

Understanding factors:

(Y) Balance ~ Income (X_1)

↳ purpose: prediction

↳ Use lm(.)

Factor = { East
South
West }

Balance ~ Income + Region

↳ how does R encode this?

↳ K categories → K-1 dummy variables

$$\text{Balance} = \hat{B}_0 + \hat{B}_1 \text{Income} + \hat{B}_2 X_{\text{south}}$$

$$+ \hat{B}_3 X_{\text{west}}$$

Credit

	X_1 Income	X_2 Region	
Balance			
y_1 14.891	x_{11} 883	SOUTH	$X_{\text{south}} = \begin{cases} 1 & \text{if S} \\ 0 & \text{if O/W} \end{cases}$
y_2 106.025	x_{12} 903	West	$X_{\text{west}} = \begin{cases} 1 & \text{if S} \\ 0 & \text{if O/W} \end{cases}$
y_3 104.593	x_{13} 580	West	
		:	
$\underbrace{y_i}_{Y_i}$	$\underbrace{x_{ii}}_{X_{ii}}$		

↳ $\hat{B} = \begin{pmatrix} \hat{B}_0 \\ \hat{B}_1 \\ \hat{B}_2 \\ \hat{B}_3 \end{pmatrix} = (X^T X)^{-1} X^T Y$

$Y = \text{Balance}, X = \begin{pmatrix} 1 & x_1 & X_{\text{south}} & X_{\text{west}} \end{pmatrix}$