

$$r = (r_1, r_2, \dots, r_n)$$

$$d^k = \left( \frac{r_1}{|r_1|}, \frac{r_2}{|r_2|}, \dots, \frac{r_n}{|r_n|} \right)$$

$$o^k = \sum e^i \operatorname{sgn}(r_i)$$

$$\alpha_k = \frac{(r^k)^t d^k}{(d^k)^t A d^k}$$

$$A \begin{pmatrix} 1 \\ \vdots \\ 1 \end{pmatrix}$$

$$\operatorname{sgn}(r_i) = \begin{cases} 0 & \text{if } r_i = 0 \\ 1 & \text{if } r_i > 0 \\ -1 & \text{if } r_i < 0 \end{cases}$$

$$\frac{\sum |r_i|}{(d^k)^t A d^k}$$

$$\begin{aligned} d^t A d &\leq \|A\|_2 n \\ r^t A^{-1} r &\leq \|A^{-1}\|_2 \|r\|_2^2 \\ \|r\|_2 &\leq \|r\|_1 \\ X^{k+1} &= X^k + \alpha_k d^k = X^k + \frac{(r^k)^t o^k}{(d^k)^t A d^k} d^k \end{aligned}$$

$$\|X^{k+1} - X^*\|_A^2 = \left( 1 - \frac{(r^k)^t d^k (r^k)^t o^k}{(d^k)^t A d^k (r^k)^t A^{-1} r^k} \right) \|X^k - X^*\|_A^2 \leq \left( 1 - \frac{\|r^k\|_1^2}{\|A\|_2 n \|A^{-1}\|_2 \|r^k\|_2^2} \right)$$