

CSL302: Compiler Design

Bottom Up Parsing

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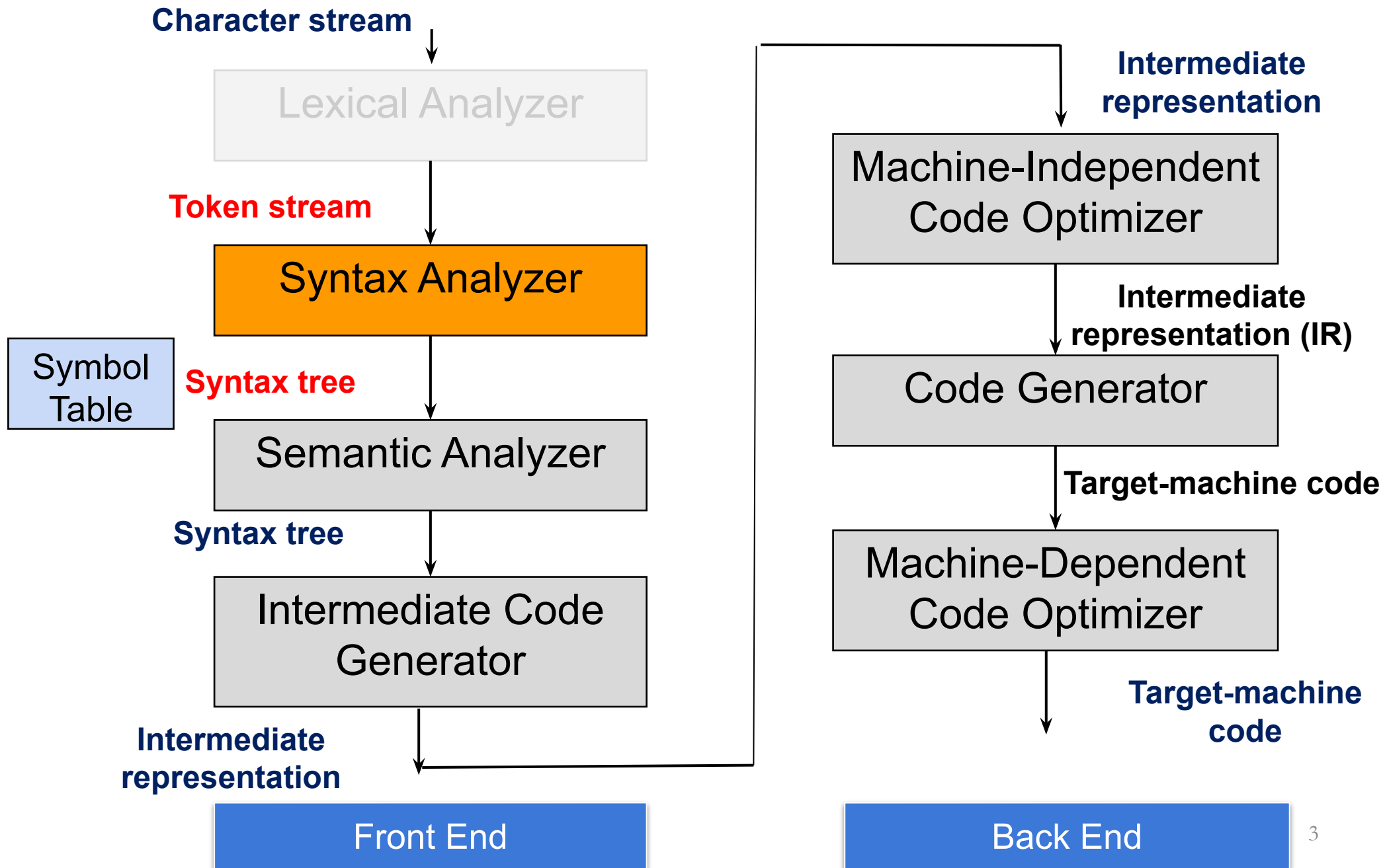
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Acknowledgement

- Today's slides are modified from that of *Stanford University*:
 - *<https://web.stanford.edu/class/archive/cs/cs143/cs143.1128/>*

Compiler Design



Analysis of SLR(1)

- Exploits lookahead in a small space.
 - Small automaton – same number of states as in LR(0).
 - Works on many more grammars than LR(0)
- Too weak for most grammars: lose context from not having extra states.

Example

S → **E**

E → **L** = **R**

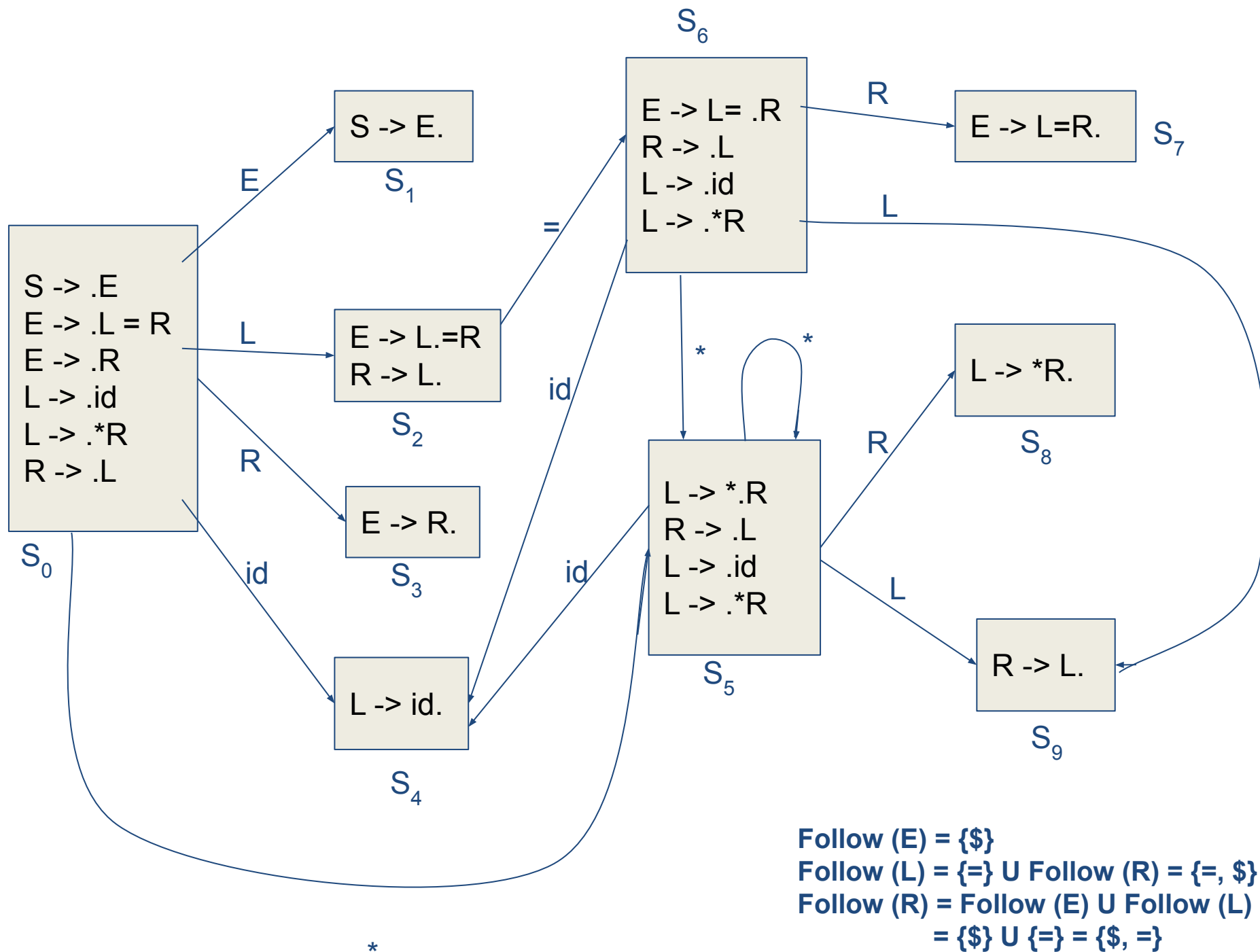
E → **R**

L → **id**

L → *******R**

R → **L**

id	=	*	id
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Follow (E) = {\$}
 Follow (L) = {=} U Follow (R) = {=, \$}
 Follow (R) = Follow (E) U Follow (L)
 = {\$} U {=} = {\$, =}

$S \rightarrow E$ (1)
 $E \rightarrow L = R$ (2)
 $E \rightarrow R$ (3)
 $L \rightarrow id$ (4)
 $L \rightarrow *R$ (5)
 $R \rightarrow L$ (6)

Follow (S) = {\$}
 Follow (E) = {\$}
 Follow (L) = {=, \$}
 Follow (R) = {=, \$}

	id	=	*	\$	E	L	R
s_0	S_4		S_5		S_1	S_2	S_3
s_1				r_2			
s_2		S_6 / r_6		r_6			
s_3				r_3			
s_4		r_4		r_4			
s_5	S_4		S_5			S_9	S_8
s_6	S_4		S_5			S_9	S_7
s_7				r_2			
s_8		r_5		r_5			
s_9		r_6		r_6			

The Limits of SLR(1)

S \rightarrow **E**

E \rightarrow **L** = **R**

E \rightarrow **R**

L \rightarrow id

L \rightarrow ***R**

R \rightarrow **L**

The Limits of SLR(1)

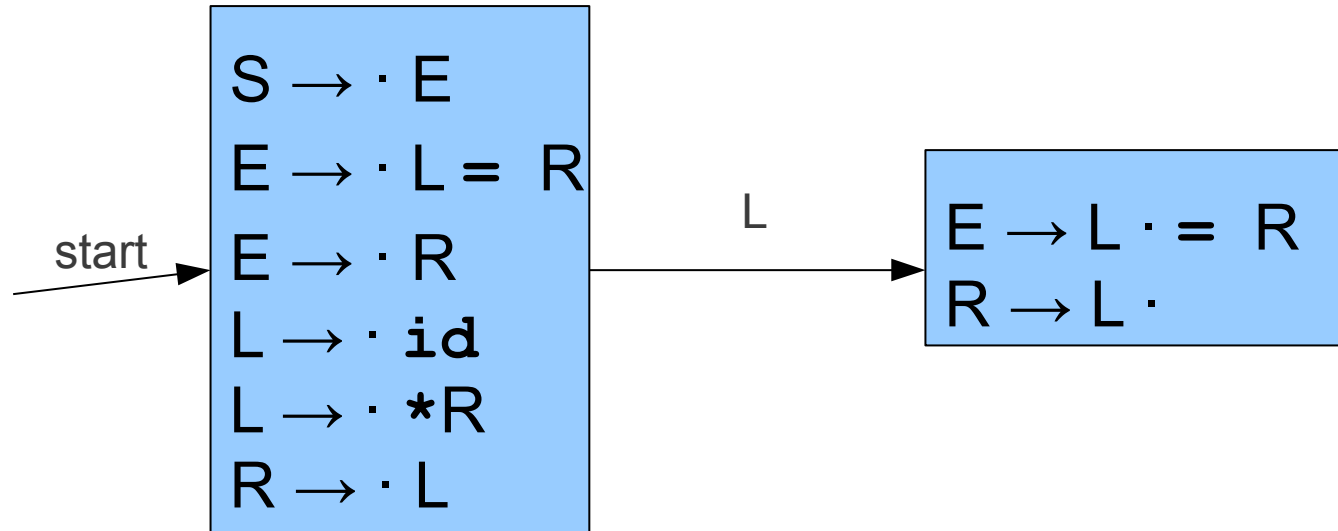
$S \rightarrow E$
 $E \rightarrow L = R$
 $E \rightarrow R$
 $L \rightarrow id$
 $L \rightarrow *R$
 $R \rightarrow L$

start →

$S \rightarrow \cdot E$
 $E \rightarrow \cdot L = R$
 $E \rightarrow \cdot R$
 $L \rightarrow \cdot id$
 $L \rightarrow \cdot *R$
 $R \rightarrow \cdot L$

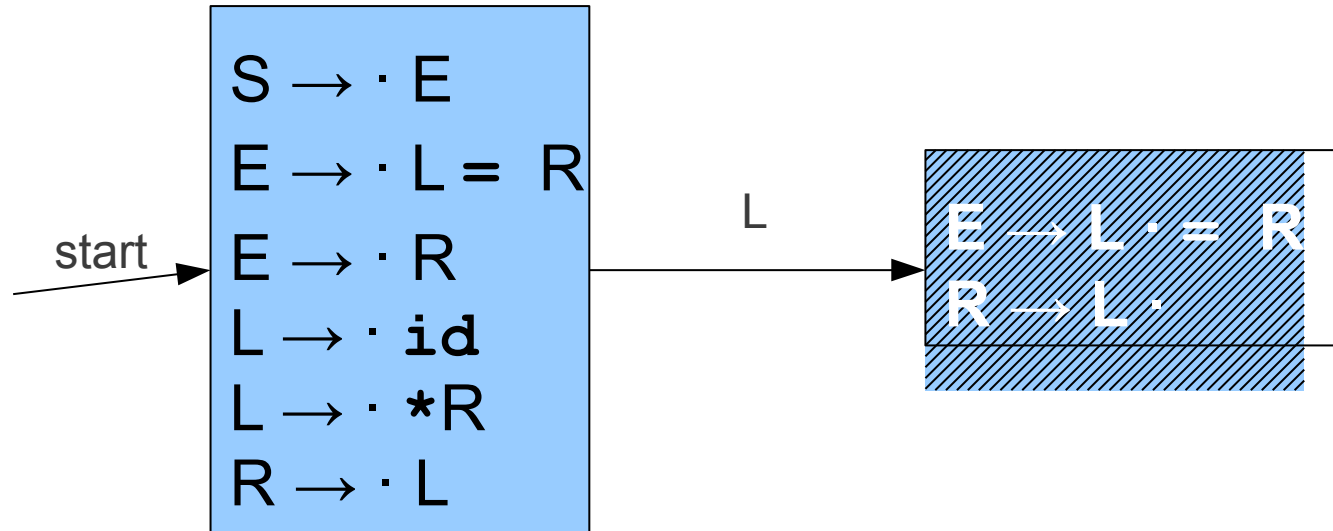
The Limits of SLR(1)

$S \rightarrow E$
 $E \rightarrow L = R$
 $E \rightarrow R$
 $L \rightarrow id$
 $L \rightarrow *R$
 $R \rightarrow L$



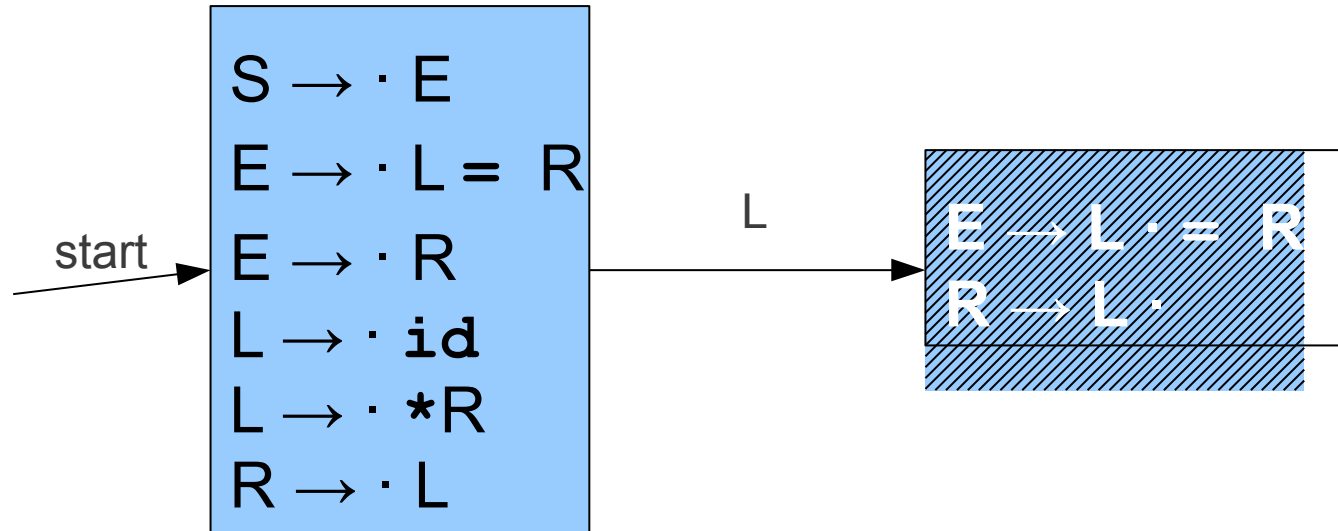
The Limits of SLR(1)

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The Limits of SLR(1)

$S \rightarrow E$
 $E \rightarrow L = R$
 $E \rightarrow R$
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 $L \rightarrow *R$
 $R \rightarrow L$

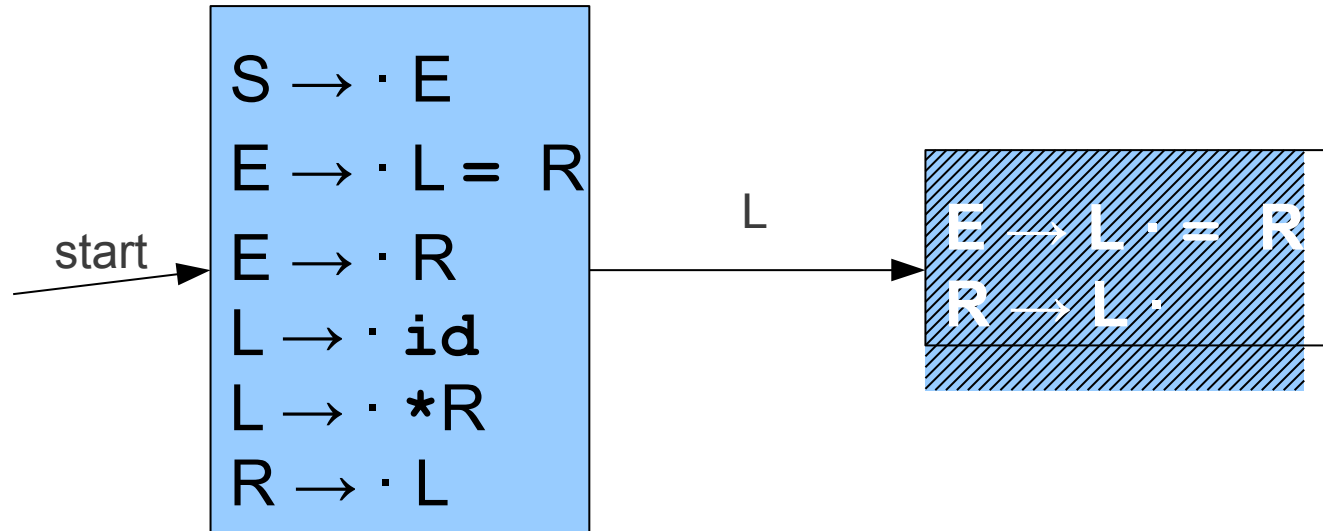


$E \rightarrow L \cdot = R$
 $R \rightarrow L \cdot$

tells us to shift on seeing =
tells us to reduce on FOLLOW(**R**).

The Limits of SLR(1)

$S \rightarrow E$
 $E \rightarrow L = R$
 $E \rightarrow R$
 $L \rightarrow id$
 $L \rightarrow *R$
 $R \rightarrow L$

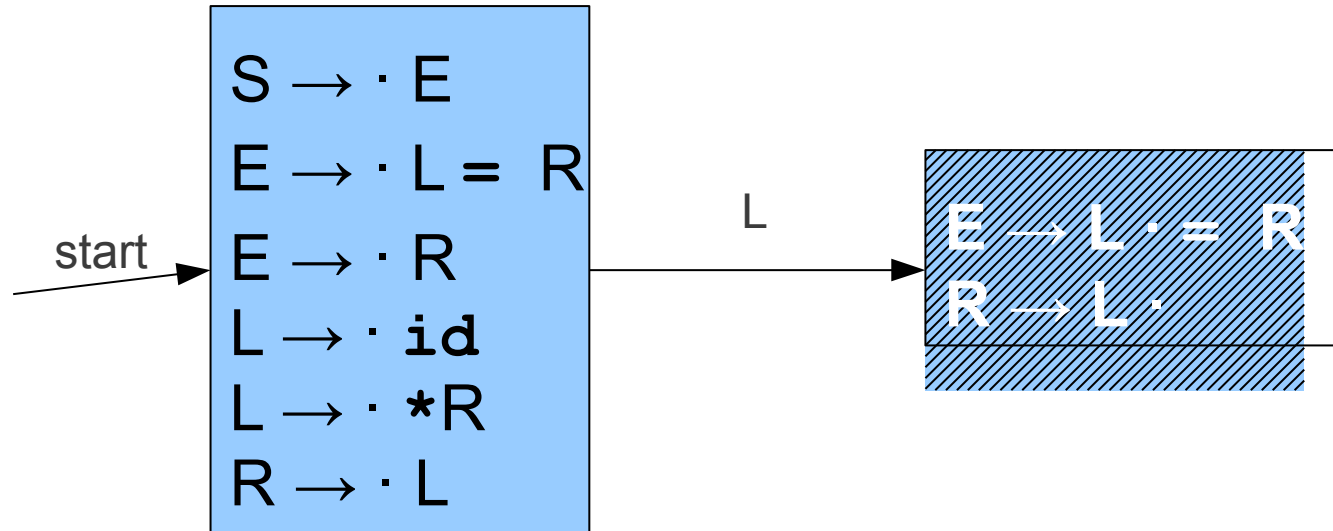


$E \rightarrow L \cdot = R$
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The Limits of SLR(1)

$S \rightarrow E$
 $E \rightarrow L = R$
 $E \rightarrow R$
 $L \rightarrow id$
 $L \rightarrow *R$
 $R \rightarrow L$



$E \rightarrow L \cdot = R$

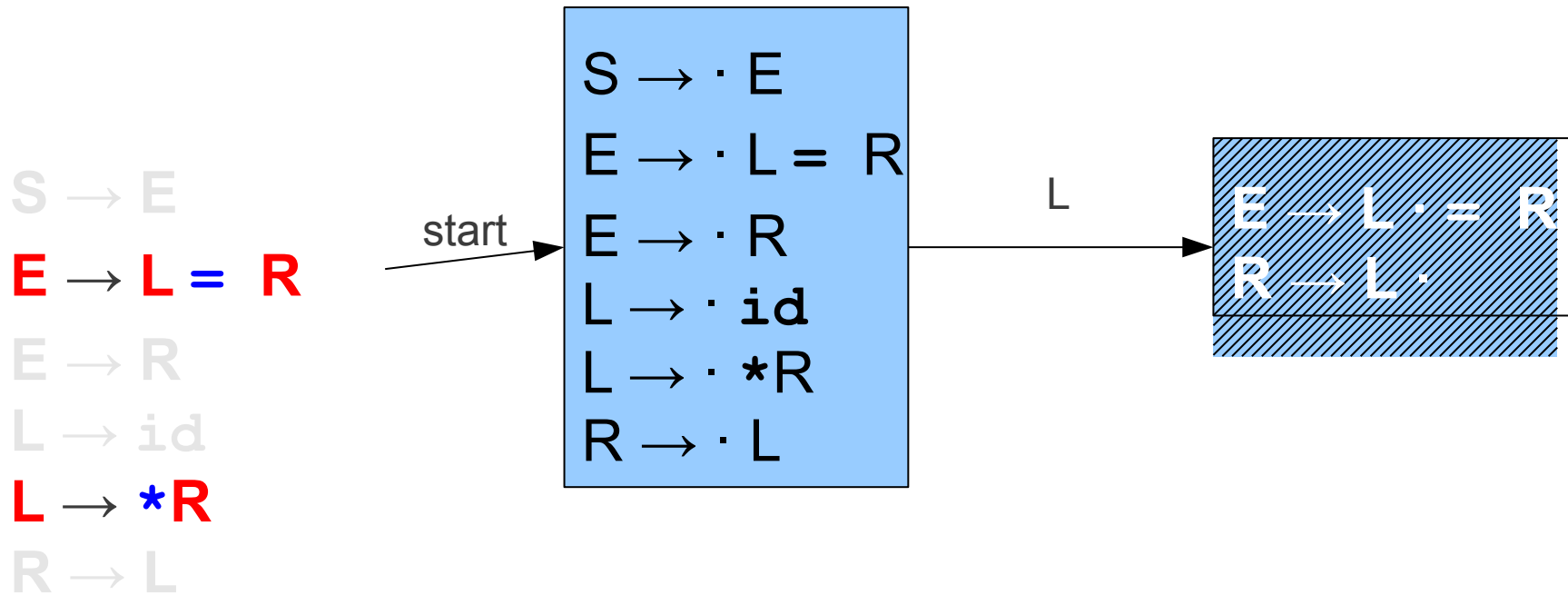
tells us to shift on seeing =

$R \rightarrow L \cdot$

tells us to reduce on FOLLOW(**R**).

= \in FOLLOW(**R**).

The Limits of SLR(1)



$E \rightarrow L \cdot = R$

tells us to shift on seeing $=$

$R \rightarrow L \cdot$

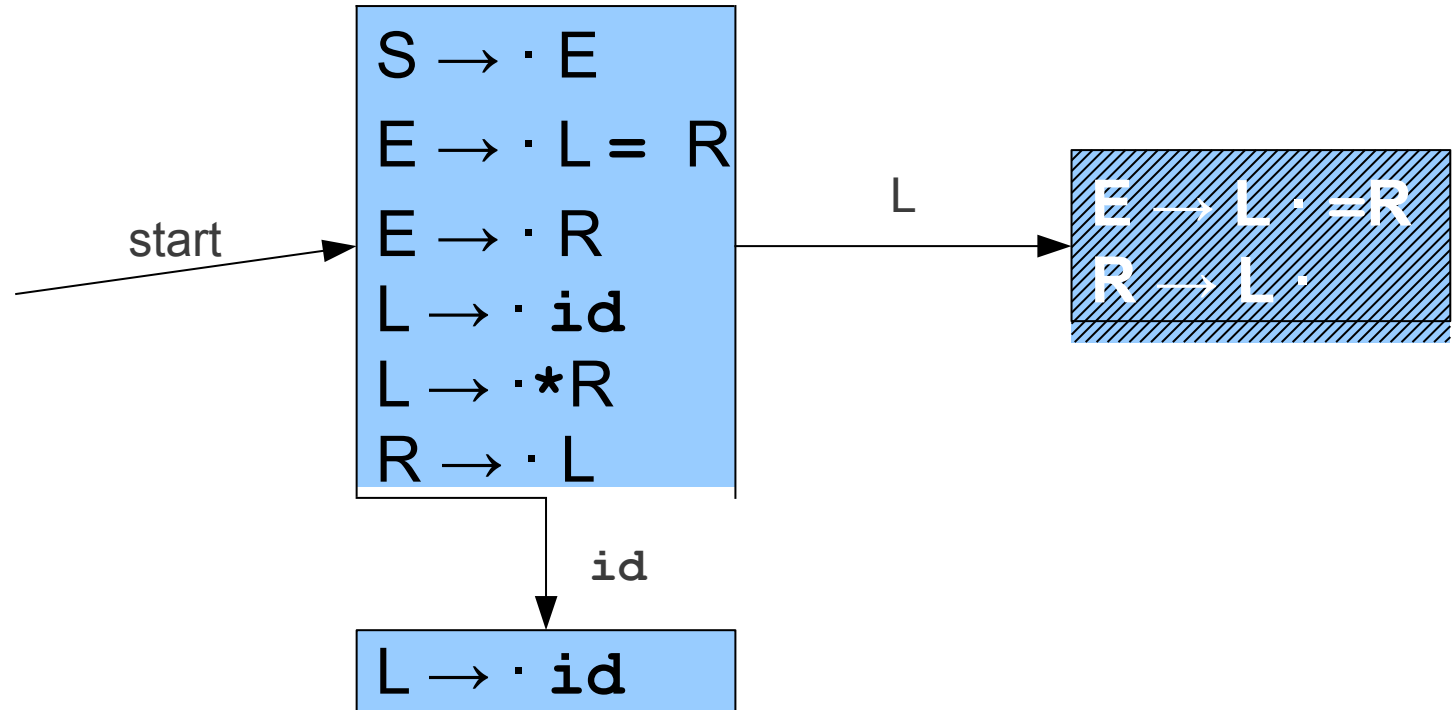
tells us to reduce on FOLLOW(R).

$= \in \text{FOLLOW}(R)$.

We have a conflict!

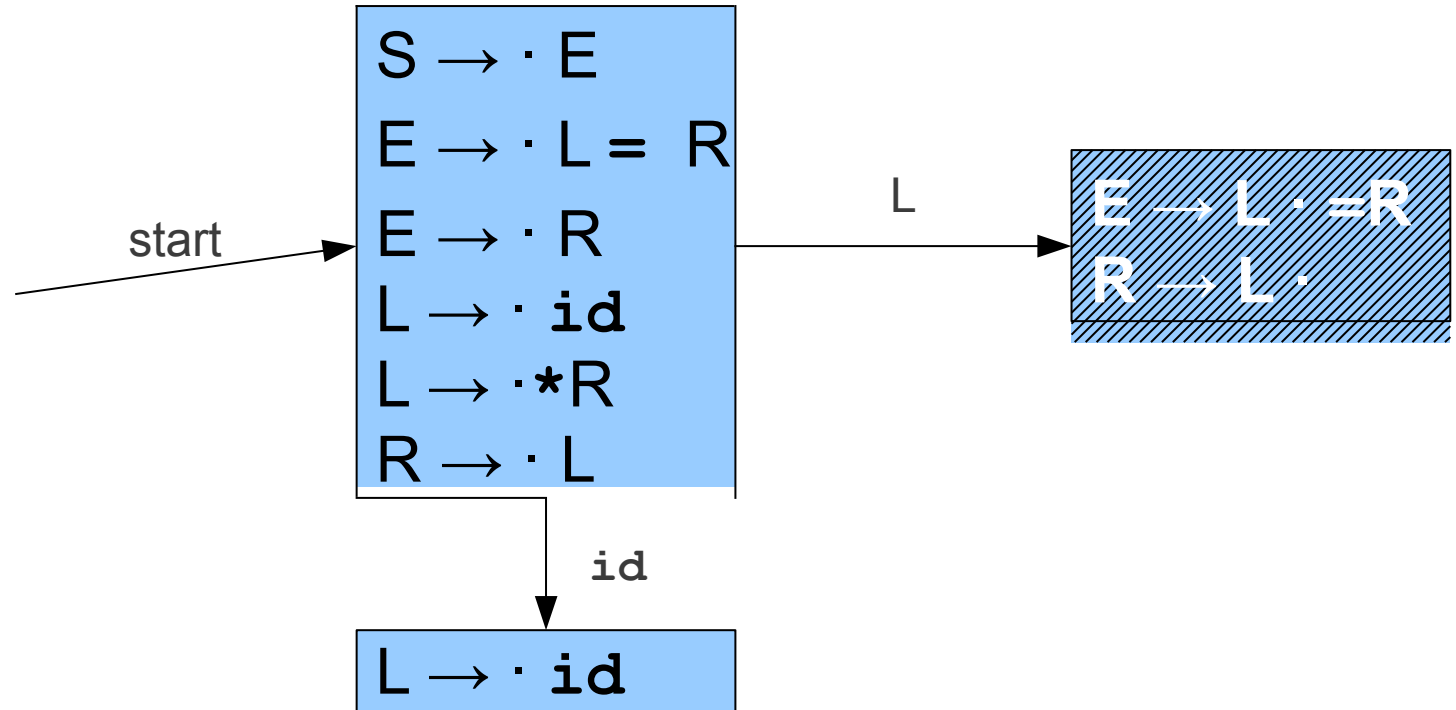
A Lack of Context

$S \rightarrow E$
 $E \rightarrow L = R$
 $E \rightarrow R$
 $L \rightarrow id$
 $L \rightarrow *R$
 $R \rightarrow L$



A Lack of Context

$S \rightarrow E$
 $E \rightarrow L = R$
 $E \rightarrow R$
 $L \rightarrow id$
 $L \rightarrow *R$
 $R \rightarrow L$

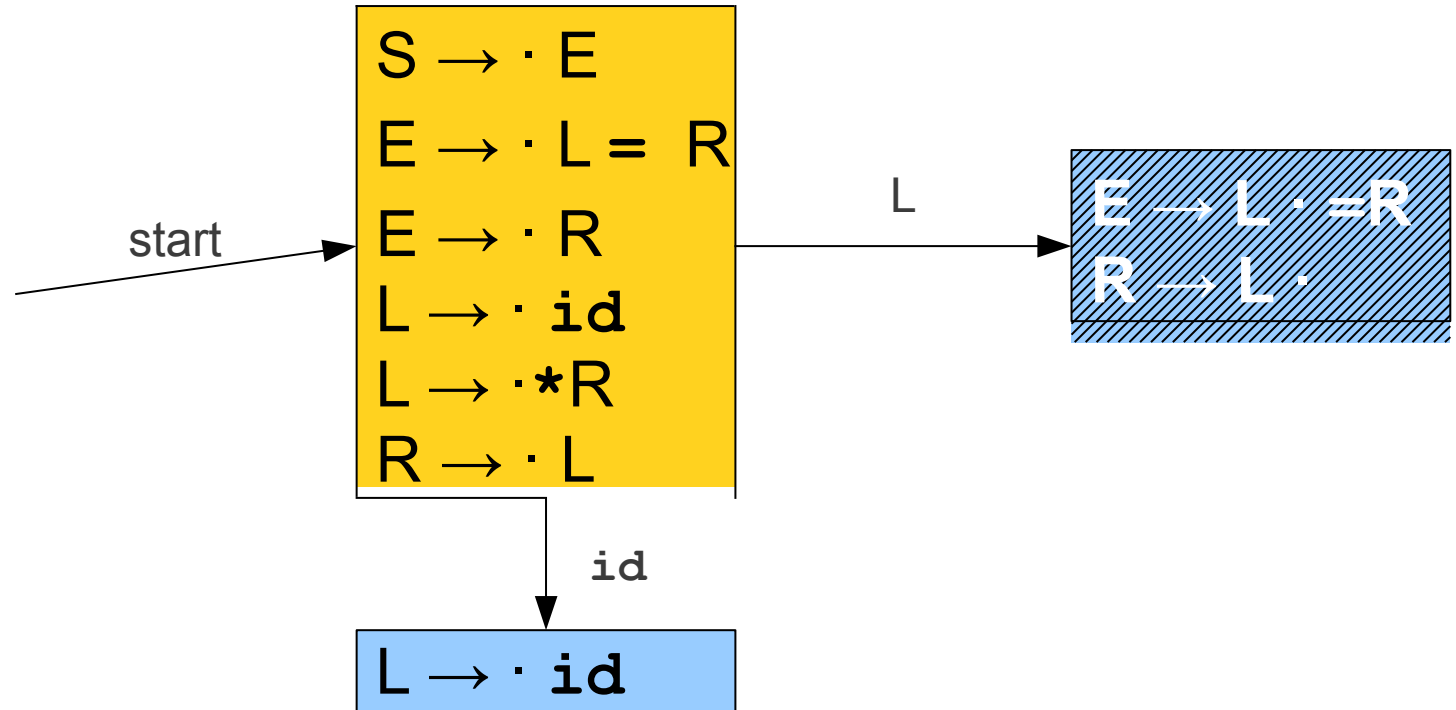


|

id	=	*	id
----	---	---	----

A Lack of Context

$S \rightarrow E$
 $E \rightarrow L = R$
 $E \rightarrow R$
 $L \rightarrow id$
 $L \rightarrow *R$
 $R \rightarrow L$

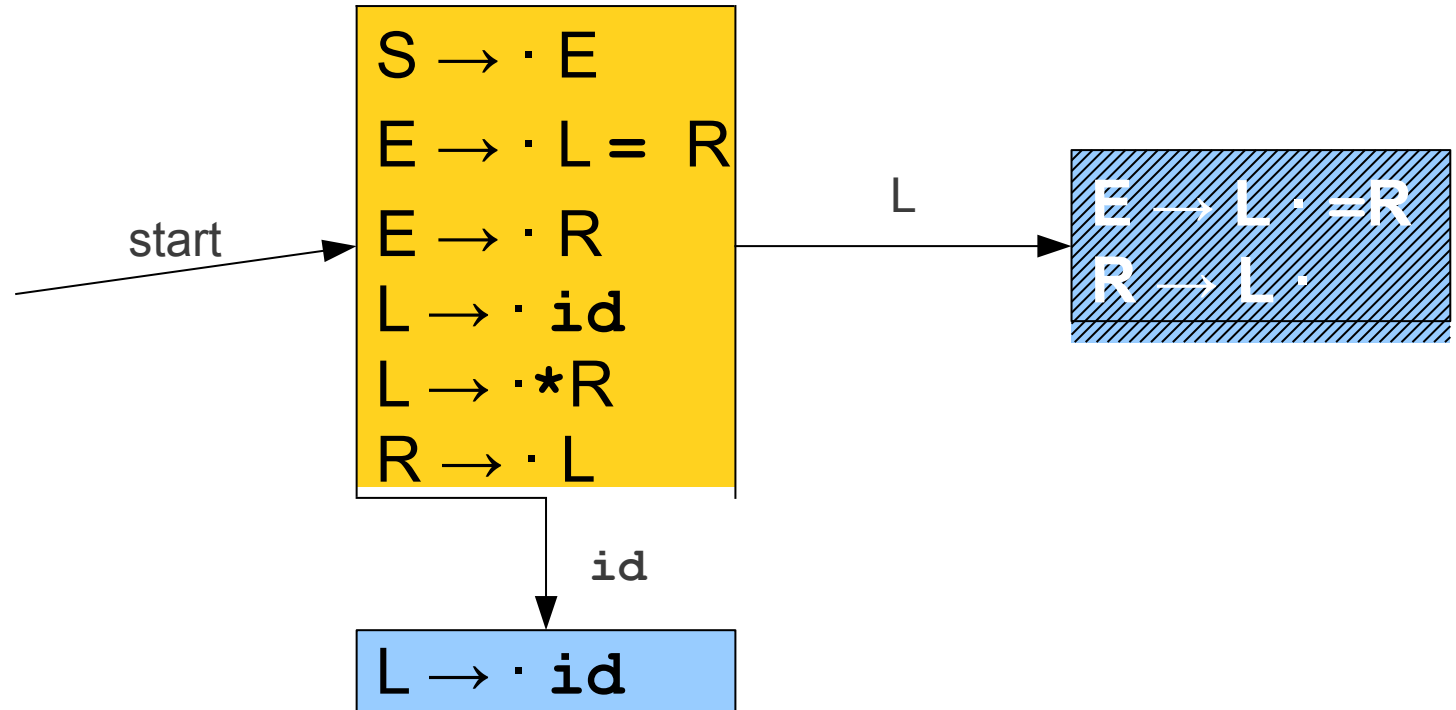


|

id	=	*	id
----	---	---	----

A Lack of Context

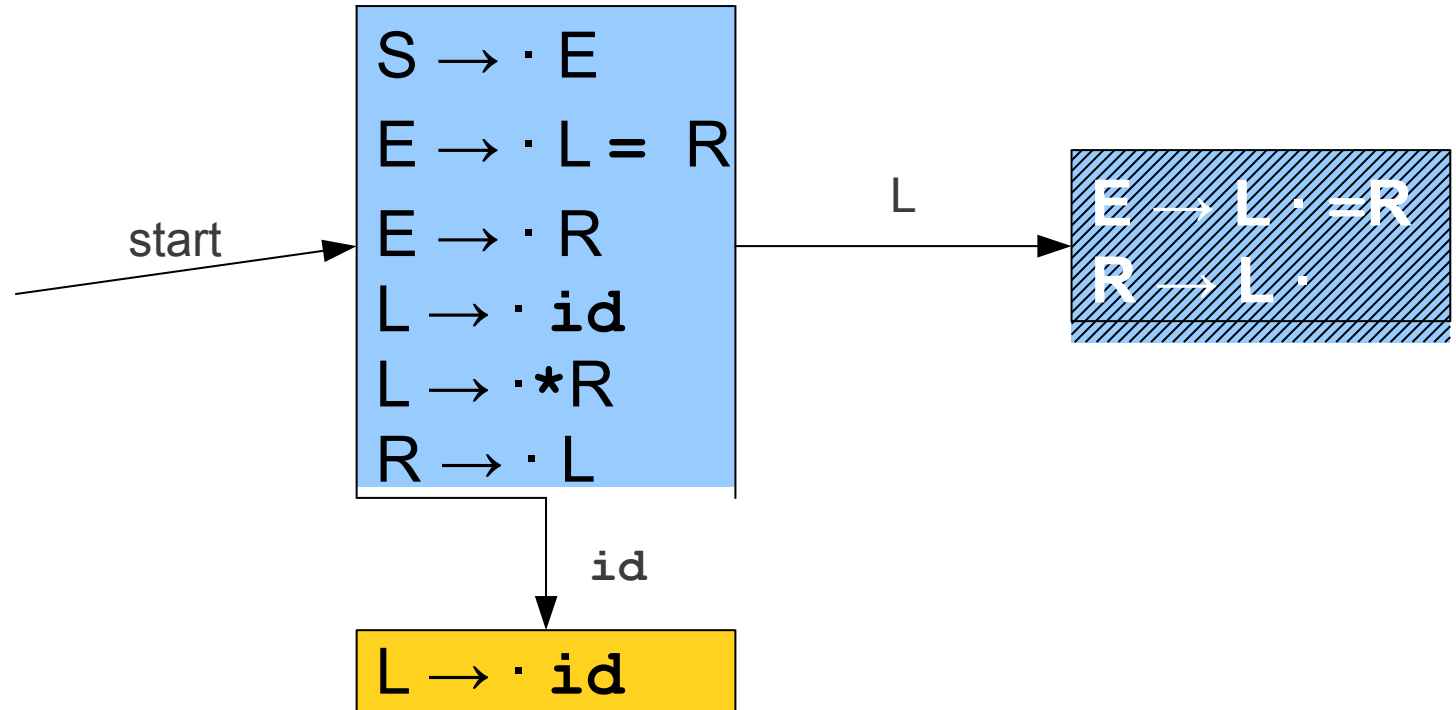
$S \rightarrow E$
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id		=	*	id
----	--	---	---	----

A Lack of Context

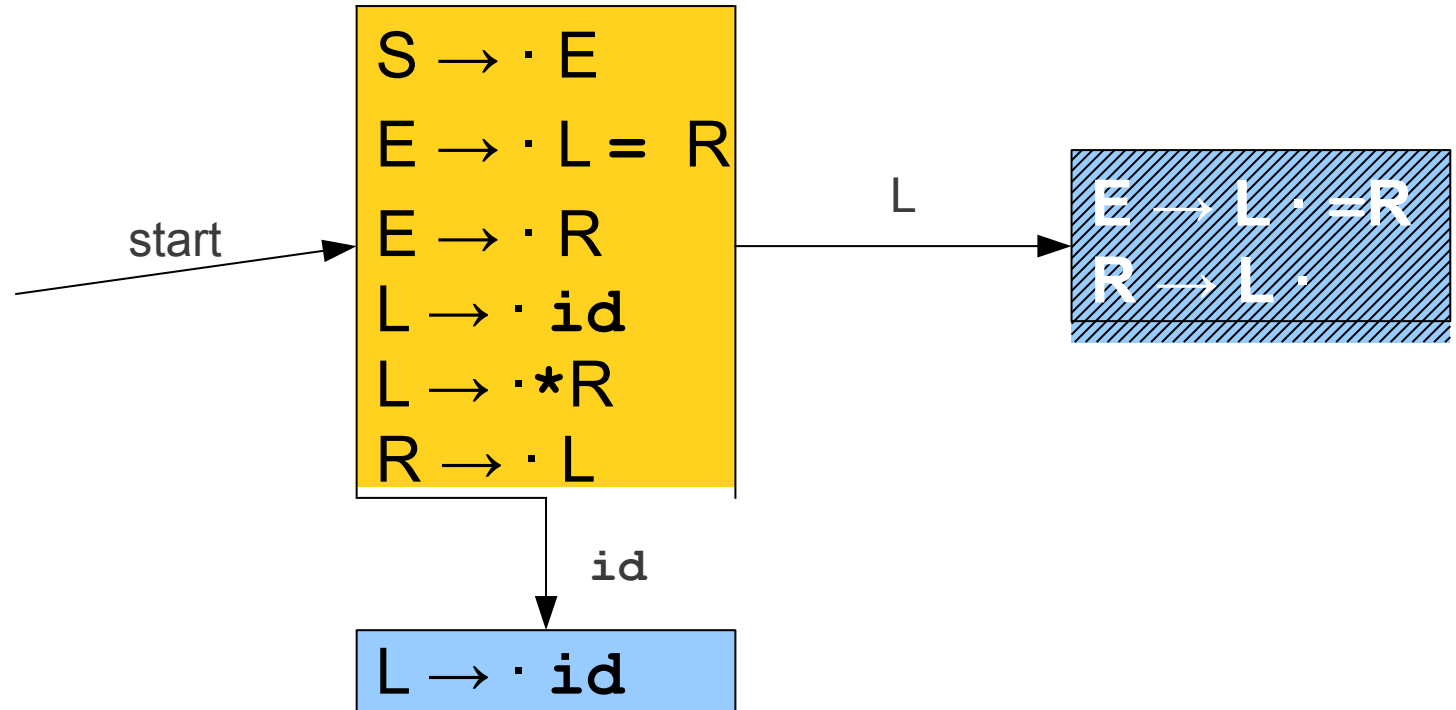
$S \rightarrow E$
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 $E \rightarrow R$
 $L \rightarrow id$
 $L \rightarrow *R$
 $R \rightarrow L$



id | = * id

A Lack of Context

$S \rightarrow E$
 $E \rightarrow L = R$
 $E \rightarrow R$
 $L \rightarrow id$
 $L \rightarrow *R$
 $R \rightarrow L$

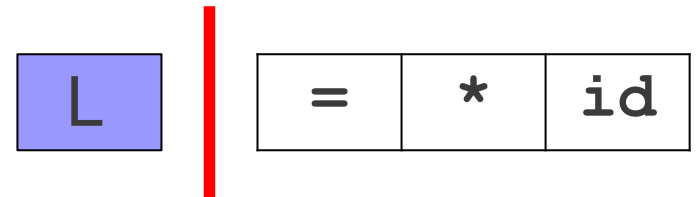
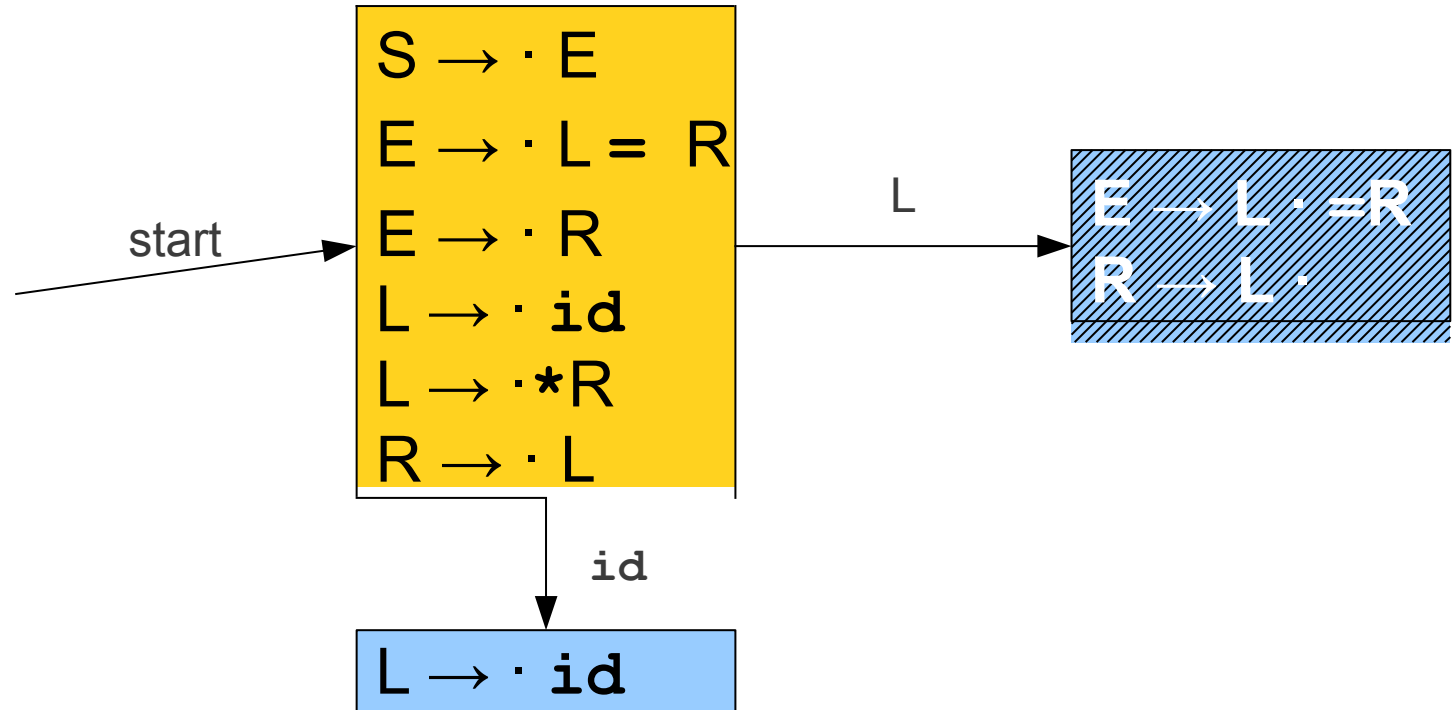


|

=	*	id
---	---	----

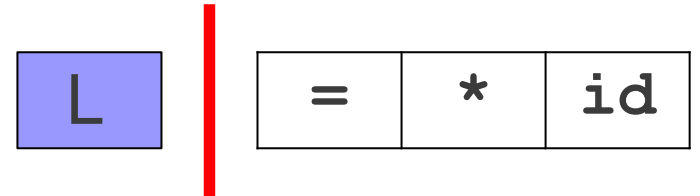
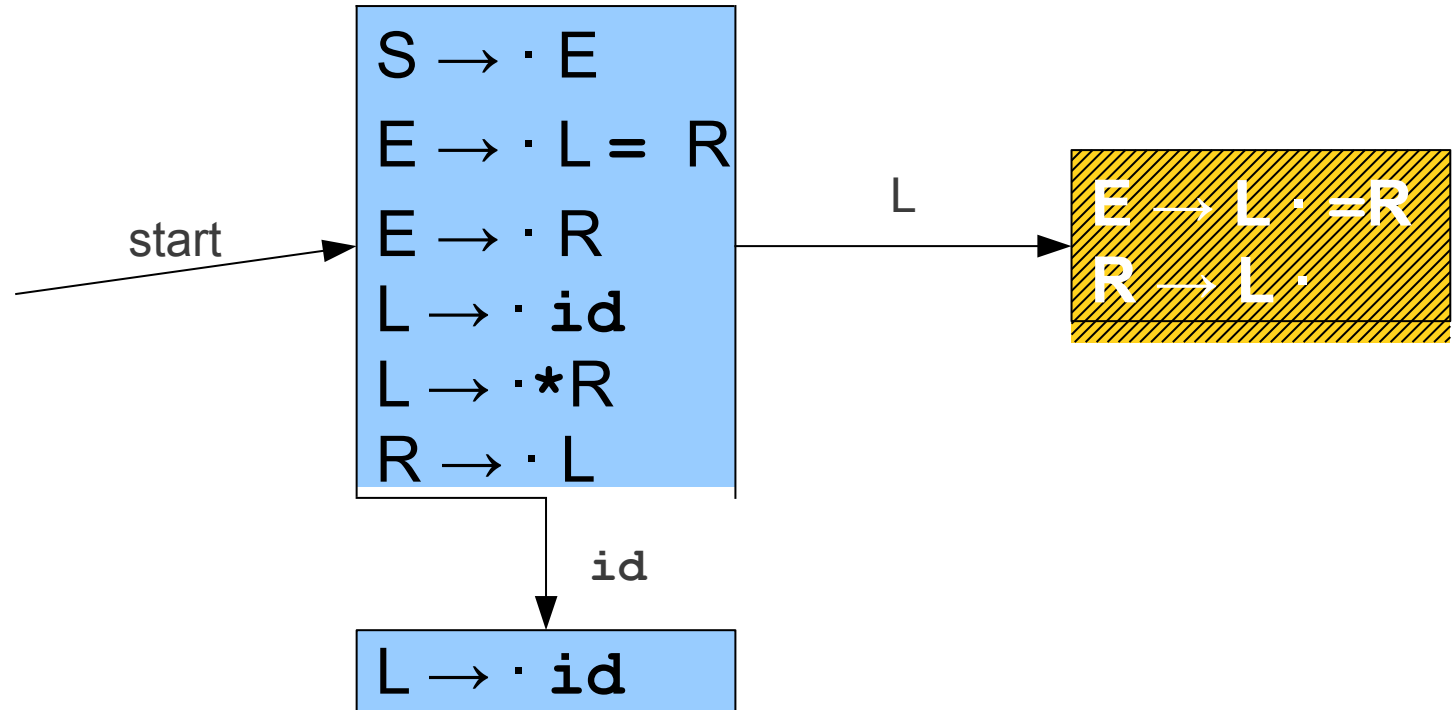
A Lack of Context

$S \rightarrow E$
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 $E \rightarrow R$
 $L \rightarrow id$
 $L \rightarrow *R$
 $R \rightarrow L$



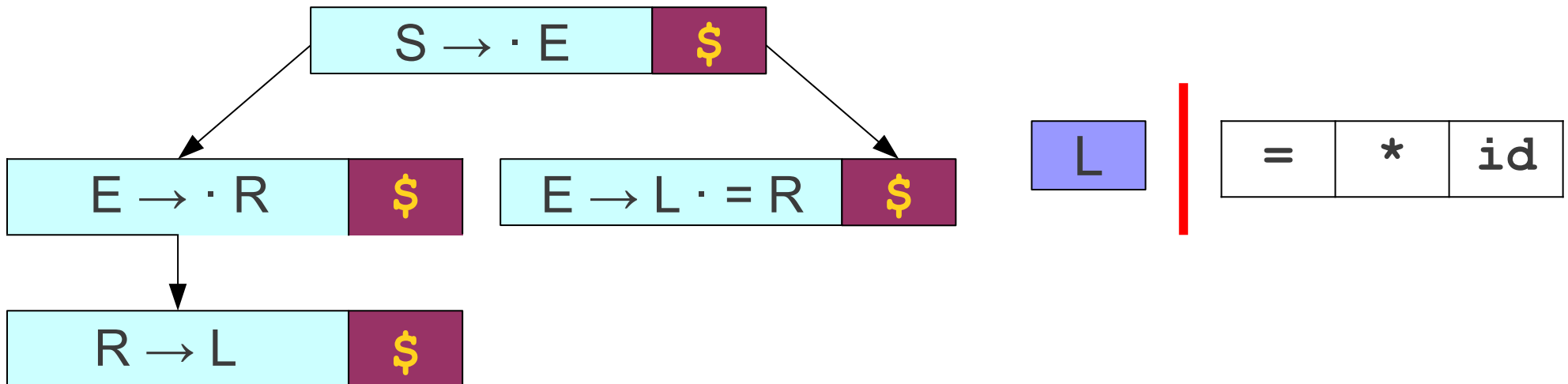
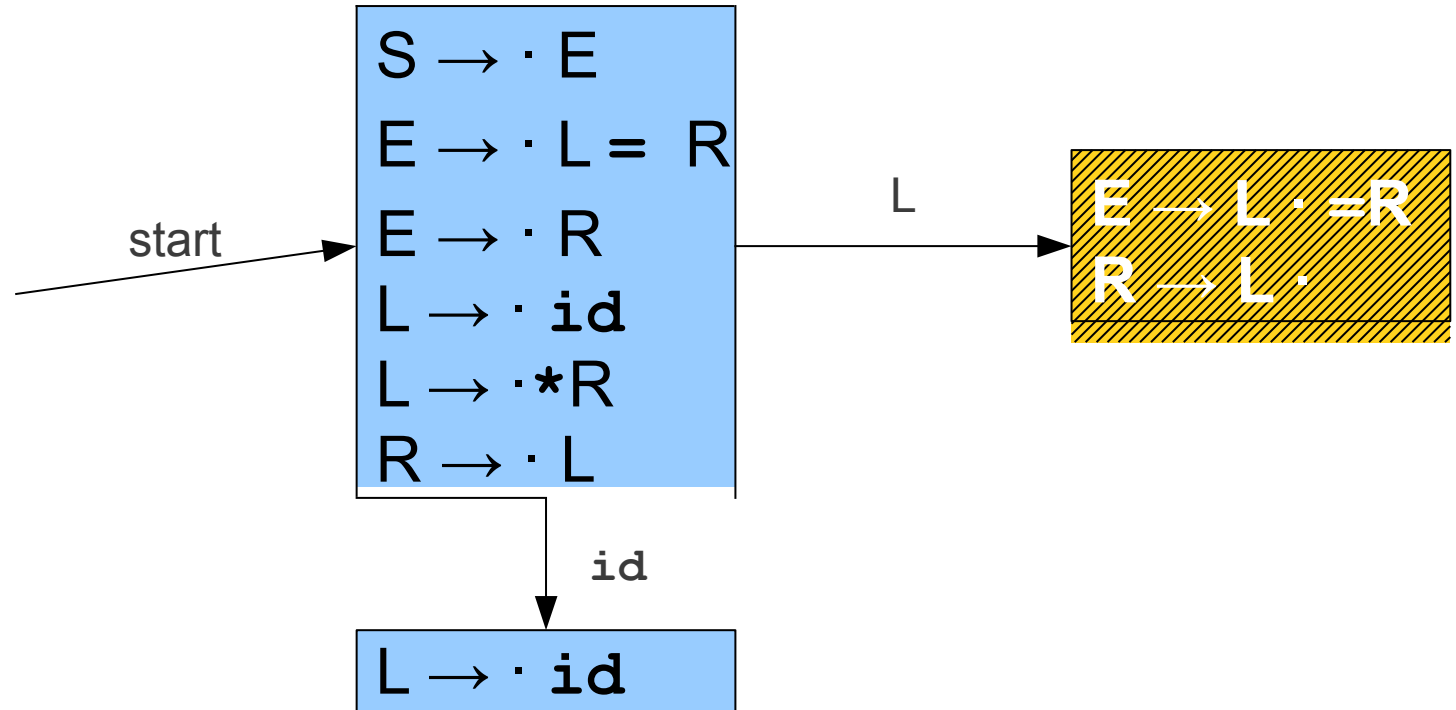
A Lack of Context

$S \rightarrow E$
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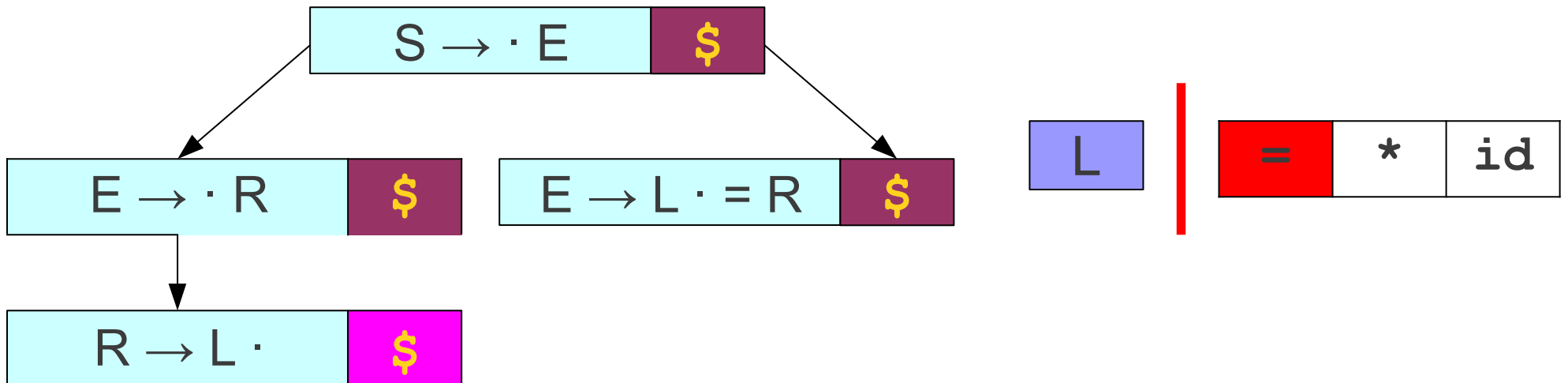
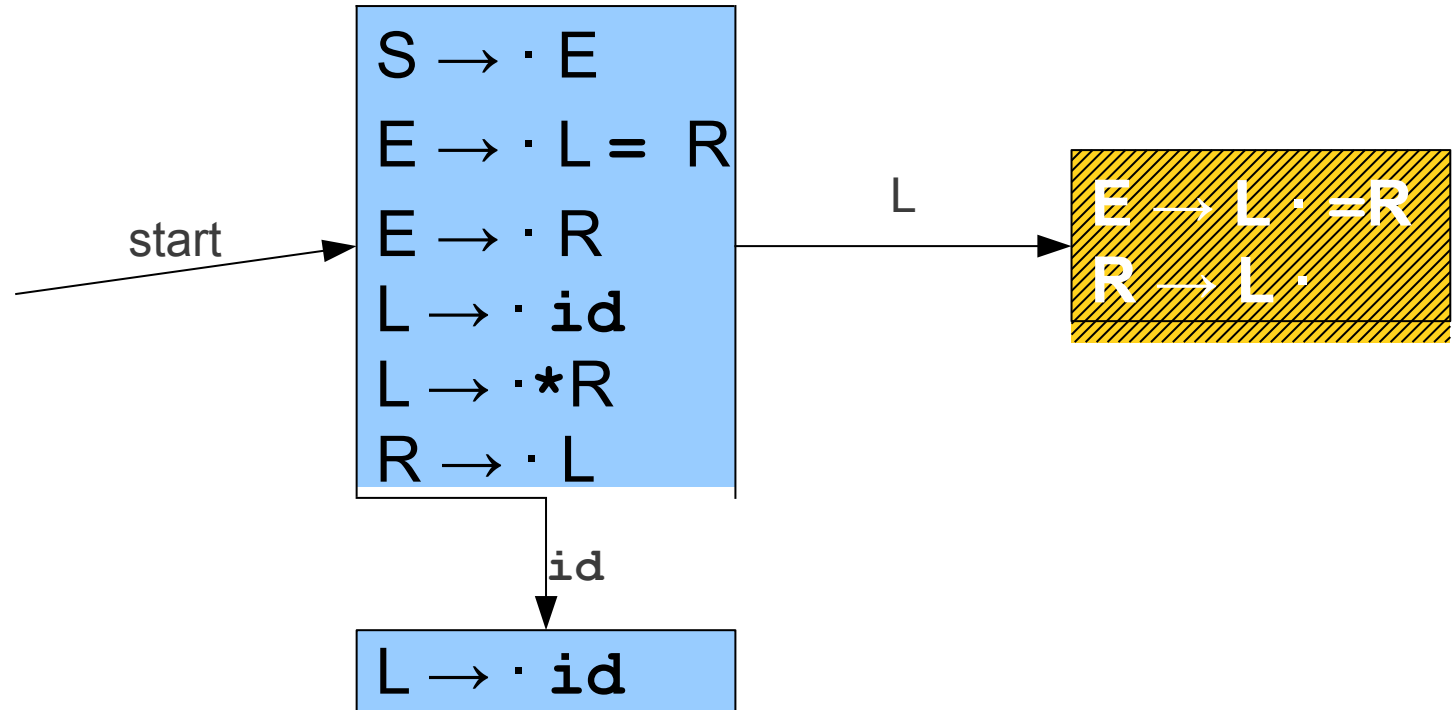
A Lack of Context

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A Lack of Context

$S \rightarrow E$
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 $E \rightarrow R$
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 $R \rightarrow L$



Why is SLR(1) Weak?

- With SLR(1), *minimal* context.
- FOLLOW(**A**) means “what could follow **A** somewhere in the grammar?,” even if in a particular state **A** couldn't possibly have that symbol after it.
- With LR(1), we have contextual information.

DFA for LR(1)

$S \rightarrow E$
 $E \rightarrow L = R$
 $E \rightarrow R$
 $L \rightarrow id$
 $L \rightarrow *R$
 $R \rightarrow L$

$S \rightarrow \cdot E$	\$
$E \rightarrow \cdot L = R$	\$
$E \rightarrow \cdot R$	\$
$L \rightarrow \cdot id$	=
$L \rightarrow \cdot *R$	=
$R \rightarrow \cdot L$	\$
$L \rightarrow \cdot id$	\$
$L \rightarrow \cdot *R$	\$

start

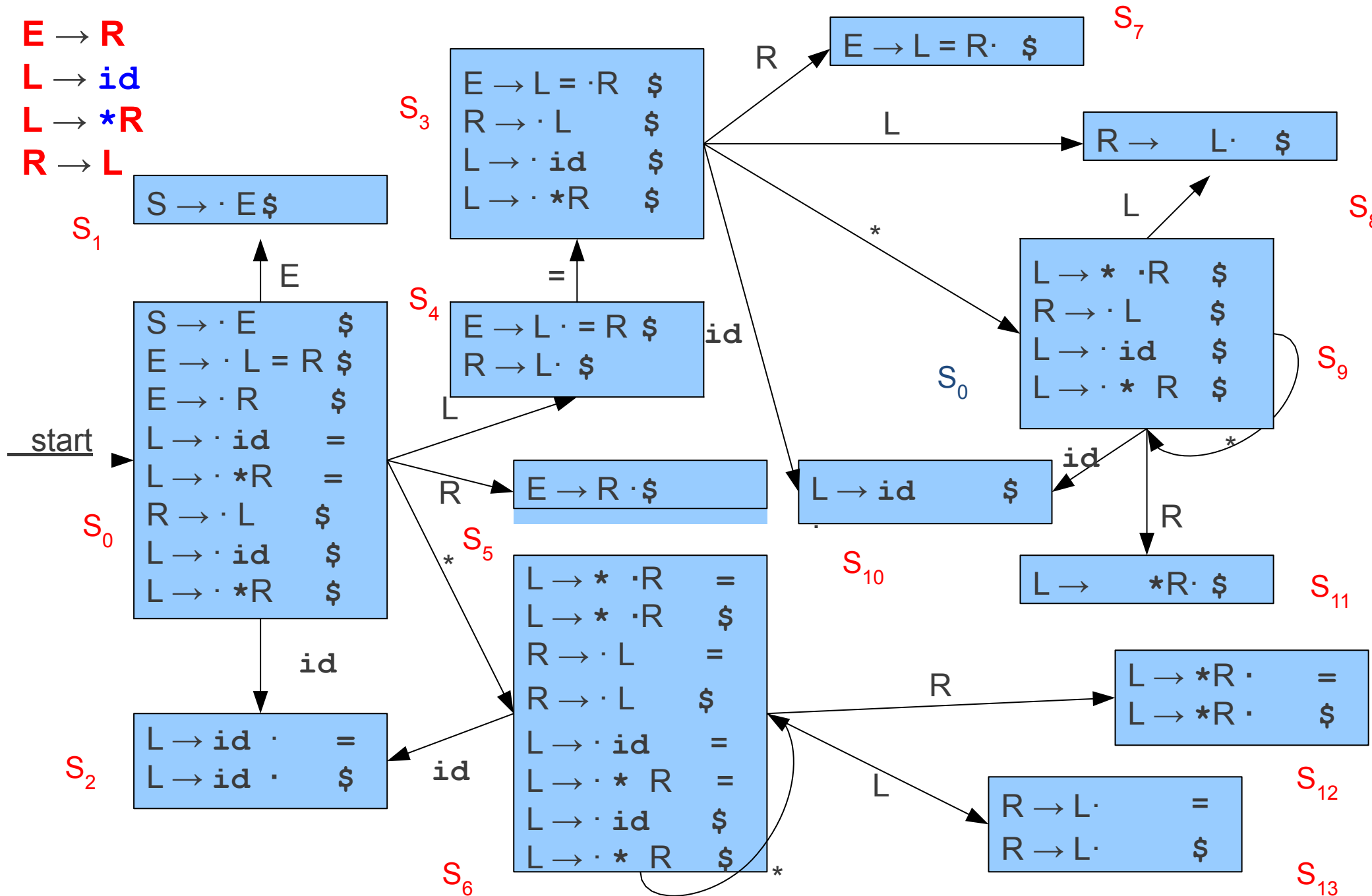
S_0

Constructing LR(1) Items

- Begin in a state containing $S \rightarrow \cdot E, \$$ where S is the start symbol and $\$$ is lookahead
- Compute the **closure** of the state:
 - If $A \rightarrow a \cdot B\omega, l$ is in the state, add $B \rightarrow \cdot \gamma, t$ to the state for each production $B \rightarrow \gamma$ and for each terminal $t \in \text{FIRST}^*(\omega l)$

DFA for LR(1)

$S \rightarrow E$
 $E \rightarrow L = R$
 $E \rightarrow R$
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 $R \rightarrow L$



The LR(1) Parsing Algorithm

- Begin with an empty stack and the input set to $\omega\$,$ where ω is the string to parse. Set **state** to the initial state.
- Repeat the following:
 - Let the next symbol of input be **t**.
 - If **action**[state, **t**] is **shift**, then shift the input and set **state** = **goto**[state, **t**].
 - If **action**[state, **t**] is **reduce** **A** $\rightarrow \omega$:
 - _ Pop $|\omega|$ symbols off the stack; replace them with **A**.
 - _ Let the state atop the stack be **top-state**.
 - _ Set **state** = **goto**[**top-state**, **A**]
 - If **action**[state, **t**] is **accept**, then the parse is done. If
 - **action**[state, **t**] is **error**, report an error.

Constructing LR(1) Parse Tables

- For each state X :
 - If there is a production $A \rightarrow \omega \cdot [t]$, set $\text{action}[X, t] = \text{reduce } A \rightarrow \omega$.
 - If there is the special production $S \rightarrow E \cdot [\$]$, where S is the start symbol, set $\text{action}[X, t] = \text{accept}$.
 - If there is a transition out of s on symbol t , set $\text{action}[X, t] = \text{shift}$.
- Set all other actions to **error**.
- If any table entry contains two or more actions, the grammar is not LR(1).