# Capital Market & Investment – FINC

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### Overview of financial markets

- Financial market: venues for allocating securities to fund and facilitate production and consumption
- Financial securities: standardized contracts (assets), issued by firms or governments, that pay cash to their owners and are usually transferable (tradable)
- Primary markets: Firms/government issue securities to fund productive business activities
- Secondary markets: Investors reallocate securities to fund consumption

### Functionality of Financial Market

- Capital Allocation: access to funding, external finance, internally generated fund
- Consumption smoothing: allow people to consume even they are not working
- Risk Sharing: use diversification to reduce investor's riks
- Price discovery: Market price indicate where capital is / is not needed

Tobin's Q: 
$$Q = \frac{\text{firm market value}}{bookvalue}$$
  $\begin{cases} Q > 1, & \text{more investment needed} \\ Q < 1, & \text{selling assets to increase value} \end{cases}$  • Key point: when making investment, we analyse  $Q = \frac{1}{2} \frac{1}$ 

### Primary and Secondary Market

- Primary: Governments and firms issue securities to investors
- Secondary: Trading of existing securities on exchanges

## Primary Market study: Eventbrite

• IPO

Before IPO: positive gross profit, fast growth, small labor force

files a Form S-1 registration statement with the SEC SEC then has a cooling off period when it conduct investigattion Underwriter then creates a draft prospectus to take on a "road show" underwriter and company determine final IPO price based on roadshow Syndicate then allocates shares to investors

first day of trading: investing public can first buy stock on an exchange

IPO with SEC in Sep 20,  $2018 \longrightarrow 10M$  shares for \$230M IPO performance: Offering share price is \$23, above expected \$19 - \$21 6 banks are underwriter

• Detail Analysis:

Procedures:

Eventbrite sold 10M shares (13% of 76M outstanding) Total capital raised in 12 years of prior funding is \$330M Buyers of the 10M shares are risk sharing

- Underwriter: help company determine amount of money to be raised
- underwriting agreement: is firm commitment where underwriter agrees to assume risk of entire inventory of stock issued in the IPO and the sale of the stock to the public at the
- Syndicate: a group of underwriters that share in the risk of the IPO offering

### Secondary Market Study: Eventbrite

None

### Motivation for company to go public

- · Raise money
- Provide exit for shareholders
- Use publicity to spur growth
- Provide executives with incentives

### Types of investors

- Individual Investors
- Corporations
- Institutional investors

### Case Study: Investment Decision

- Key formula: Assets = Liabilities = Debt + Equity
- Key point: when making investment, we analyse the return based on our original Equity
- Risk: = "standard deviation of return"
- Leverage: the ratios of the borrow amount to the equity \$100 in fund, with \$20 net worth leverage ratio is 4, portfolio is 5 times as volatile

### Valuation and returns in investment

- Payoffs: payment amount received (not return, don't care about gains or losses)
- Required returns: based on market condition
- Expected returns: based on analysis

## Security types:

- Bonds: lend money to a firm / government
- stocks: own part of the firm
- derivatives: based on other assets Commercial Paper: unsecured (no collateral) short-term debt that is often rolled over

### Case study: Lehman Brothers

- Before crisis: leverage:  $\begin{cases} 20:1 & market \\ 31:1 & book \end{cases}$ 
  - the firm decide to give out dividend and increase ratio, to give positive signal
- historical event: Fed bail out Bear Stearns give people the impression that even if bad things happened, the Fed would come out and help
- Net present value, prices (what you pay) vs value (what you get) • investment decision criteria: expected return v.s. required return / hurdle rate(from similar assets
- What happened: filed Chapter 11 bankruptcy on Sep 15, 2008 Lehman's key businesses were sold CalPERS lost \$300M

# Fixed Income - Bond Market Study

#### Bond Market size overview

• Implication on the rates: Long rate predicts economic trend

#### Fixed Income Market in US

- US Treasure: Federal Debt: T-bills, notes, bonds
- Mortgage Bonds: GNMA, FNMA, FHLMC
- Corporates
- Municipal bons:
- Agencies and GSEs:
- Private Label Backed (ABS):
- Money Markets:
- Repurchase Agreement Market (REPO):

### Detail Calculation: prices and yields

• Yield (YTM): is the IRR calculated based on prices and cash flow (can change) need to notice the compounding / reinvestment period

### **Bond Risk**

- Interest rate risk: different maturity is different to the impact of interest rate
- default risk
- Term structure / yield curve:

### ytm: yield to maturity

- what is it: The internal rate of return, calculated each time with market condition (usually calculated based on semi-annual compounding)
- When interest rate is 1. also semi-annual compounding and 2. remains the same across time frame, ytm equals to interest rate.
  - A situation when ytm  $\neq$  interest rate: interest rate are different across time-frame interest rate (from different time frame)  $\rightarrow$  bond price  $\rightarrow$  ytm
- Yield is therefore a somewhat a standardized measure of interest rate / market trend. We can say that ytm is a indicator for interest rate, which is an indicator for market trend
- Therefore: YTM offers us a convenient way to calculate bond price (though the yield is derived from interest rate, the 2 results should match)
- TODO: Input factor: Maturity Output factor: Yield and bond price: higher yield means
  market investment opportunity is higher, bond price is lower

### yield curve

- Shape: x-axis: maturity; y-axis: yield
- Trend: a growing trend, but grow gradually slowly
- Interpretation:
   for longer maturity, people is asking for higher yield to compensate the risk;
   as maturity gets longer, yield is changing less, meaning that the risk change is less for the
   same unit
- Different value of yield curve: yield curve moves up: rate for lending and borrowing is high, economic is less active; yield curve moves down, rate is less, economic is more active.

### Duration - price sensitivity to yield change

- Shape: x-axis: yield; y-axis: bond price
- Trend: a decreasing trend, the decrease get slows
- A general characteristic: maturity higher, coupon rate lower, yield lower → duration is lower
- 2 types of duration:  $\begin{cases} \text{MaD: weighted average of maturity} \\ \text{MoD: MaD}/(1+\text{ytm}/2) \end{cases}$
- From MoD to predict price change: MoD\*change in ytm = price change percentage

## convexity - The rate of change of duration

• it is decreasing, meaning that duration is growing in a slower speed

### Application of duration:

- The century bond: due to convexity, the duration of a century bond is not that bad
- And because of convexity, the duration is lower in higher yields ()
- A shorter duration bond, will have a large cashflow more nearer than a long duration bond. This cash flow is subject to the discount of yield.
- Scenario1: looks yield from low to high: a little change in yield at first, will introduce a huge change in longer duration bond's price, because its future great amount of cash flow is discounted a lot. While shorter duration bond is less impacted. A change in yield at a larger frame, will inpose a same size of effect on short duration bond, but since long duration bond have been discounted a lot, it is less depreciated because the long-maturity part's present value barely change, and the short-maturity part have little cash flow that not gonna impact a lot
- Scenarios 2: looks yield from high to low. The longer duration bond gets a quicker boost in rising the value, for the reason that it provides a reliable, stable cash flow in the future.

#### Default Risk

- Yield & Expected Return:
  - 1. yield is the promised rate of return
  - 2. expected return is the return calculated based on your expectation of the cash flow
- Relationship: yield, expected return, risk free return



risk & return in asset classes:
 stock → junk bond / high yield bond → investment grade bond → treasury

## Portfolio Choice - combine bond with stock

## Equity Valuation

- The concept of Equity: residual claim of a firm's cash flow (received after debt payout)
- CAPM model:  $k = r_f + \beta(r r_f)$
- Stock Prices vs. Values
  - 1. PRICES may differ from fundamental VALUES
  - 2. Eventually, we expect convergence  $P_n = V_n$ (market becomes efficient in n years) (basis for value investing)
  - 3. If investor don't sell the stock

$$V_0 = \frac{D_0(1+g)}{k-g} \to P_0 = \frac{D_0(1+g)}{E(r)-g}$$

we are taking the price for now see what E[r] it gives us

 $\rightarrow$  Expected return = divs yield + growth in divs  $E(r) = \frac{D_0(1+g)}{P_0} + g$ 

Things change when switch investment horizon

• Alternative method for long-run (LR) expected return: Profitability and Growth This is good for company with stable ROE but not stable dividend

When deriving the E(r) for long run: earnings yield (E/P) instead of dividend yield (D/P)Sustainable LR payout: growth =  $(1 - payout) \times ROE$ 

## Dividend Discount Model (DDM)

- Basic Idea: Value (V) equals PV of dividends Forecast cash flows Apply discount rate (k) to cash flows
- One-stage DDM required return on equity (k) is constant

stock value from future dividend  $V_0 = \frac{D_1}{1+k} + \frac{D_2}{(1+k)^2} + \ldots + \frac{D_n}{(1+k)^n}$ the difference of the 2 equations one is  $D_1$  and one is  $D_2$ Dividend grows at constant rate  $V_0 = \frac{D_0(1+g)}{1+k} + \frac{D_0(1+g)^2}{(1+k)^2} + \ldots + \frac{D_0(1+g)^n}{(1+k)^n}$  $V_0 = \frac{D_0(1+g)}{k-g}$ 

- The Multi-stage DDM: allows for multiple growth regimes
- 1. Economic Stimulus Could Produce Short-run Growth 'Sugar High'
- 2. Valuing temporarily higher (lower) growth is similar to valuing an increase (decrease) in the initial dividend (D0)

## Valuation multiples

- Advantage of multiples: Avoid directly predicting cash flows and their growth
- Disadvantages of multiples:

Incomparable k, g, and payout of comparable stocks Inability to identify pricing inefficiencies of comparables Inconsistencies across different multiples (P/E, P/B, P/S, etc.) Instability of multiples over time

• Assumption within:

Comparable assets have the same risk, CF growth, and payout as asset being valued Market pricing of comparables is efficient

• Dividend discount model (DDM) helps explain multiples (i.e., prices) g: Stock is relatively expensive because its CFs are growing faster (higher g) than similar

k: Stock is relatively expensive because its CFs are less risky (lower k, required return) than similar stocks

• Interpret P/E with the DDM

(1. P/E is price to earnings, and Dividend = Earning  $\times$  Payout

2. since the DDM gives us  $V_0 = \frac{D_0(1+g)}{k-g}$  we replace dividend and divide each side with  $E_0$   $\frac{V_0}{E_0} = \frac{Payout(1+g)}{k-g}$ , similarly, earning yield E/P is  $\frac{E_0}{V_0} = \frac{k-g}{Payout(1+g)}$ 

$$\frac{V_0}{E_0} = \frac{Payout(1+g)}{k-g} \text{ , similarly, earning yield E/P is } \frac{E_0}{V_0} = \frac{k-g}{Payout(1+g)}$$

Interpretation 1: Stocks can have high price to earnings (P/E) ratios because g is high

Interpretation 2: Stocks can have high P/E because discount rate (k) is low

Wee need to determine which factor it is that lead to a high P/E!!!

## Portfolio Optimization

• We move from long-term return to short-term return For long-term holding valuation:  $E(r) = \frac{D_0(1+g)}{P_0} + g$ 

For short-term holding valuation:  $E(r_1) = \frac{V_0(1+k)}{P_0} - 1$ 

- Sharp Ratio: the risk premium per unit of risk:  $SR_{us} = \frac{E[r_{us}] f_f}{\sigma_{us}}$ (As an investor, we always want a high sharp ratio, that's the essense of MVE)
- Mean Variance Efficient MVE: Diversification help us increase the sharp ratio (In other words, MVE is the portfolio with the highest sharp ratio) (We achieve it by adjusting the weights in different asset, and see the final outcome)
- Mean-Variance Utility:  $U_p = E(r_p) \frac{1}{2}A(\sigma_p)^2$ , with "A" being the risk aversion
- Optimal Portfolio Weights (weights in risky asset):  $w_{MVE}^* = \frac{E[r_{MVE}] r_f}{A\sigma_{MVE}^2}$

## Applying the CAPM

- CAPM: build on the idea that everyone holds the unique best portfolio. That is the market portfolio:  $SR_p \leq SR_m = \frac{E[r_M] - r_f}{\sigma}$
- Market portfolio: all risky assets held in proportion to their market capitalization
- For each asset: the weights should equate teh marginal reward-risk ratios  $E[r_i] - r_f = \beta_{i,MVE} \times (E[r_{MVE}] - r_f)$ (if one asset is "x" times riskier than the market, we require "x" times excess return)
- Market Risk Premium:  $w_M^* = \frac{E[r_m] r_f}{A\sigma_m^2} \longrightarrow \frac{E[r_m] r_f}{E[r_m]} = w_m^* A \sigma_m^2$

If keep weights in market same, then a rise in A or  $\sigma_m$  ask for higher market risk premium If keep the same expectation in market risk premium, a change in A or  $\sigma_m$  changes weights

•  $\alpha = \text{expected return} - \text{CAPM required return}$ 

### **CAPM Anomalies**

 $\bullet \ \, \text{Anomalies} \rightarrow \text{alpha:} \left\{ \begin{aligned} &\text{Size (market capitalizaion): small beats big, but this effect is eaker recently} \\ &\text{Value (B/M): high book to market ratio beats the growth} \\ &\text{Beta: low beta beats high bta in risk-adjusted return (alpha)} \\ &\text{Momentum: Past winner perform bad in the future} \end{aligned} \right.$ 

• How to quantify the effect: SMB: real excess return - theoretical return

HML (value premium): retur of high B/M - return of low B/M

Beta:

UMD Momentum: up stock - down stocks

• The Fama and French Three-Factor Model:

$$\begin{split} r_{it} - r_{f_t} &= \alpha_i^{\text{FF3}} + \beta_i \left( r_{mt} - r_{f_t} \right) + s_i SMB_t + h_i HML_t + e_{it} \\ \text{Market Factor: } MktRf_t &= r_{mt} - r_{ft} \\ \text{HML (value premium): retur of high B/M - return of low B/M} \\ \text{Beta:} \\ \text{Momentum Factor: } UMD_t &= r_{Ut} - r_{Dt} \\ \underline{r_{it} - r_{f_t}} &= \alpha_i^{\text{FF3}} + \beta_i \left( r_{mt} - r_{f_t} \right) + s_i SMB_t + h_i HML_t + e_{it} \end{split}$$

#### asset excess return

Coefficients  $s_i$  and  $h_i$  are size and value betas (loadings) Small (big) firms usually have positive (negative)  $s_i$  values Value (growth) firms usually have positive (negative)  $h_i$  values

• Information Ratio:

Meaning: extra return we can obtain from analysis, compare to, Scenario: For an investor holding the market, how much will Sharpe ratio improve if optimally weights BRK?

$$\begin{split} SR_{New} &= \sqrt{SR_{Init}^2 + IR^2} \\ SR_{\text{Portfolio}}^2 &= SR_{\text{Market}}^2 + \left[\frac{\alpha_A}{\sigma\left(e_A\right)}\right]^2 \end{split}$$

#### Performance evaluation: skill vs luck

• The CAPM and multifactor models allow us to analyze average returns, risk, and investment strategies:

Average returns: How much is alpha and how much is beta? Risk: How much is systematic and how much is idiosyncratic? Strategies: Are we using value/growth or small/big, etc.?

• actively managed funds: managers pick the portfolio weights

Example: ClearBridge Large Cap Growth Fund (Legg Mason)

people manage the fund
Sold by advisers and brokers
large-cap growth stocks
Annual turnover (trading) 20%

• passively managed index funds: computers pick index weights

Example: Vanguard 500 Index Fund (Vanguard)

dumans program computer to manage track performance of S&P500 Index Directly sold to investors Annual turnover (trading) 4%

Usually, index fund with the lowest expense ratio have higher return

Ticker	Expense Ratio	2000 – 2015 Avg. Return
AAFPX	0.60%	4.71%
PREIX	0.34%	5.01%
VFINX	0.17%	5.16%
SPY	0.09%	5.19%

Open-ended mutual funds

don't trade on the open market
executed at net asset value (NAV) at end of day market close
can't watch price fluctuate minute by minute like a stock
repriced based on number of shares bought and sold

• Exchange-traded Funds

• Closed End Funds

Similar to ETFs but actively managed
CEFs launch through an IPO, only set amt of shares enter market supply and demand determining price
CEFs higher fees

# Quantitative Finance – Derivatives

## Time value of money

- money has time value, because we can reinvest them
- always picture a timeline in thinking about this problem

### Interest

- The easiest way to make money is by earning interest from the bank
- simple interest rate (return calculation):  $a_t = a_0 * (1 + it)$
- compound interest rate (keep reinvest):  $a_t = a_0(1+i)^t$
- effective interest rate during a period:  $i = \frac{a_n a_{n-1}}{a_{n-1}}$
- nominal rate of interest:  $i^{(m)}$ , meaning that this interest i is paid m times a year an amount of  $\frac{i^{(m)}}{m}$  will be paid at each time interval, therefore at the end  $=(1+\frac{i^{(m)}}{m})^m$  let m goes to infinity, we have the continuous form  $(1+\frac{r}{m})^{mt} \longrightarrow e^{rt}$

# **Annuities and Perpetuities**

- annuity: fixed payment at each time point annuity-immediate: payment at the end of interval annuity-due: payment at the beginning of interval
- perpetuities: fixed payment at each time point, until infinity perpetuity-immediate: payment at the end of interval perpetuity-due: payment at the beginning of interval

### Bonds: a fixed income instrument

- market graph of bonds: what kinds of bonds are out there
- zero coupon bond: no coupon payment, only pay face value at maturity (treat as discount) zero rate: the annualized rate of return (annual compound)  $\longrightarrow B(t,T)(1+R(t,T))^{T-t}=1$

continuous zero rate:  $\longrightarrow B(t,T)e^{(T-t)R(t,T)}=1$  [treat R(t,T) as an interest rate] k-times per year:  $\longrightarrow B_{(t,T)}(1+\frac{R_{(r,T)}}{m})^m(T-t)=1$ 

• Bond with coupon: pay at specific time

Yield-to-Maturity: the interest rate that makes present value of cash flow equals bond price

or we can say that the YTM is the IRR at this point: internal rate of return it tells us the interest rate that this investment is representing, so that we can compare

Annual Coupon Bond:  $P = \sum \frac{CF_t}{(1+y)^t}$ Semi annual coupon bond:  $P = \sum \frac{CF_t}{(1+\frac{y}{h})^{2t}}$ 

So what happened in the market  $\longrightarrow$  we calculate the bond price, by the risk-free rate Therefore it is easy to imagine:

if risk-free rate goes up, the current bond price should drop if risk-free rate goes down, the current bond price should rise In short, the bond price is negatively correlated to the YTM

It depends on how we structure the dependent variable and independent variables:

- 1. Calculate the bond price: the DV is bond price, IDV is the interest rate, negative correlated.
- 2, Calculate YTM: the DV is YTM, IDV is bond price, if bond price is high, meaning the YTM must be low
- Relationship between zero coupon bond and coupon bond:

When a coupon bond pays no coupon, it is the same as zero coupon bond  $\longrightarrow$  same price and YTM

With coupon bond introduce coupon, we have 2 dimension to interpret the results:

- 1. how the price will change: with introduction of future cash flow, interest rate does not change, price will rise; with price rise, the YTM will drop
- 2. how the YTM will change: not a good direction, stick to PRICE  $\longrightarrow$  YTM path
- Since the zero coupon bond has a higher YTM than coupon bond, it is some how confusing because we may think the coupon bond gives us more return.
- We introduce the "Par Yield" to do standardization on the returns:
- Par Bond: the price = face value  $\longrightarrow$  issue at par  $\longrightarrow$  YTM = annual coupon rate Par Yield: when a bond is issue at par, the coupon rate (annualized return) is equal to YTM (calculated annualized return)
- Dollar Duration: the  $\frac{dP}{dy}$  the derivatives of price w.r.t. YTM Modified Duration:  $-\frac{1}{P}\frac{dp}{dy}$ , Dur normalized by price Dollar Value of 1 basis point (DV01): =  $Dur \cdot (-1bp)$

At a specific price level, the Dollar Duration Dur, decrease as:

- 1. maturity increase (Dur is a price sensitivity measure to yield, with T goes up, it is more sensitive)
- 2. coupon increases (1. more money to discount, more sensitive. 2. more coupon means price up, then more sensitive)
- 3. YTM decrease (look at the graph, when YTM is small, it is steeper)

### Forward Rates

 Diagram and calculation: separate the time into different intervals, make investment using respective rates

### **Futures**

## Options

\* Memoryless:

### **Bonds**

\* Memoryless:

## Financial Assets: Derivatives

### Forwards / Futures

- Futures: Traded in the exchange, so basically standardized contract
- Forwards: customized
- Keywords: strike price, maturity day, long, short

#### Agencies

- Clearing house: ensure trader fulfill obligations
- Margin: Trader deposit margin to fulfill obligations: Initial margin; Maintenance margin; Variation margin;

## Options

- Vanilla Option / European Option: fixed maturity date, strike price
- American Option: can exercise before maturity date
- Bermudan Option: can exercise on pre-determined date
- Barrier Option: can exercise once cross the barrier level: up and out, down and out, up and in, down and in
  - 1) Callable Bull: if always bull, then it is valid (never drop down barrier) [down and out]
- 2) Callable Bear: if always bear, then it is valid (never go up barrier) [up and out]
- Asian Option: the payoff determined by average price of pre-set period of time

Option strategies: Notice difference between prices and payoff

- Straddle: long 1 call and 1 put with same K and T
- Strangle: long call and put with same K and T
- Bull Spread: make money when price up: Buy call with  $K_1$ , sell call with  $K_2$
- Bear Spread: make money when price down: Buy call with  $K_1$ , sell call with  $K_2$
- Butterfly: long 2 calls, short call \* 2

### Warrents

- equity warrants: issue by company. represent the right to subscribe to equity securities
- derivative warrants: issued by 3rd party.

### Swap: 2 parties exchange financial instruments

- Interest rate swap
   A: expect Libor drops; B: expect Libor ups
   ????
- Benefit: 1) hedge against interest rate exposure; 2) leverage comparative advantage A: AAA rated company; B: BBB rated company.

  Company A will definitely have less lending interest rate in the market, in all loans But that doesn't mean company A can't do better. We can calculate the spread and see what is company A's comparative advantage, and borrow only that kind of loan, other company can use their comparative advantage P38

# Financial Risk: Value at Risk

Return

• Arithmetic Return:  $R_t = \frac{S_t - S_{t-1}}{S_{t-1}}$ 

• Log Return:  $log(1+R_t) = log(\frac{S_t}{S_{t-1}}) = log(S_t) - log(S_{t-1})$ 

Volatility Measure

•  $\sigma_s = \sqrt{\frac{1}{n-1}\sum(\mu_i - \bar{\mu})^2}$ 

• Then the volatility over N periods:  $\sqrt{N}\sigma_s$ 

VaR: Value-at-Risk

• if there is a distribution graph, starting from left to some point, this region is  $\alpha$ 

• the rest region to the right is  $1 - \alpha$ , stands for the confidence: 95%, 99% etc.

 $\bullet\,$  We called  $\alpha$  as the "tail probability", since it is the worst scenario

• In a graphical sense, VaR is the p-th quantile of the PnL distribution

• "Relative VaR": E[PnL] - VaR

Modeling the PnL distribution

• The fundamental of finding VaR is to model the portfolio PnL distribution

• Parametric Approach:

Keypoint: construct the mean  $\mu$  and volatility  $\sigma$  Approach: convert to approach "standard normal distribution"

Then we can calculate VaR; or extend this to a multi-time period scenario

• Non-Parametric Approach: Historical Simulation

1. we want to know the price at tomorrow

2. we convert the a problem: how much will the portfolio value change

3. based on past period-wise change data, we treat it as distribution

4. select the change we need

Financial Risk: Hedging, Optimal Hedging

Idea

• Hedge against a instrument that is negatively correlated to your portfolio

Quantify

• we want to minimize variance of new portfolio : S + NF, with S original portfolio

• we first construct the variance:  $\sigma_s + N^2 \sigma_f + 2N \sigma_{s,f}$ 

• Then N can be solved by using the solution for a square equation

# Coursera - Columbia - No Arbitrage

## Example of using No-Arbitrage pricing:

• 1. A bond that pays A in 1 year:

Pricing 1: portfolio that: buy 1 bond, borrow  $\frac{A}{1+r}$ Pricing 2: portfolio that: sell 1 bond, lend  $\frac{A}{1+r}$ 

#### • 2. Use compounding interest rate for pricing:

• 3. Floating Rate Bond:

The price of a floating rate bond, is equal to, the face value.

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# Cousera - Columbia - No Arbitrage in various assets

### Swaps

• What is it: a trade between fixed and float rates

• Why is it: leverage relative strength, capture trends in other markets

• How does it works: do your best, borrow your weakness

1. A has relative strength in fixed rate

2. B has relative strength in floating rate

3. A will borrow fixed rate, B will borrow floating rate

4. A borrow floating from B, pays fixed to B

• How to price it: What should be the exchange rate pay to each other

1. Swap should be of 0 value to each party

2. Write the Cash Flow PV for one side

3. Set it to 0 and we calculate the payment rate

### **Futures**

• What is it: An traded an exchange standardized contract

• Why need it: standardized, counter party risk, solved multiple price for same maturity

• How does it works: Margin call (go to initial margin), clearing house

• How to price it:

• Minimum variance hedging (since perfect hedge is impossible):

## Options

• In the money, at the money, out of the money

• Put-Call Parity: call + cash = put + stock try to buy a stock, and use money to help me try to sell a stock, and hold a stock to help me  $C + Ke^{-rt} = P + S$   $C + Ke^{-rt} = P + S - D$  (with dividend)

• Bounds of option prices

## **Binomial Tree Pricing**

• 1-period Binomial Tree: price goes up and down with probabilities, allow short sell

• Multi-period Binomial Tree: extend with same prob and up/down scale

 Replications: (buying shares, investing in cash) ↔ (option) make the payoff equals

• European and American Pricing: use risk-neutral prob to price:  $q=rac{R-d}{u-d}$ .  $C_0=rac{1}{R}[qC_u+(1-q)C_d]$