

Understanding factors:

(Y) Balance ~ Income (X_1)

↳ purpose: prediction

↳ use lm()

↗ Factor = $\begin{cases} \text{East} \\ \text{South} \\ \text{West} \end{cases}$

Balance ~ Income + Region

↳ how does R encode this?

↳ K categories → K-1 dummy variables

$$\text{Balance} = \hat{\beta}_0 + \hat{\beta}_1 \text{Income} + \hat{\beta}_2 X_{\text{south}}$$

$$+ \hat{\beta}_3 X_{\text{west}}$$

Credit

Balance

X_1
Income

X_2
Region

$$X_{\text{south}} = \begin{cases} 1 & \text{if S} \\ 0 & \text{if O/W} \end{cases}$$

$$X_{\text{west}} = \begin{cases} 1 & \text{if S} \\ 0 & \text{if O/W} \end{cases}$$

Y_1 14.891

X_{11} 883

South

Y_2 106.025

X_{12} 903

West

Y_3 104.593

X_{13} 580

⋮

Y_i

X_{ii}

$$\hookrightarrow \hat{\mathbf{B}} = \begin{pmatrix} \hat{\beta}_0 \\ \hat{\beta}_1 \\ \hat{\beta}_2 \\ \hat{\beta}_3 \end{pmatrix} = (\mathbf{X}^T \mathbf{X})^{-1} \mathbf{X}^T \mathbf{Y}$$

$$\mathbf{Y} = \text{Balance}, \quad \mathbf{X} = \begin{pmatrix} 1 & X_1 & X_{\text{south}} & X_{\text{west}} \\ \vdots & \vdots & \vdots & \vdots \end{pmatrix}$$