#### RESCIENCEC

#### Replication / Education Policy

# [¬Re]Simulating socioeconomic-based affirmative action

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## Introduction

The work of Reardon et al. [1] assesses the impact of different school admission policies on the probability of various ethnic groups to be admitted using an agent-based simulation model with parameters "grounded in real-world". Real-life experiments over such sociotechnical systems are complex and costly to setup and run over a long time period (e.g., years) and can in general only be done over limited pilot projects. By enabling computational experiments over school admission policies, Reardon et al. provides a useful environment for researchers focusing on the fairness issues related to the deployment and use of artificial intelligence algorithms. The proposed model is discussed in great length in the original paper, thus providing a solid basis for understanding it. However, the code of this simulation model is not publicly available. In addition, when re-implementing the model, we have faced several issues related to important parts of the model. First, some values of parameters were missing-e.g., initial colleges' quality-while others were used inconsistently along the paper-such as affirmative actions. Second, some parameters described-in natural language-in the paper were actually unused by the model. We tried to guess the appropriate formulas to fit the results and the model description of the original paper. Nonetheless, we were able to guess their probable values in most cases by trying and comparing our results with those reported in the paper, thus following a trial and error strategy. However, we did not succeed in replicating all the results. This paper describes in details our replication attempt.

## 2 Model of college admissions

Reardon et al. [1] proposes an agent-based simulation of the college admission process, mainly based on the model described in previous work [2], with the addition of a racial attribute to students and the inclusion of positive discrimination policies. We provide below a brief overview of the model, referring the interested reader to the original paper for more details.

The model consists in two sets of agents: colleges and students. A new population of 10,000 students is randomly drawn at each iteration, in which one iteration corresponds to one year. The 40 colleges are kept for the completely simulation and evolve according to the admissions.

Each iteration is composed of three steps:

**Application step.** Students decide on the "best" subset of colleges to apply by taking into account their probability of admission depending on their academic achievement

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The authors have declared that no competing interests exist.
Code is available at https://github.com/lbeziaud/mosaic..

and on each college's quality, with a noisy perception of variables varying with financial resources. That is, "high-resources families have better information about college quality" ([1]). To mimic societal biases, both academic achievements and financial resources depend on the race attribute.

**Admission step.** Colleges rank applications based on noisy version of academic achievements. A percentage of the (best) students is admitted depending on the admission rate of the college.

**Enrollment step.** Students enroll into the best college in which they are admitted.

At the end of each iteration, the colleges' admission rate and quality as well as their probability of admission are updated.

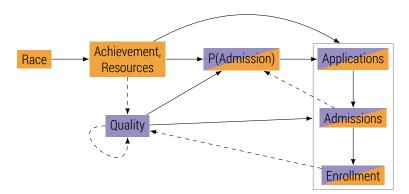
Starting from year 15 (the previous years are used for model convergence), positive discrimination policies are put in place by a subset of colleges, mostly the top 4. More precisely, three type of policies can be introduced:

**Socioeconomic-based affirmative action.** During admission, colleges favor low-income students by increasing their perceived academic achievement.

Race-based recruiting. During application, students from minority groups favor colleges by increasing their perceived quality, increasing the likelihood of an application.

**Race-based affirmative action.** During admission, colleges favor students from minority groups by increasing their perceived academic achievement.

The original experiments are concerned with the impact of using socioeconomic-based (SES) affirmative action combined with race-based recruiting instead of race-based affirmative action. The former two are therefore mostly used together by the colleges.



**Figure 1.** Simplified causal model of [1] with most of the variables being abstracted away. Students' variables are orange, colleges' variables are purple, while finally variables defined for pairs of student and college have both colors. Dashed arrows represent dependency over past iterations.

## 3 Method

We have mostly followed the detailed description of the model given in [1, Appendix C]. We have also referred to [2], which is often cited by the authors as an inspiration for this work. Code for this latter model is available in the (proprietary) Stata programming

language [3]. We have read this code for clarification but we were not able to run it<sup>1</sup>. We have contacted the authors in May 2021 but got no answer as of February 2022.

For our implementation, we have used the Python programming language, with most of the processing done using NumPy. We use scikit-learn for the logistic regression (but also used statsmodels during development).

We have experimented with the Xarray library, which provides labeled multi-dimensional arrays. Our motivation was to deduplicate the join between students and colleges. However, we have achieved no storage or time improvement by doing so.

In addition to the replication effort, we focused on execution speed to be able to use the model as a synthetic data generator in other works. For this purpose, random data for all future iterations is drawn at initialization.

## 4 Difficulties

In this section, we present the main issues encountered with respect to the description of the model in the original paper [1]. Hereafter, inconsistent descriptions are quoted but we refer the reader to the full paper for more context. Afterwards, we describe the interpretation that we have followed for the results presented in this paper.

#### Socioeconomic status (SES)-based affirmative action.

- "It is during the calculation of  $A_{cs}^{**}$  that colleges with an affirmative action policy apply additional weight to a student's perceived admissions desirability in accordance with that policy. This additional weight is captured by the term  $T_c \times [G \times (Black_s \mid Hispanic_s) + H \times resources_s]$ . In this term,  $T_c$  indicates whether a college has an affirmative action policy, [...] H is the size of the weight given to students under SES-based affirmative action policies, which is applied linearly in accordance with the student's resources, resources\_s." ([1, Section 3])
- "SES-affirmative action (corresponding to an increase in admissions consideration of 0, 50, 100 and 150 *achievement points for each decrease of one standard deviation* in applicants' resources);" ([1, Section 4]).
- "The size of the affirmative action weights we use are based on our estimate of a 1.3 standard deviation relative race weight evident in selective admissions [...]. Given this estimate, we establish a "moderate" race-based affirmative action policy that gives a 0.75 standard deviation, or 150 points on our academic achievement scale, weight to Black or Hispanic students." ([1, Appendix C])

Using  $H \times resources_s$  as in the first quite would advantage high-income students, which is the opposite of the objective. Moreover, the weight would not follow the description of the next two quotes, which involve the standard deviation. In our implementation, a weight  $H \times \max(-z\text{score}(resources_s), 0)$  is added to the score of low-income students students, with zscore being the standard score² with respect to resources, and H the size of the weight (e.g., 0, 50, 100 and 150). We keep only negative values of the standard score to impact only low-income students ("for each decrease of one standard deviation"). Note that our interpretation is not totally satisfactory (see Section 6), however we had no success either with the formula of he first quote.

 $<sup>^1\</sup>mathrm{Executing}$  this model seems to require Stata version 11, but the dependency "college sorting napps.do" is not distributed in the archive.

<sup>&</sup>lt;sup>2</sup>The number of standard deviations by which the value of a raw score is above or below the mean value of what is being observed or measured

#### Quality and own achievement reliability.

- "Quality reliability and own achievement reliability bounded by minimum values of 0.5 and maximum values of 0.9." ([1, Table 1])
- "the reliability of student perceptions of their own achievement, is a function of student resources and *bounded between 0.5 and 0.9*" ([1, Appendix C])
- "the reliability of student perceptions of college quality, is a function of student resources and *bounded between 0.5 and 0.7*" ([1, Appendix C])

We assume that 0.7 is a typo and clip the values between 0.5 and 0.9.

Race-targeted recruiting. "Colleges' binary recruitment statuses  $(S_c)$ —which had previously all been 0—are set based on model parameters that determine which schools will use recruitment [...] Utility is then calculated using model-specific recruitment magnitude values (L):  $U_{cs}^* = a_s + b_s \times Q_{cs}^* + R_{sc}$ ." ([1, Appendix C])

tude values (L):  $U_{cs}^* = a_s + b_s \times Q_{cs}^* + R_{sc}$ . "([1, Appendix C]) There is no use of  $S_c$  in the document apart from the definition, and  $R_{sc}$  is also not defined. We assume that it is a typo and that  $S_c$  is to be understood as  $R_{sc}$ . The recruitment magnitude value L is not used (but is an experimental parameter later). No specific definition of race-targeted recruitment is given but from "Recruitment efforts work in part by making students aware of specific colleges and by making these colleges seem more appealing to prospective students through additional, targeted contact with those students." ([1, Section 3]) our understanding is that targeted groups have an increased chance of applying to colleges using race-targeted recruitment. However, the race attribute is not used in conjunction with L.

We assume that the race-targeted recruitment weight is added to the perceived utility of attending colleges for minority students, such that

$$U_{cs}^* = a_s + b_s \times Q_{cs}^* + R \times (Black_s \mid Hispanic_s) \times T'_c$$

in which  $T^\prime{}_c$  indicates whether a college uses race-targeted recruitment and R is the recruitment weight.

**Quality update window.** It is unclear whether the quality of colleges depends only on the previous year or on the past five years:

- "Colleges' quality values  $(Q_c)$  are updated based on the incoming class of enrolled students before the next year's cohort of students begins the application process" ([1, Appendix C]).
- "College quality is *calculated as the five-year running average* of enrolled student caliber." ([1, Figure C5])

Using only the previous year to update colleges' quality gives satisfying results (see Figure 5). Thus, we assume that the five-year running average is not used for the model but only to smooth the plots.

Initial college quality. "Initial college quality (Q) is normally distributed" ([1, Appendix C]), but the values of the mean and variance are not given. We relies on the values from [2]:  $Q \sim \mathcal{N}(1070, 130)$ .

**Admission probability estimation.** After the fifth iteration, each iteration requires fitting a logistic model on submitted application over the past five years.

Apart from a significant speed increase, we observe no difference when fitting on the previous year only (and using the previously fitted model's parameters to initialize the new fit). However, our code still uses the past five years.

## **5** Experiments

Figures 2 to 7 present side by side examples of reproduction, with plots taken from the preprint version [4] of the original paper [1] (due to copyright issues) on the right (b) and replication results on the left (a). We attempt to replicate a representative subset of the plots, covering the gist of the model (Figures 2, 5 and 6), SES-based affirmative action and race-based recruitment (Figures 4 and 6), race-based affirmative action (Figure 3), and the main results of the original paper (Figures 7 and 6). We use the same legend as the original paper, with college not using positive discrimination policy in blue and using positive discrimination policy in orange. Figures 8 and 9 present the impact of the different strategies on the final (years 25 to 29) composition–racial and socioeconomic<sup>3</sup>– of enrolled students in colleges for our replication (in red) and the original paper (in cyan). Our replication effort involved experimenting with the full set of plots presented in the original paper. We also resorted to additional plots (not presented in the original paper or the current one) to assess the correlation between probability admission and academic achievement.

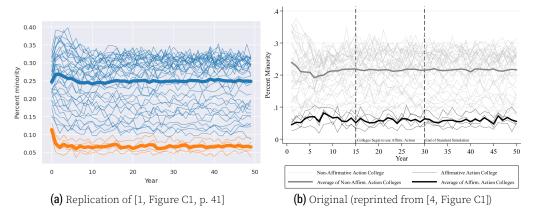
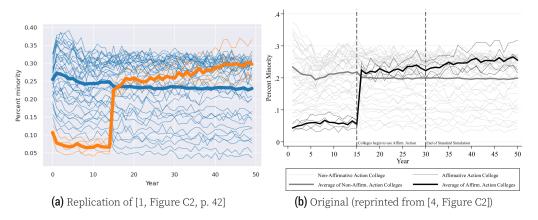
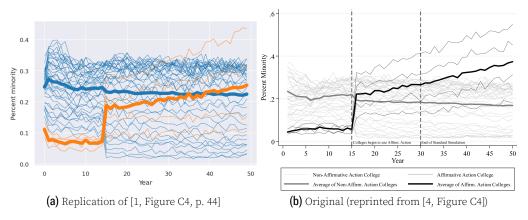


Figure 2. Minority enrollment without using affirmative action or recruiting.

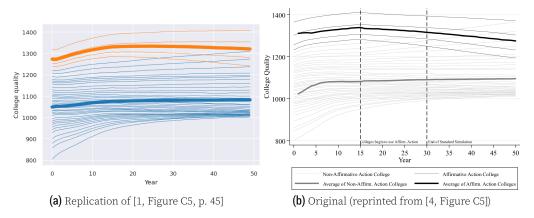


**Figure 3.** Minority enrollment with the top four schools using "real-world" race-based affirmative action (weight of 260).

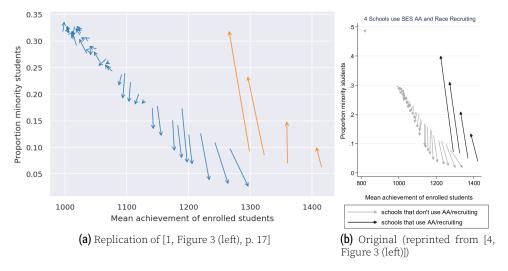
 $<sup>^3</sup>$ Our socioeconomic distribution is represented by the quintiles of the *full* students' resources distribution (not only the enrolled students).



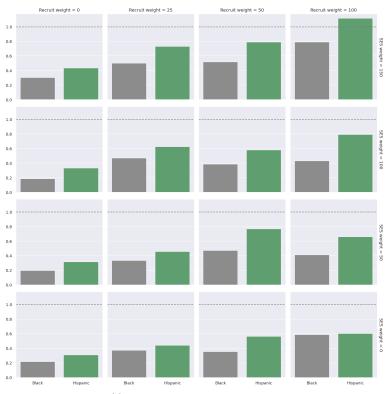
**Figure 4.** Minority enrollment with the top four colleges using strong SES-based affirmative action (weight of 150) and strong race-based recruitment (weight of 100).

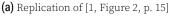


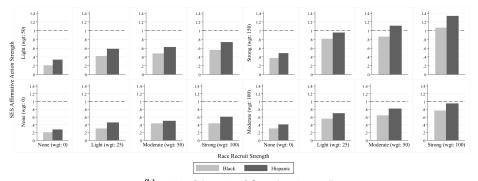
**Figure 5.** College quality with the top four colleges using strong SES-based affirmative action (weight of 150) and strong race-based recruitment (weight of 100).



**Figure 6.** Mean achievement and proportion minority with top four schools using (respectively not using) strong SES-based affirmative action (weight of 150) and strong race-based recruitment (weight of 100) in **blue** (respectively **orange**). Arrows start at a school's position in year 14 when it was not using affirmative action, and end at the school's position in year 29.

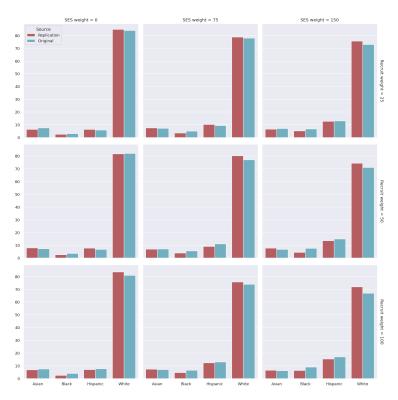




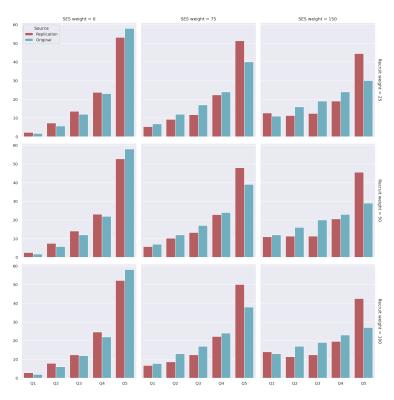


(b) Original (reprinted from [4, Figure 2])

**Figure 7.** Black (gray) and Hispanic (green) enrollment in colleges using SES-based affirmative action and race-based recruitment, as a share of estimated enrollment under race-based affirmative action (using estimated real-world affirmative action weight 260).

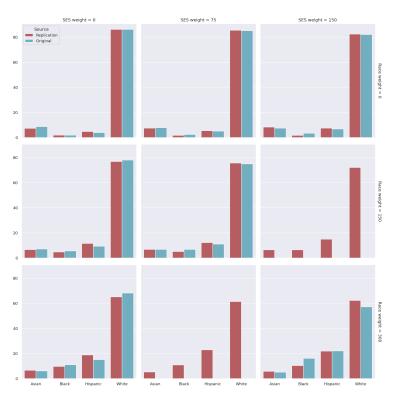


(a) Reproduction of [1, Figure A2, p. 30]: racial composition



(b) Reproduction of [1, Figure A3, p. 31]: socioeconomic composition

**Figure 8.** Replication and original composition of colleges using SES-based affirmative action and race-based recruitment, by affirmative action and recruitment weights.



(a) Reproduction of [1, Figure A4, p. 32]: racial composition



(b) Reproduction of [1, Figure A5, p. 33]: socioeconomic composition

**Figure 9.** Replication and original composition of colleges using SES-based and racial affirmative actions, by affirmative action weights.

#### 6 Results

Our objective was to replicate the overall tendencies of the model. We compare below our replicated results to the original results.

- **Figure 2: success.** The results without using positive discrimination policy presented on Figure 2 are similar to the original paper.
- **Figure 3: partial success.** Figure 3 shows that we replicated the main trends but still indicates an issue with race-based affirmative action: our replication leads to a lower impact on minority students.
- Figure 4: partial success. Looking at Figure 4, the combination of SES-based affirmative action and race-based recruitment is satisfactory. However, race-based and SES-based affirmative actions use the same mechanism, which lead us to believe that race-based recruitment is successfully replicated with a potential issue for SES-based affirmative (as with Figure 3).
- **Figure 5: success.** The behavior of quality on Figure 5 is similar to the original paper, indicating the adequacy of our quality initialization.
- **Figure 6: partial success.** Figure 6 suffers from the same issue of affirmative actions as Figure 3 but the general behavior is similar to the paper. It is important to note that this figure corresponds to an average over 10 runs (as the original paper), which requires the colleges to be sorted by quality.
- **Figure 7: partial success.** Figure 7 shows a successful replication of the general tendency of the model (*i.e.*, the relative values) and a failure in replicating the absolute numbers, probably due to the issue related to the affirmative action observed above.
- **Figure 8: partial success.** Figure 8 shows a successful replication regarding the racial impact of targeted recruiting and SES-based affirmative action strategies, but highlight an issue with the socioeconomic composition. Indeed the impact of our SES-based affirmative action is higher than the original paper.
- **Figure 9: partial success.** Figure 9 lead the same observation that SES-based affirmative action is not behaving as the original paper. However race-based affirmative action is satisfactory. Note that the combinations (race weight = 150, SES weight = 150) and (race weight = 300, SES weight = 75) are not presented in the original paper.

#### 7 Conclusion

In this paper, we presented our attempt at replicating the model presented by Reardon et al. [1]. The overall behavior is successfully reproduced, with discrepancies regarding the impact of positive discrimination policies. We attribute the later to issues with our understanding of the paper, thus highlighting the difficulties of describing complex systems. The resulting implementation, while not producing results entirely faithful to the ones from the original paper, can still be useful to simulate data grounded in real-world for fairness applications in the context of college admission. We believe however that more efforts are required regarding this replication, however we hope that this goes towards bridging the gap between computer science and social sciences.

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