Week 12 Homework due on Dec 7, 18:59 Hour

Group 5

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Exercise 1

Incorporate your digital certificate framework (this week's classwork) to your key negotiation protocol (Week 11 classwork). Then incorporate both to your secure channel implementation (Week 9 homework). More specifically, in the final system:

- a) Alice and Bob trust a CA (i.e., Alice and Bob have the CA's certificate).
- b) This CA issues certificates for Alice and Bob respectively.
- c) Alice initiates a connection with Bob, starting an authenticated key negotiation. (She needs to send her certificate which is then validated by Bob.)
- d) Bob authenticates the negotiation. (He also needs to send his certificate to Alice.)
- e) After a shared key is established, the secure channel can be initiated.

Answers:

When Alice and Bob wants to communicate securely, they would both generates their public/private key pairs. They would take their public keys to the CA to have them signed and certified. Both Alice and Bob would exchange their public keys and verify them by the certificates. They would then conduct the key negotiation protocol to set up a session key which will be used to set up a secure channel to exchange data. This protocol will utilize the Diffie-Hellman key exchange protocol (final version) and the associated parameters to generate a session key. This key will be used to establish the secure channel.

When establishing a secure channel, the session secret key with a 256-bit value is generated in the above key negotiation process for Alice and Bob only. The secure channel design is made up of three components: message numbering, authentication, and encryption. The message number will help Bob keep track of the messages from Alice and to prevent replay attack from Eve. The message number is also a source for IVs for the encryption algorithm. For authentication, we will use HMAC-SHA-256 to generate the full 256-bit results. For encryption, we will use AES in CBC mode with the nonce value generated by the message number.

Using the codes written in week 12 classwork, week 11 classwork and week 9 homework, we develop a full set of Python codes that allows Alice and Bob to generate public and private keys, have their public keys signed by CA, set up a session key using the Key Negotiation protocol and using it to establish a secure channel for communication between them. The codes and the outputs are listed below.

```
from Cryptodome.Cipher import AES
from Crypto. Hash import SHA256
from Crypto.Signature import PKCS1_v1_5
from Crypto.PublicKey import RSA
import time
import math
import random
import hashlib
import binascii
import hmac
from Cryptodome.Protocol import KDF
class KeyNego(object):
  def __init__(self):
    self.key = RSA.generate(1024)
  def isPrime(self, n):
       if n <=1: return False
       i = 2
       while i*i <= n:
               if n%i == 0: return False
               i += 1
       return True
  def generatePrime(self, keysize):
    while True:
      num = random.randrange(2**(keysize-1), 2**(keysize))
      if self.isPrime(num):
        return num
  def choose_gpq(self, Sa, Sb):
    alfa = 2
    g = 0
    s = max(Sa, Sb)
    if s > 2*Sb:
      return False
    while(True):
      p = self.generatePrime(s)
      if math.log(p,2) < s-1:
        continue
      q = (p-1)/2
      if not self.isPrime(q):
        continue
      while(True):
        alfa = random.randint(2, p-2)
        g = alfa**2 % p
        if g == 1:
          continue
```

```
if g == p-1:
        continue
      break
    b = random.randint(1, q-1)
    B = g^{**}b \% p
    break
  message = g+p+q+B
  key = RSA.generate(1024)
  publickey = key.publickey()
  h = SHA256.new(hex(message))
  signature = PKCS1_v1_5.new(key).sign(h)
  return g, p, q, b, B, publickey, signature
def receiveFromAlice(self, Sa, g, p, q, B, publickey, signature):
  message = g+p+q+B
  hash_message = SHA256.new(hex(message))
  if PKCS1_v1_5.new(publickey).verify(hash_message, signature) == False:
    print 'error'
  if ((Sa-1) < math.log(p,2)) & (math.log(p,2) < 2*Sa):
    if not self.isPrime(q):
      print 'error'
    if not self.isPrime(p):
      print 'error'
    if 2*q!= (p-1):
      print 'error'
    if g == 1:
      print 'error'
    if g == p-1:
      print 'error'
    if B == 1:
      print 'error'
    if B**q % p != 1:
      print 'error'
    a = random.randint(1, q-1)
    A = g^{**}a \% p
    K_prime = B**a % p
    h = SHA256.new()
    h.update(hex(K_prime))
    K = h.hexdigest()
    message1 = A
    key new = RSA.generate(1024)
    publickey new = key new.publickey()
    hash_new = SHA256.new(hex(message1))
    signature new = PKCS1 v1 5.new(key new).sign(hash new)
    return a, A, K_prime, K, publickey_new, signature_new
  else:
    print 'error'
```

```
def bobReceive(self, A, g, p, q, b, publickey_new, signature_new):
    message = A
    hash_message = SHA256.new(hex(message))
    if PKCS1_v1_5.new(publickey_new).verify(hash_message, signature_new) == False:
      print 'error'
    if A == 1:
      print 'error'
    if A**q % p != 1:
      print 'error'
    K prime = A^**b\% p
    h = SHA256.new()
    h.update(hex(K prime))
    K = h.hexdigest()
    return K_prime, K
class RootCA(object):
 def __init__(self):
    self.key = RSA.generate(1024)
    self.publicKey = self.key.publickey()
 def generateCertiChain(self, name, public key):
    owner = name
    issuer = 'RootCA'
    not_before = int(time.time())
    not_after = int(time.time() + 10*365*24*60*60)
    publicKey = public_key
    message = owner+issuer+str(not_before)+str(not_after)
    hash_message = SHA256.new(message)
    signature = PKCS1_v1_5.new(self.key).sign(hash_message)
    certificate = []
    certificate.append(owner)
    certificate.append(issuer)
    certificate.append(not_before)
    certificate.append(not_after)
    certificate.append(publicKey)
    certificate.append(signature)
    return certificate
 def applyCertificateChain(self, name, message, public key, signature):
    hash message = SHA256.new(message);
    verified = PKCS1 v1 5.new(public key).verify(hash message, signature)
    if verified == True:
      return self.generateCertiChain(name, public key);
  def getPublicKey(self):
    return self.publicKey;
class Alice(object):
```

```
def init (self):
    self.name = 'Alice'
    self.key = RSA.generate(1024)
    self.publicKey = self.key.publickey()
    self.CAdic = {}
    self.Sa = 8;
    self.share_key = ";
    self.certificate = None;
    self.sender_counter = 0;
    self.receiver counter = 0;
    self.encry_key = (KDF.HKDF(self.share_key, salt=None, key_len=32, hashmod=SHA256,
num keys=2, context=None))[0]
    self.auth_key = (KDF.HKDF(self.share_key, salt=None, key_len=32, hashmod=SHA256,
num_keys=2, context=None))[1]
 def getPKIKey(self, name, PKI_object):
    key = PKI object.getPublicKey();
    self.CAdic[name] = key;
 def applyCertificateChain(self, message, PKI object):
    hash message = SHA256.new(message)
    signature = PKCS1 v1 5.new(self.key).sign(hash message)
    certificate = PKI object.applyCertificateChain(self.name, message, self.publicKey,
signature)
    self.certificate = certificate
    return certificate
 def sendToBob(self, certificate, send_objetc, nego_object):
    sending = []
    N = random.randint(0, 2**256-1)
    sending.append(self.Sa)
    sending.append(N)
    sending.append(certificate)
    print '===== step 4.1: Alice sending Sa, N, certificate =======
    print 'Sa:', self.Sa
    print 'N:', N
    return send_objetc.BobVerify(sending, nego_object, self)
 def receiveBobNego(self, g, p, q, b, B, publickey, signature, nego object, bob object,
certificate):
    print '====== step 4.3: Alice verify certificate(Bob) ========
    verified = self.AliceVerify(certificate)
    if verified == True:
      a, A, K prime, K, publickey new, signature new =
nego_object.receiveFromAlice(self.Sa, g, p, q, B, publickey, signature)
      self.share key = K
      print '====== Alice sends A, sig(Alice) to Bob ============
      print 'A:', A
```

```
print '====== Alice generate shared key =============
      bob_object.generateShareKey(A, g, p, q, b, publickey_new, signature_new,
nego_object);
  def getShareKey(self):
    return self.share_key;
 def AliceVerify(self, certificate):
    if time.time() < certificate[2] or time.time() > certificate[3]:
      return False;
    message = certificate[0]+certificate[1]+str(certificate[2])+str(certificate[3]);
    hash message = SHA256.new(message);
    verified = PKCS1_v1_5.new(self.CAdic[certificate[1]]).verify(hash_message, certificate[5])
    if verified == False:
      return False;
    else:
      return True;
 def send(self, msg):
    print '====== step 5.1: Alice send (First meg from Alice!) =======
    IV = hashlib.sha256(format(self.sender counter, 'x')).hexdigest()[:16]
    cipher = AES.new(self.encry_key, AES.MODE_CBC, IV)
    if len(msg) \% 16 == 0:
      message = msg
    else:
      message = msg.encode('hex') + '80' + (16 - len(msg) % 16 - 1)*'00'
    ciphertext = binascii.hexlify(cipher.encrypt(message))
    authtext = (hmac.new(self.auth_key, ciphertext, hashlib.sha256).hexdigest())
    counter_len = len((format(self.sender_counter, 'x')))
    if counter len < 4*2:
      counter = (4*2 - counter len)*'0' + (format(self.sender counter, 'x'))
    else:
      counter = counter len
    protected_msg = counter + ciphertext + authtext
    self.sender counter += 1
    print '====== Whole sending message: ==============
    print 'counter:', counter
    print 'ciphertext:', (ciphertext)
    print 'authtext:', (authtext)
    return protected_msg
 def receive(self, protected msg):
    print '====== step 5.4: Alice decrypte meg from Bob =========
    size = len(protected msg)
    authtext = protected_msg[size-64:]
    ciphertext = (protected msg[8:size-64])
    counter = int(protected_msg[0:8], 16)
    verify_authtext = hmac.new(self.auth_key, (ciphertext), hashlib.sha256).hexdigest()
```

```
if (authtext == verify authtext):
      IV = hashlib.sha256(format(counter, 'x')).hexdigest()[:16]
      cipher = AES.new(self.encry_key, AES.MODE_CBC, IV)
      msg = cipher.decrypt((ciphertext).decode('hex'))
      msg size = len(msg)
      for i in range(msg_size / 2):
        if msg[msg_size-2:] == '00':
           msg = msg[0:msg_size-2]
          msg_size -= 2
          continue;
        if msg[msg_size-2:] == '80':
           msg = msg[0:msg size-2]
          msg_size -= 2
          break;
      self.receiver_counter += 1
      print 'Msg to Bob:', binascii.unhexlify(msg)
    else:
      print 'authenticate failed!'
class Bob(object):
  def init (self):
    self.name = 'Bob'
    self.key = RSA.generate(1024)
    self.publicKey = self.key.publickey();
    self.CAdic = {}
    self.Sb = 10;
    self.share_key = ";
    self.certificate = None;
    self.sender_counter = 0;
    self.receiver counter = 0;
    self.encry_key = (KDF.HKDF(self.share_key, salt=None, key_len=32, hashmod=SHA256,
num keys=2, context=None))[0]
    self.auth_key = (KDF.HKDF(self.share_key, salt=None, key_len=32, hashmod=SHA256,
num_keys=2, context=None))[1]
  def getPKIKey(self, name, PKI_object):
    key = PKI_object.getPublicKey();
    self.CAdic[name] = key;
  def applyCertificateChain(self, message, PKI object):
    hash message = SHA256.new(message)
    signature = PKCS1 v1 5.new(self.key).sign(hash message)
    certificate = PKI_object.applyCertificateChain(self.name, message, self.publicKey,
signature)
    self.certificate = certificate
    return certificate
  def sendToAlice(self, certificate, send_objetc):
```

```
return send objetc. AliceVerify(certificate)
  def BobSendNego(self, Sa, nego_object, alice_object):
    g, p, q, b, B, publickey, signature = nego_object.choose_gpq(Sa, self.Sb)
    print '===== then Bob sends (g,p,q), B, sig(Bob), certificate(Bob) ==='
    print '(g,p,q):', g,p,q
    print 'B:', B
    alice object.receiveBobNego(g, p, q, b, B, publickey, signature, nego_object, self,
self.certificate)
  def generateShareKey(self, A, g, p, q, b, publickey_new, signature_new, nego_object):
    print '====== step 4.4: Bob verify and generate shared key ======='
    K_prime, K = nego_object.bobReceive(A, g, p, q, b, publickey_new, signature_new)
    self.share key = K
  def getShareKey(self):
    return self.share_key;
  def BobVerify(self, certificate, nego object, alice object):
    if time.time() < certificate[2][2] or time.time() > certificate[2][3]:
      return False;
    message = certificate[2][0]+certificate[2][1]+str(certificate[2][2])+str(certificate[2][3]);
    hash message = SHA256.new(message);
    verified = PKCS1_v1_5.new(self.CAdic[certificate[2][1]]).verify(hash_message,
certificate[2][5])
    print '====== step 4.2: Bob verify certificate(Alice) ========
    if verified == False:
      return False;
    else:
      self.BobSendNego(certificate[0], nego object, alice object)
      return True;
  def send(self, msg):
    print '====== step 5.3: Bob send (First meg from Bob!) ========
    IV = hashlib.sha256(format(self.sender_counter, 'x')).hexdigest()[:16]
    cipher = AES.new(self.encry_key, AES.MODE_CBC, IV)
    if len(msg) \% 16 == 0:
      message = msg
    else:
      message = msg.encode('hex') + '80' + (16 - len(msg) % 16 - 1)*'00'
    ciphertext = binascii.hexlify(cipher.encrypt(message))
    authtext = (hmac.new(self.auth key, ciphertext, hashlib.sha256).hexdigest())
    counter_len = len((format(self.sender_counter, 'x')))
    if counter len < 4*2:
      counter = (4*2 - counter_len)*'0' + (format(self.sender_counter, 'x'))
    else:
      counter = counter_len
    protected_msg = counter + ciphertext + authtext
```

```
self.sender counter += 1
    print '====== Whole sending message: ==============
    print 'counter:', counter
    print 'ciphertext:', (ciphertext)
    print 'authtext:', (authtext)
    return protected_msg
  def receive(self, protected msg):
    print '===== step 5.2: Bob decrypte meg from Alice =========
    size = len(protected msg)
    authtext = protected msg[size-64:]
    ciphertext = (protected msg[8:size-64])
    counter = int(protected_msg[0:8], 16)
    verify_authtext = hmac.new(self.auth_key, (ciphertext), hashlib.sha256).hexdigest()
    if (authtext == verify_authtext):
      IV = hashlib.sha256(format(counter, 'x')).hexdigest()[:16]
      cipher = AES.new(self.encry_key, AES.MODE_CBC, IV)
      msg = cipher.decrypt((ciphertext).decode('hex'))
      msg size = len(msg)
      for i in range(msg_size / 2):
        if msg[msg size-2:] == '00':
          msg = msg[0:msg size-2]
          msg size -= 2
          continue;
        if msg[msg_size-2:] == '80':
          msg = msg[0:msg_size-2]
          msg_size -= 2
          break:
      self.receiver_counter += 1
      print 'Msg to Alice:', binascii.unhexlify(msg)
    else:
      print 'authenticate failed!'
print '====== Step 1: Initialize class ===========
alice = Alice()
bob = Bob()
rootca = RootCA()
keyNego = KeyNego()
print '\n====== Step 2: Alice, Bob get RootCA public key =========
alice.getPKIKey('RootCA', rootca)
bob.getPKIKey('RootCA', rootca)
print '\n====== Step 3: Alice, Bob get certificate from RootCA ======'
aliceCeriFromRoot = alice.applyCertificateChain('I am Alice!', rootca)
print 'Alice certificate:\n', aliceCeriFromRoot
bobCeriFromRoot = bob.applyCertificateChain('I am Bob!', rootca)
print 'Bob certificate:\n', bobCeriFromRoot
```

```
print '\n====== Step 4: Alice initiates connection with Bob ========
 verified = alice.sendToBob(aliceCeriFromRoot, bob, keyNego)
 alice_share_key = alice.getShareKey()
 bob share key = bob.getShareKey()
 print 'shared key of Alice is:', alice share key
 print 'shared_key of Bob is:', bob_share_key
 print '\n====== Step 5: After shared_key is established =========
 msg1 = alice.send("First meg from Alice!")
 bob.receive(msg1)
 msg3 = bob.send("First meg from Bob!")
 alice.receive(msg3)
 print '\n====== All steps finish! ===========
The outputs are listed below.
====== Step 1: Initialize class ================
```

```
====== Step 2: Alice, Bob get RootCA public key ========
====== Step 3: Alice, Bob get certificate from RootCA ======
Alice certificate:
['Alice', 'RootCA', 1543929578, 1859289578, < RSAobj @0x1c193df290
n(1024), e>
"ZK \x8fn\xc7k\xea2\x850\xfe\x10bwm\xc1q\x84\x05\x08D$\x1c\xf2\xb2[5{\
xcd \times 05 \times 11 \times c1 \times c0 \times 87 \times edg \times 0e \times 86 > \times 97 \times 98 \times b9 \times 02 \times c9 \times 95 \times 8e \times c0 \times edg \times
3\x04\x18\x14\x18\xa6,\t0^{\x}00\xe2\xf61H\x81\xe4L,]\xaeG^{\x}01G
xdd/x96cGK/x10/x01Q&|'Y/xfb^/x8e/x99/xfa(/x08/x15/xdd/x92'/xc9/x03/xc1)
\a8c\x7f\xe0v\xdc\xb9\x05\x18\x19\x8b\x19\x1aR@\x08\xb2\xe1\xa1\x85[
xc8i."1
Bob certificate:
['Bob', 'RootCA', 1543929578, 1859289578, <_RSAobj @0x1c18c0ba28
n(1024), e>
"\x18\x91{Q\t+V\x8c\xcfy2Kk<\x03\x03Rr\xfdh\xc7'\xfb\xe3RUf\r\x19\x82L
q\xde\x8f\x92'\x02\xec\xd3\x13\x02\x06c\xd8\xac\xe9Q\xc3\xa2oj\xb4\xcc
x01\xf4\x841 C\x0f\xa8\xf2\xfd\xb8\x9c\x93\xcd\xb5\xac\xbe\x12\xceY\x
xdf\xf4\xce=\xa7\xee30\xd3qb{\x7ftH\xc2\x15\xd2\x94\xd85\x00\xba\x06\x
1f\x18"]
```

===== Step 4: Alice initiates connection with Bob =======

```
====== step 4.1: Alice sending Sa, N, certificate =======
Sa: 8
7709027457061269806689754725077654279246075341707737799556902362905950
8795457
====== step 4.2: Bob verify certificate(Alice) =========
==== then Bob sends (g,p,q), B, sig(Bob), certificate(Bob) ===
(q,p,q): 189 563 281
B: 197
===== step 4.3: Alice verify certificate(Bob) =========
====== Alice sends A, sig(Alice) to Bob =============
A: 183
====== Alice generate shared key ============================
====== step 4.4: Bob verify and generate shared key =======
shared key of Alice is:
1bd69d78f424afc1d10edb599ad44be71d0b99167c51dc9f3af087a79dacb059
shared key of Bob is:
1bd69d78f424afc1d10edb599ad44be71d0b99167c51dc9f3af087a79dacb059
====== Step 5: After shared key is established ========
====== step 5.1: Alice send (First meg from Alice!) =======
====== Whole sending message: ==================
counter: 00000000
ciphertext:
eafa6ecc33c10332646e4a918e8eb3e52dd220e54540f384e635210bf30dbb90432fba
5d824e3d33a2b53604676700d5755b12d36064417438ae12ae1fb4e059
```

f80566f5b717d892dfc4a48e32109adc5f850e36c7a0ea3916bcdc51ea0ff2d7

authtext:

====== step 5.2: Bob decrypte meg from Alice ========
Msg to Alice: First meg from Alice!
====== step 5.3: Bob send (First meg from Bob!) =======
====== Whole sending message: ===============================
counter: 00000000
ciphertext: eafa6ecc33c10332646e4a918e8eb3e56f44b272fe968e10ae5c3ae928bf72e504761d 52b94df2ebc5a923b7aafe38e4a41ec9fc87851a1b1bd85e5bfa93e59b
authtext: 94d602a4f42c1926e240851c6f1ea08a21caba75f1118840c3a82ebe56c18df3
====== step 5.4: Alice decrypte meg from Bob ========
Msg to Bob: First meg from Bob!
====== All steps finish! ====================================