

# CSL302: Compiler Design

## Bottom Up Parsing

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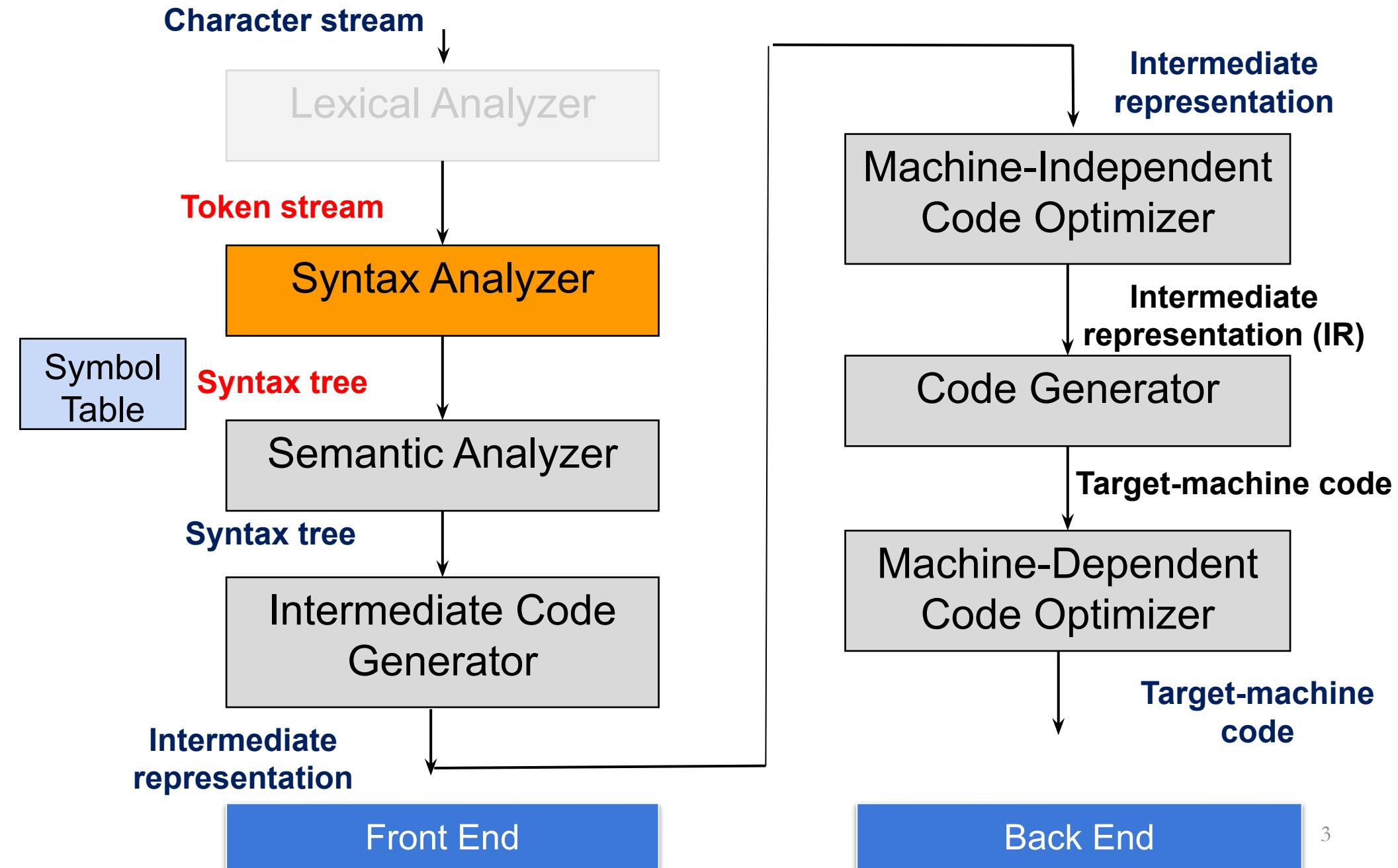
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# Acknowledgement

- Today's slides are modified from that of  
*Stanford University*:
  - <https://web.stanford.edu/class/archive/cs/cs143/cs143.1128/>

# Compiler Design



# Analysis of SLR(1)

- Exploits lookahead in a small space.
  - Small automaton – same number of states as in as LR(0).
  - Works on many more grammars than LR(0)
- Too weak for most grammars: lose context from not having extra states.

# Example

**S** → **E**

**E** → **L** = **R**

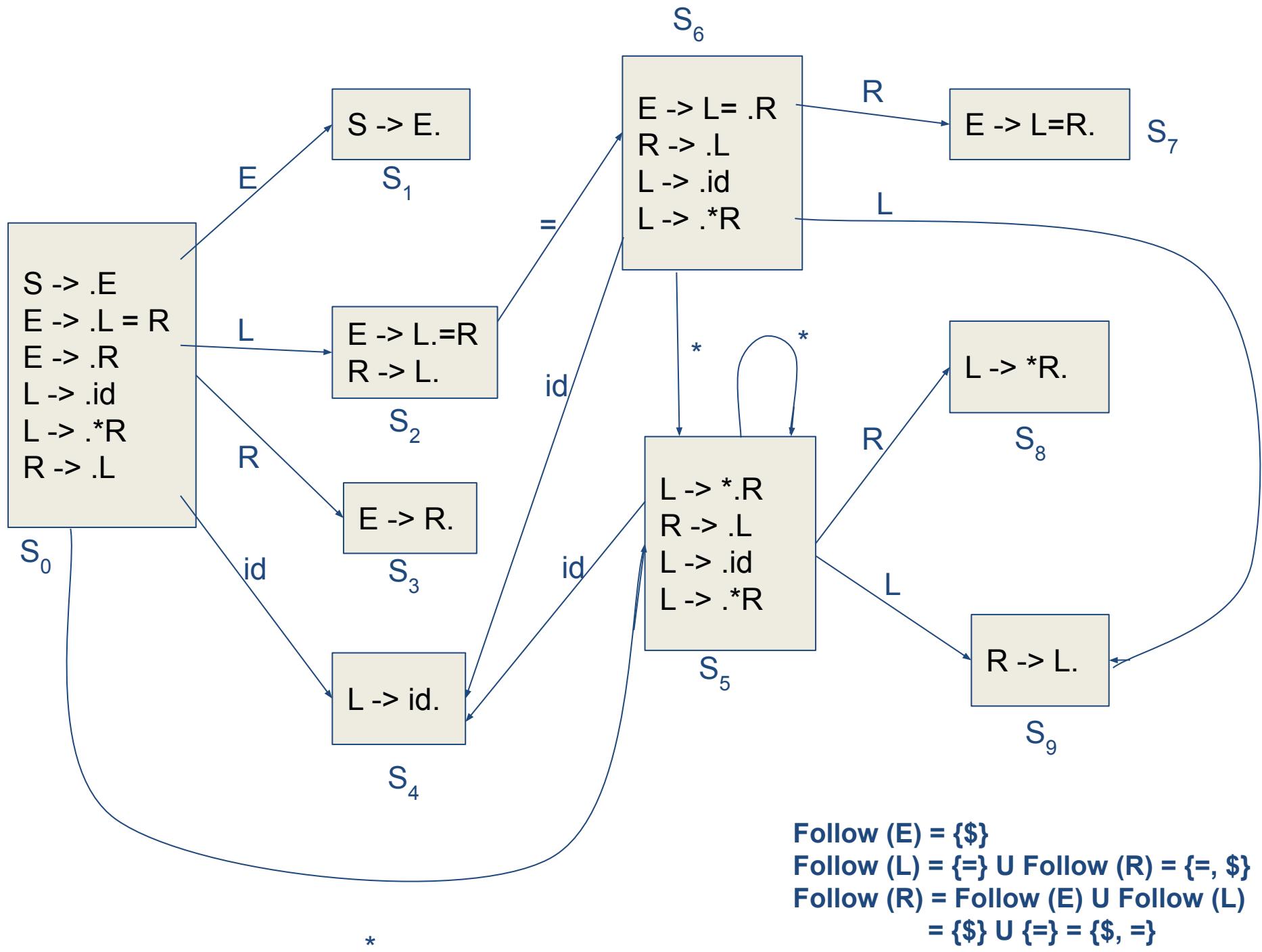
**E** → **R**

**L** → **id**

**L** → \***R**

**R** → **L**

<b>id</b>	=	*	<b>id</b>
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**Follow (E) = { $\$$ }**  
**Follow (L) = {=} U Follow (R) = {=,  $\$$ }**  
**Follow (R) = Follow (E) U Follow (L)**  
**= { $\$$ } U {=} = { $\$$ , =}**

- $S \rightarrow E$  (1)
- $E \rightarrow L = R$  (2)
- $E \rightarrow R$  (3)
- $L \rightarrow id$  (4)
- $L \rightarrow *R$  (5)
- $R \rightarrow L$  (6)

Follow ( $S$ ) = { $\$$ }  
 Follow ( $E$ ) = { $\$$ }  
 Follow ( $L$ ) = { $=, \$$ }  
 Follow ( $R$ ) = { $=, \$$ }

	id	=	*	\$	E	L	R
$s_0$	$S_4$		$S_5$		$S_1$	$S_2$	$S_3$
$s_1$				$r_2$			
$s_2$		$S_6 / r_6$		$r_6$			
$s_3$				$r_3$			
$s_4$		$r_4$		$r_4$			
$s_5$	$S_4$		$S_5$			$S_9$	$S_8$
$s_6$	$S_4$		$S_5$			$S_9$	$S_7$
$s_7$				$r_2$			
$s_8$		$r_5$		$r_5$			
$s_9$		$r_6$		$r_6$			

# The Limits of SLR(1)

**S** → **E**

**E** → **L** = **R**

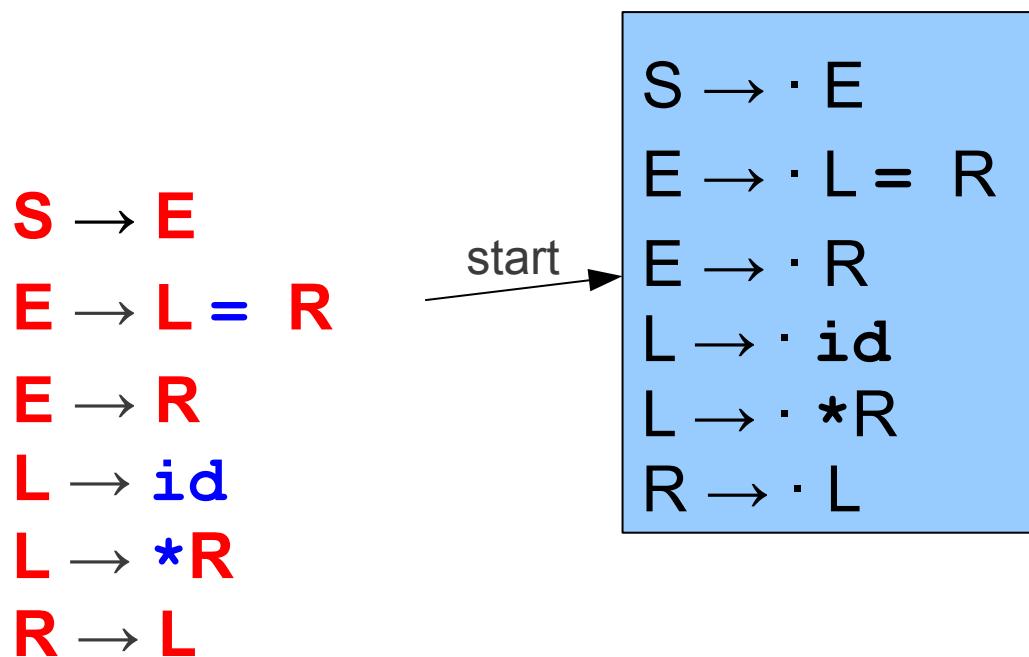
**E** → **R**

**L** → **id**

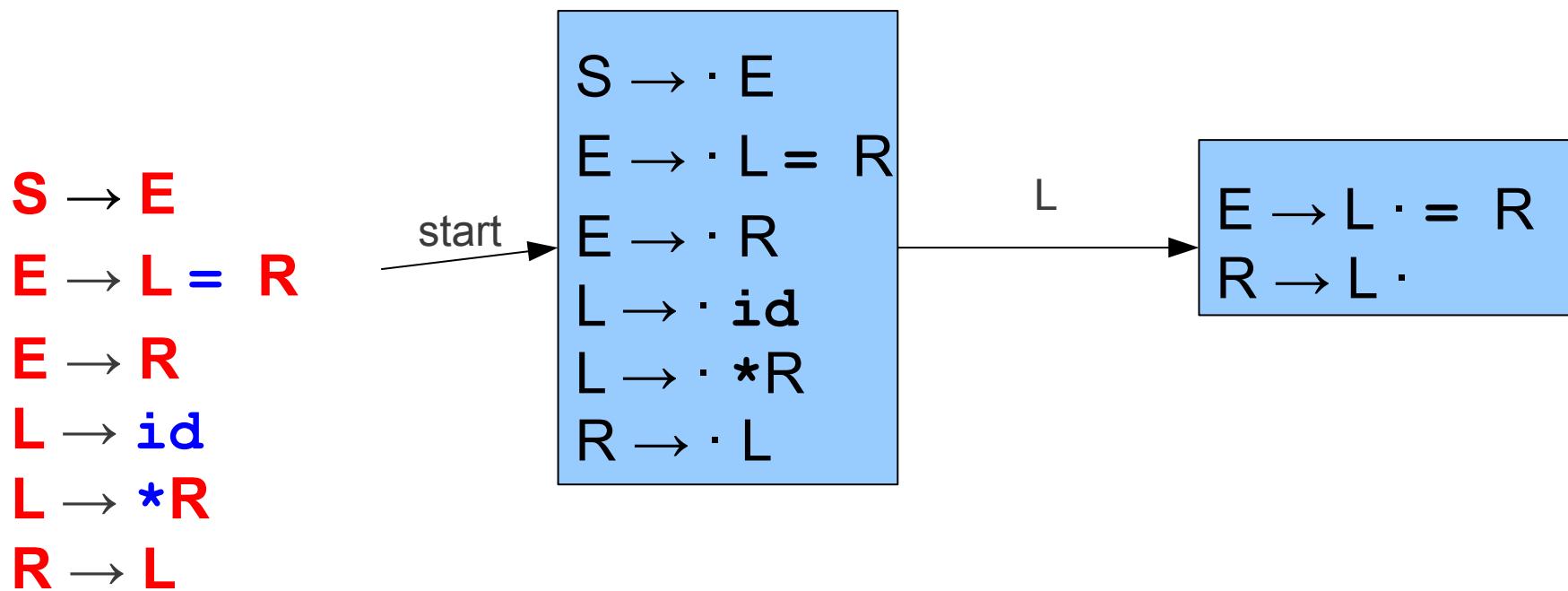
**L** → \***R**

**R** → **L**

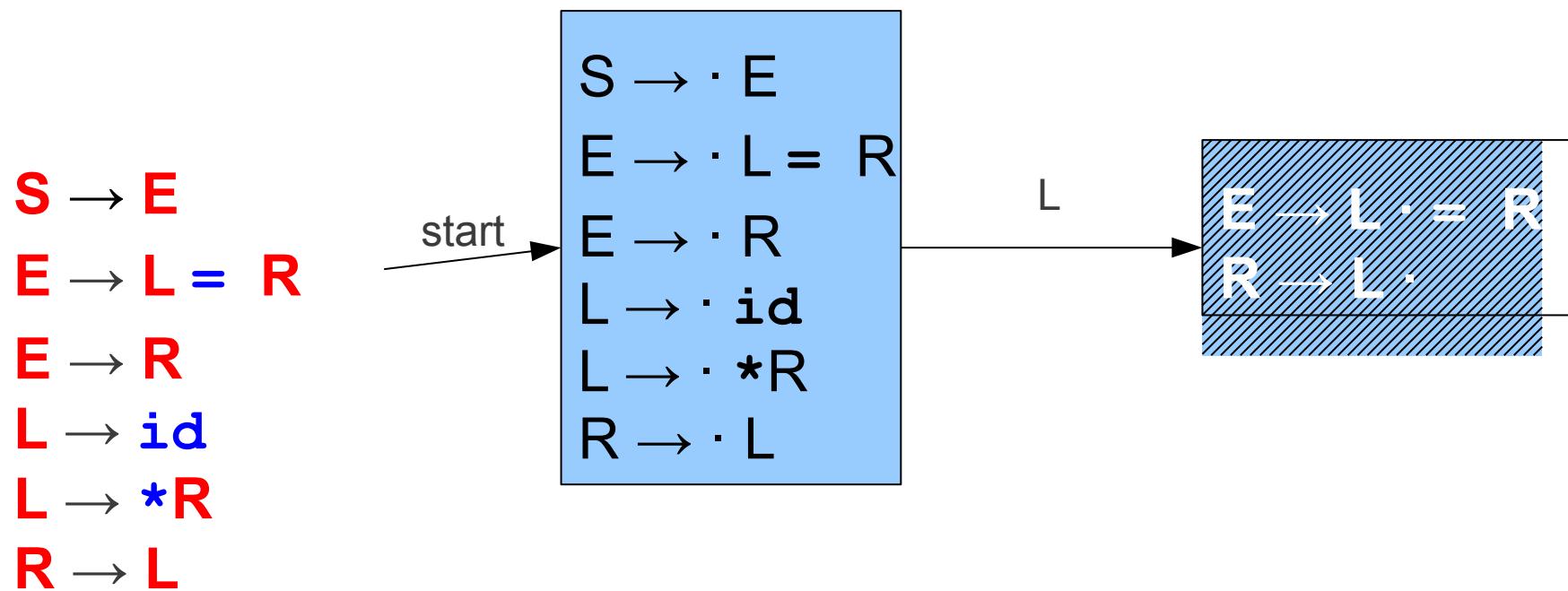
# The Limits of SLR(1)



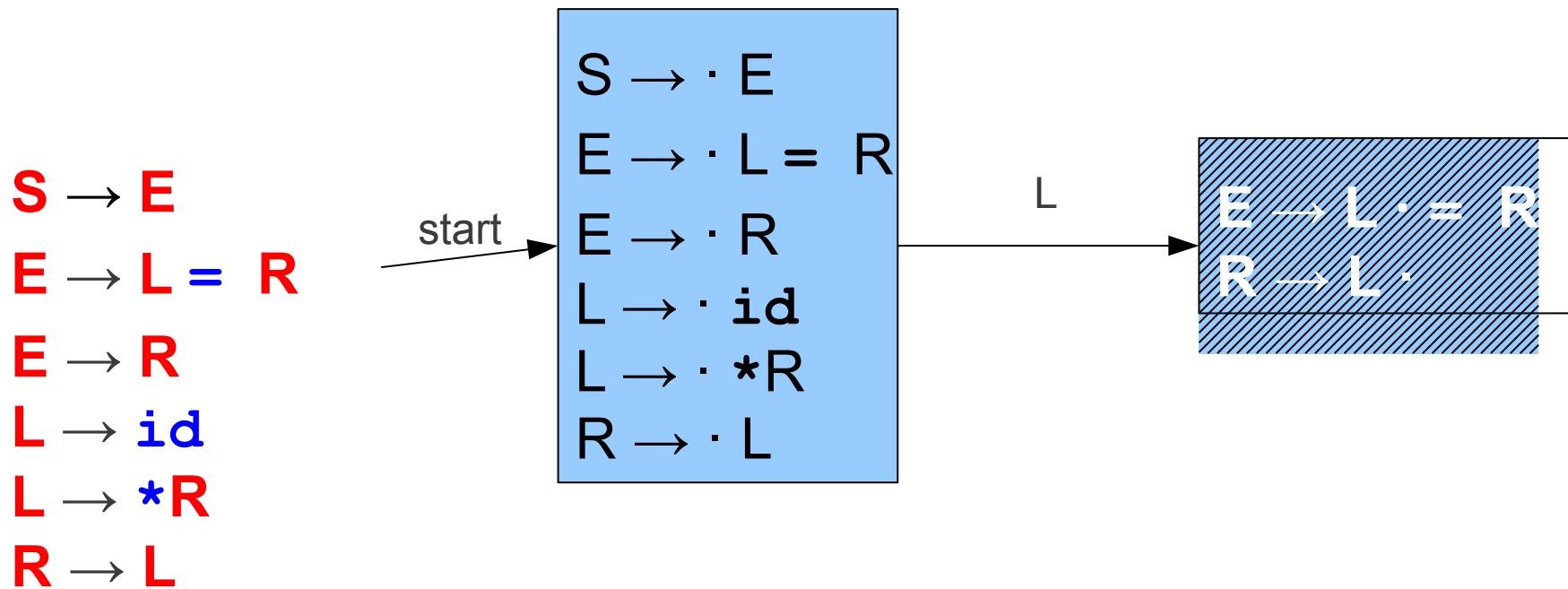
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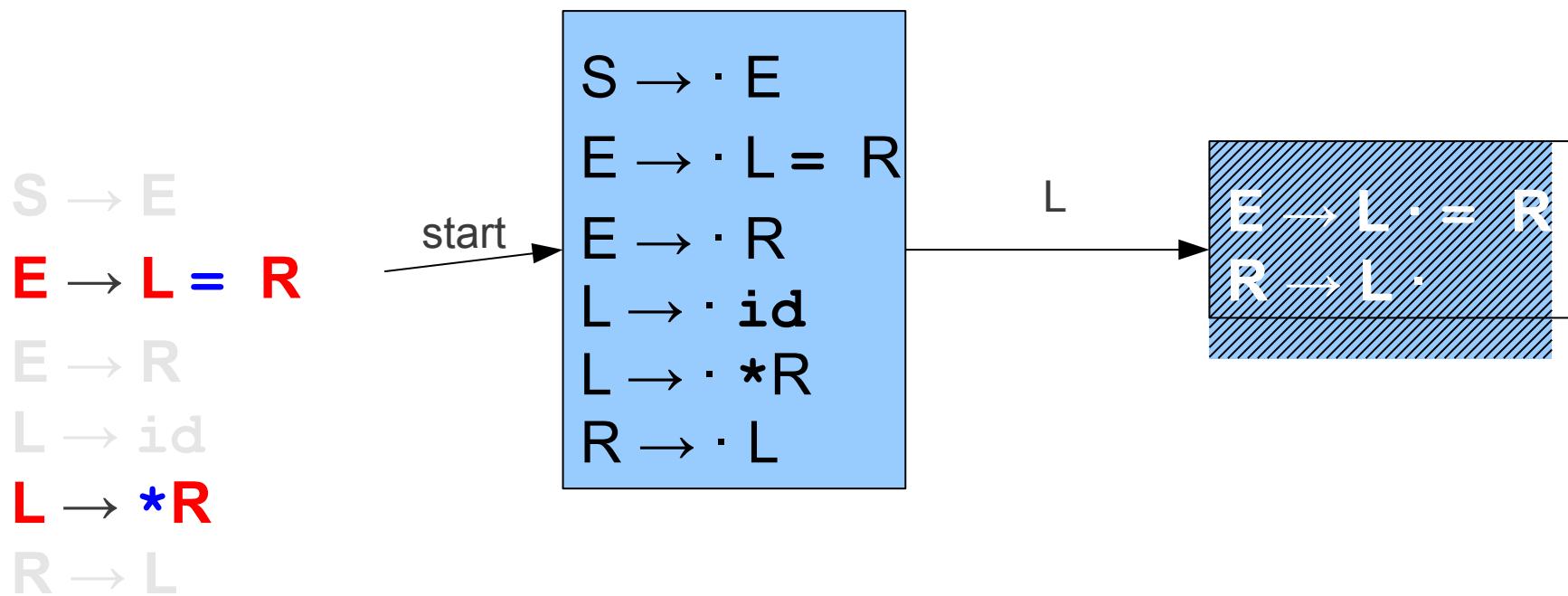


# The Limits of SLR(1)



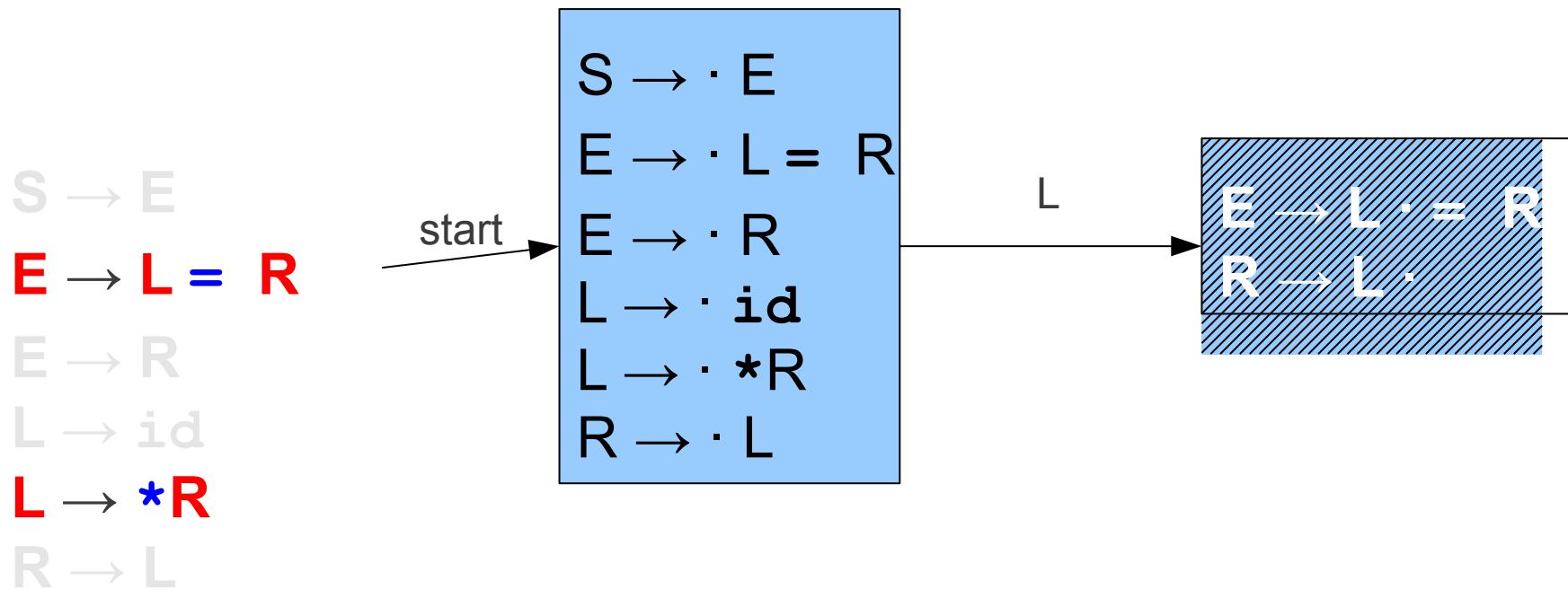
$E \rightarrow L \cdot = R$  tells us to shift on seeing  $=$   
 $R \rightarrow L \cdot$  tells us to reduce on FOLLOW( $R$ ).

# The Limits of SLR(1)



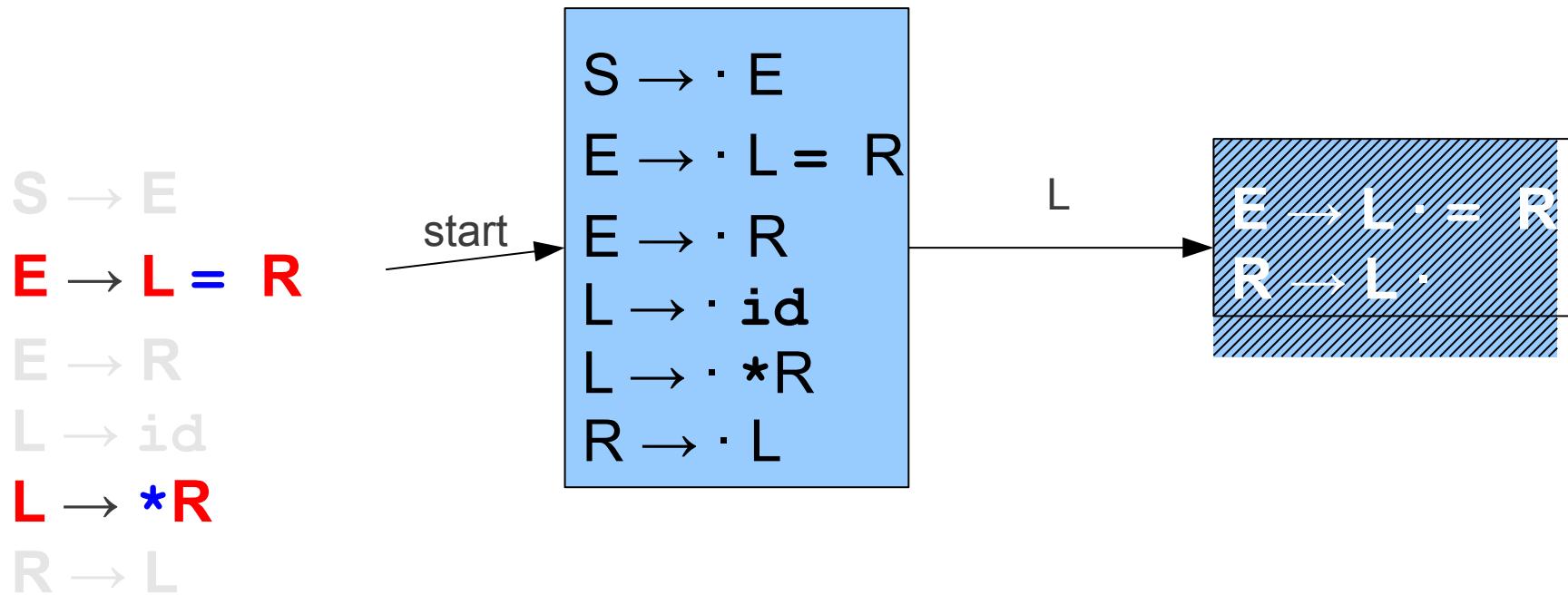
$E \rightarrow L \cdot = R$       tells us to shift on seeing  $=$   
 $R \rightarrow L \cdot$               tells us to reduce on FOLLOW( $R$ ).

# The Limits of SLR(1)



**$E \rightarrow L \cdot = R$**  tells us to shift on seeing **=**  
 **$R \rightarrow L \cdot$**  tells us to reduce on FOLLOW(**R**).  
**=**  $\in$  FOLLOW(**R**).

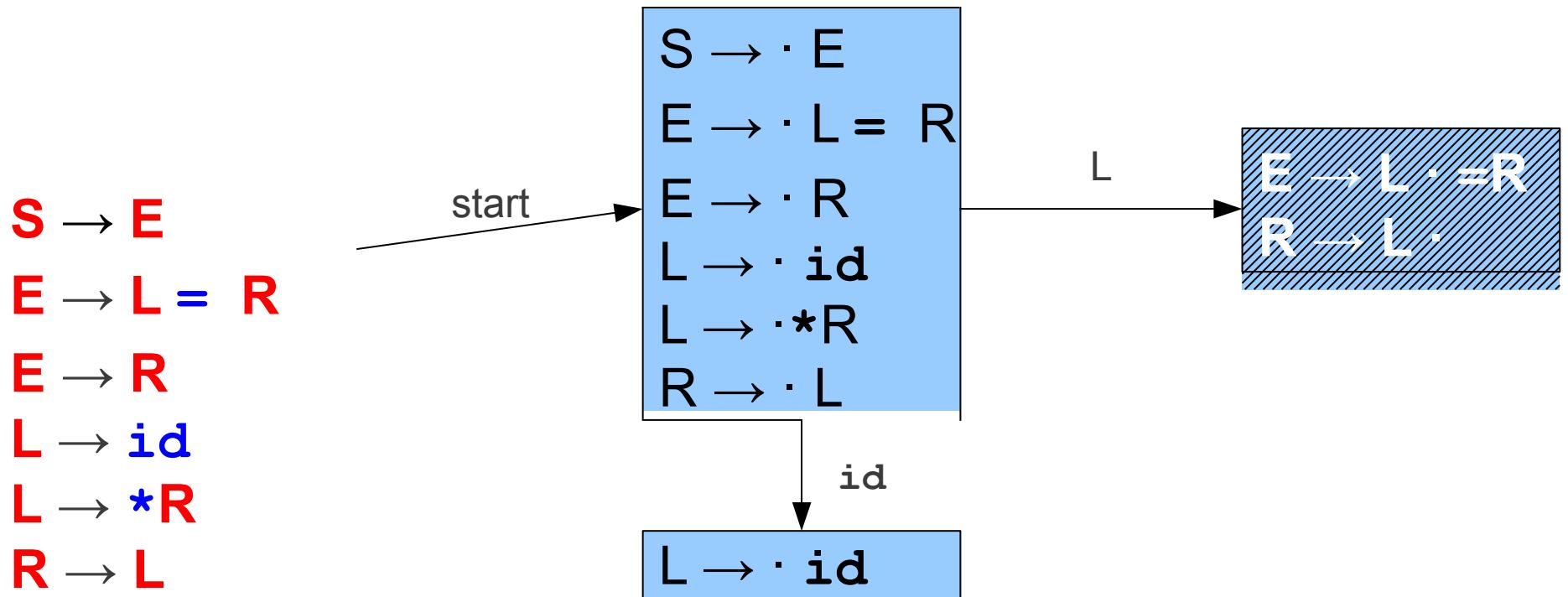
# The Limits of SLR(1)



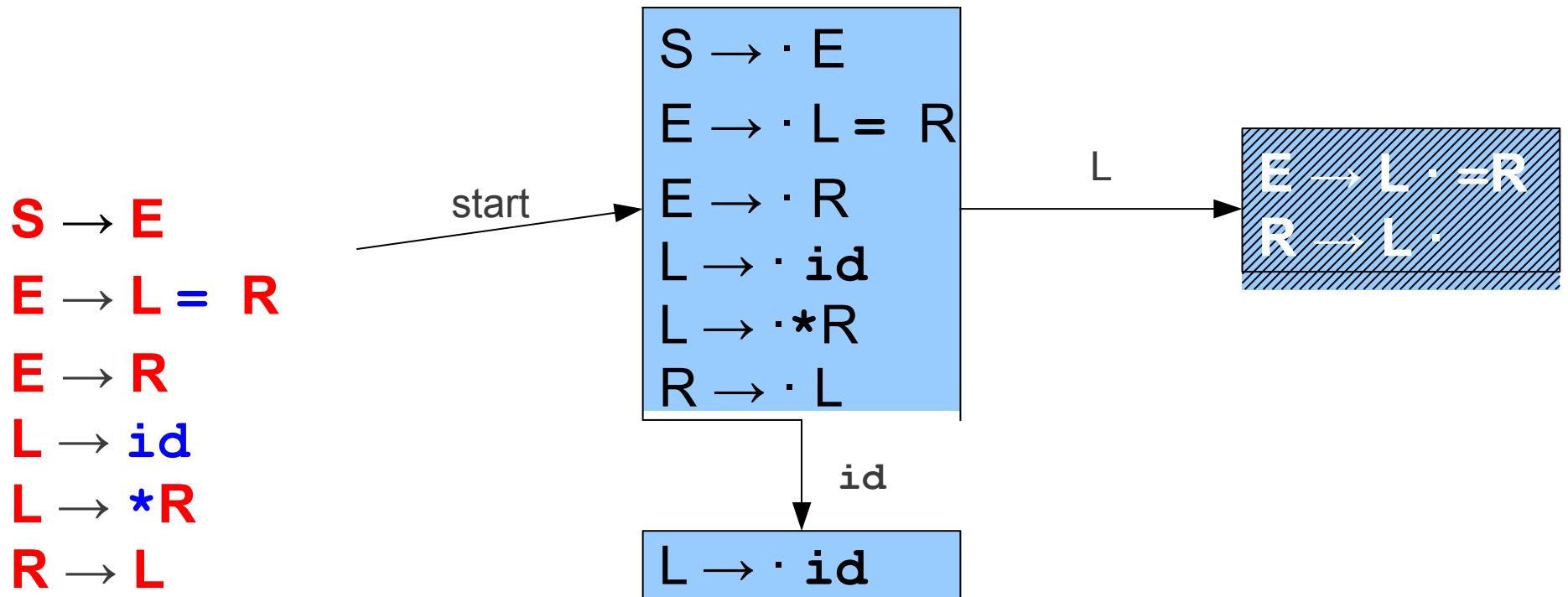
$E \rightarrow L \cdot = R$  tells us to shift on seeing  $=$   
 $R \rightarrow L \cdot$  tells us to reduce on FOLLOW( $R$ ).  
 $= \in \text{FOLLOW}(R)$ .

We have a conflict!

# A Lack of Context

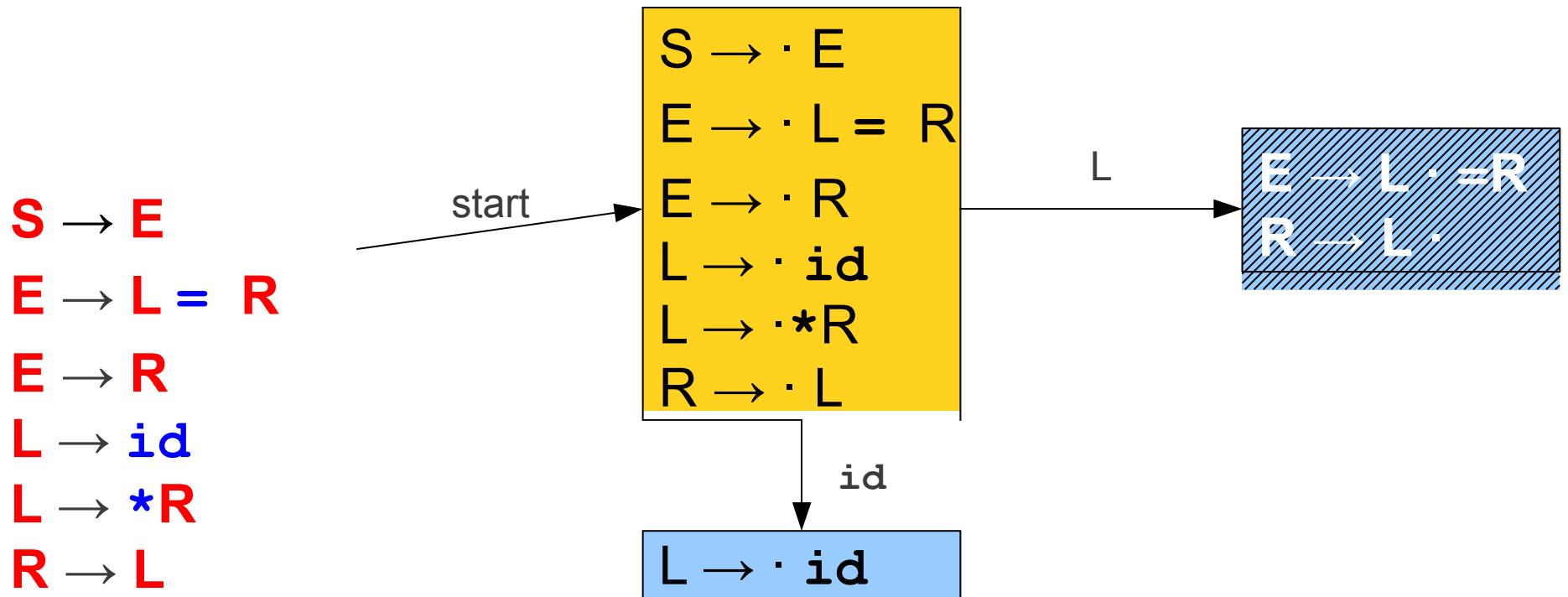


# A Lack of Context



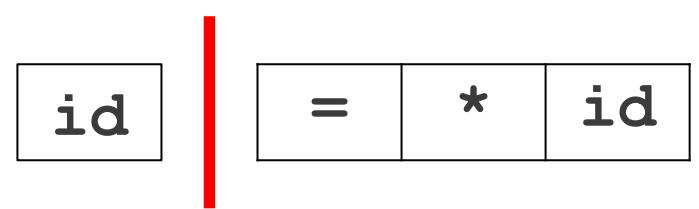
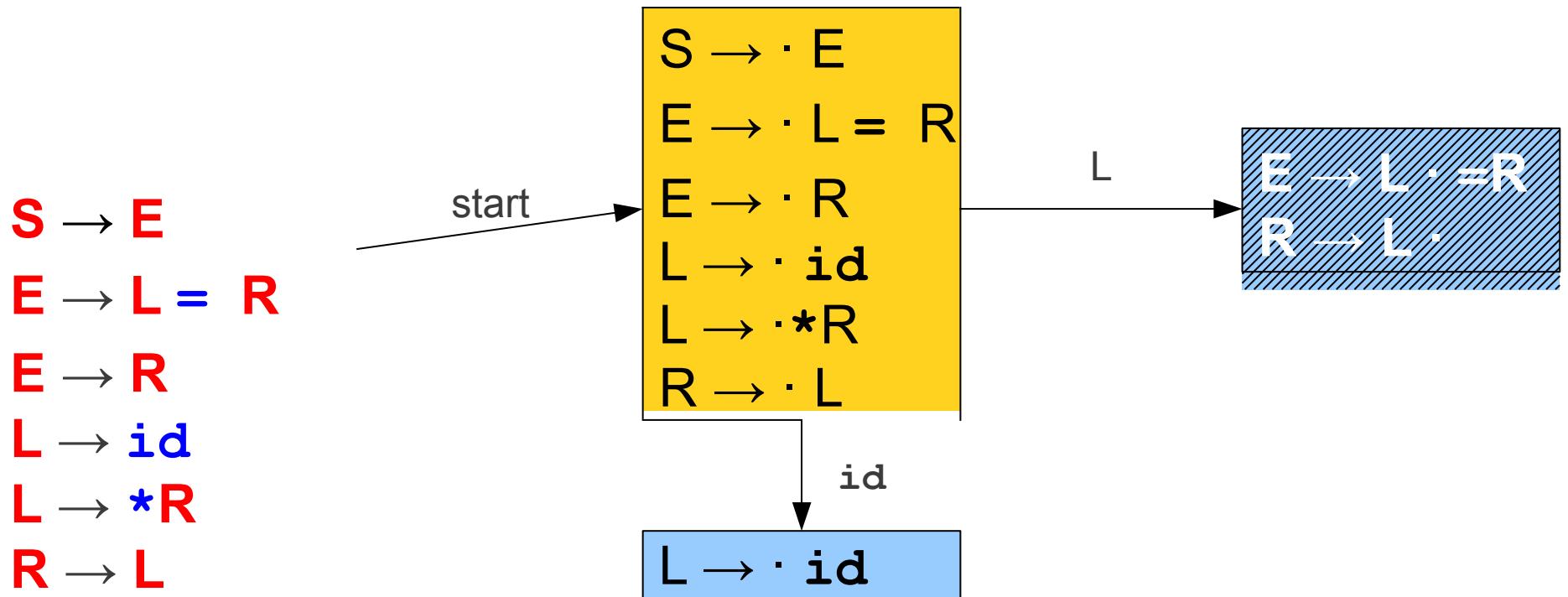
|      id    =    \*    id

# A Lack of Context

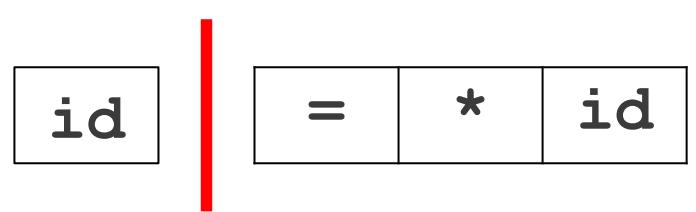
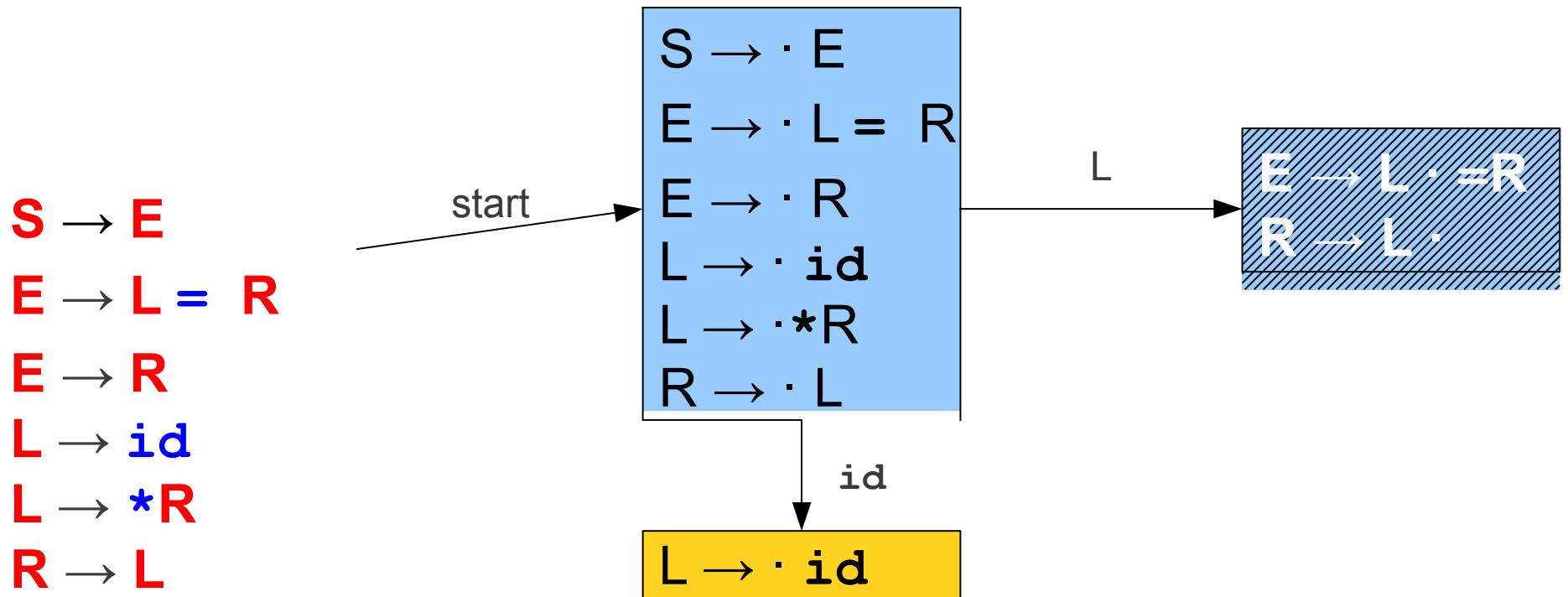


|      id      =      \*      id

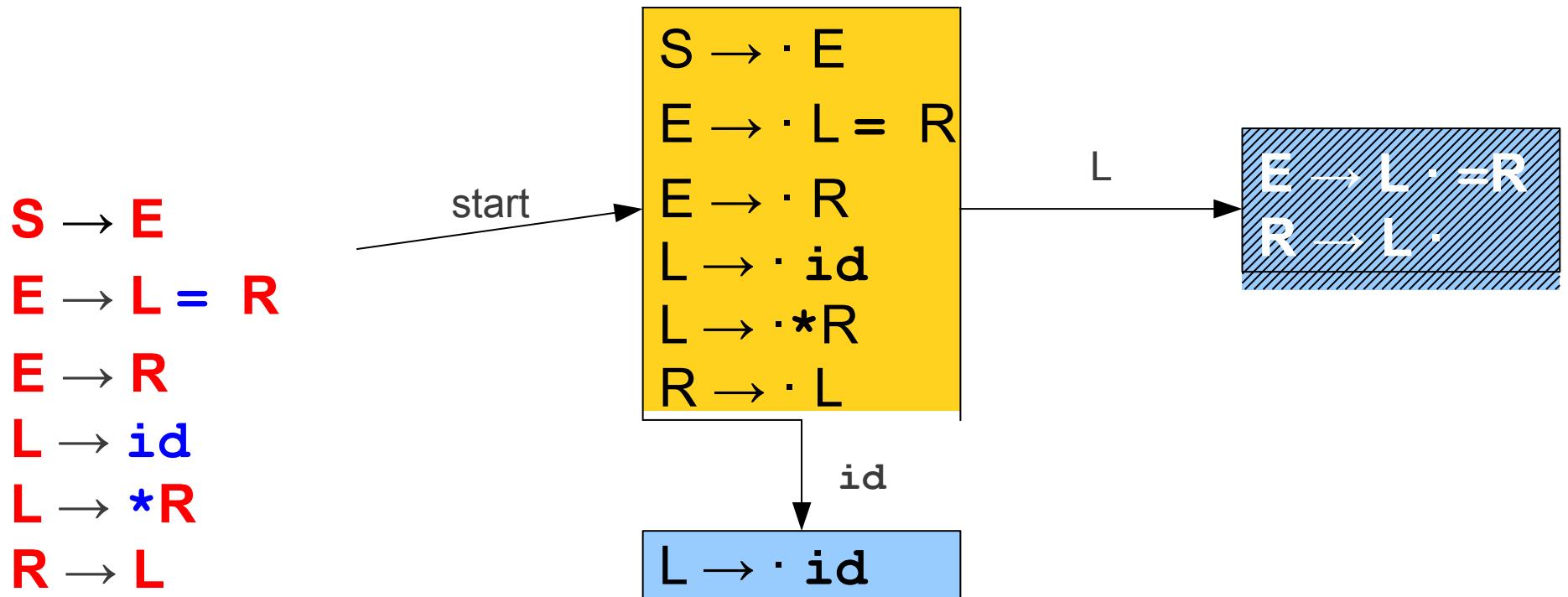
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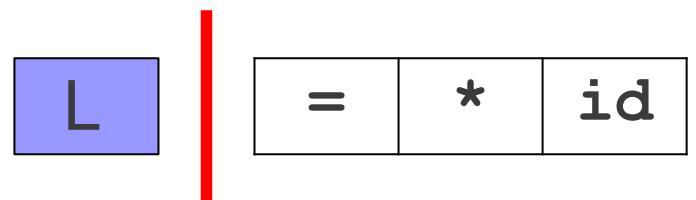
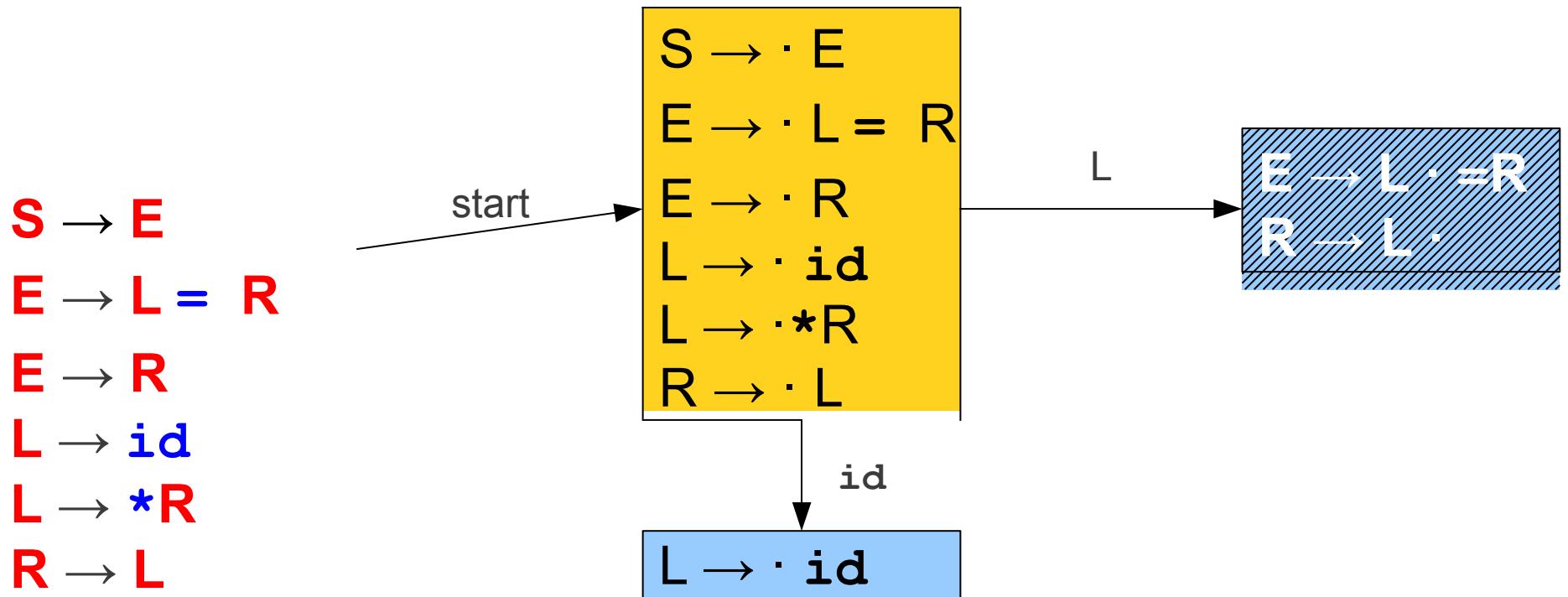


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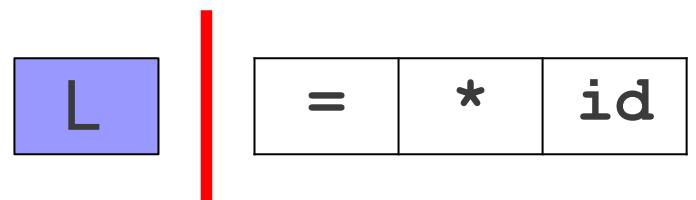
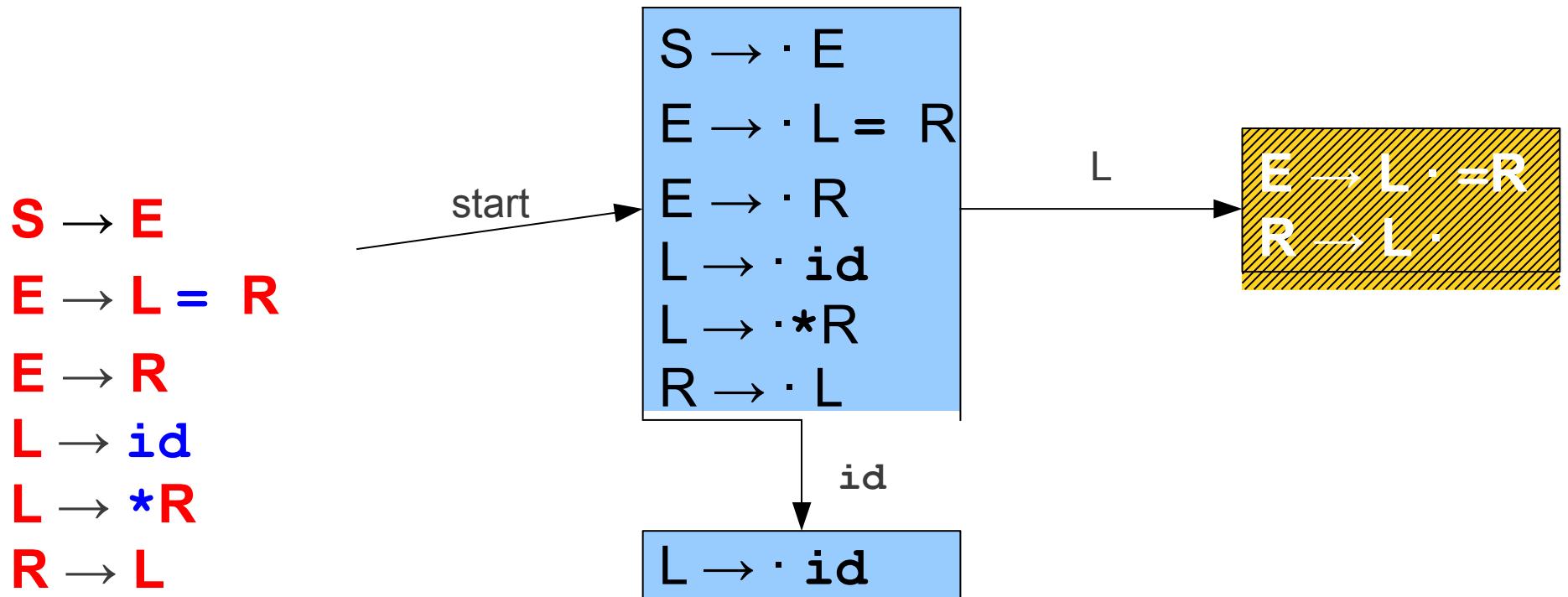


=    \*    id

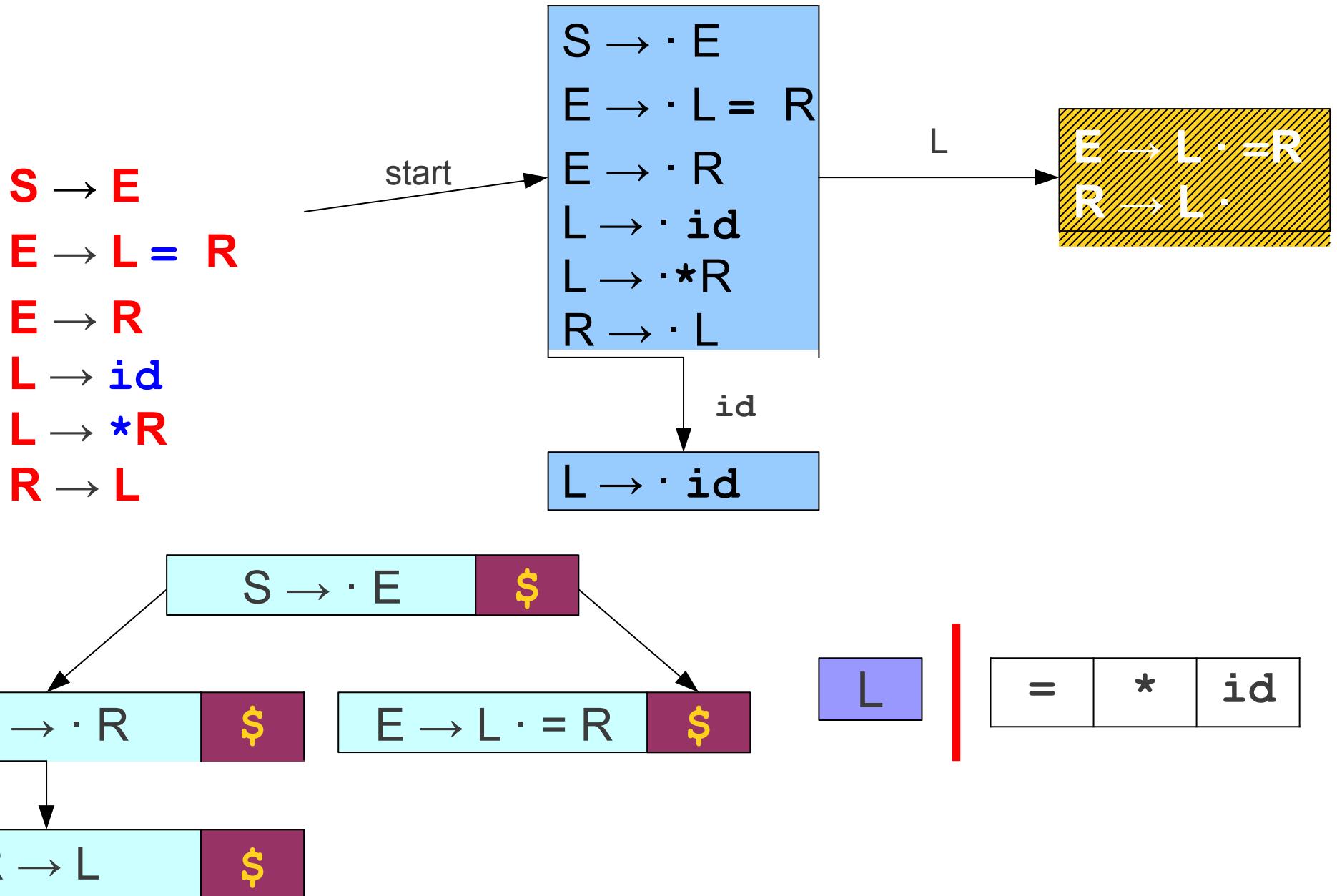
# A Lack of Context



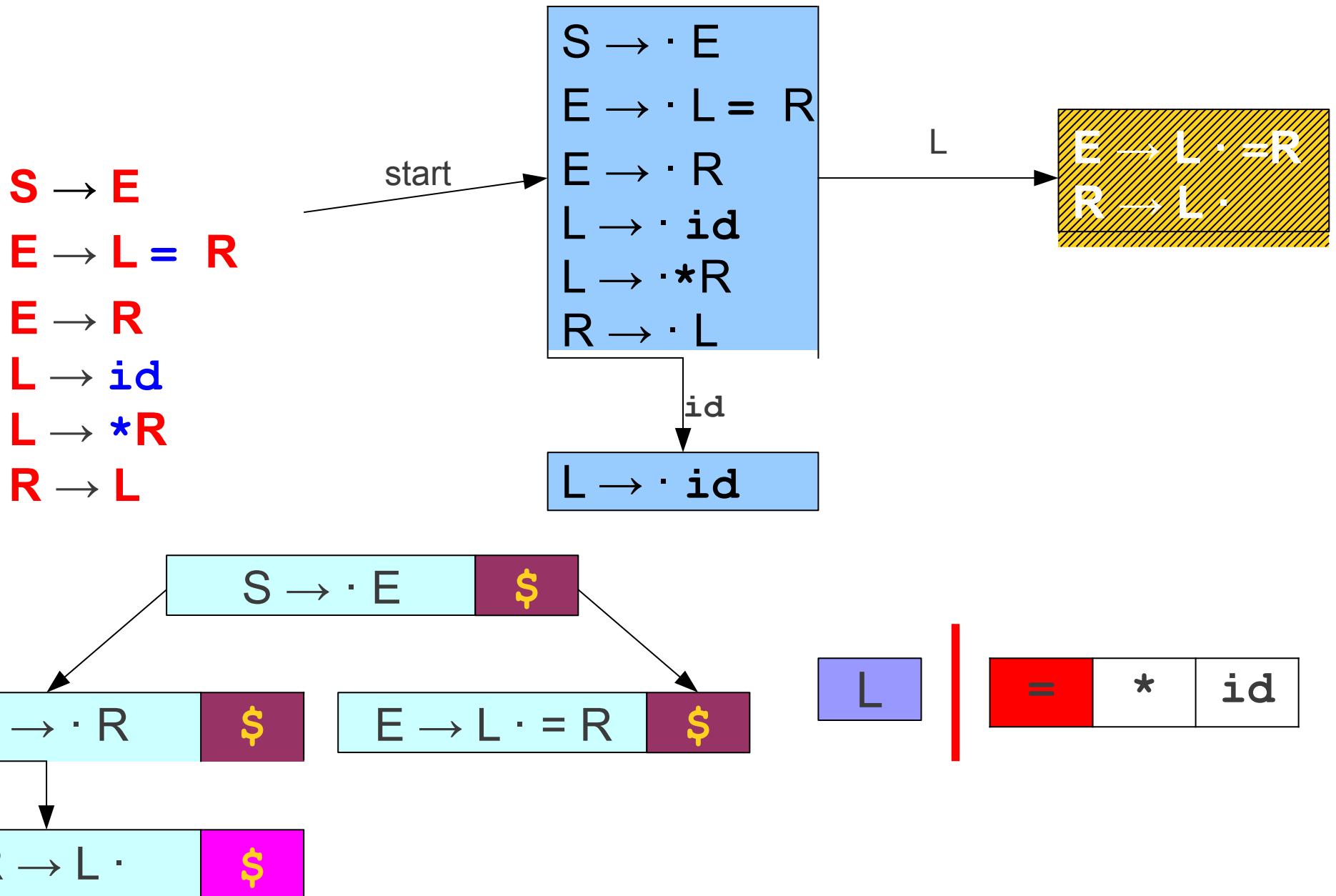
# A Lack of Context



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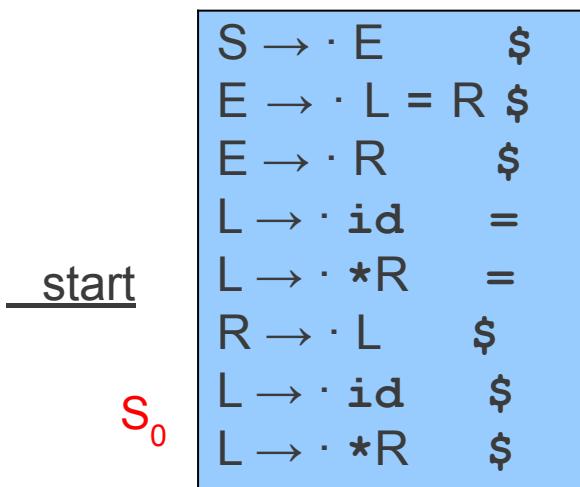


# Why is SLR(1) Weak?

- With SLR(1), *minimal* context.
  - FOLLOW(**A**) means “what could follow **A** somewhere in the grammar?,” even if in a particular state **A** couldn't possibly have that symbol after it.
- With LR(1), we have contextual information.

$S \rightarrow E$   
 $E \rightarrow L = R$   
 $E \rightarrow R$   
 $L \rightarrow id$   
 $L \rightarrow *R$   
 $R \rightarrow L$

# DFA for LR(1)

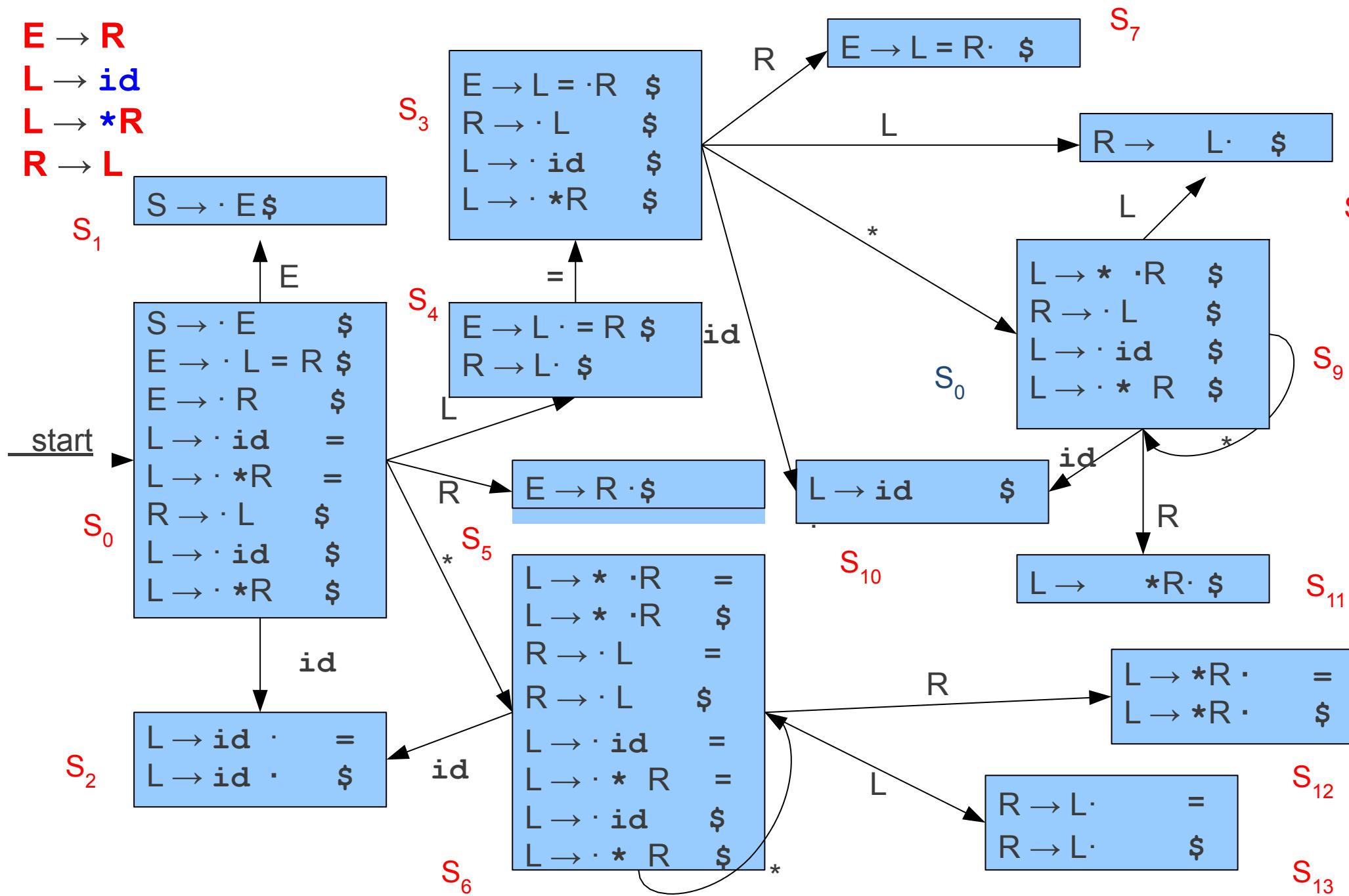


# Constructing LR(1) Items

- Begin in a state containing  $S \rightarrow \cdot E$ ,  $\$$  where  $S$  is the start symbol and  $\$$  is lookahead
- Compute the closure of the state:
  - If  $A \rightarrow a \cdot B\omega$ ,  $l$  is in the state, add  $B \rightarrow \cdot y$ ,  $t$  to the state for each production  $B \rightarrow y$  and for each terminal  $t \in \text{FIRST}^*(\omega l)$

$S \rightarrow E$   
 $E \rightarrow L = R$   
 $E \rightarrow R$   
 $L \rightarrow id$   
 $L \rightarrow *R$   
 $R \rightarrow L$

# DFA for LR(1)



# The LR(1) Parsing Algorithm

- Begin with an empty stack and the input set to  $\omega \$$ , where  $\omega$  is the string to parse. Set state to the initial state.
- Repeat the following:
  - Let the next symbol of input be  $t$ .
  - If  $\text{action}[\text{state}, t]$  is shift, then shift the input and set  $\text{state} = \text{goto}[\text{state}, t]$ .
  - If  $\text{action}[\text{state}, t]$  is reduce  $A \rightarrow \omega$ :
    - Pop  $|\omega|$  symbols off the stack; replace them with  $A$ .
    - Let the state atop the stack be top-state.
    - Set  $\text{state} = \text{goto}[\text{top-state}, A]$
  - If  $\text{action}[\text{state}, t]$  is accept, then the parse is done. If
  - $\text{action}[\text{state}, t]$  is error, report an error.

# Constructing LR(1) Parse Tables

- For each state  $X$ :
  - If there is a production  $A \rightarrow \omega \cdot [t]$ , set  $\text{action}[X, t] = \text{reduce } A \rightarrow \omega$ .
  - If there is the special production  $S \rightarrow E \cdot [\$]$ , where  $S$  is the start symbol, set  $\text{action}[X, t] = \text{accept}$ .
  - If there is a transition out of  $s$  on symbol  $t$ , set  $\text{action}[X, t] = \text{shift}$ .
- Set all other actions to error.
- If any table entry contains two or more actions, the grammar is not LR(1).