```
[NAME]
[SURNAME]
[TELEPHONE]
 \_ Telephone Directory \_\_
  persons: NAME \rightarrow SURNAME
  phoneNumbers: NAME \rightarrow TELEPHONE
  dom phoneNumbers = dom persons
  InitTelephoneDirectory
  Telephone Directory'
  phoneNumbers' = \{\}persons' = \{\}
  AddPerson \_
  The {\it Telephone Directory}
  name?: NAME
  surname?: SURNAME phone?: TELEPHONE
  name? \mapsto surname? \not\in persons
  phoneNumbers' = phoneNumbers \cup \{name? \mapsto phone?\}
  AddNumber\_
  \Delta Telephone Directory
  n?: NAME
  s?: SURNAMEp?: TELEPHONE
  n\mapsto s\in persons
  p? \notin \operatorname{ran} phoneNumbers
  phoneNumbers' = phoneNumbers \cup \{n \mapsto phone?\}
  RemovePerson\_
  \Delta Telephone Directory
  n?: NAME
  s?: SURNAMEp?: TELEPHONE
```

 $n? \mapsto s? \in persons$ 

 $\begin{array}{l} n? \mapsto p? \notin phoneNumbers \\ persons' = persons \setminus \{n? \mapsto s?\} \end{array}$ 

## $OUTPUT ::= success \mid alreadyInDirectory \mid notInDirectory \mid numberInUse$

Successmessage!:OUTPUTmessage! = success $AlreadyInDirectory\_$ message!: OUTPUTn?: NAMEs?: SURNAME $n? \mapsto s \in persons$ message! = alreadyInDirectoryNameNotInDirectory. message!:OUTPUTn?: NAMEs?:SURNAME $n? \mapsto s? \notin persons$ message! = NamenotInDirectory $NumberInUse\_$ message!:OUTPUTp?: TELEPHONE $p? \in \operatorname{ran} phoneNumbers$ message! = numberInUse

 $Total Add Person \ \widehat{=} \ (Add Person \land Success) \lor Already In Directory \\ Total Remove Person \ \widehat{=} \ (Remove Person \land Success) \lor Name Not In Directory \\ Total Add Number \ \widehat{=} \ (Add Number \land Success) \lor Name Not In Directory \lor Number In Use$