Capital Market & Investment – FINC

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Overview of financial markets

- Financial market: venues for allocating securities to fund and facilitate production and consumption
- Financial securities: standardized contracts (assets), issued by firms or governments, that pay cash to their owners and are usually transferable (tradable)
- Primary markets: Firms/government issue securities to fund productive business activities
- Secondary markets: Investors reallocate securities to fund consumption

Functionality of Financial Market

- Capital Allocation: access to funding, external finance, internally generated fund
- Consumption smoothing: allow people to consume even they are not working
- Risk Sharing: use diversification to reduce investor's riks
- Price discovery: Market price indicate where capital is / is not needed

Tobin's Q:
$$Q = \frac{\text{firm market value}}{bookvalue}$$
 $\begin{cases} Q > 1, & \text{more investment needed} \\ Q < 1, & \text{selling assets to increase value} \end{cases}$ • Key point: when making investment, we analyse $Q = \frac{1}{2} \frac{1}$

Primary and Secondary Market

- Primary: Governments and firms issue securities to investors
- Secondary: Trading of existing securities on exchanges

Primary Market study: Eventbrite

• IPO

Before IPO: positive gross profit, fast growth, small labor force

files a Form S-1 registration statement with the SEC SEC then has a cooling off period when it conduct investigattion Underwriter then creates a draft prospectus to take on a "road show" underwriter and company determine final IPO price based on roadshow Syndicate then allocates shares to investors

first day of trading: investing public can first buy stock on an exchange

IPO with SEC in Sep 20, $2018 \longrightarrow 10M$ shares for \$230M IPO performance: Offering share price is \$23, above expected \$19 - \$21 6 banks are underwriter

• Detail Analysis:

Procedures:

Eventbrite sold 10M shares (13% of 76M outstanding) Total capital raised in 12 years of prior funding is \$330M Buyers of the 10M shares are risk sharing

- Underwriter: help company determine amount of money to be raised
- underwriting agreement: is firm commitment where underwriter agrees to assume risk of entire inventory of stock issued in the IPO and the sale of the stock to the public at the
- Syndicate: a group of underwriters that share in the risk of the IPO offering

Secondary Market Study: Eventbrite

• None

Motivation for company to go public

- · Raise money
- Provide exit for shareholders
- Use publicity to spur growth
- Provide executives with incentives

Types of investors

- Individual Investors
- Corporations
- Institutional investors

Case Study: Investment Decision

- Key formula: Assets = Liabilities = Debt + Equity
- Key point: when making investment, we analyse the return based on our original Equity
- Risk: = "standard deviation of return"
- Leverage: the ratios of the borrow amount to the equity \$100 in fund, with \$20 net worth leverage ratio is 4, portfolio is 5 times as volatile

Valuation and returns in investment

- Payoffs: payment amount received (not return, don't care about gains or losses)
- Required returns: based on market condition
- Expected returns: based on analysis

Security types:

- Bonds: lend money to a firm / government
- stocks: own part of the firm
- derivatives: based on other assets Commercial Paper: unsecured (no collateral) short-term debt that is often rolled over

Case study: Lehman Brothers

- Before crisis: leverage: $\begin{cases} 20:1 & market \\ 31:1 & book \end{cases}$
 - the firm decide to give out dividend and increase ratio, to give positive signal
- historical event: Fed bail out Bear Stearns give people the impression that even if bad things happened, the Fed would come out and help
- Net present value, prices (what you pay) vs value (what you get) • investment decision criteria: expected return v.s. required return / hurdle rate(from similar assets
- What happened: filed Chapter 11 bankruptcy on Sep 15, 2008 Lehman's key businesses were sold CalPERS lost \$300M

Fixed Income - Bond Market Study

Bond Market size overview

• Implication on the rates: Long rate predicts economic trend

Fixed Income Market in US

- US Treasure: Federal Debt: T-bills, notes, bonds
- Mortgage Bonds: GNMA, FNMA, FHLMC
- Corporates
- Municipal bons:
- Agencies and GSEs:
- Private Label Backed (ABS):
- Money Markets:
- Repurchase Agreement Market (REPO):

Detail Calculation: prices and yields

• Yield (YTM): is the IRR calculated based on prices and cash flow (can change) need to notice the compounding / reinvestment period

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Bond Risk

- Interest rate risk: different maturity is different to the impact of interest rate
- default risk
- Term structure / yield curve:

vtm: vield to maturity

- what is it: The internal rate of return, calculated each time with market condition (usually calculated based on semi-annual compounding)
- When interest rate is 1. also semi-annual compounding and 2. remains the same across time frame, ytm equals to interest rate.
 - A situation when ytm \neq interest rate: interest rate are different across time-frame interest rate (from different time frame) \rightarrow bond price \rightarrow ytm
- Yield is therefore a somewhat a standardized measure of interest rate / market trend. We
 can say that ytm is a indicator for interest rate, which is an indicator for market trend
- Therefore: YTM offers us a convenient way to calculate bond price (though the yield is derived from interest rate, the 2 results should match)
- TODO: Input factor: Maturity Output factor: Yield and bond price: higher yield means market investment opportunity is higher, bond price is lower

yield curve

- Shape: x-axis: maturity; y-axis: yield
- Trend: a growing trend, but grow gradually slowly
- Interpretation:

for longer maturity, people is asking for higher yield to compensate the risk; as maturity gets longer, yield is changing less, meaning that the risk change is less for the same unit

• Different value of yield curve: yield curve moves up: rate for lending and borrowing is high, economic is less active; yield curve moves down, rate is less, economic is more active.

Duration - price sensitivity to yield change

- Shape: x-axis: yield; y-axis: bond price
- Trend: a decreasing trend, the decrease get slows
- A general characteristic: maturity higher, coupon rate lower, yield lower → duration is lower
- 2 types of duration: $\begin{cases} \text{MaD: weighted average of maturity} \\ \text{MoD: MaD}/(1+\text{ytm}/2) \end{cases}$
- From MoD to predict price change: MoD*change in ytm = price change percentage

convexity - The rate of change of duration

• it is decreasing, meaning that duration is growing in a slower speed

Application of duration:

- The century bond: due to convexity, the duration of a century bond is not that bad
- And because of convexity, the duration is lower in higher yields ()
- A shorter duration bond, will have a large cashflow more nearer than a long duration bond. This cash flow is subject to the discount of yield.
- Scenario1: looks yield from low to high: a little change in yield at first, will introduce a huge change in longer duration bond's price, because its future great amount of cash flow is discounted a lot. While shorter duration bond is less impacted. A change in yield at a larger frame, will inpose a same size of effect on short duration bond, but since long duration bond have been discounted a lot, it is less depreciated because the long-maturity part's present value barely change, and the short-maturity part have little cash flow that not gonna impact a lot
- Scenarios 2: looks yield from high to low. The longer duration bond gets a quicker boost in rising the value, for the reason that it provides a reliable, stable cash flow in the future.

Quantitative Finance – Derivatives

Time value of money

- money has time value, because we can reinvest them
- always picture a timeline in thinking about this problem

Interest

- The easiest way to make money is by earning interest from the bank
- simple interest rate (return calculation): $a_t = a_0 * (1 + it)$
- compound interest rate (keep reinvest): $a_t = a_0(1+i)^t$
- effective interest rate during a period: $i = \frac{a_n a_{n-1}}{a_{n-1}}$
- nominal rate of interest: $i^{(m)}$, meaning that this interest i is paid m times a year an amount of $\frac{i^{(m)}}{m}$ will be paid at each time interval, therefore at the end $=(1+\frac{i^{(m)}}{m})^m$ let m goes to infinity, we have the continuous form $(1+\frac{r}{m})^{mt} \longrightarrow e^{rt}$

Annuities and Perpetuities

- annuity: fixed payment at each time point annuity-immediate: payment at the end of interval annuity-due: payment at the beginning of interval
- perpetuities: fixed payment at each time point, until infinity perpetuity-immediate: payment at the end of interval perpetuity-due: payment at the beginning of interval

Bonds: a fixed income instrument

- market graph of bonds: what kinds of bonds are out there
- zero coupon bond: no coupon payment, only pay face value at maturity (treat as discount) zero rate: the annualized rate of return (annual compound) $\longrightarrow B(t,T)(1+R(t,T))^{T-t}=1$

continuous zero rate: $\longrightarrow B(t,T)e^{(T-t)R(t,T)}=1$ [treat R(t,T) as an interest rate] k-times per year: $\longrightarrow B_{(t,T)}(1+\frac{R_{(r,T)}}{m})^m(T-t)=1$

• Bond with coupon: pay at specific time

Yield-to-Maturity: the interest rate that makes present value of cash flow equals bond price

or we can say that the YTM is the IRR at this point: internal rate of return it tells us the interest rate that this investment is representing, so that we can compare

Annual Coupon Bond: $P = \sum \frac{CF_t}{(1+y)^t}$ Semi annual coupon bond: $P = \sum \frac{CF_t}{(1+\frac{y}{h})^{2t}}$

So what happened in the market \longrightarrow we calculate the bond price, by the risk-free rate Therefore it is easy to imagine:

if risk-free rate goes up, the current bond price should drop if risk-free rate goes down, the current bond price should rise In short, the bond price is negatively correlated to the YTM

It depends on how we structure the dependent variable and independent variables:

- 1. Calculate the bond price: the DV is bond price, IDV is the interest rate, negative correlated.
- 2, Calculate YTM: the DV is YTM, IDV is bond price, if bond price is high, meaning the YTM must be low
- Relationship between zero coupon bond and coupon bond:

When a coupon bond pays no coupon, it is the same as zero coupon bond \longrightarrow same price and YTM

With coupon bond introduce coupon, we have 2 dimension to interpret the results:

- 1. how the price will change: with introduction of future cash flow, interest rate does not change, price will rise; with price rise, the YTM will drop
- 2. how the YTM will change: not a good direction, stick to PRICE \longrightarrow YTM path
- Since the zero coupon bond has a higher YTM than coupon bond, it is some how confusing because we may think the coupon bond gives us more return.
- We introduce the "Par Yield" to do standardization on the returns:
- Par Bond: the price = face value \longrightarrow issue at par \longrightarrow YTM = annual coupon rate Par Yield: when a bond is issue at par, the coupon rate (annualized return) is equal to YTM (calculated annualized return)
- Dollar Duration: the $\frac{dP}{dy}$ the derivatives of price w.r.t. YTM Modified Duration: $-\frac{1}{P}\frac{dp}{dy}$, Dur normalized by price Dollar Value of 1 basis point (DV01): = $Dur \cdot (-1bp)$

At a specific price level, the Dollar Duration Dur, decrease as:

- 1. maturity increase (Dur is a price sensitivity measure to yield, with T goes up, it is more sensitive)
- 2. coupon increases (1. more money to discount, more sensitive. 2. more coupon means price up, then more sensitive)
- 3. YTM decrease (look at the graph, when YTM is small, it is steeper)

Forward Rates

 Diagram and calculation: separate the time into different intervals, make investment using respective rates

Futures

Options

* Memoryless:

Bonds

* Memoryless:

Financial Assets: Derivatives

Forwards / Futures

- Futures: Traded in the exchange, so basically standardized contract
- Forwards: customized
- Keywords: strike price, maturity day, long, short

Agencies

- Clearing house: ensure trader fulfill obligations
- Margin: Trader deposit margin to fulfill obligations: Initial margin; Maintenance margin; Variation margin;

Options

- Vanilla Option / European Option: fixed maturity date, strike price
- American Option: can exercise before maturity date
- Bermudan Option: can exercise on pre-determined date
- Barrier Option: can exercise once cross the barrier level: up and out, down and out, up and in, down and in
 - 1) Callable Bull: if always bull, then it is valid (never drop down barrier) [down and out]
- 2) Callable Bear: if always bear, then it is valid (never go up barrier) [up and out]
- Asian Option: the payoff determined by average price of pre-set period of time

Option strategies: Notice difference between prices and payoff

- Straddle: long 1 call and 1 put with same K and T
- Strangle: long call and put with same K and T
- Bull Spread: make money when price up: Buy call with K_1 , sell call with K_2
- Bear Spread: make money when price down: Buy call with K_1 , sell call with K_2
- Butterfly: long 2 calls, short call * 2

Warrents

- equity warrants: issue by company. represent the right to subscribe to equity securities
- derivative warrants: issued by 3rd party.

Swap: 2 parties exchange financial instruments

- Interest rate swap
 A: expect Libor drops; B: expect Libor ups
 ????
- Benefit: 1) hedge against interest rate exposure; 2) leverage comparative advantage A: AAA rated company; B: BBB rated company.

 Company A will definitely have less lending interest rate in the market, in all loans But that doesn't mean company A can't do better. We can calculate the spread and see what is company A's comparative advantage, and borrow only that kind of loan, other company can use their comparative advantage P38

Financial Risk: Value at Risk

Return

• Arithmetic Return: $R_t = \frac{S_t - S_{t-1}}{S_{t-1}}$

• Log Return: $log(1+R_t) = log(\frac{S_t}{S_{t-1}}) = log(S_t) - log(S_{t-1})$

Volatility Measure

• $\sigma_s = \sqrt{\frac{1}{n-1} \sum (\mu_i - \bar{\mu})^2}$

• Then the volatility over N periods: $\sqrt{N}\sigma_s$

VaR: Value-at-Risk

• if there is a distribution graph, starting from left to some point, this region is α

• the rest region to the right is $1 - \alpha$, stands for the confidence: 95%, 99% etc.

 $\bullet\,$ We called α as the "tail probability", since it is the worst scenario

• In a graphical sense, VaR is the p-th quantile of the PnL distribution

• "Relative VaR": E[PnL] - VaR

Modeling the PnL distribution

• The fundamental of finding VaR is to model the portfolio PnL distribution

• Parametric Approach:

Keypoint: construct the mean μ and volatility σ Approach: convert to approach "standard normal distribution"

Then we can calculate VaR; or extend this to a multi-time period scenario

• Non-Parametric Approach: Historical Simulation

1. we want to know the price at tomorrow

2. we convert the a problem: how much will the portfolio value change

3. based on past period-wise change data, we treat it as distribution

4. select the change we need

Financial Risk: Hedging, Optimal Hedging

Idea

• Hedge against a instrument that is negatively correlated to your portfolio

Quantify

 \bullet we want to minimize variance of new portfolio : S+NF, with S original portfolio

• we first construct the variance: $\sigma_s + N^2 \sigma_f + 2N \sigma_{s,f}$

• Then N can be solved by using the solution for a square equation

Coursera - Columbia - No Arbitrage

Example of using No-Arbitrage pricing:

• 1. A bond that pays A in 1 year:

Pricing 1: portfolio that: buy 1 bond, borrow $\frac{A}{1+r}$ Pricing 2: portfolio that: sell 1 bond, lend $\frac{A}{1+r}$

• 2. Use compounding interest rate for pricing:

• 3. Floating Rate Bond:

The price of a floating rate bond, is equal to, the face value.

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Cousera - Columbia - No Arbitrage in various assets

Swaps

• What is it: a trade between fixed and float rates

• Why is it: leverage relative strength, capture trends in other markets

• How does it works: do your best, borrow your weakness

1. A has relative strength in fixed rate

2. B has relative strength in floating rate

3. A will borrow fixed rate, B will borrow floating rate

4. A borrow floating from B, pays fixed to B

• How to price it: What should be the exchange rate pay to each other

1. Swap should be of 0 value to each party

2. Write the Cash Flow PV for one side

3. Set it to 0 and we calculate the payment rate

Futures

• What is it: An traded an exchange standardized contract

• Why need it: standardized, counter party risk, solved multiple price for same maturity

• How does it works: Margin call (go to initial margin), clearing house

• How to price it:

• Minimum variance hedging (since perfect hedge is impossible):

Options

• In the money, at the money, out of the money

• Put-Call Parity: call + cash = put + stock try to buy a stock, and use money to help me try to sell a stock, and hold a stock to help me $C + Ke^{-rt} = P + S$ $C + Ke^{-rt} = P + S - D$ (with dividend)

• Bounds of option prices

Binomial Tree Pricing

• 1-period Binomial Tree: price goes up and down with probabilities, allow short sell

• Multi-period Binomial Tree: extend with same prob and up/down scale

 Replications: (buying shares, investing in cash) ↔ (option) make the payoff equals

• European and American Pricing: use risk-neutral prob to price: $q=rac{R-d}{u-d}$. $C_0=rac{1}{R}[qC_u+(1-q)C_d]$