$OUTPUT ::= success \mid alreadyInDirectory \mid notInDirectory \mid numberInUse$

Successmessage!:OUTPUTmessage! = success $AlreadyInDirectory_$ message!: OUTPUTn?: NAMEs?: SURNAME $n? \mapsto s \in persons$ message! = alreadyInDirectoryNameNotInDirectory. message!:OUTPUTn?: NAMEs?:SURNAME $n? \mapsto s? \notin persons$ message! = NamenotInDirectory $NumberInUse_$ message!:OUTPUTp?: TELEPHONE $p? \in \operatorname{ran} phoneNumbers$ message! = numberInUse

$$\begin{split} & Total Add Person \; \widehat{=} \; (Add Person \; \wedge \; Success) \; \vee \; Already In Directory \\ & Total Remove Person \; \widehat{=} \; (Remove Person \; \wedge \; Success) \; \vee \; Name Not In Directory \\ & Total Add Number \; \widehat{=} \; (Add Number \; \wedge \; Success) \; \vee \; Name Not In Directory \; \vee \; Number In Use \end{split}$$