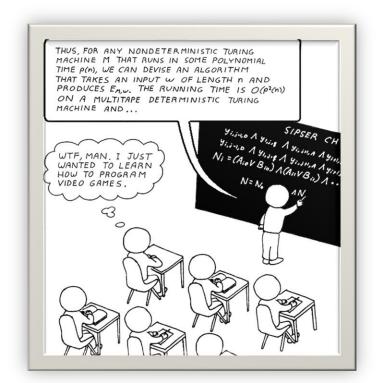
Game Theory Meets Computer Science

A Basic Introduction

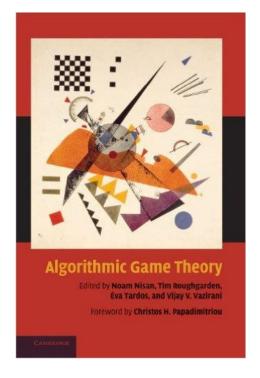




姜桂飞 南开大学·软件学院 G.Jiang@nankai.edu.cn

Algorithmic Game Theory

- Algorithmic Game Theory is an area in the intersection of game theory and algorithm design, whose objective is to design algorithms in strategic environments [Nisan et al. 2007].
- Computing in Games
 - Algorithms for computing equilibria
- Algorithmic Mechanism Design
 - Design games that have both good
 game-theoretical and algorithmic properties



Prisoner's Dilemma

Row	Deny	Confess
Deny	(-1, -1)	(-10, 0)
Confess	(0, -10)	(-8, -8)

Prisoner's Dilemma

Row	Deny	Confess
Deny	(-1, -1)	(-10, 0)
Confess	(0, -10)	(-8, -8)

- The equilibrium payoffs are (-8,-8) Pareto inefficient!!
- worse for both players than (-1, -1)

Generalized Second Price (GSP) Auction





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Algorithmic Game Theory in Artificial Intelligence

- Game Playing: computation challenge, AlphaGo, Libratus, General Game Playing
- Mechanism Design: the allocation of scarce resources (security games), Ad/online auctions, Computational Social Choice
- IJCAI Computers and Thought Award: 7 out of the 15 winners (1999-2021) had worked on AGT
 - Nick Jennings (1999), Tuomas Sandholm (2003), Peter Stone (2007),
 Vice Conitzer (2011), Ariel Procaccia (2015), Piotr Skowron (2020), Fei
 Fang (2021).

Outline

- Game Theory Basics
- Game Playing Algorithms
 - Adversarial Search
 - Monte-Carlo Tree Search
 - General Game Playing
- Beyond
 - Computational Social Choice
 - Auction



Game Theory Meets Computer Science

PART ONE GAME THEORY BASICS

Let us play a game: The Grade Game

Without showing your neighbor what you are doing, write down on a form either the letter α or the letter β . Think of this as a 'grade bid'. We will randomly pair your form with one other form. Neither you nor your pair will ever know with whom you were paired. Here is how grades may be assigned.

- If you put α and your pair puts β , then you will get grade A, and your pair grade C.
- if both you and your pair put α , then you both will get grade B-.
- if you put β and your pair puts α , then you will get grade C, and your pair grade A.
- if both you and your pair put β , then you both will get grade B+.

Outcome Matrix

you pair	α	β
α	(B-, B-)	(A, C)
β	(C, A)	(B+, B+)
Your outcome by	(α, β) Your pair's o	outcome by (α, β)

What a rational player choose?

you pair	α	β
α	(B-, B-)	(A, C)
β	(C, A)	(B+, B+)

- Payoff—each outcome yield for each player
- Preferences of players: not just you but also your opponents

Basic Concepts

- A game: strategic decision-making situation
 - rational players
 - available actions
 - possible utilities
 - Information
- Equilibrium: a strategy profile consisting of a best strategy for each player
- We focus on noncooperative games.
 - No external force or agencies enforcing coalitions.

Player Strategy

Pure strategy

- Choose an action to play
- E.g., "α", "β"
- For our purposes, simply an action.
 - In repeated or multi-move games (like Chess), need to choose an action to play at every step of the game based on history.

Mixed strategy

- Choose a probability distribution over actions
- Randomize over pure strategies
- E.g., " α with probability 0.7, and β with probability 0.3"

von Neumann and Morgenstern

1944 by Princeton University Press

Game Theory

- The study of mathematical models of strategic interaction among rational decision-makers.
- Applications in all fields of social science, as well as in logic, systems science, and computer science.

----Wikipedia

"the classic work upon which modern-day game theory is based."

Possible payoffs: Evil gits.

If every player only cares about her own grade then (assuming A > B+>B->C for each player)

you pair	α	β
α	(0, 0)	(3, -1)
β	(-1, 3)	(1, 1)

What should you choose in this case?

Possible payoffs: Evil gits.

If every player only cares about her own grade then (assuming A > B+>B->C for each player)

you pair	α	β
α	(0, 0)	(3, -1)
β	(-1, 3)	(1, 1)

- \succ Your payoff from α is *strictly* higher than that from β regardless of others' choices.
- \triangleright Your strategy α *strictly dominates* your strategy β .

Dominant Strategy

 For player i, strategy x dominates strategy y if playing x is better than playing y no matter what the other players do

Lesson 1: You should never play a strictly dominated strategy

What about the opponent?

you pair	α	β
α	(<u>0</u> , <u>0</u>)	(<u>3</u> , -1)
β	(-1, <u>3</u>)	(1, 1)

• Given the payoff, she will also choose strategy " α ".

What about the opponent?

you pair	α	β	
α	(<u>0</u> , <u>0</u>)	(<u>3</u> ,	-1)
B	(1,3)	/1 \±,	1)
	, , _,		,

- Given the payoff, she will also choose strategy " α ".
- Dominant-strategy equilibrium: (α, α) .

Something goes wrong?

you pair	α	β
α	(<u>0</u> , <u>0</u>)	(<u>3</u> , -1)
β	(-1, <u>3</u>)	(1, 1)

• Dominant-strategy equilibrium: (α, α) .

Something goes wrong?

you pair	α	β
α	(<u>0</u> , <u>0</u>)	(<u>3</u> , -1)
β	(-1, <u>3</u>)	(1, 1)

- Dominant-strategy equilibrium: $(\alpha,\alpha) \rightarrow (B-,B-)$ Pareto inefficient!!
- Games like this called Prisoners' Dilemmas.

Something goes wrong?

you pair	α	β
α	(<u>0</u> , <u>0</u>)	(<u>3</u> , -1)
β	(-1, <u>3</u>)	(1, 1)

- Dominant-strategy equilibrium: $(\alpha,\alpha) \rightarrow (B-,B-)$ Pareto inefficient!!
- Games like this called Prisoners' Dilemmas.

Recap: Prisoner's Dilemma

Row Column	Deny	Confess
Deny	(-1, -1)	(-10, 0)
Confess	(0, -10)	(-8, -8)

- A dominant strategy equilibrium is (Confess, Confess)
- The equilibrium payoffs are (-8,-8)
- worse for both players than (-1, -1)

Lesson 2: Rational play by rational players can lead to bad outcomes.

Other possible payoffs The Evil Git versus the Indignant Angel

What if you are an evil git but you know your opponent is an indignant angel who cares not only about her own grade but also about yours?

you pair	α	β
α	(0, 0)	(3, -3)
β	(-1, -1)	(1, 1)

What should you choose in this case?

The Evil Git versus the Indignant Angel

What if you are an evil git but you know your opponent is an indignant angel?

you pair	α	β
α	(0, 0)	(3, -3)
β	(-1, -1)	(1, 1)

- What should you choose in this case?
- Choose α

The Converse

What if you are an indignant angel but you know your opponent is an evil git?

you pair	α	β
α	(0, 0)	(-1, -3)
β	(-3, 3)	(1, 1)

Neither of your strategies dominates the other.

What should you choose in this case?

Put yourself in your opponents' shoes

you pair	α	β
α	(0, 0)	(-1, -3)
β	(-3, 3)	(1, 1)

• Neither of your strategies dominates the other.

Put yourself in your opponents' shoes

α (0,0) (-1,-3) β (-3,3) (1,1)	you pair	α		3
β (-3, 3) (1, 1)	α	(0, 0)	(-1	-3)
	β	(-3, 3)	(1	1)

- Neither of your strategies dominates the other.
- Your pair's strategy α strictly dominates her strategy β .

Put yourself in your opponents' shoes

you pair	α	β	
α	(<mark>0</mark> , <u>0</u>)	(-1, -	3)
β	(-3 <u>, 3</u>)	(1, 1)

- Neither of your strategies dominates the other.
- Your pair's strategy α strictly dominates her strategy β .
- Then you should play α .

Iterated Elimination

- What if there are no dominant strategies?
 - No single strategy dominates every other strategy
 - But some strategies might still be dominated

- Assume every knows everyone is rational.
 - Can remove their dominated strategies
 - Might reveal a newly dominant strategy

Iterated Elimination

you pair	α		3
α	(0, <u>0</u>)	(-1	-3)
ß	(-3, 3)	(1	1)

Lesson 3: If you do not have a dominated strategy, put yourself in your opponents' shoes to try to predict what they will do. For example, in their shoes, they would not choose a dominated strategy.

Possible payoffs: Indignant angels

Suppose that each person cares not only about her own grade but also about the grade of the person with whom she is paired.

you pair	α	β
α	(0, 0)	(-1, -3)
β	(-3, -1)	(1, 1)

What should you choose in this case?

Coordination Game

you pair	α	β
α	(<u>0</u> , 0)	(-1, -3)
β	(-3, -1)	(<u>1</u> , 1)

No strategy is dominated.

Lesson 4: To figure out what actions you should choose in a game, a good first step is to figure out what are your payoffs (what do you care about) and what are other players' payoffs.

Nash Equilibrium



John Forbes Nash (June 13, 1928 - May 23, 2015)

 Game theory, differential geometry, and partial differential equations

 Laid the foundations for modern noncooperative game theory

 Awarded the 1994 Nobel Prize for Economics

Nash Equilibrium

 A set of strategies, one for each player such that no player has incentive to deviate from her strategy given that the other players do not deviate

you pair	α	β
α	(0, 0)	(-1, -3)
β	(-3, -1)	(1, 1)

> Try to figure out the NEs

Nash Equilibrium

you pair	α	β
α	(0, 0)	(-1, -3)
β	(-3, -1)	(1, 1)

- \triangleright (α , α) and (β , β) are Nash Equilibria.
- > A Dominant-strategy equilibrium is a Nash Equilibrium.

The Battle of the Sexes

Girl	THE SECOND SECON	THE PROPERTY OF THE PROPERTY O
The Best of the Second	(2, 1)	(0, 0)
OF SOIS THE PART OF THE PART	(0, 0)	(1, 2)

- Two NEs (父辈, 父辈), (长津湖,长津湖)
- Which one to choose?

Experimental Results

What do people do in real world?

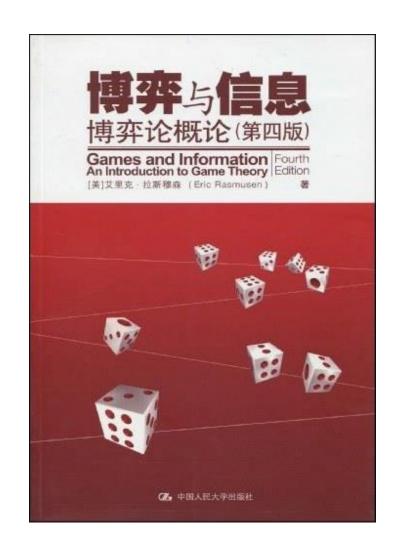
• In larger experiments with 'normal people', roughly 70% of people choose Alpha and roughly 30% choose Beta.

Mixed Strategies: Rock-Paper-Scissor

P2 P1		THE S	
	0,0	-1,1	1,-1
West	1,-1	0,0	-1,1
	-1,1	1,-1	0,0

- No dominant strategy; No NE in pure strategies
- Have a mixed-strategy NE

How to calculate the mixed-strategy NE?



Existence of Nash Equilibria

• Theorem (Nash, 1951)

Every finite game has a mixed-strategy Nash equilibrium.

Nash, J. (1951). Non-cooperative games. Annals of Mathematics, 54, 286–295

Knowledge Game: The Muddy Children Puzzle



- 1. At least one of you has mud on your forehead.
- 2. Can you tell for sure whether or not you have mud on your forehead.

Exercise: Pick up a number

- ➤ Without showing your neighbor what you're doing, put in the box below a whole number between 1 and a 100.
- > We will calculate the average number chosen in the class.
- The winner in this game is the person whose number is closest to two-thirds times the average in the class.
- The winner will win the prize and all other players win nothing.

Conclusion

- Three Concepts
 - Dominant-strategy equilibrium
 - –Nash equilibrium
 - -Mixed-strategy Nash equilibrium
- Four Lessons
 - -Put yourself in your opponents' shoes

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