# Assessing and Mitigating Algorithmic Bias in Criminal Risk Scores

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# Introduction

# **Problem Statement**

# **Data Description**

ProPublica collected data on  $\mathbf{TODO}$ 

In the data set we look at, they considered only people who either "recidivated within two years of their crime or recidivated in tow years, or had at least tow years outside of a correctional facility."

# **Data Dictionary**

ProPublica did not provide a data dictionary explaining their variables. Through some manual exploration, we came up with the following descriptions for our best guess at what each variable measures.

Variable	Description
id	unque identifier for each individual
name	first and last name
first	first name
last	last name
compas_screening_datlate on which decile_score was given	
sex	sex (male or female)
dob	date of birth
age	age in years
$age\_cat$	age category (less than 25, 25-45, greater than 45)
race	race (African-American, Asian, Caucasian, Hispanic, Native American, Other)
$juv\_fel\_count$	juvenile felony count
$decile\_score$	COMPAS Risk of Recidivism score from 1 to 10
$juv\_misd\_count$	juvenile misdemeanor count
juv_other_count	juvenile other offenses count
priors_count	prior offenses count
days_b_screening_armentmber of days between COMPAS screening and arrest TODO negative values?	
$c\_jail\_in$	jail entry date for original crime
$c\_jail\_out$	jail exit date for original crime
$c\_case\_number$	case number for original crime
$c\_offense\_date$	offense date of original crime
$c\_arrest\_date$	arrest date for original crime
c_days_from_compasdays between COMPAS screening and original crime offense date	
$c\_charge\_degree$	charge degree of original crime
$c\_charge\_desc$	description of charge for original crime

Variable	Description
is_recid	binary indicator of recidivation (1=individual recidivated, 0=individual did not recidivate)
r case number	case number of follow-up crime
r_charge_degree	charge degree of follow-up crime
r_days_from_arrest	number of days between follow-up crime and arrest date <b>TODO</b> why negative value here?
r offense date	date of follow-up crime
r_charge_desc	description of charge for follow-up crime
r_jail_in	jail entry date for follow-up crime
r_jail_out	jail exit date for follow-up crime
violent_recid	values are all NA. This column is ignored.
is_voilent_recid	binary indicator of violent follow-up crime (1=follow-up crime was violent,
	0=follow-up crime was non-violent)
vr case number	case number for violent follow-up crime
vr_charge_degree	charge degree for violent follow-up crime
$vr\_offense\_date$	date of offense for violent follow-up crime
$vr\_charge\_desc$	description of charge for violent follow-up crime
type_of_assessment	the type of COMPAS score given for decile_score (here all values are Risk of
	Recidivism)
$decile\_score.1$	repeat column of decile_score
$score\_text$	ProPublica-defined category of decile_score (High=8-10, Medium=5-7, Low=1-4)
$screening\_date$	repeat column of compas_screening_date
v_type_of_assessme	nthe type of COMPAS score given for v_decile_score (here all values are
	Risk_of_Violence)
$v\_decile\_score$	COMPAS Risk of Violence score from 1 to 10
$v\_score\_text$	ProPublica-defined category of v_decile_score (High=8-10, Medium=5-7,
	Low=1-4)
$v\_screening\_date$	date on which v_decile_score was given
$in\_custody$	date on which individual was brought into custody
$\operatorname{out}$ _custody	date on which individual was released from custody
$priors\_count.1$	repeat column of priors_count
start	TODO
end	TODO
event	TODO

ProPublica obtained this data with the goal of analyzing Northpointe Inc.'s commercial recidivism modeling tool – COMPAS. Aggregating data from public records, they collected data on 18,610 individuals who received COMPAS scores from 2013 to 2014, including demographic information, public criminal records, and incarceration records.

How are COMPAS scores used?

ProPublica describes that at least in Broward County, they "primarily [use] the score to determine whether to release or detain a defendant before his or her trial." 11,757 of the individuals in the database had their COMPAS scores used to assess whether or not they should be released before their trial.

What are COMPAS scores?

There are three types of COMPAS score. Each measures a type of 'risk' associated with a criminal re-offending in some way on a scale of 1 (low) to 10 (high). As ProPublica describes, these include

• Risk of Recidivism: ProPublica defines this as the person in question committing a "criminal offense that [results] in a jail booking and [takes] place after the crime for which the person was COMPAS

scored." Northpointe hopes to use this score to predict "a new misdemeanor or felony offense within two years of the COMPAS administration date."

- Risk of Violence: They use the FBI definition of violent crime:
  - In the FBI's Uniform Crime Reporting (UCR) Program, violent crime is composed of four offenses: murder and nonnegligent manslaughter, forcible rape, robbery, and aggravated assault. Violent crimes are defined in the UCR Program as those offenses which involve force or threat of force. ucr.fbi.gov
- Risk of Failure to Appear: As evidenced by the name, this describes a failure to appear at the court
  hearing.

# **Exploratory Data Analysis**

We first load in the data provided by ProPublica, and take a quick look at summaries of each variable to get a sense of distribution and potential outliers. We'll look at half of the columns at a time to keep things manageable.

```
compas_data <- read.csv('compas-scores-two-years.csv')
summary(compas_data[1:(ncol(compas_data)/2)])</pre>
```

```
##
           id
                                      name
                                                         first
##
    Min.
                     anthony smith
                                                michael
                                                            : 149
                                            3
    1st Qu.: 2735
                     angel santiago
                                            2
                                                christopher: 109
##
    Median: 5510
                     anthony gonzalez :
                                            2
                                                james
                                                               84
                                            2
##
    Mean
           : 5501
                     anthony louis
                                                anthony
                                                               83
    3rd Qu.: 8246
                                            2
                                                               76
##
                     brandon whitfield:
                                                robert
##
    Max.
            :11001
                     carlos vasquez
                                            2
                                                john
                                                               74
##
                                        :7201
                                                            :6639
                     (Other)
                                                 (Other)
##
          last
                     compas_screening_date
                                                 sex
                                                                     dob
##
    williams:
               83
                     2013-02-20:
                                   32
                                             Female: 1395
                                                            1987-02-04:
                                                                           5
##
    johnson :
               76
                     2013-03-20:
                                   32
                                             Male :5819
                                                            1987-12-21:
                                                                           5
##
    brown
                68
                     2013-02-07:
                                   31
                                                            1989-04-27:
                                                                           5
                     2013-04-20:
                                                            1989-08-31:
##
    smith
                65
                                   30
                                                                           5
##
                57
                     2013-01-03:
                                   29
                                                            1990-02-22:
    jones
                     2013-04-25:
                                                                           5
##
    davis
                46
                                   28
                                                            1990-05-02:
##
    (Other) :6819
                     (Other)
                                :7032
                                                            (Other)
                                                                       :7184
##
                                age_cat
                                                            race
         age
##
           :18.0
                    25 - 45
                                             African-American:3696
    Min.
                                     :4109
##
    1st Qu.:25.0
                    Greater than 45:1576
                                             Asian
    Median:31.0
##
                    Less than 25
                                    :1529
                                             Caucasian
                                                              :2454
##
    Mean
            :34.8
                                             Hispanic
                                                               : 637
##
    3rd Qu.:42.0
                                             Native American:
                                                                18
            :96.0
                                                               : 377
##
    Max.
                                             Other
##
##
                       decile_score
                                        juv_misd_count
    juv_fel_count
                                                          juv other count
##
    Min.
           : 0.000
                      Min.
                              : 1.00
                                       Min.
                                               : 0.000
                                                          Min.
                                                                 : 0.000
##
    1st Qu.: 0.000
                      1st Qu.: 2.00
                                        1st Qu.: 0.000
                                                          1st Qu.: 0.000
##
    Median : 0.000
                      Median: 4.00
                                       Median : 0.000
                                                          Median : 0.000
##
    Mean
           : 0.067
                      Mean
                              : 4.51
                                        Mean
                                               : 0.091
                                                          Mean
                                                                  : 0.109
    3rd Qu.: 0.000
                                        3rd Qu.: 0.000
                                                          3rd Qu.: 0.000
##
                      3rd Qu.: 7.00
##
    Max.
            :20.000
                      Max.
                              :10.00
                                        Max.
                                               :13.000
                                                          Max.
                                                                  :17.000
##
##
     priors_count
                     days_b_screening_arrest
                                                              c_jail_in
##
           : 0.00
                             :-414.0
                                                                    : 307
    Min.
                     Min.
```

```
1st Qu.: 0.00
                     1st Qu.:
                                -1.0
                                                2013-01-01 01:31:55:
##
    Median: 2.00
                     Median:
                                -1.0
                                                2013-01-01 03:16:15:
                                                                         1
            : 3.47
##
    Mean
                     Mean
                                  3.3
                                                2013-01-01 03:28:03:
                                                                         1
##
    3rd Qu.: 5.00
                     3rd Qu.:
                                  0.0
                                                2013-01-01 04:17:22:
                                                                         1
##
    Max.
            :38.00
                     Max.
                             :1057.0
                                                2013-01-01 04:29:04:
                                                                         1
##
                     NA's
                             :307
                                                (Other)
                                                                     :6902
##
                                        c_case_number
                   c jail out
                                                            c offense date
                         : 307
##
                                                   22
                                                                    :1159
##
    2013-09-12 10:31:00:
                             3
                                  00004068CF10A:
                                                    1
                                                        2013-01-14:
                                                                       26
##
    2013-09-14 05:58:00:
                             3
                                  00022077MM10A:
                                                    1
                                                        2013-02-22:
    2013-09-28 02:10:00:
                             3
                                  01004839CF10A:
                                                    1
                                                        2013-03-01:
                                                                       24
##
    2013-02-06 10:01:51:
                             2
                                  01006487CF10D:
                                                        2013-01-11:
                                                                       23
                                                    1
                             2
##
    2013-06-13 10:32:00:
                                  01007205MM10A:
                                                    1
                                                        2013-02-16:
                                                                       23
##
                         :6894
                                                                    :5933
    (Other)
                                  (Other)
                                                :7187
                                                         (Other)
##
       c_arrest_date
                       c_days_from_compas c_charge_degree
##
               :6077
                        Min.
                                    0
                                            F:4666
##
                                            M:2548
    2013-02-06:
                   9
                        1st Qu.:
                                    1
##
    2013-03-22:
                   8
                        Median :
                                    1
    2013-05-15:
                                   58
##
                   8
                       Mean
##
    2013-01-10:
                   7
                        3rd Qu.:
##
    2013-01-11:
                   7
                        Max.
                                :9485
##
    (Other)
               :1098
                        NA's
                                :22
##
                            c_charge_desc
                                                is_recid
                                                                     r case number
##
    Battery
                                    :1156
                                            Min.
                                                    :0.000
                                                                            :3743
##
    arrest case no charge
                                    :1137
                                            1st Qu.:0.000
                                                              13000349MM10A:
    Possession of Cocaine
                                    : 474
                                            Median : 0.000
                                                              13000445MM20A:
                                                                                 1
##
    Grand Theft in the 3rd Degree: 425
                                            Mean
                                                    :0.481
                                                              13000677MM20A:
                                                                                 1
    Driving While License Revoked: 200
                                            3rd Qu.:1.000
                                                              13000758MM30A:
                                                                                 1
##
    Driving Under The Influence
                                   : 135
                                                    :1.000
                                                              13000785MM30A:
                                                                                 1
                                            Max.
                                    :3687
##
    (Other)
                                                              (Other)
                                                                            :3466
```

Here we notice there may be large outliers in many of the crime count variables, such as <code>juv\_fel\_count</code>, <code>juv\_misd\_count</code>, <code>juv\_other\_count</code>, and <code>priors\_count</code>. We expect these are simply accurate observations corresponding to individuals with high numbers of prior offenses. Thus we will not remove these individuals from the data but will be aware of them as potential influential points when we later fit any models. We also note that the values for the 'days\_from' variables are quite variable which may be relevant if we use those variables in later analysis. Looking at the second half of the columns, we have:

#### summary(compas\_data[(ncol(compas\_data)/2 + 1):ncol(compas\_data)])

```
##
    r_charge_degree r_days_from_arrest
                                              r_offense_date
##
            :3743
                     Min.
                             : -1
                                                      :3743
##
    (M1)
            :1201
                      1st Qu.:
                                Λ
                                          2014-12-08:
                                                        12
    (M2)
            :1107
                     Median :
                                          2015-01-28:
##
    (F3)
            : 892
                                          2014-09-15:
##
                     Mean
                             :
                               20
                                                         10
                                          2014-10-17:
##
    (F2)
            : 168
                     3rd Qu.:
                                1
                                                         10
##
    (F1)
               51
                     Max.
                             :993
                                          2015-02-10:
                                                         10
##
    (Other):
              52
                     NA's
                             :4898
                                           (Other)
                                                      :3418
##
                                r_charge_desc
                                                      r_jail_in
                                         :3801
##
                                                            :4898
    Driving License Suspended
                                         : 258
                                                                9
##
                                                 2014-05-27:
    Possess Cannabis/20 Grams Or Less: 253
                                                 2013-11-22:
                                                                8
##
    Resist/Obstruct W/O Violence
                                        : 201
                                                 2014-06-05:
                                                                8
##
                                        : 192
                                                 2014-07-10:
                                                                8
    Battery
    Operating W/O Valid License
                                        : 172
                                                 2014-10-17:
```

```
##
    (Other)
                                        :2337
                                                 (Other)
                                                           :2275
##
                       violent recid
                                                                 vr_case_number
                                        is violent recid
         r_jail_out
                                                                         :6395
##
               :4898
                       Mode:logical
                                        Min.
                                               :0.000
                       NA's:7214
##
    2014-02-18:
                   9
                                        1st Qu.:0.000
                                                          13001383CF10A:
                                                                             1
##
    2014-12-09:
                   9
                                        Median :0.000
                                                          13001876CF10A:
    2015-05-15:
                   9
                                        Mean
                                               :0.114
                                                          13002119CF10A:
##
                                        3rd Qu.:0.000
                                                          13002546CF10A:
##
    2013-11-13:
                   8
    2014-07-11:
##
                   8
                                        Max.
                                               :1.000
                                                          13003421CF10A:
                                                                             1
##
    (Other)
               :2273
                                                          (Other)
                                                                         : 814
##
    vr_charge_degree
                         vr_offense_date
                                                                   vr_charge_desc
                                 :6395
##
            :6395
                                                                           :6395
            : 344
                                                                           : 329
##
                      2015-08-15:
                                          Battery
    (M1)
                                      6
           : 228
                                          Battery on Law Enforc Officer:
##
    (F3)
                      2013-11-14:
                                      4
                                                                              38
            : 162
                      2014-02-18:
                                          Felony Battery (Dom Strang)
                                                                              38
##
    (F2)
##
    (F1)
               38
                      2014-10-29:
                                          Aggravated Assault W/Dead Weap:
                                                                              37
                                      4
##
    (M2)
           :
               19
                      2014-12-26:
                                      4
                                          Aggrav Battery w/Deadly Weapon:
                                                                              34
##
    (Other):
                                          (Other)
                                                                           : 343
              28
                       (Other)
                                 : 797
##
              type of assessment decile score.1
                                                     score text
##
    Risk of Recidivism:7214
                                  Min.
                                          : 1.00
                                                    High :1403
##
                                  1st Qu.: 2.00
                                                    Low
                                                          :3897
##
                                  Median: 4.00
                                                    Medium:1914
##
                                  Mean
                                          : 4.51
##
                                  3rd Qu.: 7.00
                                  Max.
                                          :10.00
##
##
##
       screening date
                              v_type_of_assessment v_decile_score
##
    2013-02-20:
                  32
                       Risk of Violence:7214
                                                     Min.
                                                            : 1.00
    2013-03-20:
                                                     1st Qu.: 1.00
##
                  32
                                                     Median: 3.00
##
    2013-02-07:
                  31
##
    2013-04-20:
                  30
                                                     Mean
                                                            : 3.69
                                                     3rd Qu.: 5.00
##
    2013-01-03:
                  29
##
    2013-04-25:
                  28
                                                     Max.
                                                            :10.00
##
    (Other)
               :7032
##
    v_score_text
                                             in_custody
                                                                out_custody
                     v_screening_date
##
    High: 714
                   2013-02-20:
                                 32
                                                   : 236
                                                                      : 236
##
    Low
                   2013-03-20:
                                                           2020-01-01:
                                                                         61
          :4761
                                 32
                                        2013-02-22:
                                                      20
##
    Medium: 1739
                   2013-02-07:
                                 31
                                        2013-12-12:
                                                      20
                                                           2013-05-14:
                                                                          25
##
                   2013-04-20:
                                 30
                                        2014-01-04:
                                                      20
                                                           2014-02-04:
                                                                          24
##
                   2013-01-03:
                                 29
                                        2014-01-22:
                                                      20
                                                           2013-11-26:
                                                                          23
##
                   2013-04-25:
                                        2013-01-27:
                                                           2013-02-15:
                                                                         21
                                 28
                                                      19
                   (Other)
                                        (Other)
##
                              :7032
                                                   :6879
                                                           (Other)
                                                                      :6824
##
                                                           event
    priors_count.1
                          start
                                            end
##
    Min.
           : 0.00
                     Min.
                             : 0.0
                                      Min.
                                              :
                                                  0
                                                       Min.
                                                               :0.000
    1st Qu.: 0.00
                                                       1st Qu.:0.000
##
                     1st Qu.: 0.0
                                       1st Qu.: 148
    Median: 2.00
                                                       Median :0.000
##
                     Median :
                                0.0
                                       Median: 530
##
    Mean
           : 3.47
                             : 11.5
                                       Mean
                                              : 553
                                                       Mean
                                                               :0.383
                     Mean
##
    3rd Qu.: 5.00
                     3rd Qu.:
                               1.0
                                       3rd Qu.: 914
                                                       3rd Qu.:1.000
##
            :38.00
                             :937.0
                                              :1186
                                                               :1.000
    Max.
                     Max.
                                       Max.
                                                       Max.
##
```

With the second half we have similar characteristics as before. We remove the violent\_recid column given that all values are NA (as mentioned in the data dictionary). Apart from that column, we make no other changes.

#### ProPublica's Bias-Assessment Model

This section is meant to recreate ProPublica's logistic regression model for assessing bias in COMPAS scores. The code and explanations in this section are adapted from their published methodlogy and code.

Using the same data set, they first filter rows based on the following criteria.

- 1. consider only individuals with a COMPAS score
- 2. assure the COMPAS score corresponds to the correct crime i.e. the score was given within 30 days of the arrest
- 3. do not include ordinary traffic offenses

Next we use their code to perform this filtering:

```
# code from https://github.com/propublica/compas-analysis

df <- compas_data %>%
    select(age, c_charge_degree, race, age_cat, score_text, sex, priors_count, days_b_screening_arrest, d
    filter(days_b_screening_arrest <= 30) %>%
    filter(days_b_screening_arrest >= -30) %>%
    filter(is_recid != -1) %>%
    filter(c_charge_degree != "0") %>%
    filter(score_text != 'N/A')
    nrow(df)
```

#### ## [1] 6172

##

## Deviance Residuals:

In order to use this data to assess racial bias in scoring, the ProPublica analysts first create several factor variables from the existing columns.

For the age\_factor they make "25 - 45" the reference level, for race\_factor "Caucasian" is the reference level, for gender\_factor "Male" is the reference level.

Next they fit a logistic regression model to predict score\_factor from the other variables.

```
# code from https://github.com/propublica/compas-analysis
pp_model <- glm(
    score_factor ~ gender_factor + age_factor + race_factor + priors_count + crime_factor + two_year_recir
    family="binomial",
    data=df
)
summary(pp_model)

##
## Call:
## glm(formula = score_factor ~ gender_factor + age_factor + race_factor +
## priors_count + crime_factor + two_year_recid, family = "binomial",
## data = df)</pre>
```

```
##
      Min
               1Q
                   Median
                                3Q
                                       Max
  -2.997
           -0.792
                   -0.330
##
                             0.812
                                     2.602
##
## Coefficients:
##
                                Estimate Std. Error z value Pr(>|z|)
                                                      -19.43
                                                              < 2e-16 ***
##
  (Intercept)
                                 -1.5255
                                              0.0785
## gender factorFemale
                                  0.2213
                                              0.0795
                                                        2.78
                                                              0.00539 **
                                                              < 2e-16 ***
## age factorGreater than 45
                                 -1.3556
                                              0.0991
                                                      -13.68
## age_factorLess than 25
                                  1.3084
                                              0.0759
                                                       17.23
                                                              < 2e-16 ***
## race_factorAfrican-American
                                  0.4772
                                              0.0693
                                                        6.88
                                                              5.9e-12 ***
## race_factorAsian
                                 -0.2544
                                              0.4782
                                                       -0.53
                                                              0.59472
                                                       -3.34
                                                              0.00083 ***
## race_factorHispanic
                                 -0.4284
                                              0.1281
## race_factorNative American
                                  1.3942
                                              0.7661
                                                        1.82
                                                              0.06878
## race_factorOther
                                 -0.8263
                                              0.1621
                                                       -5.10
                                                              3.4e-07 ***
## priors_count
                                                       24.22
                                                              < 2e-16 ***
                                  0.2689
                                              0.0111
                                                              2.9e-06 ***
## crime_factorM
                                 -0.3112
                                              0.0665
                                                       -4.68
                                              0.0640
                                                       10.71 < 2e-16 ***
## two_year_recid
                                  0.6859
##
                   0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## Signif. codes:
##
   (Dispersion parameter for binomial family taken to be 1)
##
##
       Null deviance: 8483.3
                               on 6171
                                        degrees of freedom
## Residual deviance: 6168.4
                              on 6160
                                        degrees of freedom
## AIC: 6192
## Number of Fisher Scoring iterations: 5
```

#### Calculating Relative Risk by Demographic

Next they compute how much more likely different demographic groups are to receive a higher score than others. The logistic regression model allows us to measure this difference after correcting for the other variables included in the model. The quantity ProPublica uses to compare black defendants to white defendants (or men to women, old defendants to young defendants, etc.) is called **relative risk**. ProPublica does not explain where this quantity comes from in their analysis, so we'll provide some quick background on logistic regression to justify the calculation. The following explanation is inspired by USC professor Sandy Eckel's slides here.

Logistic regression models a linear relationship between the log odds ratio for the probability of interest and the given predictor variables. An odds ratio measures the odds of success

$${\tt odds\ ratio} = \frac{{\tt probability\ of\ success}}{{\tt probability\ of\ failure}} = \frac{P}{1-P}$$

where P is the probability of success. The log odds ratio is simply the log of this quantity. Thus the logistic regression model for observation  $x_i$  is

$$\log(\frac{P_{x_i}}{1 - P_{x_i}}) = \beta_0 + \beta_1 x_{i1} + \ldots + \beta_p x_{ip}$$

where the probability of success for  $x_i$  is  $P_{x_i}$ , and we have p predictors with corresponding coeffecients  $\beta_j$  and observed values  $x_{ij}$  for j = 1, ..., p. Given that our model here uses categorical predictors (factors), the coeffecients we estimate give us the **change in log odds** for the corresponding variable. Thus if we let  $P_{x_i}$ 

be the probability that individual  $x_i$  gets a high COMPAS score, then with coefficient  $\beta_1$  for gender\_factor, we would have

 $\beta_0$ : the log odds of getting a high COMPAS score for men

 $\beta_1$ : the difference in log odds of getting a high COMPAS score for women compared to men

The important observation here is that because men are the reference level for the **gender\_factor** categorical variable,  $\beta_1$  measures a **difference** relative to men. Thus if we want to answer the question, "How much more likely are women to get a high COMPAS score than men?" we'll want to use

 $\beta_0 + \beta_1$ : the log odds of getting a high COMPAS score for women

to get the comparison. One other observation will also be helpful to calculate relative risk. We solve for  $P_{x_i}$  as follows.

$$\log(\frac{P}{1-P}) = x \to P = \frac{e^x}{1+e^x} = \operatorname{sigmoid}(x)$$

Thus we calculate relative risk for the categorical variable corresponding to  $\beta_1$  as:

$$\texttt{relative risk} = \frac{P_1}{P_2} = \frac{\texttt{sigmoid}(\beta_0 + \beta_1)}{\texttt{sigmoid}(\beta_0)}$$

ProPublica computes relative risk to compare blacks to whites, men to women, and people under 25 to middle-aged people in terms of COMPAS scores. They get the following results.

```
# code adapted from https://github.com/propublica/compas-analysis
model_intercept <- coef(pp_model)['(Intercept)']
black_coef <- coef(pp_model)['race_factorAfrican-American']
(relative_risk_black_v_white <- sigmoid(model_intercept + black_coef) / sigmoid(model_intercept))
## (Intercept)
## 1.453</pre>
```

As ProPublica states, this shows us that "Black defendants are 45% more likely than white defendants to receive a higher [COMPAS] score correcting for the seriousness of their crime, previous arrests, and future criminal behavior." Similarly, women are 19.4% more likely than men and people under 25 are 2.5 times as likely as middle aged people to get a higher score:

```
likely as middle aged people to get a higher score:
# code adapted from https://github.com/propublica/compas-analysis
woman_coef <- coef(pp_model)['gender_factorFemale']
(relative_risk_woman_v_man <- sigmoid(model_intercept + woman_coef) / sigmoid(model_intercept))
## (Intercept)
## 1.195
# code adapted from https://github.com/propublica/compas-analysis
age_coef <- coef(pp_model)['age_factorLess than 25']
(relative_risk_young_v_middleage <- sigmoid(model_intercept + age_coef) / sigmoid(model_intercept))
## (Intercept)
## 2.496</pre>
```

# Our Logistic Regression Model

#### Variable Selection

TODO: talk about excluding race but including sex

```
vars <- compas_data %>%
  select(sex, age, ends_with('count'), c_charge_degree, is_recid)
# ggplot(vars, aes(x = race, y = decile_score)) + geom_boxplot()
```

#### Training the Model

```
regmod <- glm(is_recid ~., family = binomial(link='logit'), data = vars)
summary(regmod)
##
## Call:
## glm(formula = is_recid ~ ., family = binomial(link = "logit"),
##
       data = vars)
##
## Deviance Residuals:
                                     Max
     Min
             1Q Median
                               3Q
##
   -3.14
           -1.04
                   -0.56
                            1.09
                                     2.46
##
## Coefficients:
##
                    Estimate Std. Error z value Pr(>|z|)
                               0.09947
                                           7.37 1.7e-13 ***
## (Intercept)
                    0.73332
## sexMale
                     0.32061
                               0.06522
                                           4.92 8.8e-07 ***
## age
                    -0.04534
                               0.00246 -18.40 < 2e-16 ***
## juv_fel_count
                    0.20658
                               0.09108
                                           2.27
                                                 0.0233 *
## juv misd count
                     0.05195
                               0.07813
                                           0.66
                                                  0.5062
                                           3.03
                                                 0.0024 **
## juv_other_count
                     0.19885
                               0.06559
## priors_count
                     0.15587
                               0.00730
                                          21.34 < 2e-16 ***
## c_charge_degreeM -0.14752
                               0.05407
                                          -2.73
                                                  0.0064 **
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## (Dispersion parameter for binomial family taken to be 1)
##
##
       Null deviance: 9990.5 on 7213
                                       degrees of freedom
## Residual deviance: 8844.8 on 7206
                                       degrees of freedom
## AIC: 8861
## Number of Fisher Scoring iterations: 4
# fitted_values <- fitted(regmod)</pre>
```

# Using ProPublica's Bias-Assessment Model on Our Model

Big TODO: we should nest this bias calculation inside cross-validation to make sure we're assessing our bias on future data (also interesting to look at the bias on the training data, however)

We can see if our model suffers from the same bias using ProPublica's bias-assessment methodology. We'll set up the same model they did, but this time instead of predicting score\_factor for the COMPAS score, we'll create a score\_factor variable from our model's predictions. To get valid predictions for the training data, we use 10-fold cross-validation.

```
set.seed(123)
all predictions <- data.frame(id = compas data$id, predicted score = NA)
# split the data into 10 folds
all_indices <- 1:nrow(compas_data)</pre>
folds <- createFolds(all_indices, k = 10)</pre>
for (i in 1:10) {
  # make train/test split
  test_indices <- folds[[i]]</pre>
  training_indices <- all_indices[-test_indices]</pre>
  test_data <- compas_data[test_indices,]</pre>
  training_data <- compas_data[training_indices,]</pre>
  # build model on training data
  vars <- training_data %>%
    select(sex, age, ends_with('count'), c_charge_degree, is_recid)
  regmod <- glm(is_recid ~., family = binomial(link='logit'), data = vars)</pre>
  # store predictions on test data
  predicted_scores <- predict(regmod, newdata = test_data, type = 'response')</pre>
  all predictions [names (predicted scores),] $predicted score <- predicted scores
}
```

Next we create a new data frame with new\_score as our risk of recidivism score. We also create a new\_score\_text variable that defines score categories in the same way, but this time based on a 0-1 scale instead of a 0-10 scale. Recall ProPublica defined this category as: High=8-10, Medium=5-7, Low=1-4. Thus we'll do: High=0.75-1.0, Medium=0.45-0.75, Low=0-0.45.

Now we train the same bias-assessment model, this time using new\_score instead of decile\_score and new\_score\_text instead of score\_text.

```
new_df <- our_scores %>%
select(age, c_charge_degree, race, age_cat, new_score_text, sex, priors_count, days_b_screening_arrest
filter(days_b_screening_arrest <= 30) %>%
```

```
filter(days_b_screening_arrest >= -30) %>%
  filter(is_recid != -1) %>%
  filter(c_charge_degree != "0") %>%
  filter(new_score_text != 'N/A') %>%
  mutate(crime_factor = factor(c_charge_degree)) %>%
  mutate(age_factor = as.factor(age_cat)) %>%
  within(age_factor <- relevel(age_factor, ref = "25 - 45")) %>%
  mutate(race_factor = factor(race)) %>%
  within(race_factor <- relevel(race_factor, ref = "Caucasian")) %>%
  mutate(gender_factor = factor(sex, labels= c("Female","Male"))) %>%
  within(gender_factor <- relevel(gender_factor, ref = "Male")) %>%
  mutate(score_factor = factor(new_score_text != "Low", labels = c("LowScore", "HighScore")))
new_pp_model <- glm(</pre>
  score_factor ~ gender_factor + age_factor + race_factor + priors_count + crime_factor + two_year_reci
  family="binomial",
  data=new df
```

# Bias against black vs. white people

```
model_intercept <- coef(new_pp_model)['(Intercept)']
black_coef <- coef(new_pp_model)['race_factorAfrican-American']
(relative_risk_black_v_white <- sigmoid(model_intercept + black_coef) / sigmoid(model_intercept))
## (Intercept)
## 1.209</pre>
```

# Bias against women vs. men

```
woman_coef <- coef(new_pp_model)['gender_factorFemale']
(relative_risk_woman_v_man <- sigmoid(model_intercept + woman_coef) / sigmoid(model_intercept))
## (Intercept)
## 0.03223</pre>
```

## Bias against under 25 vs. middle-aged

```
age_coef <- coef(new_pp_model)['age_factorLess than 25']
(relative_risk_young_v_middleage <- sigmoid(model_intercept + age_coef) / sigmoid(model_intercept))
## (Intercept)
## 5.75</pre>
```

# Mitigating Bias

Much work has been done exploring techniques that allow for fair modeling and prediction in the presence of biased data or algorithms, and this area of study is rich and actively researched. Researchers Faisal Kamiran and Toon Calders, in their 2011 paper "Data preprocessing techniques for classification without

discrimination," describe several techniques that alter the given dataset to (ideally) eliminate the source of the bias. Several other techniques deal with modifying classification/regression algorithms themselves to make fairer predictions. Here, the general idea is to instead clean the bias out of the data, after which normal classification methods can be used. Before we discuss the techniques we employ for dealing with bias, we first introduce a few key concepts.

#### Algorithmic Bias

This Wikipedia article provides a nice overview of different types of Algorithmic bias and several examples. Bias can manifest in an algorithm in various ways and can have multiple causes. The Wikipedia article linked above uses to term "pre-existing bias" to loosely describe a type of bias resulting from baking social or institutional biases into algorithms. Here the source of bias is not necessarily the algorithm but instead the values encoded into it by its creators or by the data it sees. For our brief foray into algorithmic bias here, we focus on this type of bias under the assumption that some underlying bias does exist in the United States criminal justice system and thus in our data set.

## Protected/Sensitive Attributes

The term *protected attribute* or *sensitive attribute* typically refers to a discriptor of an individual upon which it is illegal to discriminate under the Fair Work Act. These include characteristics such as sexual orientation, gender identity, and race.

#### Combatting Algorithmic Bias

Broadly speaking, research in algorithmic bias works to (1) identify where and in what way bias is present (ProPublica's analysis is one such example), (2) come up with ways to constrain models to enforce fair predictions, or (3) alter the underlying data to minimize bias in the data itself. For our recidivism predictions, we'll employ some techniques from category 3 – altering the underlying data – based on Kamiran and Calders' work.

## Mitigating Bias Through Data Preprocessing

Kamiran and Calders outline four types of techniques for preprocessing to mitigate bias, described at length in their paper:

- 1. **Suppression:** Given a sensitive attribute S, find and remove S and the other features most correlated with S.
- 2. Massaging the dataset: Given a sensitive attribute S, swap the labels of some observations with differing values for S to decrease discrimination while maintaining the same overall class distribution.
- 3. **Reweighing:** Up- or down-weight observations in the training data based on whether they have an under- or over-represented combinations of sensitive attribute S and the response variable.
- 4. Sampling: Calculate sample sizes for combinations of sensitive attribute S and the response that would, as Kamiran and Calders put it, "make the dataset descrimination-free." Then under- or over-sample observations accordingly to create a data set with those proportions.

Here we focus on Sampling.

#### Applying Sampling to the COMPAS Data to Combat Racial Bias

To narrow the scope of this report, we focus on *racial bias* against black people as compared to white people, and we implement sampling to combat this type of bias only. If our example words for racial bias, we could theoretically extend it to each of the protected attributes in the data.

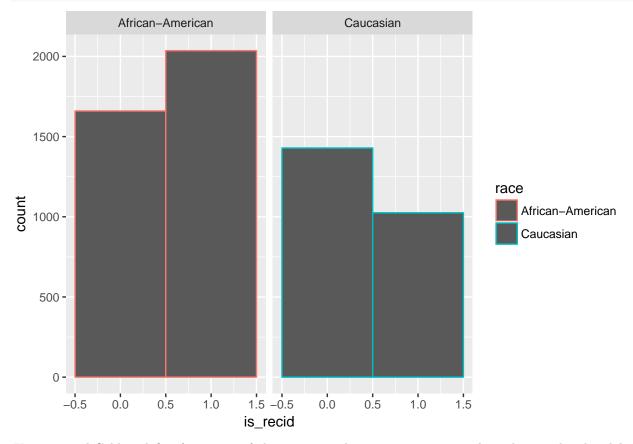
First we need to establish what the class imbalance is between blacks and whites in our data. We look for an imbalance in terms of recidivism rates, since recidivism is what our model predicts.

```
(recid_rates <- compas_data %>%
  select(race, is_recid) %>%
  group_by(race) %>%
  summarize(yes_recid = sum(is_recid == 1), no_recid = sum(is_recid == 0)))
```

```
## # A tibble: 6 x 3
##
                  race yes_recid no_recid
##
                <fctr>
                            <int>
                                      <int>
## 1 African-American
                             2036
                                       1660
## 2
                 Asian
                               11
                                         21
## 3
                             1025
                                       1429
             Caucasian
## 4
              Hispanic
                              245
                                        392
                                          7
## 5
      Native American
                               11
## 6
                 Other
                              143
                                        234
```

Focusing on African-Americans and Caucasians and plotting this table as a bar chart, we have:

```
compas_data %>%
  filter(race %in% c('African-American', 'Caucasian')) %>%
  ggplot(aes(x = is_recid, color = race)) +
   geom_histogram(bins = 2) +
  facet_wrap(~ race)
```



Kamiran and Calders define four types of observation with respect to a protected attribute and a class label. Their definitions are as follows:

• Deprived community with positive class labels (DP)

- Deprived community with negative class labels (DN)
- Favored community with positive class labels (FP)
- Favored community with negative class labels (FN)

In our case these correspond to:

- DP: African-Americans with is recid = 1
- DN: African-Americans with is recid = 0
- FP: Caucasians with is recid = 1
- FN: Caucasians with is recid = 0

```
DP_data <- compas_data %>%
  filter(race == 'African-American' & is_recid == 1)
DN_data <- compas_data %>%
  filter(race == 'African-American' & is_recid == 0)
FP_data <- compas_data %>%
  filter(race == 'Caucasian' & is_recid == 1)
FN_data <- compas_data %>%
  filter(race == 'Caucasian' & is_recid == 0)
```

The process for sampling to get a non-discrimatory sample is as follows.

- 1. Compute the expected size for each group if the data were non-discriminatory
- 2. Under- and over-sample accordingly to eliminate descrimination
- 3. Train the model on the sampled data

In order to get an estimation of how biased our model is after making this adjustment to the data, we nest this process in cross-validation. Thus our overall process will be the following (using k-fold cross-validation).

- 1. Split the data into k folds
- 2. Hold out one fold as test data, use the remaining k-1 folds as training data
- 3. Perform sampling on the training data
  - Compute the expected size for each group if the data were non-discriminatory
  - Under- and over-sample accordingly to eliminate descrimination
- 4. Train our model on the training data
- 5. Predict recidivism scores on the test data and store predictions
- 6. Repeat (2) (5) for each fold, getting one prediction for each data point
- 7. Compute relative risk with new predictions

First we walk through an example of the sampling process on the whole data set before embedding the enitre process in cross-validation.

#### Demonstration of the sampling process

# 1. Compute the expected size for each group if the data were non-discriminatory

Here we have the following counts for each group:

```
recid_rates %>% filter(race %in% c('African-American', 'Caucasian'))

## # A tibble: 2 x 3

## race yes_recid no_recid

## <fctr> <int> <int>
## 1 African-American 2036 1660

## 2 Caucasian 1025 1429
```

Thus we'll say the expected number of observations for each group is the mean of the four counts:

```
(expected_num_observations <- mean(c(nrow(DP_data), nrow(DN_data), nrow(FP_data), nrow(FN_data))))
## [1] 1538</pre>
```

## 2. Under- and over-sample to eliminate descrimination

We want equal representation for each group (DP, DN, FP, and FN). This means getting 1537.5 observations of each. We under- or over-sample accordingly. Kamiran and Calders describe two methods for performing this sampling: *Preferential Sampling*, which is more likely to sample boundary observations (with a high probability of being in either class); and *Uniform Sampling*, which samples all points with equal probability. Here we perform Uniform Sampling with replacement.

```
set.seed(123)
# sample indices

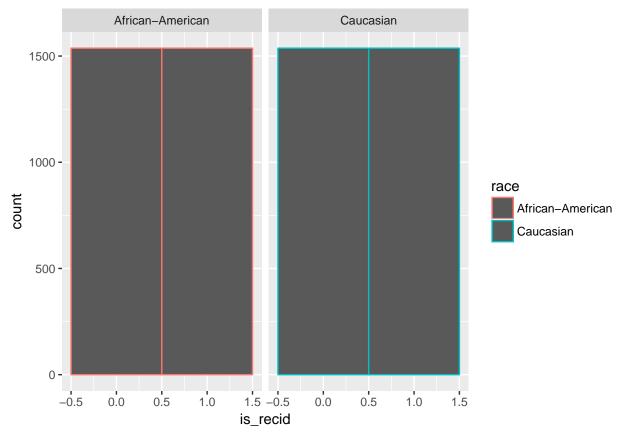
DP_sampled_indices <- sample(1:nrow(DP_data), size = expected_num_observations, replace = TRUE)
DN_sampled_indices <- sample(1:nrow(DN_data), size = expected_num_observations, replace = TRUE)
FP_sampled_indices <- sample(1:nrow(FP_data), size = expected_num_observations, replace = TRUE)
FN_sampled_indices <- sample(1:nrow(FN_data), size = expected_num_observations, replace = TRUE)</pre>
```

And we build a new data set from the sampled observations.

```
# build a new data set
sampled_compas_data <- rbind(
   DP_data[DP_sampled_indices,],
   DN_data[DN_sampled_indices,],
   FP_data[FP_sampled_indices,],
   FN_data[FN_sampled_indices,])</pre>
```

We double check visually that our sampling successfully leveled the classes for each partition.

```
sampled_compas_data %>%
filter(race %in% c('African-American', 'Caucasian')) %>%
ggplot(aes(x = is_recid, color = race)) +
  geom_histogram(bins = 2) +
  facet_wrap(~ race)
```



With Uniform Sampling applied to our data for the *black/white* protected race attributes, we're ready to train our model again and see (1) if its level of bias has decreased and also see (2) how its predictive accuracy has changed.

## 3. Train the model on the sampled data

Here we'll train the model following the same process from above and see how our bias (measured by ProPublica's methodology) compares to the bias before sampling.

We train our logistic regression model.

```
vars <- sampled_compas_data %>%
   select(sex, age, ends_with('count'), c_charge_degree, is_recid)
post_sample_regmod <- glm(is_recid ~., family = binomial(link='logit'), data = vars)</pre>
```

Next we would predict scores **for observations we haven't seen**. Given that we didn't hold out a test set, we don't have any such observations. However, we have now seen how sampling works and are thus ready to do so within cross-validation.

#### Sampling with Cross-validation

Given that we have seen most of the following process step by step in previous sections, we implement this section without explanation of those parts we have seen already.

```
set.seed(123)
all_predictions <- data.frame(id = compas_data$id, predicted_score = NA)
#### 1. Split the data into 10 folds</pre>
```

```
all_indices <- 1:nrow(compas_data)</pre>
folds <- createFolds(all_indices, k = 10)</pre>
#### 2. Hold out one fold as test data, use the remaining k-1 folds as training data
for (i in 1:10) {
 test_indices <- folds[[i]]</pre>
 training_indices <- all_indices[-test_indices]</pre>
 test data <- compas data[test indices,]</pre>
  training_data <- compas_data[training_indices,]</pre>
  #### 3. Perform sampling on the training data
  # create partitions
  DP data <- training data %>%
   filter(race == 'African-American' & is_recid == 1)
  DN_data <- training_data %>%
   filter(race == 'African-American' & is_recid == 0)
  FP_data <- training_data %>%
   filter(race == 'Caucasian' & is_recid == 1)
  FN_data <- training_data %>%
   filter(race == 'Caucasian' & is_recid == 0)
  # get expected number of observations
  expected_num_observations <- mean(c(nrow(DP_data), nrow(DN_data), nrow(FP_data), nrow(FN_data)))</pre>
  # under- and over-sample to eliminate descrimination
  DP_sampled_indices <- sample(1:nrow(DP_data), size = expected_num_observations, replace = TRUE)
  DN_sampled_indices <- sample(1:nrow(DN_data), size = expected_num_observations, replace = TRUE)
  FP_sampled_indices <- sample(1:nrow(FP_data), size = expected_num_observations, replace = TRUE)
  FN_sampled_indices <- sample(1:nrow(FN_data), size = expected_num_observations, replace = TRUE)
  # build new data set
  sampled_training_data <- rbind(</pre>
   DP_data[DP_sampled_indices,],
   DN_data[DN_sampled_indices,],
   FP_data[FP_sampled_indices,],
   FN_data[FN_sampled_indices,]
  #### 4. Train our model on the training data
  vars <- sampled_training_data %>%
    select(sex, age, ends_with('count'), c_charge_degree, is_recid)
  post_sample_regmod <- glm(is_recid ~., family = binomial(link='logit'), data = vars)</pre>
  #### 5. Predict recidivism scores on the test data and store predictions
  predicted_scores <- predict(post_sample_regmod, newdata = test_data, type = 'response')</pre>
 #### 7. Compute relative risk with new predictions
# turn predictions from log odds ratios into probabilities of recidivating
recidivism_scores <- all_predictions$predicted_score</pre>
# create new scores and score categories
post_sample_scores <- compas_data %>%
 mutate(new_score = recidivism_scores) %>%
 mutate(
   new_score_text = as.factor(
     ifelse(new_score >= 0.75, 'High',
```

```
ifelse(new_score >= 0.45, 'Medium', 'Low'))))
# build ProPublica's data frame with our scores
post_sample_df <- post_sample_scores %>%
  select(age, c_charge_degree, race, age_cat, new_score_text, sex, priors_count, days_b_screening_arres
  filter(days_b_screening_arrest <= 30) %>%
  filter(days_b_screening_arrest >= -30) %>%
  filter(is_recid != -1) %>%
  filter(c_charge_degree != "0") %>%
  filter(new_score_text != 'N/A') %>%
  mutate(crime_factor = factor(c_charge_degree)) %>%
  mutate(age_factor = as.factor(age_cat)) %>%
  within(age_factor <- relevel(age_factor, ref = "25 - 45")) %>%
  mutate(race_factor = factor(race)) %>%
  within(race_factor <- relevel(race_factor, ref = "Caucasian")) %>%
  mutate(gender_factor = factor(sex, labels= c("Female", "Male"))) %>%
  within(gender_factor <- relevel(gender_factor, ref = "Male")) %>%
  mutate(score_factor = factor(new_score_text != "Low", labels = c("LowScore", "HighScore")))
# train ProPublica's model
post_sample_pp_model <- glm(</pre>
  score_factor ~ gender_factor + age_factor + race_factor + priors_count + crime_factor + two_year_reci
  family="binomial",
  data=post_sample_df
)
```

Now we can measure the amount of bias in our model after applying sampling and compare to the bias before.

#### Bias Before and After Sampling

We can re-compute the relative risk for blacks vs. whites and compare it to the relative risk for our model before sampling to see if sampling improved the level of bias in our mode.

# References