Università degli studi di Padova
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Tesi di Dottorato

Search for heavy resonances decaying into a Z boson and a vector boson in the $\nu\bar{\nu}\,q\bar{q}$ final state at CMS

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"I have no special talent. I am only passionately curious."
(A. Einstein)

Contents

1 *Abstract*

Chapter 1

Introduction

This analysis searches for signal of heavy resonances decaying into a pair of heavy vector bosons. One Z boson is identified through its invisible decay ($\nu\nu$), while the other is required to decay hadronically into a pair of quarks. The final states probed by this analysis therefore consists in two quarks and two neutrinos, reconstructed as missing transverse energy (met). The hadronically decaying boson (Z, W) is reconstructed as a fat jet, whose mass is used to define the signal region. Two purity categories are exploited, based on the n-subjettines of the fat jet.

The search is performed by examining the distribution of the diboson reconstructed transverse mass of the resonance VZ (mtVZ) for a localized excess. The shape and normalization of the main background of the analysis (V+jets) are estimated with an hybrid approach using the distribution of data in the sidebands, corrected for a function accounting for potential differences between the signal region and the sidebands, while the minor background sources are taken from simulations.

Chapter 2

Theoretical motivation

The Standard Model (SM) of particles represents, so far, the best available description of the particles and their interactions. It is the summation of two gauge theories: the electroweak interaction, that pictures together the weak and electromagnetic interactions, and the strog interaction, or Quantum Chromodynamics (QCD). Particles, namely quarks and leptons, are described by spin 1/2 fermions, whilst interactions are embodied by spin 1 bosons. The simmetry group of the standard model is:

$$SU_C(3) \times SU_L(2) \times U_Y(1), \tag{2.1}$$

where the first factor is related to strong interactions, whose mediators are eight gluons, whilst $SU_L(2) \times U_Y(1)$ is the electroweak simmetry group, whose mediators are photons and Z-$W^\pm$ bosons.

In renormalizable theories, with no anomalies, all gauge bosons are expected to be massless, in contrast with our experimental knowledge (cite W-Z discovery). This kind of dilemma can be solved by introducing a new scalar particle, the Higgs boson (cite Higgs article), that can give mass to weak bosons and fermions via the spontaneous symmetry breaking mechanism.

In the last decades, Standard Model has been accurately probed by many experimental facilities (LEP, Tevatron), demonstrating an impressive agreement between theoretical predictions and experimental results. The discovery of the Higgs boson at the CERN Large Hadron Collider, measured by both CMS and ATLAS collaborations [1–7], represents not only an extraordinary confirmation of the model, but also the latest biggest achievement in particle physics as a whole.

2.1 Beyond Standard Model theories

Even though the Standard Model is the most complete picture of the universe of the particles, many questions are still left open by the model. From a phenomenological point of view, some experimental observations are not included in the theory:

- in SM, neutrinos are massless (whilst experimentally it has been confirmed to be non-zero, i.e. by the neutrino oscillation);

44   • no candidate for the dark matter is foreseen (whilst it has been observed in cosmology);

45   • no fields included in the SM can explain the cosmological inflation;

46   • SM can not justify the matter-antimatter asymmetry.

47 From a purely theoretical perspective, some issues are still relevant in the formulation of the
48 model:

49   • *Flavour problem.*
50   The Standard Model has 18 free parameters: 9 fermionic masses; 3 angular parameters in
51   Cabibbo-Kobayashi-Maskawa matrix, plus 1 phase parameter; electromagnetic coupling
52   α; strong coupling α_{strong}; weak coupling α_{weak}; Z mass; the mass of the Higgs boson.
53   Such a huge number of degrees of freedom is considered as weakly predictive.

54   • *Unification.*
55   There is not a "complete" unification of strong, weak and electromagnetic interactions,
56   since each one has its own coupling constant, behaving differently at different energy
57   scales; not to mention the fact that gravitational interaction, completely excluded from
58   the SM.

59   • *Hierarchy problem.*
60   From Quantum Field Theory, it is known that perturbative corrections to the mass of
61   the scalar bosons included in the theory tend to make it increase towards the energy
62   scale at which the considered theory is valid [cite n. 4 of master thesis]. If the Standard
63   Model is seen as a low-mass approximation of a more general theory valid uo to the
64   Planck mass scale (i.e., $\approx 10^{19}$ GeV), a fine-tuning cancellation of the order of 1 over 10^{34}
65   is needed in order to protect the Higgs mass at the electroweak scale (≈ 100 GeV). Such
66   an astonishing correction is perceived as very unnatural.

67 Numerous Beyond Standard Model theories (BSM) have been proposed in order to over-
68 come the limits of the Standard Model.

69 Grand Unified Theories (GUT) aim at extending the symmetry group of the SM (eq. 1) into
70 largest candidates, such as $S0(10)$, $SU(5)$ and $E(6)$. At GUT scale, approximately at 10^{16} GeV,
71 non-gravitational interactions are expected to be ruled by only one coupling constant, α_{GUT}.

72 Super Symmetryc (SUSY) models state that every fermion (boson) of the Standard Model
73 has a bosonic (fermionic) superpartner, with exactly the same quantum numbers, except the
74 spin. If SUSY is not broken, each couple of partners and superpartners should have the same
75 masses, hypotesis easily excluded by the non-observation of the s-electron. Super Symmetry
76 represents a very elegant solution of the hierarchy problem of the Higgs boson mass, since
77 the perturbative corrections brought by new SUSY particles exactly cancel out the divergences
78 caused by SM particles corrections. A particular sub-class of SUSY models, Minimal Super
79 Symmetric Standard Models, is characterized by the introduction of a new symmetry, the R-
80 parity, that guarantees the proton stability and also the stability of the lightest SUSY particle,
81 a possible good candidate for dark matter.

82 Two other possible theoretical pictures are extensively described in sec. 2.2-2.3.

2.2 Heavy Vector Triplet

The heavy vector triplet model [8] provides a general framework aimed at studying new physics beyond the standard model, that can manifest into the appearance of new resonances. The adopted approach is that of the simplified model, in which an effective Lagrangian is introduced, in order to describe the properties and interactions of new particles (in this case, a triplet of spin-1 bosons) by using a limited set of parameters, that can be easily linked to the physical observables at the LHC experiments. These parameters can describe many physical motivated theories (such as sequential extensions of the SM [9, 10] or Composite Higgs [11, 12]).

Since a simplified model is not a complete theory, its validity is restricted to the on-shell quantities related to the production and decay mechanisms of new resonances, that is the case of most of the LHC BSM searches are performed. Given these conditions, experimental results in the resonant region are sensitive to a limited number of the phenomenological Lagrangian parameters (or to a combination of those), whilst the remaining parameters tend to influence the tail of the distributions.

Limits on production cross-section times branching ratio ($\sigma \mathcal{B}$), as a function of the invariant mass spectrum of the probed resonance, can be extracted from experimental data. Given that $\sigma \mathcal{B}$ are functions of the simplified model parameters and of the parton luminosities, it is then possible to interpret the observed limits in the parameter space.

2.2.1 Simplified Lagrangian

The heavy vector triplet framework assumes the existence of an additional vector triplet, V_μ^a, $a = 1, 2, 3$, in which two spin-1 particles are charged and one is neutral:

$$V_\mu^\pm = \frac{V_\mu^1 \mp i V_\mu^2}{\sqrt{2}}; \ V_\mu^0 = V_\mu^3.$$ (2.2)

The triplet interactions are described by a simplified Lagrangian, that is invariant under SM gauge and CP symmetry, and accidentally invariant under the custodial symmetry $SU(2)_L \times SU(2)_R$:

$$
\begin{aligned}
\mathcal{L}_\mathcal{V} = & -\frac{1}{4} \left(D_\mu V_\nu^a - D_\nu V_\mu^a \right) \left(D^\mu V^{\nu\,a} - D^\nu V^{\mu\,a} \right) + \frac{m_V^2}{2} V_\mu^a V^{\mu\,a} \\
& + i g_V c_H V_\mu^a \left(H^\dagger \tau^a D^\mu H - D^\mu H^\dagger \tau^a H \right) + \frac{g^2}{g_V} c_F V_\mu^a \sum_f \bar{f}_L \gamma^\mu \tau^a f_L \\
& + \frac{g_V}{2} c_{VVV} \epsilon_{abc} V_\mu^a V_\nu^b \left(D^\mu V^{\nu\,c} - D^\nu V^{\mu\,c} \right) + g_V^2 c_{VVHH} V_\mu^a V^{\mu\,a} H^\dagger H - \frac{g}{2} c_{VVW} \epsilon_{abc} W^{\mu\nu\,a} V_\mu^b V_\nu^c.
\end{aligned}
$$ (2.3)

In the first line of the formula 2.3, V mass and kinematic terms are included, described with the covariant derivative $D_\mu V_\nu^a = \partial_\mu V_\nu^a + g \epsilon^{abc} W_\mu^b V_\nu^c$, where W_μ^a are the fields of the weak interaction and g is the weak gauge coupling. V_μ^a are not mass eigenstates, since they mix with the electroweak fields after the spontaneous symmetry breaking, therefore m_V isn't the physical mass of the V bosons.

4

The second line describes the interaction of the triplet with the Higgs field and the SM left-handed fermions; c_H describes the vertices with the physical Higgs and the three unphysical Goldstone bosons that, for the Goldstone equivalence theorem, are connected to the longitudinal polarization of W and Z bosons at high-energy; hence, c_H is related to the bosonic decays of the resonances. c_F is the analogous parameter describing the V interaction with fermions, that can be generalized as a flavour dependent coefficent, once defined $J_F^{\mu\ a} = \sum_f \bar{f}_L \gamma^\mu \tau^a f_L$:
$c_F V_\mu^a J_F^{\mu\ a} = c_\ell V_\mu^a J_\ell^{\mu\ a} + c_q V_\mu^a J_q^{\mu\ a} + c_3 V_\mu^a J_3^{\mu\ a}$.
The last part of the equation includes terms that are relevant only in strongly coupled scenarios (see sec. 2.2.2) through the V-W mixing, but it does not include vertices of V with light SM fields, hence it can be neglected while describing the majority of the LHC phenomenology, under the assumptions previously stated. Additional dimension four quadrilinear V interactions are non relevant for the processes discussed, otherwise their effects would be appreciated in electroweak precision tests and precise Higgs coupling measurements [13].

The parameters in the Lagrangian can be interpreted as follows: g_V describes the strenght of the interaction, that is weighted by c parameters. g_V ranges from $g_V \sim 1$ when the coupling is weak (sec. 2.2.4), to $g_V \sim 4\pi$ when the coupling is strong (sec. 2.2.5). c parameters are expected to be $c \sim 1$, except to c_H, that can be smaller for weak couplings. The combinations describing the vertices, $g_V c_H$ and $g^2/g_v c_F$, can be considered as the fundamental parameters, used to interpret the experimental results.

2.2.2   Mass eigenstates, mixing parameters and decay widths

The newly introduced $SU(2)_L$ triplet is expected to mix with the weak SM fields. The $U(1)_{em}$ symmetry is left unbroken by the new interaction, hence the massless combination of the electroweak fields, namely the photon, is the same as the SM:

$$A_\mu = B_\mu \cos\theta_W + W_\mu^3 \sin\theta_W, \tag{2.4}$$

with the usual definitions of the electroweak parameters:

$$\tan\theta_W = \frac{g'}{g}$$
$$e = \frac{gg'}{\sqrt{g^2 + g'^2}} \tag{2.5}$$
$$g = e/\sin\theta_w; g' = e/\cos\theta_w.$$

The Z boson, on the other hand, mixes with the neutral component of the triplet, V^0, with a rotation parametrized with the angle θ_N:

$$\begin{pmatrix} \cos\theta_N & \sin\theta_N \\ -\sin\theta_N & \cos\theta_N d \end{pmatrix} \begin{pmatrix} Z \\ V^0 \end{pmatrix}. \tag{2.6}$$

The mass matrix of the rotated system is given by:

$$\mathbb{M}_N^2 = \begin{pmatrix} \hat{m}_Z^2 & c_H \zeta \hat{m}_Z \hat{m}_V \\ c_H \zeta \hat{m}_Z \hat{m}_V & \hat{m}_V^2 \end{pmatrix}, \tag{2.7}$$

where the parameters are defined as:

$$\begin{cases} \hat{m}_Z = \frac{e}{2\sin\theta_W \cos\theta_W}\hat{v} \\ \hat{m}_V^2 = m_V^2 + g_V^2 c_{VVHH}\hat{v}^2 \\ \zeta = \frac{g_V\hat{v}}{2\hat{m}_V} \\ \frac{\hat{v}^2}{2} = \langle H^\dagger H \rangle \end{cases} , \tag{2.8}$$

and $\hat{v}$, the vacuum expectation value of the Higgs field, can be different from the SM $v = 246$ GeV. The physical masses of Z and V^0, m_Z and M_0, and θ_N come from the matrix relations:

$$\begin{aligned} \text{Tr}\left(\mathbb{M}_N^2\right) &= \hat{m}_Z^2 + \hat{m}_V^2 = m_Z^2 + M_0^2 \\ \left\|\mathbb{M}_N^2\right\| &= \hat{m}_Z^2 + \hat{m}_V^2\left(1 - c_H^2\zeta^2\right) = m_Z^2 M_0^2 \\ \tan 2\theta_N &= \frac{2c_H\zeta\hat{m}_Z\hat{m}_V}{\hat{m}_V^2 - \hat{m}_Z^2}. \end{aligned} \tag{2.9}$$

The $W^\pm$ bosons mix with the charged components of the triplet, $V^\pm$, leading to a mass matrix analogous to eq. 2.10:

$$\mathbb{M}_C^2 = \begin{pmatrix} \hat{m}_W^2 & c_H\zeta\hat{m}_W\hat{m}_V \\ c_H\zeta\hat{m}_W\hat{m}_V & \hat{m}_V^2 \end{pmatrix}, \tag{2.10}$$

where $\hat{m}_W$ is defined as:

$$\left\{ \hat{m}_W = \frac{e}{2\sin\theta_W}\hat{v} = \hat{m}_Z\cos\theta_W \right. ; \tag{2.11}$$

the physical masses of W and $V^\pm$, m_W and $M_\pm$, and the angle θ_C parametrizing the rotation of the charged sector are described by:

$$\begin{aligned} \text{Tr}\left(\mathbb{M}_C^2\right) &= \hat{m}_W^2 + \hat{m}_V^2 = m_W^2 + M_\pm^2 \\ \left\|\mathbb{M}_C^2\right\| &= \hat{m}_W^2 + \hat{m}_V^2\left(1 - c_H^2\zeta^2\right) = m_W^2 M_\pm^2 \\ \tan 2\theta_C &= \frac{2c_H\zeta\hat{m}_W\hat{m}_V}{\hat{m}_V^2 - \hat{m}_W^2}. \end{aligned} \tag{2.12}$$

The custodial symmetry of eq. 2.3 guarantees that:

$$\mathbb{M}_C^2 = \begin{pmatrix} \cos\theta_W & 0 \\ 0 & 1 \end{pmatrix} \mathbb{M}_N^2 \begin{pmatrix} \cos\theta_W & 0 \\ 0 & 1 \end{pmatrix}. \tag{2.13}$$

By taking the determinant of this matrices, a custodial relation among the masses can be extracted:

$$m_W^2 M_\pm^2 = \cos\theta_W m_Z^2 M_0^2, \tag{2.14}$$

that has some very important consequences.
Given that this model aims at searching new particles in the TeV scale and that the scale of the electroweak interactions must lay at ~ 100 GeV, a hierarchy of the physical masses seems very natural:

$$\frac{\hat{m}_{(W,Z)}}{\hat{m}_V} \sim \frac{m_{(W,Z)}}{M_{(\pm,0)}} \ll 1; \tag{2.15}$$

159 ζ parameter can be $\zeta \ll 1$ (weakly coupled scenario) or $\zeta \sim 1$ (strongly coupled scenario).

160 When eq. 2.15 applies, the second lines in eq. 2.9 and eq. 2.12 can be approximated as follows:

161

$$
\begin{aligned}
m_Z^2 &= \hat{m}_Z^2 \left(1 - c_H^2 \zeta^2\right) \left(1 + \mathcal{O}(\hat{m}_Z^2/\hat{m}_V^2)\right) \\
m_W^2 &= \hat{m}_W^2 \left(1 - c_H^2 \zeta^2\right) \left(1 + \mathcal{O}(\hat{m}_W^2/\hat{m}_V^2)\right)
\end{aligned}
\tag{2.16}
$$

162

163 From eq. 2.11, the ratio of the physical masses of the charged and neutral electroweak bosons

164 can be approximated as:

$$
\frac{m_W^2}{m_Z^2} \approx \cos \theta_W^{\ 2}, \tag{2.17}
$$

165 that satisfies the SM tree-level relation $\rho = 1$ if $\cos \theta_W^{\ 2} \approx 1. - 0.23$. Adding this approximation

166 into eq. 2.14, the V bosons are expected to have the same masses, hence the same production

167 rates:

$$
M_\pm^2 = M_0^2 \left(1 + \mathcal{O}(\%)\right). \tag{2.18}
$$

168 The degenerate mass of the triplet will be called $M_V \approx M_\pm \approx M_0$; given 2.15, $M_V = \hat{m}_V$.

169 Another consequence of the mass hierarchy (2.15) is that the mixing angles $\theta_{(N,C)}$ between the

170 electroweak fields and the triplet are small:

$$
\theta_{(N,C)} \approx c_H \zeta \frac{\hat{m}_{(W,Z)}}{\hat{m}_V} \ll 1, \tag{2.19}
$$

171 hence the couplings among SM particles are very close to the couplings predicted by the SM.

172 **Decay widths into fermions**

173 The couplings among the triplet and SM fermions are expressed as a function of the rotational

174 parameters $\theta_{(C,N)}$ and SM couplings (omitting the CKM matrix elements for quarks):

$$
\begin{cases}
g_L^N = \frac{g^2}{g_V} \frac{c_F}{2} \cos \theta_N + \left(g_L^Z\right)_{SM} \sin \theta_N \approx \frac{g^2}{g_V} \frac{c_F}{2} \\
g_R^N = \left(g_R^Z\right)_{SM} \sin \theta_N \approx 0
\end{cases} ,
$$
$$
\begin{cases}
g_L^C = \frac{g^2}{g_V} \frac{c_F}{2} \cos \theta_C + \left(g_L^W\right)_{SM} \sin \theta_N \approx \frac{g^2}{g_V} \frac{c_F}{2} \\
g_R^C = 0
\end{cases} ,
\tag{2.20}
$$

175 where $g_L^W = g/2$. The V bosons interact with SM left fermions, and the strenght of the

176 couplings with fermions is determined by $g^2/g_V c_F$, as stated in sec. 2.2.1. The decay width

177 into fermions is then given by:

$$
\Gamma_{V^\pm \to f \bar{f}'} \approx 2 \Gamma_{V^0 \to f \bar{f}} \approx N_c \left(\frac{g^2 c_F}{g_V}\right)^2 \frac{M_V}{48\pi}, \tag{2.21}
$$

178 where N_c is the number of colours (3 for quarks, 1 for leptons).

Decay widths into bosons

As a starting point, a proper choice of the gauge makes easier the derivation of approximate decay widths. While the unitary gauge is very convenient in discussing the electroweak symmetry breaking mechanism, since it provides a basis in which the Goldstone components of the scalar fields of the theory are set to zero, it does not properly describe the logitudinally polarized bosons in high-enery regimes, since it introduces a dependence of the type E/m in the logitudinal polarization vector, not corresponding to the experimental results. This pathological behaviour can be overcome profiting of the equivalence theorem: while calculating the scattering amplitude of an high-energy process, the longitudinally polarized vectors are equivalent to their corresponding Goldstone scalars. The scattering amplitude can therefore be calculated with Goldstone diagrams.

In the so-called equivalent gauge [14], the Higgs doublet is then parametrized as:

$$H = \begin{pmatrix} i\pi_+ \\ \frac{\hat{h}+h-i\pi_0}{\sqrt{2}} \end{pmatrix}, \tag{2.22}$$

and the Goldstones π_0 and π_+ describe respectively W and Z longitudinal bosons; h is the physical Higgs boson. Rewriting the simplified Lagrangian 2.3 with 2.22 parametrization, two terms held the information of the interaction of the Vs with the Goldstones:

$$\mathcal{L}_\pi = ... + c_H \zeta \hat{m}_V V_\mu^a \partial^\mu \pi^a + \frac{g_V c_H}{2} V_\mu^a \left(\partial^\mu h \pi^a - h \partial^\mu \pi^a + \epsilon^{abc} \pi^b \partial^\mu \pi^c \right) + ..., \tag{2.23}$$

that are ruled by the $c_H g_V$ parameters combination. When ζ parameter is $\zeta \approx 1$, the first term in eq. 2.23 becomes important, and it is absorbed by a redefinition of the V_μ^a and π^a fields,

$$
\begin{aligned}
V_\mu^a &\to V_\mu^a + \frac{c_H \zeta}{\hat{m}_V} \partial_\mu \pi^a \\
\pi^a &\to \frac{1}{\sqrt{1 - c_H^2 \zeta^2}} \pi^a; \; c_H^2 \zeta^2 < 1
\end{aligned}
\tag{2.24}
$$

By properly taking into account all the terms of the simplified lagrangian in the equivalent gauge, the partial widths of the dibosonic decays are ($\hat{m}_V = M_V$):

$$
\begin{aligned}
\Gamma_{V^0 \to W_L^+ W_L^-} &\approx \Gamma_{V^\pm \to W_L^\pm Z_L} \approx \frac{g_V^2 c_H^2 M_V}{192\pi} \frac{(1 + c_H c_{VVV} \zeta^2)^2}{(1 - c_H^2 \zeta^2)^2} = \frac{g_V^2 c_H^2 M_V}{192\pi} \left(1 + \mathcal{O}(\zeta^2)\right) \\
\Gamma_{V^0 \to Z_L h} &\approx \Gamma_{V^\pm \to W_L^\pm h} \approx \frac{g_V^2 c_H^2 M_V}{192\pi} \frac{(1 - 4 c_H c_{VVV} \zeta^2)^2}{(1 - c_H^2 \zeta^2)^2} = \frac{g_V^2 c_H^2 M_V}{192\pi} \left(1 + \mathcal{O}(\zeta^2)\right).
\end{aligned}
\tag{2.25}
$$

Decays in fermions and bosons: concluding remarks

From eq. 2.21-2.25, some important conclusions can be extracted.

- When ζ parameter is small, all the triplet decays (both in fermions and in dibosons), branching fractions and productions are completely determined by $g^2 c_F / g_V$, $g_V c_H$, and the degenerate mass of the triplet M_V

- c_{VVV}, c_{VVHH}, c_{VVW} can be neglected, as long as the interest is focused in narrow resonances

8

2.2.3 HVT production

Given the mass scale of the resonances, the relevant expected production mechanisms are Drell-Yan (fig. 2.1) and Vector Boson Fusion (VBF) (fig. 2.2).
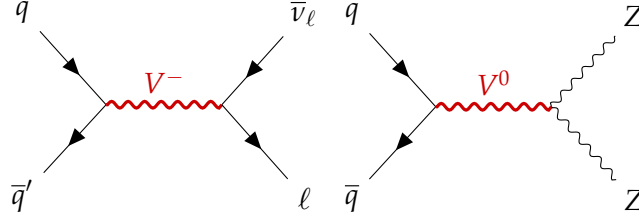

Figure 2.1: Examples of Drell-Yan production mechanism of a heavy V HVT boson: $q - \bar{q}'$ quark scattering producing a charged V^- that decays leptonically (left); $q - \bar{q}$ scattering producing a neutral V^0 that decays in a couple of Z bosons (right).
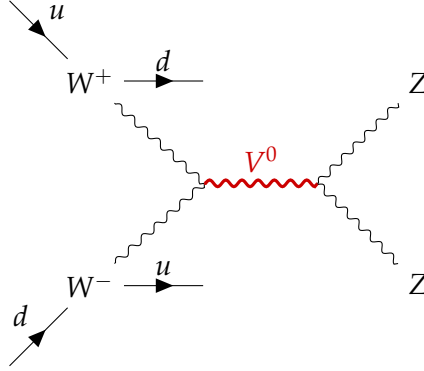

Figure 2.2: Examples of VBF production mechanism of a heavy V HVT boson: a neutral V^0 boson is produced by a couple of W bosons, as a result of an electroweak interactions of initial state u and d quarks. V^0 decays in a couple of Z bosons. The final state signature includes the presence of a pair of quarks, as a result of the primary interactions.

The cross-section of the production mechanisms is given by:

$$\sigma(pp \rightarrow V + X) = \sum_{i,j \in p} \frac{\Gamma_{V \rightarrow ij}}{M_V} f(J, S_i, S_j) g(C_i, C_j) \frac{dL_{ij}}{ds} \bigg|_{s=M_V^2}, \qquad (2.26)$$

where i, j are the partons involved in the hard interaction, Γ_{ij} is the partial width of the process $V \rightarrow ij$, $f(J, S_i, S_j)$ is a function of the spin of the resonance and of the partons, $g(C_i, C_j)$ is a function of the colour factors of each parton, s is the center-of-mass energy and $\frac{dL_{ij}}{ds}$ are the parton luminosities, that are independent from HVT model (that enters only in Γ_{ij}). Parton luminosities, calculated for a center-of-mass energy of 14 TeV starting from quark and antiquark parton distribution functions (PDF), are displayed in fig. 2.3 (Drell-Yan mechanism) and 2.4 (VBF mechanism). VBF luminosities are suppressed by the α_{EW} factor, therefore the process is relevant only when the bosonic decays of the triplet are dominant (strongly coupled scenario).
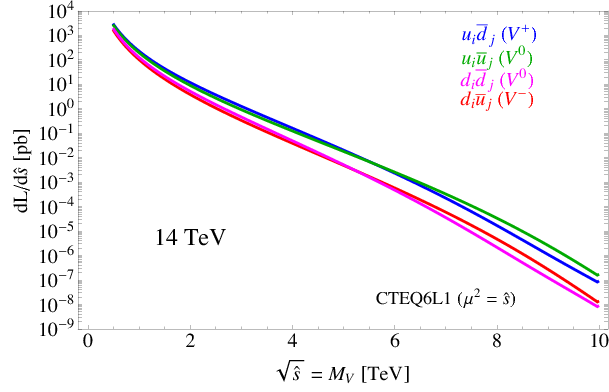
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Figure 2.3: Parton luminosities for Drell-Yan process between i and j partons, as a function of the parton center-of-mass energy, for the LHC proton-proton collisions performed at 14 TeV.
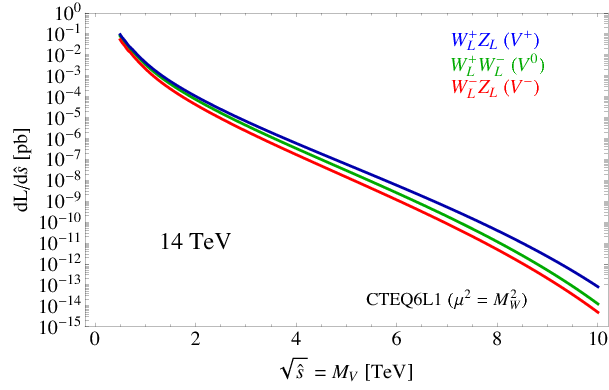

Figure 2.4: Parton luminosities for VBF process between i and j partons, as a function of the parton center-of-mass energy, for the LHC proton-proton collisions performed at 14 TeV.

2.2.4 Benchmark model A: weak coupling scenario

Model A scenario aims at reproducing a simple generalization of the SM [9], obtained by extending the gauge symmetry group with an additional $SU(2)'$. The low-energy phenomnena are expected to be dominated by the SM, while the high-energy processes are relevant for the additional symmetry, bringing additional light vector bosons in play.

It can be shown that this kind of picture is portrayed by HVT when $c_H \sim -g^2/g_V^2$ and $c_F \sim 1$. This implies that:

$$\begin{aligned} g_V c_H &\approx g^2/g_V \\ g^2 c_F/g_V &\approx g^2/g_V, \end{aligned} \tag{2.27}$$

hence the partial decay in widths into fermions (eq. 2.21) and bosons (eq. 2.25) differ only by a factor 2 and the colour factor (N_c). Branching fractions for the model A benchmark scenario ($g_V = 1$) are shown in fig. 2.5 (left); total widths are reported in fig.2.5 (right) for different coupling parameters g_V.
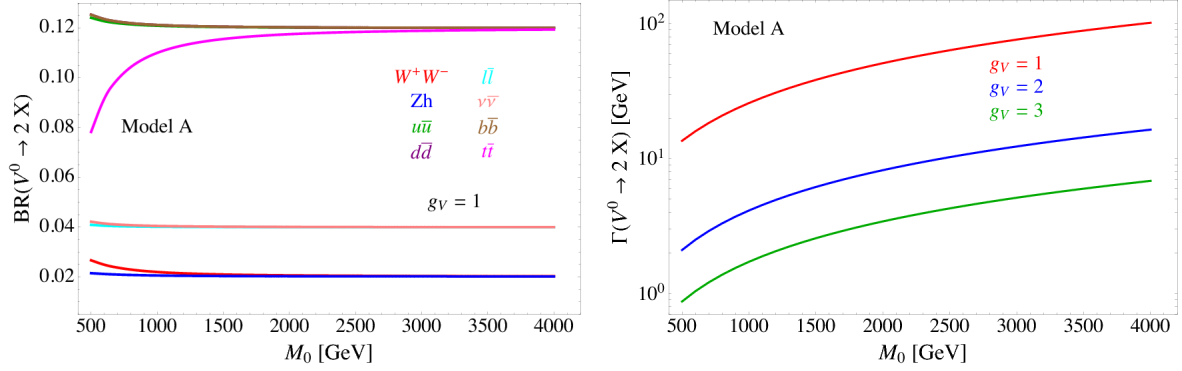
Figure 2.5: HVT model A scenario: branching fractions for fermionic and bosonic decays when $g_V = 1$ (left) as a function of the mass of the resonance M_0; total width of the resonance, as a function of its mass, considering different values of the parameter g_V (right).

2.2.5 Benchmark model B: strong coupling scenario

In composite Higgs models [11], the Higgs boson is the result of the spontaneous symmetry breaking of an $SO(5)$ symmetry to a $SO(4)$ group. New vector bosons are expected to appear, and the lightest ones can be represented by HVT model B when $c_H \sim c_F \sim 1$. In this case:

$$
\begin{aligned}
g_V c_H &\approx -g_V \\
g^2 c_F / g_V &\approx g^2 / g_V,
\end{aligned}
\tag{2.28}
$$

hence the decay into bosons is not suppressed by g_V parameter. In the benchmark scenario $g_V = 3$, decays into dibosons are largely dominant, as it can be seen in fig. 2.6 (left); the total decay width increases for larger g_V (fig. 2.6, right). When the resonances start to be very broad, *i.e.* $\Gamma/M_V \gg 0.1$, the assumptions leading to the simplified model are no longer valid, hence higher order, non -resonant effects must be taken into account.
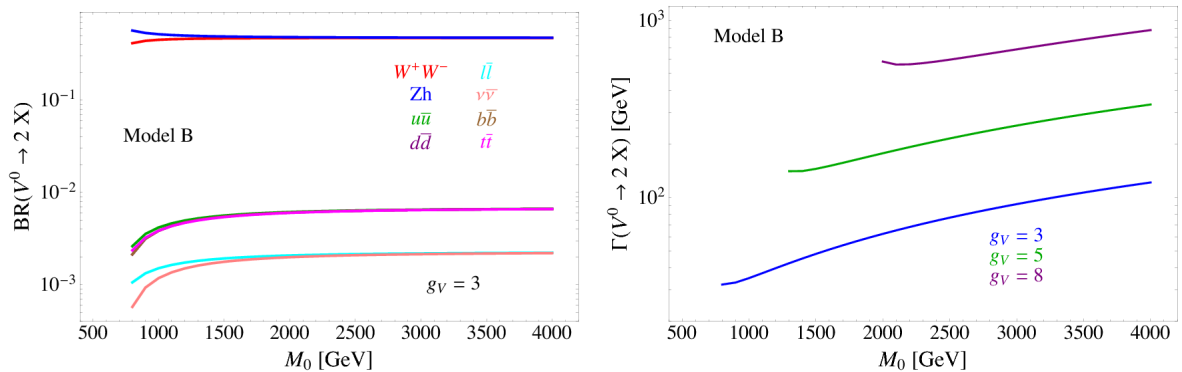

Figure 2.6: HVT model B scenario: branching fractions for fermionic and bosonic decays when $g_V = 3$ (left) as a function of the mass of the resonance M_0; total width of the resonance, as a function of its mass, considering different values of the parameter g_V (right).

2.2.6 HVT limits set by LHC at a center-of-mass energy of 8 TeV and perspectives at 14 TeV

Data collected by ATLAS and CMS experiments are used to set limits on the HVT resonance masses and coupling parameters. Experimental results, both from Run 1 LHC data (at a center-of-mass energy of 8 TeV) and Run 2 (at a center-of-mass energy of 13 TeV) will be discussed in detail in chapter 2.3.3.

A weakly coupled resonance, in the context of benchmark model A ($g_V = 1$) is excluded up to 3 TeV by Run 1 data. By looking at parton luminosities in fig.2.3, in data produced by LHC proton-proton collision at 14 TeV, collected for an integrated luminosity of 300 fb^{-1}, sensitivity should increase up to $m_V \approx 6$ TeV. A strongly coupled resonance, in the context of benchmark model B ($g_V = 3$) is excluded up to 2 TeV by Run 1 data. Data produced by LHC at 14 TeV should increase the sensitivity up to $m_V \approx 3 - 4$ TeV.

2.3 Warped extra dimension

The Randall-Sundrum model [15,16] (referred as RS1) proposes the introduction of one additional warped dimension in order to solve the hierarchy problem. The metric of the 5-dimensional space (a slice of AdS_5) generates an exponential hierarchy between the electroweak and Planck scales, associated to the TeV three-brane, where the SM particles are confined, and the Planck three-brane. As a consequence of the new geometry, spin-2 massive gravitons are predicted to exist.

The bulk extension of the Randall-Sundrum model [17,18] states that the SM fields can propagate in the extra dimension. Light fermions are near the Planck brane, heavy fermions are close to the TeV brane, while the Higgs sector is confined in the TeV brane. Higgs couplings to the heavy fermions are therefore expected to be stronger: this naturally arising hierarchy of the masses of the SM fields gives a solution to the flavour problem. In this scenario, the fermionic decays of the bulk gravitons are suppressed, while the bosonic decays are preferred.

2.3.1 Randall-Sundrum original model (RS1)

The existence of additional n-dimensions implies that the effective Planck scale observed in 4-dimensions, $M_{PL} = 1.2209 10^{19}$ GeV, is related to the fundamental (4+n) Planck scale, M, expected to be of the order of the reduced $\overline{M}_{PL} = M_{PL}/2\pi$, via the geometry. If the 4-dimensional and the n additional metrics are factorizable, $\overline{M}_{PL}$ is the product of M and the volume of the compact space V_n:

$$\overline{M}_{PL}^2 = V_n M^{2+n}. \tag{2.29}$$

If $M \sim$ TeV, this implies than V_n must be very large, hence the compactification scale $\mu \sim V_n^{1/n}$ is small (eV – MeV for n=2 – 7). Given the smallness of the scale when compared to the electroweak scale, the effects of the extra dimension should be evident in SM processes. Since they are not observed, SM particles are assumed to be confined in a 4-dimensional space, the TeV three-brane, while only gravity is allowed to propagate into the 4+n-dimensional space, the bulk. This mechanism solves the hierarchy of the Higgs scale but introduces a new hierarchy between μ and M.

In the Randall-Sundrum model [15,16], only one additional dimension is added. The geometry of the 5-dimensional bulk is non-factorizable, and it is a slice of AdS_5 spacetime.[1] The 4-dimensional metric is multiplied by an exponential function of the fifth dimension (the "warp" factor):

$$ds^2 = e^{-2kr_c\phi}\eta_{\mu\nu}dx^\mu dx^\nu + r_c^2 d\phi^2; \tag{2.30}$$

x^μ are the usual 4-dimensional coordinates, $\eta_{\mu\nu} = diag(-1,1,1,1)$, k is a scale of order of $\overline{M}_{PL}$, ϕ is the coordinate of the extra dimension, $0 < |\phi| < \pi$, and r_c is the compactification radius of this finite interval. 4-dimensional mass scales are obtained multiplying bulk masses by $e^{-2kr_c\phi}$: given the exponential form of the warp factor, a small r_c suffices for generating a large hierarchy between Planck and Higgs scales.

The two 4-dimensional three-branes are located at the boundaries of the fifth dimension: the visible brane at $\phi = \pi$; the hidden brane at $\phi = 0$, and their metrics are obtained starting from

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[1]An n-dimensional anti-de Sitter space (AdS_n) is a maximally simmetric Lorentiaz mainfold, that solves the Einstein equation with a negative curvature; it is a solution to the Einstein equation with negative cosmological constant.

288 the bulk 5-dimensional metric G_{MN}, where $M, N = \mu, \phi$:

$$g_{\mu\nu}^{\text{vis}}(x^\mu) = G_{\mu\nu}(x^\mu, \phi = \pi)$$
$$g_{\mu\nu}^{\text{hid}}(x^\mu) = G_{\mu\nu}(x^\mu, \phi = 0). \tag{2.31}$$

289 The classical action is given by:

$$S = S_{\text{gravity}} + S_{\text{vis}} + S_{\text{hid}}$$
$$S_{\text{gravity}} = \int d^4x \int_{-\pi}^{+\pi} d\phi \sqrt{-G} \left(-\Lambda + 2M^3 \mathcal{R} \right)$$
$$S_{\text{vis}} = \int d^4x \sqrt{-g_{\text{vis}}} \left(\mathcal{L}_{\text{vis}} - V_{\text{vis}} \right) \tag{2.32}$$
$$S_{\text{hid}} = \int d^4x \sqrt{-g_{\text{hid}}} \left(\mathcal{L}_{\text{hid}} - V_{\text{hid}} \right),$$

290 where G (g) is the trace of the G_{MN} ($g_{\mu\nu}$) metric, Λ is the cosmological constant in the bulk,
291 $\mathcal{R}$ is the 5-dimensional Ricci scalar, $\mathcal{L}$ and V are the lagrangian and the vacuum energy of the
292 hidden and visible branes.
293 A 5-dimensional metric that preserves the 4-dimensional Poincaré invariance is:

$$ds^2 = e^{-2\sigma(\phi)} \eta_{\mu\nu} dx^\mu dx^\nu + r_c^2 d\phi^2. \tag{2.33}$$

294 The Poincaré invariance guarantees that r_c does not depend on x^μ. Given 2.33, the solution of
295 the 5-dimensional Einstein's equations simplifies into:

$$\sigma = r_c |\phi| \sqrt{\frac{-\Lambda}{24M^3}}. \tag{2.34}$$

296 Furthermore, the Poincaré invariance imposes constraints to the vacuum energies and cosmo-
297 logical constant:

$$V_{\text{hid}} = -V_{\text{vis}} = 24M^3 k$$
$$\Lambda = -24M^3 k^2. \tag{2.35}$$

298 The final 5-dimensional metric is then:

$$ds^2 = e^{-2kr_c|\phi|} \eta_{\mu\nu} dx^\mu dx^\nu + r_c^2 d\phi^2. \tag{2.36}$$

299   A small r_c is considered, so the effects of the fifth dimension on 4-dimensional spacetime
300 can't be appreciated. A 4-dimensional effective field theory approach is therefore motivated,
301 and its mass parameters are related to the bulk parameters, M, k and r_c. In the Randall-
302 Sundrum model, SM matter fields are therefore confined in the TeV brane.
303 The massless gravitons, the mediators of the gravitaional interaction in the effective field
304 theory, are the zero modes ($\overline{h}_{\mu\nu}$) of the quantum fluctuations of the classical solution (2.36):

$$ds^2 = e^{-2kT(x)|\phi|} \left(\eta_{\mu\nu} + h_{\mu\nu}(x) \right) dx^\mu dx^\nu + T^2(x) d\phi^2, \tag{2.37}$$

305 where the usual Minkowski metric has been replaced by $\overline{g}_{\mu\nu}(x) = \eta_{\mu\nu} + h_{\mu\nu}$; $h_{\mu\nu}$ are the
306 tensor fluctuations around the Minkowski space, and represent both the physical graviton in
307 4-dimensions and the massless mode of the Kaluza-Klein decomposition of the bulk metric.

308 r_c is the vacuum expectation value of $T(x)$.

309 Substituting eq. 2.37 in the classical action 2.32, an effective action can be extracted, and in

310 particular the curvature term helds:

$$S_{\text{eff}} \sim \int d^4x \int_{-\pi}^{+\pi} d\phi\, 2M^3 r_c e^{-2kr_c|\phi|}\overline{\mathcal{R}}\sqrt{-\overline{g}}, \tag{2.38}$$

311 where $\overline{g}$ is the trace of $\overline{g}_{\mu\nu}$ and $\overline{\mathcal{R}}$ is the 4-dimensional Ricci scalar of $\overline{g}_{\mu\nu}$ metric. In this

312 effective 4-dimensional action, the ϕ dependence can be integrated out, and the 4-dimensional

313 Planck mass can be calculated:

$$\overline{M}_{PL}^2 = M^3 r_c \int_{-\pi}^{+\pi} d\phi\, e^{-2kr_c|\phi|} = \frac{M^3}{k}\left(1 - e^{-2kr_c\pi}\right). \tag{2.39}$$

314 It can be shown [15] that a field with a fundamental mass parameter m_0 in the bulk manifests

315 in the visible three-brane with a physical mass m:

$$m = e^{-2kr_c\pi}m_0. \tag{2.40}$$

316 Scales $m \sim$ TeV are generated from $m_0 \sim \overline{M}_{PL}$ if $e^{kr_c\pi} \sim 10^{15}$. This relation stands still when

317 Higgs field is introduced and confined in the visible three-brane:

$$v = e^{-2kr_c\pi}v_0, \tag{2.41}$$

318 where v is the Higgs vacuum expectation value in the TeV brane and v_0 is the 5-dimensional

319 Higgs v.e.v.

320 The hierarchy problem is then solved by the exponential warp factor. The weakness of gravity

321 in the TeV three-brane is motivated by the small overlap of the graviton wave function.

322 In order to calculate the mass specturm of the graviton in the TeV brane, the tensor fluctuations

323 of the Minkowski metric are expanded into a Kaluza-Klein (KK) tower $h_{\mu\nu}^{(n)}$:

$$h_{\mu\nu}(x, \phi) = \sum_{n=0}^{\infty} h_{\mu\nu}^{(n)}(x)\frac{\chi^{(n)}(\phi)}{\sqrt{r_c}}. \tag{2.42}$$

324 Once a suitable gauge is chosen, i.e. $\eta^{\mu\nu}\partial_\mu h_{\nu\alpha}^{(n)} = \eta^{\mu\nu}h_{\mu\nu}^{(n)} = 0$, the equation of motion of $h_{\mu\nu}^{(n)}$

325 becomes the Klein-Gordon relation, where $m_n^G \geq 0$:

$$\left(\eta^{\mu\nu}\partial_\mu\partial_\nu - (m_n^G)^2\right) h_{\mu\nu}^{(n)}(x) = 0. \tag{2.43}$$

326 By substituting eq. 2.42 into Einstein's equation, the solutions for $\chi^{(n)}(\phi)$ (commonly called

327 "profiles") are [19, 20]:

$$\chi^{(n)}(\phi) = \frac{e^{2\sigma}}{N}\left[J_2(z_n^G) + \alpha_n Y_2(z_n^G)\right], \tag{2.44}$$

328 where J_2 and Y_2 are second order Bessel functions, N is the normalization of the wavefunction,

329 α_n are coefficients and $z_n^G = m_n^G e^{\sigma(\phi)}/k$. m_n^G is the mass of the n-mode, and it depends on the

330 roots of the Bessel functions $z_n^G = (3.83, 7.02, 10.17, 13.32, ...)$. In the limit $m_n^G/k \ll 1$ and

331 $e^{kr_c\pi} \gg 1$:

$$m_n^G = k z_n^G(\pi)e^{-kr_c\pi}. \tag{2.45}$$

The interactions between the graviton KK modes and the matter fields in the TeV brane can be derived from the 4-dimensional effective Lagrangian, once $h_{\mu\nu}$ is replaced by its KK decomposition:

$$\mathcal{L} = -\frac{1}{\overline{M}_{PL}} T^{\mu\nu}(x) h_{\mu\nu}^{(0)} - \frac{1}{e^{-kr_c\pi}\overline{M}_{PL}} T^{\mu\nu}(x) \sum_{n=1}^{\infty} h_{\mu\nu}^{(n)}(x); \qquad (2.46)$$

$T^{\mu\nu}$ is the space energy-momentum tensor of the matter fields. The zero mode of the gravitons coupling is $1/\overline{M}_{PL}$, while higher order KK modes couplings to all SM fields are suppressed by $e^{-kr_c\pi}\overline{M}_{PL}$, that is of the order of the TeV scale. Spin-2 KK masses and couplings are hence determined by the TeV scale, or, equivalently, KK gravitons are close to the TeV brane. This implies that KK gravitons can be produced via $q\bar{q}$ or gluon fusion, and that a leptonic decay of the resonance could represent a very clear signal signature.

2.3.2 Bulk extension of RS1: graviton production and decays

An extension of the original RS1 formulation has been proposed. It states that SM fields are no longer confined in the TeV brane, but they are the zero modes of the corresponding 5-dimensional SM fields. If first and second generation fermions are close to the Planck brane, contribution to flavour changing neutral currents by higher-dimensional operators are suppressed. These contributions are excluded by electroweak precision tests, but they were not prevented in original RS1. The second motivation behind the choice is, as mentioned previously, the naturally arising flavour hierarchy: first and second generation quarks have small Yukawa couplings to the Higgs sector, confined in the TeV brane, while top quark and bosons have stronger Yukawa couplings.

In this picture, couplings between higher-order KK gravitons and light fermions are strongly suppressed, resulting into a negligible KK gravitons production via $q\bar{q}$, whilst gluon fusion production becomes dominant. KK gravitons decays into top quark and Higgs bosons are dominant, given that both their profiles are near the TeV brane, while leptonic decays are negligible. Via the equivalence theorem, the Goldstone bosons are equivalent to the longitudinally polaried weak bosons, $W_L^{\pm}$ and Z_L, that have profiles close to the TeV brane. Decays of KK gravitons into weak dibosons (and production in VBF) are comparable to di-top and di-Higgs decays.

The KK decomposition and the KK mass spectrum of the graviton have already been presented in sec. 2.3.1. The KK decomposition of a massless 5-dimensional gauge field $A_M(x,\phi)$ is similarly performed:

$$A_\mu(x,\phi) = \sum_{n=0}^{\infty} A_\mu^{(n)}(x) \frac{\chi^{(n)_A}(\phi)}{\sqrt{r_c}}. \qquad (2.47)$$

The profiles for the gauge fields are

$$\chi_A^{(n)}(\phi) = \frac{e^\sigma}{N_A} \left[J_1(z_n^A) + \alpha_n^A Y_1(z_n^A) \right], \qquad (2.48)$$

where J_1 and Y_1 are first order Bessel functions. Similarly to eq. 2.49, the mass spectrum of the gauge field is:

$$m_n^A = k z_n^A(\pi) e^{-kr_c\pi}; \qquad (2.49)$$

the first roots of the Bessel functions are $z_n^A = (2.45, 5.57, 8.70, 11.84, ...)$.

The Lagrangian expressing the interaction between the m and n modes of the bulk field F to the q KK gravitons mode G is [21]:

$$\mathcal{L}_{G-F} = \sum_{m,n,q} C_{mnq}^{FFG} \frac{1}{\overline{M}_{PL}} \eta^{\mu\alpha} \eta^{\nu\beta} h_{\alpha\beta}^{(q)}(x) T_{\mu\nu}^{(m,n)}(x), \tag{2.50}$$

C_{mnq}^{FFG} is the overlap integral of the profiles:

$$C_{mnq}^{FFG} = \int \frac{d\phi}{\sqrt{k}} e^{t\sigma} \frac{\chi_F^{(m)} \chi_F^{(n)} \chi_G^{(q)}}{\sqrt{r_c}}; \tag{2.51}$$

t depends on the type of field considered.

The coupling between gluons and the q KK graviton mode is given by:

$$C_{00q}^{AAG} = e^{k\pi r_c} \frac{2\left[1 - J_0(x_n^G)\right]}{k\pi r_c (x_n^G)^2 |J_2(x_n^G)|}. \tag{2.52}$$

Once eq. 2.52 is put in eq. 2.50, the most significant partial decay widths into the q KK graviton mode are:

$$\begin{aligned}
\Gamma\left(G \to t_R \bar{t}_R\right) &\sim N_c \frac{\left[\tilde{k} x_q^G\right]^2 m_q^G}{320\pi} \\
\Gamma\left(G \to hh\right) &\sim \frac{\left[\tilde{k} x_q^G\right]^2 m_q^G}{960\pi} \\
\Gamma\left(G \to W_L^+ W_L^-\right) &\sim \frac{\left[\tilde{k} x_q^G\right]^2 m_q^G}{480\pi} \\
\Gamma\left(G \to Z_L Z_L\right) &\sim \frac{\left[\tilde{k} x_q^G\right]^2 m_q^G}{960\pi},
\end{aligned} \tag{2.53}$$

where $\tilde{k} = k/\overline{M}_{PL}$; the total decay width is:

$$\Gamma_G = \frac{13 \left[\tilde{k} x_q^G\right]^2 m_q^G}{960\pi}. \tag{2.54}$$

Calculations, so far, have been performed considering $M \sim \overline{M}_{PL}$ and $k < M$, hypoteses under which the solution for the bulk metric (eq. 2.36) is valid. Hence, $\tilde{k} = k/\overline{M}_{PL} \leq 1$ is taken as a reference interval. This also has phenomenological consequences on the width of the resonance, as stated in eq. 2.54. The total decay width of the lightest KK graviton mode, compared to its mass, is shown as a function of $\tilde{k}$ in fig. 2.7 [22]. At $\tilde{k} = 1$, in the bulk scenario, the KK graviton width is expected to be few % of its mass, up to 4 TeV (dotted red curve). The narrow width approximation holds, hence the resonance properties can be probed at the peak, neglecting the effects in the tails of the mass distribution.

2.3.3 Search of KK gravitons at LHC

The total cross-section of a bulk graviton, produced at LHC in proton-proton interactions via gluon fusion, decaying into a couple of vector bosons (for the purpose of this work, a final
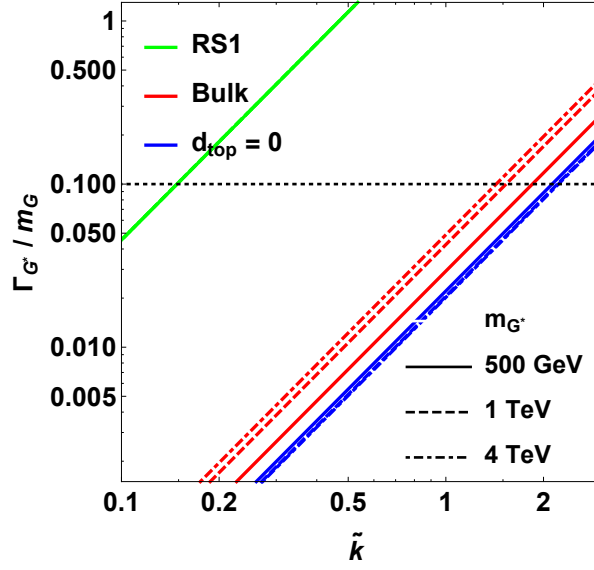
Figure 2.7: Width of the KK gravitons, in units of the mass of the resonance, as a function of the curvature parameter $\tilde{k}$. The red curves represent the bulk extension of RS1 original model for different mass hypoteses (from 500 GeV up to 4 TeV).

state with two longitudinally polarized Z bosons is considered) is expressed as a function of the parton level cross-section $\hat{\sigma}$, the gluon parton distribution functions f_q, the momentum transfer $Q^2 \sim (m_q^G)^2$ and the center-of-mass energy s:

$$\sigma(pp \rightarrow ZZ) = \int dx_1 dx_2 f_g(x_1, Q^2) f_g(x_2, Q^2) \hat{\sigma}(x_1 x_2 s). \tag{2.55}$$

The differential parton level cross-section, averaged over colors and initial spin states, is (hatted quantities are calculated in the center-of-mass frame):

$$\frac{d\hat{\sigma}(gg \rightarrow ZZ)}{d\cos\hat{\theta}} \approx \frac{|\mathcal{M}_{+-00}|^2}{1024\pi\hat{s}}, \tag{2.56}$$

where $|\mathcal{M}_{+-00}|$ is the matrix element

boosted jet **discussion on k/MPL less 1 postponed**

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