

# COMPAS Data Visualization

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## Introduction

## Problem Statement

## Data Description

ProPublica collected data on **TODO**

In the data set we look at, they considered only people who either “recidivated within two years of their crime or”recidivated in tow years, or had at least tow years outside of a correctional facility."

## Data Dictionary

ProPublica did not provide a data dictionary explaining their variables. Through some manual exploration, we came up with the following descriptions for our best guess at what each variable measures.

Variable	Description
id	unqe identifier for each individual
name	first and last name
first	first name
last	last name
compas_screening_date	date on which decile_score was given
sex	sex (male or female)
dob	date of birth
age	age in years
age_cat	age category (less than 25, 25-45, greater than 45)
race	race (African-American, Asian, Caucasian, Hispanic, Native American, Other)
juv_fel_count	juvenile felony count
decile_score	COMPAS Risk of Recidivism score from 1 to 10
juv_misd_count	juvenile misdemeanor count
juv_other_count	juvenile other offenses count
priors_count	prior offenses count
days_b_screening_arrest	number of days between COMPAS screening and arrest <b>TODO</b> negative values?
c_jail_in	jail entry date for original crime
c_jail_out	jail exit date for original crime
c_case_number	case number for original crime
c_offense_date	offense date of original crime
c_arrest_date	arrest date for original crime
c_days_from_compas	days between COMPAS screening and original crime offense date
c_charge_degree	charge degree of original crime
c_charge_desc	description of charge for original crime
is_recid	binary indicator of recidivation (1=individual recidivated, 0=individual did not recidivate)
r_case_number	case number of follow-up crime

Variable	Description
r_charge_degree	charge degree of follow-up crime
r_days_from_arrest	number of days between follow-up crime and arrest date <b>TODO</b> why negative value here?
r_offense_date	date of follow-up crime
r_charge_desc	description of charge for follow-up crime
r_jail_in	jail entry date for follow-up crime
r_jail_out	jail exit date for follow-up crime
violent_recid	values are all NA. This column is ignored.
is_voilent_recid	binary indicator of violent follow-up crime (1=follow-up crime was violent, 0=follow-up crime was non-violent)
vr_case_number	case number for violent follow-up crime
vr_charge_degree	charge degree for violent follow-up crime
vr_offense_date	date of offense for violent follow-up crime
vr_charge_desc	description of charge for violent follow-up crime
type_of_assessment	the type of COMPAS score given for decile_score (here all values are Risk of Recidivism)
decile_score.1	repeat column of decile_score
score_text	ProPublica-defined category of decile_score (High=8-10, Medium=5-7, Low=1-4)
screening_date	repeat column of compas_screening_date
v_type_of_assessment	the type of COMPAS score given for v_decile_score (here all values are Risk_of_Violence)
v_decile_score	COMPAS Risk of Violence score from 1 to 10
v_score_text	ProPublica-defined category of v_decile_score (High=8-10, Medium=5-7, Low=1-4)
v_screening_date	date on which v_decile_score was given
in_custody	date on which individual was brought into custody
out_custody	date on which individual was released from custody
priors_count.1	repeat column of priors_count
start	<b>TODO</b>
end	<b>TODO</b>
event	<b>TODO</b>

ProPublica obtained this data with the goal of analyzing Northpointe Inc.’s commercial recidivism modeling tool – COMPAS. Aggregating data from public records, they collected data on 18,610 individuals who received COMPAS scores from 2013 to 2014, including demographic information, public criminal records, and incarceration records.

#### *How are COMPAS scores used?*

ProPublica describes that at least in Broward County, they “primarily [use] the score to determine whether to release or detain a defendant before his or her trial.” 11,757 of the individuals in the database had their COMPAS scores used to assess whether or not they should be released before their trial.

#### *What are COMPAS scores?*

There are three types of COMPAS score. Each measures a type of ‘risk’ associated with a criminal re-offending in some way on a scale of 1 (low) to 10 (high). As ProPublica describes, these include

- *Risk of Recidivism*: ProPublica defines this as the person in question committing a “criminal offense that [results] in a jail booking and [takes] place after the crime for which the person was COMPAS scored.” Northpointe hopes to use this score to predict “a new misdemeanor or felony offense within two years of the COMPAS administration date.”
- *Risk of Violence*: They use the FBI definition of violent crime:

*In the FBI's Uniform Crime Reporting (UCR) Program, violent crime is composed of four offenses: murder and nonnegligent manslaughter, forcible rape, robbery, and aggravated assault. Violent crimes are defined in the UCR Program as those offenses which involve force or threat of force. - ucr.fbi.gov*

- *Risk of Failure to Appear*: As evidenced by the name, this describes a failure to appear at the court hearing.

## Exploratory Data Analysis

We first load in the data provided by ProPublica, and take a quick look at summaries of each variable to get a sense of distribution and potential outliers. We'll look at half of the columns at a time to keep things manageable.

```
compas_scores <- read.csv('compas-scores-two-years.csv')
summary(compas_scores[1:(ncol(compas_scores)/2)])
```

```
##           id           name           first
## Min.      : 1    anthony smith      : 3    michael      : 149
## 1st Qu.: 2735   angel santiago    : 2    christopher: 109
## Median : 5510   anthony gonzalez : 2    james       : 84
## Mean    : 5501   anthony louis    : 2    anthony     : 83
## 3rd Qu.: 8246   brandon whitfield: 2    robert      : 76
## Max.    :11001   carlos vasquez   : 2    john       : 74
##           (Other) :7201 (Other) :6639
##           last    compas_screening_date sex      dob
## williams: 83    2013-02-20: 32    Female:1395 1987-02-04: 5
## johnson : 76    2013-03-20: 32    Male :5819 1987-12-21: 5
## brown   : 68    2013-02-07: 31                1989-04-27: 5
## smith   : 65    2013-04-20: 30                1989-08-31: 5
## jones   : 57    2013-01-03: 29                1990-02-22: 5
## davis   : 46    2013-04-25: 28                1990-05-02: 5
## (Other) :6819   (Other)   :7032                (Other)   :7184
##           age      age_cat      race
## Min.    :18.0    25 - 45      :4109   African-American:3696
## 1st Qu.:25.0    Greater than 45:1576   Asian          : 32
## Median :31.0    Less than 25   :1529   Caucasian      :2454
## Mean    :34.8                Hispanic       : 637
## 3rd Qu.:42.0                Native American : 18
## Max.    :96.0                Other          : 377
##
## juv_fel_count    decile_score    juv_misd_count    juv_other_count
## Min.    : 0.000    Min.    : 1.00    Min.    : 0.000    Min.    : 0.000
## 1st Qu.: 0.000    1st Qu.: 2.00    1st Qu.: 0.000    1st Qu.: 0.000
## Median : 0.000    Median : 4.00    Median : 0.000    Median : 0.000
## Mean    : 0.067    Mean    : 4.51    Mean    : 0.091    Mean    : 0.109
## 3rd Qu.: 0.000    3rd Qu.: 7.00    3rd Qu.: 0.000    3rd Qu.: 0.000
## Max.    :20.000    Max.    :10.00    Max.    :13.000    Max.    :17.000
##
## priors_count    days_b_screening_arrest    c_jail_in
## Min.    : 0.00    Min.    : -414.0                : 307
## 1st Qu.: 0.00    1st Qu.: -1.0                2013-01-01 01:31:55: 1
## Median : 2.00    Median : -1.0                2013-01-01 03:16:15: 1
## Mean    : 3.47    Mean    : 3.3                2013-01-01 03:28:03: 1
## 3rd Qu.: 5.00    3rd Qu.: 0.0                2013-01-01 04:17:22: 1
```

```
## Max. :38.00 Max. :1057.0 2013-01-01 04:29:04: 1
## NA's :307 (Other) :6902
## c_jail_out c_case_number c_offense_date
## : 307 : 22 :1159
## 2013-09-12 10:31:00: 3 00004068CF10A: 1 2013-01-14: 26
## 2013-09-14 05:58:00: 3 00022077MM10A: 1 2013-02-22: 26
## 2013-09-28 02:10:00: 3 01004839CF10A: 1 2013-03-01: 24
## 2013-02-06 10:01:51: 2 01006487CF10D: 1 2013-01-11: 23
## 2013-06-13 10:32:00: 2 01007205MM10A: 1 2013-02-16: 23
## (Other) :6894 (Other) :7187 (Other) :5933
## c_arrest_date c_days_from_compas c_charge_degree
## :6077 Min. : 0 F:4666
## 2013-02-06: 9 1st Qu.: 1 M:2548
## 2013-03-22: 8 Median : 1
## 2013-05-15: 8 Mean : 58
## 2013-01-10: 7 3rd Qu.: 2
## 2013-01-11: 7 Max. :9485
## (Other) :1098 NA's :22
## c_charge_desc is_recid r_case_number
## Battery :1156 Min. :0.000 :3743
## arrest case no charge :1137 1st Qu.:0.000 13000349MM10A: 1
## Possession of Cocaine : 474 Median :0.000 13000445MM20A: 1
## Grand Theft in the 3rd Degree: 425 Mean :0.481 13000677MM20A: 1
## Driving While License Revoked: 200 3rd Qu.:1.000 13000758MM30A: 1
## Driving Under The Influence : 135 Max. :1.000 13000785MM30A: 1
## (Other) :3687 (Other) :3466
```

Here we notice there may be large outliers in many of the crime count variables, such as `juv_fel_count`, `juv_misd_count`, `juv_other_count`, and `priors_count`. We expect these are simply accurate observations corresponding to individuals with high numbers of prior offenses. Thus we will not remove these individuals from the data but will be aware of them as potential influential points when we later fit any models. We also note that the values for the 'days\_from' variables are quite variable which may be relevant if we use those variables in later analysis. Looking at the second half of the columns, we have:

```
summary(compas_scores[(ncol(compas_scores)/2 + 1):ncol(compas_scores)])
```

```
## r_charge_degree r_days_from_arrest r_offense_date
## :3743 Min. : -1 :3743
## (M1) :1201 1st Qu.: 0 2014-12-08: 12
## (M2) :1107 Median : 0 2015-01-28: 11
## (F3) : 892 Mean : 20 2014-09-15: 10
## (F2) : 168 3rd Qu.: 1 2014-10-17: 10
## (F1) : 51 Max. :993 2015-02-10: 10
## (Other): 52 NA's :4898 (Other) :3418
## r_charge_desc r_jail_in
## :3801 :4898
## Driving License Suspended : 258 2014-05-27: 9
## Possess Cannabis/20 Grams Or Less: 253 2013-11-22: 8
## Resist/Obstruct W/O Violence : 201 2014-06-05: 8
## Battery : 192 2014-07-10: 8
## Operating W/O Valid License : 172 2014-10-17: 8
## (Other) :2337 (Other) :2275
## r_jail_out violent_recid is_violent_recid vr_case_number
## :4898 Mode:logical Min. :0.000 :6395
## 2014-02-18: 9 NA's:7214 1st Qu.:0.000 13001383CF10A: 1
```

```

## 2014-12-09: 9 Median :0.000 13001876CF10A: 1
## 2015-05-15: 9 Mean :0.114 13002119CF10A: 1
## 2013-11-13: 8 3rd Qu.:0.000 13002546CF10A: 1
## 2014-07-11: 8 Max. :1.000 13003421CF10A: 1
## (Other) :2273 (Other) : 814
## vr_charge_degree vr_offense_date vr_charge_desc
## :6395 :6395 :6395
## (M1) : 344 2015-08-15: 6 Battery : 329
## (F3) : 228 2013-11-14: 4 Battery on Law Enforc Officer : 38
## (F2) : 162 2014-02-18: 4 Felony Battery (Dom Strang) : 38
## (F1) : 38 2014-10-29: 4 Aggravated Assault W/Dead Weap: 37
## (M2) : 19 2014-12-26: 4 Aggrav Battery w/Deadly Weapon: 34
## (Other): 28 (Other) : 797 (Other) : 343
## type_of_assessment decile_score.1 score_text
## Risk of Recidivism:7214 Min. : 1.00 High :1403
## 1st Qu.: 2.00 Low :3897
## Median : 4.00 Medium:1914
## Mean : 4.51
## 3rd Qu.: 7.00
## Max. :10.00
##
## screening_date v_type_of_assessment v_decile_score
## 2013-02-20: 32 Risk of Violence:7214 Min. : 1.00
## 2013-03-20: 32 1st Qu.: 1.00
## 2013-02-07: 31 Median : 3.00
## 2013-04-20: 30 Mean : 3.69
## 2013-01-03: 29 3rd Qu.: 5.00
## 2013-04-25: 28 Max. :10.00
## (Other) :7032
## v_score_text v_screening_date in_custody out_custody
## High : 714 2013-02-20: 32 : 236 : 236
## Low :4761 2013-03-20: 32 2013-02-22: 20 2020-01-01: 61
## Medium:1739 2013-02-07: 31 2013-12-12: 20 2013-05-14: 25
## 2013-04-20: 30 2014-01-04: 20 2014-02-04: 24
## 2013-01-03: 29 2014-01-22: 20 2013-11-26: 23
## 2013-04-25: 28 2013-01-27: 19 2013-02-15: 21
## (Other) :7032 (Other) :6879 (Other) :6824
## priors_count.1 start end event
## Min. : 0.00 Min. : 0.0 Min. : 0 Min. :0.000
## 1st Qu.: 0.00 1st Qu.: 0.0 1st Qu.: 148 1st Qu.:0.000
## Median : 2.00 Median : 0.0 Median : 530 Median :0.000
## Mean : 3.47 Mean : 11.5 Mean : 553 Mean :0.383
## 3rd Qu.: 5.00 3rd Qu.: 1.0 3rd Qu.: 914 3rd Qu.:1.000
## Max. :38.00 Max. :937.0 Max. :1186 Max. :1.000
##

```

With the second half we have similar characteristics as before. We remove the `violent_recid` column given that all values are NA (as mentioned in the data dictionary). Apart from that column, we make no other changes.

```

vars <- compas_scores %>%
  select(sex, race, age, ends_with('count'), c_charge_degree, is_recid)

# ggplot(vars, aes(x = race, y = decile_score)) + geom_boxplot()

```

## ProPublica's Bias-Assessment Model

This section is meant to recreate ProPublica's logistic regression model for assessing bias in COMPAS scores. The code and explanations in this section are taken from their published methodology and code.

Using the same data set, they first filter rows based on the following criteria.

1. consider only individuals with a COMPAS score
2. assure the COMPAS score corresponds to the correct crime i.e. the score was given within 30 days of the arrest
3. do not include ordinary traffic offenses

Next we use their code to perform this filtering:

```
# code from https://github.com/propublica/compas-analysis
df <- compas_scores %>%
  select(age, c_charge_degree, race, age_cat, score_text, sex, priors_count, days_b_screening_arrest, d
  filter(days_b_screening_arrest <= 30) %>%
  filter(days_b_screening_arrest >= -30) %>%
  filter(is_recid != -1) %>%
  filter(c_charge_degree != "0") %>%
  filter(score_text != 'N/A')
nrow(df)

## [1] 6172
```

In order to use this data to assess racial bias in scoring, the ProPublica analysts first create several factor variables from the existing columns.

```
# code from https://github.com/propublica/compas-analysis
df <- mutate(df, crime_factor = factor(c_charge_degree)) %>%
  mutate(age_factor = as.factor(age_cat)) %>%
  within(age_factor <- relevel(age_factor, ref = 1)) %>%
  mutate(race_factor = factor(race)) %>%
  within(race_factor <- relevel(race_factor, ref = 3)) %>%
  mutate(gender_factor = factor(sex, labels= c("Female","Male"))) %>%
  within(gender_factor <- relevel(gender_factor, ref = 2)) %>%
  mutate(score_factor = factor(score_text != "Low", labels = c("LowScore","HighScore")))
```

For the `age_factor` they make “25 - 45” the reference level, for `race_factor` “Caucasian” is the reference level, for `gender_factor` “Male” is the reference level.

Next they fit a logistic regression model to predict `score_factor` from the other variables.

```
# code from https://github.com/propublica/compas-analysis
pp_model <- glm(
  score_factor ~ gender_factor + age_factor + race_factor + priors_count + crime_factor + two_year_recid,
  family="binomial",
  data=df
)
summary(pp_model)

##
## Call:
## glm(formula = score_factor ~ gender_factor + age_factor + race_factor +
##     priors_count + crime_factor + two_year_recid, family = "binomial",
##     data = df)
##
## Deviance Residuals:
```

```
##      Min      1Q  Median      3Q      Max
## -2.997 -0.792 -0.330   0.812   2.602
##
## Coefficients:
##              Estimate Std. Error z value Pr(>|z|)
## (Intercept)      -1.5255    0.0785  -19.43 < 2e-16 ***
## gender_factorFemale      0.2213    0.0795   2.78 0.00539 **
## age_factorGreater than 45  -1.3556    0.0991  -13.68 < 2e-16 ***
## age_factorLess than 25     1.3084    0.0759   17.23 < 2e-16 ***
## race_factorAfrican-American  0.4772    0.0693   6.88 5.9e-12 ***
## race_factorAsian      -0.2544    0.4782  -0.53 0.59472
## race_factorHispanic     -0.4284    0.1281  -3.34 0.00083 ***
## race_factorNative American  1.3942    0.7661   1.82 0.06878 .
## race_factorOther      -0.8263    0.1621  -5.10 3.4e-07 ***
## priors_count           0.2689    0.0111   24.22 < 2e-16 ***
## crime_factorM          -0.3112    0.0665  -4.68 2.9e-06 ***
## two_year_recid         0.6859    0.0640   10.71 < 2e-16 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## (Dispersion parameter for binomial family taken to be 1)
##
##      Null deviance: 8483.3  on 6171  degrees of freedom
## Residual deviance: 6168.4  on 6160  degrees of freedom
## AIC: 6192
##
## Number of Fisher Scoring iterations: 5
```

## Calculating Relative Risk by Demographic

Next they compute how much more likely different demographic groups are to receive a higher score than others. The logistic regression model allows us to measure this difference after correcting for the other variables included in the model. The quantity ProPublica uses to compare black defendants to white defendants (or men to women, old defendants to young defendants, etc.) is called **relative risk**. ProPublica does not explain where this quantity comes from in their analysis, so we'll provide some quick background on logistic regression to justify the calculation. The following explanation is inspired by USC professor Sandy Eckel's slides here.

Logistic regression models a linear relationship between the log odds ratio for the probability of interest and the given predictor variables. An odds ratio measures the odds of success

$$\text{odds ratio} = \frac{\text{probability of success}}{\text{probability of failure}} = \frac{P}{1-P}$$

where  $P$  is the probability of success. The log odds ratio is simply the log of this quantity. Thus the logistic regression model for observation  $x_i$  is

$$\log\left(\frac{P_{x_i}}{1-P_{x_i}}\right) = \beta_0 + \beta_1 x_{i1} + \dots + \beta_p x_{ip}$$

where the probability of success for  $x_i$  is  $P_{x_i}$ , and we have  $p$  predictors with corresponding coefficients  $\beta_j$  and observed values  $x_{ij}$  for  $j = 1, \dots, p$ . Given that our model here uses categorical predictors (factors), the coefficients we estimate give us the **change in log odds** for the corresponding variable. Thus if we let  $P_{x_i}$

be the probability that individual  $x_i$  gets a high COMPAS score, then with coefficient  $\beta_1$  for `gender_factor`, we would have

$\beta_0$  : the log odds of getting a high COMPAS score for men

$\beta_1$  : the difference in log odds of getting a high COMPAS score for women compared to men

The important observation here is that because men are the reference level for the `gender_factor` categorical variable,  $\beta_1$  measures a **difference** relative to men. Thus if we want to answer the question, “How much more likely are women to get a high COMPAS score than men?” we’ll want to use

$\beta_0 + \beta_1$  : the log odds of getting a high COMPAS score for women

to get the comparison. One other observation will also be helpful to calculate relative risk. We solve for  $P_{x_i}$  as follows.

$$\log\left(\frac{P}{1-P}\right) = x \rightarrow P = \frac{e^x}{1+e^x} = \text{sigmoid}(x)$$

Thus we calculate relative risk for the categorical variable corresponding to  $\beta_1$  as:

$$\text{relative risk} = \frac{P_1}{P_2} = \frac{\text{sigmoid}(\beta_0 + \beta_1)}{\text{sigmoid}(\beta_0)}$$

ProPublica computes relative risk to compare blacks to whites, men to women, and people under 25 to middle-aged people in terms of COMPAS scores. They get the following results.

```
# code adapted from https://github.com/propublica/compas-analysis
model_intercept <- coef(pp_model)['(Intercept)']
black_coef <- coef(pp_model)['race_factorAfrican-American']
(relative_risk_black_v_white <- sigmoid(model_intercept + black_coef) / sigmoid(model_intercept))
```

```
## (Intercept)
##          1.453
```

As ProPublica states, this shows us that “Black defendants are 45% more likely than white defendants to receive a higher [COMPAS] score correcting for the seriousness of their crime, previous arrests, and future criminal behavior.” Similarly, women are 19.4% more likely than men and people under 25 are 2.5 times as likely as middle aged people to get a higher score:

```
# code adapted from https://github.com/propublica/compas-analysis
woman_coef <- coef(pp_model)['gender_factorFemale']
(relative_risk_woman_v_man <- sigmoid(model_intercept + woman_coef) / sigmoid(model_intercept))
```

```
## (Intercept)
##          1.195
```

```
# code adapted from https://github.com/propublica/compas-analysis
age_coef <- coef(pp_model)['age_factorLess than 25']
(relative_risk_young_v_midleage <- sigmoid(model_intercept + age_coef) / sigmoid(model_intercept))
```

```
## (Intercept)
##          2.496
```



## Our Logistic Regression Model

```
regmod <- glm(is_recid ~., family = binomial(link='logit'), data = vars)
summary(regmod)
```

```
##
## Call:
## glm(formula = is_recid ~ ., family = binomial(link = "logit"),
##      data = vars)
##
## Deviance Residuals:
##      Min       1Q   Median       3Q      Max
## -3.129  -1.034  -0.553   1.082   2.530
##
## Coefficients:
##              Estimate Std. Error z value Pr(>|z|)
## (Intercept)    0.77823    0.10057   7.74 1.0e-14 ***
## sexMale         0.32969    0.06541   5.04 4.6e-07 ***
## raceAsian      -0.30232    0.39242  -0.77  0.4411
## raceCaucasian  -0.08537    0.05813  -1.47  0.1420
## raceHispanic   -0.30169    0.09438  -3.20  0.0014 **
## raceNative American 0.11833    0.53100   0.22  0.8237
## raceOther      -0.27493    0.11788  -2.33  0.0197 *
## age            -0.04445    0.00251 -17.72 < 2e-16 ***
## juv_fel_count   0.19759    0.09079   2.18  0.0295 *
## juv_misd_count  0.04865    0.07767   0.63  0.5311
## juv_other_count 0.19531    0.06538   2.99  0.0028 **
## priors_count    0.15166    0.00740  20.50 < 2e-16 ***
## c_charge_degreeM -0.14113    0.05420  -2.60  0.0092 **
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## (Dispersion parameter for binomial family taken to be 1)
##
##      Null deviance: 9990.5  on 7213  degrees of freedom
## Residual deviance: 8830.2  on 7201  degrees of freedom
## AIC: 8856
##
## Number of Fisher Scoring iterations: 4
```

```
fitted_values <- fitted(regmod)
vars <- cbind(vars, fitted_values)
```

## Using ProPublica's Bias-Assessment Model on Our Model

We can see if our model suffers from the same bias using ProPublica's bias-assessment methodology. We'll set up the same model they did, but this time instead of predicting `score_factor` for the COMPAS score, we'll create a `score_factor` variable *from our model's predictions*.

**Variable Selection**

**Clustering**