992 | 5 | 45 | Yes | 5.81 s | 1.49 s | TL | 7.12 s | 5.04 s |
| p2 | 992 | 5 | 44 | No | $5.86 \mathrm{\ s}$ | $1.70 \mathrm{s}$ | TL | $8.31 \ s$ | 5.23 s |
| p3 | 1271 | 5 | 49 | Yes | 11.25 s | $2.32 \mathrm{s}$ | 58.28 s | $9.50 \ s$ | 6.42 s |
| p4 | 1271 | 5 | 48 | No | 11.29 s | $2.40 { m s}$ | TL | 10.93 s | 6.74 s |
| p5 | 1401 | 5 | 43 | Yes | 15.23 s | $2.92 \mathrm{s}$ | TL | $16.01 \ s$ | $9.18 \ s$ |
| p6 | 1401 | 5 | 42 | No | 15.36 s | $3.25 {\rm \ s}$ | TL | 17.88 s | $9.67 \ s$ |
| p7 | 1887 | 4 | 55 | Yes | 31.37 s | 4.83 s | 170.16 s | 19.58 s | $9.30 \ s$ |
| p8 | 1887 | 4 | 54 | No | 31.43 s | $4.91 \mathrm{s}$ | TL | 21.09 s | $9.68 \ s$ |
| p9 | 2223 | 4 | 57 | Yes | 51.63 s | $6.73 \mathrm{\ s}$ | 225.95 s | 25.21 s | 11.56 s |
| p10 | 2223 | 4 | 56 | No | 51.79 s | $6.91 \mathrm{\ s}$ | TL | 27.26 s | 12.19 s |

References

[1] Peter Brucker. On the complexity of clustering problems. In Optimization and Operations Research: Proceedings of a Workshop Held at the University of Bonn, October 2–8, 1977, pages 45–54. Springer, 1978.

¹https://github.com/lazarow/ASP-via-WMaxSat

Table 2: The Longest Path Problem' results.

| Problem | V | E | Clingo | DLV | smodels | ${\bf WMaxSAT}$ |
|---------|----|-----|-----------|---------------|----------|---------------------|
| p1 | 30 | 120 | 88.87 s | 50.70 s | 48.31 s | 38.33 s |
| p2 | 30 | 120 | 47.55 s | $_{ m TL}$ | 39.05 s | $0.98 \mathrm{\ s}$ |
| p3 | 30 | 120 | 62.83 s | 22.57 s | 25.45 s | $0.58 \mathrm{\ s}$ |
| p4 | 30 | 120 | 110.06 s | 138.93 s | 45.10 s | TL |
| p5 | 30 | 120 | 58.22 s | TL | 39.13 s | 110.95 s |
| p6 | 30 | 110 | 49.28 s | TL | 22.36 s | 11.58 s |
| p7 | 30 | 110 | 48.96 s | 4.85 s | 28.90 s | 25.60 s |
| p8 | 30 | 110 | 56.92 s | TL | 24.60 s | 10.68 s |
| p9 | 30 | 110 | 36.07 s | 131.07 s | 19.49 s | $2.99 \mathrm{\ s}$ |
| p10 | 30 | 110 | 76.20 s | TL | 56.98 s | $1.44 \mathrm{\ s}$ |

Table 3: The Max Cut Problem' results.

| Problem | V | E | Clingo | DLV | smodels | WMaxSAT |
|---------|----|-----|---------------|---------------------|---------------|---------------------|
| p1 | 70 | 130 | 52.06 s | 2.77 s | TL | 2.61 s |
| p2 | 60 | 130 | 96.16 s | $1.62 { m s}$ | $_{ m TL}$ | $3.20 \ s$ |
| p3 | 40 | 160 | $_{ m TL}$ | $_{ m TL}$ | $_{ m TL}$ | 4.55 s |
| p4 | 30 | 170 | 159.75 s | $_{ m TL}$ | 67.00 s | $3.05 \mathrm{s}$ |
| p5 | 30 | 190 | TL | $_{ m TL}$ | 101.91 s | 2.15 s |
| p6 | 40 | 180 | 197.72 s | 77.71 s | $_{ m TL}$ | 1.83 s |
| p7 | 70 | 140 | 54.87 s | $0.49 \mathrm{s}$ | $_{ m TL}$ | $2.59 \ s$ |
| p8 | 30 | 150 | 85.58 s | $_{ m TL}$ | 40.12 s | 2.99 s |
| p9 | 30 | 180 | 159.66 s | $_{ m TL}$ | 49.97 s | 2.62 s |
| p10 | 75 | 150 | TL | $2.31 \mathrm{\ s}$ | TL | $2.44 \mathrm{\ s}$ |

Table 4: The Minimum Cover problems' results.

| Problem | Clingo | DLV | smodels | ${\rm WMaxSAT}$ |
|---------|----------------------|---------------------|-----------|---------------------|
| p1 | $55.37 \mathrm{\ s}$ | $0.09 \mathrm{\ s}$ | 136.66 s | 1.41 s |
| p2 | 125.04 s | $0.82 \mathrm{\ s}$ | 105.79 s | 5.31 s |
| p3 | $14.55 \ s$ | $0.06 \mathrm{\ s}$ | 36.16 s | $0.54 \ s$ |
| p4 | 39.84 s | $0.29 \mathrm{\ s}$ | 39.63 s | $1.27 \ s$ |
| p5 | $20.80 \ s$ | $0.06 \mathrm{\ s}$ | 20.19 s | $0.68 \mathrm{\ s}$ |
| p6 | 79.50 s | $0.97 \mathrm{\ s}$ | 233.18 s | 1.14 s |
| p7 | 146.15 s | $1.36 \mathrm{\ s}$ | 219.74 s | 5.56 s |
| p8 | TL | $0.22 \mathrm{\ s}$ | 153.91 s | $0.89 \ s$ |
| p9 | TL | $1.03 \mathrm{\ s}$ | 133.55 s | 4.54 s |
| p10 | TL | $1.10 \mathrm{\ s}$ | 219.84 s | $5.43 \mathrm{\ s}$ |
| | | | | |

Table 5: The Minimum Test Set problems' results.

| Problem | Clingo | DLV | smodels | WMaxSAT |
|---------|--------------------|---------------------|---------------|---------------------|
| p1 | 90.06 s | $6.80 \mathrm{\ s}$ | $_{ m TL}$ | 6.74 s |
| p2 | 67.57 s | 25.33 s | TL | 15.26 s |
| p3 | 60.13 s | 4.66 s | TL | 6.76 s |
| p4 | 54.76 s | $5.01 \mathrm{\ s}$ | TL | $6.41 \ s$ |
| p5 | $84.53 \ s$ | 40.62 s | $_{ m TL}$ | 16.20 s |
| p6 | 54.26 s | 8.30 s | TL | $9.55 \ s$ |
| p7 | 65.53 s | $5.37 \mathrm{\ s}$ | TL | $6.51 \ s$ |
| p8 | 88.95 s | $16.61 \ s$ | TL | 11.26 s |
| p9 | 75.27 s | 18.12 s | TL | 11.15 s |
| p10 | $57.64~\mathrm{s}$ | $5.08~\mathrm{s}$ | TL | $5.41 \mathrm{\ s}$ |