pr2_ii_math548_midterm_Lazizbek

March 19, 2024

1 Math 548, Midterm. Problem 2. LS

Problem 2

Solve the following systems of linear equations with the Jacobi iteration method using the initial guess as [0, 0, 0].

- In each case, will the Jacobi iteration converge to a solution? Give the justification for your answer?
- If yes, find the solutions.

ii.

```
[ 8 3 2] [x1] [ 13]
[ 1 5 1] [x2] = [ 7 ]
[ 2 1 6] [x3] [ 9 ]
```

2 Finding eigenstuff of a matrix

Source:

3 Solving Ax=b matrix equation

E-vector [[-0.89442719 -0.4472136]

[0.4472136 -0.89442719]]

Source:

```
#Problem 2. (ii)
```

To check with the actual(real) solution, here, I'm giving the real solution as well:

Real solution:

[1. 1. 1.]

Using Jacobi Iteration:

```
[]: A = np.array([[8, 3, 2],
                  [1, 5, 1],
                  [2, 1, 6]])
    L = np.array([[ 0, 0, 0],
                  [1, 0, 0],
                  [1, 1, 0]])
    D = np.array([[8, 0, 0],
                 [0, 5, 0],
                  [0, 0, 6]])
    U = np.array([[0, 3, 2],
                  [0,0,1],
                  [0,0,0]])
    D_inverse = np. linalg. inv(D)
    b = np.transpose(np.array([ 13, 7, 9]))
    D_inverse_b = np.dot(D_inverse, b)
    BJ = np.dot(-D_inverse, L+U)
    w,v=eig(BJ)
    print('BJ evalues:', w)
    x0 = np.transpose(np.array([ 0,  0,  0]))
    x = list();
    x.append(x0)
```

```
for i in range(5):
    x1 = np.dot(BJ, x0)+ D_inverse_b
    x0 = x1
    x.append(x1)
Aproximations = np.array(x)
print(Aproximations)
# print((2.083**2 + 2.312**2)**(1/2))
```

```
BJ evalues: [-0.44378452 0.26976158 0.17402294]
[[0. 0. 0. ]
[1.625 1.4 1.5 ]
[0.725 0.775 0.99583333]
[1.08541667 1.05583333 1.25 ]
[0.9165625 0.93291667 1.143125 ]
[0.989375 0.9880625 1.19175347]]
```

Also pay attention that the spectral radius of matrix BJ, P(BJ) = 0.44378452 < 1, Jacobi Iteration does converge.

```
[]: # !jupyter nbconvert --to pdf /content/Math548_hw6_Lazizbek.ipynb
```